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Probabilistic forecasting of the wind energy resource at the monthly to seasonal scale

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Abstract

We build and evaluate a probabilistic model designed for forecasting the distribution of the daily mean wind speed at the seasonal timescale in France. On such long-term timescales, the variability of the surface wind speed is strongly influenced by the atmosphere large-scale situation. Our aim is to predict the daily mean wind speed distribution at a specific location using the information on the atmosphere large-scale situation, summarized by an index. To this end, we estimate, over 20 years of daily data, the conditional probability density function of the wind speed given the index. We next use the ECMWF seasonal forecast ensemble to predict the atmosphere large-scale situation and the index at the seasonal timescale. We show that the model is sharper than the climatology at the monthly horizon, even if it displays a strong loss of precision after 15 days. Using a statistical postprocessing method to recalibrate the ensemble forecast leads to further improvement of our probabilistic forecast, which then remains sharper than the climatology at the seasonal horizon.

Keywords: Wind energy, Wind speed forecasting, Seasonal forecasting, Probabilistic forecasting, Ensemble forecasts, Ensemble model output statistics

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1 1. Introduction

In the recent years, energy transition has been on the forefront of political 2 and societal issues, mainly due to the increasing awareness of the need to act 3 against the climate disruption. This has led many countries to encourage the use of renewable energy. Since 2008, the European Union (EU) targets 20% 5 of renewable energy contribution to the total energy mix by 2020, and 27%6 by 2030. Consequently, wind energy has seen a major growth in Europe. To 7 give an idea of this sharp increase, the total installed wind power capacity 8 in the EU has changed from 12.9 GW in 2000 to 141.6 GW in 2015 (EWEA 9 (2016)). The actual share in the final consumption met by wind energy in 10 the EU was 11.4% in 2015 (EWEA (2016)). 11

At such scales, the variability of the wind power production due to the 12 natural intermittency of the wind resource becomes a critical issue for suc-13 cessful network integration of this source of energy (Albadi and El-Saadany 14 (2010)). As a consequence, the interest and demand for near-surface wind 15 speed forecasts has seen a major boost. Numerous methods exist for fore-16 casting wind speed at different horizons, motivated by different applications 17 (Chang (2014); Soman et al. (2010)). Many studies focus on the short-term 18 scale ranging from several minutes to one day (Carpinone et al. (2015); Gomes 19 and Castro (2012); Stesfos (2002)). Medium-term forecasting methods, rang-20 ing typically from 3 days up to 10 days, have also been investigated in depth 21 (Barbounis et al. (2006); Taylor et al. (2009); Wytock and Kolter (2013)). 22 On much longer timescales and with very different motivations, the impact 23 of the climate change on wind speeds has also been adressed (Najac et al. 24 (2009); Pryor and Barthelmie (2010); Sailor and M. Smith (2008)). 25

Whereas both relatively short and very long timescales have been thor-26 oughly studied, the intermediate timescale going from monthly to seasonal 27 horizon is a research topic for which not so many studies exist. This timescale 28 is becoming very important for the transmission system operators (TSOs) as 29 the proportion of intermittent ressources in the energy mix increases. The 30 TSOs are responsible for balancing the supply and demand of energy and 31 they are required to make seasonal projections, e.g., to guarantee the secu-32 rity of energy supply during the coming winter, which becomes more difficult 33 with the increased variability of energy production. The risk of not being 34 able to satisfy the energy demand may be quantified in terms of the notion 35 of Loss of load expectation (LOLE). Quoting from NationalGrid (2016), the 36 LOLE is a "measure of the risk across the whole winter of demand exceeding 37

³⁸ supply under normal operation. It gives an indication of the amount of time ³⁹ across the whole winter that the System Operator may need to call on a ⁴⁰ range of emergency balancing tools to increase supply or reduce demand." ⁴¹ For instance, a cold winter characterized by weaker winds than normal may ⁴² in some cases lead to a lack of energy if not enough other production means ⁴³ have been made available upstream to meet the energy demand.

Among the few existing studies of long term wind speed forecasting, (Azad 44 et al. (2014); Bilgili et al. (2007)) advocate the use of Artificial Neural Net-45 works (ANN) for forecasting average monthly wind speed. These studies give 46 an accurate estimate of the trend of the wind speed at the yearly horizon 47 but provide limited information on the wind variability at higher frequencies. 48 ANN models have also been used for forecasting daily mean wind speed at 49 the seasonal scale providing more information on the wind variability within 50 a given season for energy production evaluation (Guo et al. (2012); J. Wang 51 et al. (2015); More and Deo (2003)). 52

