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# Classification of Multisensor and Multiresolution Remote Sensing Images through Hierarchical Markov Random Fields

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**Abstract**—This letter proposes two methods for the supervised classification of multisensor optical and SAR images with possibly different spatial resolutions. Both methods are formulated within a unique framework based on hierarchical Markov random fields. Distinct quad-trees associated with the individual information sources are defined to jointly address multisensor, multiresolution, and possibly multifrequency fusion, and are integrated with finite mixture models and the marginal posterior mode criterion. Experimental validation is conducted with Pléiades, COSMO-SkyMed, RADARSAT-2, and GeoEye-1 data.

**Index Terms**—Multisensor, multiresolution, multifrequency fusion, quad-tree, hierarchical Markov random field (MRF), marginal posterior mode (MPM), finite mixture models.

## I. INTRODUCTION

**G**IVEN the current amount and variety of data from high or very-high resolution (HR/VHR) satellite missions, a major challenge is to develop classifiers that can benefit from multiresolution, multisensor, and multifrequency input imagery [1]–[3]. The use of multiband and multiresolution data has been shown to favor accuracy and spatial precision of the classification maps [2]. Furthermore, the use of multisensor data generally allows complementary properties, such as those of SAR and optical imagery, to be exploited [1]. Hence, there is a definite need for classification methods that can fuse images taken on the same area both by different sensors and at different resolutions. One way to address multisensor data classification is to compute joint class-conditional distributions given the marginal probability density function (PDF) of the data collected by each sensor. Meta-Gaussian [4], copula [5], or non-parametric models [6] can be used for this purpose. However, finding such joint statistical models is generally complex, time-demanding, and possibly prone to over-fitting.

In this paper, we build on the theory of hierarchical Markov random fields (MRFs) [7] to address the challenging problem of the supervised classification of data that are both multiresolution and multisensor (and possibly multifrequency). The rationale is to benefit from the fusion capabilities of

hierarchical MRFs and avoid the computation of joint statistics of multisensor data. Inference is accomplished by extending the approach that was previously developed in [8] for multitemporal fusion and is based on the marginal posterior mode (MPM) criterion. PDF estimation is addressed using mixtures of Gaussian and generalized Gamma distributions.

Two methods are proposed in this framework. In the case of the first one, the image acquired by each sensor is associated with a separate quad-tree according to its resolution. In regard to the second method, the focus is on the specific case of the fusion of multifrequency X-band COSMO-SkyMed (CSK) and C-band RADARSAT-2 (RS2) SAR data together with optical visible and near-infrared (VNIR) Pléiades data. Distinct quad-trees are used again, but here, optical and SAR data are both included in each quad-tree to benefit from the finest resolution available from each sensor. While the first technique addresses the fusion of data from generally arbitrary SAR and optical sensors, the second method focuses on the synergy among three specific and topical satellite data sources. The main novel contribution of the proposed framework is the formalization of the joint problem of multisensor, multiresolution, and possibly multifrequency fusion in terms of a multiple quad-tree topology and of hierarchical MRFs.

The letter is organized as follows. Section II-A describes the proposed framework and the quad-tree structures of the two methods. Sections II-B and II-C discuss the MPM inference and PDF estimation issues. Experimental results are presented in Section III and conclusions are drawn in Section IV.

## II. PROPOSED MULTISENSOR HIERARCHICAL APPROACH

### A. Overview of the proposed methodology

To address multisensor and possibly multifrequency fusion, the proposed framework extends and adapts the approach developed in [8] for multitemporal fusion and based on multiple quad-trees in cascade and on hierarchical MRFs (Fig. 1). This hierarchical formulation also allows multiresolution data to be naturally incorporated. In particular, a pair of quad-trees in cascade is constructed using the input multisource imagery. Given a training set for  $M$  thematic classes, inference can be efficiently formulated on this topology using MPM (see Section II-B), while the statistics of the data from each sensor are modeled using finite mixtures and the stochastic expectation-maximization (SEM) algorithm [9] (see Section II-C). In this framework, two methods, which differ in how data are incorporated in the quad-trees, are defined.

