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# The Joule heating problem in silver nanowire transparent electrodes

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#### **Abstract**

Silver nanowire transparent electrodes have shown considerable potential to replace conventional transparent conductive materials. However, in this report we show that Joule heating is a unique and serious problem with these electrodes. When conducting current densities encountered in organic solar cells, the average surface temperature of indium tin oxide (ITO) and silver nanowire electrodes, both with sheet resistances of 60 ohms/square, remains below 35 °C. However, in contrast to ITO, the temperature in the nanowire electrode is very non-uniform, with some localized points reaching temperatures above 250 °C. These hotspots accelerate nanowire degradation, leading to electrode failure after 5 days of continuous current flow. We show that graphene, a commonly used passivation layer for these electrodes, slows nanowire degradation and creates a more uniform surface temperature under current flow. However, the graphene does not prevent Joule heating in the nanowires and local points of high temperature ultimately shift the failure mechanism from nanowire degradation to melting of the underlying plastic substrate. In this paper, surface temperature mapping, lifetime testing under current flow, post-mortem analysis, and modelling illuminate the behaviour and failure mechanisms of nanowires under extended current flow and provide guidelines for managing Joule heating.

Supplementary material for this article is available online

Keywords: transparent electrode, silver nanowire, Joule heating, reduced graphene oxide

(Some figures may appear in colour only in the online journal)

#### 1. Introduction

Silver nanowire (AgNW) transparent electrodes have emerged as an alternative material to conventional transparent conductive oxides. They can exhibit similar conductivity and transparency values as indium tin oxide (ITO) films [1, 2], the most common transparent conductive material, while being lower in cost. Furthermore, nanowire electrodes have the advantages of being deposited on substrates using low

temperature solution deposition methods and are able to maintain their conductivity after repeated bending. These aspects make them particularly desirable for use on plastic substrates for flexible electronics, for which ITO is inappropriate [3].

AgNW transparent electrodes are already being used in commercial touchscreen applications. These touchscreens work by creating and changing an electric field between the nanowire electrode and a parallel electrode, with an active

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dielectric material in between that responds to the field. A current flows across the nanowire electrode only for a short time to change its potential during switching, with minimal current flowing otherwise. This is also true for other capacitive-type devices such as smart windows [4]. However, for devices such as solar cells, organic light emitting diodes (OLEDs), and transparent heaters, there are long periods of time when current continuously flows across the transparent electrode during device operation, resulting in Joule heating. Although not typically problematic for ITO electrodes, we have previously shown that the Joule heating created at the current levels typically encountered in organic solar cells causes nanowire electrodes to fail in a matter of days. The nanowires breakup and electrical discontinuities appear in the electrode [5].

Multiple mechanisms can lead to silver nanowire degradation. Silver nanowires corrode in air, specifically due to the presence of trace amounts of sulfur [6], and this corrosion phenomenon is accelerated at elevated temperatures [7]. Additionally, silver nanowires are not morphologically stable owing, in part, to their high surface-area volume ratio. They tend to break into small segments, a behaviour usually attributed to the Rayleigh instability [8 10]. Like corrosion, this instability of metal nanowires is also worsened at higher temperatures [10]. In order to slow nanowire degradation and thus increase the lifetime of AgNW electrodes, various passivation strategies have been developed that use an outer layer to protect the silver nanowires from corrosion and other side reactions with the environment. The passivation layer must be optically transparent, and electrically conductive as well if it stands, for example, between the nanowire network and the active part of a solar cell. Passivation materials such as zinc oxide (ZnO), titanium oxide (TiO<sub>2</sub>), and graphene have been used [11 14]. Reduced graphene oxide (RGO), in particular, is attractive since it can act as a barrier for both moisture and gases in air [15]. It can be deposited as films thinner than ZnO and TiO<sub>2</sub> ones, optimizing optical transparency. Furthermore, like AgNW films, RGO is mechanically flexible and can be deposited from solution. Several studies have demonstrated the utility of RGO as a passivation layer for AgNW electrodes [13, 16 19]. For instance, whereas the sheet resistance of an unpassivated AgNW electrode more than tripled in less than a week while annealed at 70 °C in air, the resistance of the same nanowire electrode passivated with a uniformly dip-coated RGO layer increased by less than 50% over the same time [20]. If a layer of graphene is instead deposited on a AgNW electrode using chemical vapour deposition (CVD), it can stabilize the silver nanowires more effectively. A recent experiment revealed only a 10% increase of sheet resistance after one month while annealed at 70 °C [21]. However, this latter method is presently not economical for commercial manufacturing, especially since the graphene layer cannot be directly synthesized on the nanowires but rather needs to be first deposited on a substrate and then transferred onto the nanowire film.

