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Role of heat-flux density and mechanical loading on the microscopic heat-checking of high temperature tool steels under thermal fatigue experiments

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ABSTRACT

Thermal fatigue of a hot work tool steel (X38CrMoV5) is investigated under various test conditions. A microscopic interconnected heat-checking pattern forms on the oxidized surface of the specimen. The evolution of the crack density and morphology is characterized by Scanning Electron Microscopy (SEM) and image analysis. The effects of the initial hardness, the maximum temperature and the heating period of the thermal cycle are reported. It is shown that the saturated heat-checking density is independent of the maximum temperature of the thermal cycle, but is dependent on the heating rate. No significant effect of the initial hardness is observed. In the saturated regime, a linear relationship is established between the heat-checking density and the maximum heat-flux density applied to the specimen. The saturated crack density is explained by the difference between the thermo-mechanical strains of the oxide layer and the steel. A damage criterion, independent of the initial hardness of the steel, is proposed to describe the microscopic heat-checking life.

Keywords: Thermal fatigue Crack network Image analysis Heat-checking life Hot work tool steel

1. Introduction

Thermal fatigue (TF) is a major life-limiting factor of several key industrial components, like hot-forming tool (rolling mill rolls [1,2], moulds for die casting or forging [3–8]), engine cylinder heads and blocks in automotive industry [9], gas-turbine blades in aircraft engines [10] and pressurized water reactors in nuclear industry [11,12]. These components, as with the laboratory samples, experience the variation of temperature with time, during start-up (heating) and shutdown (cooling) operations [2,9] or thermal fluctuations in service [3–8,10]. The repetition of these thermal fluctuations induces transient thermal gradients, which result in thermal strains and subsequent stresses by self-constraining of component or sample. It should be remembered that the surface of the tools is also subjected to additional efforts required to form parts. The cyclic thermo-mechanical solicitations are further coupled with reactive environments (such as oxidation in hot forging and/or corrosion in die-casting), which can lead to a dissolution ("wash-out") of the dies [3,13].

In high temperature forming processes (e.g. High-pressure Die Casting, hot-stamping or forging), the heat exchange between the molten alloy (or hot part) and the die increases the temperature

of the surface. However, the heat-flux density and thus the maximum temperature (T_{max}) may vary from one region to another, depending on tool design and dimensions (e.g. small or large), and/or processing conditions [6,8]. Therefore, the resulting thermo-mechanical stress-strain hysteresis loops differ locally. One can assume that each sector of a tool is a TF specimen experiencing specific test conditions (applied temperatures T_{min} and T_{max} , transient thermal gradient, heating and cooling rates, etc.). According to the amplitude of the thermo-mechanical solicitation, thermoplastic or thermo-visco-plastic yielding can occur and lead cracks to initiate and propagate under non-isothermal fatigue conditions. Near geometrical singularities constituting stress raisers (e.g. corners, holes, etc.), a uniaxial thermo-mechanical fatigue state prevails and the amplitude of the solicitation is in general high enough to initiate and propagate very early the first cracks [4,6]. On planar surfaces, a network of interconnected cracks, commonly named "heat-checking", is initiated and propagated under multiaxial (or at least bi-axial) thermo-mechanical loading [3-6,14]. As the tool is facing cyclic oxidation and/or corrosion reactions, a multi-layered material (oxide or others scales) can be formed. The diffusion of chemical elements (like oxygen, chromium, and iron) changes the composition of the surface and may alter its mechanical properties and strength [7,13]. The cracking of this "multi-layered" material results from mechanical loading induced by the mismatch of thermal expansion between an oxide layer (with elastic behaviour) and the substrate steel (with an elastovisco-plastic behaviour) [3,5,6,8]. During hot forming, the "free" thermal expansion of the die surface is (self-)constrained by the

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Nomenclature

Α	area of the heat-checking cells	W_c
С	Manson–Coffin exponent	ZZ
cr	mean cooling rate of the thermal cycle	α
ct	cooling time of the thermal cycle	ε_p
С	compactness factor of the heat-checking cells	ε_t
dɛ/dt	creep strain-rate	$ ho_{hc}$
hr	mean heating rate of the thermal cycle	ρ_{sat}
ht	heating time of the thermal cycle	θ
L _{sat}	saturation crack spacing	$\theta \theta$
т	strain rate exponent	σ_{max}
N_i	number of cycles to initiate the cracking	ΔT
N_n	number of crack junctions	ΔT_c
Nt	total number of cycles	$\Delta \varepsilon_i$
P(A)	size frequency distribution of the heat-checking cells	$\Delta \varepsilon_m$
P(C)	shape frequency distribution of the heat-checking cells	$\Delta \varepsilon_p$
$P(\theta)$	orientation frequency distributions of micro-cracks	$\Delta \varepsilon_s$
R	determination coefficient	$\Delta \varepsilon_t$
t	time	
Т	temperature	$\Delta \sigma_m$
T_{min}	minimum temperature of the thermal cycle	Φ_{max}
T_{max}	maximum temperature of the thermal cycle	
W	input energy per unit-area	

bulk, which is at a lower temperature. Therefore, the surface undergoes compressive strains and subsequent stresses [4–6,14]. During ejection of parts, the working surface is rapidly cooled, in particular when a cooling system is employed. The "free" contraction of the surface is again constrained by the bulk, that stands now at higher temperatures. Thus, the surface is stretched under tensile thermal stresses. However, as the modulus of elasticity increases when the temperature decreases, if any plastic shielding occurs, its amplitude would be lower than at higher temperature (e.g. T_{max}) and can be neglected in many conditions.

