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To cite this version:

Abdelghani Chahmi, Abdelhak Djoudi. Diagnosis of the Induction Machine by the Kalman Filter . The 5th International Conference on Electrical Engineering (ICEE 2017), Oct 2017, Boumerdes, Algeria. hal- 01649861

HAL Id: hal-01649861 <https://hal.science/hal-01649861v1>

Submitted on 27 Nov 2017

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Diagnosis of the Induction Machine by the Kalman Filter

Abdelghani Chahmi, Abdelhak Djoudi

*Abstract***—This paper deals with the detection and localization of electrical drives faults, especially those containing induction machines. First, the context of the study is presented and an Extended Kalman Filter is described for induction machines fault detection. Then the modeling procedure under faulty conditions is shown, and the machine diagnosis methods are developed. The proposed diagnosis approach requires only little experimental data, and more importantly it provides efficient simulation tools that allow characterizing faulty behaviors**

Index Terms—**Induction Motor, Modeling, Rotor Defect, Stator Defect, Extended Kalman Filter.**

I. INTRODUCTION

arge industrial systems are widely confronted to the challenges of reliability and availability of the production devices. Electric drives containing an induction machine are largely used in the industrial applications thanks to their low costs, high performances and robustness [1]. As known, a system can realize the assigned task, only under conditions ensuring the security. An early detection of anomalies in electrical motors may help avoiding downtimes [2]. Thus, in order to detect an incipient fault, we should give a special attention to the spectral analysis of stator currents [3], [4]. Most of recent researches on defects detection of induction machines use the stator currents analysis. Several condition-monitoring methods [5] have been developed and were used to help the detection of electric defects in induction machine. Among these methods, the authors in [17] consider the vibrations monitoring, torque control, the temperature monitoring, etc. In this paper, the rotor resistance is estimated using a method of Extended Kalman Filter (EKF). This state observer is proved to be a useful tool to determine the parameter variations [6], [7]. In this paper, it is shown that L

EKF can be employed to identify the disturbance in rotor resistance. Recently, the Kalman filter was applied successfully for defect forecasting in [8]. For example it is used to interpolate the trends of a signal-learned g from the recorded data and then estimate the evolution of defects in the proposed diagnosis methods in [9]. In this study, the proposed approach considers the value of rotor resistance as fixed for condition monitoring. This value in the diagnostic tools which one uses is not fixed contrary to the classical approaches of control of machine. Hence, we propose a method that considers a variation of rotor resistance in order to give a good estimate as well as a good robustness for the control of the induction machine. This paper is organized as follows: part II describes the induction machine model under simplifying assumptions. Induction machine models have been developed

under healthy and faulty conditions in the (abc) reference frame. Part III, presents a state of the art review of Extended Kalman Filter. Finally, part IV gives digital simulations of the proposed faulty model. The obtained results prove the effectiveness of the proposed monitoring method based on an Extended Kalman Filter.

II. INDUCTION MOTOR DRIVES

A. Overview of the Drive

The drive under study is composed of a machine with induction, inverter of width of impulse, ordering of rotor flow - directed, a loop of measurement of the current and a loop of speed control. Figure 1 presents the total diagram of the unit.

Fig.1. Schematic diagram of the system under study

B. MODEL OF THE INDUCTION MOTOR

 The objective of this section is to present the different models used for our study. This is first of all to model the induction machine finely enough to introduce a relevant modeling of defects. Then we present how the default templates are not used in their simplified and balanced version diagnostic purposes.

1) Models Simulation Proposed in the Reference Frame (abc): The induction machine is a known system-well [10]; models exist and allowing, in the majority of the cases and under certain simplifying assumptions, a representation of the machine without fault. These assumptions are the following ones [11-12]:

-The air-gap is of constant width without effect of notch (not of eccentricity, of unbalance, reduction amongst harmonics in the development of inductances expression).

- Assimilation of the cage to a short-circuit having the same number of phases as static winding (simplification of the equations of the machine by taking into account the average effect of the cage).

- Sinusoidal distribution, along the air-gap, of the magnetic fields of each winding (simplification of the equations of the machine by taking into account of the expressions in complex of the currents, allows to use a vectorial model).

- Absence of saturation in the magnetic circuit (identical behavior of each phase, allows use of a vectorial model).

- The influences of the effect of skin and the heating of the drivers are neglected (not variation of the parameters intervening in the machine under normal functioning).

- Star coupling of windings (the currents form a system balanced under normal functioning).

 Under the conditions pointed out previously, the equations of the electrical circuits utilize clean and mutual inductances making it possible to define flows according to the currents [11].

