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Influence of fluid-flow direction on effective permeability of the vertebral end plate: an analytical model

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Convective transports in the vertebral end plate (VEP) play a significant role in the homeostasis of the spine. A few studies hypothesised that the hydraulic resistance or effective permeability of the VEP could be dependant upon fluid-flow direction. Results were influenced by species, region of interest within the end plate and pathology. Some results were contradictory. We propose an analytical model based on steady-state Newtonian flows in capillary media to develop a phenomenological analysis of convective transport through the VEP. This dependence was established using a biquadratic analytical function involving porosities of subchondral bone, capillary bed and cartilage end plate. Discussion of results provided a theoretical justification for variable and/or contradictory experimental results concerning the amount of energy lost by fluid during its course through the end plate. Tissue porosities and, especially, those relative to the capillary bed could strongly influence the dependence of fluid energy loss on flow direction and could potentially modify tissue homeostasis related to the day and night cycle.

Keywords: convective transport; permeability; hydraulic resistance; vertebral end plate; spine

1. Introduction

Solute transport contributing to the metabolic pathways of intervertebral disc (IVD) cells is induced by diffusion and convection. Convective transport is of utmost importance to large solutes such as glycosaminoglycans, whereas diffusion drives the exchange of small solutes such as glucose, oxygen and lactate (Holm et al. 1981; Katz et al. 1986; Ferguson et al. 2004; Urban et al. 2004). *In vivo* phenomena involve coupling effects. The pumping effect due to day and night cycles plays a significant role in nutrient transport and waste clearance, while modifying diffusion gradients along with osmotic and electrical potentials (Bibby et al. 2005; Grunhagen et al. 2006; Soukane et al. 2007).

The annulus fibrosus periphery and the vertebral end plate (VEP) are the two pathways for nutrient transport by convection (Roberts et al. 1989; Houben et al. 1997), but the role of the VEP zone is preponderant. This nutritive pathway is vulnerable and IVD disorders generally show histological modifications of its constitutive tissue (Urban et al. 2004). Correlations between variation in transport properties of the VEP and IVD alteration have been detected by marked pH diminution in IVD presenting degenerative radiographic signs (Nachemson et al. 1970). This observation was later confirmed by studies showing that diminution of the permeability was modifying both diffusive and convective transports (Sélard et al. 2003; Ferguson et al. 2004).

Roberts et al. (1993) suggested that onset/progression of scoliosis may be a consequence of a disorder of VEP permeability. A decrease of nitrogen protoxide diffusion was observed in the convexity of neuromuscular scoliosis *in vivo* (Urban et al. 2001) and correlated with calcifications of the cartilage end plate (CEP) on radiographs. A decrease of VEP effective permeability was also quantified *ex vivo* at the apex of an experimental scoliosis in a porcine animal model (Laffosse 2008).

Because fluid migrates through a non-symmetrical biological tissue stacking sequence with different porosities, the question of dependence of energy loss on fluid to flow direction can be raised. The energy loss was expressed using the hydraulic resistance or the effective permeability of tissue. It was shown that it was dependant upon the type of investigated tissue (isolated CEP or global end plate), region of interest (disc level, central of peripheral zone of the VEP), pathological modification of the spine and species. In normal tissue, we demonstrated that results varied with growth (Accadbled 2007; Accadbled, Ambard et al. 2008; Accadbled, Laffosse et al. 2008) and flow direction (Ayotte et al. 2001; Laffosse et al. 2005; Accadbled, Laffosse et al. 2008). Pathology has a significant influence on VEP's properties (Rajasekaran et al. 2004). In a scoliosis animal model (Laffosse 2008; Odent et al. 2008), we highlighted some variations though not statistically significant. Contradictory results have also

been reported (Ayotte et al. 2000; Ayotte et al. 2001; Laffosse et al. 2005).

Notwithstanding the role of fluid-flow direction on energy loss that has been quantified objectively with *in vitro* studies, the theoretical rationale is still an open problem. In this paper, we propose an analytical model based on steady state flows in capillaries to develop a phenomenological analysis of convective transport through the VEP. Then we evaluate how such a model could support a unified theoretical justification of multiple experimental results.

