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Proof of Concept for an Ultrasensitive Technique to Detect and Localize Sources of Elastic Nonlinearity Using Phononic Crystals

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The appearance of nonlinear effects in elastic wave propagation is one of the most reliable and sensitive indicators of the onset of material damage. However, these effects are usually very small and can be detected only using cumbersome digital signal processing techniques. Here, we propose and experimentally validate an alternative approach, using the filtering and focusing properties of phononic crystals to naturally select and reflect the higher harmonics generated by nonlinear effects, enabling the realization of time-reversal procedures for nonlinear elastic source detection. The proposed device demonstrates its potential as an efficient, compact, portable, passive apparatus for nonlinear elastic wave sensing and damage detection.

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In recent years, phononic crystals (PCs) have attracted great attention due to their unconventional dynamic behavior, with effects such as negative refraction [1], frequency band gaps [2,3], wave filtering or focusing [4–6], acoustic cloaking [7–9], subwavelength sensing [10,11], etc. Their periodic structure, rather than single material constituents, is responsible for their behavior, which exploits Bragg scattering [12,13]. Their attractive properties to act as stop-band filters [12] or to concentrate energy in selected frequency ranges [14] makes them potentially interesting for nonlinear elastic source detection and to reveal the presence of defects, e.g. cracks, in a sample. This is because, in general, a nonlinear response is generated at the defect location and several possible features may appear, including the generation of higher order harmonics [15–17] or subharmonics [18,19], the nonlinear dependence of the elastic modulus and of attenuation coefficients on strain [20–22], and, as a consequence, the shift of the resonance frequency with increasing excitation amplitude [23,24] and the failure of the superposition principle [25,26]. All of these possible signatures can be used to detect and monitor the presence and evolution of damage, exploiting the greater sensitivity of nonlinear detection techniques compared to conventional linear ones [27].

In the past years, nonlinear imaging techniques such as *b* scan, *c* scan, and tomography [28] have attracted much interest. A particularly robust and efficient approach is the combination of time reversal (TR) and nonlinear elastic wave spectroscopy (NEWS). This technique (TR-NEWS) exploits space-time focusing of the wave field achieved in TR [29] and applies it to a defect acting as a source of nonlinear elastic waves [30–33]. The scattered signal is recorded, the frequency generated by the primary source is filtered out using a bandpass filter, and the resulting signal is time reversed and reinjected by the receiver: due to the $(t \to -t)$ symmetry, the wave field back propagates to its original (nonlinear) source, focusing energy at the defect location at a specific time. Many studies have proved the efficiency and robustness of TR-NEWS in various configurations, for different types of nonlinear sources [34–36] and in assorted experimental conditions [31]. However, TR-NEWS relies—as do most of the techniques for both the detection and the location of damage—on extensive signal manipulation (normally, digital filtering), which might be critical in the case of short signals and/or when continuous signal acquisition is required (such as in acoustic emissions). Furthermore, the nonlinear components of the wave field are often very small, if not submerged by the noise level, making it difficult to detect and estimate them. The concept adopted in this Letter overcomes these limitations, combining TR-NEWS and phononic crystals in order to introduce a technique capable of filtering out and concentrating energy in target frequency ranges. We experimentally demonstrate the feasibility and the efficiency of this technique, providing the proof of concept for an ultrasensitive phononic crystal device to detect and localize nonlinear elastic sources such as cracks or delaminations.

A schematic representation of the experimental setup is given in Fig. 1. The sample is a pristine $300 \times 300 \times 3$ mm^3 aluminum plate (the density $\rho = 2700$ kg/m^3, the Young's modulus $E = 70$ GPa, and the Poisson's ratio $\nu = 0.33$),

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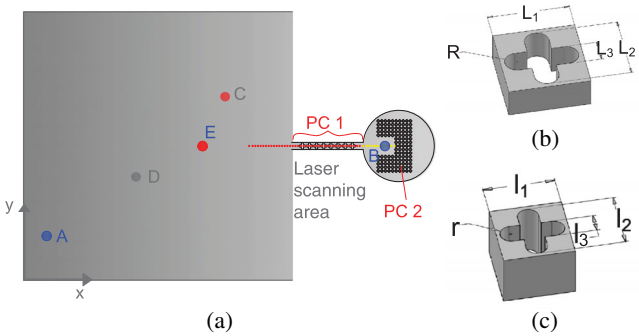

FIG. 1. (a) Schematic representation of the specimen composed of an aluminum plate connected to a filtering phononic crystal region (PC1) and a chaotic cavity [37] with an additional focusing phononic crystal–based structure (PC2). Three-dimensional view of the unit cells for (b) the PC1 region and (c) the PC2 region.