These studies provide 'point forecasts', which give one value for the wind 53 energy production at the specified horizon, but do not consider the uncer-54 tainty on the forecast (as a rule, forecast uncertainty is difficult to quantify 55 with neural networks since the underlying probabilistic model is not easy 56 to define). At such timescales, the idea of point forecast can be very ques-57 tionable due to the dominant chaotic nature of the atmospheric system at 58 the timescales exceeding typically 10 days. At this long-term horizon, the 59 idea of probabilistic forecasting therefore gains sense. Indeed, forecasting 60 centers such as the European Center for Medium-range Weather Forecasts 61 (ECMWF) use ensemble forecasts to take into account the uncertainty due 62 to the growing small errors in the atmospheric system. Surface wind speed 63 is a variable that is not provided by such prediction models because of its 64 complexity and interaction with the surface, but valuable information on 65 the general circulation of the atmosphere can be retrieved from such fore-66 casts. Indeed, several works have confirmed the predictability at seasonal 67 timescales of recurrent oscillating patterns in the atmosphere, such as the El 68 Nino (Cassou (2008); Owen and Palmer (1987)) or the North Atlantic Os-69 cillation (NAO) (Davies et al. (1997); Rodwell et al. (1999)). On the other 70 hand, large-scale atmospheric patterns have already been shown to partly 71 explain the surface wind speed in France at such timescales (Alonzo et al. 72 (2017)).73

In this paper, our aim is to use long-term forecasts of large-scale circulation patterns provided by ECMWF to obtain probabilistic long-term

forecasts of local surface wind speeds. Our approach is to build a prob-76 abilistic model describing the relationship between the local surface wind 77 speed and the large-scale circulation of the atmosphere, summarized by a 78 single purpose-built index. To this end we estimate the conditional proba-79 bility density function of the wind speed given the index by gaussian kernel 80 density estimation over 20 years of daily data. We next use the ECMWF 81 seasonal forecast ensemble to predict the large-scale situation of the atmo-82 sphere and the index at the seasonal timescale. The prediction of the index is 83 then plugged into our model, to obtain probabilistic forecasts of the surface 84 wind speed. The ensemble forecast displays a growing uncertainty with time 85 leading to an increase of the confidence interval width predicted by the prob-86 abilistic model. We show that the model is sharper than the climatology at 87 the horizon of one month, even if it displays a strong loss of precision after 15 88 days. Using the statistical postprocessing method EMOS (Ensemble Model 89 Output Statistics) to recalibrate the ensemble forecast leads to a further im-90 provement of our probabilistic forecast, which then remains sharper than the 91 climatology at the seasonal horizon. 92

This paper is structured as follows. Section 2 describes the method to build the probabilistic model as well as the data used in this study. In section 3, the performance of the model is assessed. In section 4, the probabilistic model is used to forecast the wind speed at the monthly and seasonal horizon by applying it to seasonal ensemble forecasts of large scale circulation patterns of the atmosphere.

99 2. Data & methods

100 2.1. Data : ECMWF reanalysis and forecasts

In this paper, we use the so called "perfect model" approach meaning that the ECMWF ERA-I reanalysis is considered as the reality. This is justified by the comparison of ECMWF products and observation, in particular for surface wind speed (Jourdier (2015)). The model is estimated and evaluated the surface wind speed retrieved from this data. We use ECMWF reanalysis for 37 years between 1 January 1979 and 31 December 2015¹.

The basic idea of this work is to link the large-scale circulation of the atmosphere with the daily mean surface wind speed distribution in France. The

¹ECMWF Data are available at http://apps.ecmwf.int/datasets/



Figure 1: a. Domain used to perform the PCA on the Z500. The red box corresponds to the domain covering France on which the model is built and assessed. b. Domain covering France and part of its neighbouring countries. The colors represents the altitude above the sea level.

large-scale circulation is well described by the 500-hPa geopotential height
(Z500) over the North Atlantic/European region (Michelangeli et al. (1995)).

We therefore retreive from the ECMWF reanalysis the daily time series of 111 500-hPa geopotential height (Z500) over a large domain that spans over North 112 Atlantic Ocean and Europe (20° N to 80° N and 90° W to 40° E), (Figure 1. 113 a), with grid size of 0.75° . The daily surface wind speed used to build and 114 evaluate the probabilistic model is also retrieved from ECMWF reanalysis. 115 The data spans the same period, but over a smaller domain which covers 116 France and parts of neighbouring countries (40.5°N to 52.5°N and -6.75°W 117 to $10.5^{\circ}E$), (Figure 1, b). 118

The 37 years of data are split into three periods. The first 20-year period 119 (1 January 1979 to 31 December 1998), is used to build and estimate the 120 model. This period is referred to as the fitting period. On the subsequent 121 13-year period (1 January 1999 to 31 December 2011), the probabilistic model 122 is evaluated and compared to the past seasonal climatology of the wind speed, 123 considered as the benchmark for wind speed forecasting at such long-term 124 horizon. The seasonal climatology is defined as the empirical distribution of 125 the daily average wind speed computed over all days in a given season of the 126 fitting period. This period is referred to as the validation period. The results 127 of the validation of our model are described in section 3. 128

On the 4 remaining years, we use the model to build probabilistic fore-129 casts of the surface wind speed at the seasonal horizon. 48 ECMWF seasonal 130 ensemble forecasts of the Z500 field over the large domain are retrieved. Sets 131 of forecasts are retrieved from 2012 to 2015, beginning on every first day of 132 each month. A major change of the assimilation system and forecast model 133 limits the use of seasonal forecasts before November 2011. Seasonal forecasts 134 provide a prediction of the Z500 at more than three months horizon, allow-135 ing to predict the surface wind speed at either monthly or seasonal horizon. 136 The seasonal ensemble forecasts consist of 41 members. Each member has 137 a slightly different initial state, so that the uncertainty on the atmospheric 138 circulation grows with the forecast horizon giving a range of different possi-139 ble states of the atmosphere. The forecasting performance of our model is 140 analyzed in section 4. 141

142 2.2. Statistical methods

In the first step of building our model we apply the Principal Component Analysis (PCA) to the Z500 variable to reduce its dimension. The outputs of the PCA are the Empirical Orthogonal Functions (EOF) describing the prevalent spatial patterns in the data, and the associated Principal Components (PC) time series which show how the state of the atmosphere projects onto these patterns. The first EOFs may be identified with the classical
large-scale weather patterns (NAO, SCA, ...) which control the European
climate variability (Casanueva et al. (2014); Folland et al. (2008); Wallace
and Gutzler (1980)). We expect the PCs to be well predicted in the seasonal
ensemble forecasts.

