

# Solubility of drug-like molecules in pure organic solvents with the CPA EoS

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#### 1 Abstract

Solubility data in different solvents are an important issue for separation processes involving complex molecules such as natural products and pharmaceutical drugs. Nonetheless, solubility data are in general scarce and difficult to obtain, and so models are important tools to generate the necessary estimates.

6 Different correlative, statistical and thermodynamic models have been proposed 7 to evaluate solubilities. From these, the more theoretically sound thermodynamic 8 models allow to generate estimates at broader temperature, pressure and composition 9 conditions while using a smaller amount of experimental information. Among these, the 10 Cubic-plus-Association equation of state that combines the simplicity and robustness of 11 a cubic equation of state with the Wertheim's association contribution has been under 12 attention. In this work, this EoS is for the first time proposed to model organic phase 13 solubilities of drug-like molecules in a wide range of temperatures.

Solubilities of acetanilide, acetylsalicylic acid, adipic acid, ascorbic acid, hydroquinone, ibuprofen, paracetamol and stearic acid were estimated in alcohols, ketones, alkanes, esters, acids, aromatics, chlorinated solvents, as well as in other common solvents. The hydrogen bonding behaviour was explicitly accounted for with each associating group being treated individually, as well as multiple group substitutions.

Accurate correlations were obtained using a single binary interaction parameter (global AAD of 24.2%), while considering the complexity of the studied systems predictions were generally also satisfactory.

23

24 Keywords: CPA, drug-like, modelling, solubility, organic solvents.

#### 1 1. Introduction

The first step in the physicochemical characterization of a pharmaceutical drug candidate involves solubility studies. In general, solubility data in several solvents at various temperatures are important during pre-formulation steps [1].

Given the complexity of most drug and drug-like molecules, and the variety of their solvent interactions, many thermodynamic tools have been proposed for modelling such equilibrium data. Reviews on the most commonly used models in the pharmaceutical industry can be found elsewhere [2, 3]. However, the readily application of these theoretical methods is commonly hampered by the lack of information about the molecules under study, and therefore empirical or semiempirical models are usually used, showing good agreement between experimental and correlated data [4-11].

12 One of the most widely used thermodynamic approaches in the pharmaceutical 13 industry is the regular solution theory [12], which is still being used [13]. The solubility 14 is a function of the solvent and solute solubility parameters, and the determination of 15 solubility parameters has been subject of many studies [14-16]. As a drawback, 16 solubilities higher than the ideal solubility cannot be described, as the minimum activity 17 coefficient is one. In spite of some poor results were obtained and temperature 18 dependence cannot be described accurately, this model became very popular for solvent 19 screening due to its higher predictive character.

20 On the other hand, models based on the excess Gibbs energy have been widely 21 used and proved to be able to describe properly the experimental data [6, 7, 13, 17-19]. 22 However, the application of these models is limited to the availability of interaction 23 parameters or, when not available, to the existence of data for their fitting. In this sense, 24 the application of predictive group-contribution methods, such as UNIFAC, has been 25 increasing [13, 19, 20], but the description of the solubility temperature-dependence of

1 high molecular weight compounds are still a weakness of this model [21], as well as the 2 necessary group-interaction parameters can sometimes be unavailable. A successful and 3 quite recent model is the Non-random Two Liquid Segment Activity Coefficient 4 (NRTL-SAC) model [22, 23], which has been widely applied to correlate and predict 5 phase equilibria of non-ideal systems, like those containing complex pharmaceuticals 6 [2, 24]. One advantage is that it only requires a set of well-chosen data to fit a small 7 number of parameters. Despite its suitability, this model has a correlative nature since 8 the solute parameters have to be estimated from mixture data. Other models applied for 9 pharmaceuticals are based on statistical mechanics, especially COSMO and its 10 derivatives, where only data from quantum chemical calculations are used [20]. Some 11 attempts were done to use these models for complex pharmaceuticals, but their 12 capabilities for solid-liquid equilibria have not yet been proven [20, 21, 25].

The increasing interest on the high pressure processing of pharmaceuticals suggests the use of equations of state for modeling their phase equilibria. Some equations of state have already been applied for that purpose, not so widely to pharmaceutical compounds, but to more simpler drug-like molecules.

17 Ruether and Sadowiski [26] investigated the use of the Perturbed-Chain 18 Statistical Associating Fluid Theory (PC-SAFT) to predict the solubility of five typical 19 drug substances and intermediates in pure and mixed solvents. The model allowed an 20 accurate description of the temperature dependence of the solubility applying a linear 21 temperature-dependent binary interaction parameter per system. The solubility in mixed 22 solvents was reliably predicted without any additional fitted parameter. Tsivintzelis et 23 al. [27, 28] applied the nonrandom hydrogen-bonding (NRHB) EoS to model the phase 24 behaviour of several mixtures of pharmaceuticals. Very satisfactory correlations were 25 obtained using only one optimized binary interaction parameter, even in supercritical

CO<sub>2</sub> and ethane. This model was also able to predict accurately the solubility in mixed
 solvents based on interaction parameters fitted to the corresponding single solvent data.
 Recently, our group successfully used the CPA EoS for modeling the aqueous solubility
 of drug-like molecules [29].

5 The aim of this work is to evaluate the CPA EoS for modeling drug-like 6 solubilities in organic solvents in a wide temperature range. The solubilities of 7 acetanilide, acetylsalicylic acid, adipic acid, ascorbic acid, hydroquinone, ibuprofen, 8 paracetamol and stearic acid were studied in solvents covering several alcohols, 9 ketones, alkanes, esters, benzene derivatives and carboxylic acids. The molecular 10 structures of the compounds under study are presented in Figure 1.

11 As observed before for the aqueous solubilities [29], there is a good agreement 12 between the experimental and calculated data using a single temperature independent 13 binary interaction parameter.