2. Materials and methods

The analytical model dealt with the convective transport through the VEP. Governing equations of transport were established assuming flows of Newtonian fluid with a low Reynolds number. The exchanges were isothermal, gravity effects were negligible and porous substrates were not deformable under fluid pressure. Governing equations were derived from the generalised Bernoulli's theorem (Idelchik 2001). Flow was investigated using a capillary-type model with evolving cross-sections and no physico-chemical interactions with the interfaces. The model described in Figure 1 was established at the scale of a group of connected pores. Subchondral bone and CEP the cross-section of which were, respectively, s_b and s_c were connected by the capillary bed represented by a rectilinear micro channel of cross-section s_{cb} and length l_{cb} . *Flow in* and *flow out* represented, respectively, flow from the vertebral body to the IVD (trajectory: A-B-C-D) and flow from the IVD to the vertebral body (trajectory: D-C-B-A).

2.1 Governing equations

The restriction of flow coming from the vertebral body generated an energy loss, which was associated with the difference in pressure between the flow in pressure p_{sb} (point A) and the pressure p_{cb} in the capillary bed (point B). The differential pressure (or singular pressure drop) is expressed by the Darcy–Weisbach equation (1). It is dependant upon the square of the down stream fluid velocity after the cross-section restriction, the fluid density and an empirical shape coefficient limited to 0.6 (Rohsenow 1985; Dullien 1992; Idelchik 2001). In the application to the VEP modelled in Figure 1, v_{cb} is the fluid velocity into the connective capillary, ρ_f is the fluid density and c_{sb-cb} is the shape coefficient relative to the flow restriction:

$$p_{sb} - p_{cb} = \rho_f v_{cb}^2 (1 - c_{sb-cb}). \quad (1)$$

The flow into the capillary (point B, point C) induced an energy loss described by the differential pressure (or regular pressure drop) as expressed by Equation (2). With a constant cross-section, the pressure drop is proportional to the fluid velocity (Rohsenow 1985; Dullien 1992; Idelchik 2001). In our application, v_f is the fluid dynamic viscosity, s_{cb} is the cross-section of the capillary and l_{cb} is its length:

$$\Delta p_{cb} = \frac{8\pi v_f l_{cb}}{s_{cb}} v_{cb}. \quad (2)$$

The flow opening into the cartilaginous layer induced the energy loss described by Equation (3) (Rohsenow 1985; Dullien 1992; Idelchik 2001). This equation expresses the

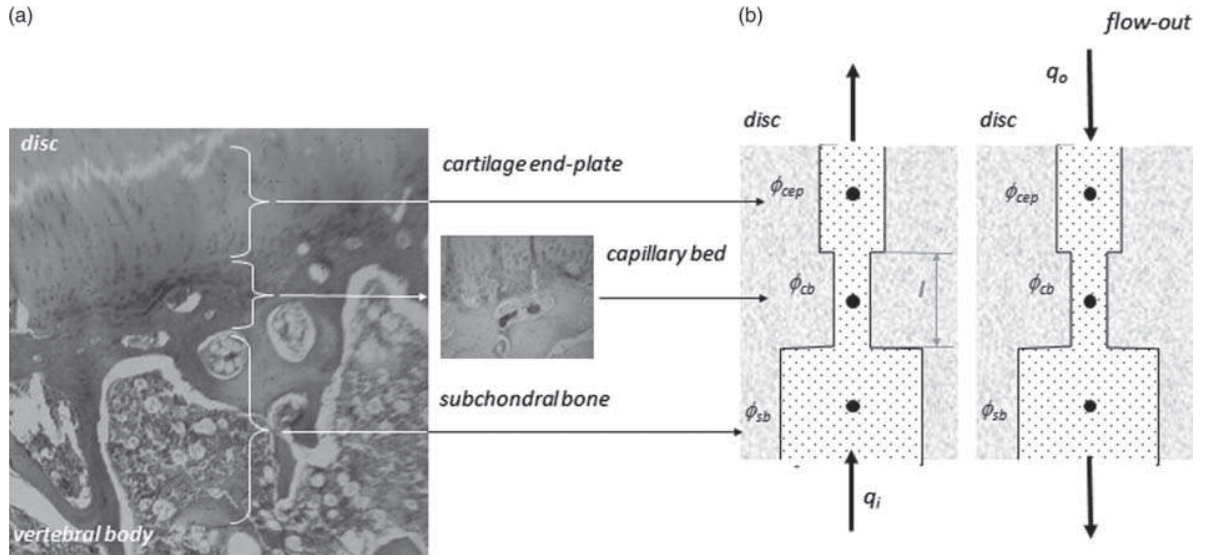


Figure 1. (a) Histological slice showing the stacking sequence of subchondral bone, capillary bed and CEP (Laffosse 2008). (b) Capillary model representing the convective exchanges between IVD and vertebral body. 'Flow-in' (rate q_i) described the fluid motion from the vertebral body towards the disc; 'flow-out' (rate q_o) described the fluid motion from the disc towards the vertebral body. In the zone of interest, the simplified model of the capillary bed was a tubular micro channel of length l_{cb} associated with the porosity ϕ_{cb} .