In the second step, we build a model giving the probability distribution 153 of the daily mean wind speed knowing the first n PCs. In other words, we 154 want to compute the conditional density $p(y|X_1,...,X_n)$ of the daily mean 155 surface wind speed Y given the PCs of Z500 X_1 to X_n . Computing this 156 conditional density directly is difficult due to the high dimension of the vector 157 (X_1,\ldots,X_n) . To overcome this issue, we use the single index approximation 158 (Delacroix et al. (2003)): we assume that the information about the PCs 159 (X_1,\ldots,X_n) may be summarized by a single scalar index 160

$$I = \beta_0 + \sum_{i=1}^N \beta_i X_i + \sum_{i=1}^N \beta_{ii} X_i^2 + \sum_{i=1}^{N-1} \sum_{j>i}^N \beta_{ij} X_i X_j,$$
(1)

where the coefficients β_0 , β_i and β_{ij} are computed by least-squares regression of the surface wind speed Y on the principal components X_1, \ldots, X_n for each location. A test of optimization of the index parameters β_i by minimization of the continuous ranked probability score (CRPS – see below) has been performed at several locations, but did not produce a significant improvement (only of the order of 0.1% of the initial CRPS).

The conditional probability density function p(y|I) is given by the standard formula

$$p(y|I) = \frac{p(y,I)}{p(I)},\tag{2}$$

where p(y, I) is the joint density of the surface wind speed Y and the index I and p(I) is the marginal density of the index. A gaussian kernel density estimator (KDE) is used to estimate the joint density and the marginal density over the period of length T:

$$\widehat{p}(y|I=i) = \frac{\sum_{t=1}^{T} K_{h_1}(y-Y_t) K_{h_2}(i-I_t)}{\sum_{t=1}^{T} K_{h_2}(i-I_t)},$$
(3)

where K_h is the gaussian kernel function writen as :

$$K_h(x) = \frac{1}{h\sqrt{2\pi}} \exp\left(-\frac{x^2}{2h^2}\right).$$
(4)

While the estimated density is not very sensitive to the choice of the kernel function, the bandwidth parameters h_1 and h_2 have a significant impact on the resulting probability density function. In our study, the bandwidth parameters have been computed by cross-validation.

178 3. Evaluation and optimization of the model

179 3.1. Criteria for model evaluation: calibration and sharpness

The performance of a probabilistic forecasting model is typically assessed 180 in terms of calibration and sharpness (Carney and Cunningham (2006); Fos-181 ter and Vohra (1998); Gneiting et al. (2007); Thorarinsdottir (2013)). While 182 calibration refers to the statistical consistency between the model and the 183 actual values of the variable to predict, sharpness is a property of the model 184 only and measures the width of the confidence intervals. Different modes 185 of calibration exist and must be considered for the model to be fully cali-186 brated. In the following, we evaluate probabilistic calibration and marginal 187 calibration. Consider a probabilistic forecast at time t in the form of a pre-188 dictive distribution function $F_t(x)$, and corresponding to the realization x_t . 180 Probabilistic calibration (Gneiting et al. (2007)) measures the compatibility 190 of the probabilistic forecast $F_t(x)$ with the actual realization x_t by means of 191 the probability integral transform (PIT) defined by $p_t = F_t(x_t)$. The fore-192 cast is said to be probabilistically calibrated if the PIT follows a uniform 193 distribution. 194

On the other hand, the <u>marginal calibration</u> (Gneiting et al. (2007)) compares the long-run distribution of the probabilistic forecast $\overline{F}(x) := \frac{1}{T} \sum_{t=1}^{T} F_t(x)$ to the long-run (climatological) distribution of the data, provided that the data is stationary. In meteorological terms, the assumption of stationarity of the data corresponds to the common assumption of the existence of a stable climate.

To evaluate the model performance we consider as the benchmark the seasonal climatology, which is often used within the wind energy industry for such long-term wind energy prediction (Pinson and Kariniotakis (2009)). Indeed, the persistence and autocorrelation of the wind disappear after 5 days at most so that the seasonal pattern is the only information that remains in absence of additional data.

207 Probabilistic calibration.

²⁰⁸ Probabilistic calibration is assessed using the Probability Integral Transform (Gneiting et al. (2007)). By applying, at each time step, the predicted



Figure 2: Example of a PIT histogram for one point in France $(49.5^{\circ}N/2.25^{\circ}E)$, for the model (a.) and the climatology (b.). The p-value of the KS test performed on the 3 days sampled PIT is indicated. In this particular example the null hypothesis of uniformly distributed PIT is not rejected at the 5% confidence interval for neither the model nor the climatology.