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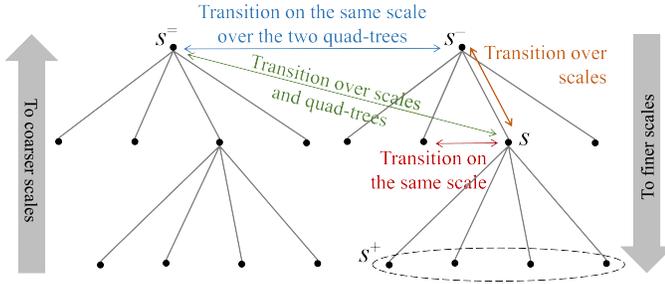


Fig. 1. Multisensor hierarchical structure.

1) *Quad-trees of the first proposed method:* Let an optical and a SAR image, acquired at the same time over the same area, be given. In the first method, these images are included in the finest-scale levels (the leaves) of two quad-trees. Coarser-scale levels of each quad-tree are filled in using wavelet transforms of the finest-scale level [10]. The roots of the quad-trees are assumed to have the same spatial resolution. Hence, there generally are different numbers of levels in the quad-trees, from the roots at a common resolution to the input resolutions of the optical and SAR data. The quad-tree topology also implies that the resolutions of the two input images are in a power-of-2 relation. With current HR satellite sensors, this condition is easily met up to minor resampling.

2) *Quad-trees of the second proposed method:* The second method is aimed at classifying multisensor, multifrequency (X-band radar, C-band radar, VNIR optical), and multiresolution data from CSK, RS2, and Pléiades. These prominent sensors support multiple resolutions, up to 0.5 m for Pléiades and approximately 1 m for CSK and 1-2 m for RS2. Given input CSK, RS2, and Pléiades images acquired on the same area at the same time, case-specific quad-trees are constructed to classify at the finest of the input resolutions. Each SAR image is inserted in a separate quad-tree according to its own resolution. These resolutions are expected to be coarser than the finest resolution achieved using Pléiades. Therefore, the input Pléiades image is embedded in the finest-resolution levels of both quad-trees. Empty levels are filled in using wavelet transforms of the Pléiades data. The comment on the power-of-2 relation among the input resolutions holds again.

## B. Multisensor hierarchical formulation of MPM

Owing to the quad-tree structure, a hierarchical MRF model, which consists of a series of random fields linked, at various scales, by suitable transition relations, can be defined (Fig. 1). The formulation of MPM proposed in [8] for multitemporal classification is extended here to multisensor fusion. MPM is used instead of the maximum *a-posteriori* (MAP) rule because MAP formulations on quad-trees, although they are feasible [11], [12], are affected by underflow and penalize errors regardless of the scale at which they occur – an undesired behavior for multiscale classification [8], [12], [13].

Collecting all the (optical, SAR, and wavelet) features of both quad-trees in the vector  $y$ , the posterior marginal  $p(x_s|y)$  of the label  $x_s$  of each site  $s$  in the second quad-tree is expressed, under suitable conditional independence assumptions, as a function of the posterior marginals  $p(x_{s^-}|y)$

and  $p(x_s=y)$  of the parent node  $s^-$  in the same quad-tree and the parent node  $s^-$  in the first quad-tree, i.e. [8]:

$$p(x_s|y) = \sum_{x_{s^-}, x_s=} \frac{p(x_s, x_{s^-}, x_s=y_{d(s)})p(x_s=y)p(x_s=y)}{\sum_{x_s} p(x_s, x_{s^-}, x_s=y_{d(s)})}, \quad (1)$$

where it is proven in [8] that, under appropriate assumptions:

$$p(x_s, x_{s^-}, x_s=y_{d(s)})p(x_s) = p(x_s|x_{s^-}, x_s=y_{d(s)})p(x_s=y_{d(s)}), \quad (2)$$