In the above studies, degradation of passivated and unpassivated silver nanowire electrodes were evaluated either at room temperature or when the electrode was annealed in an oven (or on a hotplate) to achieve an elevated temperature. In all cases, the temperature was the same at all points on the electrode. However, the surface temperature profile across a nanowire electrode is not uniform when it is used in a solar cell, OLED, or tranparent heater. Unlike in a continuous conducting film (e.g. ITO) where current flows throughout the entire area of the film, in the case of nanowire electrodes current only flows through the thin metal pathways. Furthermore, there are variations in the nanowire density across the film and thus the current density flowing in some nanowire pathways is higher than in others. These factors combined result in a non-uniform temperature distribution in the electode where the temperatures of some individual nanowires are significantly higher than the average surface temperature of the electrode [2]. In this work we investigate AgNW electrodes and RGO-passivated AgNW electrodes under current flow. Compared to annealing, this is a more realistic situation for studying the performance and lifetime of the electrodes when they are operated in a solar cell or OLED. As other reports have shown, we confirm that a RGO passivation layer does increase lifetimes by slowing nanowire degradation during an anneal. However, when the nanowire electrode is instead under current flow, RGO is not nearly as effective as it does not prevent Joule heating. It is shown that the Joule heating in RGO-passivated electrodes results in local melting and deformation of the plastic substrate leading ultimately to electrode failure. These results indicate that Joule heating is an issue that cannot be overlooked and needs to be effectively addressed and managed if nanowire electrodes are to be used in devices such as solar cells, OLEDs, and transparent heaters.

#### 2. Experimental section

## 2.1. Nanowire electrode fabrication

Silver nanowires dispersed in ethanol were purchased from Blue Nano Inc. (Charlotte, NC) with an average diameter and length of 90 nm and 25  $\mu$ m, respectively. Polyethylene terephthalate (PET) films (127  $\mu$ m thick from Dupont Tianjin Inc.) were used as substrates for the electrodes (PET was used rather than glass since a distinct advantage of AgNW electrodes is their suitability for plastic substrates). The PET films were cleaned sequentially in a sonication bath of acetone, isopropanol alcohol, and distilled water each for 1 min, then dried with nitrogen gas. The nanowires were deposited on the PET films using the Mayer rod coating technique to obtain a random network of silver nanowires [22]. The active area of the deposited AgNW film was  $2 \text{ cm} \times 2 \text{ cm}$  with two strips of 0.5 cm wide copper tape installed at the two ends of the electrodes (2 cm apart) as current collectors. The transparency and conductivity of the silver nanowire electrodes can be controlled by changing the concentration of the nanowires in ethanol and the number of coating layers. The dependency of the transmitance and conductivity has been reported elsewhere [23]. The deposited films were dried in air for 5 min and mechanically pressed by rollers at room temperature to reduce the nanowire junction resistances [24].

ITO on PET with a sheet resistance of 60 ohms/sq was purchased from Sigma Aldrich. Although lower sheet resistances are desired for solar cell applications, ITO on PET has higher resistance than on glass due to the need for lower deposition temperatures. To be able to compare with ITO, the AgNW electrodes were also made with a sheet resistance of  $60 \pm 10\%$  ohms/sq. AgNW electrodes with sheet resistances of 20 ohms/sq were prepared as well to see the effect of Joule heating in lower resistance networks.

#### 2.2. Determining current value

The current density assumed in this study was 20 mA cm<sup>2</sup>, which is the typical operating current of the best performing organic solar cells in the literature [25, 26]. Current densities in OLEDs can also reach values as high as 20 mA cm<sup>2</sup> [27]. The maximum current is usually incurred near the current collector bar in these devices. In common designs of organic solar cell modules the width of the active layer is around 1 cm, and the current flowing through the transparent electrode is collected at one end only (see figure S1, available online at stacks.iop.org/NANO/28/425703/mmedia) [28 30]. Therefore, with a current density of 20 mA cm<sup>2</sup>, the current at the current collector bar will reach 20 mA per centimetre length (20 mA cm<sup>1</sup>) of current collector. As this is the typical maximum current incurred in the transparent electrode, this is the value we used in the experiments.

#### 2.3. Graphene oxide (GO) monolayer fabrication

GO was first prepared using the Tour method [31]. A continuous, densely tiled, monolayer of the GO was then formed on the surface of water using a modified Langmuir Blodgett (LB) trough technique [32]. Instead of using mechanical barriers to compress the film, as in the typical LB process, the spreading force of the solvent is used to compress the films against the edge of the trough. Thus, in principle, this approach has the potential to be adapted to a roll-to-roll manufacturing by withdrawing a substrate during material deposition. Such a system will be reported elsewhere. The asprepared AgNW-coated PET samples were placed at the bottom of the trough prior to GO deposition, and the floating monolayer GO film was lowered onto the substrates by slowly draining the water. In addition to coating PET samples, mica and highly oriented pyrolytic graphite (HOPG) substrates were coated at the same time to verify film morphology and coverage using atomic force microscopy (AFM) and scanning electron microscopy (SEM). The GO was chemically reduced using NaBH<sub>4</sub>. Further details of the GO synthesis, monolayer formation, and chemical reduction can be found in the supplementary information.

#### 2.4. Characterization

Contact mode AFM was carried out on GO films deposited on atomically flat muscovite mica (SPI) substrates using NP-STT10 tips (Bruker) and a Nanoscope MultiMode AFM (Veeco). AFM images were analysed using Gwyddion software to extract height profiles between the atomically smooth

substrate and the GO sheets, and a custom MATLAB code was used to estimate sheet thicknesses from the steps in the height profiles.