209

Cumulative Distribution Function (CDF) $F_t(\cdot)$, to the actual value y_t , we 210 obtain a sample $(F(y_t))_{t=1}^T$ of values in [0, 1], which must follow a uniform 211 distribution on [0,1] if the forecast is probabilistically calibrated. Unifor-212 mity of the PIT can be evaluated visually by ploting its histogram, usually 213 referred to rank histogram in meteorology, (Figure 2), or more rigorously by 214 performing a Kolmogorov-Smirnov (KS) test on the sample. The KS test 215 is to be performed on independent and identically distributed random vari-216 ables. Hamill (Hamill (2000)) shows that the correlated errors of samples can 217 lead to misinterpretation of the PIT while testing uniformity. The samples 218 thus have to be spaced far enough in space and time to be reasonably close 219 to being independent. As the daily mean wind speed is autocorrelated up to 220 time scales of about 3 to 5 days, so is the PIT. Figure 3 shows the autocor-221 relation of the entire sample of the PIT (Fig 3 a) and of the PIT resampled 222 every 3 days (Fig 3 b). After 3 days, the sampled PIT shows little or no 223 autocorrelation and the KS test is thus performed on a 3 day sampled PIT. 224

225 Marginal calibration.

Marginal calibration can be seen as a way to ensure that the actual climatology of the wind speed over the validation period is well represented by



Figure 3: Autocorrelation of the PIT of the model (bold black curves) and the climatology (green curves), as function of the time lag : for the entire PIT sample (a) and for the PIT sampled every 3 days (b). The straight line represents the spatially averaged autocorrelation, and the dashed lines represent the 20^{th} and the 80^{th} percentiles.

the model. Actual climatology refers here to the probability density function of the wind speed over the validation period (and should not be confused with the past seasonal climatology computed on the fitting period, taken as a predictive distribution of reference). Marginal calibration can be assessed visually by plotting the difference between the climatological CDF on the validation period and the mean predicted CDF given by the model.

Figure 4 shows the marginal calibration computed using the probabilistic model (black dashed line) and the past seasonal climatology (black solid line) on the validation period at one grid point in the center of France (49.5°N/2.25°E).

To highlight the fact that part of the deviation comes from the statistical 238 variations of the samples, we generate fifty random samples from the distribu-239 tion of the actual wind speed over the 17 years of validation period (actual 240 climatology) estimated by KDE. From these random samples we compute 241 fifty different resampled actual climatologies, and calculate the difference 242 between the distribution obtained for each one of them and that of the ac-243 tual climatology. The red solid line represents the mean difference between 244 the actual climatology and resampled actual climatologies, and red dotted 245 lines represent the 20^{th} and 80^{th} percentiles. We see that for this particu-246 lar point the curve corresponding to the past seasonal climatology is outside 247 this bootstrap-style confidence interval, while the curve corresponding to our 248 probabilistic foreacast is well inside it. 249

250

In order to visualize marginal calibration on a map, we compute at each



Figure 4: Difference between the actual CDF (actual climatology) on the validation period and : the mean predicted CDF (bold black solid line), the mean past seasonal climatology (black solid line), the mean of the resampled actual climatologies (red solid line), the 20^{th} and 80^{th} percentiles of the resampled actual climatologies (red dotted lines) for one point in France ($49.5^{\circ}N/2.25^{\circ}E$).

grid point the Mean Absolute Errors (MAE) between those distributions.
MAE is calculated following the equation.

$$MAE = \int_{-\infty}^{\infty} |F_{real}(Y) - F_{pred}(Y)| dy$$
(5)

The model is considered marginally calibrated if the computed MAE defined above is less than the 95th percentile of the MAE computed for the so called resampled actual climatologies.

256 Sharpness.

²⁵⁷ Sharpness refers to the width of the predictive distribution, that is to ²⁵⁸ say, the accuracy of the forecast. Confidence interval widths are therefore good diagnostics of the sharpness of a probabilistic forecasting model. In this
paper, the 90% confidence interval width is used as measure of sharpness.

²⁶¹ Continuous Ranked Probability Score (CRPS).

The Continuous Ranked Probability Score (CRPS) is a widely used scoring rule in meteorological probabilistic forecasts (Candille et al. (2007); Candille and Talagrand (2005)). It aims to evaluate both calibration and sharpness simultaneously. The CRPS for a single predictive distribution F and realization y_t is defined by:

$$CRPS(F, y_t) = \int_{-\infty}^{\infty} (F(y) - 1_{(y \le y_t)})^2 dy$$
 (6)

with $1_{(y \leq y_t)}$ being defined as :

$$1_{(y \le y_t)} = \begin{cases} 1, & \text{if } y \ge y_t. \\ 0, & \text{otherwise.} \end{cases}$$
(7)

For the entire sample of size T we define the CPRS by

$$CPRS = \frac{1}{T} \sum_{t=1}^{T} CPRS(F_t, Y_t).$$

²⁶⁸ 3.2. Optimization of the model

In this section we discuss the choice of the number of principal compo-269 nents to be used in the model. By adding more PCs, the variability of the 270 large scale circulation is better accounted for, but too many PCs can also 271 lead to overfitting and thus poor calibration of the model. Depending on the 272 region, the optimal number of PCs can be estimated. For example, although 273 the onshore wind variability can be partially explained by the large-scale at-274 mosphere circulation, smaller scale phenomena such as topography effects, 275 can have a significant influence on the wind speed. Conversely, offshore wind 276 speed is more regular and obviously not impacted by orography so that large-277 scale atmosphere circulation is the main driver of its variability at those long 278 timescales. 279

To determine the optimal number of PCs we increase their number from 5 to 30 with an increment of 5 (which corresponds to 6 different models) and evaluate the probabilistic and marginal calibration and sharpness on the validation period of 17 years for the model based on the index computedwith the corresponding number of PC.