Testing of real components under service conditions is expensive. Laboratory in-house TF experiments are generally developed to assess the behaviour of materials [4,7,15]. Different unconstrained specimens (with various sizes and geometries) and heating and cooling systems are used. Also, tests are conducted on the basis of a "standard in-house" thermal cycle, i.e. a variation of the temperature vs. time compatible with the design requirements and test facility available [3-7,12]. The direct measurement of thermal and mechanical strains in operation conditions is difficult [16]. The thermo-mechanical history seen by the specimen must be calculated by appropriate constitutive laws and an elasto-visco-plastic thermomechanical modelling [4–6,9]. However, a non-linear thermomechanical analysis of industrial tools is often time-consuming, and one can use linear thermo-elastic calculations. We have previously proposed a normalized approach for assessing the heat-transfer and thermo-elastic stresses under transient conditions. It was shown that our laboratory TF test and the data produced can be reliably up-scaled to analyze and/or design tools in HPDC [17].

It is very common and straightforward to use the maximal temperature T_{max} as a damage parameter. In fact, the temperature per see is not a cracking criterion. The temperature (and more specifically T_{max}) can undoubtedly contribute to form oxidation and corrosion products, and also, by coupling with mechanical loading, initiate and propagate cracks. By considering a uniaxial thermo-elastic case for the sake of simplification, the mechanical strain amplitude ($\Delta \varepsilon_m$) and the stress amplitude ($\Delta \sigma_m$) can be calculated as:

$$\Delta \varepsilon_m (= \varepsilon_{max} - \varepsilon_{min}) = \alpha \cdot \Delta T, \text{ and thus } \Delta \sigma_m (= \sigma_{max} - \sigma_{min})$$
$$= \alpha \cdot E \cdot \Delta T,$$

W _c	critical input energy
ZZ	longitudinal axis of the specimen
χ	coefficient of thermal expansion
Sp.	plastic strain
B _t	total strain
o_{hc}	heat-checking density
0 _{sat}	saturated heat-checking density
9	orientation of micro-crack branches
9 <i>0</i>	circumferential axis of the specimen
σ_{max}	calculated maximum stress
ΔT	temperature variation
ΔT_c	critical temperature amplitude
$\Delta \varepsilon_i$	critical strain difference
$\Delta \varepsilon_m$	mechanical strain amplitude
$\Delta \varepsilon_p$	plastic strain amplitude
$\Delta \varepsilon_s$	saturation strain difference
$\Delta \varepsilon_t$	difference of total strain between the oxide layer and
	the steel
$\Delta \sigma_m$	mechanical stress amplitude
Φ_{max}	maximum heat-flux density

where α is the mean thermal expansion, ΔT is the temperature amplitude ($\Delta T = T_{max} - T_{min}$), and *E* is the mean modulus of elasticity. Therefore, these are the "mechanical" strains and stresses that must be considered as criteria for crack initiation and propagation [15].

This paper deals with the influence of the TF test conditions on the microscopic heat-checking pattern formed on the surface of a X38CrMoV5 steel specimen. The effects of the initial hardness of the steel, the maximum temperature and the heating rate of the thermal cycle on the crack density and the network morphology, are reported. We have previously shown that the evolution of the microscopic heat-checking density vs. number of cycles is sigmoidal, and the micro-crack density achieves rapidly an asymptotic saturated value in the "stabilized regime" [18]. The saturated heat-checking density is here related to the maximum heat-flux density and to the TF strains and stresses generated in the base steel. Crack propagation aspects and detailed post-mortem crosssections observations are reported in [6,19].

2. Experimental procedures

2.1. Thermal fatigue experiments

Thermal fatigue (TF) tests were performed on a X38CrMoV5 (AISI H11) tool steel, quenched and double tempered to achieve a martensitic structure with either 42 or 47 HRC hardness. The chemical composition is given in Table 1. The hollow cylindrical shaped specimens, with an inner diameter of 10 mm and an outer diameter of 30 mm, have a wall thickness of 10 mm in the useful area of 40 mm length (Fig. 1). The external surface was mechanically polished to a mean arithmetic roughness (R_a) close to 0.02 µm. The thermal fatigue rig (Fig. 2a) consists of an induction heating system, using a CELES-25 kW high frequency generator

 Table 1

 Chemical composition of X38CrMoV5 (AISI H11) steel.