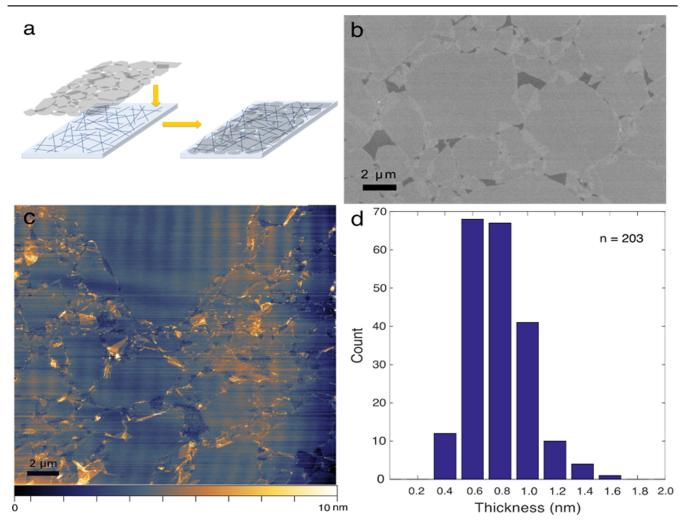
The sheet resistance of the electrodes with and without the RGO layer was measured by either a multimeter or a 4-point probe measurement system. UV vis photospectroscopy with an integrating sphere was used to measure the transparency of the electrodes. SEM images were taken before and after failure of the electrodes.

A DC power supply was connected to the current collectors to apply a constant current of 20 mA cm<sup>-1</sup> across the electrodes. A multimeter and a flat leaf-style thermocouple were used to continuously monitor the voltage across the electrode and its average surface temperature, respectively, during extended time experiments and PC link software was used to record the data (a schematic of the experimental setup is shown in figure S2). In a separate measurement, an infrared (IR) camera was used to map the spatial temperature distribution over the electrode area while the electrode was conducting 20 mA cm<sup>-1</sup> of current. The IR camera (FLIR SC7000) had an indium antimony detector composed of a focal plane array featuring 81 920 pixels (matrix 320 × 256), and a simultaneous measurement at all 81 920 spots could be performed using the snapshot mode. The camera was equipped with an IR lens with a focal length of 25 mm. The resulting spatial resolution per pixel is around 250  $\mu$ m  $\times$  250  $\mu$ m. A previously reported calibration method [32, 33] was used to retrieve the absolute temperature of the samples (semi-transparent samples) from the raw intensity data provided by the IR camera. More details about the calibration can be found in the supplementary information.

#### 2.5. Modelling

Random networks of silver nanowires were modelled in MATLAB. The nanowires were modelled as cylinders having the same average diameter and length as the nanowires used in our experiment (90 nm and 25  $\mu m$ , respectively). The resistivity of the nanowires considered in the model was set to 27 n $\Omega$  m, which is the average resistivity reported for 90 nm diameter silver nanowires [34 36]. The nanowires were randomly distributed over a 300  $\mu m \times 300 \ \mu m$  area (figure 5(a)) and treated as pure resistors. The density of nanowires was chosen to generate nanowire networks with sheet resistances of  $60 \pm 15\%$  ohms/sq. The overall circuit was analysed using HSPICE. An HSPICE netlist was constructed for this random nanowire network in order to calculate the sheet resistance of the modelled network and extract the electrical current in individual nanowires.

The electric current values retrieved from HSPICE simulations were subsequently used to model Joule heating in individual nanowires using the Joule heating module of COMSOL Multiphysics software. The temperature profile of nanowires under the range of current densities were simulated for wires lying on a PET substrate with and without a RGO passivation layer. The graphene sheets are much larger than the diameter of the nanowires and cover their surface and the surrounding substrate conformably, as shown by others [19].



**Figure 1.** Reduced graphene oxide blocking layer. (a) Schematic illustrating graphene oxide monolayer deposition on a silver nanowire/PET film. (b) SEM image showing contrast between the graphene oxide film (light) and some pinholes exposing the HOPG substrate (dark). (c) Contact mode AFM image of the graphene oxide film on mica. (d) Histogram of graphene oxide sheet thickness estimated from AFM imaging.

In the COMSOL model the conformal contact was simplified to square shape. This shape has three points of contact with the nanowire with small gaps between the nanowire and the RGO layer which is similar to the real structure. The area of the substrate was selected according to the experimental nanowire density by dividing the area of the substrate by the number of nanowires. Heat convection was considered at the top and bottom of the PET sample and all surfaces of the nanowires and the RGO layer as the boundary condition. More details about modelling can be found in the supplementary information.

#### 3. Results and discussion

#### 3.1. Characterization of electrodes

Our first goal was to create a transparent barrier film of RGO to protect the Ag nanowires as illustrated schematically in figure 1. The morphology and coverage of the RGO film, deposited by a modified LB technique, are shown in the SEM

and AFM images in figures 1(b) and (c), respectively. The contrast in the SEM image (figure 1(b)) shows the RGO film (bright) and the underlying HOPG substrate (dark) and indicates that the film is composed of densely tiled and partially overlapping (even brighter contrast regions) sheets. The film coverage, estimated by pixel counting, is over 95%. The AFM images of films deposited on mica (figure 1(c)) show the same coverage. A histogram generated by analysing AFM thickness profiles of over 200 sheets is shown in figure 1(d) and indicates that the tiled sheets have a narrow distribution of thicknesses centred around 0.7 nm. This indicates that the film is composed almost entirely of monolayers. Imaging many samples over large areas indicates that this morphology persists over the entirety of the coated substrate area and confirms that the LB approach yields higher quality films [37, 38] compared to those deposited by spin [16] or dip-coating [18]. These latter methods typically result in a more random deposition, requiring more material to cover the same area. On the other hand, single layer films produced by our method leave about 5% of the area exposed compared to CVD grown films, the latter which may possess fewer film defects but remain more challenging and costly to produce. It was challenging to verify the film morphology and coverage on PET substrates directly because the surface roughness is larger than the expected film thickness and the secondary electron contrast difference between PET and RGO is poor. However, the fact that we could achieve similar morphologies on both hydrophilic (mica) and hydrophobic (HOPG) substrates suggests that our film coverage and thickness should be very similar on PET.

