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Sub-nanosecond delays of light emitted by streamer in
atmospheric pressure air: analysis of $N_2(C^3\Pi_u)$ and
 $N_2^+(B^2\Sigma_u^+)$ emissions and fundamental streamer structure

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Abstract

Both experimental and theoretical analysis of an ultra-short phenomena occurring during the positive streamer propagation in atmospheric pressure air is presented. With tens-of-picoseconds and tens-of-microns precision, it is shown that when the streamer head passes a spatial coordinate, emission maxima from N_2 and N_2^+ radiative states follow with different delays. These different delays are caused by differences in the dynamics of populating the radiative states, due to different excitation and quenching rates. Associating the position of the streamer head with the maximum value of the self-enhanced electric field, a delay of 160 ps was experimentally found for the peak emission of the first negative system of N_2^+ . For the first time, a delay dilatation was observed experimentally on early-stage streamers and clarified theoretically. Thus, in the case of second positive system of N_2 the delay can reach as much as 400 ps. In contrast to the highly-nonlinear behaviour of streamer events, it is shown theoretically that emission maxima delays linearly depend on the ratio of the streamer radius and its velocity. This is found to be one of the fundamental streamer features and its use in streamer head diagnostics is proposed. Moreover, radially-resolved spectra are synthesized for selected subsequent picosecond moments in order to visualize spectrometric fingerprints of radial structures of $N_2(C^3\Pi_u)$ and $N_2^+(B^2\Sigma_u^+)$ populations created by streamer-head electrons.

1 Introduction

Streamer in atmospheric pressure air is a contracted ionizing wave that propagates into a low- or non-ionised medium exposed to a high electric field. It is characterised by a self-generated field enhancement at the head of the growing discharge channel, leaving a trail of filamentary plasma behind. Such a wave phenomenon results from the space charge left by electron avalanches [1, 2]. Streamers are present in a large number of plasmas, whether operated in the laboratory [3–8], in industrial applications [9] or occurring in lightning and transient luminous events in upper atmosphere [10–14].

In recent time, raising interest to investigate this ultra-fast phenomenon has been enabled by better accessibility of fast gated intensified CCD cameras. However, high-speed camera investigations neglect one very important fact: increasing the temporal resolution of measuring devices to nanoseconds (or a bit under) is insufficient to follow the basic processes within the streamer discharge in atmospheric pressure air. As a consequence, one has to take into account additional effects. One of them is, e.g., the influence of nanosecond gated recordings on the accuracy of the electric field strength estimation from the ratio of emission intensities of the (0,0) vibrational bands of second positive system of N_2 (SPS, with spectral band head at 337.1 nm) and first negative system of N_2^+ (FNS, at 391.5 nm) by ICCD cameras, as shown in [15–17].

Typically, the estimation of basic parameters of practically all nitrogen-containing plasmas at different pressures is widely based on the emission of the two above mentioned nitrogen spectral systems [18–22] - dominantly due to the large difference in their excitation potentials. Thus, also for streamers in atmospheric pressure air, these emissions have been in focus for a long time as well [15, 16, 23–29]. Mutual delay (or shift) of the SPS and FNS emission signal maxima (i.e. SPS-to-FNS delay) of propagating streamer can be found in older literature dealing with time and space highly-resolved streamer investigations. In 1976, Ikuta and Kondo [26] applied probably for the first time the time-correlated single photon counting (TC-SPC) based technique in the investigation of streamer discharges. From their results this delay is visible. Moreover, in [28] it is shown theoretically that FNS and SPS emission maxima occur with different delays behind the electric field peak, but not commented. From the theoretical works of Wang et al. [30] or Kulikovskiy [31] one can learn about the synchronised development of the effective ionization (or excitation) rates in comparison with the electrical field and electron density development. Nevertheless, its detailed impact on the spectrally resolved emission development has not been discussed yet. The presence of SPS-to-FNS delay is analysed in detailed works of Matveev, Djakov and co-workers [32, 33] based on the

1D simulations of Djakov et al. [34]. In their papers, the authors studied theoretically the influence of the spatial and temporal resolution on the determination of the electric field by possible experimental approach. For cases under investigation one can conclude that the temporal resolution of the spectrometric device is a very important parameter which should be of order of tens of picoseconds and the spatial resolution of few tens of microns. Only under such conditions the determination of the electric field by the FNS/SPS intensity ratio method is not distorted significantly [33, 35]. Shcherbakov and Sigmond [36, 37] applied the TC-SPC technique with sufficiently high resolution and emphasised the necessity to have a high enough temporal resolution to be able to resolve SPS-to-FNS delay. Obviously, if this is not the case the estimation of the synchronous electric field or even exact peak field values by the ratio method fails.