and where  $y_{d(s)}$  collects the features of all descendants of  $s$ ,  $p(x_s)$  is the prior probability,  $p(x_s|x_{s^-}, x_s=y_{d(s)})$  is the parent-child transition probability,  $p(x_{s^-}|x_s=y_{d(s)})$  is the transition probability between sites at the same scale, and  $p(x_s|y_{d(s)})$  is the partial posterior marginal. While these quantities are made available, (1) and (2) recursively calculate  $p(x_s|y)$  on each site  $s$  of the second quad-tree. This is obtained using one bottom-up and two top-down recursive passes, which are described in the next subsections. Note that, by (1), the quad-trees are ordered. In the first proposed method, SAR and optical data are related to the first and second quad-trees, respectively. In the second method, two options are possible, i.e., CSK in the first quad-tree and RS2 in the second one or vice versa.

1) *Initialization on the first quad-tree:* First, classification is performed only on the first quad-tree using a traditional MPM on a single quad-tree [11]. As in [8] (to which we refer for details), the prior distribution at the root is modeled using a Potts MRF to favor spatial consistency. After the initialization stage,  $p(x_f|y)$  is known for each site  $f$  of the first quad-tree and  $p(x_f|y_{d(f)})$  is derived as a by-product.

2) *First top-down pass on the second quad-tree:* The first top-down pass proceeds from the root to the leaves of the second quad-tree to recursively compute  $p(x_s)$ . As in [8], this prior is initialized in each site  $s$  of the root of the second quad-tree as  $p(x_s) = p(x_f|y_{d(f)})$ , where  $f$  is the site of the root of the first quad-tree with the same location as  $s$ . Then, the recursion proceeds along the other levels down to the leaves:

$$p(x_s) = \sum_{x_{s^-}} p(x_s|x_{s^-})p(x_{s^-}). \quad (3)$$

This favors the same parent-child labeling and characterizes the statistical interactions between consecutive levels. We model the parent-child transition probability  $p(x_s|x_{s^-})$  through the parametric form in [14]. As a result of this top-down pass,  $p(x_s)$  is derived on each site  $s$  of the second quad-tree.

3) *Bottom-up pass on the second quad-tree:* A bottom-up recursion is performed to compute  $p(x_s, x_{s^-}, x_s=y_{d(s)})$  starting from the leaves of the second quad-tree and using (2) until the root is reached. In addition to  $p(x_s)$ , three sets of probabilities are required: (i) the transition probabilities at the same scale  $p(x_{s^-}|x_s=y_{d(s)})$ ; (ii) the parent-child transition probabilities  $p(x_s|x_{s^-}, x_s=y_{d(s)})$ ; and (iii) the partial posterior marginals  $p(x_s|y_{d(s)})$ . Details of the modeling of (i) and (ii), which is performed parametrically, can be found in [8]. Concerning (iii), it has been proved that [11]:

$$p(x_s|y_{d(s)}) \propto p(y_s|x_s)p(x_s) \prod_{u \in \mathcal{S}^+} \sum_{x_u} \frac{p(x_u|y_{d(u)})p(x_u|x_s)}{p(x_u)} \quad (4)$$

where  $s^+$  and  $y_s$  are the set of four children and the feature vector of site  $s$ , respectively. First,  $p(x_s|y_{d(s)})$  is initialized on the leaves of the second quad-tree with  $p(x_s|y_{d(s)}) = p(x_s|y_s) \propto p(y_s|x_s)p(x_s)$ . Then,  $p(x_s|y_{d(s)})$  is recursively estimated with (4) up to the root. This recursion involves the pixelwise class-conditional PDF  $p(y_s|x_s)$  (see Section II-C). After the bottom-up pass,  $p(x_s, x_{s^-}, x_{s^+}|y_{d(s)})$  is computed on each site  $s$  of the second quad-tree.

