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# Melting of iron determined by X-ray absorption spectroscopy to 100 GPa

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Temperature, thermal history, and dynamics of Earth rely critically on the knowledge of the melting temperature of iron at the pressure conditions of the inner core boundary (ICB) where the geotherm crosses the melting curve. The literature on this subject is overwhelming, and no consensus has been reached, with a very large disagreement of the order of 2,000 K for the ICB temperature. Here we report new data on the melting temperature of iron in a laser-heated diamond anvil cell to 103 GPa obtained by X-ray absorption spectroscopy, a technique rarely used at such conditions. The modifications of the onset of the absorption spectra are used as a reliable melting criterion regardless of the solid phase from which the solid to liquid transition takes place. Our results show a melting temperature of iron in agreement with most previous studies up to 100 GPa, namely of 3,090 K at 103 GPa.

iron melting curve | XAS | megabar range

ron is the principal constituent of the Earth's core (1), and knowledge of its melting curve at inner core boundary (ICB) conditions is one of the major concerns in geophysics. At the ICB, corresponding to a depth of 5,150 km and to a pressure of 330 GPa, the solid inner core melts and the outer core is liquid. Even though the temperature at which the solid core becomes liquid should be adjusted to take into account the effects of light elements in the solid and liquid cores, the knowledge of the melting temperature of iron is an important fixed point in the thermal profile of Earth's interior. Earth's magnetic field is generated by a dynamo in the liquid iron core that has a convection motion as a result of cooling of the overlying mantle. Because the melting temperature of iron puts a constraint on the thermal gradient across the core—mantle boundary and the heat flow from the core, it represents the key to understand Earth's dynamo and therefore the implications to the terrestrial magnetic field.

A considerable effort has been expended to study the melting of iron at high pressure both theoretically (2–5) and experimentally, but this has led to considerable discrepancies in the estimates of the temperature in the center of Earth. This discrepancy, as large as 2,000 K at ICB conditions (330 GPa), has a significant impact on dynamic and thermal evolution models. The numerous studies have been summarized in several recent papers (6, 7).

Besides shock compression, laser heating in diamond anvil cells (LHDAC) allows one to generate the very high pressure and temperature conditions of Earth's core. In LHDAC studies, the maximum pressure for which iron melting temperatures have been reported is 200 GPa (8, 9), but the difference in the melting temperature in these measurements exceeds 1,000 K. Even the two most recent studies using synchrotron X-ray diffraction (XRD) and X-ray Mössbauer techniques (8, 10) show melting temperatures differing by 800 K at 100 GPa. The difficulty in measuring the melting temperature is particularly concerning, given that two X-ray diffraction measurements, carried out at the same beamline at the European Synchrotron Radiation Facility (ESRF) (8, 11), led to a difference in the melting temperature of 980 K at 130 GPa.

Here we report a determination of the solid–liquid phase boundary of iron compressed to over 100 GPa in an LHDAC by means of energy-dispersive X-ray absorption spectroscopy (EDXAS) using a well calibrated optical system and a novel sample encapsulating technique, which avoids chemical reactions and deterioration of the sample geometry.

X-ray absorption spectroscopy (XAS) provides structural information within a few angstroms around the photoabsorbing atom, and therefore maintains the same sensitivity and accuracy regardless of the physical state of the investigated sample (crystalline, amorphous, or liquid). This is a considerable asset with respect to diffraction techniques in which the onset of melting appears as a weak diffuse halo superimposed onto strong Bragg reflections from partially molten sample and sample environment. Similarly to diffraction techniques, X-ray absorption near edge structure (XANES) spectra may distinguish different crystallographic phases, but, in addition, it may shed some light on the electronic structure. A further advantage with respect to other methods is that, given its chemical selectivity, the XANES spectra contain solely the signal relative to the absorbing element, without any interference of the container or experimental environment. This is particularly convenient when the sample environment is particularly bulky, such as at high-pressure conditions. From the XANES part of the spectrum, it is possible to retrieve the coordination geometry of the atom of interest and its speciation, giving information about possible chemical reactions that may

#### **Significance**

There is a long-standing controversy over the melting curve of Fe at high pressure as determined from static laser heated diamond anvil cell and dynamic compression studies. X-ray absorption spectroscopy measurements are used here as a criterion to detect melting under pressure. Confronted with a diversity of obtained melting curves, this technique, used at such pressure and temperature conditions, is eligible to be at the forefront to probe Earth's deep interior. Furthermore, the experiment reported here holds promise for addressing important issues related to the structure and phase diagram of compressed melts, such as the existence of structural complexity (polyamorphism) in the liquid phase or the extent of icosahedral ordering whose investigation has been limited until now to ambient conditions.