differential pressure (or singular pressure drop) measured between point C (p_{cb}) and point D (p_{cep}). The flow-out cross-section is s_{cep} . The pressure drop is proportional to the square of the fluid velocity in the larger section and the shape coefficient depends on the ratio of cross-sections (Rohsenow 1985; Dullien 1992; Idelchik 2001):

$$p_{cb} - p_{cep} = \rho_f v_{cb}^2 \frac{s_{cb}}{s_{cep}} \left(1 - \frac{s_{cb}}{s_{cep}} \right). \quad (3)$$

The overall relative pressure $\Delta p_{flow-in}$ expresses the energy lost by the fluid. It is the sum of the three successive losses expressed by Equations (1)–(3), and this results in Equation (4):

$$\begin{aligned} \Delta p_{flow-in} = p_{sb} - p_{cep} = & \frac{8\pi\nu_f l_{cb}}{s_{cb}} v_{cb} \\ & + \rho_f v_{cb}^2 \left[\frac{s_{cb}}{s_{cep}} - \left(\frac{s_{cb}}{s_{cep}} \right)^2 + 1 - c_{sbcb}^{-1} \right]. \end{aligned} \quad (4)$$

The ratio of pressure $\Delta p_{flow-in}$ by flow rate q_i is the overall hydraulic resistance R_i opposed to the fluid in its course through the stacking sequence of tissue: subchondral bone, capillary bed and CEP. The reciprocal expression of hydraulic resistance is the effective permeability κ_i at Darcy scale. The flow rate is constant whatever the zone of interest and we used the flow rate into the capillary bed, i.e. $q_i = s_{cb} \cdot v_{cb}$. Finally, Equation (4) was modified to obtain the expression of hydraulic resistance and effective permeability in *flow-in* in the form of Equation (5):

$$\begin{aligned} R_i = \kappa_i^{-1} = & \frac{\Delta p_{flow-in}}{q_i} = \frac{8\pi\nu_f l_{cb}}{s_{cb}^2} \\ & + \frac{\rho_f q_i}{s_{cb}^2} \left[\frac{s_{cb}}{s_{cep}} - \left(\frac{s_{cb}}{s_{cep}} \right)^2 + 1 - c_{sbcb}^{-1} \right]. \end{aligned} \quad (5)$$

A similar methodology was used to obtain the *flow-out* hydraulic resistance R_o and the effective permeability κ_o . In this configuration, the flow direction was CEP – capillary bed – subchondral bone. Equation (1) involving the updated shape coefficient c_{cep-cb} described the pressure loss due to the restriction of flow between the CEP (point D) and the capillary bed (point C). Equation (2) was unchanged to express the energy loss between the capillary bed (point C) and capillary bed (point B). Equation (3) is used to express the energy loss when the fluid is flowing from the capillary bed (point B) to the subchondral bone (point A), with s_{cep} replaced by s_{sb} . Finally, hydraulic resistance and effective permeability in *flow-out* are given by Equation (6):

$$\begin{aligned} R_o = \kappa_o^{-1} = & \frac{\Delta p_{flow-out}}{q_o} = \frac{p_{cep} - p_{sb}}{q_o} = \frac{8\pi\nu_f l_{cb}}{s_{cb}^2} \\ & + \frac{\rho_f q_o}{s_{cb}^2} \left[\frac{s_{cb}}{s_{sb}} - \left(\frac{s_{cb}}{s_{sb}} \right)^2 + 1 - c_{cep-cb}^{-1} \right]. \end{aligned} \quad (6)$$