Unexpectedly, marginal calibration shows no significant variation depending on the number of PC (no more than 10% of the statistical error), probably because of the CDF averaging effect. Conversely, probabilistic calibration and sharpness show high sensitivity to the number of PC (Figure 5). Unfortunately, on average, adding PCs sharpens the model, but also decalibrates it (Figure 5 a and c).



Figure 5: **a.** Spatially averaged p-value of the KS test performed on 3 days sampled PIT used to assess probabilistic calibration; **b.** Spatially averaged MAE between actual climatology and the predicted climatology given by the model used to assess marginal calibration; **c.** Spatially averaged 90% confidence interval width used to assess sharpness. All three graphs are plotted as function of the number of PCs used to fit the index. The black line with point markers is the average over the entire domain, the black doted line with 'x' markers is the average over the offshore part of the domain, and the black doted line with '+' markers over the onshore part of the domain.

In our final model, we use the following methodology to choose the opti-291 mal number of PCs for each location. We first test the null hypothesis that 292 the PIT follows a uniform distribution with a 95% confidence level using the 293 3 days sampled PIT for each model. If the hypothesis is not rejected for 294 any of the 6 models corresponding to different numbers of PCs, we keep the 295 model which maximizes the sharpness. If the null hypothesis is rejected for 296 all 6 models, we keep the model that maximizes the p-value of the KS test, 297 with the risk to have a non-calibrated model. 298

Figure 6 shows the result of the choice described above. Over the northern half of the domain and along the western coast of France, a large number of PC (> 15) is required to build the index meaning that the variability can be explained by shorter scale phenomena without compromising the calibration quality of the model. This results in a sharper model than when using less PCs. Conversely, for offshore wind taking a large number of PCs reduces the calibration quality.



Figure 6: Optimal number of PCs used to fit the index of the model determined using the optimization process described in the text. 'x' markers show points where the model is not calibrated (Figure 7).

In the southeast of France, over the Mediterranean coast and the sea, we 306 can find a clear signature of the orography. Offshore, the Mistral, which refers 307 to the strong wind blowing over the Mediterranean sea after being channeled 308 in the valley formed by the Alps and the Massif Central (Drobinski et al. 300 (2017)), can be identified by an intermediate number of PC (20-30). The 310 Tramontane also refers to an orographic wind blowing over the same region 311 but channeled in the valley formed by the Pyrenees and the Massif Central 312 (Brossier and Drobinski (2009)) (Fig 1 b). South of the Alps, the model is 313 not calibrated, and south of the Massif Central only 5 PCs are used resulting 314 in model that is less sharp. 315

316 3.3. Evaluation of the optimized model

Figure 7 shows the results of the KS test performed on the 3 days sampled 317 PIT given by the optimized model (Fig 7 a and b) and the climatology (Fig 318 7 c and d). The p-value for the climatology ranges between 0 and 0.8, while 319 it ranges between 0 and 0.5 for the model. The null hypothesis of adequate 320 calibration is not rejected in the North part of the domain for the model, 321 while for the climatology this hypothesis is rejected over the North part of 322 the domain. The climatology does not represent the law of the wind well 323 in those regions but the probabilistic model represents it quite well (Fig 324 7 b and d). This can be surprising as the climatology is built using 20 325 years of data which may seem to be sufficient to ensure calibration over a 326

period of the same length. Nevertheless, it has been shown that annual wind 327 trends can be significant over 1 to 2 decades in this region (Jourdier (2015)). 328 Using only the past five years of wind speed data to build the empirical 329 seasonal CDF allows to follow those trends. This sliding CDF displays a 330 null hypothesis of adequate calibration which is not rejected over the entire 331 domain. Nevertheless, it performs as well as the seasonal climatology in terms 332 of sharpness (Not shown). In the South of the domain, the model and the 333 climatology perform similarly in terms of probabilistic calibration showing 334 large non-calibrated areas. Indeed, the region is very complex and strongly 335 influenced by orography. This complexity seems to be hard to recover with 336 the information on the season only (climatology) or the information on the 337 large-scale circulation (model). 338

Figure 8 shows the MAE between the real climatological CDF over the 13-339 year validation period and, on the one hand, the averaged CDF predicted by 340 the model (Fig 8 a.) and on the other hand the climatological CDF based on 341 the 20 year fitting period (Fig 8 b). We can clearly see a strong correlation 342 between marginal calibration and probabilistic calibration. The model is 343 considered marginally calibrated if the computed MAE is inferior to the 344 95^{th} percentile of the MAE computed for the resampled actual climatologies. 345 Applying this criterion to MAE computed for the model and for the past 346 seasonal climatology gives a map (not shown) which is very similar to those 347 in Figures 7c and 7. If the model or the climatology is probabilistically 348 calibrated in a given location, it is also marginally calibrated there. Overall, 349 for both calibration criteria, the calibration of the model is at least as good 350 as that of the climatology and often much better. 351