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- 16 2. Thermodynamic framework
- 17

The solubility of a solid in a liquid solvent is calculated by solving the thermodynamic equations of equilibrium [12]. Assuming a pure solid phase, no significant temperature dependence on the difference between the heat capacity of the pure liquid and solid ( $\Delta C_p$ ), and neglecting the effect of pressure on melting temperature ( $T_m$ ), solute enthalpies of solid-solid and melting transition ( $\Delta_t H$ ), and  $\Delta C_p$ , the following expression for the mole fraction solubility is obtained [12]:

$$x_{s} = \frac{\varphi_{s}^{liq_{0}}}{\varphi_{s}^{liq}} \exp\left\{-\sum_{tr} \frac{\Delta_{tr}H}{R} \left(\frac{1}{T} - \frac{1}{T_{tr}}\right) + \frac{\Delta C_{p}}{R} \left[\frac{T_{m}}{T} - 1 - \ln\left(\frac{T_{m}}{T}\right)\right]\right\}$$
(1)

2

1

3 where  $x_s$  is the solute mole fraction solubility, *R* is the ideal gas constant, *T* is the 4 absolute temperature,  $\varphi$  is the fugacity coefficient and subscripts  $\theta$  refers to a pure 5 component, *tr* for a pure solute phase transition and *m* for melting. The different solid-6 solid and fusion phase transitions of the solute are concerned in the summation.

7 The CPA-EoS [30] combines a cubic contribution accounting for physical 8 interactions, and a chemical term from the Wertheim theory, taking into account the 9 association due to hydrogen bonding between like molecules (self-association) and 10 unlike molecules (cross-association or solvation). The activity of each bonding site is 11 assumed independent of the other bonding sites on the same molecule being steric 12 hindrance and cooperativity effects neglected. This model has already been successfully 13 employed for mixtures of water with other associating compounds [29, 31-32]. The 14 cubic and association contributions to the Helmholtz energy (A) are the following [31, 15 33, 34]:

16 
$$A^{cubic} = \frac{an}{b(\delta_2 - \delta_1)} \ln\left(\frac{1 + b\rho\delta_1}{1 + b\rho\delta_2}\right) - nRT\ln(1 - b\rho)$$
(2)

17 
$$A^{assoc} = RT \sum_{i} n_{i} \sum_{A_{i}} \left[ \ln(X_{A_{i}}) - \frac{X_{A_{i}}}{2} + \frac{1}{2} \right]$$
(3)

18

19 where *i* is a component index, *b* is the co-volume parameter, *a* is the energy parameter, 20  $\rho$  is the molar density, *n* is the number of moles, and  $X_{A_i}$  is the mole fraction of 21 component *i* not bonded at site *A*. As the Soave-Redlich-Kwong cubic term is used in

1 this work,  $\delta_l$  is set equal to 1 and  $\delta_2$  to 0. The pure-component energy parameter *a* is 2 given by a Soave-type temperature dependency, while *b* is constant:

3 
$$a(T) = a_0 \left[ 1 + c_1 \left( 1 - \sqrt{T_r} \right) \right]^2$$
 (4)

where  $a_0$  and  $c_1$  are pure component parameters and  $T_r$  is the reduced temperature. For mixtures, classical van der Waals one-fluid mixing rules are employed, where a binary interaction parameter  $k_{ij}$  is introduced on the cross-energy parameter.  $X_{A_i}$  is the key element of the association term and is related to the association strength,  $\Delta^{A_iB_j}$ , between two sites belonging to two different molecules, site *A* on molecule *i* and site *B* on molecule *j* by:

11 
$$X_{\mathcal{A}_{i}} = \frac{1}{1 + \rho \sum_{j} x_{j} \sum_{B_{j}} X_{B_{j}} \Delta^{A_{i}B_{j}}}$$
(5)

For cross-associating systems, the computationally simpler Elliot rule is adoptedfor the cross-association strength [35].

14 Experimental solubility data are used for the regression of the  $k_{ij}$  parameters with 15 the objective function (*OF*):

16 
$$OF = \sum_{i}^{NP} \left( \frac{x_i^{\exp} - x_i^{calc}}{x_i^{\exp}} \right)^2$$
(6)

where *NP* is the number of available solubility points, and the superscripts *exp* and *calc*refer to experimental and calculated values, respectively.

19 The absolute average deviations (AAD) were used to compare experimental and20 calculated results:

$$AAD\left(\%\right) = \frac{1}{NP} \sum_{i} \frac{\left|x_{i}^{\exp} - x_{i}^{calc}\right|}{x_{i}^{\exp}} \times 100$$
(7)

2

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3

#### 4 **3. Results and Discussion**

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In a previous work, the nature and number of associating groups in each of the studied solutes were established [29], following the associating schemes proposed by Huang and Radosz [36]. The one-site (1A) scheme was used for carboxylic acid groups; the two-site (2B) for alcohols and the three-site (3B) and two-site (2B) schemes for primary and secondary amines, respectively [34]. Solvents like chloroform, alkanes, 1,4-dioxane, ketones, toluene, acetonitrile and esters are considered to be non-selfassociating.

13 The pure component parameters were obtained regressing experimental vapor 14 pressure and liquid density data compiled from the DIPPR database [37], where the 15 critical properties and van der Waals volume, as well as property correlations as a 16 function of temperature, were also collected. These properties and parameters were 17 presented by Mota et al. [29]. Regression of all the CPA parameters was performed in 18 the reduced temperature range from 0.45 up to 0.85 where, in general, the DIPPR 19 correlations are in agreement with the experimental data. Only for hydroquinone and 20 paracetamol liquid density data are not available, and like that just the correlations are 21 used. The AAD's found for vapor pressure and liquid density were 2.5 and 1.8%, 22 respectively, which are good results given the complexity of the studied molecules. 23 Parameters for the various solvents are well established and were collected from the

Following a previous work where the aqueous solubilities of the same drug-like molecules were studied [29], in this work the same set of CPA parameters for describing the solubility in organic solvents are evaluated. Results of the model predictions (without fitting any parameter) and correlations (with a temperature independent binary interaction parameter  $k_{ij}$ ) are given in Tables 2 to 5.