attached to which is a device, consisting of two phononic crystal regions (referred to as PC1 and PC2, respectively). PC1 consists of a 1D array of eight crosslike cavities cut in a narrow rectangular waveguide and PC2 of a C-shaped array of smaller unit cells. The cavities are fabricated using water-jet cutting, with different lattice parameters depending on the filtering [Fig. 1(b)] or reflecting [Fig. 1(c)] function that they are designed for. Specifically, the lattice parameters are $L_1 = 8$ mm, $L_2 = 0.9L_1$, and $L_3 = 2R = 0.3L_1$ for PC1 and $l_1 = 4$ mm, $l_2 = 0.9l_1$, and $l_3 = 2r = 0.3l_1$ for PC2, respectively. A crosslike geometry is chosen because it allows large band gap (BG) nucleation [38].

In order to investigate the BG structure of the PC1 region, its transmission spectrum is first investigated in a pitch-catch experiment [38] according to the schematic representation of Fig. 1(a) (see Ref. [39] for details). An ultrasonic pulse with a frequency content between 50 and 450 kHz is launched by a transducer attached to the top surface of the plate [point E in Fig. 1(a)] and received at points A and B using 5-mm-diameter piezoelectric disk sensors. Figure 2(a) shows the fast Fourier transform (FFT) of the input signal in E (the green line) and those recorded in A and B (the blue and red lines, respectively). A large BG appears between 172 and 244 kHz, highlighted by a considerable frequency drop at the corresponding frequencies (up to 100 dB). Three smaller BGs are visible around 153, 285, and 380 kHz. On the contrary, the spectral content of the signal recorded in the plate [the blue line in Fig. 2(a)], which is not subject to any filtering, shows the same frequency content as the excitation. These results are in agreement with numerically computed dispersion diagrams using Bloch-Floquet theory [41] in full 3D FEM simulations [Fig. 2(b)]. Here, the band structure is shown in terms of the reduced wave vector $k^* = [k_x L_1/\pi; k_y L_1/\pi]$, varying along the first irreducible Brillouin zone boundary $\Gamma - X$, with colors indicating mode polarization [39]. The BGs are highlighted in grey.

Further information on the dynamical properties of the PC1 region is obtained by injecting a short pulse at point E and using a scanning laser Doppler vibrometer (SLDV) to measure the out-of-plane component of the velocity at the surface along the dotted path highlighted in Fig. 1(a)

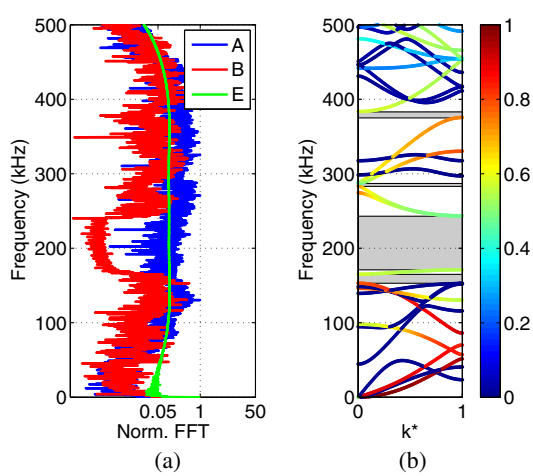

FIG. 2. (a) Experimental normalized transmission frequency spectrum and (b) the corresponding numerically predicted dispersion band structure for the PC1 region. Mode polarization is indicated by color, ranging from pure in plane (blue) to pure out of plane (red).