4) *Second top-down pass on the second quad-tree and output labeling*: First, the posterior marginal is initialized at the root of the second quad-tree as  $p(x_s|y) = p(x_s|y_{d(s)})$ . Then, given the quantities computed by the previous stages,  $p(x_s|y)$  is derived on all sites  $s$  of all other levels of the second quad-tree in a top-down pass using the recursion (1). Then, in principle, the class label  $x_s$  that maximizes  $p(x_s|y)$  over the set of  $M$  classes could be assigned to  $s$  directly. This approach is often avoided in the literature of hierarchical MRFs because of its computational burden and of possible blocky artifacts [5], [11]. As an alternate approach, the case-specific formulation of the modified Metropolis dynamics algorithm [15] that was combined in [8] with MPM is extended here as well. The labeling result on the leaves of the second quad-tree represents the output classification map.

### C. PDF estimation through finite mixtures

For each class  $m \in \{1, 2, \dots, M\}$  and each level  $n$  between the leaves and the root of each quad-tree  $q \in \{1, 2\}$ , we use a finite-mixture model for the pixelwise PDF  $p(y_s|x_s = m)$ . This choice is explained by the flexibility of finite mixtures in characterizing heterogeneous statistics such as those of HR imagery [8]. If the data at level  $n$  of quad-tree  $q$  are optical, then a multivariate Gaussian mixture is used [6]. The same model is used for wavelet transforms of optical data, because of the linearity of the wavelets. If the data at level  $n$  of quad-tree  $q$  are SAR, a mixture of generalized Gamma distributions is used. The generalized Gamma model has been found accurate for HR SAR [16], [17]; here, it is also extended as an empirical model for wavelet transforms of SAR data.

The mixture parameters are estimated using SEM, which is an iterative stochastic algorithm developed for problems characterized by data incompleteness. SEM generates a random sequence of estimates, which does not converge almost surely but, under suitable assumptions, forms an ergodic homogeneous Markov chain converging to a unique stationary distribution, which is expected to concentrate around the global log-likelihood maxima [9]. Hence, initialization is not critical and is usually performed randomly with uniform distribution [9], [18]. The number of mixture components is also automatically estimated using the specific SEM formulation in [19]. For each scale  $n$  of each quad-tree  $q$ , SEM is separately applied to the training samples of each class  $m$ . For generalized Gamma mixtures, it is also combined with the method of log-cumulants (details can be found in [18], [19]).

## III. EXPERIMENTAL RESULTS

### A. Results of the first proposed method

An HR dataset collected in 2010 over Port-au-Prince, Haiti, and composed of an HH-polarized single-look CSK stripmap

image with 2.5-m pixel spacing ( $325 \times 400$  pixels; Fig. 2(a)) and of a GeoEye-1 RGB image resampled at 2.5-m resolution (Fig. 2(b)), was used to experimentally validate the first proposed method. 2D Daubechies wavelets of order 10 were used. Five land cover classes were considered (see Table I and Fig. 2(c)). We compared the result of the proposed method (Fig. 2(i)) with those of: (i) the single-sensor multiscale classification of the image of each sensor, obtained by applying the original MPM to a single quad-tree [11] with Gaussian or generalized Gamma mixtures for the class-conditional PDFs of optical and SAR data, respectively (Figs. 2(d) and (e)); (ii) the multisensor multiresolution method in [5], in which a hierarchical MRF on a single quad-tree is used and multisensor fusion is addressed through copulas (Fig. 2(f)); (iii) the multisensor single-resolution approach in [4], in which the joint class-conditional PDFs of multisensor data are modeled with meta-Gaussian distributions and combined with the maximum likelihood rule (Fig. 2(g)); and (iv) a support vector machine (SVM) applied to the stacked optical-SAR data as a nonparametric pixelwise benchmark (Fig. 2(h)). The Gaussian radial basis function kernel was used and the SVM parameters were optimized using the method in [20].

A visual analysis of the classification maps suggest that the first proposed method led to rather accurate results, especially as compared to the separate hierarchical classifications of the images of the two sensors. The results obtained using only SAR data accurately detected roads and poorly discriminated most other classes, while the map generated using only optical data better discriminated classes that were spatially homogeneous. The proposed method took benefit from both sources and generated a result that visually discriminated quite well most classes. Compared to the multisensor single-scale method in [4], the proposed algorithm provided a spatially more regular map thanks to MRF modeling and wavelets.