Recently, this approach was further theoretically developed by Naidis in [15]. Bonaventura, Celestin and co-workers [16, 17] analysed theoretically the effect of these delays on ICCD-based electric field estimation in more details (also applying this to streamers in sprites in upper atmosphere in [17]) adding the influence of the radial integration over the streamer structure which was not possible in the 1.5D model of Naidis [15] or in the 0D pioneering work of Djakov [34].

Even though there is an increased attention to this topic in last years, so far, no study has investigated in detail the emission maxima peculiarities with all consequences for streamer spectroscopy and diagnostics. In the present work, motivated by high-precision experimental results, systematic computer simulations were performed to study in detail emission delays. The study is based on well established 2D streamer model which enables deeper insight into the delay-issue than previous 0D or 1.5D approaches or computations in 2D focused only on nanosecond-gated cameras. Based on the model of Kulikovsky [31] and our results from 2D computer simulations, analytical description for the delay-parameter is developed.

The manuscript is organised as follows. Section 2 summarizes motivations for the present work based on recent experimental findings and the strategy proposed for the modelling. In section 3 the 2D streamer model is described. The section 4 analyses numerical outcomes. The origin of delays is discussed in detail and its analytical expression and linear dependency are presented in subsections 4.1 and 4.2, respectively. Finally, in the last subsection 4.3, the high-resolved synthetic spectral representation of the streamer head is presented, enabling detailed insight into the radial structure of the streamer-head emission.

2 Experimental motivation and strategy adopted for the modelling

In this work, we have carefully analysed experimental data obtained in two different streamer-discharge setups. We applied the TC-SPC technique on the negative corona Trichel pulses [38] and barrier discharges [39] both in atmospheric pressure air and the synchronous developments of the SPS and FNS emissions for positive streamers were recorded and analysed. Their ratio was computed and according to the simple kinetic scheme [18, 29, 38] the corresponding electric field development was determined for a selected coordinate of tens of micrometers dimension.

The experimental setup for the measurements on Trichel pulse of negative corona discharge streamer was the same as the one used in [38]. It consisted of a grounded cathode with a tip curvature of $190\ \mu\text{m}$ and a positive dc voltage (+7.8 kV) connected plate, both made of stainless steel with a gap of 7 mm. This setup resulted in pulses with a frequency of approximately 200 kHz and a current amplitude reaching 4 mA. A single shot of the breakdown event is shown in figure 1. For the case of streamer measurements in asymmetric barrier discharge (one metallic electrode and the other covered by dielectrics [39]), the setup was the following: The applied sinusoidal voltage has amplitude of $11\ \text{kV}_{p-p}$ (the metal electrode was powered, while the dielectric electrode grounded) and frequency of 60 kHz. As a dielectrics, an alumina of 96% purity was used and the discharge gap was 1 mm. The spatial resolution

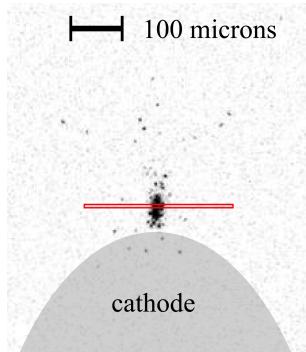


Figure 1: Intensified CCD single-shot image of the positive streamer breakdown in the cathode-sheath of the negative corona Trichel pulse at atmospheric pressure air, see also [38]. The ten-micrometers wide red slit depicts the area for the temporally resolved FNS and SPS signal detection, as shown in Fig. 2.

of spectroscopic measurements was not worse than $50\ \mu\text{m}$. In both setups the air flow was of 300 sccm.

The spatio-temporal highly-resolved emission was recorded by detection system based on TC-SPC. For selected spatial coordinate, the TC-SPC method substitutes the real-time emission-measurement of the discharge event by a statistically averaged determination of cross-correlation function between two optical signals, both originating from the same source. These are the so-called ‘main signal’ (spatially and spectrally resolved single photon, the actual detection of the streamer emission) and the ‘synchronizing signal’ (integral light intensity pulse of the microdischarge-event which gives the time-reference). The time between the detections of these signals is measured. Consequently, time histograms of counted photons for all spatial positions of the discharge are accumulated. The TC-SPC detection instrument consists of a time correlated single photon counting module (Becker&Hickl SPS-150) and two high-sensitive photomultipliers (Hamamatsu PMC-100-4) combined with a monochromator (Acton SpectraPro-500) [39]. The temporal resolution was 12 ps which is the technical division of used TC-SPC memory box. The ICCD image was taken by nanosecond gated camera (DiCam Pro 25 SVGA from PCO Imaging) via a far-field microscope (Questar QM 100BK7).