Element	С	Cr	Мо	V	Si	Mn	S	Р	Fe
Weight (%)	0.396	5.05	1.25	0.47	0.94	0.36	<0.003	0.009	Bal.

(100–400 kHz). An induction frequency of 115 kHz was used, resulting in a very fast heating of a thin surface layer of the specimen due to the induction "skin effect". The external surface is aircooled by natural convection. During the test, the specimen is continuously internally cooled by cold water circulating with a flow rate of 20 l/min (Fig. 2b). The temperature of the specimen is measured by a K-type thermocouple with a wire diameter of 0.1 mm, spot welded to the external surface in the middle of the "gauge area" (central part of 20 mm length, where the thermal gradient is lower than 1 °C/mm) [6,19].

Various thermal cycles are performed, with a minimal temperature (T_{min}) fixed to 100 °C (Table 2). The maximum temperature (T_{max}) of the thermal cycle varied from 550 to 685 °C (Fig. 3a). The heating time (*ht*) is controlled by adjusting the power of the induction generator between 60% to 100% of the full generator load capacity. For the tests with a maximum temperature of 650 °C, ht ranged from 1.2 to 6.5 s (Fig. 3b), leading to very different mean heating rates (85 °C s⁻¹ \leq hr \leq 458 °C s⁻¹), as indicated in Table 2. The maximum heat-flux density applied at the surface of the specimen is related to the test conditions (Table 2), and mainly to the mean heating rate (2.13 MW m⁻² $\leqslant \Phi_{max} \leqslant$ 4.95 MW m⁻²). For each thermal cycle, the cooling time (*ct*) is adjusted to achieve T_{min} on the specimen surface. Therefore, the cooling rate (cr) does not change much from one test to another, varying between 18 $^\circ C \, s^{-1}$ and 33 $^\circ C \, s^{-1}.$ In order to investigate the evolution of the crack pattern on the surface of the specimen, the TF experiments were regularly stopped: every 500 or 1000 cycles until 3000 cycles, then every 2000 or 2500 cycles up to 15,000 cycles, and finally every 10,000 cycles right up to the end of the test [6,19]. In Table 2 are given, for each TF test, the interruption cycle when the micro-cracks are first detected, and the last interruption cycle to the end of the test, when the macro-crack are well propagated.

2.2. Image analysis of the crack pattern

After each cycling interruption, the surface of the specimen was observed with a Scanning Electron Microscope (SEM), using a backscattering electron detector and a magnification sufficiently high to reveal the micro-cracks (×250). A randomly selected area of about 1 mm² (located in the centre of the "gauge area") is then reconstructed by assembly a matrix of (3×3) images, leading to a high resolution cartography (0.5 µm/pixel) representing the crack pattern. Using the commercial image analysis Aphelion[®] software (ADCIS), the micro-cracks are segmented with an algorithm including pre-processing techniques, Boolean operations, and mathematical morphology transformations. The heat-checking density (ρ_{hc} , expressed in mm⁻¹) was then defined as the cumulated crack length per unit area. Individual analysis of both crack branches and heat-checking cells provides a full statistical description of the geometrical and morphological characteristics of the crack pattern [18].



Fig. 1. Specimen geometry (the longitudinal and circumferential axis are respectively noted "zz" and " $\theta\theta$ ").



Fig. 2. Thermal fatigue rig: (a) general view; (b) induction coil and specimen.

Thermal cycles used in the TF tests for 47 HRC treated X38CrMoV5 (only tests 3, 5 and 9 were performed on 42 HRC heat-treated steels).

No. test	Thermal cycle		Heating period		Maximum heat-flux	Cooling period		First and last cycling stops	
	$T_{min} - T_{max}$ (°C)	ΔT (°C)	Duration ht (s)	Mean rate hr (°C s ⁻¹)	density Φ_{max} (MW m ⁻²)	Duration ct (s)	Mean rate cr (°C s ⁻¹)	(number of cycles)	
1	100-550	450	0.90	14.5	4.75	500	31	30,000-80,000 ^a	
2	100-575	475	0.95	14.8	4.84	500	32	5000-50,000	
3	100-600	500	1.0	15.0	4.85	500	33	2500-60,000	
4	100-625	525	1.1	16.0	4.93	477	33	10,000-50,000 ^a	
5	100-650	550	1.2	17.0	4.95	458	32	1000-20,000	
6	100-650	550	2.0	20.0	3.93	275	28	1000-30,000	
7	100-650	550	3.7	22.0	2.78	149	25	2000-30,000	
8	100-650	550	6.5	30.0	2.13	85	18	3000-50,000	
9	100-685	585	1.6	22.0	4.75	366	27	500-3000	

^a Test is not interrupted in the early stages of crack initiation.



Fig. 3. Temperature–time profiles measured in the gauge area of the specimen, for various maximum temperatures T_{max} (a) and heating periods *ht* (b).