10 All the investigated solutes are associating molecules, while some solvents such 11 as ketones, esters, cyclic ethers and toluene, although not explicitly forming solute-12 solvent hydrogen bonds, can present increased solubilities due to stronger solvating interactions. To account for this issue, Folas et al. [38] proposed to use a cross-13 14 association energy half of that of the associating component and left the cross-15 association volume as an adjustable parameter, to be fitted from equilibrium data. This 16 was initially done in this work but it was found that in most of the cases, this fitting was 17 not necessary, as the fit of a single and small  $k_{ij}$  already provided excellent results. 18 Whenever higher  $k_{ii}$  values were found for a particular solute it was also observed that 19 this also occurred for associating solvents. So to keep a higher predictive character of 20 the model, only the  $k_{ij}$  values were fitted from binary data.

The results for acetanilide are presented in Table 2. Except for the alkane solvents (n-hexane and cyclohexane), where CPA overpredicts the experimental data, the model is able to represent the data with small  $k_{ij}$ 's. In the alkane solvents the solubilities are, unexpectedly, very low, considering that the solvent with the maximum solubilities is octanol. For this same solvent the model is able to correctly estimate the

1 solubilities. In Figure 2, the solubility of acetanilide in the studied alcohols is presented 2 and it can be seen that as long as the molecular weight of the alcohol increases, the 3 solubility increases, but the model reverses the order between methanol and ethanol. 4 The results obtained by Tsivintzelis et al. [27] with the NRHB EoS in chloroform are 5 better (AAD of 1.5%). Only one parameter was used in both works, but these authors investigated a narrower temperature range. However, if the regression of  $k_{ij}$  is made in 6 7 the same temperature range as Tsivintzelis et al. [27], a higher value is found and the 8 results have almost the same accuracy. In octanol, the results found in this work are 9 better than those found by Tsivintzelis et al. [27] with the NRHB EoS.

10 Acetylsalicylic acid has the associating group -COOH and the ester group (-11 COO), which are able to cross associate with alcohol molecules. Thus, the associating 12 behaviour in the corresponding solutions is rather complicated. The correlation results 13 showed that all the interaction parameters are small and negative (Table 3), proving that 14 the interactions are stronger than expected by the model. Nevertheless the model is still 15 able to adequately correlate the data. For this solute, the solubility values are similar, 16 except in acetone where they are slightly higher. Indeed, acetone is the solvent where 17 the model gives the best estimates, both for prediction and correlation. The results in 18 alcohols are in the same accuracy range of those obtained before for aqueous solubilities 19 (AAD of 15.5%) [29], but the  $k_{ij}$  values were significantly more pronounced for the 20 water binaries.

Excluding the adipic acid/toluene system where the solubilities are very low, the correlation results found with CPA are very good, with small interaction parameters (Table 3). The results are in the same order of accuracy of those found before by Mao et al. [7] with the UNIFAC method, and not much worse than those found with the  $\lambda h$  and Apelbat correlative equations. Comparing with the results obtained for aqueous

solubilities in a previous work [29], only for the toluene system poorer results were
obtained. As presented in Figure 3, very good correlative results were found for the
systems acetylsalicylic acid/acetone and adipic acid/acetone at the expense of a small
binary interaction parameter.

5 Ascorbic acid is a complex chiral molecule containing as much oxygens as 6 carbons in its molecular structure. It has four hydroxyl groups located in different 7 environments that for modelling purposes were divided into two classes: ring and 8 aliphatic, having different associating parameters [29]. The solubilities are low in all the 9 solvents studied and probably the high melting point is a reason for that. In Table 3 it 10 can be seen that the model results are rather satisfactory. If a comparison is made with 11 the previous solutes, the interaction parameters are more pronounced, except in the case 12 of acetonitrile where the model is satisfactory even in pure prediction. A great 13 improvement is achieved after estimating a single temperature independent binary 14 interaction parameter: in average, from 87.1 to 18.1%. In Figure 4 a comparison of the 15 correlated solubilities in several solvents is presented. Among the solvents studied in 16 this work and the previous results in water [29], it can be concluded that the results here 17 are much better than for the water solubilities.

Hydroquinone is the solute showing more pronounced corrections (Table 4), except in acetic acid where the predictions are excellent. The solubility values in this solvent are the lowest, in the order of  $10^{-2}$  (mole fraction) and, like that, do not contradict some indications from the other solutes that showed larger deviations in solvents where the solubilities were very low. Excluding esters, where the correlated solubilities are overestimated, the values in the other solvents are underestimated. In Figure 5, the results for the solubility in ethyl acetate are presented. Once again, the

studied solvents in this work presented better results than the aqueous solubilities [29],
 but in this case the *k<sub>ij</sub>* were in the same order of magnitude.

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3 Among the studied compounds, ibuprofen has in general the higher solubilities 4 and also the lowest melting point. Figure 6 shows a comparison for the solubility of 5 ibuprofen in ethanol and ethyl acetate. The results for ibuprofen are presented in Table 5 6 where it can be seen that the higher interaction parameters were found for the simplest 7 alcohol solvents. In the systems ibuprofen/acetone, 4-methyl-2-pentanone or propylene 8 glycol, the interaction parameters and the results found in this work are very close to 9 those by Tsivintzelis et al. [28] with the NRHB EoS. For the other systems, the results reported by these authors are slightly better. Among the solvents studied, only in 2-10 11 propanol and cyclohexane the AAD's were higher than those obtained for aqueous 12 solubilities, but in this last case the  $k_{ii}$  (absolute value) was higher [29].