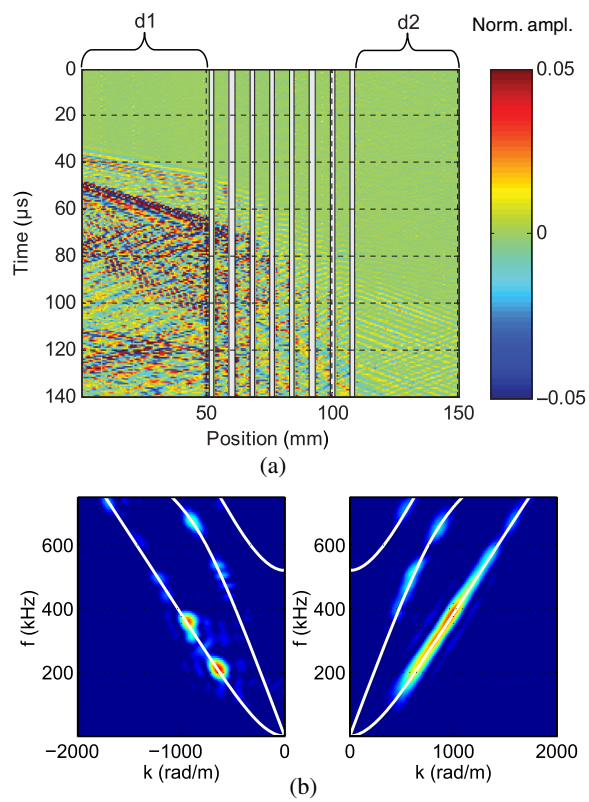

FIG. 3. (a) Out-of-plane displacement as a function of time t and position d along the dotted line in Fig. 1(a). White areas correspond to the crosslike cavities of the PC1 region. (b) Frequency f vs wave number k representation of the measured signals. Theoretical dispersion curves (in white) are superimposed.

(details are provided in the Supplemental Material [39]). Results for the space-time evolution of the measured amplitudes are shown in Fig. 3(a). Because of the excitation, mainly antisymmetric $A0$ Lamb waves are generated. However, Fig. 3(a) also clearly shows the presence of the $S0$ mode (i.e., the faster waves visible in the $t = 40\ \mu$s region), derived from direct generation by the transducer. Strong reflections of the incident waves are clearly visible at a distance $d = 50$ mm (corresponding to the first cavity in the PC1 waveguide) due to Bragg scattering from PC1. Finally, Fig. 3(a) highlights a slight variation of the slope for the modes crossing the PC1 region, corresponding to a gradual decrease of the wave speed with the distance traveled in PC1.

The signals detected at various positions along the path are processed by applying a two-dimensional (2D) FFT and determining the energy values for each processed point. This enables us to obtain a frequency wave number representation [Fig. 3(b)]. Data are shown for the $d1$ acquisition region of the plate (i.e., from $d = 0$ up to the first cavity), with negative and positive values of the wave number k_x corresponding to reflected and incident waves, respectively. This representation clearly identifies the energy distribution among the excited modes. The energy maxima of the reflected waves [Fig. 3(b), left panel] occur near the predicted BG frequency range, i.e. around 200 and 380 kHz, associated with the incident $A0$ mode [Fig. 3(b), right panel]. The excited $S0$-mode frequencies are greater than 450 kHz [see Fig. 3(b)], i.e., outside the PC1 BG. In this frequency range, the polarization of the propagating waves in PC1 is predominantly in plane [see Fig. 2(b)]. Therefore, most of the $S0$ wave field appears to be reflected since the SLDV setup is mainly sensitive to out-of-plane components (see also the Supplemental Material [39]). Numerically predicted dispersion curves (the white lines) are superimposed onto the experimental data, showing excellent agreement (see also the Supplemental Material [39]).

The PC1 region thus acts as a natural filter for frequencies in the 172–244 kHz range. The excitation of a nonlinear elastic material with a monochromatic wave of frequency falling inside the BG of PC1 (e.g., 200 kHz) produces higher harmonics in the plate that can cross the PC1 barrier and enter the circular "chaotic cavity" [37]. Owing to its ergodic properties and negligible absorption, the latter is widely used in TR experiments to generate multiple reflections and a reverberant acoustic field, making a single transducer sufficient for signal acquisition [37,42,43]. The additional C-shaped phononic crystal structure (PC2) is designed to reflect the higher harmonics of the signal falling within the BG and to concentrate them in the geometric center of the mirror, thus enhancing their signal-to-noise ratio. Analysis of SLDV-measured signals filtered at the frequencies of interest shows that there is good energy concentration at the center of the mirror structure compared to peripheral regions in the chaotic cavity [39].

Additional FEM transmission simulations using the ABAQUS software are performed. The incoming wave is

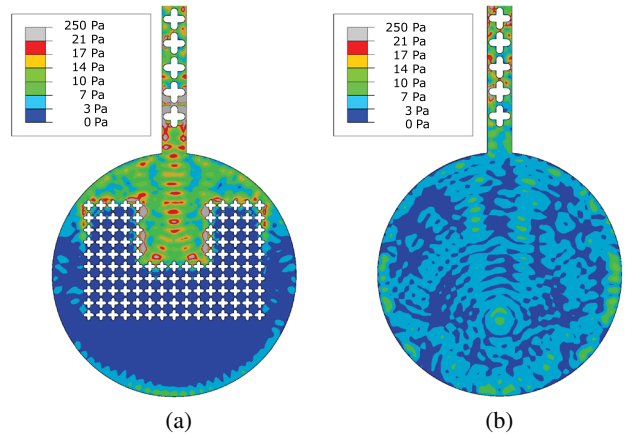

FIG. 4. Snapshots of the von Mises stress (in Pa) inside the chaotic cavity showing the energy focusing by (a) the C-shaped phononic structure in comparison with (b) a homogeneous chaotic cavity at $t = 160\ \mu$s.

