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Discussion of "Water Distribution System Analysis: Newton-Raphson Method Revisited" by M. Spiliotis and G. Tsakiris

Dejan Brkić

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Discussion of "Water Distribution System Analysis: Newton-Raphson Method Revisited" by M. Spiliotis and G. Tsakiris August 2011, Vol. 137, No. 8, pp. 852-855. DOI: 10.1061/(ASCE)HY.1943-7900.0000364

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Corresponding Author:	Dejan Brkic, Ph.D. in Petroleum Eng. - Beograd, SERBIA
Corresponding Author Secondary Information:	
Corresponding Author's Institution:	-
Corresponding Author's Secondary Institution:	
First Author:	Dejan Brkic, Ph.D. in Petroleum Eng.
First Author Secondary Information:	
Order of Authors:	Dejan Brkic, Ph.D. in Petroleum Eng.
Order of Authors Secondary Information:	

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I do not have any tables in my text; (Etable 1 and Etable 2 are submitted as Electronic Annexes to the discussion; do not embed them into the text, instead provide a link to this material). This is possible for technical papers, technical notes and case studies since there is separate item description in editorial system for such purposes. This item description does not exist for discussions. So I have uploaded them as figures. Please, advise me if you have additional requests with these materials.

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Discussion of "Water Distribution System Analysis: Newton-Raphson Method Revisited" by M. Spiliotis and G. Tsakiris

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DOI: 10.1061/(ASCE)HY.1943-7900.0000364

My discussion contains Supplemental Data; Electronic tables, E-table 1 and E-table 2 (the Excel files with calculations converted in PDF). They can be attached to the electronic version of the discussion in the ASCE Library.

Sincerely yours,

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Dejan Brkić, Ph.D., Petroleum and Natural Gas Engineer, Strumička 88, 11050 Belgrade, Serbia, e-mail: dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Spiliotis and Tsakiris (2011) show the nodal formulation for water distribution system analysis using the head-loss dependent Jacobian. Some issues about the node formulation of the discussed problem will be commented on here. Also, as an addition to the discussed paper, the procedure with pressure drop formulation of the Jacobian will be presented where the method is similar to, but different from Spiliotis and Tsakiris (2011). The procedure uses elements of the methods by Cross (1936), Shamir and Howard (1968) and Epp and Fowler (1970).

As shown in Brkić (2011a), all methods for the analysis of looped water distribution systems can be divided in two general groups: loop oriented and node oriented methods. To date, all loop oriented methods contained a flow independent Jacobian while all node oriented methods contained a pressure drop (or a head loss) independent Jacobian. In their recent paper, Simpson and Elhay (2011) show an improved loop method with the flow-dependent Jacobian where the problem is how to find the derivative of the implicitly given equation by Colebrook (1939) which is in a common use as a standard for the calculation of flow friction, λ [the Colebrook equation is Eq. 1b in the discussed paper (the Darcy friction is noted as f in the discussed paper and in this discussion as λ)]. The problem can be addressed by using some of the available explicit approximations of the Colebrook equation [Swamee and Jain (1976)

approximation is used in Simpson and Elhay (2011)], but as shown in Brkić (201x) it is not always possible to find a balance between accuracy and complexity among many available approximate formulas (Brkić 2011b). On the other hand, Spiliotis and Tsakiris (2011) show the node oriented method with the head-loss dependent Jacobian. In general, the convergence properties of the nodal formulation are not as good as those of the looped version, but, on the other hand, the derivative of the implicitly given Colebrook equation used in the proposed pressure drop or head-loss dependent Jacobian can be easily calculated when the nodal method is employed. To accomplish the solution of the problem in the pressure drop dependent form, Eq. 13, is used for non-iterative calculation of flow Q.

$$F = Q = \pi \cdot \sqrt{\frac{\Delta p \cdot D^5}{2 \cdot L \cdot \rho}} \cdot \log\left(\frac{2.51 \cdot \nu \cdot \sqrt{L \cdot \rho}}{\sqrt{2 \cdot \Delta p \cdot D^3}} + \frac{\varepsilon}{3.7 \cdot D} \right) \tag{13}$$

Eq. 13 is derived combining the Darcy-Weisbach equation, $\lambda = \Delta p \cdot \pi^2 \cdot D^5/(8 \cdot L \cdot \rho \cdot Q^2)$, and the equation for the Reynolds number, $Re = 4 \cdot Q/(D \cdot \pi \cdot \nu)$ as in Eq. 14, and then combining the Colebrook equation and again the Darcy-Weisbach equation to produce Eq. 13.

$$\mathrm{Re} \cdot \sqrt{\lambda} = \frac{4 \cdot Q}{D \cdot \pi \cdot \nu} \cdot \sqrt{\frac{\Delta p \cdot \pi^2 \cdot D^5}{8 \cdot L \cdot \rho \cdot Q^2}} = \frac{1}{\nu} \cdot \sqrt{\frac{2 \cdot \Delta p \cdot D^3}{L \cdot \rho}} \tag{14}$$

In that way, friction factor, λ, is eliminated from Eq. 13 which implies that flow, Q, in a single pipe can be calculated using the implicit Colebrook equation but also at the same time, avoiding iteration (Swamee and Jain 1976). On the contrary, standard procedure requires the iterative calculation of flow friction λ, using the implicitly given Colebrook equation [Eq. 1b of the discussed paper] and then the Darcy-Weisbach equation rearranged for calculation of flow $Q = [\Delta p \cdot \pi^2 \cdot D^5/(8 \cdot L \cdot \rho \cdot \lambda)]^{0.5}$. However, a calculation of flow (or head, i.e. pressure distribution) in a looped system of pipes still requires an iterative procedure, but by using Eq. 13, a double iterative procedure can be avoided (an iterative procedure for the calculation of a looped system of pipes still exists while the sub-iterative calculation of a single pipe in a

looped system required by the Colebrook equation is not needed). Of course, Eq. 13 has additional value because it can be used for the calculation of the partial derivative $F'=\partial Q(\Delta p)/\partial(\Delta p)$, where pressure drop Δp is treated as the variable.

Appropriate partial derivatives, F', are the terms in the pressure drop dependent Jacobian matrix [matrix [J] in Eq. 15 of this discussion (the relevant head-loss dependent Jacobian matrix is presented by Eq. 9 in the discussed paper)].

As noted in the discussed paper, this calculation is simple and hence can be performed in Excel. An Excel file converted to PDF are accompanied as an electronic annex to this discussion (Electronic tables; E-tables 1 and 2) [the example network (shown in Fig. 1 of the discussed paper is used as the example]. In this discussion, two versions of the standard procedure with a standard pressure drop independent Jacobian are shown (in E-tables 1 and 2) where convergence properties of both are investigated. The presented procedures start from a pressure-drop distribution which satisfies the second Kirchhoff law for all closed paths in the network of pipes and which is iterated until continuity at each node is approximately satisfied. Initial choices for pressure drops are; for the first loop: Δp_{12}=1000kPa, Δp_{25}=500kPa, Δp_{56}=-750kPa, Δp_{61}=-750kPa; and for the second loop: Δp_{52}=-500kPa, Δp_{23}=600kPa, Δp_{34}=-600kPa and Δp_{45}=500kPa [direction of both loops is counterclockwise, i.e. positive]. Also, as shown in Brkić (2011a), the standard procedure with pressure drop independent Jacobian demands assumption of the velocity of water (here 10m/s) required for the Reynolds number, Re, at the start of the procedure where the velocity can be chosen at random in a reasonable range without causing any trouble [the Reynolds number, Re, can be treated as independent of flow (as in E-table 1) or calculated in each iteration using flow Q from the previous iteration (as in E-table 2)]. On the contrary, assumption of the starting velocity is sufficient for the procedure shown in this discussion [using Eq. 13 and related derivatives F'] and in the discussed paper

(but note that the Reynolds number, velocity and viscosity still remain connected). The choice of initial pressure drop is not critical but should satisfy the second Kirchhoff law (Gay and Middleton 1971). Kinematic viscosity of water, ν, is 1.004 10^{-6} m^2/s, water density, ρ is 1000kg/m^3 and pipe roughness coefficient, ε is 3 10^{-6} m [inner roughness of the third generation polyethylene (PE) pipes]. Pipe lengths (L_{12}=L_{45}=L_{56}=400m, L_{16}=L_{25}=900m, L_{23}=500m, and L_{34}=800m), pipe diameters (D_{12}=0.3526m, D_{16}=D_{34}=0.2204m, D_{23}=D_{25}=0.2468m, D_{45}=0.1102m, and D_{56}=0.0968m) and water demands (q_1=-130L/s [input in network], q_2=15L/s, q_3=10L/s, q_4=35L/s, q_5=40L/s, and q_6=30L/s) are from Fig. 1 of the discussed paper and in the electronic annex to this discussion [numbers in the index are related to nodes (first number in the index is the starting node and the second is the ending node)]. The network is supplied by water through node 1 where the pressure is 1962kPa [node 5 is chosen to be excluded as redundant from the Jacobian matrix to preserve linear independency of rows and columns in the matrix (node 5 is chosen at random, i.e. any other node can be chosen instead of node 5; node 1 is chosen in the discussed paper)]. The calculated corrections of pressure drops in iteration i can be calculated as Δx=Δ(Δp), Eq. 15 ([J]x[Δx]=[F], where: [J]=[F']-the Jacobian matrix (here with symmetrical properties, diagonal terms are positive and non-diagonal terms are negative); [Δx]-single column matrix of corrections and [F]-single column matrix of flows where its terms are calculated using Eq. 13). The corrections have to be algebraically added to the values of pressure drop in the appropriate pipes in iteration i-1 [in the zeroth iteration the initial pressure drop pattern (initial choices) are chosen as explained above]. Algebraic rules for the corrections can be seen in Brkić (2009, 2011a) and in Corfield et al. (1974).

$$\overbrace{\begin{bmatrix} F_1'(|-x_{12}|,|-x_{16}|) & -|F_1'(x_{12})| & 0 & 0 & -|F_1'(x_{16})| \\ -|F_2'(x_{21})| & F_2'(|+x_{21}|,|-x_{23}|,|-x_{25}|) & -|F_2'(x_{23})| & 0 & 0 \\ 0 & -|F_3'(x_{32})| & F_3'(|+x_{32}|,|+x_{34}|) & -|F_3'(x_{34})| & 0 \\ 0 & 0 & -|F_4'(x_{43})| & F_4'(|-x_{43}|,|-x_{45}|) & 0 \\ -|F_6'(x_{61})| & 0 & 0 & 0 & F_6'(|+x_{61}|,|-x_{65}|) \end{bmatrix}}^{[J]} x \overbrace{\begin{bmatrix} \Delta x_1 \\ \Delta x_2 \\ \Delta x_3 \\ \Delta x_4 \\ \Delta x_6 \end{bmatrix}}^{[\Delta x]} = \overbrace{\begin{bmatrix} -Q_{12} - Q_{16} + q_1 \\ +Q_{21} - Q_{23} - Q_{25} - q_2 \\ +Q_{32} + Q_{34} - q_3 \\ -Q_{43} - Q_{45} - q_4 \\ +Q_{61} - Q_{65} - q_6 \end{bmatrix}}^{[F]}$$

(15)

Standard nodal oriented calculation (with flow independent Jacobian) can be with a constant value of the Reynolds number, Re [velocity, v=const→Re=v·D/ν] and with the flow dependent version [$v=4\cdot Q/(D^2\cdot\pi)\rightarrow Re=f(Q)$] (shown in E-tables 1 and 2, respectively). Final calculated pressure drops and related flows after 7 iterations for a constant value of the Reynolds number (E-table 1) are Δp_{12}=-5559kPa, Q_{12}=-97.1L/s; Δp_{16}=-16244kPa, Q_{16}=-32.9L/s; Δp_{23}=-7566kPa, Q_{23}=-40.3L/s; Δp_{25}=-14612kPa, Q_{25}=-41.8L/s; Δp_{34}=-12287kPa, Q_{34}=-30.3L/s; Δp_{45}=5241kPa, Q_{45}=4.7L/s; and Δp_{56}=3926kPa, Q_{56}=2.9L/s [where velocity used for the calculation of the Reynolds number does not change between two iterations (velocity in E-table 1 is 10 m/s in all iterations, tests with a value of randomly chosen velocity between 0.1 m/s and 500 m/s resulted in only a minor influence on the final results)]. On the other hand, when calculation with the flow dependent Reynolds number takes place, results are similar but slightly different. Results after 12 iterations are (E-table 2): Δp_{12}=-7983kPa, Q_{12}=-97.4L/s; Δp_{16}=-23769kPa, Q_{16}=-32.6L/s; Δp_{23}=-11343kPa, Q_{23}=-40.5L/s; Δp_{25}=-21696kPa, Q_{25}=-41.9L/s; Δp_{34}=-18740kPa, Q_{34}=-30.5L/s; Δp_{45}=8387kPa, Q_{45}=4.5L/s; and Δp_{56}=5910kPa, Q_{56}=2.6L/s. The last results are maybe more accurate, but using the same stopping criterion for comparison, the calculation with the flow-dependent Reynolds number does not fulfilled the required accuracy even after 12 iterations (in E-table 2, calculation of the Reynolds number also starts with a velocity of 10 m/s but then the velocity for the next iteration is calculated using value of flow, Q, from the previous iteration). To conclude, as can be seen from Fig. 13, a less sophisticated method with a constant value of the Reynolds number requires less iterative cycles (but maybe produces less reliable results). Every new method should be employed with caution and tested with a wide range of criteria (not only

with the required number of iterations). Therefore, the new method with pressure drop and head-loss dependent Jacobian should be further evaluated (to avoid unfounded conclusions).