13 Good correlation results were also obtained for paracetamol in 16 solvents with 14 an average deviation of 28% (Table 2) and a maximum deviation of 65% in 15 cyclohexane where the solubilities are especially low. However, even in this solvent, the 16 improvement was significant between prediction and correlation, using a small 17 interaction parameter. It must be noted that the presence of the –ACOH group renders 18 the hydrogen-bonding behaviour of paracetamol much more complicated compared to 19 that of acetanilide, but the results are similar, what shows the importance of explicitly 20 considering association. A comparison between several prediction and correlation 21 results is presented in Figure 7, showing the importance of fitting a  $k_{ij}$  parameter. In 2-22 propanol, the results are almost similar to those obtained by Hojjati and Rohani [13] 23 with the UNIQUAC model, what is very good since this model has two adjustable 24 parameters from experimental binary data. The interaction parameters found in this 25 work for alcohols are all negative, except for propylene glycol, where those found

previously with the NRHB EoS [27] are mostly positive. So, in prediction, CPA
 considers the solute-alcohol interactions to be weaker, while the NRHB EoS considers
 them to be stronger. Generally, the results found by these authors are slightly better.

The predictions of the mole fraction solubilities of stearic acid are surprisingly good (average AAD of 61.4%) and, after regressing small binary interaction parameters, the deviations are further reduced being specially good for the alkanes, as can be seen in Table 3. The solubility results for n-heptane are presented in Figure 8.

8 Ethanol systems were studied for all the solutes and, in all of them, CPA 9 estimates were good. The maximum AAD found was 39% in paracetamol and the 10 average AAD was 22%. Except for paracetamol in propylene glycol, all the binary 11 interaction parameters for these solutes in alcohols are negative, showing that the 12 interactions are stronger than that estimated by the model.

In acetone, the results are also good with an average AAD of 21%, as well as in the esters where the deviations did not exceed 41%. However, for the esters it must be focused that the group –COO is considered non-self-associating, and its effects to increase the solvation are not explicitly taken into account by the model.

Many pharmaceutical solids and molecular crystals show polymorphism, which is the ability to exhibit more than one crystalline form, displaying different thermodynamic properties [39]. In fact, each polymorph should be regarded as a different solid material and the control of polymorphism provides a way to tune the properties of a product. As referred in the previous work [29], some of the compounds studied in this assay were reported to show polymorphic forms.

Solubility data of stearic acid polymorphs were available in n-hexane and methanol [18]. In the n-hexane system, good predictions were obtained in the case of form *B* (AAD 13.0%), while for form *C* the use of the corresponding  $k_{ij}$  value (Table 3)

was required, leading to an AAD of 49.2%. In the case of methanol, better estimates 1 2 were obtained for the solubility of form C (AAD of 19.9% with  $k_{ij} = -0.037$ ) than for form B (AAD of 46.8% with  $k_{ij} = -0.031$ ). No polymorph solubility data for the other 3 4 solutes were found, and so, only the effect of the melting properties could be evaluated. 5 For paracetamol, the results considering the melting data of form I [40] were better 6 (AAD of 26.0%). For example in methanol, the AAD is 0.64% with the melting data of 7 form I, while with the DIPPR properties or form II, the AAD's are 14.9 and 33.5%, 8 respectively. Ibuprofen is one of the most widely known chiral compounds, and also no 9 solubility data were found for the racemate and enantiomers [41]. But, analyzing in 10 terms of different thermal data, different values of binary interaction parameters were 11 obtained for the (+)-enantiomer and the racemic mixture, leading to different correlation 12 results. The use of the racemic properties gave in general better results.

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#### 14 **4.** Conclusions

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16 Given the previous success of the CPA EoS to model complex molecules in 17 aqueous systems, its performance for organic systems of complex molecules was 18 investigated in this work. The CPA EoS was applied to model the solubility of several 19 drug-like molecules, namely acetanilide, acetylsalicylic acid, adipic acid, ascorbic acid, 20 hydroquinone, ibuprofen, paracetamol and stearic acid in liquid solvents: such as 21 alcohols, alkanes, acetone, acids and esters. The complex associating behavior was 22 explicitly accounted for in the association energy and volume parameters, where the 23 corresponding parameters were estimated from vapor pressure and liquid density data. 24 Each associating group is treated individually as well as multiple group substitutions 25 were considered in the association term.

1 In the solvents studied, a rather good representation of the solubility data is 2 obtained: AAD's of 66.7 and 24.2%, respectively for model predictions and correlations 3 (using only one temperature independent binary interaction parameter per system). In 4 general the results obtained are better than those for the aqueous systems of the same 5 complex molecules. Very good results were obtained in some acetone systems where 6 the solubilities were the highest, as well as in some alcohols. In general, the binary 7 interaction parameters were small and, in the majority of the cases, negative, showing 8 that the real interactions are stronger than those estimated by the model. Often the 9 predictions are poor for very insoluble materials, but after correlating relatively small 10 and temperature independent binary interaction parameters good estimates were 11 obtained. Using thermal properties of different polymorphic forms, solubility results 12 showed quite the same quality. Even the solubility of ibuprofen, considering its 13 enantiomer or racemic properties was successfully correlated.

In general, the CPA EoS showed to be able to represent the solid-liquid equilibrium data of drug-like molecules, proving the importance of taking into account association effects. The results obtained so far in pure solvents suggest further work concerning mixed solvent systems, as well as supercritical solvents.