3. Results

3.1. Effect of the maximum temperature (T_{max}) of the thermal cycle

Fig. 4a shows the effect of the maximum temperature (T_{max} , investigated in the range between 550 and 685 °C) on the microscopic heat-checking aspect in the "gauge area" of the specimen. It should be specified that the heating period (ht) of these tests increases from 0.9 to 1.6 s by increasing T_{max} from 550 to 685 °C. However, the estimated maximum heat-flux density (Φ_{max}) imposed in the mid section of the specimen during the heating period is nearly constant at 4.85 ± 0.1 MW m⁻² (Table 2). The evolution of the heat-checking density vs. number of cycles presents a sigmoidal trend [18], rapidly reaching a saturated value after the crack pattern initiation (Fig. 4b). This saturated heat-checking density is almost T_{max} -independent ($\rho_{sat} = 144 \text{ mm}^{-1}$ on average, with a variation of ±9% around this mean value), whereas the number of



Fig. 4. Effect of the maximum temperature (T_{max}) on the microscopic heat-checking pattern in the gauge area of the specimen ($T_{min} = 100 \,^{\circ}$ C, $\Phi_{max} \approx 4.85 \,\text{MW m}^{-2}$): (a) increased sight of the cartographies showing the aspect of the saturated heat-checking for various T_{max} ; (b) evolution of the heat-checking density ρ_{hc} vs. number of cycles.

cycles to initiate the micro-cracking seems to decrease with increasing T_{max} . Whatever T_{max} , rather similar size (Fig. 5a) and shape frequency distributions (Fig. 5b) are observed for the heat-checking cells in the saturated regime.

In Figs. 6a–c are plotted the roses of directions (cumulated length of micro-crack branches in a given direction) for three different T_{max} . Two preferential orientations are revealed, at 0° (corresponding to the longitudinal "zz" axis) and 90° (corresponding to the circumferential " $\theta\theta$ " axis). Four symmetry plans, along the 0°, 45°, 90° and 135° directions, can be observed. The heat-checking network seems more isotropic when T_{max} exceeds 600 °C (Fig. 6c). Table 3 indicates that whatever the maximum temperature of the



Fig. 5. Morphological characteristics of the microscopic heat-checking cells for various maximum temperatures T_{max} , in the gauge area of the specimen (saturated regime): (a) size frequency distributions P(A); (b) compactness frequency distributions P(C).

test, a majority of trivalent crack junctions (3 branches per node – class 3) is found (between 60% and 78%, depending on T_{max}), whereas tetravalent (class 4) and pentavalent (class 5) crack junctions are much less represented.

3.2. Effect of the heating period (ht) of the thermal cycle

For the tests performed with a T_{max} of 650 °C, the microscopic heat-checking aspect observed in the "gauge area" of the specimen differs depending on the heating period *ht*, investigated in the range from 1.2 s to 6.5 s (Fig. 7a). As indicated in Table 3, the estimated maximum heat-flux density (Φ_{max}) ranges from 2.1 MW m⁻² for the test with the slowest heating (*ht* = 6.5 s and *hr* = 85 °C s⁻¹) to 4.95 MW m⁻² for the test with the fastest heating (with *ht* = 1.2 s

and $hr = 458 \text{ °C s}^{-1}$). As shown in Fig. 7b, a similar sigmoidal trend is observed for the heat-checking density as a function of number of cycles. However, the saturated heat-checking density is almost tripled (ρ_{sat} increased from 50 to 140 mm⁻¹) when the heating period ht decreases from 6.5 to 1.2 s, or in other words, when Φ_{max} increases from 2.13 to 4.95 MW m⁻². The number of cycles to crack initiation appears to be delayed when the heating period increases (Fig. 7b). The heat-checking cells exhibit very different size frequency distributions depending on ht: faster heating cycles, achieved with greater maximum flux densities, produce smaller cells (Fig. 8a). In addition, these distribution curves are more scattered by increasing *ht*. The fastest heating cycles (with Φ_{max} > 3.8 - $MW m^{-2}$) present a normal Gaussian size distribution, while a negatively skewed distribution is observed for the slowest cycles (Φ_{max} < 2.9 MW m⁻²). The shape frequency distributions of the heat-checking cells are also more scattered when the TF tests were performed using a low heating rate (Fig. 8b).

The frequency distributions of the micro-crack branch orientations present a bi-directional aspect, with two prevailing directions at 0° and 90° (Fig. 9). Irrespectively of the heating period of the thermal cycle, the heat-checking patterns are close to trivalent networks, with a large majority of class 3 crack-junctions (between 78% and 87%), as reported in Table 3.

3.3. Effect of the initial hardness of the steel

Some TF tests (see Table 2) have also been performed on steel specimens with an initial hardness of 42 HRC. As shown in Figs. 10a and b, a very similar trend was observed for the heat-checking density ρ_{hc} vs. the number of cycles, regardless of the hardness of the steel and the maximum temperature (T_{max} = 650 and 685 °C).

Neither the saturated crack density, nor the number of cycles to crack initiation appear to be significantly affected by the initial hardness of steel.