Figure 1. Convergence properties of the proposed method for the solution of the problem of water distribution analysis expressed in the nodal form (both with the independent Jacobian)

As can be seen from Eqs. 15 [and Eqs. 5 and 10 of the discussed paper], the procedure with the pressure drop dependent Jacobian [or head-loss dependent one from the discussed paper], does not require calculation of the Reynolds number at all (problem from E-tables 1 and 2 is exceeded). On the other hand, Eqs. 15 [and Eq. 4 and 5 of the discussed paper] and its derivative F' [Eq. 10 of the discussed paper] are complex for computing by hand but they can be easily implemented in a computer code.

In addition to the discrepancy in results from the use of a dependent versus independent Jacobian matrix, a portion of the discrepancy in results of this discussion (in addition to the fact that the discussed paper head, h is in m, and in this discussion pressure drops Δp are in Pa, where $\Delta p=\rho \cdot g \cdot h$) compared with the discussed paper is probably caused by use of different values for the roughness of pipes, ε, and kinematic viscosity of water, ν [Spiliotis and Tsakiris (2011) did not report these values].

Supplemental Data

The Excel files converted in PDF (Electronic tables; E-tables 1 and 2) used as examples in this discussion is available online in the ASCE Library (www.ascelibrary.org)

Notation

The following symbols are used in this discussion:

D	inner pipe diameter (m)
L	pipe length (m)
Q	flow rate (m^3/s)
q	water demand (m^3/s)
Re	Reynolds number (-)
Δp	pressure drop (Pa)
Δx	correction of pressure drop (Pa)
ε	pipe roughness coefficient (m)
λ	Darcy (Darcy-Weisbach) or Moody friction factor (-)
ν	kinematic viscosity (m^2/s)
ρ	water density (kg/m^3)

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Figure 1 FB
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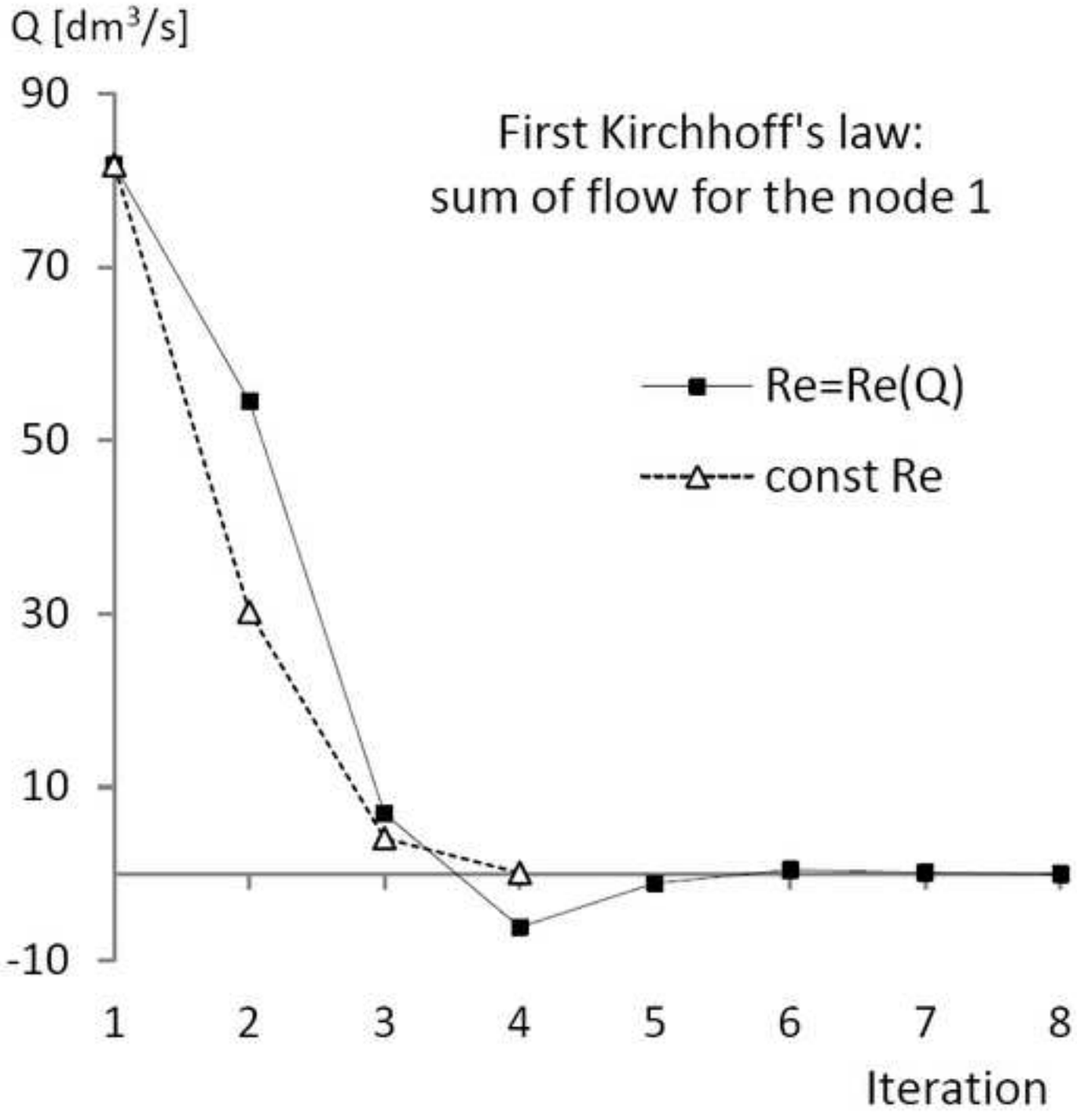
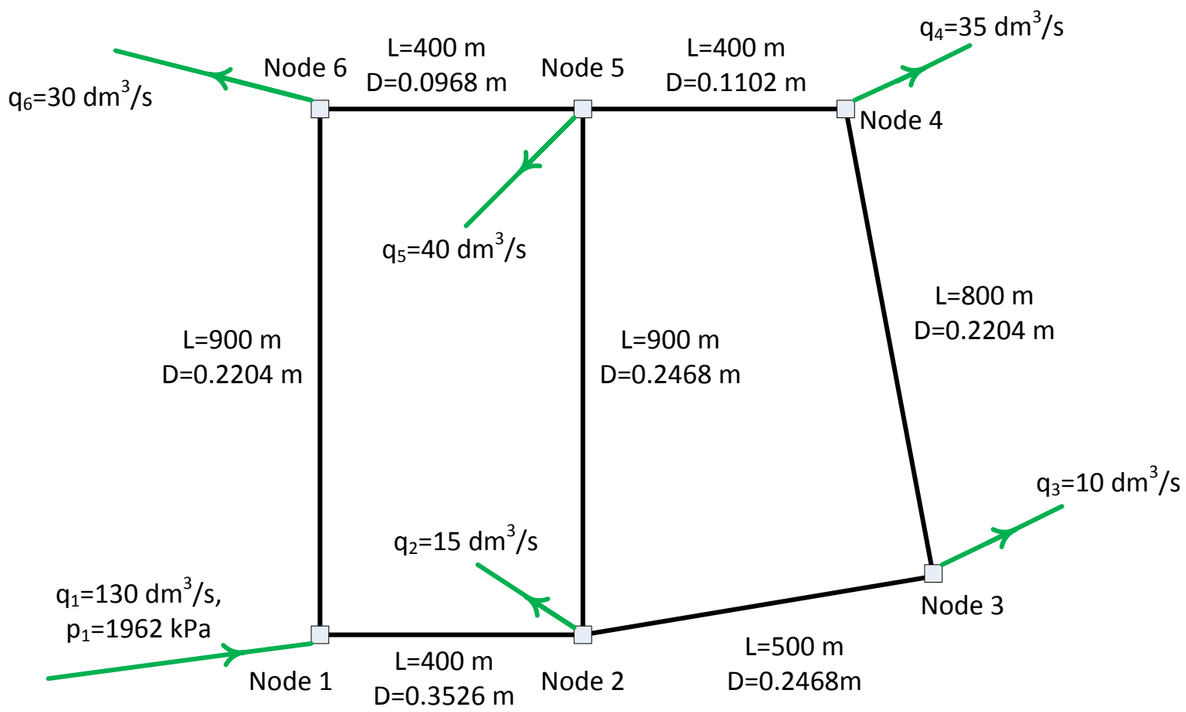


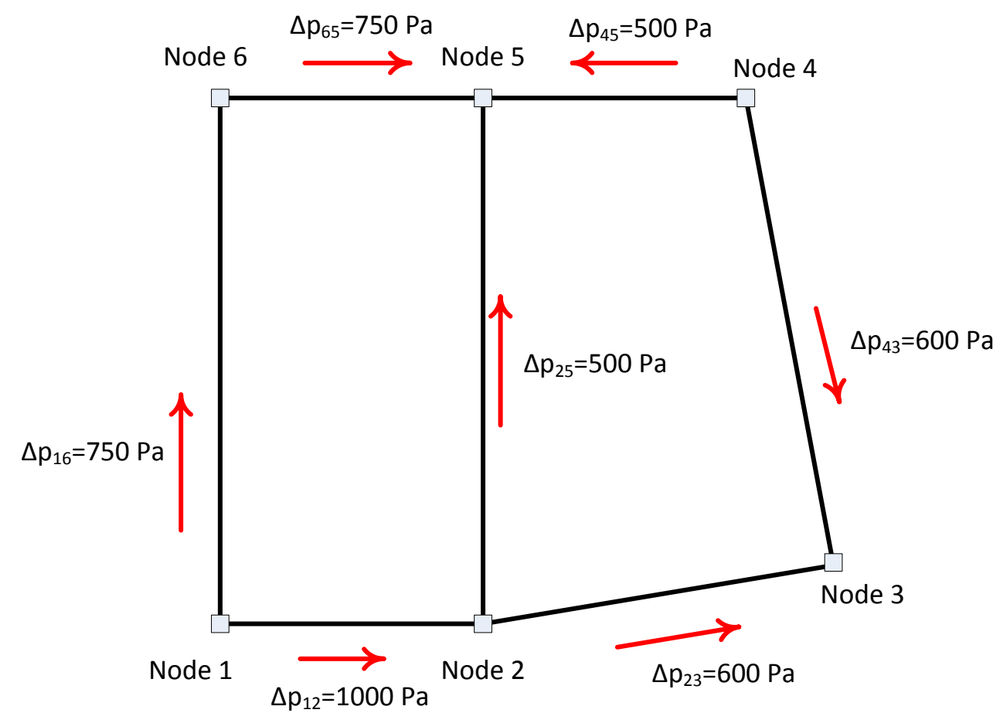
Electronic tables; Etable 1
Click here to download Figure: ETable 1.pdf