To take into account a group of capillaries in a zone of interest, we assumed that the distribution pattern of interconnected pores is homogenous and the flow rate is identical in all capillaries of the zone. This allowed replacing the cross-sections s_{sb} , s_{cep} and s_{cb} in Equations (5) and (6) with the subchondral bone porosity ϕ_{sb} , the CEP porosity ϕ_{cep} and the capillary bed porosity ϕ_{cb} , respectively. The difference of Equation (5) and Equation (6) resulted in Equation (7) expressing the influence on fluid-flow direction upon the hydraulic resistance and effective permeability at the capillary scale:

$$\Delta R = R_o - R_i = \kappa_o^{-1} - \kappa_i^{-1} = \frac{\rho_f}{s_{cb}^2} q_i (\alpha \beta_o - \beta_i),$$

with

$$\begin{aligned} \beta_i = & \left(\frac{\phi_{cb}}{\phi_{cep}} \right) - \left(\frac{\phi_{cb}}{\phi_{cep}} \right)^2 + 1 - c_{sbcb}^{-1} \\ \beta_o = & \left(\frac{\phi_{cb}}{\phi_{sb}} \right) - \left(\frac{\phi_{cb}}{\phi_{sb}} \right)^2 + 1 - c_{cep-cb}^{-1} \quad \text{and} \quad \alpha = \frac{q_o}{q_i}. \end{aligned} \quad (7)$$

We assumed that in quasi-static behaviour, *flow-in* and *flow-out* rates were identical, i.e. $\alpha = 1$. Flow dependence on shape coefficients was of second order and $c_{sbcb} \approx c_{cep-cb}$. These supplementary hypotheses allow transforming Equation (7) into the biquadratic Equation (8), where two variables were introduced: a expressed the ratio of capillary bed porosity ϕ_{cb} over the subchondral bone porosity ϕ_{sb} and b expressed the ratio of capillary bed porosity ϕ_{cb} over CEP porosity ϕ_{cep} . Fluid viscosity ρ_f , capillary bed cross-section s_{cb} and flow rate q_i were controlled parameters. Finally, the investigation of the dependence of hydraulic resistance and effective permeability on the VEP to fluid-flow direction consisted in studying the evolution of function $\Delta\beta$:

$$\begin{aligned} \Delta R = R_o - R_i = & \frac{\rho_f}{s_{cb}^2} q_i (\beta_o - \beta_i) = \delta \Delta\beta \\ = & \delta(a - b)(1 - a - b), \end{aligned} \quad (8)$$

with

$$a = \frac{\phi_{cb}}{\phi_{sb}}, \quad b = \frac{\phi_{cb}}{\phi_{cep}} \quad \text{and} \quad \delta = \frac{\rho_f}{s_{cb}^2} q_i.$$

3. Results

Governing Equation (8) describing the dependence of energy loss on fluid-flow direction is plotted in Figure 2. First, it appeared that two groups of singular values, $b_o = 1 - a$ and $b_o = a$, could cancel $\Delta\beta$. The intersection of these groups of solutions is $b_o = a = 0.5$. As the porosity of the CEP ϕ_{cep} is a priori lower than that of subchondral bone ϕ_{sb} , b is strictly lower than a . The definition domain of function $\Delta\beta$ is $a \in]0; 1]$ and $b \in]a; 1]$.

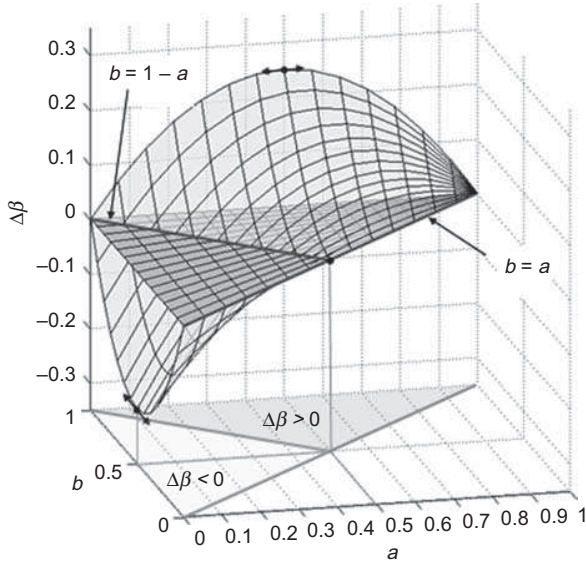


Figure 2. Function $\Delta\beta$ described the dependence of energy loss on fluid-flow direction in the form of a biquadratic function of porosity ratios (a, b); a is the ratio of capillary bed porosity ϕ_{cb} over subchondral bone porosity ϕ_{sb} , and b is the ratio of capillary bed porosity ϕ_{cb} over CEP porosity ϕ_{cep} .