The optical transparency of the 60 ohms/sq AgNW films (not including the PET substrate) at a wavelength of 550 nm were 94%. The transmittance of the AgNW electrode dropped from 94% 91% after the deposition of the RGO layer. The observed 3% transmittance decrease is consistent with the transmittance value of a single layer of graphene in the visible range which is in direct agreement with our AFM and SEM analysis of the graphene film discussed above [39]. The RGO sheets are electrically conductive, however, their electrical conductivity is significantly less than the conductivity of the nanowires [40], and the contact resistance between two overlapping RGO sheets is high. Thus, the overall sheet resistance of the AgNW electrodes did not decrease significantly after adding the RGO layer (only by 0% 10%).

### 3.2. Annealing study

We first confirmed prior studies of the literature showing the effectiveness of RGO in protecting the nanowire films against degradation when annealed in a furnace. Both the AgNW and AgNW-RGO electrodes were annealed at 70 °C in air for 14 days. After 6 days, the sheet resistance of the AgNW electrode increased by a factor of 180 compared to the initial sheet resistance of 60 ohms/sq, whereas the sheet resistance of the AgNW-RGO electrode increased only by a factor of 1.5 after 14 days. This indicates that the RGO layer is quite successful in slowing down silver nanowire electrode degradation under annealing conditions, as concluded by many others. However, testing its effectiveness under current flow is essential to mimic the stress faced by the AgNW electrode during use in a solar cell or OLED.

#### 3.3. Surface temperature distribution under current flow

A 20 mA DC current was passed across the electrodes per centimetre length of the current collectors (20 mA cm<sup>-1</sup>). Figure 2 shows the evolution of the surface temperature profiles obtained using thermal imaging for 60 ohms/sq ITO, AgNW, and AgNW-RGO electrodes. Temperature images in figures 2(a), (d), (g) are shown 10 s after the current flow was applied whereas images in figures 2(b), (e), (h) are recorded after the temperature has stabilized (60 s). In these images, the current flows from top to bottom, as indicated schematically in figure 2(a). As can be seen, the temperature appears uniform over the ITO electrode. However, local temperature variations greater than 20 °C are evidenced across the AgNW electrode (figures 2(d) (f)). The presence of such hot spots in nanowire electrodes has also been reported by others [41, 42] and may be due to the non-uniform density distribution of the

nanowires across the electrode. In bottleneck regions where there is a sparser nanowire concentration, individual nanowires must sustain high current densities and thus local Joule heating will be significantly higher than in denser nanowire regions. The hotspots observed in the unpassivated nanowire electrode exist along a line across the electrode parallel to the current collectors. We hypothesize that there are regions of sparse nanowires along this line and thus much of the current cannot re-route through denser locations. Thus Joule heating, equal to  $I^2R$  where I is current and R is resistance, is high along this line. The existence of hot spots accelerates both corrosion and Rayleigh instability in these regions leading to nanowire breakdown. When nanowires break down, more current is forced through other available pathways, causing those regions to then locally increase in temperature. This situation can be observed in figures 2(d) (f). A hotspot present after 10 s, which figure 2(f) indicates is at the highest temperature on the electrode, no longer exists after 60 s. This suggests that some nanowires failed rapidly after current was applied due to this high temperature. As can be observed, it cooled down once current could no longer flow through that pathway, but consequently, the regions around the failed nanowires became hotter. This in turn accelerates nanowire degradation at these points until ultimately, as we observed when higher currents were applied to accelerate failure times, an open circuit exists in a line extending across the electrode.

It is important to note that the smallest detected area (pixel resolution) of the thermal imaging camera is  $250 \, \mu \mathrm{m} \times 250 \, \mu \mathrm{m}$  which corresponds to an area with more than one hundred nanowires. Thus, the temperature of individual nanowires is not directly detectable, and we get an average temperature over the pixel area. In the modelling results reported later, we will see that the temperature variations on the nanoscale are far higher than ones observed on the microscale in thermal maps such as these.

In figures 2(g) (i) it is evidenced that the RGO passivation layer smooths out the temperature variation over the AgNW electrode such that the resulting temperature uniformity appears comparable to that of the ITO electrode. This is likely because of the high thermal conductivity of the RGO (above 1000 W m  $^{1}$  K  $^{1}$ ) [43] compared to air (0.024 W m  $^{1}$  K  $^{1}$ ) [44] and the plastic substrate (0.20 W m  $^{1}$  K  $^{1}$ ) [45] which assists in the lateral distribution of heat over the surface of the electrode. The absence of hot spots is one of the reasons why we will later see that the RGO extends the lifetime of AgNW electrodes under current flow. Also, because the RGO distributes the heat more evenly across the surface, it effectively provides a larger surface area from which the heat can dissipate and thereby slightly lowers the average surface temperature of the electrode.