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The authors declare no conflict of interest.

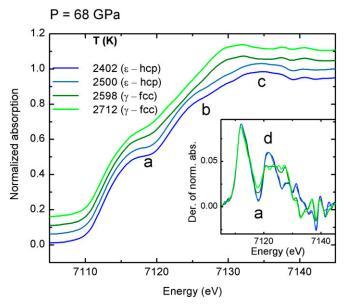
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**Fig. 1.** XANES spectra of iron recorded at 68 GPa with increasing temperature through the  $\varepsilon$ -hcp to  $\gamma$ -fcc phase transition. The blue curves correspond to the  $\varepsilon$ -hcp structure, and the green curves correspond to the  $\gamma$ -fcc phase. (*Inset*) The derivatives of the XANES spectra are reported.

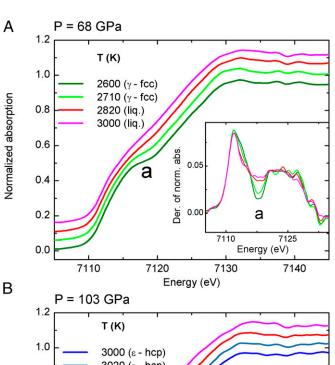
occur at specific conditions of the sample. EDXAS allows fast (from nanoseconds to a few seconds per spectrum depending on the experimental conditions) acquisition of the whole spectrum with a small (<5  $\mu m)$  X-ray focal spot. These are significant advantages for studies of molten systems at high pressure with in situ LHDAC, in which samples are small and unstable under laser heating. In a previous exploratory study (12), EDXAS was coupled to an in situ LHDAC to follow the structural evolution of Fe up to 3,000 K and 80 GPa, assessing the capability of the method for melting diagnostics. A major issue in EDXAS studies is that the sample is required to maintain uniform thickness during heating and melting over an area larger than the synchrotron X-ray beam diameter. For this reason, particular care has been taken in the sample preparation (see Materials and Methods and Supporting Information).

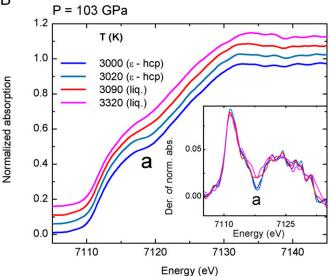
#### Results

Fig. 1 shows some illustrative XANES spectra of iron between 2,400 K and 2,710 K along the 68-GPa heating series. The XANES spectra were normalized to one absorption event and are shown together with their derivatives (Fig. 1, *Inset*). They show evidence of a structural phase transition that, according to the well-established iron phase diagram in this P-T range, can be attributed to  $\varepsilon$ -Fe (hcp) to  $\gamma$ -Fe (fcc) transition. The spectra collected at lower temperature (blue curves) depict features typical of the ε-hcp phase (13), characterized by a pronounced shoulder in the onset of the absorption, that gives rise to a plateau (feature "a"), followed by a bump (feature "b") and by a maximum (feature "c"). Upon heating (green curves), some changes occur: plateau "a" is smoothed out, bump "b" disappears, and maximum "c" shifts to lower energy (14, 15). These modifications are even more evident in the derivatives of the spectra (Fig. 1, Inset). At the transition, the deep minimum in the derivative corresponding to the plateau in the normalized spectra, both indicated as "a," becomes more shallow, and peak "d" (originating from bump "b") flattens out to a constant value between  $\sim$ 7,120 eV and  $\sim$ 7,128 eV. These changes are observed for all heating series (see Supporting Information) in agreement with the known  $\varepsilon$ -hcp to  $\gamma$ -fcc phase boundary.