Quantitative analysis on the test set confirmed that the proposed method provided quite high overall accuracy (OA) and Cohen's  $\kappa$ , and improved as compared to the method in [4] (Table I). Poor discrimination was obtained by all techniques for "containers," because of its large overlapping with "urban" in the multisensor or multispectral feature space. To improve the accuracy for this class, texture features could be integrated as an extension of the proposed method. The multisensor multiscale method in [5] also provided high accuracies, similar to those of the proposed algorithm, with slightly lower OA and higher  $\kappa$ . However, as compared to this technique, the proposed method improved in terms of spatial detail (Figs. 2(f) and (i)) and computation time (Table I). The approach to multisensor fusion based on distinct quad-trees related to individual sensors avoids the difficult and possibly time-expensive task of estimating the joint optical-SAR PDFs, whereas copula and meta-Gaussian models are used for this task in [5] and [4], respectively. The SVM provided lower accuracy than the other considered methods, which was expected because of its noncontextual formulation. The values of McNemar's  $Z$  statistics of the maps of the benchmark methods with respect to the map of the proposed method are all much larger than the 5% significance threshold ( $|Z| > 1.96$ ), which confirms that the differences among these results are significant.

TABLE I

FIRST PROPOSED METHOD, CSK-GEOEYE-1 DATASET: TRAINING AND TEST SAMPLE SIZES; CLASSIFICATION ACCURACIES AND  $\kappa$ ; MCNEMAR'S  $Z$  WITH RESPECT TO THE PROPOSED METHOD; AND COMPUTATION TIMES (INTEL I7 QUAD-CORE, 2.40 GHZ, 8 GB RAM, 64 BIT LINUX SYSTEM).

	water	urban	vegetation	bare soil	containers	OA	$\kappa$	$Z$	computation time [s]
Proposed method	100%	78.12%	89.46%	98.78%	47.12%	82.69%	0.76	–	254
Method in [4]	99.95%	97.32%	90.81%	96.22%	37.25%	79.44%	0.68	1843.7	298
Method in [5]	100%	75.24%	87.16%	98.89%	49.31%	82.12%	0.79	89.6	668
SVM	96.52%	70.31%	44.28%	78.15%	43.20%	66.49%	0.57	2298.3	372
Training samples	50043	79492	51312	11667	38936				
Test Samples	49057	75508	50688	10333	31064				

TABLE II

SECOND PROPOSED METHOD, CSK-RS2-PLÉIADES DATASET: TRAINING AND TEST SAMPLE SIZES; CLASSIFICATION ACCURACIES AND  $\kappa$ ; AND MCNEMAR'S  $Z$  WITH RESPECT TO THE PROPOSED METHOD.

	water	urban	vegetation	bare soil	containers	OA	$\kappa$	$Z$
Pléiades only	100%	61.66%	81.69%	82.82%	56.72%	76.57%	0.63	1361.7
Pléiades + CSK	100%	44.32%	83.54%	74.75%	49.12%	70.34%	0.58	2102.7
Pléiades + RS2	92.56%	44.85%	79.85%	78.62%	42.15%	67.60%	0.57	2163.7
Proposed method (Pléiades + RS2 + CSK)	90.79%	91.45%	82.59%	81.02%	54.85%	80.14%	0.78	–
SVM	92.86%	92.56%	61.86%	69.91%	56.64%	74.76%	0.61	2302.9
Training samples	12943	15492	10312	8667	6016			
Test samples	12057	14508	9688	6333	5984			