# 3.4. Electrode failure under current flow

Figure 3(a) shows the average surface temperature (measured with a thermocouple that was attached to the bottom of the substrate) and sheet resistance evolution for an unpassivated 60 ohms/sq AgNW electrode under 20 mA cm<sup>-1</sup> of linear

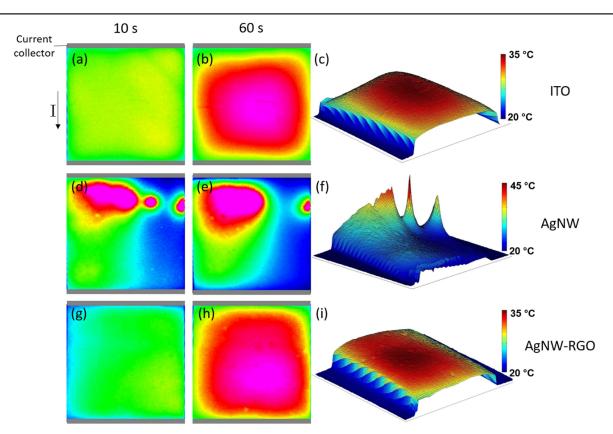


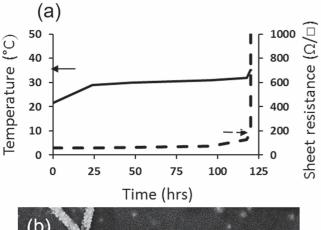
Figure 2. Temperature profiles of  $2 \text{ cm} \times 2 \text{ cm}$  electrodes, measured using a thermal imaging camera, when  $20 \text{ mA cm}^{-1}$  of current is applied from top to bottom. (a), (b) surface temperature of ITO, (c) 3D temperature profile of ITO after 60 s. (d), (e) Surface temperature of the AgNW electrode, (f) 3D temperature profile of the AgNW electrode after 10 s. (g), (h) Surface temperature of the AgNW RGO electrode, (i) 3D temperature profile of the AgNW RGO electrode after 60 s.

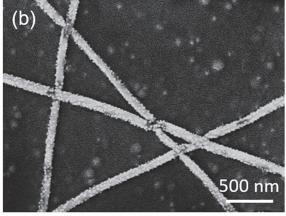
current density. The electrode failed after 120 h (5 days), where failure is defined as when the sheet resistance exceeded 1500 ohms/sq. SEM images of nanowires after electrode failure are shown in figures 3(b) and (c), illustrating the two different types of nanowire breakdown that were observed. In figure 3(b), the presence of nanoparticles on the nanowires indicate nanowire corrosion [5] which eventually lead to electrical discontinuities. Other nanowires (figure 3(c)) are completely melted in addition to damaging the plastic substrate underneath, implying a very high localized temperature. We suggest that these latter nanowires were subjected to very high levels of current and thus heated up and failed quickly, like those associated with the disappearing hotspot in figures 2(d) and (e), whereas the corroded nanowires were subject to lower current densities over a longer time period. These issues will be further discussed when the modelling of current levels and temperatures of individual nanowires is presented.

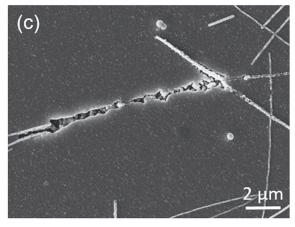
Figure 4(a) shows the average temperature and sheet resistance of the AgNW-RGO electrodes under a linear current of 20 mA cm<sup>-1</sup>. The RGO passivation layer extended the lifetime of the AgNW electrode to 285 h (~12 days). There are three possible mechanisms by which RGO passivates the electrodes: (1) nanowire corrosion is slowed since the RGO impedes air from reaching the nanowires. This is supported by the observed increase in lifetime upon extended annealing at 70 °C with no current flow; (2) the RGO prevents hotspots

(as discussed above) where the fastest degradation occurs; and (3) the RGO increases the morphological stability of the nanowires and thus increases the temperature at which the nanowires break-up [46]. Indeed, SEM images taken after electrode failure show that the RGO-passivated electrodes do not fail due to NW melting or corrosion (figure 4(b)), which is the case for unpassivated electrodes. Rather, the electrode instead breaks down due to deformation and melting of the PET substrate on a micron length-scale (figures 4(c) and (d)). The substrate deformation causes breakage in the nanowires and thus electrical discontinuities.

A melted substrate indicates that the local temperature of the nanowires exceeds the melting point of PET ( $\sim$ 250 °C) during current flow. The silver nanowires, normally unstable at this temperature [47], remain due to the RGO passivation. Although the thermal imaging data indicated the RGO-passivated electrodes had an average surface temperature of 32 °C under this same current flow (figure 2(i)), the local temperature of some nanowires are much higher. These results demonstrate the inadequacy of annealing a nanowire electrode to assess stability and lifetimes, which is the method used by many others and done above. The Joule heating that would take place in an electrode during solar cell operation, which causes very high localized temperatures, is not incurred. As measured above, the resistance of the RGO-passivated electrode annealed in a furnace at 70 °C only increased by 1.5 times after 12 days, whereas under a current flow causing







**Figure 3.** (a) Temperature and sheet resistance of a AgNW electrode over time under a linear current density of 20 mA cm<sup>-1</sup>. (b), (c) SEM images of nanowires after electrode failure. The nanowires in (b) show evidence of accelerated corrosion leading to discontinuities, and in (c) a nanowire along with with part of the PET substrate underneath has melted.

an average surface temperature of 32 °C, the resistance increased by more than 25 times.