Figure 9 displays the 90% confidence interval width averaged over the vali-352 dation period for the model (IC_{90mod}) (Fig 9 a) and the climatology (IC_{90clim}) 353 (Fig 9 b), and the ratio of IC_{90clim} to IC_{90mod} (Fig 9 c). The first striking 354 observation is that the 90% confidence interval is much larger offshore than 355 onshore for both the model and the climatology. This highlights the fact that 356 even if the wind may be more regular, it can also be much stronger because 357 of the low roughness, so that the difference between weak and strong wind 358 events is by far larger than onshore. The signature of the Mistral and Tra-359 montane is clear (Fig 9 a, b), with even larger interval width that may come 360 from the bimodal distribution of the wind speed in this region (Drobinski 361 et al. (2015)). 362

Over the entire domain, on average, the model is sharper than the climatology. The model does not perform more than 50% better than the clima-



Figure 7: Left graphs: p-value of the KS test performed on the 3 days sampled PIT of the model (a.) and the climatology (b.) and for the empirical seasonal CDF based on the last five years of wind speed (e). Right graphs: the blue area (0 value) shows the regions where the null hypothesis of adequate calibration is rejected for the model (b) and the climatology (d) and for the empirical seasonal CDF based on the last five years of wind speed (f).



Figure 8: Mean Absolute Error between the real climatological CDF over the 15 years of validation and the averaged CDFs predicted by the model (a.) and the climatological predictive CDFs based on the 20 years of calibration period (b.). 'x' marker on panel a. and '+' markers on panel b. show respectively points where the model and the climatology are not probabilistically calibrated.



Figure 9: 90% confidence interval width averaged over the validation period, for the model (a.) and the climatology (b.). Panel c. displays the ratio of the confidence interval width of the climatology over the model. 'x' and '+' markers indicate places where respectively the model or the climatology are not calibrated.

tology, except in the northeast of the domain. Over the north of France, the model is sharper than the climatology by more than 40% which is encouraging because of the high wind energy potential in those regions. Unfortunately,

over the west Atlantic ocean, the model is not as sharp as expected compared

to climatology, but still, it performs 20% to 30% better. Over the south of France, in addition to the bad calibration of the model, its performance in terms of sharpness is not as spectacular as in other regions. Again, this can be due to the complexity of the wind variability in this region.

-	-	All seasons	Winter	Spring	Summer	Fall
Model	Mean IC90	5.2	5.5	5.1	4.8	5.4
	σ	2.1	2.3	2.0	1.9	2.2
Climatology	Mean IC90	6.9	7.9	6.4	5.8	7.7
	σ	2.4	2.7	2.1	2.1	2.6
Ratio	IC_{90clim}/IC_{90mod}	1.3	1.4	1.2	1.2	1.4

Table 1: 90% confidence interval width (IC90) $(m.s^{-1})$ averaged on the validation period and on the whole domain, for all seasons, and every season separately, for the model and the climatology.

By averaging the interval width separately for each season, we can high-373 light a strong seasonal variability of the interval given by the climatology, 374 which is not so noticeable for the model (Table 1). Thus, the model shows 375 even better performance compared to the climatology in winter and fall (40%)376 sharper than climatology on average over the domain) which are the seasons 377 when the risk of high LOLE may be larger because of low temperature. The 378 model is 80% sharper than the climatology in the northeast regions in winter 379 and fall (not shown). Differences between land and sea are present for all 380 seasons, and the Mediterranean region is always more problematic. 381

The CRPS of the model and the climatology should inform us on both 382 the calibration and sharpness. It is expressed in the same units as the pre-383 dicted quantity $(m.s^{-1})$ in the case of wind speeds) and reduces to the MAE 384 for point forecasts. Figure 10 shows the mean CRPS on the validation pe-385 riod, for the model (Fig 10a), the climatology (Fig 10b) and the ratio of 386 $CRPS_{clim}/CRPS_{mod}$ (Fig 10c). All panels are very comparable to those of 387 Figure 9. Even if there is no doubt that the CRPS addresses both calibration 388 and sharpness, on average, it appears to put too much weight on sharpness. 389 For instance, over the Alps, the model is not calibrated, nevertheless the 390 CRPS has very low values, indicating that the model has good performance. 391 The CRPS values do display a very significant difference between land and 392 sea, and so does the confidence interval width. It is thus clear by comparing 393 figures 9 and 10 that the average CRPS is informative about the sharpness 394 of the model more than about its calibration quality. 395



Figure 10: CRPS of the model (a.) and the seasonal climatology (b.). 'x' marker on panel a. and '+' markers on panel b. show respectively points where the model and the climatology are not calibrated. c. is ratio of the CRPS