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10	Nomenclature
11	a = energy parameter
12	$a_0$ = parameter in the CPA EoS cubic term (Pa.m <sup>6</sup> /mol <sup>2</sup> )
13	A = Helmholtz energy (J)
14	b = co-volume parameter (m3/mol)
15	$c_1$ = parameter in the CPA EoS cubic term
16	$k_{ij}$ = binary interaction parameter
17	n = number of moles
18	NP = number of data points
19	R = gas constant (8.314  J/(mol.K))
20	T = absolute temperature (K)
21	x = mole fraction

- $X_{A_i}$  = mole fraction of component *i* not-bonded at site A
- 3 Greek Symbols
- $\delta$  = specific parameters in each cubic equation
- $\beta$  = association volume
- $\beta_{ij}$  = solvation parameter
- $\Delta^{A_i B_j}$  = association strength between site A on molecule *i* and site B on molecule *j*
- $\Delta C_p$  = difference between the heat capacity of the solute pure liquid and solid (J/mol.K)
- $\Delta_{fus}H =$  fusion enthalpy (J/mol)
- $\varepsilon$  = association energy (J/mol)
- $\rho = \text{molar density (mol/m}^3)$
- $\varphi$  = fugacity coefficient
- 14 Subscripts
- $\theta$  = pure component
- c = critical
- i, j, k = component index
- m = melting
- r = reduced
- $20 \quad s = \text{solute}$

tr = transition
Superscripts
<i>assoc</i> = association term
<i>calc</i> = calculated
<i>cubic</i> = cubic term
exp = experimental
List of Abbreviations
AAD =absolute average deviation (%)
<i>CPA</i> = cubic-plus-association
EoS = equation of state
<i>NRHB</i> = Non-Random Hydrogen Bonding
<i>OF</i> = objective function

V

#### 1 References

- 2
- 3 [1] P. Kolář, J. W. Shen, A. Tsuboi, T. Ishikawa, Fluid Phase Equilib. 194 (2002) 771-

4 782.

- 5 [2] F. L. Mota, A. P. Carneiro, A. J. Queimada, S. P. Pinho, E. A. Macedo, Eur. J.
- 6 Pharm. Sci. 37 (2009) 499-507.
- 7 [3] S. P. Pinho, E. A. Macedo, Solubility in Food, Pharmaceuticals, and Cosmetic
- 8 Industries, Royal Society of Chemistry, Durban, South Africa, 2003.
- 9 [4] G. D. Maia, M. Giulietti, J. Chem. Eng. Data 53 (2008) 256-258.
- 10 [5] G. L. Perlovich, A. Bauer-Brandl, Pharm. Res. 20 (2003) 471-478.
- 11 [6] L. H. Fan, P. S. Ma, Z. L. Xiang, Chin. J. Chem. Eng. 15 (2007) 110-114.
- 12 [7] Z. B. Mao, X. B. Sun, X. H. Luan, Y. Wang, G. J. Liu, Chin. J. Chem. Eng. 17
- 13 (2009) 473-477.
- 14 [8] D. W. Wei, W. J. Cao, J. Chem. Eng. Data 54 (2009) 152-153.
- 15 [9] X. N. Li, Q. X. Yin, W. Chen, J. K. Wang, J. Chem. Eng. Data 51 (2006) 127-129.
- 16 [10] A. Jouyban, O. Azarmir, S. Mirzaei, D. Hassanzadeh, T. Ghafourian, W. E. Acree,
- 17 A. Nokhodchi, Chem. Pharm. Bull. (Tokyo) 56 (2008) 602-606.
- 18 [11] C. M. Wassvik, A. G. Holmen, C. A. S. Bergstrom, I. Zamora, P. Artursson, Eur.
- 19 J. Pharm. Sci. 29 (2006) 294-305.
- 20 [12] J. M. Prausnitz, R. N. Lichtenthaler, E. G. Azevedo, Molecular Thermodynamics
- 21 of Fluid-phase Equilibria, Third Prentice Hall PTR, New Jersey, 1999.
- 22 [13] H. Hojjati, S. Rohani, Org. Proc. Res. Dev. 10 (2006) 1110-1118.
- 23 [14] B. C. Hancock, P. York, R. C. Rowe, Int. J. Pharm. 148 (1997) 1-21.
- 24 [15] P. Bustamante, M. A. Pena, J. Barra, Int. J. Pharm. 194 (2000) 117-124.

- 1 [16] S. Romero, A. Reillo, B. Escalera, P. Bustamante, Chem. Pharm. Bull. (Tokyo) 44
- 2 (1996) 1061-1064.
- 3 [17] U. Domańska, A. Pobudkowska, A. Pelczarska, P. Gierycz, J. Phys. Chem. B 113
- 4 (2009) 8941-8947.
- 5 [18] M. Mirmehrabi, S. Rohani, Can. J. Chem. Eng. 82 (2004) 335-342.
- 6 [19] B. Calvo, E. A. Cepeda, J. Chem. Eng. Data 53 (2008) 628-633.
- 7 [20] I. Hahnenkamp, G. Graubner, J. Gmehling, Int. J. Pharm. 388 (2010) 73-81.
- 8 [21] J. Abildskov, R. Gani, P. Rasmussen, J. P. O'Connell, Fluid Phase Equilib. 181
- 9 (2001) 163-186.
- 10 [22] C. C. Chen, P. A. Crafts, Ind. Eng. Chem. Res. 45 (2006) 4816-4824.
- 11 [23] C. C. Chen, Y. H. Song, Ind. Eng. Chem. Res. 43 (2004) 8354-8362.
- 12 [24] P. B. Kokitkar, E. Plocharczyk, Org. Proc. Res. Dev. 12 (2008) 249-256.
- 13 [25] S. Gracin, T. Brinck, A. C. Rasmuson, Ind. Eng. Chem. Res. 41 (2002) 5114-5124.
- 14 [26] F. Ruether, G. Sadowski, J. Pharm. Sci. 98 (2009) 4205-4215.
- 15 [27] I. Tsivintzelis, I. G. Economou, G. M. Kontogeorgis, AlChE J. 55 (2009) 756-770.
- 16 [28] I. Tsivintzelis, I. G. Economou, G. M. Kontogeorgis, J. Phys. Chem. B 113 (2009)
- 17 6446-6458.
- [29] F. L. Mota, A. J. Queimada, S. P. Pinho, E. A. Macedo, Fluid Phase Equilib. 298
  (2010) 75-82.
- 20 [30] G. M. Kontogeorgis, E. C. Voutsas, I. V. Yakoumis, D. P. Tassios, Ind. Eng.
- 21 Chem. Res. 35 (1996) 4310-4318.
- 22 [31] F. L. Mota, A. J. Queimada, S. P. Pinho, E. A. Macedo, Ind. Eng. Chem. Res. 47
- 23 (2008) 5182-5189.
- 24 [32] A. J. Queimada, F. L. Mota, S. P. Pinho, E. A. Macedo, J. Phys. Chem. B 113
- 25 (2009) 3469-3476.