For $a \in]0; 0.5]$ and $b \in]a; 1 - a]$, $\Delta\beta$ was negative which meant that the hydraulic resistance in *flow-out* was superior to that in *flow-in*, i.e. $R_o > R_i$. Effective permeability followed the reverse relationship, i.e. $\kappa_o < \kappa_i$. Opposite results were obtained for $a \in]0; 0.5]$ and $b \in]1 - a; 1]$ and for $a \in]0.5; 1]$ and $b \in]a; 1]$. Positive value of $\Delta\beta$ described a weaker effective permeability in *flow-out* compared to that in *flow-in*, i.e. $\kappa_o > \kappa_i$ and $R_o < R_i$.

Secondly, values that cancelled the first derivative of $\Delta\beta$ referring to a were $a = 0.5$ whatever be the value of b with $\Delta\beta$ positive. Similarly, nil first derivative referring to b was obtained for $b = 0.5$ whatever be the value of a , with $\Delta\beta$ negative. As shown in Figure 2, greater absolute values of $\Delta\beta$ were obtained for these particular values of a and b .

We found that alternation of $\Delta\beta$ sign describing the dependence of energy loss on flow direction was obtained for the particular value $b_0 = 1 - a$. When b_0 and a were replaced by their value, a relationship between tissue porosities of the VEP was obtained. This is expressed by Equation (9) in which we introduced ε representing the ratio of CEP porosity over the subchondral bone porosity. Physiologically, ε was much lower than 1, and this allowed the linearisation in ε of Equation (9) to be obtained by implementing a Taylor expansion at the first order:

$$\begin{aligned} \phi_{cb} &= \phi_{cep}(1 + \varepsilon)^{-1} \\ &\approx \phi_{cep}(1 - \varepsilon) + O(\varepsilon^2) \text{ with } \varepsilon = \frac{\phi_{cep}}{\phi_{sb}} \ll 1. \end{aligned} \quad (9)$$

Equation (9) associated with the solutions of Equation (8) allowed highlighting the role of capillary bed porosity

ϕ_{cb} in energy loss, hydraulic resistance and effective permeability of the VEP. As expressed by Equation (10a), it was found that effective permeability of the VEP might be independent of fluid-flow direction for a threshold value of ϕ_{cb} . Alternatively, perturbations of capillary bed porosity might induce flow-direction dependence as shown in Equations (10b) and (10c):

$$\begin{aligned} &\text{if } \phi_{cb} = \phi_{cep}(1 - \varepsilon), \\ &\text{then } b = b_0 \Leftrightarrow \Delta\beta = 0, \text{ so } R_o = R_i \text{ and } \kappa_o = \kappa_i; \end{aligned} \quad (10a)$$

$$\begin{aligned} &\text{if } \phi_{cb} \leq \phi_{cep}(1 - \varepsilon), \\ &\text{then } b < b_0 \Leftrightarrow \Delta\beta < 0, \text{ so } R_o < R_i \text{ and } \kappa_o > \kappa_i; \end{aligned} \quad (10b)$$

$$\begin{aligned} &\text{if } \phi_{cb} > \phi_{cep}(1 - \varepsilon), \\ &\text{then } b > b_0 \Leftrightarrow \Delta\beta > 0, \text{ so } R_o > R_i \text{ and } \kappa_o < \kappa_i. \end{aligned} \quad (10c)$$

4. Discussion and conclusion

We proposed an analytical model based on Newtonian flow in capillaries to express the relationship between the stacking sequence of tissue and energy lost by fluid in its course through the VEP. The dependence of hydraulic resistance and effective permeability upon fluid-flow direction was established using ratios of porosities of subchondral bone, capillary bed and CEP into a biquadratic analytical function denoted by $\Delta\beta$, which could be nil, and it could alternate between positive and negative values.

In Ayotte et al. (2001), ovine VEP resistance to flow was lower for *flow-out* than for *flow-in*. This result corresponded to a positive value of $\Delta\beta$. According to our model, the ratio of capillary porosity ϕ_{cb} over cartilage porosity ϕ_{cep} defined by b corresponded to values greater than 0.5.