³⁹⁶ 4. Forecasting the wind at the monthly and seasonal horizon

397 4.1. Methodology

To make monthly / seasonal forecasts with our model, we must take into 398 account the uncertainty of the Z500 forecast, and thus also of the index. The 399 seasonal ensemble forecasts of ECMWF are based on 41 members displaying 400 a large range of possible Z500 fields. For each member, we first calculate 401 the values of the principal components by projecting the corresponding Z500 402 field onto the EOFs identified during the stage of model calibration. Next, 403 for each member of the ensemble forecast, and for each location where sur-404 face wind speed forecast is needed, we compute the corresponding index 405 value using equation (1), where the coefficients β_i were identified during 406 the stage of model calibration. This gives us an ensemble of index values 407 I_1, \ldots, I_n . From this ensemble we construct the predictive distribution of in-408 dex values, denoted by μ . This can be done in two different ways. The first 409 method (raw forecast) consists in taking simply the empirical distribution of 410 I_1, \ldots, I_n , that is, $\mu = \frac{1}{n} \sum_{k=1}^n \delta_{I_k}$, where δ_x is the point mass at point x. 411 The second method uses statistical post-processing of the ensemble forecast 412 to construct a distribution μ with better calibration / sharpness properties 413 than the raw forecast. In this paper, we use the Ensemble Model Output 414 Statistics (EMOS) method, described below, for forecast post-processing. 415 Once the predictive distribution for the index has been constructed, the 416

density of the predictive distribution for the surface wind speed given the forecast p(y|F) is obtained by integrating the density of the conditional distribution of the wind speed given the index with respect to the predictive distribution of the index:

$$p(y|F) = \int_{-\infty}^{\infty} p(y|I=x)\mu(dx), \qquad (8)$$

This should produce a less sharp model with a higher chance to be calibrated than if only the mean of the forecast ensemble is used.

423 Ensemble Model Output Statistics - EMOS.

To recalibrate and sharpen a forecast ensemble different statistical post-424 processing methods exist such as the Bayesian Model Averaging (BMA) 425 (Möller et al. (2013); Raftery et al. (2005); Sloughter et al. (2013)) or the En-426 semble Model Output Statistics (EMOS) (Gneiting et al. (2005); N.Schuhen 427 et al. (2012); Thorarinsdottir and Gneiting (2010)). EMOS aims at recali-428 brating the distribution of ensemble forecasts, but also at sharpening it. This 429 method is inspired by Gneiting et al. (2005) apart from the optimization al-430 gorithm. This method is based on the assumption that μ has a normal 431 distribution $N(m_I, \sigma_I)$, where m_I is a weighted linear combination of the 432 index values of the ensemble, 433

$$m_I = b_0 + \sum_{m=1}^n b_m I_m,$$
(9)

434 and σ_I is parameterized by

$$\sigma_I = c + d \operatorname{Var}(I), \tag{10}$$

435 where Var(I) is the empirical variance of the ensemble.

The parameters of the EMOS method b_0, \ldots, b_n , c and d are estimated 436 as follows. In the first step of the estimation procedure, on the training 437 period, set to three years in this study, we perform a linear regression of 438 the index I computed from the actual ERAI-reanalysis on the index values 439 I_1, \ldots, I_n computed from the ECMWF seasonal forecasts. This gives us 440 a first estimate of b_0, \ldots, b_n . In this first step we set c = 0 and d = 1. 441 Then, in the second step, we improve the first-step estimates by minimizing 442 the Continuous Ranked Probability Score (CRPS) of the forecasts, averaged 443

over the training period, seen as function of the parameters b_0, \ldots, b_n, c and d using the Powell algorithm (Powell (1964)).

In the end, we obtain a set of parameters $b_1, ..., b_m, c$ and d that min-446 imize the CRPS score. The minimization of the CRPS must optimizes the 447 calibration and the sharpness. We apply the obtained parameters on the 448 remaining year of forecasts to estimate the gaussian distribution $N(m_I, \sigma_I)$ 449 of the index and then integrate over this distribution as in eq. (8). The pro-450 cedure is repeated 4 times by training on three different years and testing 451 on the remaining year. This results in 48 EMOS forecasts of the daily mean 452 wind speed distribution at the seasonal horizon. 453

454 *4.2. Results*

Figure 11 displays the p-value of the KS test performed on the 3 days 455 sampled PIT of the 4 years of forecasts², for the climatology (Fig 11 a), 456 raw forecasts (Fig 11 b), and EMOS forecasts (Fig 11 c). The colorbar is 457 designed to test the null hypothesis at 95% confidence. Regarding this test, 458 forecasts are not calibrated in the northeast part of France which disagrees 459 with the test performed on the validation period. As this behaviour is quite 460 comparable to the climatology, this suggests that the fitting period of 20 461 years used to build the model and climatology may not be representative 462 enough of the wind in the forecasting years in those regions. 463

Figure 12 shows the ratio IC_{90clim}/IC_{90mod} averaged at 15 days (Fig 12 a.), monthly (Fig 12 b.) and seasonal horizon (Fig 12 c.) for raw forecasts (black dots) and EMOS forecasts (green dots), for all forecast years.

The accuracy decreases with the forecast horizon. It appears that the forecast is quite sharp within 15 days and deteriorates significantly for larger horizons. The largest deterioration occurs between November and February. In spring and summer, forecasting performance does not seem to be highly sensitive to the forecast horizon.