Standard procedure (pressure drop independent Jacobian); Re=const

Parameters of network

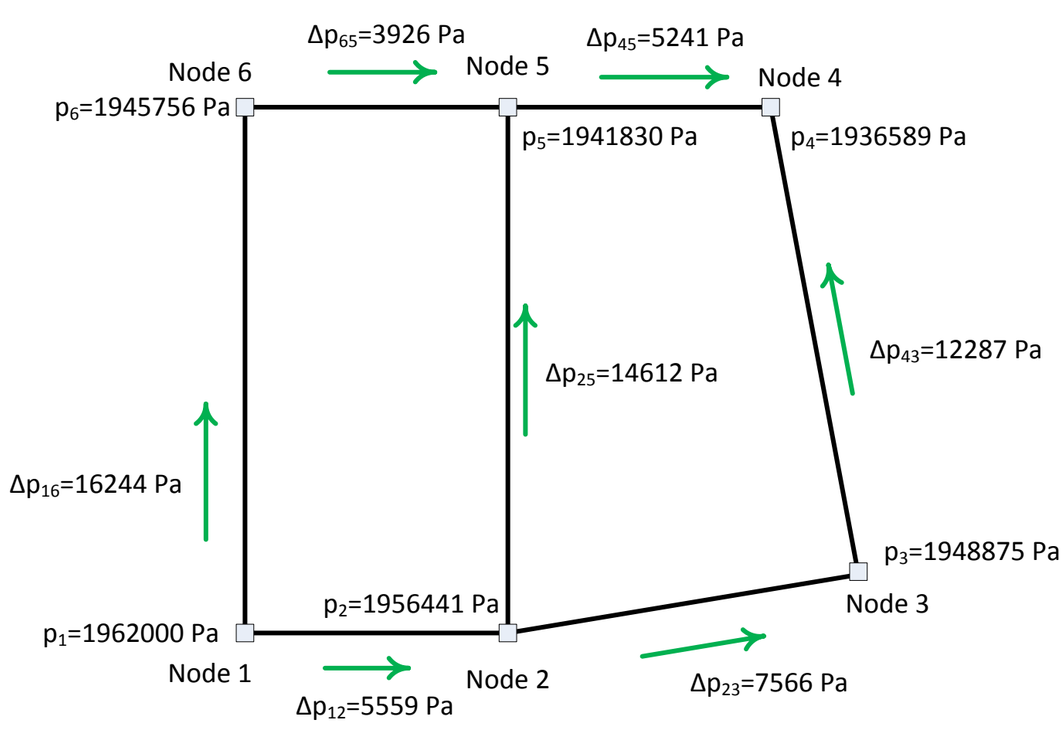


Initial pattern of pressure drops

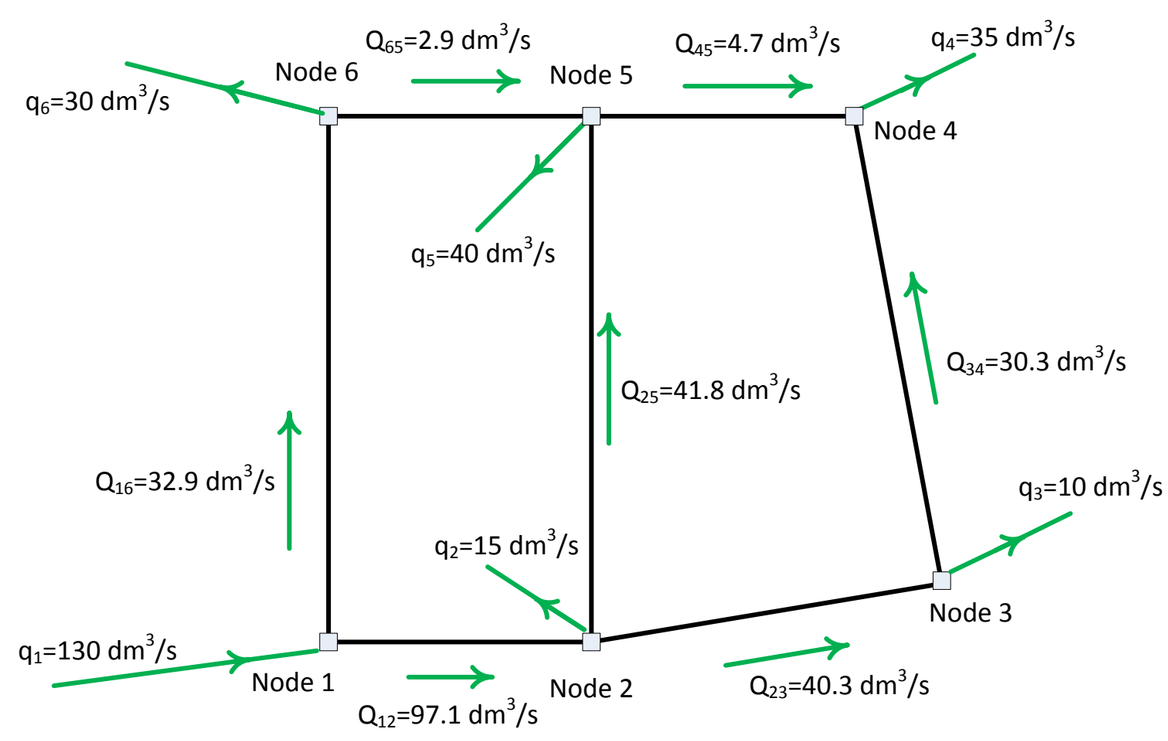


L-length
D-diameter
q-water demands and input, Q-flows
p-pressure, Δp-pressure drop
ε-roughness of pipes; ε=3· 10^{-6} m
ν-kinematic viscosity of water; ν=1.004· 10^{-6} m^2/s
ρ-water density; ρ=1000 kg/m^3

Final pattern of pressure (after 7 iterations)



Final flows (after 7 iterations)



Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re-const

Iteration 1

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity** (m/s)	Re***	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-1000	-1	10	3511952.19	0.0000085082	10.04640976	0.009907823	-0.04119	0.0000205950	-7261.262805	4540.579691	-3721
1	16	900	0.2204	-750	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.00707	0.0000047108	-7261.262805	1803.307753	-6208
											0.13000				
										stopping criterion Σ=0; Σ	0.081743812410				
											Σ	0.0000253058			
2	21	400	0.3526	1000	1	10	3511952.19	0.0000085082	10.04640976	0.009907823	0.04119	0.0000205950	-4540.579691	7261.262805	3721
2	23	500	0.2468	-600	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.01136	0.0000094654	-4540.579691	1577.81829	-3563
2	25	900	0.2468	-500	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.00773	0.0000077285	-4540.579691		-5041
											-0.01500				
										stopping criterion Σ=0; Σ	0.007103023684				
											Σ	0.0000377889			
3	32	500	0.2468	600	1	10	2458167.33	0.0000121556	9.755779122	0.010506936	0.01136	0.0000094654	-1577.81829	4540.579691	3563
3	34	800	0.2204	600	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.00670	0.0000055863	-1577.81829	-4885.424419	-5863
											-0.01000				
										stopping criterion Σ=0; Σ	0.008062080158				
											Σ	0.0000150517			
4	43	800	0.2204	-600	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.00670	0.0000055863	4885.424419	1577.81829	5863
4	45	400	0.1102	-500	-1	10	1097609.56	0.0000272232	9.100473186	0.01207458	-0.00144	0.0000014407	4885.424419		4385
											-0.03500				
										stopping criterion Σ=0; Σ	-0.043144310939				
											Σ	0.0000070270			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	750	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.00707	0.0000047108	-1803.307753	7261.262805	6208
6	65	400	0.0968	-750	-1	10	964143.43	0.0000309917	8.995308178	0.012358561	-0.00126	0.0000008409	-1803.307753		-2553
											-0.03000				
										stopping criterion Σ=0; Σ	-0.024195064118				
											Σ	0.0000055517			

Jacobian

0.0000253058	-0.0000205950	0	0	-0.0000047108
-0.0000205950	0.0000377889	-0.0000094654	0	0
0	-0.0000094654	0.0000150517	-0.0000055863	0
0	0	-0.0000055863	0.0000070270	0
-0.0000047108	0	0	0	0.0000055517

inverse Jacobian

145888.8662	102387.5583	91335.74753	72609.7091	123792.6379
102387.5583	105934.6875	94499.9962	75125.21022	86880.00844
91335.74753	94499.9962	178543.7473	141937.9586	77502.09742
72609.7091	75125.21022	141937.9586	255144.5743	61612.29202
123792.6379	86880.00844	77502.09742	61612.29202	285169.4619

[F]	[Δx]
0.0817438124	7261.262805
0.0071030237	4540.579691
0.0080620802	1577.81829
-0.0431443109	-4885.424419
-0.0241950641	1803.307753

*chosen initial pattern

**assumed velocity 10m/s

***constant value of the Reynolds number

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re-const

Iteration 2

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re**	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-3721	-1	10	3511952.19	0.0000085082	10.04640976	0.009907823	-0.07945	0.0000106770	-8824.264907	7167.672128	-5377
1	16	900	0.2204	-6208	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.02033	0.0000016374	-8824.264907	1171.096558	-13861
											0.13000				
										stopping criterion Σ=0; Σ	0.030218689494				
											Σ	0.0000123144			
2	21	400	0.3526	3721	1	10	3511952.19	0.0000085082	10.04640976	0.009907823	0.07945	0.0000106770	-7167.672128	8824.264907	5377
2	23	500	0.2468	-3563	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.02768	0.0000038844	-7167.672128	3955.948689	-6774
2	25	900	0.2468	-5041	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.02454	0.0000024341	-7167.672128		-12208
											-0.01500				
										stopping criterion Σ=0; Σ	0.012234887370				
											Σ	0.0000169955			
3	32	500	0.2468	3563	1	10	2458167.33	0.0000121556	9.755779122	0.010506936	0.02768	0.0000038844	-3955.948689	7167.672128	6774
3	34	800	0.2204	-5863	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.02096	0.0000017870	-3955.948689	-1191.181637	-11010
											-0.01000				
										stopping criterion Σ=0; Σ	-0.003277436616				
											Σ	0.0000056714			
4	43	800	0.2204	5863	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.02096	0.0000017870	1191.181637	3955.948689	11010
4	45	400	0.1102	4385	1	10	1097609.56	0.0000272232	9.100473186	0.01207458	0.00427	0.0000004865	1191.181637		5577
											-0.03500				
										stopping criterion Σ=0; Σ	-0.009777583049				
											Σ	0.0000022735			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	6208	1	10	2195219.12	1.36116E-05	9.663698962	0.01070812	0.02033	0.0000016374	-1171.096558	8824.264907	13861
6	65	400	0.0968	-2553	-1	10	964143.43	3.09917E-05	8.995308178	0.012358561	-0.00233	0.0000004557	-1171.096558		-3724
											-0.03000				
										stopping criterion Σ=0; Σ	-0.011997517539				
											Σ	0.0000020931			

Jacobian

0.0000123144	-0.0000106770	0	0	-0.0000016374
-0.0000106770	0.0000169955	-0.0000038844	0	0
0	-0.0000038844	0.0000056714	-0.0000017870	0
0	0	-0.0000017870	0.0000022735	0
-0.0000016374	0	0	0	0.0000020931

inverse Jacobian

390078.41	309443.8036	281712.0059	221433.0028	305149.0192
309443.8036	319775.9225	291118.1789	228826.5008	242070.4933
281712.0059	291118.1789	499398.791	392540.508	220376.5706
221433.0028	228826.5008	392540.508	748396.167	173221.7469
305149.0192	242070.4933	220376.5706	173221.7469	716469.2059

[F]	[Δx]
0.03022	8824.264907
0.01223	7167.672128
-0.00328	3955.948689
-0.00978	-1191.181637
-0.01200	1171.096558

*from the previous iteration

**constant value of the Reynolds number

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re-const

Iteration 3

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re**	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-5377	-1	10	3511952.19	0.0000085082	10.04640976	0.009907823	-0.09552	0.0000088814	-2484.809459	2304.674894	-5557
1	16	900	0.2204	-13861	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03038	0.0000010958	-2484.809459	196.7879626	-16149
											0.13000				
										stopping criterion Σ=0; Σ	0.004107031176				
											Σ	0.0000099772			
2	21	400	0.3526	5377	1	10	3511952.19	0.0000085082	10.04640976	0.009907823	0.09552	0.0000088814	-2304.674894	2484.809459	5557
2	23	500	0.2468	-6774	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.03817	0.0000028169	-2304.674894	1539.595414	-7540
2	25	900	0.2468	-12208	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.03819	0.0000015641	-2304.674894		-14513
											-0.01500				
										stopping criterion Σ=0; Σ	0.004159970650				
											Σ	0.0000132624			
3	32	500	0.2468	6774	1	10	2458167.33	0.0000121556	9.755779122	0.010506936	0.03817	0.0000028169	-1539.595414	2304.674894	7540
3	34	800	0.2204	-11010	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.02872	0.0000013041	-1539.595414	308.7516734	-12241
											-0.01000				
										stopping criterion Σ=0; Σ	-0.000550070355				
											Σ	0.0000041210			
4	43	800	0.2204	11010	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.02872	0.0000013041	-308.7516734	1539.595414	12241
4	45	400	0.1102	5577	1	10	1097609.56	0.0000272232	9.100473186	0.01207458	0.00481	0.0000004314	-308.7516734		5268
											-0.03500				
										stopping criterion Σ=0; Σ	-0.001471912869				
											Σ	0.0000017355			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	13861	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03038	0.0000010958	-196.7879626	2484.809459	16149
6	65	400	0.0968	-3724	-1	10	964143.43	0.0000309917	8.995308178	0.012358561	-0.00281	0.0000003773	-196.7879626		-3921
											-0.03000				
										stopping criterion Σ=0; Σ	-0.002432933964				
											Σ	0.0000014731			

Jacobian

0.0000099772	-0.0000088814	0	0	-0.0000010958
-0.0000088814	0.0000132624	-0.0000028169	0	0
0	-0.0000028169	0.0000041210	-0.0000013041	0
0	0	-0.0000013041	0.0000017355	0
-0.0000010958	0	0	0	0.0000014731

inverse Jacobian

550959.5984	455776.4985	408740.2066	307136.7631	409834.8885
455776.4985	470180.4494	421657.6648	316843.2374	339032.3193
408740.2066	421657.6648	696502.7013	523368.0997	304044.0669
307136.7631	316843.2374	523368.0997	969483.9882	228465.6832
409834.8885	339032.3193	304044.0669	228465.6832	983690.4851

[F]	[Δx]
0.0041070312	2484.809459
0.0041599706	2304.674894
-0.0005500704	1539.595414
-0.0014719129	308.7516734
-0.0024329340	196.7879626