Fig. 2 shows XANES spectra through the solid to liquid phase transitions at 68 GPa from 2,600 K to 3,000 K (Fig. 24) and at 103 GPa from 3,000 K to 3,320 K (Fig. 2B). The modifications of the onset of the absorption can be used as a signature for the solid to liquid phase transition. At the solid (either  $\gamma$ -fcc or  $\varepsilon$ -hcp) to liquid phase transition, the data show a discontinuous behavior. The derivatives of the XANES highlight this change, with minimum "a" flattening abruptly.

The energy region around plateau "a" between 7,115 eV and 7,120 eV is the most sensitive to disruptions in crystalline order. This part of the spectrum is affected by broadening with increasing temperature, ascribed by recent density functional theory (DFT) based theoretical calculations (16) to the thermal motion of the atoms. However, at melting, either from  $\varepsilon$ -hcp or  $\gamma$ -fcc, the broadening increases discontinuously following the breakdown of crystalline order characteristic of the liquid phase. A similar effect has been observed at all of the recorded pressures (see *Supporting Information*). The K edge XANES of iron involves, in the dipole approximation, the electronic transition from the 1s to the empty 4p states (17). The observed smoother





**Fig. 2.** XANES spectra of iron recorded at 68 GPa (A) and 103 GPa (B) with increasing temperature through the  $\gamma$ -fcc to liquid (A) and the  $\epsilon$ -hcp to liquid (B) phase transition. (*Insets*) The derivatives of the XANES spectra are reported.

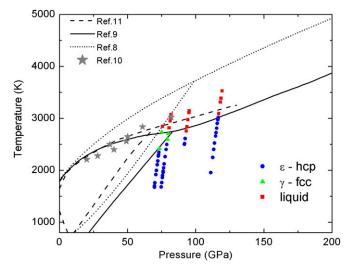


Fig. 3. P-T conditions at which XANES spectra were collected. Blue dots correspond to  $\epsilon$ -hcp Fe. Green triangles correspond to  $\gamma$ -fcc Fe. Red squares correspond to liquid Fe. Half thermal pressure has been considered. This has been determined from Fe phonon density of states to 151 GPa (10). Phase boundaries for iron from other experimental studies are also shown (solid black line, ref. 9; dashed black line, ref. 11; dotted line, ref. 8; stars, ref. 10).

absorption onset in the liquid phase can therefore be attributed to a broader distribution of empty 4p states as a consequence of the lack of crystalline order. The same effect of discontinuous broadening in the XANES spectra has not only been theoretically predicted by DFT calculations on iron at high temperature and pressure conditions (16) but has also been observed experimentally at the solid to liquid transition in other transition metals such as Cu (18) and Ni (19) at ambient pressure. In these studies, the solid to liquid phase transition was additionally confirmed by combined X-ray diffraction measurements.

Fig. 3 shows the P-T conditions at which all of the XANES measurements have been collected. Different symbols and colors correspond to  $\varepsilon$ -Fe (blue dots),  $\gamma$ -Fe (green triangles) and liquid Fe (red squares) phases as determined from the XANES spectra. Phase boundaries reported in refs. 8-11 are also shown for comparison. The phase diagram is reported with thermal pressure corrections (10).

#### Discussion

In the context of continuous efforts to provide additional experimental data toward resolving the discrepancy in the measured melting curve of Fe at high pressure, the results here reported are an independent measurement of the melting curve obtained by an experimental technique different from those used in previous experimental studies. The XAS experiment provides continuous monitoring of the changes of both the atomic and electronic structure as a function of temperature, and it is optimally suited to detect the onset of order-disorder or solid-liquid transitions. The melting criterion here adopted is based on changes occurring in the near-edge region of the absorption spectrum (XANES) that is known to be less affected by thermal damping and by the noise associated with extreme experimental conditions. We show here that the detection of the new phase does not appear gradually as a weak background superimposed to a much larger signal as in XRD methods but as a discontinuous change in the XANES signal that has similar amplitude with respect to that in the solid phase. This is an advantage of XANES over XRD because, in a partially molten sample caused by temperature instabilities (11), the signature of the melting has the same intensity as that of the solid sample whereas, in XRD, the diffused halo characteristic of the liquid sample is weak with respect to the signal coming from the solid part of the sample. This is especially true when phenomena defined as "recrystallization" (11) or "fast crystallization" (8) occur, giving rise to intense Bragg peaks.