#### 3.5. Modelling of current in a nanowire network

As evidenced by SEM imaging, electrode failure occurs at the level of individual nanowires. However, measuring the local temperature and the levels of electric current flowing through individual nanowires in an electrode is experimentally prohibitive. Therefore, modelling was employed to better

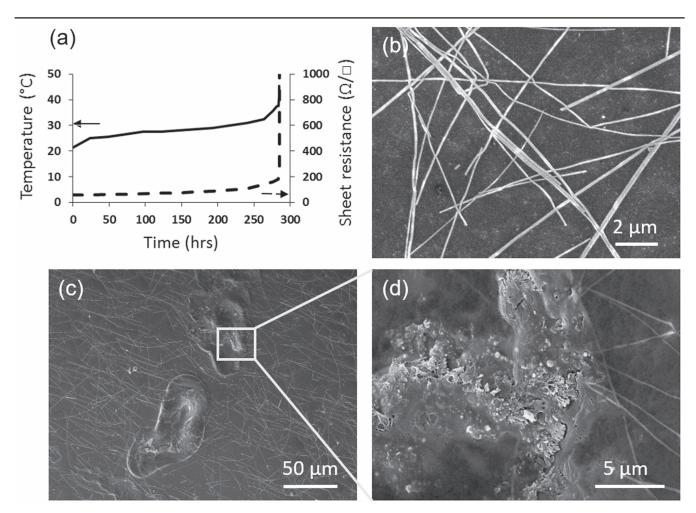
understand the extent of Joule heating in an electrode and the mechanisms of failure.

The silver network modelled in MATLAB is shown in figure 5(a). Figure 5(b) tabulates the typical current densities in individual nanowire segments (segments span between two red dots in figure 5(a), where red dots are the locations of nanowire junctions and nanowire endpoints) when 20 mA cm<sup>-1</sup> is applied across the metal end bars. This level of current does not lead to problematic current densities in continuous films, however, in the case of nanowire electrodes, as previously discussed, high current densities occur when the current is forced through 90 nm thick nanowire pathways. The average current density in the nanowires is calculated to be 1.2  $\pm$  $0.1 \times 10^5$  A cm<sup>2</sup>. As a comparison, in the case of a 130 nm thick film of ITO corresponding to the approximate thickness to achieve 60 ohms/sq, the current density would be  $1.5 \times 10^3$  A cm<sup>2</sup>, two orders of magnitude less than the one observed in the nanowires.  $0.5 \pm 0.1\%$  (error based on running the simulation with a different random network 5 times) of the nanowires in the electrode may carry a current density superior to  $5.5 \times 10^5$  A cm<sup>2</sup> and are expected to break down relatively fast due to Joule heating (to be discussed in the subsequent section).

# 3.6. Joule heating modelling of nanowires in electrodes

Figure 6 shows the results of the COMSOL Joule heating simulations and the steady state temperatures reached by an individual AgNW, a AgNW passivated with RGO, and ITO. It is worth mentioning that at steady state the whole system is at a similar temperature and thus the colouring indicates only very minor differences in temperature. The colours however are useful to show how heat is dissipated in the system. A single AgNW carrying the average current previously calculated in the section above  $(1.2 \times 10^5 \,\mathrm{A\,cm}^2)$  reached 33 °C (figure 6(a)) and a RGO-passivated AgNW reached 30 °C (figure 6(b)). The RGO film helps spread out the heat and reduces the surface temperature by 8% 10%. Our simulated results match closely to experiment: the calculated average surface temperature of the AgNW electrode under 20 mA cm<sup>-1</sup> of current, recorded by the IR camera, was found to be  $33 \pm 2$  °C, and the measured average temperature of the AgNW-RGO (figure 2(i)) was  $32 \pm 2$  °C. In the case of a 60 ohms/sq, 130 nm thick ITO film on a PET substrate under the calculated ITO average current density of  $1.5 \times 10^3 \,\mathrm{A\,cm}^2$  (figure 6(c)), the steady state temperature was calculated to be 32 °C, also close to the  $34 \pm 2\,^{\circ}\text{C}$  average temperature recorded by the IR camera (figure 2(c)).

Although the temperature of a nanowire conducting the average current density is 33 °C, there are some individual nanowire segments in the whole metallic network that can become much hotter. Figure 6(d) shows the simulated temperature of silver nanowires on a PET substrate at different current densities. As calculated in the previous section, 0.5% of the nanowire segments in a 60 ohms/sq AgNW electrode under 20 mA cm  $^{-1}$  current flow are carrying a current density higher than  $5.5 \times 10^5$  A cm  $^{-2}$ . Figure 6(d) shows that the temperature of unpassivated NWs carrying such levels of



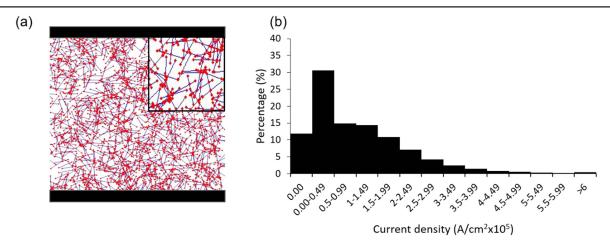
**Figure 4.** (a) Temperature and sheet resistance versus time of a AgNW RGO electrode under a linear current density of 20 mA cm<sup>-1</sup>. SEM images after failure of (b) a non melted region and (c), (d) localized substrate melting.