With an asymmetric tether in a porcine animal model developed by us (Accadbled 2007), we found that effective permeability was greater for *flow-out* than for *flow-in*. This was confirmed by animal studies based on an ovine growing model (Accadbled, Laffosse et al. 2008). The differences were bolder in the central zone of the VEP, which corresponded to the location of the nucleus pulposus. The associated finding from our model was $\Delta\beta$ negative. In that case, the ratio a of capillary porosity ϕ_{cb} over subchondral bone porosity ϕ_{sb} corresponded to values lower than 0.5.

Another animal study concerned a scoliosis porcine model (Laffosse 2008; Odent et al. 2008). Discrepancies were observed between *flow-in* and *flow-out* permeabilities, but they were not proved significant. This case could reveal one of the singular values $b_0 = 1 - a$ of our analytical model corresponding to a function $\Delta\beta$ close to zero.

Finally, comparison with experimental results from the literature corroborated the findings from the analytical model unified by Equations (10). Assuming that the cartilage porosity was much lower than that of the subchondral bone, we saw that the modification of capillary bed porosity ϕ_{cb} relative to cartilage and subchondral bone porosities could induce the alternation or cancellation of $\Delta\beta$ and it could consequently explain how the energy loss could be flow-direction dependent. Capillary bed obstruction, translated into a decrease of capillary porosity ϕ_{cb} in the analytical model, could induce a sclerosis of the CEP, and by cascade could affect convective transports and, therefore, alter diffusion of nutriment. Potentially, this could result in a disorder of tissue homeostasis (Ayotte et al. 2000; Grignon et al. 2000).

Experimental studies allowed assuming that porosity ratios were dependant upon species, region of interest within the VEP and mechanical stimuli that conditioned remodeling of the vertebral segment, especially in conditions such as scoliosis. Our analytical model could support the main tendencies observed *in vivo*, but its formulation was dependant upon ratio of porosities scarcely reported in the literature, especially for pathological tissues. We obtained $a = 0.1$ and $b = 0.4$ using approximate values of capillary bed porosity $\phi_{cb} \approx 0.02$, CEP porosity $\phi_{cep} \approx 0.05$ and subchondral bone porosity $\phi_{sb} \approx 0.2$ (Cowin 2001; Ferguson et al. 2004). For these values, Equation (8) and Figure 2 confirmed that $\Delta\beta$ was negative meaning that exudation of fluid from the IVD was easier than absorption. According to phenomena observed *in vivo*, the mathematical solutions could evolve significantly, because the model was strongly dependant upon the ratio of CEP porosity over subchondral bone porosity. We also pointed out a singular value of 0.5 for ratios a and b for which absolute values of difference of flow resistance were maximal. Could these theoretical values be realistic *in vivo*, and how pathology could alter these values? These questions require further histology and imaging investigations, especially with pathological tissue. In any case, the analytical model allowed confirming that small perturbations of porosities of the VEP could induce significant modifications of convective transport in the vertebral segment.

The capillary bed was modelled using a rectilinear micro channel with constant cross-section. This is a simplified model and such connections might show tortuosity with evolving cross-sections *in vivo*. For a more complex description of the microarchitecture, a pure analytical modelling approach found its limits and the translation towards a numerical 3-D model could be suggested. Even if this perspective seemed attractive, the reliability of the computational model would be strongly dependant on the accuracy of the geometry segmentation and reconstruction, which would be challenging at this scale.

To implement our analytical approach. We assumed that flow rates were identical in and out to implement our

analytical approach. The assumption was valid in quasi-static flows and also consistent with *ex vivo* experimental procedures (Ayotte et al. 2001; Laffosse et al. 2005; Accadbled, Ambard et al. 2008), but the relevance of the model could be enhanced taking into account the dynamic effects over the day and night cycle. This approach would require a more complete thermodynamic approach involving time distributions of loadings and induced fluid–structure interactions as well as energetic potentials, such as osmotic and electrochemical potentials, driving diffusive flows of nutriment and modifying relative pressure and flow rates.

Finally, we showed that the proposed analytical model based on fluid flow in capillary medium could contribute to the phenomenological analysis of convective flow through the VEP. It helped to obtain a plausible response to the question of dependence of energy loss on flow direction by fluid in its course through the VEP.

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Conflict of interest. The authors hereby declare they have no conflict of interest.

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