In addition, the distribution of the crack junction classes are very similar for both hardness (Table 3). Therefore, it can be stated that the microscopic heat-checking is hardness-independent under these testing conditions.

4. Discussion

4.1. Dependence of the size of the heat-checking cells to heat-flux density

It is usually claimed that there is a critical temperature range ΔT_c for the crack initiation of "brittle materials" (elastic rupture behaviour), such as oxide scale [20] or ceramics [21]. Korneta et al. investigated the cracking of thermal shocked ceramics from



Fig. 6. Rose of directions of micro-crack branches (cumulated length vs. θ) for various maximum temperatures: T_{max} = 550 °C (a); T_{max} = 650 °C (b); T_{max} = 650 °C (c).

Table 3

Distribution of the trivalent (class 3), tetravalent (class 4) and pentavalent (class 5) crack junctions in the microscopic saturated heat-checking pattern produced by different thermal fatigue test conditions on 42 and 47 HRC heat-treated steel specimens.

TF test	Steel hardness (HRC)	Maximum temperature T_{max} (°C)	Heating time t (s)	Number of cycles N _t	Number of crack junctions N _n	Relative percentage of crack junction classes		
						3	4	5
1	47	550	0.90	80,000	4777	64.0	26.7	9.3
2	47	575	0.95	50,000	5563	60.5	28.9	10.6
3	47	600	1.0	80,000	4818	70.8	22.6	6.6
4	47	625	1.1	50,000	6253	67.5	24.2	8.3
5	42	650	1.2	20,000	5065	77.7	16.9	5.6
	47	650	1.2	20,000	5623	78.2	16.4	5.4
6	47	650	2.0	30,000	3388	77.7	16.0	6.3
7	47	650	3.7	30,000	1265	87.1	9.6	3.2
8	47	650	6.5	50,000	890	77.8	15.3	7.0
9	42	685	1.6	3000	6131	69.2	21.5	9.3
	47	685	1.6	3000	6524	69.1	20.4	10.6



Fig. 7. Effect of the heating time *ht* on the microscopic heat-checking, in the gauge area of the specimen ($T_{min} = 100$ °C, $T_{max} = 650$ °C, $\Phi_{max} \approx 4.85$ MW m⁻²): (a) increased sight of the cartographies showing the aspect of the saturated heat-checking for various *ht*; (b) evolution of the heat-checking density ρ_{hc} vs. number of cycles.

various maximum temperatures ranging from 300 to 700 °C, and observed that the crack density changes with the temperature range ΔT , when $\Delta T > \Delta T_c$ [21]. However, Fig. 11a shows that the saturated heat-checking density ρ_{sat} measured on our TF specimens in the stabilized regime does not vary much ($\rho_{sat} = 144 \pm 13 - \text{mm}^{-1}$, i.e. a difference of $\pm 9\%$) by changing T_{max} (and therefore ΔT). On the other hand, ρ_{sat} increases by increasing the heating rate hr (or decreasing the heating period ht (Fig. 11b). It should be highlighted that hr is a mean rate calculated by the ratio of the temperature amplitude ΔT to the heating period ht of the thermal cycle:



Fig. 8. Morphological characteristics of the microscopic heat-checking cells for various heating times ht, in the gauge area of the specimen (saturated regime): (a) size frequency distributions P(A); (b) compactness frequency distributions P(C).

$$hr = \Delta T/ht = (T_{max} - T_{min})/ht.$$
⁽¹⁾

This approximate estimation may explain the scattering observed on the best-fit curve (power law) of Fig. 11b (ρ_{sat} vs. hr) when hr is greater than 300 °C/s, although the correlation coefficient of the regression curve (R = 0.970) is relatively high. In addition, the heating period and heat-flux density are inter-dependent, if all other influencing parameters (such as the specimen geometry, T_{min} , and T_{max}) remain unchanged. By plotting the saturated microscopic heat-checking density ρ_{sat} as a function of the maximum heat-flux density Φ_{max} (Fig. 12) for all thermal cycling conditions, a remarkable linear relationship is found:

$$\rho_{sat} = 33.6\Phi_{max} - 23.2. \tag{2}$$



Fig. 9. Frequency distributions $P(\theta)$ of micro-crack branch orientations (cumulated length vs. θ), for various heating times *ht*.



Fig. 10. Evolution of the microscopic heat-checking density ρ_{hc} vs. number of cycles, in the gauge area of the specimen, for 42 and 47 HRC treated steels: (a) $T_{max} = 650 \text{ °C}$, ht = 1.2 s; (b) $T_{max} = 685 \text{ °C}$, ht = 1.6 s.

This correlation indicates that the saturated heat-checking density increases proportionally to the maximum heat-flux density, establishing a strong "size dependence" of the microscopic heat-checking cells with Φ_{max} in the investigated range (2 MW m⁻² < $\Phi_{max} < 5$ MW m⁻²). However, it could be expected that ρ_{sat} might not infinitively increase by increasing Φ_{max} , and may achieve a certain ultimate limit. Thus, a logarithmic law might be physically more consistent, although the determination coefficient (*R* = 0.955) is slightly lower than for Eq. (2) (*R* = 0.971). Unfortunately, due to limitation of our test facility, tests with very high heat-flux densities could not be performed to experimentally assess this point.