*from the previous iteration

**constant value of the Reynolds number

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re-const

Iteration 4

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re**	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-5557	-1	10	3511952.19	0.0000085082	10.04640976	0.009907823	-0.09710	0.0000087363	-99.91325401	98.4984645	-5559
1	16	900	0.2204	-16149	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03279	0.0000010152	-99.91325401	4.825012366	-16244
											0.13000				
										stopping criterion Σ=0; Σ	0.000108893461				
											Σ	0.0000097515			
2	21	400	0.3526	5557	1	10	3511952.19	0.0000085082	10.04640976	0.009907823	0.09710	0.0000087363	-98.4984645	99.91325401	5559
2	23	500	0.2468	-7540	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.04026	0.0000026702	-98.4984645	71.81068141	-7566
2	25	900	0.2468	-14513	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.04164	0.0000014345	-98.4984645		-14611
											-0.01500				
										stopping criterion Σ=0; Σ	0.000200197582				
											Σ	0.0000128409			
3	32	500	0.2468	7540	1	10	2458167.33	0.0000121556	9.755779122	0.010506936	0.04026	0.0000026702	-71.81068141	98.4984645	7566
3	34	800	0.2204	-12241	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03028	0.0000012368	-71.81068141	26.4205966	-12287
											-0.01000				
										stopping criterion Σ=0; Σ	-0.000015124132				
											Σ	0.0000039070			
4	43	800	0.2204	12241	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03028	0.0000012368	-26.4205966	71.81068141	12287
4	45	400	0.1102	5268	1	10	1097609.56	0.0000272232	9.100473186	0.01207458	0.00468	0.0000004439	-26.4205966		5241
											-0.03500				
										stopping criterion Σ=0; Σ	-0.000044410182				
											Σ	0.0000016806			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	16149	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03279	0.0000010152	-4.825012366	99.91325401	16244
6	65	400	0.0968	-3921	-1	10	964143.43	0.0000309917	8.995308178	0.012358561	-0.00288	0.0000003677	-4.825012366		-3926
											-0.03000				
										stopping criterion Σ=0; Σ	-0.000094759151				
											Σ	0.0000013829			

Jacobian

0.0000097515	-0.0000087363	0	0	-0.0000010152
-0.0000087363	0.0000128409	-0.0000026702	0	0
0	-0.0000026702	0.0000039070	-0.0000012368	0
0	0	-0.0000012368	0.0000016806	0
-0.0000010152	0	0	0	0.0000013829

inverse Jacobian

584493.0924	488088.6072	434889.9307	320034.2533	429069.5712
488088.6072	503170.712	448328.1782	329923.4211	358300.1615
434889.9307	448328.1782	733149.9848	539522.9721	319247.6327
320034.2533	329923.4211	539522.9721	992047.358	234933.4177
429069.5712	358300.1615	319247.6327	234933.4177	1038072.878

[F]	[Δx]
0.0001088935	99.91325401
0.0002001976	98.4984645
-0.0000151241	71.81068141
-0.0000444102	26.4205966
-0.0000947592	4.825012366

*from the previous iteration

**constant value of the Reynolds number

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re-const

Iteration 5

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re**	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-5559	-1	10	3511952.19	0.0000085082	10.04640976	0.009907823	-0.09711	0.0000087351	-0.143966437	0.143953852	-5559
1	16	900	0.2204	-16244	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03289	0.0000010122	-0.143966437	0.003325347	-16244
											0.13000				
									stopping criterion Σ=0; Σ		0.000000142470				
											Σ	0.0000097474			
2	21	400	0.3526	5559	1	10	3511952.19	0.0000085082	10.04640976	0.009907823	0.09711	0.0000087351	-0.143953852	0.143966437	5559
2	23	500	0.2468	-7566	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.04034	0.0000026655	-0.143953852	0.108162659	-7566
2	25	900	0.2468	-14611	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.04178	0.0000014297	-0.143953852		-14612
											-0.01500				
									stopping criterion Σ=0; Σ		0.000000301095				
											Σ	0.0000128303			
3	32	500	0.2468	7566	1	10	2458167.33	0.0000121556	9.755779122	0.010506936	0.04034	0.0000026655	-0.108162659	0.143953852	7566
3	34	800	0.2204	-12287	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03034	0.0000012345	-0.108162659	0.039799441	-12287
											-0.01000				
									stopping criterion Σ=0; Σ		-0.000000011007				
											Σ	0.0000039000			
4	43	800	0.2204	12287	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03034	0.0000012345	-0.039799441	0.108162659	12287
4	45	400	0.1102	5241	1	10	1097609.56	0.0000272232	9.100473186	0.01207458	0.00466	0.0000004450	-0.039799441		5241
											-0.03500				
									stopping criterion Σ=0; Σ		-0.000000066684				
											Σ	0.0000016795			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	16244	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03289	0.0000010122	-0.003325347	0.143966437	16244
6	65	400	0.0968	-3926	-1	10	964143.43	0.0000309917	8.995308178	0.012358561	-0.00289	0.0000003675	-0.003325347		-3926
											-0.03000				
									stopping criterion Σ=0; Σ		-0.0000001411				
											Σ	0.0000013797			

Jacobian

0.0000097474	-0.0000087351	0	0	-0.0000010122
-0.0000087351	0.0000128303	-0.0000026655	0	0
0	-0.0000026655	0.0000039000	-0.0000012345	0
0	0	-0.0000012345	0.0000016795	0
-0.0000010122	0	0	0	0.0000013797

inverse Jacobian

585703.1321	489301.4772	435821.8724	320349.9922	429692.3916
489301.4772	504404.3594	449274.0418	330237.9823	358968.7513
435821.8724	449274.0418	734332.2032	539769.4115	319734.2346
320349.9922	330237.9823	539769.4115	992184.6484	235020.0072
429692.3916	358968.7513	319734.2346	235020.0072	1040013.305

[F]	[Δx]
0.0000001425	0.143966437
0.0000003011	0.143953852
-0.0000000110	0.108162659
-0.0000000667	0.039799441
-0.0000001411	0.003325347

*from the previous iteration

**constant value of the Reynolds number

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re-const

Iteration 6

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re**	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-5559	-1	10	3511952.19	0.0000085082	10.04640976	0.009907823	-0.09711	0.0000087351	-0.0000003050	0.0000003050	-5559
1	16	900	0.2204	-16244	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03289	0.0000010122	-0.0000003050	0.0000000006	-16244
											0.13000				
										stopping criterion Σ=0; Σ	0.000000000000				
											Σ	0.0000097474			
2	21	400	0.3526	5559	1	10	3511952.19	0.0000085082	10.04640976	0.009907823	0.09711	0.0000087351	-0.0000003050	0.0000003050	5559
2	23	500	0.2468	-7566	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.04034	0.0000026655	-0.0000003050	0.0000002361	-7566
2	25	900	0.2468	-14612	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.04178	0.0000014297	-0.0000003050		-14612
											-0.01500				
										stopping criterion Σ=0; Σ	0.000000000001				
											Σ	0.0000128303			
3	32	500	0.2468	7566	1	10	2458167.33	0.0000121556	9.755779122	0.010506936	0.04034	0.0000026655	-0.0000002361	0.0000003050	7566
3	34	800	0.2204	-12287	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03034	0.0000012345	-0.0000002361	0.0000000836	-12287
											-0.01000				
										stopping criterion Σ=0; Σ	0.000000000000				
											Σ	0.0000038999			
4	43	800	0.2204	12287	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03034	0.0000012345	-0.0000000836	0.0000002361	12287
4	45	400	0.1102	5241	1	10	1097609.56	0.0000272232	9.100473186	0.01207458	0.00466	0.0000004450	-0.0000000836		5241
											-0.03500				
										stopping criterion Σ=0; Σ	0.000000000000				
											Σ	0.0000016795			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	16244	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03289	0.0000010122	-0.0000000006	0.0000003050	16244
6	65	400	0.0968	-3926	-1	10	964143.43	0.0000309917	8.995308178	0.012358561	-0.00289	0.0000003675	-0.0000000006		-3926
											-0.03000				
										stopping criterion Σ=0; Σ	0.000000000000				
											Σ	0.0000013797			

Jacobian

0.0000097474	-0.0000087351	0	0	-0.0000010122
-0.0000087351	0.0000128303	-0.0000026655	0	0
0	-0.0000026655	0.0000038999	-0.0000012345	0
0	0	-0.0000012345	0.0000016795	0
-0.0000010122	0	0	0	0.0000013797

inverse Jacobian

585704.8442	489303.2155	435823.2102	320350.4172	429693.2006
489303.2155	504406.1292	449275.4013	330238.406	358969.6532
435823.2102	449275.4013	734333.8498	539769.6809	319734.8835
320350.4172	330238.406	539769.6809	992184.7735	235020.0745
429693.2006	358969.6532	319734.8835	235020.0745	1040015.954

[F]	[Δx]
0.0000000000	0.0000003050
0.0000000000	0.0000003050
0.0000000000	0.0000002361
0.0000000000	0.0000000836
0.0000000000	0.0000000006

*from the previous iteration

**constant value of the Reynolds number

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re-const

Iteration 7

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re**	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)
1	12	400	0.3526	-5559	-1	10	3511952.19	0.0000085082	10.04640976	0.009907823	-0.09711	0.0000087351	0	0
1	16	900	0.2204	-16244	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03289	0.0000010122	0	0
											0.13000			
									stopping criterion Σ=0; Σ		0.0000000000000000000000000000			
											Σ	0.0000097474		
2	21	400	0.3526	5559	1	10	3511952.19	0.0000085082	10.04640976	0.009907823	0.09711	0.0000087351	0	0
2	23	500	0.2468	-7566	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.04034	0.0000026655	0	0
2	25	900	0.2468	-14612	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.04178	0.0000014297	0	
											-0.01500			
									stopping criterion Σ=0; Σ		0.0000000000000000000000000000			
											Σ	0.0000128303		
3	32	500	0.2468	7566	1	10	2458167.33	0.0000121556	9.755779122	0.010506936	0.04034	0.0000026655	0	0
3	34	800	0.2204	-12287	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.03034	0.0000012345	0	0
											-0.01000			
									stopping criterion Σ=0; Σ		0.0000000000000000000000000000			
											Σ	0.0000038999		
4	43	800	0.2204	12287	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03034	0.0000012345	0	0
4	45	400	0.1102	5241	1	10	1097609.56	0.0000272232	9.100473186	0.01207458	0.00466	0.0000004450	0	
											-0.03500			
									stopping criterion Σ=0; Σ		0.0000000000000000000000000000			
											Σ	0.0000016795		
5	omitted to preserve linear indenpendency of Jacobian													
6	61	900	0.2204	16244	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.03289	0.0000010122	0	0
6	65	400	0.0968	-3926	-1	10	964143.43	0.0000309917	8.995308178	0.012358561	-0.00289	0.0000003675	0	
											-0.03000			
									stopping criterion Σ=0; Σ		0.0000000000000000000000000000			
											Σ	0.0000013797		

Pipe	Final pressure drop (Pa)	Final flow distribution (dm^3/s)
12	-5559	-97.1
16	-16244	-32.9
21	5559	97.1
23	-7566	-40.3
25	-14612	-41.8
32	7566	40.3
34	-12287	-30.3
43	12287	30.3
45	5241	4.7
61	16244	32.9
65	-3926	-2.9

Jacobian

0.0000097474	-0.0000087351	0	0	-0.0000010122
-0.0000087351	0.0000128303	-0.0000026655	0	0
0	-0.0000026655	0.0000038999	-0.0000012345	0
0	0	-0.0000012345	0.0000016795	0
-0.0000010122	0	0	0	0.0000013797

inverse Jacobian

585704.8442	489303.2155	435823.2102	320350.4172	429693.2006
489303.2155	504406.1292	449275.4013	330238.406	358969.6532
435823.2102	449275.4013	734333.8498	539769.6809	319734.8835
320350.4172	330238.406	539769.6809	992184.7735	235020.0745
429693.2006	358969.6532	319734.8835	235020.0745	1040015.954

[F]	[Δx]
0.0000000000	0
0.0000000000	0
0.0000000000	0
0.0000000000	0
0.0000000000	0