Fig. 4 reports a comparison between the experimental XANES recorded at 68 GPa at different temperatures (blue line, ε-Fe (hcp); green line,  $\gamma$ -Fe (fcc); red line, liquid iron) compared with full multiple-scattering calculations to simulate the XANES region of the spectra at thermodynamic conditions comparable to the experimental ones (the details of the calculations are reported in Supporting Information). Concerning the hcp to fcc transition, the calculations confirm the flattening of the bump "b" and the shifts of the maximum "c" to lower energy. On the other side, the XANES calculation of iron in the fcc phase shows a second maximum just above 7,135 eV which is less evident in the experimental data presented in this work. As well, the smoothing of the plateau "a" discussed before on Fig. 1 is less pronounced in the calculated XANES. Approximations used for the theoretical XANES calculations could be invoked to explain these discrepancies. More interesting, instead, is the behavior of the onset of the absorption that has been used in discussing Fig. 2 as a signature for the solid to liquid phase transition. In fact, consistent with the experimental

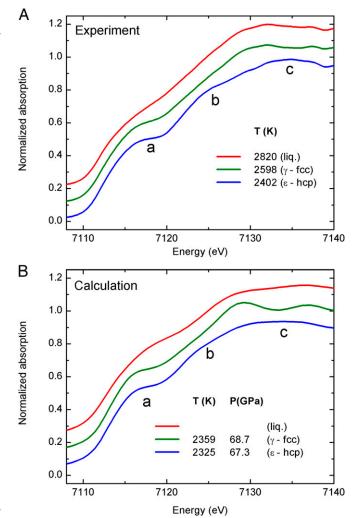


Fig. 4. Experimental XANES spectra of iron recorded at 68 GPa (A). Calculated XANES spectra of iron in the  $\varepsilon$ -hcp phase (blue line),  $\gamma$ -fcc phase (green line), and liquid phase (red line) (B).

data, the XANES calculation shows the same modifications of plateau "a" between 7,115 eV and 7,120 eV in the liquid phase with respect to the solid phases characteristic of the disruption of the crystalline order.

The present results show excellent agreement for the ε-Fe (hcp) to  $\gamma$ -Fe (fcc) transition reported earlier (6, 7), and the present melting data are in agreement with most previous studies up to 100 GPa resulting in a flat melting curve near 3,000 K at that pressure range. This is in stark disagreement with the recent XRD study by Anzellini et al. (8). The latter reports a much steeper melting curve at that pressure range and a melting temperature that is 700 K higher than the majority of all previous studies (6). This difference has significant implications for estimating the temperature in Earth's interior, which determines the value of the temperature jump at the core-mantle boundary, which is key for calculating the core-mantle heat flow, inner core age, dynamo models, and cooling history of Earth. Although an accurate extrapolation of the present data to Earth's core conditions is difficult given the limited number of experimental data above the triple point, our results are in agreement with the majority of diamond anvil cells (DACs) measurements in the 100-GPa pressure range (7) and with previous data to 200 GPa (9). The latter suggests a melting temperature of iron below 5,000 K when extrapolated to ICB conditions.

The experimental method here reported paves the way for extensive studies of molten metals at extreme pressures. For liquids, it is known that frustration, defined as the presence of locally preferred structures incompatible with the crystal periodicity, may have important consequences in the melting. For molten iron, together with other metals with partially filled d bands, liquid frustration was proposed as an explanation for the low slope of the melting curve (20). In the present work, the analysis is focused on the features of the near-edge region of the XAS spectrum because they are clear fingerprints for the occurrence of melting. However, previous studies have demonstrated that XAS is capable to evidence the existence and extent of preferred local geometries in molten metals at ambient conditions (18, 19). Therefore, beyond geophysical implications, the present results may be used to investigate the structure of compressed liquid Fe and possibly validate the hypothesis on the presence of frustration.