On the level of the stator, the tensions check:

$$
\begin{bmatrix}\nVsa \\
Vsb \\
Vsc\n\end{bmatrix} = [R_s] \begin{bmatrix}\nisa \\
isb \\
isc\n\end{bmatrix} + \frac{d}{dt} \begin{bmatrix} \varphi sa \\
 \varphi sb \\
 \varphi sc\n\end{bmatrix}
$$
\n(1)

Where the resistances matrix is written according to the supposition of symmetry

$$
[R_s] = \begin{bmatrix} r_s & 0 & 0 \\ 0 & r_s & 0 \\ 0 & 0 & r_s \end{bmatrix}
$$
 (2)

On the level of the rotor, under - assumption-that - rotor-is comparable to a rotor with three-phase rollings up, the voltage are written

$$
\begin{bmatrix}\nVra \\
Vrb \\
Vrc\n\end{bmatrix} = [R_R] \begin{bmatrix}\nira \\
irb \\
irc\n\end{bmatrix} + \frac{d}{dt} \begin{bmatrix}\n\varphi ra \\
\varphi rb \\
\varphi rc\n\end{bmatrix}
$$
\n(3)

Matrix RR has the same form that RS, flux vector are expressed according to the inductances matrix and stator and rotor currents

$$
\begin{bmatrix} \n\phi sa \\ \n\phi sb \\ \n\phi ac \n\end{bmatrix} = [L_s] \begin{bmatrix} isa \\ isb \\ isc \end{bmatrix} + [M_{SR}] \begin{bmatrix} ira \\ irb \\ irc \end{bmatrix}
$$
\n(4)

$$
\begin{bmatrix} \varphi ra \\ \varphi rb \\ \varphi rc \end{bmatrix} = [M_{RS}] \begin{bmatrix} isa \\ isb \\ isc \end{bmatrix} + [L_R] \begin{bmatrix} ira \\ irb \\ ire \end{bmatrix}
$$
 (5)

 In order to be able to give an account of the interactions between the phases, we expressed each resistance and inductance matrix according to the number of whorls of rollings up of the machine.

$$
\begin{bmatrix} R_{S} \end{bmatrix} = \begin{bmatrix} R_{sa} & 0 & 0 \\ 0 & R_{sb} & 0 \\ 0 & 0 & R_{sc} \end{bmatrix} = R_{s} \begin{bmatrix} n_{sa} & 0 & 0 \\ 0 & n_{sb} & 0 \\ 0 & 0 & n_{sc} \end{bmatrix}
$$

\n
$$
\begin{bmatrix} R_{R} \end{bmatrix} = \begin{bmatrix} R_{ra} & 0 & 0 \\ 0 & R_{rb} & 0 \\ 0 & 0 & R_{rc} \end{bmatrix} = R_{r} \begin{bmatrix} n_{ra} & 0 & 0 \\ 0 & n_{rb} & 0 \\ 0 & 0 & n_{rc} \end{bmatrix}
$$
 (6)

 nsa corresponds to the number of whorls of the phase a has stator.

$$
\begin{bmatrix} L_S \end{bmatrix} = \begin{bmatrix} L_{sa} & M_{sab} & M_{sca} \\ M_{sab} & L_{sb} & M_{sbc} \\ M_{sca} & M_{sbc} & L_{sc} \end{bmatrix} = \begin{bmatrix} n_{sads}^2 & n_{sa}n_{sb}m_s & n_{sa}n_{sc}m_s \\ n_{sa}n_{sb}m_s & n_{s}^2l_s & n_{sb}n_{sc}m_s \\ n_{sa}n_{sc}m_s & n_{s}^2l_s & n_{s}^2l_s \end{bmatrix}
$$
\n(7)
\n
$$
\begin{bmatrix} L_R \end{bmatrix} = \begin{bmatrix} L_{ra} & M_{rab} & M_{rca} \\ M_{rab} & L_{rb} & M_{rbc} \\ M_{rca} & M_{rbc} & L_{rc} \end{bmatrix} = \begin{bmatrix} n_{ra}^2l_r & n_{ra}n_{rb}m_r & n_{ra}n_{rc}m_r \\ n_{ra}n_{rb}m_r & n_{rb}^2l_r & n_{rb}n_{rc}m_r \\ n_{ra}n_{rc}m_r & n_{rb}n_{rc}m_r & n_{rc}^2l_r \end{bmatrix}
$$
\n(9)
\n
$$
\begin{bmatrix} [n_{sa}n_{sa}m_{sc}\cos(\theta)] & n_{sa}n_{sa}m_{sc}\cos(\theta/2\pi/3) & n_{sa}n_{sa}m_{sc}\cos(\theta/2\pi/3) \\ n_{sa}n_{sa}m_{sc}\cos(\theta/2\pi/3) & n_{sa}n_{sa}m_{sc}\cos(\theta/2\pi/3) & n_{sa}n_{sa}m_{sc}\cos(\theta/2\pi/3) \\ n_{sa}n_{sa}m_{sc}\cos(\theta/2\pi/3) & n_{sa}n_{sa}m_{sc}\cos(\theta/2\pi/3) & n_{sa}n_{sa}m_{sc}\cos(\theta/2\pi/3) \end{bmatrix}
$$