*from the previous iteration

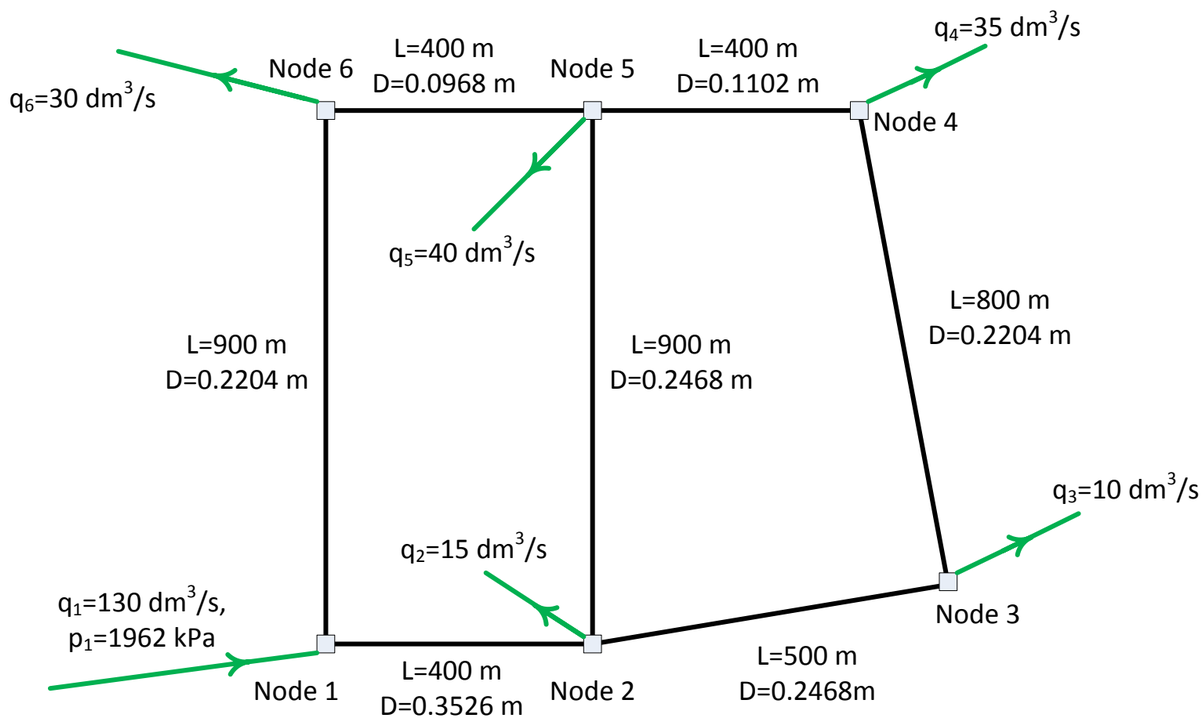
**constant value of the Reynolds number

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Electronic tables; Etable 2
Click here to download Figure: ETable 2.pdf

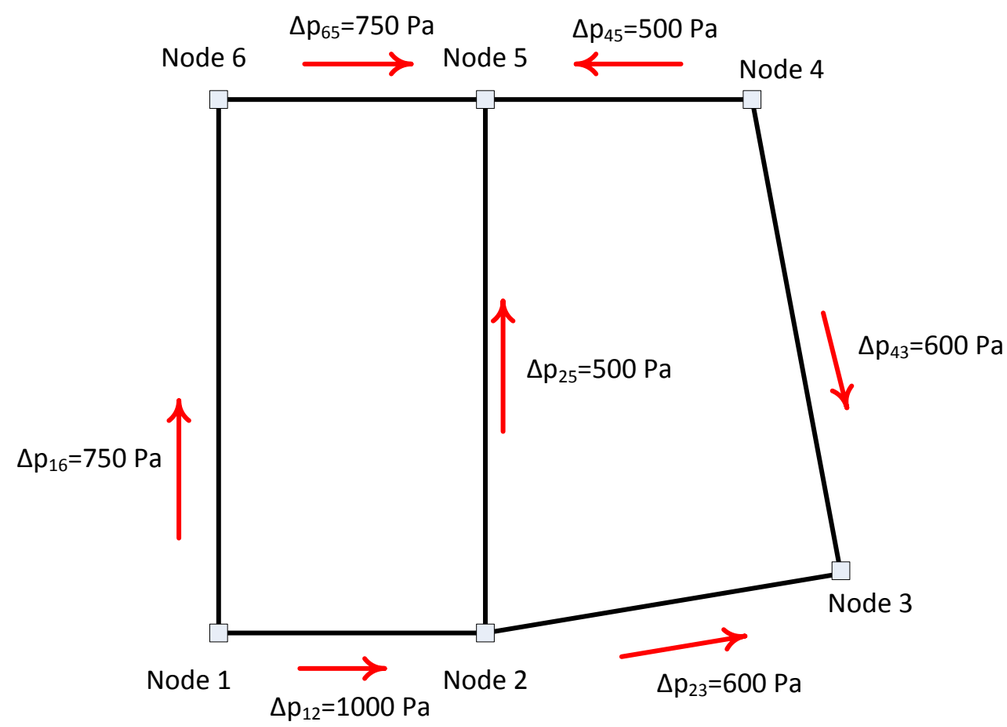
Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Parameters of network

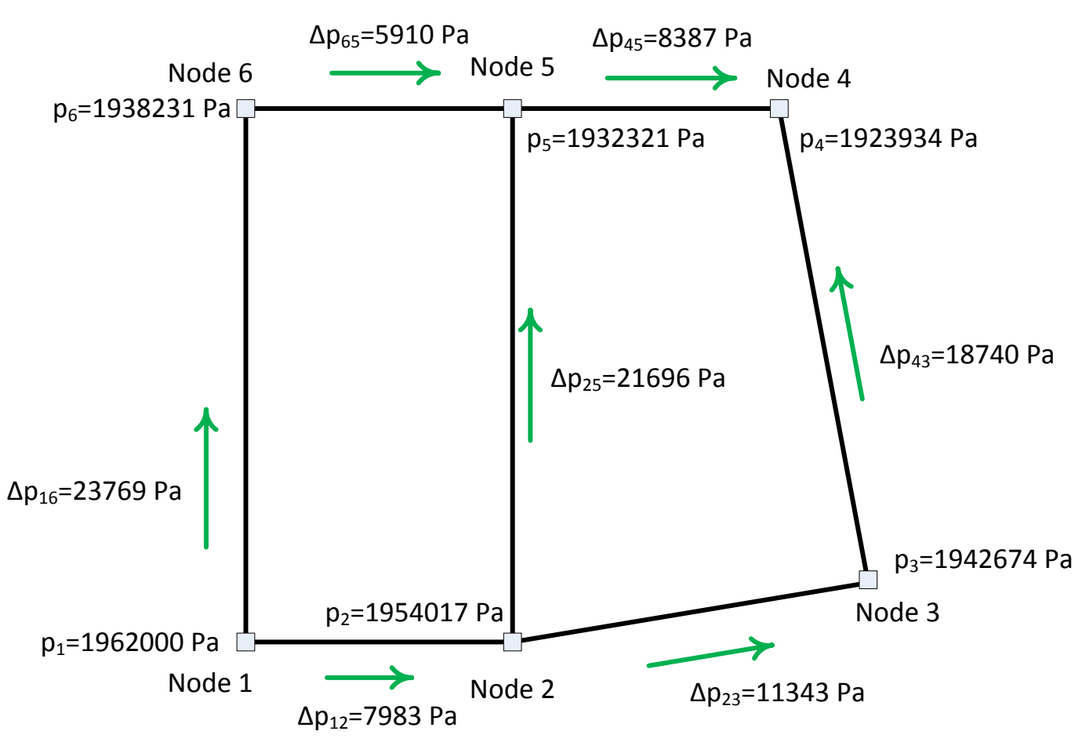


L-length
D-diameter
q-water demands and input, Q-flows
p-pressure, Δp-pressure drop
ε-roughness of pipes; $\varepsilon=3\cdot 10^{-6}$ m
ν-kinematic viscosity of water; $\nu=1.004\cdot 10^{-6}$ m^2/s
ρ-water density; $\rho=1000$ kg/m^3

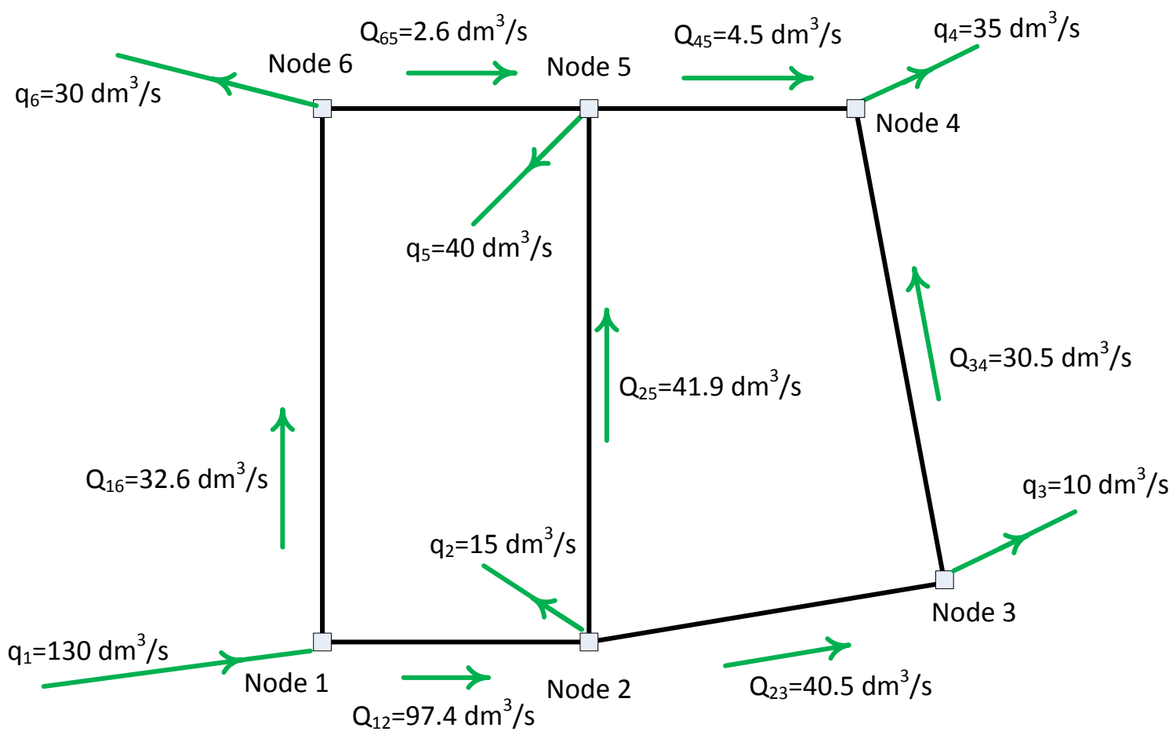
Initial pattern of pressure drops



Final pattern of pressure (after 12 iterations)



Final flows (after 12 iterations)



Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 1

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity** (m/s)	Re***	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-1000	-1	10	3511952.19	0.0000085082	10.04640976	0.009907823	-0.04119	0.0000205950	-7261.262805	4540.579691	-3721
1	16	900	0.2204	-750	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.00707	0.0000047108	-7261.262805	1803.307753	-6208
											0.13000				
										stopping criterion Σ=0; Σ	0.081743812410				
											Σ	0.0000253058			
2	21	400	0.3526	1000	1	10	3511952.19	0.0000085082	10.04640976	0.009907823	0.04119	0.0000205950	-4540.579691	7261.262805	3721
2	23	500	0.2468	-600	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.01136	0.0000094654	-4540.579691	1577.81829	-3563
2	25	900	0.2468	-500	-1	10	2458167.33	0.0000121556	9.755779122	0.010506936	-0.00773	0.0000077285	-4540.579691		-5041
											-0.01500				
										stopping criterion Σ=0; Σ	0.007103023684				
											Σ	0.0000377889			
3	32	500	0.2468	600	1	10	2458167.33	0.0000121556	9.755779122	0.010506936	0.01136	0.0000094654	-1577.81829	4540.579691	3563
3	34	800	0.2204	600	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.00670	0.0000055863	-1577.81829	-4885.424419	-5863
											-0.01000				
										stopping criterion Σ=0; Σ	0.008062080158				
											Σ	0.0000150517			
4	43	800	0.2204	-600	-1	10	2195219.12	0.0000136116	9.663698962	0.01070812	-0.00670	0.0000055863	4885.424419	1577.81829	5863
4	45	400	0.1102	-500	-1	10	1097609.56	0.0000272232	9.100473186	0.01207458	-0.00144	0.0000014407	4885.424419		4385
											-0.03500				
										stopping criterion Σ=0; Σ	-0.043144310939				
											Σ	0.0000070270			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	750	1	10	2195219.12	0.0000136116	9.663698962	0.01070812	0.00707	0.0000047108	-1803.307753	7261.262805	6208
6	65	400	0.0968	-750	-1	10	964143.43	0.0000309917	8.995308178	0.012358561	-0.00126	0.0000008409	-1803.307753		-2553
											-0.03000				
										stopping criterion Σ=0; Σ	-0.024195064118				
											Σ	0.0000055517			

Jacobian

0.0000253058	-0.0000205950	0	0	-0.0000047108
-0.0000205950	0.0000377889	-0.0000094654	0	0
0	-0.0000094654	0.0000150517	-0.0000055863	0
0	0	-0.0000055863	0.0000070270	0
-0.0000047108	0	0	0	0.0000055517

inverse Jacobian

145888.8662	102387.5583	91335.74753	72609.7091	123792.6379
102387.5583	105934.6875	94499.9962	75125.21022	86880.00844
91335.74753	94499.9962	178543.7473	141937.9586	77502.09742
72609.7091	75125.21022	141937.9586	255144.5743	61612.29202
123792.6379	86880.00844	77502.09742	61612.29202	285169.4619

[F]	[Δx]
0.0817438124	7261.262805
0.0071030237	4540.579691
0.0080620802	1577.81829
-0.0431443109	-4885.424419
-0.0241950641	1803.307753