current exceed 250 °C, a temperature above the melting point of PET. Importantly, at such a temperature unpassivated 90 nm diameter AgNWs are not thermally stable either [47]. Such nanowires would fail quickly after the current is applied. These nanowire segments are hotter than the hottest spot evidenced in the IR images because, as mentioned above, the camera measures an average temperature of several hundred nanowires. However, the existence of these very hot nanowires still corroborates with our experimental results. The IR data in figures 2(d) and (e) insinuate that there is a rapid failure of some nanowires, and the SEM image in figure 3(c) indicates the melting of both the nanowire and a localized portion of the PET substrate. Once these high current carrying nanowires break and are no longer conductive, the current is redistributed amongst the other nanowires.

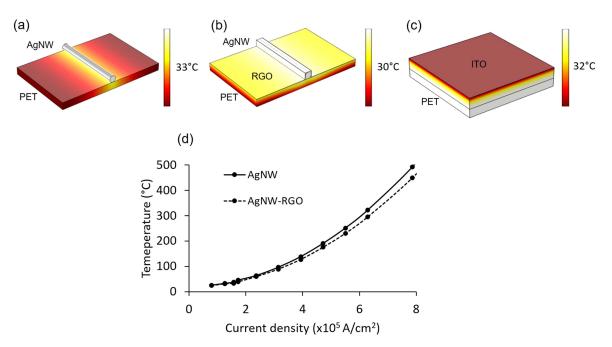
The existence of localized nanoscale hotspots of high temperatures is in stark contrast to ITO electrodes where the current is distributed evenly throughout the film. In an ITO film carrying the same linear current density as the nanowire electrode, all points over the surface are expected to be close to 32 °C. The existence of a non-uniform temperature distribution and localized hotspots reaching 250 °C is a unique issue for nanowire electrodes.

Because RGO is not as electrically conductive as the nanowire network, it does not significantly lower the current densities in the nanowires and therefore Joule heating still occurs. Although it initially avoids larger microscale hotspots and slightly lowers the average surface temperature by spreading heat more uniformly over the surface, we can see in figure 6(d) that the temperatures of individual nanowires in the AgNW-RGO case can still be very high. And because a single layer of RGO does not thoroughly prevent nanowire degradation, as evidenced by the slight resistance increase during annealing (1.5 times after 14 days) and by the observation of some nanowire corrosion in the SEM after extended current flow, the current densities in the nanowires increase over time. As a consequence, this leads to more and more Joule heating until ultimately the PET substrate melts over larger microscale areas (rather than melting only underneath the nanowires in the case of unpassivated electrodes, since the RGO distributes the heat beyond the location of an individual nanowire). This causes the nanowire networks to distort and fail.

In addition to concerns about electrode failure, our models show that the temperature of  $5.5 \pm 0.5\%$  of the unpassivated nanowires and  $5.0 \pm 0.5\%$  of the RGO-passivated nanowires may exceed  $100\,^{\circ}\text{C}$ , which could adversely



**Figure 5.** (a) Silver nanowire electrode modelled as a random network of interconnected conducting sticks with a sheet resistance of 60 ohms/sq (red dots show nanowire junctions and sticks endpoints). (b) The distribution of current densities in individual nanowire segments (i.e. between two red dots) of the nanowire electrode.



**Figure 6.** Steady state thermal profile of a (a) AgNW, (b) RGO passivated AgNW, and (c) 130 nm thick film of ITO on PET when they are carrying the average current density encountered when 20 mA cm<sup>-1</sup> is passed across the electrode. (d) Calculated steady state temperature of individual unpassivated and passivated silver nanowires on PET substrates under different current densities.

affect other materials on top of the electrode in a device. Because organic materials are not stable at high temperatures, the maximum operating temperature for organic solar cells and LEDs is commonly below 100 °C [48 51]. This is lower than the melting point of PET and thus these devices require a more stringent thermal budget. This is another reason why Joule heating in nanowire electrodes is a major concern that needs to be addressed.

#### 3.7. Managing Joule heating

Our results show that a passivation layer alone is not sufficient to manage the Joule heating problem in silver nanowire transparent electrodes. In order to reduce Joule heating, the current density in individual nanowires needs to be reduced. One way to achieve this is to increase the density of the nanowires in the electrode so that there are more current pathways. A 20 ohms/sq AgNW electrode was modelled (figure 7(a)) and the current density distribution in the nanowire segments when 20 mA cm  $^{1}$  of current is applied across the electrode is plotted in figure 7(b). The average current density in the nanowire segments is 0.6  $\pm$  0.1  $\times$  10 $^{5}$  A cm  $^{2}$ , which is half of the average current density expected in a 60 ohms/sq AgNW electrode.