the superposition of two quasimonocromatic waves centered around $f_1 = 200$ kHz and $f_2 = 400$ kHz, respectively, with an imposed out-of-plane displacement of 1×10^{-6} mm at point E. Two models are compared: one comprising both the filtering and focusing regions and another consisting of only the filtering region (i.e., with a homogeneous aluminum chaotic cavity). Figures 4(a) and 4(b) provide snapshots of the von Mises stress maps at $t = 160\ \mu$s for the two configurations. In the case of the chaotic cavity with the C-shaped structure, the formation of stationary waves occurs between the vertical portion of the mirror and the beginning of the waveguide. This allows the focusing of the energy of the wave at the frequency f_2 (i.e., the signature of the nonlinearity) to be enhanced.

The possibility of combining both the filtering and focusing functionalities of the device for TR-NEWS is now demonstrated. As discussed, the higher harmonics generated by the nonlinear source are transmitted through the PC1 region without the need for any postprocessing procedure (e.g., FFT). This allows the signal recorded by the sensor in the C-shaped mirror to be readily inverted and retransmitted into the sample. On the other hand, the PC2 region allows us to focus energy of the second harmonic in order to enhance the signal-to-noise ratio in TR.

To perform the TR experiment, two piezoelectric disk transducers (PZT 1, 1.25 cm/1 MHz, and PZT 2, 5 mm) are placed on the plate at points C and B [Fig. 1(a)], with the latter acting both as a receiver and as an actuator in the forward and backward TR propagation steps, respectively. Higher order harmonics are locally generated in the linear elastic plate by inducing the wave field to interact with an obstacle (e.g., a small cylinder, 8 mm in diameter and 20 mm high, placed on the surface of the sample at a point D) whose contact surface has been previously humidified. The emergence of nonlinearity can be ascribed to two different reasons: the first is the fact that the two surfaces are in "clapping" contact [44], mimicking the behavior of a

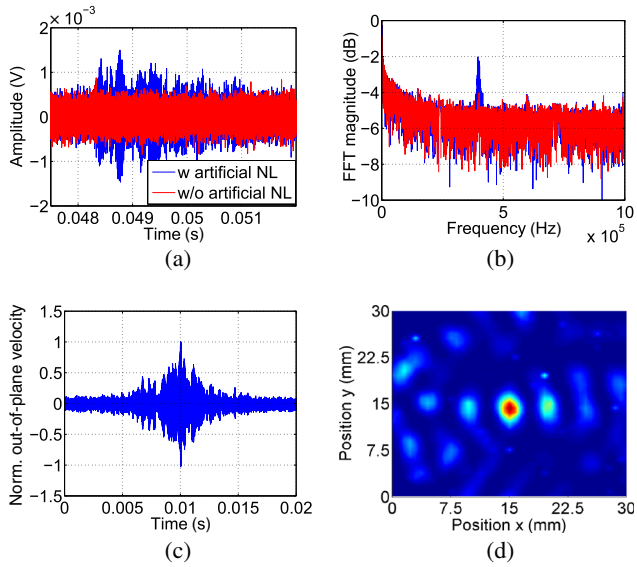

FIG. 5. (a) Time and (b) frequency domain representations of the signals without (red) and with (blue) the nonlinear (NL) source acquired inside the C-shaped mirror. Note the difference in frequency content. Evidence for (c) time and (d) spatial refocusing onto the nonlinear source location.

macroscopic crack in the sample; the second is due to the intrinsic nonlinear elastic behavior of water [45], amplified by the presence of the small cylinder. The sample (with and without the nonlinear element) is excited by a source of the form

$$Y(t) = Y_1 = A_1 \sin(2\pi f_1 t) H(t_0), \tag{1}$$

where A_1 is the amplitude of the sine function and $H(t_0)$ is the Hanning window centered in t_0 with a width corresponding to 21 cycles of the sine wave of the frequency f_1. The time and frequency domain representations of the signal received by PZT 2 are shown in Figs. 5(a) and 5(b), respectively. In the case without the nonlinear scatterer, only noise is recorded inside the cavity (the red signal), whereas, in the presence of the artificial nonlinearity, a resonance peak appears (the blue signal) around the second harmonic (i.e., $f_2 = 2f_1 = 400$ kHz).