$$
\left[M_{SR}(\theta)\right] = \left[M_{RS}(\theta)\right]^T
$$

2) Cage Electric Failures in the (abc) Model: This model that we have just described in the previous part allows in particular creating asymmetrical faults in both stator and rotor by the variation amongst whorl of the rolling up of the phase at fault. The defect can be localized on one or more phases. It should be noted that this modeling can be criticized: the defects of type short-circuit are represented in the model like removals of whorls i.e. openings partial of phase; that does not correspond completely to reality since it would also be necessary to take account of the shading rings [12]. This model constitutes a progress compared to the balanced models or /and considering only one variation of resistance usually used to validate the algorithms [13].

A. Model "The Good Performance" for Control and of Monitoring

 Models are necessary to design and improve the controllers and the observers. They are commonly balanced. One passes from the reference frame (abc), fixes, with the fixed reference frame (α, β) by the transformation of Concordia [14].

$$
\begin{cases} pX = A_c X + B_c U \\ Y = C_c X \end{cases}
$$

With $X = [isa \text{ is } \beta \text{ or } \alpha \text{ or } \beta] T$

$$
A_c = \begin{bmatrix} -\gamma & 0 & \frac{K}{\tau} & K\omega \\ 0 & -\gamma & -K\omega & \frac{K}{\tau} \\ \frac{L_m}{\tau} & 0 & -\frac{1}{\tau} & -\omega \\ 0 & \frac{L_m}{\tau} & \omega & -\frac{1}{\tau} \end{bmatrix}
$$

$$
B_c = \begin{bmatrix} \frac{1}{\sigma L_s} & 0 & 0 & 0 \\ 0 & \frac{1}{\sigma L_s} & 0 & 0 \end{bmatrix}^T C_c = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}
$$
and
$$
\gamma = \frac{R_s}{\sigma L_s} + \frac{1-\sigma}{\sigma \tau} \quad \tau = \frac{L_r}{R_r} \quad K = \frac{L_m}{\sigma L_s L_r} \quad \sigma = 1 - \frac{L_m^2}{L_s L_r}
$$

 D. Induction Machine Discrete Model

 We develop in this paragraph a discrete model of an induction machine in order to be able to use these equations in the development of Kalman Filter. We consider indeed that the equations of the observer at ends of diagnosis will be inevitably used in a system containing microprocessor or other and thus entered in the form of a discrete model. The discrete version is obtained by using the formula of Euler:

$$
\begin{cases}\n\frac{x(k+1) - x(k)}{T_s} = A_c x(k) + B_c U(k) \\
y(k) = C_c x(k)\n\end{cases}
$$
\nOf or

\n
$$
\begin{cases}\nx(k+1) = (T_s A_c + I)x(k) + T_s B_c U(k) \\
y(k) = C_c x(k)\n\end{cases}
$$
\nOr

\n
$$
\begin{cases}\nx(k+1) = A_d x(k) + B_d U(k) \\
y(k) = C_d x(k)\n\end{cases}
$$

$$
A_d = I + A_c T_s, B_d = B_c T_s, C_d = C_c
$$

III. INDUCTION MACHINE OBSERVER-BASED EKF

 This part presents the proposed method to supervise the application. We will develop the method by using the observer model previously described.

A. The Extended Kalman Filter

 The basic equations of the extended Kalman filter are deduced from that of the discrete model of the machine in good fonctionnement.la discrete matrix of state. One introduces noises of state and noises of measurement [15] - [16]. The function F is defined so that one to extend filter of Kalman has all the parameters of the machine. The estimate of rotor resistance is considered like means of monitoring.

$$
\begin{cases} x(k+1) = A_d x(k) + B_d U(k) + w(k) \\ y(k) = C_d x(k) + v(k) \end{cases}
$$

Where

 $f(x(k),U(k)) = A_d x(k) + B_d U(k)$ The process noise w (k) is characterized by $E{w(k)}=0$ $E\left\{w(k)w(k)^{T}\right\} = Q$ Where Q is definite positive. The measurement noise v (k) respects:

$$
E\{v(k)\} = 0
$$

$$
E\{v(k)v(k)^{T}\} = R
$$

R is definite positive too.