- 1 [33] G. M. Kontogeorgis, M. L. Michelsen, G. K. Folas, S. Derawi, N. von Solms, E. H.
- 2 Stenby, Ind. Eng. Chem. Res. 45 (2006) 4869-4878.
- 3 [34] G. M. Kontogeorgis, M. L. Michelsen, G. K. Folas, S. Derawi, N. von Solms, E. H.
- 4 Stenby, Ind. Eng. Chem. Res. 45 (2006) 4855-4868.
- 5 [35] E. C. Voutsas, I. V. Yakoumis, D. P. Tassios, Fluid Phase Equilib. 158 (1999)
- 6 151-163.
- 7 [36] S. H. Huang, M. Radosz, Ind. Eng. Chem. Res. 29 (1990) 2284-2294.
- 8 [37] DIPPR Tables, DIPPR 801 Thermophysical Properties Database, Brigham Young
- 9 University, Provo, UT, 1998.
- 10 [38] G. K. Folas, G. M. Kontogeorgis, M. L. Michelsen, E. H. Stenby, Ind. Eng. Chem.
- 11 Res. 45 (2006) 1527-1538.
- 12 [39] H. G. Brittain, Polymorphism in Pharmaceutical Solids, Informa Health Care, New
- 13 York, 1999.
- 14 [40] M. Sacchetti, J. Therm. Anal. Calorim. 63 (2000) 345-350.
- 15 [41] G. L. Perlovich, S. V. Kurkov, L. K. R. Hansen, A. Bauer-Brandl, J. Pharm. Sci.
- 16 93 (2004) 654-666.
- 17 [42] A. Seidell, J. Am. Chem. Soc. 29 (1907) 1091-1095.
- [43] G. L. Perlovich, T. V. Volkova, A. Bauer-Brandl, J. Pharm. Sci. 95 (2006) 21582169.
- 20 [44] P. Bustamante, S. Romero, A. Peña, B. Escalera, A. Reillo, J. Pharm. Sci. 87
- 21 (1998) 1590-1596.
- 22 [45] Y. Baena, J. A. Pinzón, H. J. Barbosa, F. Martínez, Phys. Chem. Liq. 42 (2004)
- 23 603**-**613.
- 24 [46] R. A. Granberg, A. C. Rasmuson, J. Chem. Eng. Data 44 (1999) 1391-1395.
- 25 [47] J. A. Jiménez, F. Martínez, J. Braz. Chem. Soc. 17 (2006) 125-134.

- 1 [48] H. Hojjati, S. Rohani, Org. Proc. Res. Dev. 10 (2006) 1101-1109.
- 2 [49] J. A. Jiménez, F. Martínez, J. Solution Chem. 35 (2006) 335-352.
- 3 [50] R. A. Granberg, A. C. Rasmuson, J. Chem. Eng. Data 45 (2000) 478-483.
- 4 [51] C. M. McLoughlin, W. A. M. McMinn, T. R. A. Magee, Powder Technol. 134
- 5 (2003) 40-51.
- 6 [52] Y. J. Yi, D. Hatziavramidis, A. S. Myerson, M. Waldo, V. G. Beylin, J. Mustakis,
- 7 Ind. Eng. Chem. Res. 44 (2005) 5427-5433.
- 8 [53] A. Shalmashi, A. Eliassi, J. Chem. Eng. Data 53 (2008) 1332-1334.
- 9 [54] Y. J. Manrique, D. P. Pacheco, F. Martínez, J. Solution Chem. 37 (2008) 165-181.
- 10 [55] D. P. Pacheco, Y. J. Manrique, F. Martinez, Fluid Phase Equilib. 262 (2007) 23-
- 11 31.
- 12 [56] L. C. Garzón, F. Martínez, J. Solution Chem. 33 (2004) 1379-1395.

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Compound	<i>T<sub>m</sub></i> (K)	∠ <sub>fus</sub> H (kJ/mol)	∠C <sub>p</sub> (J/mol.K)	a <sub>0</sub> (Pa m <sup>6</sup> /mol <sup>2</sup> )	c <sub>1</sub>	b x 10 <sup>5</sup> (m <sup>3</sup> /mol)	Group	E (kJ/mol)	β
Acetanilide [29]	388	21.65	1.92	4.37	1.17	12.25	NH	3.74	1.00 x10 <sup>-1</sup>
Acetylsalicylic acid [29]	408	25.60	26.55	4.62	1.48	13.56	СООН	11.4	1.68 x10 <sup>-4</sup>
Adipic acid [29]	426	34.85	108.07	4.80	1.49	12.48	СООН	18.5	3.45 x10 <sup>-4</sup>
Accorbic acid [20]	165	20.20	<u> </u>	2 70	2.06	11.04	OH ring	14.9	9.08 x10 <sup>-3</sup>
Ascolute actu [29]	403	29.20	81.40	5.79	2.90	11.94	OH aliphatic	14.7	4.10 x10 <sup>-5</sup>
Hydroquinone [29]	445	27.11	55.19	2.20	1.27	10.37	ОН	19.2	2.38 x10 <sup>-2</sup>
Ibuprofen [29]	349	25.61	149.74	7.33	1.37	20.47	СООН	1.10	9.61 x10 <sup>-4</sup>
Paracetamol [29]	441	27.70	32.14	3.45	1.76	15.96	NH	6.45	5.48 x10 <sup>-2</sup>
Stearic acid [29]	343	61.21	116.84	12.2	1.58	33.47	ОН	17.9	2.06 x10 <sup>-2</sup>
methanol [33]				0.405	0.431	3.09	ОН	2.46	1.61 x10 <sup>-2</sup>
ethanol [33]				0.867	0.737	4.91	ОН	2.15	8.00 x10 <sup>-3</sup>
1-propanol [33]				1.19	0.917	6.41	OH	2.10	8.1 x10 <sup>-3</sup>
2-propanol [33]				1.06	0.947	6.41	OH	2.10	9.1 x10 <sup>-3</sup>
1-butanol [33]				1.57	0.978	7.97	OH	2.10	8.2 x10 <sup>-3</sup>
1-octanol [33]				4.16	1.15	14.9	OH	2.68	1.40 x10 <sup>-4</sup>
propylene glycol [33]				1.38	0.937	6.75	OH	1.74	1.90 x10 <sup>-2</sup>
acetic acid [33]				0.912	0.464	4.69	COOH	4.03	4.5 x10 <sup>-3</sup>
n-hexane [38]				2.37	0.831	10.8			
n-heptane [38]				2.92	0.914	12.5			
cyclohexane*				2.11	0.771	9.09			
acetone*				1.39	0.788	6.14			
4-methyl-2-pentanone*				2.41	0.856	8.72			
ethyl acetate*				1.87	0.957	8.31			
butyl acetate*				2.92	1.03	11.7			
isopropyl myristate*				10.5	1.57	32.1			
1,4-dioxane*				1.85	0.825	7.39			
chloroform*				1.50	0.782	6.64			
toluene*				2.34	0.804	9.24			
acetonitrile*				1.28	0.605	4.68			
tetrahydrofuran*				1.56	0.771	6.80			
trichloroethylene*				1.85	0.771	7.60			