The TR-NEWS experiment is thus performed as follows: the PZT 1 transducer emits a signal $Y = Y_1$ [Eq. (1)]; the signal detected by PZT 2 [the blue signal in Fig. 5(a)] is time reversed and transmitted back in the sample. SLDV measurements are performed on a spatial grid covering a 30×30 mm^2 region around the nonlinear source (removed in the back propagation experiment) consisting of 200×200 equally spaced grid points. The laser vibrometer is positioned perpendicularly at 50 cm from the surface to record the out-of-plane velocities of the points over the target area. Multiple (128) measurements are performed and averaged for each node, to filter out part of the noise.

After the backward propagation, time compression of the signal and spatial focusing of the wave field are observed at the nonlinear scatterer location. Figure 5(c) reports an

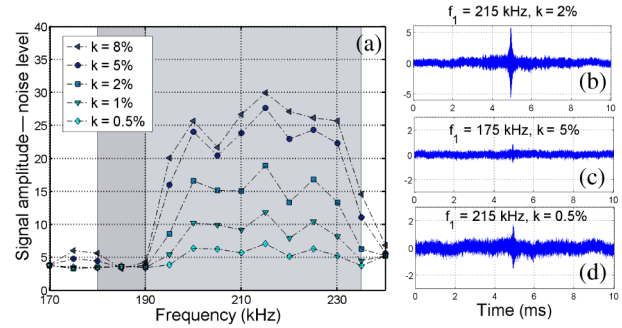

FIG. 6. Bandwidth of the proposed device for time reversal. (a) Quality of the focusing (signal-to-noise ratio) vs frequency. (b)–(d) Time-reversed signals for various nonlinearity levels and frequencies.

example of a time recompressed signal detected with the SLDV. Also, at the focal time, the spatial map of the recorded velocities reveals focusing at the location of the defect, with a considerable concentration of energy, as shown in Fig. 5(d).

The bandwidth and performance of the C-shaped mirror is evaluated by means of an additional experiment: PZT 1 is used to emit pulses [Eq. (1)] with variable frequencies in BG1 ($170 < f_1 < 240$ kHz) and a controlled nonlinearity is introduced by replacing the nonlinear scatterer with a transducer PZT 3 emitting pulses [Eq. (1)] in the same time interval with amplitude $A_2 = kA_1$ ($k \ll 1$) and frequency $f_2 = 2f_1$, thus simulating the generation of second order harmonics. Signals received in the cavity are time reversed and the signal is detected by PZT 3. The quality of the focusing is evaluated as the ratio between the amplitude of the signal at the focal time and the root mean square (rms) of the signal excluding the peak. Results are shown in Fig. 6. Four frequency ranges are identified. (i) For $170 < f_1 < 180$ kHz and $235 < f_1 < 240$ kHz, the focusing is very poor even for high levels of nonlinearity (large k) since f_2 does not fall in BG2, so there is no effect of the mirror [see also Fig. 6(c)]. (ii) For $180 < f_1 < 190$ kHz, focusing is poor, even though the mirror is expected to be effective. This is due to the presence of a band gap in PC1 at f_2 that prevents the second harmonic from reaching the device. (iii) For $190 < f_1 < 235$ kHz, the presence of the mirror (f_2 falls in BG2) allows a significant improvement in the quality of the focusing [see also Figs. 6(b) and 6(d)]. Thus, the PC2 is effective even for very small nonlinearity levels ($k = 0.005$), for which focusing is absent outside the mirror operating frequencies.

In conclusion, we have presented combined experimental and numerical results to demonstrate the feasibility of a novel passive sensor for signals generated by nonlinear elastic scatterers, such as cracks and delaminations. To do this, we have exploited the advanced frequency filtering and spatial focusing properties of phononic crystals, and we have proved the applicability of the sensor to time-reversal experiments that allow us to determine the spatial location

of damage. A time-reversal experiment was carried out, showing good refocusing in time and space onto the nonlinear source, demonstrating the feasibility of the proposed device for damage localization in structures. The imaging results indicate that the PC mirror is necessary to achieve ultrasensitive detection, particularly when the nonlinear signature of the features to be localized is very small, and could provide additional functionalities such as frequency-selective focalization on multiple nonlinear scatterers with different characteristic frequencies.

In the future, we aim to improve the design of this PC sensor addressing issues such as optimized filter or focusing mirror designs, exploitation of multiple band gaps, or frequency tunability using piezoelectric patches, and its effective application to external tested structures with reduced signal losses. Nevertheless, the results presented in this Letter already provide the proof of concept for an efficient, portable damage sensor with applications for passive continuous structural health and acoustic emission monitoring in, e.g., civil engineering and the aerospace industry.

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