If we call P the matrix of covariance of the error in estimation, this matrix is obtained to leave:

$$
p(k/k) = E\left\{ (x(k) - \hat{x}(k)) (x(k) - \hat{x}(k))^T \right\}
$$

The notation k/k corresponds to a prediction at time K based on data up to and including time K (a priori covariance) and $k+1/k$ corresponds to a prediction at time $k+1$ starting from the data until the time K (a posteriori covariance). In the following equations, t represents the Jacobian matrix of the nonlinear function f is used [6].

$$
J = \frac{\partial f}{\partial x(k)}\bigg|_{\hat{x}(k), U(k)}
$$

Applied to the system under study, J can be expressed as

$$
J = \begin{bmatrix} 1 - \gamma T_s & 0 & \frac{K}{\tau} T_s & K\omega T_s & -\frac{1}{\sigma L_s} T_s \hat{i}_{sd} \\ 0 & 1 - \gamma T_s & -K\omega T_s & \frac{K}{\tau} T_s & -\frac{1}{\sigma L_s} T_s \hat{i}_{sq} \\ \frac{L_m}{\tau} T_s & 0 & 1 - \frac{T_s}{\tau} & -\omega T_s & 0 \\ 0 & \frac{L_m}{\tau} T_s & \omega T_s & 1 - \frac{T_s}{\tau} & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}
$$

At each integration time, the Kalman Filter equations to be solved are:

1/Computation of the observer states

$$
\hat{x}(k+1/k) = J\hat{x}(k/k) + B_d U(k)
$$
\n(16)

2/Computation of the a posteriori covariance matrix $P(k+1/k)$

$$
P(k+1/k) = JP(k/k)JT + Q
$$
\n(17)

3/Computation of the outputs of the filter

$$
\hat{x}(k+1/k+1) = \hat{x}(k+1/k) + G_d(k+1).
$$
\n[18]

$$
\[y(k+1) - C_d \hat{x}(k+1/k)\]
$$

4/Computation of the feedback gain matrix of the Kalman Filter

$$
G_d(k+1) = P(k+1/k)C_d(k+1)^T
$$

\n
$$
[C_d(k)P(k+1/k)C_d(k)^T + R]^{-1}
$$
\n(19)

5/ Computation of the a priori covariance matrix $P(k+1/k+1)$ $G_d (k+1)C_d (k+1)P(k+1/k)$ $P(k+1/k+1) = P(k+1/k) -$ (20)

We consider that Q and R matrix are constant but they can be time variant. The behavior and the stability of the Kalman Filter are functions of Q and R.

IV. Simulation Results and Discussion

The test conditions are the following:

- From t=0 to t=0.3s, flux application
- From 0.3 to 1.8s, liner increase of the speed reference
- From 1.8s constant speed
- At t=3s, fault in the machine

The observers are enabled from beginning.

A. Good performance

 Our approach in this part of simulation is to see the behavior of the induction machine in healthy mode and with electric defect (rotor, stator, inverter) in the mode transitory and permanent, after from there will introduce an observer on the outlet side of the machine (extended Kalman filter) is to see its reaction. The results result from rotor resistance, the stator current FFT.

 The following figure takes the form of the current in a phase of the induction machine. One can distinguish there the various phases related to the order from the system: phase of fluxing, phase of application of the instruction of couple related to the slope of speed, then stabilization the speed and instruction of couple. Up to 0.3 second, the purpose of the applied voltages is to position the vector flow in the machine, as from this moment, an instruction of couple is applied to the order and speed believes.

 The following figure takes the form of stator flux following the axis alpha. One finds well the phase of fluxing as well as the evolution of flow according to the increase number of revolutions of the machine and thus of the frequency of the supply voltages.

The following figure presents the evolution of the produced torque by the induction machine. One finds the phase of acceleration (with a going beyond related to the speed control) and the phase of stabilization speed and thus couple.

 The following figure takes the form the speed of the system. One finds well there the various phases, which one describes previously.

 The following figure takes the form of rotor resistance at exit of the filter of Kalman (for a healthy system). One notes a drift of rotor resistance according to speed. This derivative was corrected: according to speed, the estimated parameter is compensated for so that it is closer to the expected value. This compensation has the form of a linear relation between the drift of rotor resistance and speed.

Fig. 6.Estimate of rotor resistance by the filter of Kalman without compensation

 The following figure takes the form of rotor resistance with compensation of the drift according to speed.