The simulation results of Joule heating in the 20 ohms/sq electrodes are shown in figures 7(c) and (d). The steady state temperature of the AgNW and AgNW-RGO samples under the average current density reached to 27 °C and 25 °C, respectively (figures 7(c) and (d)), which are 6° and 5° lower than in the 60 ohms/sq case. In the AgNW and AgNW-RGO

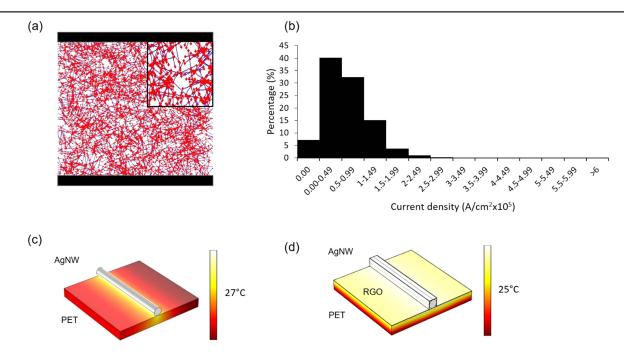


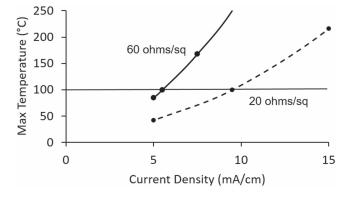
Figure 7. (a) Silver nanowire electrode model with a sheet resistance of 20 ohms/sq (red dots show nanowire junctions and endpoints). (b) The distribution of current densities in individual nanowire segments (i.e. between two red dots) of the 20 ohms/sq nanowire electrode. Steady state thermal profile of a (c) AgNW and (d) RGO passivated AgNW under the average current density of  $0.6 \times 10^5 \,\mathrm{A}\,\mathrm{cm}^{-2}$ .

electrodes, less than  $0.006\pm0.003\%$  and  $0.002\pm0.001\%$  of the nanowires, respectively, carry a current that results in a temperature above 250 °C. In addition, only  $0.45\pm0.15\%$  and  $0.15\pm0.1\%$  of the nanowires get hotter than 100 °C in the AgNW and AgNW-RGO electrodes, respectively.

Experimentally, 20 mA cm<sup>-1</sup> was passed across a 20 ohms/sq unpassivated AgNW electrode. The surface temperature was 26 °C, 6 °C lower than what was measured for the 60 ohms/sq case (figure 3(a)). The electrode failed after 25 days of sustained current compared to failure after 5 days for the 60 ohms/sq electrode. The effect of elevated currents was also assessed; under a sustained current of 50 mA cm<sup>-1</sup>, a 20 ohms/sq AgNW electrode failed after 7 days. Overall, the effect of Joule heating is reduced in NW electrodes with lower sheet resistance and the lifetime is thus increased. Increasing the nanowire density in the electrodes has drawbacks however; the electrode transparency would decrease and the material cost would increase.

A second way to reduce the current density in individual nanowires is to, of course, have less current flowing across the electrode. In a solar cell this is achieved by making the active area smaller, or in other words, making the electrical contacts (current collectors) closer together, to lower the maximum current levels which occur near a contact. This, however, reduces the efficiency of the solar cells by increasing the surface area covered by the metal bars.

Thirdly, because excessive Joule heating leading to NW breakdown is most likely to occur in areas of sparse NWs, the nanowire networks should be made as uniformly dense as possible. However, in a random film there will always be variations in local density. Assembling the NWs into a regularly spaced grid, as has been achieved with some success using NW alignment techniques [52, 53], or depositing a



**Figure 8.** Maximum nanowire temperature in electrodes with sheet resistances of 20 and 60 ohms/sq as a function of linear current density between the current collectors.

Ag grid using patterning techniques [54, 55], would result in a more uniform current distribution and thus avoid hot spots. This would extend electrode lifetimes though at a cost of a more complex deposition process.

If the temperature of a AgNW electrode needs to remain below a certain value during operation for a given device (e.g. an organic device which cannot tolerate temperatures above 100 °C), our model and simulations can calculate the maximum linear current density that can be conducted. Figure 8 shows the temperature of the hottest nanowire in 300  $\mu m \times 300~\mu m$  electrodes with sheet resistances of 20 and 60 ohms/sq. If the thermal budget of a device is 100 °C, for example, the maximum linear current density that should be conducted across the 60 ohms/sq electrode is 5.5 mA cm  $^{-1}$ . This number increases to 9.5 mA cm  $^{-1}$  for an electrode with a sheet resistance of 20 ohms/sq.

#### 4. Conclusion

This study demonstrates that the Joule heating taking place in silver nanowire electrodes when they continuously conduct current is a much more serious problem than in conventional transparent homogeneous conductive electrodes like ITO. When a 60 ohms/sq AgNW electrode conducts current at the levels incurred near the metal contacts of organic solar cells, the resulting Joule heating leads to electrode failure in 5 days. An RGO passivation layer extends the electrode lifetime, but only to 12 days since it cannot prevent the Joule heating that ultimately leads to failure due to localized melting of the plastic substrate. Modelling indicates that the temperature of some individual nanowires under current flow reach much higher temperatures than the average surface temperature recorded. This explains the observation of substrate melting and the faster failure times as compared to electrodes whose lifetimes are assessed by annealing rather than current flow. If silver nanowire electrodes are used in solar cells, OLEDs, or transparent heaters, steps must be taken to reduce the Joule heating problem to extend both the lifetime of the electrode and the rest of the device as well. Lowering the electrode sheet resistance or lowering the current flowed across the electrode would both be effective strategies.

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