In Fig. 13, the variation of ρ_{sat} is reported as a function of the input energy per unit-area (*W*) at the external surface of the specimen,



Fig. 11. Effect on the saturated heat-checking density ρ_{sat} of the temperature range ΔT (a), and the heating rate hr (b) of the thermal cycle.



Fig. 12. Effect of the maximum heat-flux density Φ_{max} applied during the heating period on the saturated heat-checking density ρ_{sat} .

which is roughly estimated by multiplying the maximum heat-flux density by the heating period. This curve better indicates that beyond a critical limit of the transmitted energy per unit-area ($W_c \sim 3 \times 10^3$ J mm⁻²), the heat-checking density remains quasiunchanged. In fact, the oxide layer cannot dissipate the total thermo-mechanical dynamic energy imposed at the surface by self-constraint cracking, and therefore only a part of this energy is "sufficient" and contributes to the heat-checking. One can imagine that the oxide layer acts as a "thermo-mechanical dissipative barrier" material. Undissipated thermo-mechanical energy that is transmitted to the steel substrate, leads to propagate by thermal fatigue solicitations the micro-cracks initiated on the oxide-layer into the sub-layer steel. Repetition of such TF cycling can affect, in addition, the local properties of the steel (for example softening, highlighted by RT hardness measurements [3,5]), leading to thermal



Fig. 13. Effect of the input energy per unit-area *W* applied during the heating period on the saturated heat-checking density ρ_{sat} .

fatigue cracking. Indeed, beyond W_c , the TF macro-crack initiation life in base steel is reduced, and the crack growth rate is also increased [6,19].

4.2. Effect of thermal expansion mismatch on the saturated crack density

Detailed microscopic observations on the surface of the TF specimens show that the oxide scale is actually formed of two layers of equal individual thickness [18,19]. For the sake of simplification, one can consider that the specimen is composed of a bi-lamellar composite, consisting of an equivalent oxide layer and the steel parent. This equivalent oxide layer is mainly constituted of an iron oxide (Fe₂O₃) and a chromium oxide (Cr₂O₃), with different coefficients of thermal expansion ($\alpha = 14.9 \times 10^{-6} \text{ K}^{-1}$ and $7.3 \times 10^{-6} \text{ K}^{-1}$, respectively) [22]. Considering an average coefficient of thermal expansion for the equivalent oxide layer, whose deformation is controlled mainly by its thermal expansion, the total strain in the oxide layer can be calculated as:

$$\varepsilon_{t,ox} = \alpha_{ox} \cdot \Delta T = (\alpha_{\text{Fe}_2\text{O}_3} + \alpha_{\text{Cr}_2\text{O}_3}) \cdot (T_{max} - T_{min})/2.$$
(3)

For the bulk steel, the total strain $\varepsilon_{t,s}$ was calculated by FEM analysis, using ABAQUSTM software and a thermo-elasto-plastic constitutive law [19]. Fig. 14a and b illustrate the effects of the TF conditions (ΔT and ht) on the total strain in the equivalent oxide layer ($\varepsilon_{t,ox}$) and in the sub-layer steel ($\varepsilon_{t,s}$), and consequently on the strain difference $\Delta \varepsilon_t$:

$$\Delta \varepsilon_t = \varepsilon_{t,ox} - \varepsilon_{t,s}. \tag{4}$$

Whatever the temperature variation ΔT of the test, the total strain in the oxide layer and in the steel shows quite similar trends, with an approximately constant difference $\Delta \varepsilon_t$ of 0.365 ± 0.035% (Fig. 14a). Consequently, it can be claimed that T_{max} has no significant effect on the saturated heat-checking density, which shows similar values ($\rho_{sat} = 144 \pm 13 \text{ mm}^{-1}$, as previously shown, Fig. 11) provided that the maximum heat-flux density applied during the heating period is equivalent ($\Phi_{max} = 4.85 \pm 0.1 \text{ MW m}^{-2}$). On the other hand, a variation in the heating time – which results in various Φ_{max} values – affects the total strain only in the steel substrate, and not in the oxide layer (Fig. 14b). This implies a variation in the strain difference $\Delta \varepsilon_t$, leading to very different saturated heat-checking density $(47 < \rho_{sat} < 140 \text{ mm}^{-1})$. The strain difference represents in fact a local mechanical incompatibility generated by the thermal mismatch between two layers constituting the "composite material". This "mismatch strain" is therefore the main driving force leading to the cracking of the superficial oxide layer: the higher $\Delta \varepsilon_t$, the higher ρ_{sat} , as shown in Fig. 15.