⁴⁷² Moreover, EMOS forecasts only significantly improves the accuracy with ⁴⁷³ respect to raw forecasts, in winter and fall, especially at monthly and seasonal ⁴⁷⁴ horizon. Raw and EMOS forecasts at 15 days horizon are almost always

²Note that we only have 48 independent forecasts which is not enough to test calibration. To get around this difficulty, we use forecasts obtained at the same date for different horizons (3 days, 6 days, 9 days, ..., 30 days) as if they were independent. Autocorrelation analysis shows that they are indeed uncorrelated. Each forecast thus corresponds to 10 data points.



Figure 11: p-value of the KS test performed on the 3 days sampled PIT of the 4 years forecasts, for the climatology (a.), raw forecasts (b.), and EMOS forecasts (c.). Blue areas correspond to regions where the null hypothesis of calibration is rejected at the 5% confidence level.

better than the climatology. The improvement with EMOS optimization
does not seem to be very large at this horizon, most probably because the
distribution of the index is already very sharp. EMOS forecasts still slightly
improve raw forecasts by about 5% in the beggining and at the end of the
year.

The seasonal variability described in Table 1 is recovered at the 15 days 480 and monthly horizon, which is encouraging. At the seasonal horizon, raw 481 forecasts performance does not display a strong seasonal variability and the 482 ratio is close to one, so the model does not perform better than the clima-483 tology. EMOS forecasts performance displays an even lower intra-annual 484 variability but the ratio is systematically around 1.10. This is a very in-485 teresting result as it shows that there is a valuable statistical information 486 on the local surface wind speeds in the seasonal forecasts of the large-scale 487 circulation post-processed using the EMOS method, which leads to a 10%488 improvement over the climatology on average even at this long timescale. 489

Figures 13, 14 and 15 show the ratio IC_{90clim}/IC_{90mod} for each year of forecasts, respectively at 15 days, monthly and seasonal horizons, for raw forecasts (top) and EMOS forecasts (bottom). A sharp decrease of the ratio can be seen between figures 13 and 14. Comparatively, the acuracy decrease



Figure 12: Ratio IC_{90clim}/IC_{90mod} at 15 days (a.), monthly (b.) and seasonal horizon (c.) for every raw forecasts (black cross) - the black slight line represents the mean ratio ; and EMOS forecasts (green dots) - the green bold line represents the mean ratio. Four forecasted years are 2012, 2013, 2014, 2015.

is less pronounced, between figure 14 and 15. In the northeast of the domain,
the ratio is the highest so that the model seems to be very sharp, especially
at the 15 days horizon for the year 2015. This could be the cause of the
decalibration of the model (Fig 11).



Figure 13: Ratio of IC_{90clim} over IC_{90mod} averaged over 12 seasonal forecasts, for forecasted years 2012 (a., e.), 2013 (b., f.), 2014 (c., g.), and 2015 (d., h.) at 15 days horizon for raw forecasts (top) and EMOS forecasts (bottom)

498

Those figures also show the efficiency of the EMOS method to reduce



Figure 14: Same as figure 13 for monthly horizon forecasts.



Figure 15: Same as figure 13 for seasonal horizon forecasts.

the uncertainty on the index and thus to highly sharpen the model so that forecasts at the seasonal horizon give more information on the wind than the climatology which is at this moment widely used for such long-term wind energy evaluation. The EMOS forecasts display a consistent spatial pattern in terms of accuracy for any forecast horizon which is not the case for raw

forecasts. Indeed, the performance of raw forecasts displays a noticeable 504 inter-annual variability. For instance, at the monthly horizon, forecasted 505 year 2015 is comparable to the climatology in the east of the domain while 506 year 2012, 2013, and 2014 are sharper than the climatology in this part of 507 France. It again highlights the added value of EMOS forecasts compared to 508 raw forecasting method, even if a larger sample of forecasted years should be 509 analysed to confirm this behaviour. The Mediterranean region is the region 510 where the model performs the worst compared to the climatology. This result 511 confirms what was found on the validation period. For EMOS forecasts, the 512 spatial pattern of the ratio is very comparable to the Fig 9 for any forecast 513 horizon and for all years. This is not as clear for raw forecasts. It means 514 that the uncertainty on the ensemble forecast is highly reduced by EMOS 515 method, but moreover that this method reduces the inter-annual variability 516 of the uncertainty of the ensemble. 517

518 5. Conclusion

A probabilistic model is proposed to predict daily wind speed distribu-519 tion from a few days to seasonal timescale. It is compared to the climatology 520 which is often the reference used as the best seasonal forecast for energy man-521 agement. The study shows that the model is better statistically calibrated 522 than the climatology and is able to follow very long-term trends of the wind 523 speed. On average over France, the model is shown to be 30% sharper than 524 the climatology. It is shown to be more accurate than the climatology espe-525 cially onshore, in the northwest regions and in winter and fall. 526

We apply the probabilistic model to the seasonal forecast ensemble of 527 ECMWF. We test two methods to forecast wind speed with these ensembles. 528 The first method uses the empirical density of the raw calculated index, 529 and the second estimates the density of the calculated index by optimizing 530 calibration and sharpness of the ensemble using the EMOS statistical post-531 processing technique (Gneiting et al. (2005)). We show that the model is 532 able to be more precise than the climatology at 15 days and monthly horizon 533 using both methods and that at the seasonal horizon, the EMOS method is 534 systematically more precise than climatology. 535

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