B. Defect with the rotor

 Rotor faults Figure 8 takes the form of the stator current for an unbalanced defect (40% of whorls removed in the phase at fault), note the appearance of the lines in the spectrum of the current. The defect with the rotor is characterized by the appearance of two frequencies $(1\pm 2g)$ or g represents the slip (92,2Hz et107Hz) around the electric frequency f electric (100Hz). If the FFT of this signal is made, this defect will be very difficult to detect in the spectrum of the current because the amplitude of the line at the fundamental frequency is very important compared to that of the required line and these lines are at a frequency frame the line with fundamental with a difference related to the slip (in general very weak).

The following figure takes the form of resistance estimated for a defect unbalanced to the rotor (40% of whorls removed at fault on a phase). Noting however that the estimate of rotor

resistance is assigned to the moment $t=3$ second (time of the application of defect) from where appearance of the low frequency oscillations. This existence of the frequency allows then on the basis of resistance rotor estimated characterizing that it is well a defect with the rotor

Fig. 9 Estimation resistance rotor for an asymmetrical fault witch the rotor

C. Defect with the Stator

Figure 10 takes the form of the stator current for a defect unbalanced to the stator (40% of whorls removed at fault on a phase). Let us note the appearance of the frequency, which characterizes the defect, which is 3felectric (300Hz). The appearance of the lines in the spectrum of the current is due to the application of the defect to the moment $t= 3s$, it is easy to detect the frequency, which characterizes the defect in low frequency. (See figure below after the stator phase current FFT).

Fig.11. FFT of the static current of the phase

The following figure presents the current of the phase at exit of the machine and the current for the same phase at exit of the observer, it should be specified that the two currents (measured and estimated) are similar. The observer thus modified the rotor size resistance so that the two currents are "identical". The error, which exists between the two currents, explains by the fact why the observer is a discrete system: he thus does the calculations of the sizes on the basis of measure taken at previous time. This explains the light error of hauling.

Fig.13 .Estimation rotor resistance for an asymmetrical fault witch the stator

1) Synchronous Demodulation Applied to Rotor Resistance: Each defect has a frequency which characterizes it, the idea of this method consists with research the amplitude of the line associated with this frequency to detect the evolution of this one. The principle of this demodulation is exposed to the following figure.

Fig.14. Principe of the demodulation

 The following figure has the amplitude of the line associates with the frequency of defect (2fe). The characteristic is well detected by this monitoring system. The defect is applied to 3 seconds.

D. Inverter fault

 Figure 16 takes the form of the stator current of the machine at fault of inverter. We chose to give an account of the effects of an open component. For that, we included a block allowing to block the control commands arriving at the switch considered as failing. After the period of fluxing (0s-0.3s), one notices that the size is sinusoidal until the application of the defect to the moment t=3seconde. The occurrence of the defect thus leads to the appearance of the frequencies, which characterize this defect in low and high frequency (see figure 17 which presents the FFT of the stator current).

Figure.16.Stator current of the machine at fault of inverter

IV. CONCLUSION

 The study presented in this paper is a contribution to the diagnosis of the defects of electric machinery, with special focus on squirrel-cage induction machine. Indeed, induction machines are appropriate for applications where high power and speed are required. This is due, to multiple advantages (simplicity of construction, robustness, performances…).However, for certain applications requiring high degree of reliability, it is necessary to carry out a fast and early detection of possible failures. The presented study focus on the contribution of the analytical in this article exposes the contribution of the analytical method containing models of the system to the diagnosis of the electric defects of the asynchronous machines. The vectorial control of the induction machine requires observers (possibly extended). We first of all showed that the use of an extended observer for diagnosis purpose made it possible to detect the principal defects in the electrical machine. The parameter used for the diagnosis is the estimated rotor resistance. We showed that by coupling a spectral analysis of the estimated parameter that the technique could appear useful. The Kalman filter uses dynamics of the rotor resistance, which defines the evolution its value in time domain to obtain reliable data in the case of healthy machine (convergence of the estimate). We are aware of having studied only certain aspects of a very vast subject of study, which requires the comprehension of the system and the use of suitable tools. The prospects with this work are multiple, from the point of view of the monitoring, the use of other parameters (stator resistance, stator inductance) to evaluate the performance of the wide observer. Then, from the point of view the detection of the defects, it will be interesting to study the monitoring of this kind of machine used as a generator of power (of wind turbines type for example) connected to the electrical.

APPENDIX

 $Rs = 0.0142Ω$; Ls = 0.001314 H; Rr = 0.0126Ω; Lr = 0.001286H; Lm = 0.00123H; $p = 3$; $\sigma = 0.1047$; Q = 0, 1; R= 0, 01

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