Fig. 14. Evolution of the calculated total strain ε_{tr} generated in the oxide layer and in the substrate, as a function of the temperature variation ΔT (a) and the heating time *ht* (b) of the thermal cycle.

Nevertheless, the heat-checking density exhibits an asymptotic trend beyond a maximal critical $\Delta \varepsilon_t$ value (estimated at 0.35%), which can be defined as a "saturation strain difference" ($\Delta \varepsilon_s$) leading to a maximum value for the saturated crack density. In addition, it can be claimed that a total strain amplitude higher than $\Delta \varepsilon_s$ would result in crack opening and in-depth propagation into the parent steel [6,19]. The same conclusion was reached by Zhu et al., regarding the cracking behaviour of a Cu–Ni multilayer deposited on a polyimide substrate subjected to bending [23]. By extrapolating the curve of Fig. 15 to a null crack density ($\rho_{sat} = 0$), one can approximately estimate the critical strain difference ($\Delta \varepsilon_i \sim 0.13\%$) below which no micro-cracking could initiate in the oxide layer [23].

As mentioned earlier, Korneta et al. have attributed the variation of the crack density observed on thermally shocked ceramics at various T_{max} to the temperature amplitude ΔT [21]. However, these authors did not consider the cooling rate, presumably because of the thermo-elastic time independent behaviour of such fragile materials. In fact, during the cooling period, ΔT generates thermo-elastic strains and associated stresses that damage the ceramic. Nonetheless, a thermo-elastic loading approach is not relevant for materials with an elasto-plastic or elasto-visco-plastic behaviour, such as metallic alloys. For example, it is reported that the crack spacing observed in the oxide scale formed on steels and metallic alloys under creep experiments, stabilizes to a saturated value after reaching equilibrium [22]. This saturation crack spacing (named " L_{sat} ") and the saturated crack network density (ρ_{sat}) reported here - that is proportional to the inverse of the mean crack spacing - are in fact two reciprocal damage criteria [24]. In addition, it should be mentioned that ρ_{sat} is relevant to characterize multi-axial cracking (i.e. heat-checking), while Lsat better describes macroscopic uniaxial cracking. The creep experiments reported by



Fig. 15. Effect of the difference of total strain $\Delta \varepsilon_t$ between the oxide layer and the steel substrate $[\Delta \varepsilon_t = \varepsilon_{ox} - \varepsilon_s]$ on the saturated microscopic heat-checking density ρ_{sat} .

Schütze [22] have revealed that when the creep strain-rate of the substrate de/dt increases, the saturation crack spacing L_{sat} decreases (Fig. 16). By reporting the data from our experiments on the same figure, one can observe that the TF specimens present the same trend, even if the strain range is higher than under these creep experiments:

$$L_{sat} = 0.3904 (d\varepsilon/dt)^{-0.418}.$$
 (5)

It can be noted that the strain rate exponent calculated from our curve is lower than 0.5 (m = -0.418). This value is very close to those reported in creep experiments (-0.33 < m < -0.41) [22]. Under creep conditions, the oxide layer behaves as a quasi-elastic material constrained by a substrate having an elasto-visco-plastic behaviour. Schütze interpreted L_{sat} as a "viscous sliding" due to the ability of the substrate steel to creep in the range of 10^{-8} to 10^{-6} strain rate (without specifying whether it is a secondary creep strain rate or not). Under the TF conditions investigated in this study, the behaviour of the sub-surface layer can be described to a lesser extent by a low strain time-dependant creep behaviour than by the frequency-dependent cyclic plasticity, even if the physically based phenomena of plastic cyclic softening and creep would be similar.

4.3. Micro-crack initiation life

It is observed that for a prescribed maximum heat-flux density, the estimated number of cycles N_i to initiate microscopic



Fig. 16. Evolution of the saturation crack spacing L_{sat} in the oxide scale as a function of the strain rate $d\epsilon/dt$ of the substrate, for various metallic alloys under creep experiments [22] and thermal fatigue tests.

heat-checking [18] is strongly dependent on the temperature amplitude of the thermal cycle: a higher ΔT leads to an earlier micro-crack initiation (Fig. 17a). In addition, Fig. 17b shows that for TF tests performed under the same T_{max} (600 and 650 °C), the heat-checking life N_i also changes with the heating rate: a slower hr delays the crack initiation. It appears that different curves are obtained depending on T_{max} , indicating that the dependence of N_i with hr would be more sensitive at high T_{max} . However, this statement needs to be verified by additional tests, with different heating rates at 600 °C and/or 685 °C. It can be noted that a similar effect of ΔT and hr was also observed – in larger number of cycles – on macro-crack initiation life, as reported in [6,19].