### 1 **Table 1. Pure component properties and CPA parameters.**

2 \*Obtained in this work.

### 1 Table 2. CPA Modelling Results for Acetanilide and Paracetamol, and Respective

### 2 **Binary Interaction Parameter.**

3

		_	Prediction	Correla	ation
Compound	Solvent	Temperature (K)	AAD (%)	k <sub>ij</sub>	AAD (%)
	methanol [42]	273.15 - 333.15	73.1	-0.0728	53.0
	ethanol [42]	273.15 - 333.15	90.0	-0.0145	26.5
	1-octanol [43]	293.15 - 315.15	72.1	-0.0472	2.01
	1,4-dioxane [44]	273.15 - 313.15	35.3	-0.00124	32.7
acetanilide	isopropyl myristate [45]	283.15 - 333.15	44.4	-0.0100	41.0
	chloroform [42]	293.15 - 333.15	29.6	-0.00244	26.1
	n-hexane [43]	293.15 - 315.15	49026	0.235	44.9
	cyclohexane [43]	298.15 - 313.15	10429	0.180	42.1
			57.4 <sup>a</sup>		24.2
	methanol [46]	268.15 - 298.15	75.3	-0.0647	14.9
	ethanol [46, 47]	268.15 - 313.15	60.9	-0.0490	39.2
	1-propanol [46]	268.15 - 298.15	35.8	-0.0193	11.2
	2-propanol [46, 48]	268.15 - 313.15	65.3	-0.0332	14.9
	1-butanol [46]	268.15 - 298.15	55.6	-0.0207	11.7
	1-octanol [43, 45]	293.15 - 313.15	37.8		
	propylene glycol [47, 49]	293.15 - 313.15	56.8	0.00830	30.4
	toluene [46, 50]	273.15 - 303.15	34.9		
paracetamol	acetone [46, 50]	268.15 - 303.15	99.7	-0.181	29.1
	1,4-dioxane [44]	293.15 - 313.15	98.6	-0.0700	51.4
	ethyl acetate [46]	268.15 - 298.15	95.7	-0.0722	34.0
	isopropyl myristate [45]	298.15 - 313.15	59.0	-0.0428	22.9
	acetonitrile [46]	268.15 - 298.15	99.6	-0.0955	39.0
	chloroform [45]	298.15 - 313.15	42.7	0.0112	5.87
	n-hexane [43]	298.15 - 315.15	6799	0.174	15.1
	cyclohexane [45]	298.15 - 313.15	1297	0.0748	64.8
			65.5 <sup>a</sup>		27.5

4 <sup>a</sup>Without outliers: AAD > 150%.

### 1 Table 3. CPA Modelling Results for the Acids, and Respective Binary Interaction

### 2 **Parameter.**

Compound	Solvent	Temperature	Prediction	Correlation	
		<b>(K)</b>	AAD (%)	k <sub>ij</sub>	AAD (%)
	methanol [51]	293.15 - 333.15	91.8	-0.0903	23.0
	ethanol [4]	276.30 - 336.60	87.2	-0.0683	21.8
acetylsalicylic	2-propanol [4]	291.80 - 330.20	70.1	-0.0319	24.5
acid	propylene glycol [4]	295.70 - 333.90	50.9	-0.0197	31.4
	acetone [4]	281.90 - 326.30	45.3	-0.0246	8.00
			69.0		21.7
	ethanol [7, 52]	299.95 - 340.95	84.1	-0.0588	12.2
	n-butanol [7]	298.85 - 358.15	87.3	-0.0684	9.92
	chloroform [7,8]	298.15 - 331.55	65.2	0.0137	18.9
adipic acid	acetic acid [6]	297.93 - 347.65	64.5	-0.0361	19.3
	toluene [8]	298.15 - 333.15	1575	0.0652	85.6
	acetone [7,8]	288.05 - 325.85	79.6	-0.0417	6.40
			76.2 <sup>a</sup>		25.4
	methanol [53]	293.15 - 323.15	99.9	-0.167	19.3
	ethanol [53]	293.15 - 323.15	98.9	-0.106	6.50
	2-propanol [53]	293.15 - 323.15	71.8	-0.0225	17.3
	ethyl acetate [53]	293.15 - 323.15	98.9	-0.110	19.9
ascorbic acid	tetrahydrofuran [53]	293.15 - 323.15	99.1	-0.113	11.9
	acetone [53]	293.15 - 323.15	96.5	-0.0781	21.4
	acetonitrile [53]	293.15 - 318.15	44.4	0.0126	30.1
			87.1		18.1
	ethanol [19]	391.45 - 323.65	79.0	-0.0166	29.1
	2-propanol [19]	292.35 - 321.95	97.5	-0.0411	41.8
	acetone [19]	291.95 - 322.55	50.1		
stearic acid	tricloroethylene [19]	292.75 - 323.25	67.2	-0.0183	21.1
	n-hexane [19]	293.75 - 323.55	27.8	0.00247	10.9
	n-heptane [19]	293.45 - 324.85	46.6	0.00723	9.74
			61.4		22.5