- 1. Poirier J-P (2000) Introduction to the Physics of the Earth's Interior (Cambridge Univ Press, New York), 2nd Ed.
- Alfè D, Gillan MJ, Price GD (1999) The melting curve of iron at the pressures of the Earth's core from ab initio calculations. Nature 401(6752):462–464.
- Laio A, Bernard S, Chiarotti GL, Scandolo S, Tosatti E (2000) Physics of iron at Earth's core conditions. Science 287(5455):1027–1030.
- Sola E, Alfè D (2009) Melting of iron under Earth's core conditions from diffusion Monte Carlo free energy calculations. Phys Rev Lett 103(7):078501.
- Belonoshko AB, Ahuja R, Johansson B (2000) Quasi-ab initio molecular dynamic study of Fe melting. Phys Rev Lett 84(16):3638–3641.
- of Fe melting. *Phys Rev Lett* 84(16):3638–3641.

  6. Komabayashi T, Fei Y (2010) Internally consistent thermodynamic database for iron to the Earth's core conditions. *J Geophys Res* 115(B3):803202.
- Boehler R, Ross M (2007) Properties of rocks and minerals High-pressure melting. Treatise on Geophysics, ed Schubert G (Elsevier, Amsterdam), pp 527–541.
- 8. Anzellini S, Dewaele A, Mezouar M, Loubeyre P, Morard G (2013) Melting of iron at
- Earth's inner core boundary based on fast X-ray diffraction. *Science* 340(6131):464–466.

  9. Boehler R (1993) Temperatures in the Earth's core from melting-point measurements.
- of iron at high static pressures. *Nature* 363(6429):534–536.

  10. Jackson JM, et al. (2013) Melting of compressed iron by monitoring atomic dynamics. *Earth Planet Sci Lett* 362:143–150.
- Boehler R, Santamaría-Pérez D, Errandonea D, Mezouar M (2008) Melting, density, and anisotropy of iron at core conditions: New X-ray measurements to 150 GPa. J Phys Conf Ser 121(2):022018.
- Boehler R, Mushoff HG, Ditz R, Aquilanti G, Trapananti A (2009) Portable laserheating stand for synchrotron applications. Rev Sci Instrum 80(4):045103.
- 13. Mathon O, et al. (2004) Dynamics of the magnetic and structural  $\alpha$ – $\epsilon$  phase transition in iron. *Phys Rev Lett* 93(25):255503.
- Filipponi A, et al. (1998) Single-energy X-ray absorption detection: A combined electronic and structural local probe for phase transitions in condensed matter. J Phys Condens Matter 10(1):235.
- Marini C, et al. (2014) A microsecond time resolved X-ray absorption near edge structure synchrotron study of phase transitions in Fe undergoing ramp heating at high pressure. J Appl Phys 115(9):093513.

### **Materials and Methods**

The pressure is generated using a Boehler–Almax plate DAC equipped with monocrystalline conical diamond anvils (21) of 250–300  $\mu m$  of diameter. A rhenium gasket is preindented to a thickness 40  $\mu m$ . A hole of 100  $\mu m$  diameter is then drilled on the culet imprint.

The sample container consists of two discs of sapphire manufactured using a combination of micropolishing and focused ion beam milling (FIBM). The cavity dimension of 18  $\mu m$  diameter and 6  $\mu m$  depth is chosen to optimize the synchrotron beam condition at the beamline ID24 (22) at ESRF. The single-crystal capsule and its lid are embedded in very fine-grained (3–5  $\mu m$  grain size) dried Al $_2$ O $_3$  powder, which molds around the capsule to prevent fracture during loading and after laser heating. One ruby grain of 2–3  $\mu m$  size was also mixed with the Al $_2$ O $_3$  powder (see Supporting Information).