*chosen initial pattern

**assumed velocity 10m/s for the start of calculation

***the Reynolds number calculated for velocity of 10m/s

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 2

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity** (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-3721	-1	0.42	148144.54	0.0000085082	7.748505571	0.016655746	-0.06128	0.0000082349	-19290.31926	14899.69072	-8111
1	16	900	0.2204	-6208	-1	0.19	40658.51	0.0000136116	6.752406402	0.021932233	-0.01421	0.0000011441	-19290.31926	3243.047121	-22255
											0.13000				
										stopping criterion Σ=0; Σ	0.054516105450				
											Σ	0.0000093790			
2	21	400	0.3526	3721	1	0.42	148144.54	0.0000085082	7.748505571	0.016655746	0.06128	0.0000082349	-14899.69072	19290.31926	8111
2	23	500	0.2468	-3563	-1	0.24	58364.88	0.0000121556	7.029694664	0.020236112	-0.01994	0.0000027990	-14899.69072	7571.140532	-10891
2	25	900	0.2468	-5041	-1	0.16	39712.27	0.0000121556	6.735132125	0.022044881	-0.01694	0.0000016804	-14899.69072		-19940
											-0.01500				
										stopping criterion Σ=0; Σ	0.009393981992				
											Σ	0.0000127143			
3	32	500	0.2468	3563	1	0.24	58364.88	0.0000121556	7.029694664	0.020236112	0.01994	0.0000027990	-7571.140532	14899.69072	10891
3	34	800	0.2204	-5863	-1	0.18	38572.05	0.0000136116	6.71218502	0.022195869	-0.01456	0.0000012412	-7571.140532	-5239.473291	-18674
											-0.01000				
										stopping criterion Σ=0; Σ	-0.004611303413				
											Σ	0.0000040402			
4	43	800	0.2204	5863	1	0.18	38572.05	0.0000136116	6.71218502	0.022195869	0.01456	0.0000012412	5239.473291	7571.140532	18674
4	45	400	0.1102	4385	1	0.15	16579.55	0.0000272232	6.066929703	0.027168276	0.00284	0.0000003243	5239.473291		9625
											-0.03500				
										stopping criterion Σ=0; Σ	-0.017600196387				
											Σ	0.0000015655			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	6208	1	0.19	40658.51	0.0000136116	6.752406402	0.021932233	0.01421	0.0000011441	-3243.047121	19290.31926	22255
6	65	400	0.0968	-2553	-1	0.17	16523.84	0.0000309917	6.063556479	0.027198512	-0.00157	0.0000003072	-3243.047121		-5796
											-0.03000				
										stopping criterion Σ=0; Σ	-0.017363570708				
											Σ	0.0000014513			

Jacobian

0.0000093790	-0.0000082349	0	0	-0.0000011441
-0.0000082349	0.0000127143	-0.0000027990	0	0
0	-0.0000027990	0.0000040402	-0.0000012412	0
0	0	-0.0000012412	0.0000015655	0
-0.0000011441	0	0	0	0.0000014513

inverse Jacobian

556645.4698	451580.4812	413586.0364	327909.4576	438822.2534
451580.4812	464860.4479	425748.6719	337552.5376	355996.0066
413586.0364	425748.6719	717143.8627	568583.6425	326043.7142
327909.4576	337552.5376	568583.6425	1089553.347	258501.9998
438822.2534	355996.0066	326043.7142	258501.9998	1034976.103

[F]	[Δx]
0.0545161055	19290.31926
0.0093939820	14899.69072
-0.0046113034	7571.140532
-0.0176001964	-5239.473291
-0.0173635707	3243.047121

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 3

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-8111	-1	0.63	220396.17	0.0000085082	8.053574983	0.015417806	-0.09404	0.0000057969	-6197.128544	5614.524376	-8694
1	16	900	0.2204	-22255	-1	0.37	81735.41	0.0000136116	7.286294946	0.018835906	-0.02902	0.0000006520	-6197.128544	737.810175	-27715
											0.13000				
										stopping criterion Σ=0; Σ	0.006936969187				
											Σ	0.0000064489			
2	21	400	0.3526	8111	1	0.63	220396.17	0.0000085082	8.053574983	0.015417806	0.09404	0.0000057969	-5614.524376	6197.128544	8694
2	23	500	0.2468	-10891	-1	0.42	102481.12	0.0000121556	7.460882598	0.017964684	-0.03701	0.0000016990	-5614.524376	3530.014773	-12976
2	25	900	0.2468	-19940	-1	0.35	87049.07	0.0000121556	7.335888597	0.018582089	-0.03670	0.0000009202	-5614.524376		-25555
											-0.01500				
										stopping criterion Σ=0; Σ	0.005331117729				
											Σ	0.0000084162			
3	32	500	0.2468	10891	1	0.42	102481.12	0.0000121556	7.460882598	0.017964684	0.03701	0.0000016990	-3530.014773	5614.524376	12976
3	34	800	0.2204	-18674	-1	0.38	83750.33	0.0000136116	7.304920399	0.018739976	-0.02827	0.0000007569	-3530.014773	515.961554	-21688
											-0.01000				
										stopping criterion Σ=0; Σ	-0.001260223488				
											Σ	0.0000024560			
4	43	800	0.2204	18674	1	0.38	83750.33	0.0000136116	7.304920399	0.018739976	0.02827	0.0000007569	-515.961554	3530.014773	21688
4	45	400	0.1102	9625	1	0.30	32733.95	0.0000272232	6.581436002	0.023086531	0.00457	0.0000002375	-515.961554		9109
											-0.03500				
										stopping criterion Σ=0; Σ	-0.002158906865				
											Σ	0.0000009944			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	22255	1	0.37	81735.41	0.0000136116	7.286294946	0.018835906	0.02902	0.0000006520	-737.810175	6197.128544	27715
6	65	400	0.0968	-5796	-1	0.21	20551.49	0.0000309917	6.228113731	0.025780239	-0.00243	0.0000002094	-737.810175		-6534
											-0.03000				
										stopping criterion Σ=0; Σ	-0.003405176411				
											Σ	0.0000008615			

Jacobian

0.0000064489	-0.0000057969	0	0	-0.0000006520
-0.0000057969	0.0000084162	-0.0000016990	0	0
0	-0.0000016990	0.0000024560	-0.0000007569	0
0	0	-0.0000007569	0.0000009944	0
-0.0000006520	0	0	0	0.0000008615

inverse Jacobian

933294.7716	786307.8105	710695.2482	540972.7189	706413.7612
786307.8105	807808.4521	730128.3552	555764.9674	595158.8659
710695.2482	730128.3552	1191889.071	907251.6987	537927.4787
540972.7189	555764.9674	907251.6987	1696210.772	409463.96
706413.7612	595158.8659	537927.4787	409463.96	1695512.422

[F]	[Δx]
0.0069369692	6197.128544
0.0053311177	5614.524376
-0.0012602235	3530.014773
-0.0021589069	515.961554
-0.0034051764	737.810175

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 4

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-8694	-1	0.96	338227.57	0.0000085082	8.380949593	0.014236838	-0.10132	0.0000058269	4093.117544	-3421.522911	-8022
1	16	900	0.2204	-27715	-1	0.76	166993.74	0.0000136116	7.831619812	0.016304099	-0.03481	0.0000006280	4093.117544	-566.7642687	-24188
											0.13000				
										stopping criterion Σ=0; Σ	-0.006127957496				
											Σ	0.0000064549			
2	21	400	0.3526	8694	1	0.96	338227.57	0.0000085082	8.380949593	0.014236838	0.10132	0.0000058269	3421.522911	-4093.117544	8022
2	23	500	0.2468	-12976	-1	0.77	190171.01	0.0000121556	7.933209399	0.015889205	-0.04295	0.0000016551	3421.522911	-1948.574579	-11503
2	25	900	0.2468	-25555	-1	0.77	188580.17	0.0000121556	7.926813297	0.015914857	-0.04489	0.0000008784	3421.522911		-22133
											-0.01500				
										stopping criterion Σ=0; Σ	-0.001530003977				
											Σ	0.0000083604			
3	32	500	0.2468	12976	1	0.77	190171.01	0.0000121556	7.933209399	0.015889205	0.04295	0.0000016551	1948.574579	-3421.522911	11503
3	34	800	0.2204	-21688	-1	0.74	162662.02	0.0000136116	7.81162916	0.016387653	-0.03258	0.0000007511	1948.574579	798.7639351	-18941
											-0.01000				
										stopping criterion Σ=0; Σ	0.000374436202				
											Σ	0.0000024062			
4	43	800	0.2204	21688	1	0.74	162662.02	0.0000136116	7.81162916	0.016387653	0.03258	0.0000007511	-798.7639351	-1948.574579	18941
4	45	400	0.1102	9109	1	0.48	52606.86	0.0000272232	6.940828154	0.020757613	0.00469	0.0000002574	-798.7639351		8310
											-0.03500				
										stopping criterion Σ=0; Σ	0.002269130779				
											Σ	0.0000010085			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	27715	1	0.76	166993.74	0.0000136116	7.831619812	0.016304099	0.03481	0.0000006280	566.7642687	-4093.117544	24188
6	65	400	0.0968	-6534	-1	0.33	31805.22	0.0000309917	6.558142742	0.02325082	-0.00271	0.0000002077	566.7642687		-5967
											-0.03000				
										stopping criterion Σ=0; Σ	0.002096943068				
											Σ	0.0000008357			

Jacobian

0.0000064549	-0.0000058269	0	0	-0.0000006280
-0.0000058269	0.0000083604	-0.0000016551	0	0
0	-0.0000016551	0.0000024062	-0.0000007511	0
0	0	-0.0000007511	0.0000010085	0
-0.0000006280	0	0	0	0.0000008357

inverse Jacobian

956117.2803	810109.0778	726010.6185	540687.0449	718505.1279
810109.0778	831808.3481	745457.2598	555169.6802	608782.5611
726010.6185	745457.2598	1209528.934	900781.0746	545584.0649
540687.0449	555169.6802	900781.0746	1662387.64	406316.696
718505.1279	608782.5611	545584.0649	406316.696	1736514.579

[F]	[Δx]
-0.0061279575	-4093.117544
-0.0015300040	-3421.522911
0.0003744362	-1948.574579
0.0022691308	798.7639351
0.0020969431	-566.7642687

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 5

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-8022	-1	1.04	364397.76	0.0000085082	8.437656496	0.014046118	-0.09798	0.0000061069	822.7871268	-726.6128476	-7926
1	16	900	0.2204	-24188	-1	0.91	200300.90	0.0000136116	7.969712731	0.015743985	-0.03309	0.0000006841	822.7871268	-105.5573975	-23471
											0.13000				
										stopping criterion Σ=0; Σ	-0.001077990309				
											Σ	0.0000067910			
2	21	400	0.3526	8022	1	1.04	364397.76	0.0000085082	8.437656496	0.014046118	0.09798	0.0000061069	726.6128476	-822.7871268	7926
2	23	500	0.2468	-11503	-1	0.90	220714.24	0.0000121556	8.046465161	0.015445065	-0.04102	0.0000017830	726.6128476	-439.5999529	-11216
2	25	900	0.2468	-22133	-1	0.94	230681.41	0.0000121556	8.079990194	0.015317163	-0.04259	0.0000009621	726.6128476	0	-21407
											-0.01500				
										stopping criterion Σ=0; Σ	-0.000623468032				
											Σ	0.0000088520			
3	32	500	0.2468	11503	1	0.90	220714.24	0.0000121556	8.046465161	0.015445065	0.04102	0.0000017830	439.5999529	-726.6128476	11216
3	34	800	0.2204	-18941	-1	0.85	187458.07	0.0000136116	7.919447902	0.015944474	-0.03087	0.0000008148	439.5999529	-0.015372369	-18501
											-0.01000				
										stopping criterion Σ=0; Σ	0.000153569358				
											Σ	0.0000025978			
4	43	800	0.2204	18941	1	0.85	187458.07	0.0000136116	7.919447902	0.015944474	0.03087	0.0000008148	0.015372369	-439.5999529	18501
4	45	400	0.1102	8310	1	0.49	53972.04	0.0000272232	6.960221573	0.0206421	0.00449	0.0000002703	0.015372369		8310
											-0.03500				
										stopping criterion Σ=0; Σ	0.000358174487				
											Σ	0.0000010851			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	24188	1	0.91	200300.90	0.0000136116	7.969712731	0.015743985	0.03309	0.0000006841	105.56	-823	23471
6	65	400	0.0968	-5967	-1	0.37	35558.24	0.0000309917	6.642491483	0.022664074	-0.00263	0.0000002201	105.56		-5862
											-0.03000				
										stopping criterion Σ=0; Σ	0.0004674254				
											Σ	0.0000009042			

Jacobian

0.0000067910	-0.0000061069	0	0	-0.0000006841
-0.0000061069	0.0000088520	-0.0000017830	0	0
0	-0.0000017830	0.0000025978	-0.0000008148	0
0	0	-0.0000008148	0.0000010851	0
-0.0000006841	0	0	0	0.0000009042

inverse Jacobian

884762.7501	745142.0769	668991.5563	502354.9599	669376.2731
745142.0769	765462.4548	687235.2734	516054.4179	563744.8303
668991.5563	687235.2734	1120534.279	841424.6002	506132.3781
502354.9599	516054.4179	841424.6002	1553416.841	380061.7632
669376.2731	563744.8303	506132.3781	380061.7632	1612333.78