3 <sup>a</sup>Without outliers: AAD > 150%.

### 1 Table 4. CPA Modelling Results for Hydroquinone, and Respective Binary

- 2 Interaction Parameter.
- 3

Compound	Solvent	Temperature	Prediction	Correlation	
Compound		( <b>K</b> )	AAD (%)	k <sub>ij</sub>	AAD (%)
	methanol [9]	281.65 - 343.40	86.5	-0.164	6.27
	ethanol [9]	276.65 - 342.15	87.2	-0.145	22.6
	2-propanol [9]	279.45 - 342.55	85.5	-0.131	8.63
hydroquinone	acetic acid [9]	289.45 - 341.25	8.32		
	ethyl acetate [9]	278.70 - 345.10	98.3	-0.196	23.0
	butyl acetate [9]	279.55 - 344.70	98.9	-0.231	22.2
			77.5		16.5

4

### 1 Table 5. CPA Modelling Results for Ibuprofen, and Respective Binary Interaction

#### 2 **Parameter.**

3

Compound	Solvent	Temperature	Prediction	Correlation	
		( <b>K</b> )	AAD (%)	k <sub>ij</sub>	AAD (%)
	methanol [25]	283.15 - 308.15	97.8	-0.189	18.1
	ethanol [25,54,55]	283.15 - 313.15	91.2	-0.121	15.2
	2-propanol [25]	283.15 - 308.15	91.9	-0.0932	25.5
	1-octanol [25]	298.15 - 313.15	66.6	-0.0585	18.4
	propylene glycol [55]	293.15 - 313.15	64.7	-0.0236	17.5
	toluene [25]	283.15 - 308.15	31.7	0.0151	14.8
ibuprofen	acetone [25]	283.15 - 308.15	14.0	0.00229	12.7
	4-methyl-2-pentanone [25]	283.15 - 308.15	17.8	0.00821	10.6
	chloroform [25, 56]	283.15 - 313.15	28.7		
-	ethyl acetate [25]	283.15 - 308.15	21.6	0.0116	14.3
	isopropyl myristate [25]	298.15 - 313.15	26.1	-0.00616	10.9
	cyclohexane [25]	298.15 - 313.15	87.7	0.0199	37.6
			53.3		17.8



## 1 Figure Captions:

2	
3	Figure 1. Molecular structure of: (a) acetanilide, (b) acetylsalicylic acid, (c) adipic acid,
4	(d) ascorbic acid, (e) hydroquinone, (f) ibuprofen (g) stearic acid and (h) paracetamol.
5	
6	<b>Figure 2.</b> Solubility of acetanilide in methanol [42] (\$), ethanol [42] (•) and 1-octanol
7	[43] ( <b>•</b> ), and CPA correlations (—, methanol and 1-octanol;, ethanol).
8	
9	<b>Figure 3.</b> Solubility of acetylsalicylic acid [4] (●) and adipic acid [7] (■) in acetone,
10	and CPA correlation results.
11	
12	Figure 4. Summarized results for ascorbic acid solubility in several solvents:
13	experimental data [53] versus CPA correlations: ethanol (•), methanol (o), 2-propanol
14	( $\blacklozenge$ ), acetone ( $\diamondsuit$ ), acetonitrile ( $\blacksquare$ ), ethyl acetate ( $\Box$ ), and tetrahydrofuran ( $\blacktriangle$ ).
15	
16	Figure 5. Solubilities of hydroquinone as a function of temperature in ethyl acetate [9],
17	and CPA modelling results: correlation () and prediction ().
18	
19	Figure 6. Solubilities of ibuprofen as a function of temperature in (a) ethanol [25] and
20	(b) ethyl acetate [25], and CPA modelling results: correlation () and prediction ().
21	
22	Figure 7. Summarized results for paracetamol in several solvents: experimental data
23	versus CPA (a) predictions and (b) correlations: ethanol [46, 49] (•), methanol [46] (o),
24	2-propanol [46, 48] (♦), acetone [46, 50] (◊), acetonitrile [46] (■), ethyl acetate [46] (□),
25	propylene glycol [47, 49] ( $\Delta$ ), 1-propanol [46] ( $\oplus$ ), and 1-butanol [46] (x).
26	
27	Figure 8. Solubilities of stearic acid as a function of temperature in n-heptane [19] and
28	CPA results: correlation (—) and prediction ().
29	

#### ACCE CR 2 D

#### Figure 1: 1

2

H<sub>3</sub>C











(c)





(f)

OH

NH

(h)

(e)



4

1 **Figure 2:** 



#### ACCEP **USCRIP**1 ED

#### Figure 3: 1



1 **Figure 4:** 



**Figure 5:** 











## 1 **Figure 8:**



#### ACCEPTED **ANUSCRIP** W

#### Highlight 1

2 •	The CPA EoS is applied for drug-like solubility calculations in organic solvents.
4 • 5	Only a single, small and temperature independent $k_{ij}$ parameter is required.
6 • 7 8	Each associating group as well as multiple group substitutions are explicitly considered.
9 • 10 11 12	Accurate correlations are obtained (global AAD of 24 %)