The principal optical layout of the laser heating and temperature measurement system is very similar to the one described in ref. 23. The major difference is that the optical components do not interfere with the direct X-ray beam, allowing true simultaneous measurements of temperature from both sides of the sample as well as the X-ray absorption spectra. Further details are given in *Supporting Information*.

The XAS measurements in transmission geometry are carried out at the dispersive extended X-ray absorption fine structure (EXAFS) beamline ID24 at ESRF (22). The size of the beam at the sample is of  $5 \times 5 \mu m^2$  FWHM. Spectra are recorded using a CCD-based position sensitive detector. Pixel energy calibration is obtained by measuring spectra on a metallic Fe foil at ambient conditions. XAS spectra are collected every few seconds before, during, and after heating in four different runs in the pressure range 63-103 GPa and temperatures up to 3,530 K. For each heating cycle, the laser power is ramped up incrementally and kept constant for several seconds to record the XAS spectrum and light emission to measure the temperature. Pressures are determined before and after heating cycles using both ruby and the Raman spectra of the diamond anvil tips (24), with the accuracy within 2 GPa at the highest pressure achieved. After several heating cycles, these pressures are within 5 GPa. XANES spectra of the same sample are recorded at the beginning of each heating cycle and show that chemical reactions of the sample with the environment, if any, occur for a fraction of the sample that is below the XANES detection limit. Moreover, in each cycle we find the same transition temperatures within the experimental error. See Supporting Information for additional experimental details.

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- Mazevet S, et al. (2014) Ab initio calculation of x-ray absorption of iron up to 3 Mbar and 8000 K. Phys Rev B 89(10):100103.
- Raji AT, Scandolo S, Härting M, Britton DT (2013) Probing the structure of iron at extreme conditions by X-ray absorption near-edge structure calculations. High Pressure Res 33(1):119–123.
- Di Cicco A, Trapananti A (2007) Study of local icosahedral ordering in liquid and undercooled liquid copper. J Non-Cryst Solids 353(32-40):3671–3678.
- Di Cicco A, et al. (2014) Local fivefold symmetry in liquid and undercooled Ni probed by x-ray absorption spectroscopy and computer simulations. Phys Rev B 89(6):060102.
- Ross M, Boehler R, Errandonea D (2007) Melting of transition metals at high pressure and the influence of liquid frustration: The late metals Cu, Ni, and Fe. Phys Rev B 76(18):184117.
- Boehler R, De Hantsetters K (2004) New anvil designs in diamond-cells. High Pressure Res 24(3):391–396.
- Pascarelli S, Mathon O, Muñoz M, Mairs T, Susini J (2006) Energy-dispersive absorption spectroscopy for hard-X-ray micro-XAS applications. J Synchrotron Radiat 13(Pt 5):351–358
- Boehler R (2000) High-pressure experiments and the phase diagram of lower mantle and core materials. Rev Geophys 38(2):221–245.
- Akahama Y, Kawamura H (2010) Pressure calibration of diamond anvil Raman gauge to 410 GPa. J Phys Conf Ser 215(1):012195.
- Murphy CA, Jackson JM, Sturhahn W, Chen B (2011) Melting and thermal pressure of hcp-Fe from the phonon density of states. Phys Earth Planet Inter 188(1-2):114–120.
- Ravel B, Newville M (2005) ATHENA, ARTEMIS, HEPHAESTUS: Data analysis for X-ray absorption spectroscopy using IFEFFIT. J Synchrotron Radiat 12(Pt 4):537–541.
- Rehr JJ, Kas JJ, Vila FD, Prange MP, Jorissen K (2010) Parameter-free calculations of X-ray spectra with FEFF9. Phys Chem Chem Phys 12(21):5503–5513.
- Komabayashi T, Fei Y, Meng Y, Prakapenka V (2009) In-situ X-ray diffraction measurements of the γ-ε transition boundary of iron in an internally-heated diamond anvil cell. Farth Planet Sci Lett 282(1-4):252–257.
- Soper AK (1996) Empirical potential Monte Carlo simulation of fluid structure. Chem Phys 202(2-3):295–306.
- 30. Waseda Y (1980) The Structure of Non-Crystalline Materials (McGraw-Hill, New York).