### B. Results of the second proposed method

A challenging VHR dataset, collected again over Port-au-Prince and composed of a Pléiades pansharpened image at 0.5-m resolution ( $1000 \times 1000$  pixels; Fig. 3(a)), an HH-polarized CSK spotlight image at 1-m resolution (Fig. 3(b)), and an HH-polarized RS2 ultrafine image with 1.56-m pixel spacing (Fig. 3(c)), was used for experiments. The same five classes of the previous section were considered (Table II). Given the 0.5-m resolution of the Pléiades data, we slightly resampled the RS2 image to obtain 2-m pixel spacing and fit with the power-of-2 constraint implied by the quad-tree. Downsampling from 1.56 to 2 m is expected to have a minor impact on the classification map, because the resampling ratio is quite close to 1. Preliminary experiments (not shown for brevity) indicated that the order in which CSK and RS2 data were inserted in the quad-trees did not significantly affect the results.

The second proposed method obtained rather high OA and  $\kappa$  on the test set (Table II) and remarkable spatial regularity (Fig. 3(h)). Again, poor discrimination was obtained for “containers.” To investigate the capability of the method to exploit the synergy among X-band, C-band, and VNIR data, comparisons with the results obtained by using the Pléiades image only by itself or together with either SAR image (Table II and Figs. 3(d), (e), and (f)) were conducted. In all these comparisons, the same quad-tree, MPM, and finite-mixture formulations as in the proposed method were used. The results obtained using only SAR data poorly discriminated the classes and are not reported for brevity. A comparison with a nonparametric pixelwise benchmark was performed by resampling the CSK and RS2 images on the 0.5-m grid, stacking them together, and applying an SVM with the same model selection strategy as in Section III-A (Fig. 3(g)). Quantitative analysis on the test set confirmed that the joint use of all three sensors led to substantially higher accuracies as compared to the use of a subset of the input data sources. The use of only the Pléiades image allowed “water,” “vegetation,” and “bare soil” to be effectively discriminated but led to poor detection of “urban.” The joint use of this VNIR image and of X-

band and C-band SAR through the second proposed method allowed improving the discrimination of “urban” of nearly 30% and outperformed the results obtained using the Pléiades data together with only one of the two SAR images. These results suggest the potential of the second proposed method in exploiting the complementarity of multisensor, multifrequency, and multiresolution data from current VHR satellite sensors. In this case as well, the noncontextual SVM obtained lower test-set accuracy and a more noisy map than the proposed method. McNemar’s test indicates that the differences between the results of the proposed method and of each benchmark are again significant. A shortcoming of the proposed technique was the lower accuracy for “water” than when only Pléiades or Pléiades and CSK data were used. Indeed, “water” appears highly textured in the RS2 image (Fig. 3(c)), whereas the proposed technique uses no texture features. On one hand, the accuracy of the proposed method for “water” is still around 91%. On the other hand, incorporating texture features could be a feasible extension of the second proposed method as well.

## IV. CONCLUSION

A hierarchical MRF approach to multisensor and multiresolution optical-SAR image classification has been formulated, extending inference procedures originally introduced for multitemporal fusion and incorporating suitable finite mixture models. Two classification methods have been developed in this framework. Experimental results on challenging HR/VHR data sets have suggested the effectiveness of this approach to data fusion and the improvement of the two proposed methods as compared to single-sensor, single-resolution, and/or previous techniques in terms of accuracy, spatial precision, or computational burden. A further advantage of the proposed approach to fusion is its flexibility. While multitemporal fusion was already formalized in this framework in [8], the multiple quad-tree structure could be extended to also incorporate data from further sensors or feature extraction stages (e.g., textures or morphological profiles). This extension will be pursued in the near future. Moreover, alternate wavelet de-