[F]	[Δx]
-0.0010779903	-822.7871268
-0.0006234680	-726.6128476
0.0001535694	-439.5999529
0.0003581745	-0.015372369
0.0004674254	-105.5573975

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 6

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-7926	-1	1.00	352408.69	0.0000085082	8.412213013	0.014131214	-0.09710	0.0000061253	-268.3902544	219.9339521	-7975
1	16	900	0.2204	-23471	-1	0.87	190424.05	0.0000136116	7.931361281	0.015896611	-0.03244	0.0000006911	-268.3902544	38.01860534	-23701
											0.13000				
									stopping criterion Σ=0; Σ		0.000456029738				
											Σ	0.0000068165			
2	21	400	0.3526	7926	1	1.00	352408.69	0.0000085082	8.412213013	0.014131214	0.09710	0.0000061253	-219.9339521	268.3902544	7975
2	23	500	0.2468	-11216	-1	0.86	210776.56	0.0000121556	8.011466049	0.015580307	-0.04033	0.0000017978	-219.9339521	119.8158634	-11316
2	25	900	0.2468	-21407	-1	0.89	218832.29	0.0000121556	8.039962097	0.01547006	-0.04167	0.0000009734	-219.9339521		-21627
											-0.01500				
									stopping criterion Σ=0; Σ		0.000097270189				
											Σ	0.0000088966			
3	32	500	0.2468	11216	1	0.86	210776.56	0.0000121556	8.011466049	0.015580307	0.04033	0.0000017978	-119.8158634	219.9339521	11316
3	34	800	0.2204	-18501	-1	0.81	177600.88	0.0000136116	7.878429262	0.016110934	-0.03035	0.0000008202	-119.8158634	-76.10732644	-18697
											-0.01000				
									stopping criterion Σ=0; Σ		-0.000019305963				
											Σ	0.0000026180			
4	43	800	0.2204	18501	1	0.81	177600.88	0.0000136116	7.878429262	0.016110934	0.03035	0.0000008202	76.10732644	119.8158634	18697
4	45	400	0.1102	8310	1	0.47	51695.38	0.0000272232	6.927596042	0.020836985	0.00447	0.0000002690	76.10732644		8386
											-0.03500				
									stopping criterion Σ=0; Σ		-0.000181163269				
											Σ	0.0000010892			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	23471	1	0.87	190424.05	0.0000136116	7.931361281	0.015896611	0.03244	0.0000006911	-38.01860534	268.3902544	23701
6	65	400	0.0968	-5862	-1	0.36	34418.18	0.0000309917	6.617849084	0.022833174	-0.00259	0.0000002213	-38.01860534		-5900
											-0.03000				
									stopping criterion Σ=0; Σ		-0.000150806063				
											Σ	0.0000009124			

Jacobian

0.0000068165	-0.0000061253	0	0	-0.0000006911
-0.0000061253	0.0000088966	-0.0000017978	0	0
0	-0.0000017978	0.0000026180	-0.0000008202	0
0	0	-0.0000008202	0.0000010892	0
-0.0000006911	0	0	0	0.0000009124

inverse Jacobian

877418.3539	738171.4792	663420.3159	499563.1751	664629.9133
738171.4792	758370.6529	681574.014	513233.1199	559152.7052
663420.3159	681574.014	1112454.086	837690.8	502529.9335
499563.1751	513233.1199	837690.8	1548913.28	378410.8553
664629.9133	559152.7052	502529.9335	378410.8553	1599440.45

[F]	[Δx]
0.0004560297	268.3902544
0.0000972702	219.9339521
-0.0000193060	119.8158634
-0.0001811633	-76.10732644
-0.0001508061	38.01860534

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 7

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-7975	-1	0.99	349233.64	0.0000085082	8.40532649	0.014154379	-0.09732	0.0000061017	-103.2760659	90.00523078	-7988
1	16	900	0.2204	-23701	-1	0.85	186676.91	0.0000136116	7.916278277	0.015957244	-0.03254	0.0000006865	-103.2760659	13.54338157	-23791
											0.13000				
									stopping criterion Σ=0; Σ		0.000142572813				
											Σ	0.0000067882			
2	21	400	0.3526	7975	1	0.99	349233.64	0.0000085082	8.40532649	0.014154379	0.09732	0.0000061017	-90.00523078	103.2760659	7988
2	23	500	0.2468	-11316	-1	0.84	207225.07	0.0000121556	7.998549009	0.015630669	-0.04044	0.0000017870	-90.00523078	53.19904573	-11353
2	25	900	0.2468	-21627	-1	0.87	214144.15	0.0000121556	8.023511147	0.015533563	-0.04180	0.0000009665	-90.00523078		-21717
											-0.01500				
									stopping criterion Σ=0; Σ		0.000071784087				
											Σ	0.0000088551			
3	32	500	0.2468	11316	1	0.84	207225.07	0.0000121556	7.998549009	0.015630669	0.04044	0.0000017870	-53.19904573	90.00523078	11353
3	34	800	0.2204	-18697	-1	0.80	174618.70	0.0000136116	7.865562181	0.016163688	-0.03046	0.0000008145	-53.19904573	-8.565709334	-18759
											-0.01000				
									stopping criterion Σ=0; Σ		-0.000015462794				
											Σ	0.0000026015			
4	43	800	0.2204	18697	1	0.80	174618.70	0.0000136116	7.865562181	0.016163688	0.03046	0.0000008145	8.565709334	53.19904573	18759
4	45	400	0.1102	8386	1	0.47	51453.11	0.0000272232	6.924039497	0.020858397	0.00449	0.0000002677	8.565709334		8395
											-0.03500				
									stopping criterion Σ=0; Σ		-0.000052601500				
											Σ	0.0000010822			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	23701	1	0.85	186676.91	0.0000136116	7.916278277	0.015957244	0.03254	0.0000006865	-13.54338157	103.2760659	23791
6	65	400	0.0968	-5900	-1	0.35	33985.86	0.0000309917	6.608290265	0.022899277	-0.00260	0.0000002202	-13.54338157		-5913
											-0.03000				
									stopping criterion Σ=0; Σ		-0.000058615355				
											Σ	0.0000009067			

Jacobian

0.0000067882	-0.0000061017	0	0	-0.0000006865
-0.0000061017	0.0000088551	-0.0000017870	0	0
0	-0.0000017870	0.0000026015	-0.0000008145	0
0	0	-0.0000008145	0.0000010822	0
-0.0000006865	0	0	0	0.0000009067

inverse Jacobian

882915.2641	743154.417	667862.6001	502680.877	668451.4312
743154.417	763463.0485	686113.6864	516417.9422	562639.0819
667862.6001	686113.6864	1119510.719	842623.363	505635.9642
502680.877	516417.9422	842623.363	1558281.129	380577.5767
668451.4312	562639.0819	505635.9642	380577.5767	1608975.255

[F]	[Δx]
0.0001425728	103.2760659
0.0000717841	90.00523078
-0.0000154628	53.19904573
-0.0000526015	-8.565709334
-0.0000586154	13.54338157

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 8

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-7988	-1	1.00	350012.76	0.0000085082	8.407022272	0.01414867	-0.09742	0.0000060979	15.64678921	-12.4224294	-7985
1	16	900	0.2204	-23791	-1	0.85	187234.06	0.0000136116	7.918540357	0.015948129	-0.03261	0.0000006854	15.64678921	-2.204883833	-23778
											0.13000				
									stopping criterion Σ=0; Σ		-0.000028874273				
											Σ	0.0000067832			
2	21	400	0.3526	7988	1	1.00	350012.76	0.0000085082	8.407022272	0.01414867	0.09742	0.0000060979	12.4224294	-15.64678921	7985
2	23	500	0.2468	-11353	-1	0.85	207812.31	0.0000121556	8.000700322	0.015622265	-0.04052	0.0000017846	12.4224294	-6.280508448	-11347
2	25	900	0.2468	-21717	-1	0.87	214800.99	0.0000121556	8.025838021	0.015524557	-0.04190	0.0000009647	12.4224294		-21704
											-0.01500				
									stopping criterion Σ=0; Σ		-0.000003283335				
											Σ	0.0000088472			
3	32	500	0.2468	11353	1	0.85	207812.31	0.0000121556	8.000700322	0.015622265	0.04052	0.0000017846	6.280508448	-12.4224294	11347
3	34	800	0.2204	-18759	-1	0.80	175254.17	0.0000136116	7.868322633	0.016152349	-0.03052	0.0000008135	6.280508448	6.976695969	-18745
											-0.01000				
									stopping criterion Σ=0; Σ		0.000000176288				
											Σ	0.0000025980			
4	43	800	0.2204	18759	1	0.80	175254.17	0.0000136116	7.868322633	0.016152349	0.03052	0.0000008135	-6.976695969	-6.280508448	18745
4	45	400	0.1102	8395	1	0.47	51661.65	0.0000272232	6.927101861	0.020839959	0.00449	0.0000002676	-6.976695969		8388
											-0.03500				
									stopping criterion Σ=0; Σ		0.000012651510				
											Σ	0.0000010811			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	23791	1	0.85	187234.06	0.0000136116	7.918540357	0.015948129	0.03261	0.0000006854	2.204883833	-15.64678921	23778
6	65	400	0.0968	-5913	-1	0.35	34046.65	0.0000309917	6.609641599	0.022889915	-0.00260	0.0000002200	2.204883833		-5911
											-0.03000				
									stopping criterion Σ=0; Σ		0.000008727435				
											Σ	0.0000009054			

Jacobian

0.0000067832	-0.0000060979	0	0	-0.0000006854
-0.0000060979	0.0000088472	-0.0000017846	0	0
0	-0.0000017846	0.0000025980	-0.0000008135	0
0	0	-0.0000008135	0.0000010811	0
-0.0000006854	0	0	0	0.0000009054

inverse Jacobian

884135.2837	744293.124	668819.3565	503247.8269	669267.4931
744293.124	764623.2528	687087.9435	516993.8804	563410.6029
668819.3565	687087.9435	1120956.442	843454.795	506278.9172
503247.8269	516993.8804	843454.795	1559632.545	380945.5608
669267.4931	563410.6029	506278.9172	380945.5608	1611104.18

[F]	[Δx]
-0.0000288743	-15.64678921
-0.0000032833	-12.4224294
0.0000001763	-6.280508448
0.0000126515	6.976695969
0.0000087274	-2.204883833

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 9

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-7985	-1	1.00	350374.55	0.0000085082	8.407808403	0.014146024	-0.09741	0.0000060997	11.27034377	-9.764773828	-7983
1	16	900	0.2204	-23778	-1	0.85	187641.76	0.0000136116	7.920191301	0.015941481	-0.03261	0.0000006857	11.27034377	-1.473030063	-23768
											0.13000				
									stopping criterion Σ=0; Σ		-0.000015901479				
											Σ	0.0000067854			
2	21	400	0.3526	7985	1	1.00	350374.55	0.0000085082	8.407808403	0.014146024	0.09741	0.0000060997	9.764773828	-11.27034377	7983
2	23	500	0.2468	-11347	-1	0.85	208205.99	0.0000121556	8.00213906	0.015616648	-0.04052	0.0000017854	9.764773828	-5.665890179	-11343
2	25	900	0.2468	-21704	-1	0.88	215309.93	0.0000121556	8.027635962	0.015517604	-0.04190	0.0000009652	9.764773828		-21694
											-0.01500				
									stopping criterion Σ=0; Σ		-0.000007559800				
											Σ	0.0000088502			
3	32	500	0.2468	11347	1	0.85	208205.99	0.0000121556	8.00213906	0.015616648	0.04052	0.0000017854	5.665890179	-9.764773828	11343
3	34	800	0.2204	-18745	-1	0.80	175605.01	0.0000136116	7.86984233	0.016146111	-0.03051	0.0000008139	5.665890179	1.614375179	-18738
											-0.01000				
									stopping criterion Σ=0; Σ		0.000001392479				
											Σ	0.0000025993			
4	43	800	0.2204	18745	1	0.80	175605.01	0.0000136116	7.86984233	0.016146111	0.03051	0.0000008139	-1.614375179	-5.665890179	18738
4	45	400	0.1102	8388	1	0.47	51710.89	0.0000272232	6.927823091	0.02083562	0.00449	0.0000002678	-1.614375179		8386
											-0.03500				
									stopping criterion Σ=0; Σ		0.000006357783				
											Σ	0.0000010817			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	23778	1	0.85	187641.76	1.36116E-05	7.920191301	0.015941481	0.03261	0.0000006857	1.473030063	-11.27034377	23768
6	65	400	0.0968	-5911	-1	0.35	34092.67	3.09917E-05	6.610663188	0.022882841	-0.00260	0.0000002201	1.473030063		-5910
											-0.03000				
									stopping criterion Σ=0; Σ		0.000006393787				
											Σ	0.0000009058			