In figure 2, experimentally obtained FNS and SPS time-resolved emissions of the positive streamer in negative corona Trichel pulse in atmospheric pressure air are shown. They were collected from the red-marked area as shown in figure 1. The kinetic scheme presented in [18, 29, 38] results in following equation:

$$\frac{I_{FNS}/\tau_{eff}^{FNS} + dI_{FNS}/dt}{I_{SPS}/\tau_{eff}^{SPS} + dI_{SPS}/dt} \cdot \frac{\tau_{eff}^{FNS}}{\tau_{eff}^{SPS}} = R_{FNS/SPS}(E) \quad (1)$$

where the letter I denotes the highly-resolved measured light intensity of the given radiative state in the streamer. τ_{eff} is denoting the effective lifetimes and these are given in [40] and computed from data in [40–42]. The dependency $R_{FNS/SPS}$ on the electric field E was estimated experimentally from the emission of the non-self-sustaining Townsend discharge with known applied voltage and electrode gap. This was measured in single-table setup for identical parameters and adjustments of the detecting device as for the recording of streamer emission. Furthermore, spatially resolved spectra were taken with spatial resolution of $10\ \mu\text{m}$ and the intensities of the FNS signal were corrected on the overlap with the neighbouring spectral band of SPS (transition 2-5).

The development of the electric field strength was determined and its normalised value is shown in Fig. 2 as well. It is important to note that the primary objective of this work is to investigate mutual delays between the occurrence of the electric field maximum and

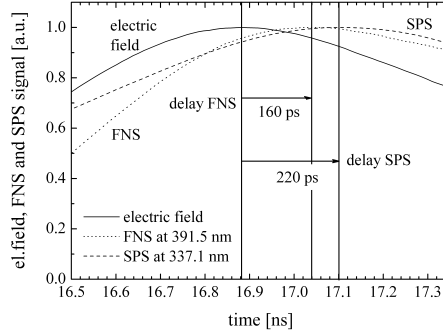


Figure 2: Experimentally obtained FNS and SPS signals of positive streamer in its early stage together with determined electric field development. Delays of the FNS and SPS signals maxima to the electric field maximum are denoted. The uncertainty of the obtained delay values is not worse than ± 20 ps.

the optical emissions maxima. The discussion on the absolute magnitude of the electric field determined from the optical emissions is out of scope of the present paper. It is apparent from Fig. 2 that the maxima of the FNS and SPS emissions are delayed differently with respect to the determined electric field maximum, by 160 ps and 220 ps, for FNS and SPS respectively. Converting these plots using the propagation velocity of the streamer into the spatial structure of the streamer head one can obtain a picture similar to that shown in [15] where it is described as the excitation rate maximum shift. Emissions presented in Fig. 2 were measured close to the electrically highly-stressed region in needle-cathode vicinity where the velocity of the streamer was approx. $6 \cdot 10^4 \text{ ms}^{-1}$. The FNS and SPS radially integrated light emissions were collected from identical position through a slit of $10 \mu\text{m}$ width in axial direction. The experimentally obtained radius of the streamer is $20 \pm 4 \mu\text{m}$ which was estimated as an average value from single-shot ICCD images similar to Fig. 1. In our case, on its very short path of about $90 \mu\text{m}$ the streamer is in its early stage of development.

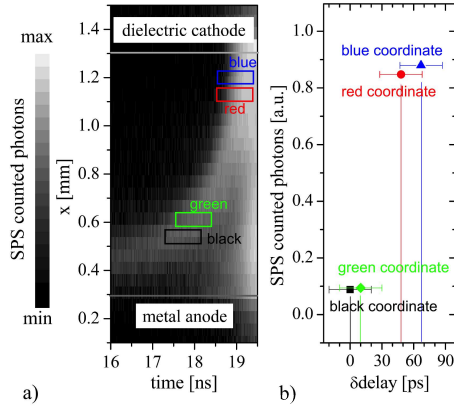


Figure 3: Experimentally obtained SPS signal of positive streamer propagating towards dielectric cathode in barrier discharge arrangement (a) with depicted coordinates for the estimation of the delay dilatation. The dilatation of the delay $\delta delay$ as well as the increase of the emitted intensity of the SPS signal from the streamer head is shown in part (b).

In the barrier discharge setup we observed the same delay phenomena for the FNS and

SPS streamer emissions. Moreover, due to the larger electrode gap of 1 mm, we could observe a change in the delay duration as a function of the distance of the streamer head to the cathode. We describe this phenomenon for early-stage streamer emissions as a dilatation of emission delay. In Fig. 3, the results on the delay dilatation measurements in different stages of streamer development are shown. In Fig. 3 a) the spatio-temporal development of the SPS signal generated by the positive streamer in the inter-electrode gap of barrier discharge is shown. At the coordinate $x = 0.4$ mm and $t = 16$ ns the streamer starts close to the metal anode and propagates towards the dielectric cathode with increasing velocity. At the spatio-temporal coordinate “black” the SPS signal maximum is measured and its delay value behind the electric field is taken as a reference for the delays measured in latter stages of the streamer development. Thus, the delay dilatation “black” is set to be equal zero in Fig. 3 b). The dilatation of the delay parameter is longer in latter stages of the streamer development. Spatio-temporally localised measurements were taken in “green”, “red” and “blue” coordinates and the further change of the delay parameter of the SPS signal is shown in Fig. 3 b). This delay dilatation is approx. +50 and +70 ps for the “red” and “blue” coordinate, respectively. At the same time the increase of the SPS signal intensity maximum for given coordinates is shown. To summarize: it is obvious that in the latter stage of the streamer development the streamer head SPS emission is more intense with a longer dilatation of the delay.