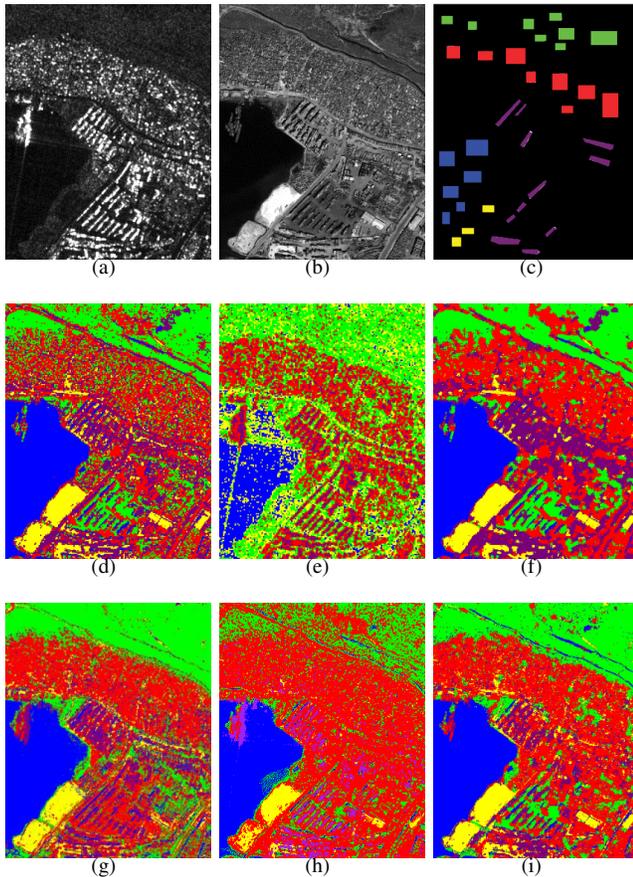


Fig. 2. First proposed method: (a) CSK (©ASI 2010) and (b) GeoEye-1 (©GeoEye 2010; R-band display) images; (c) ground truth (training and test areas); results of the hierarchical MRF-based classifications of (d) the GeoEye-1 and (e) the CSK image; and (f) results of the techniques in [5] and (g) in [4], (h) SVM, and (i) the proposed method. Color legend: see Table I.

compositions [10] will also be investigated, including wavelet packets, with which the number of transformed samples in the quad-tree is increased, and undecimated stationary wavelets, which preserve image size along different levels and could be incorporated into a multisource MRF energy as in [21].

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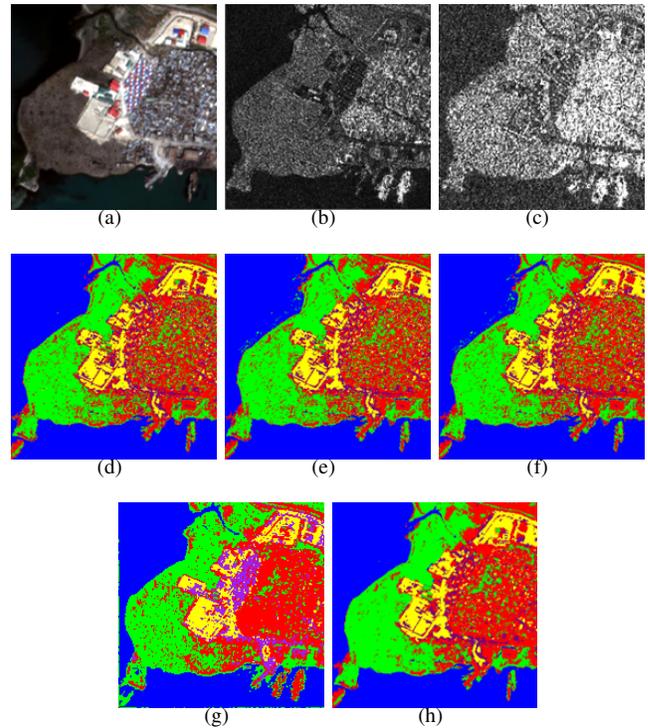


Fig. 3. Second proposed method: (a) Pléiades (©CNES distribution Airbus DS; true-color display), (b) CSK (©ASI 2011), and (c) RS2 (©CSA 2011) images, and classification maps obtained using (d) only the Pléiades image, (e) the Pléiades and CSK images, (f) the Pléiades and RS2 images, (g) SVM, and (h) the proposed method with all images. Color legend: see Table II.

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