Jacobian

0.0000067854	-0.0000060997	0	0	-0.0000006857
-0.0000060997	0.0000088502	-0.0000017854	0	0
0	-0.0000017854	0.0000025993	-0.0000008139	0
0	0	-0.0000008139	0.0000010817	0
-0.0000006857	0	0	0	0.0000009058

inverse Jacobian

883726.3969	743923.4822	668482.0413	502997.3527	668982.3671
743923.4822	764245.1827	686742.9138	516737.6927	563151.3258
668482.0413	686742.9138	1120411.02	843049.9879	506042.0283
502997.3527	516737.6927	843049.9879	1558832.824	380769.841
668982.3671	563151.3258	506042.0283	380769.841	1610404.839

[F]	[Δx]
-0.0000159015	-11.27034377
-0.0000075598	-9.764773829
0.0000013925	-5.665890179
0.0000063578	1.614375178
0.0000063938	-1.473030064

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 10

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-7983	-1	1.00	350336.58	0.0000085082	8.407725945	0.014146301	-0.09740	0.0000061002	-0.401422549	0.24529831	-7983
1	16	900	0.2204	-23768	-1	0.85	187627.86	0.0000136116	7.920135052	0.015941707	-0.03260	0.0000006858	-0.401422549	0.058059084	-23768
											0.13000				
										stopping criterion Σ=0; Σ	0.000001187876				
											Σ	0.0000067860			
2	21	400	0.3526	7983	1	1.00	350336.58	0.0000085082	8.407725945	0.014146301	0.09740	0.0000061002	-0.24529831	0.401422549	7983
2	23	500	0.2468	-11343	-1	0.85	208187.09	0.0000121556	8.002070061	0.015616917	-0.04051	0.0000017857	-0.24529831	0.045310755	-11343
2	25	900	0.2468	-21694	-1	0.88	215296.56	0.0000121556	8.027588783	0.015517786	-0.04189	0.0000009654	-0.24529831		-21695
											-0.01500				
										stopping criterion Σ=0; Σ	-0.000000358452				
											Σ	0.0000088513			
3	32	500	0.2468	11343	1	0.85	208187.09	0.0000121556	8.002070061	0.015616917	0.04051	0.0000017857	-0.045310755	0.24529831	11343
3	34	800	0.2204	-18738	-1	0.80	175576.86	0.0000136116	7.869720474	0.016146611	-0.03051	0.0000008141	-0.045310755	-0.544487718	-18739
											-0.01000				
										stopping criterion Σ=0; Σ	0.000000123019				
											Σ	0.0000025997			
4	43	800	0.2204	18738	1	0.80	175576.86	0.0000136116	7.869720474	0.016146611	0.03051	0.0000008141	0.544487718	0.045310755	18739
4	45	400	0.1102	8386	1	0.47	51694.78	0.0000272232	6.927587182	0.020837039	0.00449	0.0000002678	0.544487718		8387
											-0.03500				
										stopping criterion Σ=0; Σ	-0.000000625939				
											Σ	0.0000010818			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	23768	1	0.85	187627.86	0.0000136116	7.920135052	0.015941707	0.03260	0.0000006858	-0.058059084	0.401422549	23768
6	65	400	0.0968	-5910	-1	0.35	34091.59	0.0000309917	6.610639052	0.022883008	-0.00260	0.0000002201	-0.058059084		-5910
											-0.03000				
										stopping criterion Σ=0; Σ	-0.000000222710				
											Σ	0.0000009060			

Jacobian

0.0000067860	-0.0000061002	0	0	-0.0000006858
-0.0000061002	0.0000088513	-0.0000017857	0	0
0	-0.0000017857	0.0000025997	-0.0000008141	0
0	0	-0.0000008141	0.0000010818	0
-0.0000006858	0	0	0	0.0000009060

inverse Jacobian

883571.1344	743779.1659	668357.8493	502918.4147	668877.5103
743779.1659	764098.0505	686616.3414	516657.3599	563052.7496
668357.8493	686616.3414	1120219.906	842930.5044	505957.6041
502918.4147	516657.3599	842930.5044	1558622.659	380717.3005
668877.5103	563052.7496	505957.6041	380717.3005	1610136.352

[F]	[Δx]
0.0000011879	0.40142255
-0.0000003585	0.245298311
0.0000001230	0.045310757
-0.0000006259	-0.544487717
-0.0000002227	0.058059085

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Iteration 11

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)	pressure drop (Pa)
1	12	400	0.3526	-7983	-1	1.00	350300.12	0.0000085082	8.407646735	0.014146568	-0.09740	0.0000061001	-1.102568369	0.950998724	-7983
1	16	900	0.2204	-23768	-1	0.85	187587.87	0.0000136116	7.91997326	0.015942358	-0.03260	0.0000006858	-1.102568369	0.141673816	-23769
											0.13000				
									stopping criterion Σ=0; Σ		0.000001583582				
											Σ	0.0000067859			
2	21	400	0.3526	7983	1	1.00	350300.12	0.0000085082	8.407646735	0.014146568	0.09740	0.0000061001	-0.950998724	1.102568369	7983
2	23	500	0.2468	-11343	-1	0.85	208147.69	0.0000121556	8.001926176	0.015617479	-0.04051	0.0000017856	-0.950998724	0.540744448	-11343
2	25	900	0.2468	-21695	-1	0.88	215246.85	0.0000121556	8.02741338	0.015518464	-0.04189	0.0000009654	-0.950998724		-21696
											-0.01500				
									stopping criterion Σ=0; Σ		0.000000726086				
											Σ	0.0000088511			
3	32	500	0.2468	11343	1	0.85	208147.69	0.0000121556	8.001926176	0.015617479	0.04051	0.0000017856	-0.540744448	0.950998724	11343
3	34	800	0.2204	-18739	-1	0.80	175540.04	0.0000136116	7.869561121	0.016147265	-0.03051	0.0000008140	-0.540744448	-0.223278803	-18739
											-0.01000				
									stopping criterion Σ=0; Σ		-0.000000110621				
											Σ	0.0000025996			
4	43	800	0.2204	18739	1	0.80	175540.04	0.0000136116	7.869561121	0.016147265	0.03051	0.0000008140	0.223278803	0.540744448	18739
4	45	400	0.1102	8387	1	0.47	51688.04	0.0000272232	6.927488535	0.020837632	0.00449	0.0000002678	0.223278803		8387
											-0.03500				
									stopping criterion Σ=0; Σ		-0.000000681726				
											Σ	0.0000010818			
5	omitted to preserve linear indenpendency of Jacobian														
6	61	900	0.2204	23768	1	0.85	1.9E+05	1.36116E-05	7.91997326	0.015942358	0.03260	0.0000006858	-0.141673816	1.102568369	23769
6	65	400	0.0968	-5910	-1	0.35	3.4E+04	3.09917E-05	6.610542057	0.022883679	-0.00260	0.0000002201	-0.141673816		-5910
											-0.03000				
									stopping criterion Σ=0; Σ		-0.000000627811				
											Σ	0.0000009059			

Jacobian

0.0000067859	-0.0000061001	0	0	-0.0000006858
-0.0000061001	0.0000088511	-0.0000017856	0	0
0	-0.0000017856	0.0000025996	-0.0000008140	0
0	0	-0.0000008140	0.0000010818	0
-0.0000006858	0	0	0	0.0000009059

inverse Jacobian

883595.1532	743800.6368	668378.3123	502935.1464	668894.3818
743800.6368	764120.0603	686637.3206	516674.5165	563067.8998
668378.3123	686637.3206	1120254.202	842958.5474	505972.1032
502935.1464	516674.5165	842958.5474	1558681.159	380729.2204
668894.3818	563067.8998	505972.1032	380729.2204	1610176.49

[F]	[Δx]
0.0000015836	1.102568372
0.0000007261	0.950998727
-0.0000001106	0.540744451
-0.0000006817	-0.223278801
-0.0000006278	0.141673818

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Standard procedure (pressure drop independent Jacobian)

Iteration 12

Node	Pipe	Length (m)	Diameter (m)	Pressure drop (Pa)*	Sign	Velocity (m/s)	Re	ε/D	Colebrook: $\lambda^{-0.5}$	λ	Q (m^3/s)	|∂Q/∂(Δp)|	correction 1 (Pa)	correction 2 (Pa)
1	12	400	0.3526	-7983	-1	1.00	3.5E+05	8.50822E-06	8.407647007	0.014146567	-0.09740	0.0000061000	-0.067492331	0.067847344
1	16	900	0.2204	-23769	-1	0.85	1.9E+05	1.36116E-05	7.919963238	0.015942399	-0.03260	0.0000006858	-0.067492331	0.008751709
											0.13000			
									stopping criterion Σ=0; Σ		0.000000038119			
										Σ		0.0000067858		
2	21	400	0.3526	7983	1	1.00	3.5E+05	8.50822E-06	8.407647007	0.014146567	0.09740	0.0000061000	-0.067847344	0.067492331
2	23	500	0.2468	-11343	-1	0.85	2.1E+05	1.21556E-05	8.001919208	0.015617506	-0.04051	0.0000017856	-0.067847344	0.048257143
2	25	900	0.2468	-21696	-1	0.88	2.2E+05	1.21556E-05	8.027401075	0.015518512	-0.04189	0.0000009654	-0.067847344	
											-0.01500			
									stopping criterion Σ=0; Σ		0.000000102645			
										Σ		0.0000088510		
3	32	500	0.2468	11343	1	0.85	2.1E+05	1.21556E-05	8.001919208	0.015617506	0.04051	0.0000017856	-0.048257143	0.067847344
3	34	800	0.2204	-18739	-1	0.80	1.8E+05	1.36116E-05	7.869557693	0.016147279	-0.03051	0.0000008140	-0.048257143	0.032289467
											-0.01000			
									stopping criterion Σ=0; Σ		-0.000000021982			
										Σ		0.0000025996		
4	43	800	0.2204	18739	1	0.80	1.8E+05	1.36116E-05	7.869557693	0.016147279	0.03051	0.0000008140	-0.032289467	0.048257143
4	45	400	0.1102	8387	1	0.47	5.2E+04	2.72232E-05	6.927502331	0.020837549	0.00449	0.0000002678	-0.032289467	
											-0.03500			
									stopping criterion Σ=0; Σ		-0.000000004352			
										Σ		0.0000010818		
5	omitted to preserve linear indenpendency of Jacobian													
6	61	900	0.2204	23769	1	0.85	1.9E+05	1.36116E-05	7.919963238	0.015942399	0.03260	0.0000006858	-0.008751709	0.067492331
6	65	400	0.0968	-5910	-1	0.35	3.4E+04	3.09917E-05	6.610534676	0.022883731	-0.00260	0.0000002201	-0.008751709	
											-0.03000			
									stopping criterion Σ=0; Σ		-0.000000038358			
										Σ		0.0000009059		

Pipe	Final pressure drop (Pa)	Final flow distribution (dm^3/s)
12	-7983	-97.4
16	-23769	-32.6
21	7983	97.4
23	-11343	-40.5
25	-21696	-41.9
32	11343	40.5
34	-18740	-30.5
43	18740	30.5
45	8387	4.5
61	23769	32.6
65	-5910	-2.6

Jacobian

0.0000067858	-0.0000061000	0	0	-0.0000006858
-0.0000061000	0.0000088510	-0.0000017856	0	0
0	-0.0000017856	0.0000025996	-0.0000008140	0
0	0	-0.0000008140	0.0000010818	0
-0.0000006858	0	0	0	0.0000009059

inverse Jacobian

883612.1988	743816.4602	668392.1731	502944.3933	668905.9242
743816.4602	764136.2005	686651.4563	516683.938	563078.7323
668392.1731	686651.4563	1120275.844	842972.8491	505981.5662
502944.3933	516683.938	842972.8491	1558707.502	380735.4455
668905.9242	563078.7323	505981.5662	380735.4455	1610205.659

[F]	[Δx]
0.0000000381	0.067492339
0.0000001026	0.067847351
-0.0000000220	0.048257149
-0.0000000044	0.032289472
-0.0000000384	0.008751715

*from the previous iteration

**velocity calculated using calculated flow, Q from the previous iteration

Standard procedure (pressure drop independent Jacobian); Re=Re(Q)

Dejan Brkic, Strumicka 88, 11050 Belgrade, Serbia; dejanrgf@tesla.rcub.bg.ac.rs, dejanbrkic0611@gmail.com

Figure caption list

Figure 1. Convergence properties of the proposed method for the solution of the problem of water distribution analysis expressed in the nodal form (both with the independent Jacobian)

Etable 1.

Etable 2.

(Etable 1 and Etable 2 are submitted as Electronic Annexes to the discussion; do not embed them into the text, instead provide a link to this material)

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Manuscript Authors: DEJAN BRKIĆ

Corresponding Author Name and Address: DEJAN BRKIĆ
STRUMIČKA 88, 11050 BELGRADE, SERBIA

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I have accepted all your suggestions. I am not native English speaker and therefore I appreciate your grammar corrections of my text. Thank you!

Additional request for tables: I do not have any tables in my text; (Etable 1 and Etable 2 are submitted as Electronic Annexes to the discussion; do not embed them into the text, instead provide a link to this material). This is possible for technical papers, technical notes and case studies since there is separate item description in editorial system for such purposes. This item description does not exist for discussions. So I have uploaded them as figures. Please, advise me if you have additional requests with these materials.

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Dejan Brkić, Ph.D.