It is generally stated that under stretching, an oxide layer or a thin film initiates cracking when it reaches a critical thickness [20,24,25], and that beyond this critical thickness, the crack density increases with the thickness of the layer [24,25]. Based on thickness measurements of the oxide layer formed on our specimens after different numbers of cycles, a model was established to estimate the oxide thickness at a given cycle time [6,19]. For T_{max} > 600 °C and a large number of cycles, it has been shown that the oxide growth rate follows a parabolic law. The thickness of the oxide layer formed during the TF test is higher when the heating rate is slower, since the total oxidation time is longer. However, as mentioned above, N_i is governed by the heating rate. For example, the test performed with a T_{max} of 650 °C and a high heating rate $(hr = 458 \text{ °C.s}^{-1})$ led to a shorter micro-crack initiation life (almost three time lower) than a test performed at the same T_{max} with a slower heating rate ($hr = 85 \circ C s^{-1}$), while the oxide scale was five times thicker in the second case (Fig. 17b).

In our TF experiments, the oxide thickness alone cannot be a consistent factor to explain the initial formation of the crack pattern. In fact, the cracking of the oxide scale is mainly governed by the strains and stresses induced in the specimen, due to the



Fig. 17. Effect of the temperature variation ΔT (a) and of the heating rate hr (b) on the number of cycles N_i to initiate the microscopic heat-checking.



Fig. 18. Effect of maximum stress σ_{max} (a) and plastic strain $\Delta \varepsilon_p$ (b) on the number of cycles N_i to initiate the microscopic heat-checking.

thermal fatigue loading. Fig. 18a and b respectively show the effects of the maximal stress σ_{max} and plastic strain amplitude $\Delta \varepsilon_p$ on the microscopic heat-checking life N_i . It should be noted that σ_{max} and $\Delta \varepsilon_p$ are calculated for the parent steel, since the proper mechanical properties of the oxide layer (which are not really known) could not be included in the FEM analysis [19]. By plotting N_i as a function of σ_{max} (Fig. 18a), two different curves were obtained depending on the initial hardness of the steel. This can be attributed to the fact that the maximum stress σ_{max} , achieved at T_{min} of the thermal cycle, is higher for the steel with a lower initial hardness (42 HRC) [19]. This is consistent with thermo-mechanical cycling of many metallic materials, where a higher plastic strain produced at T_{max} results in higher σ_{max} . However, the difference in σ_{max} reduces when the temperature increases. Thus, the hysteresis loops of both steels are quasi identical for T_{max} = 685 °C [19], leading to the same micro-crack initiation life N_i (as shown in Fig. 18 a).

On the other hand, a single power law is found by plotting N_i vs. $\Delta \varepsilon_p$ (Fig. 18b):

$$\Delta \varepsilon_p = 0.5813 N_i^{-0.587}.$$
 (6)

It can be noted that the exponent found in Eq. (6) is very close to the Manson–Coffin exponent (c = -0.6) generally reported for metallic materials. Therefore, the plastic strain amplitude seems to be a reliable criterion for predicting the micro-cracking initiation in TF experiments, whatever the test conditions and the initial hardness of the base steel.

5. Conclusions

Heat-checking of X38CrMoV5 hot work tool steel was investigated under thermal fatigue experiments. The specimen surface was subjected to cyclic induction heating and natural cooling, under various test conditions. Thermal cycles, with a minimal temperature of 100 °C and a maximal temperature (T_{max}) ranging from 550 °C to 685 °C, were performed. The heating time (*ht*) was also changed for T_{max} = 650 °C, leading to various maximum heat-flux densities applied on the specimen surface. The tests were regularly stopped and the oxidized surface of the specimen was observed by scanning electron microscopy (SEM). The evolution of the density and morphology of the microscopic crack pattern was quantified using image analysis techniques.

It is shown that the evolution of the heat-checking density vs. number of cycles presents a sigmoidal trend and achieves rapidly a saturated density regime following the crack pattern initiation. It was observed that the heat-checking density is independent of the maximum temperature of the thermal cycle, whereas an increased heating rate leads to a higher micro-cracks density. The size of the heat-checking cells observed in the saturated regime can be linearly related to the maximum heat-flux density applied during the heating period. It is shown that the energy transmitted to the specimen leads to the cracking of the oxide layer, until a certain limit corresponding to the smallest size of the heat-checking cells. The difference between the thermo-mechanical strains in the oxide layer and in the parent steel can explain the change in crack density observed on the surface of the TF specimen. The initial hardness of the steel has no effect on the heat-checking density and morphology.

Whatever the parameters of the thermal cycle (i.e. low or high maximum temperatures, slow or fast heating rates), the crack patterns exhibit a strong similarity in the stabilized regime. Two preferential orientations are observed for the micro-cracks, corresponding to the longitudinal and circumferential axis. Although the size of the heat-checking cells may vary, their shape and orientation remain almost unchanged. All the saturated heatchecking networks are nearly trivalent and isotropic.

The initiation of the microscopic heat-checking is strongly delayed when the temperature amplitude of the thermal cycle decreases, and in a lesser extent when the heating time increases. It is shown that the number of cycles to crack initiation is less dependent on the oxide scale thickness than on thermo-mechanical loading imposed to the specimen. It appears that a criterion based on plastic strain amplitude rationalizes the TF heat-checking life, independently of the initial hardness of the steel.

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