It is important to note that many parameters may influence streamer characteristics and thus the delays. For example, as key parameters, we can mention the repetition frequency of the discharge [43–45], the electrode setup geometry and the air pressure. Indeed, under transient luminous event conditions in upper atmosphere the emission delays are expected to be observable as well [17]. However, for low pressure conditions, the delay should be scaled up towards longer durations in comparison to atmospheric pressure discharges. As delays in emission maxima and the dilatation of the delays occur for several streamer discharge conditions in air, in this work, as a first step, we have chosen to study them theoretically with a 2D model case of an air streamer discharge generated in the vicinity of a high voltage spherical electrode immersed into an external homogeneous electric field.

3 Streamer model

In order to investigate delays in optical emissions we have simulated the propagation of positive streamer in 2D axi-symmetric geometry in air at atmospheric pressure using drift-diffusion equations for electrons, positive and negative ions coupled with Poisson’s equation [46]:

$$\begin{aligned} \partial_t n_e - \nabla \cdot (n_e \mu_e \mathbf{E}) - \nabla \cdot (D_e \nabla n_e) &= S_{\text{ph}} + S_e^+ - S_e^-, \\ \partial_t n_p &= S_{\text{ph}} + S_p^+ - S_p^-, \end{aligned} \quad (2)$$

$$\begin{aligned} \partial_t n_n &= S_n^+ - S_n^-, \\ \epsilon_0 \nabla^2 \phi &= -q_e (n_p - n_n - n_e), \end{aligned} \quad (3)$$

where subscripts ‘e’, ‘p’ and ‘n’ refer to electrons, positive and negative ions, respectively, n_i is the number density of species i , ϕ is the electric potential, $\mathbf{E} = -\nabla\phi$ is the electric field, D_e and μ_e are the electron diffusion coefficient and the absolute value of electron mobility, q_e is the absolute value of electron charge, and ϵ_0 is permittivity of free space. The S_i^+ and S_i^- terms stand for the rates of production and loss of charged particles. The S_{ph} term is the rate of electron-ion pair production due to photoionization in a gas volume. Reaction rates and transport coefficients for air are assumed to be functions of the local reduced electric field E/N , where $E = |\mathbf{E}|$ is the electric field magnitude and $N = 2.688 \times 10^{25} \text{ m}^{-3}$ is the air neutral density. The transport and source parameters are taken from [47]. The photoionization is taken into account through the 3-Group SP₃ method derived by [48] and [49]. Note that on timescales of interest for this work, ions are considered motionless. Positive streamer

is initiated by placing a Gaussian plasma cloud with a peak density of 10^{18} m^{-3} and a characteristic length scale 10^{-4} m in a high-field region in the vicinity of a conducting sphere of radius 0.1 cm with an applied potential of 6.5 kV , see Figure 4. The sphere is immersed in a homogeneous electric field E_{amb} that ranges between 8 and 18 kVcm^{-1} . Similar configuration was considered for derivation of a correction factor stemming from geometrical shape of luminous streamer heads for sprite conditions in [17] and for streamers at ground pressure air in [16]. For the sake of brevity we just point out that, in this work, we have used a $1.0 \times 0.3 \text{ cm}^2$ (i.e., length \times radius) computational domain discretised on a fixed rectilinear grid with a mesh size of $6.2 \mu\text{m}$. More details about the model can be found in [16]. Detailed justification for similar fluid model of streamer propagation, including discussion on limits of its validity, is presented in [53]. Moreover, direct comparison of results of PIC-MCC model [52] for streamer propagation and results of fluid model [51] also shows excellent agreement [52].

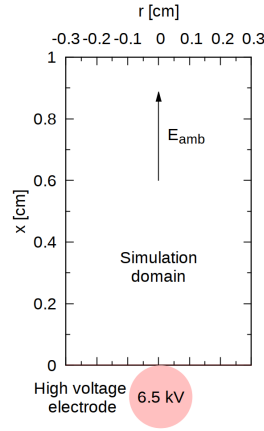


Figure 4: Simulation domain: High voltage electrode is a conducting sphere of radius 0.1 cm and voltage 6.5 kV . Homogeneous ambient electric field E_{amb} of 12 kVcm^{-1} is established by remote planar electrodes.

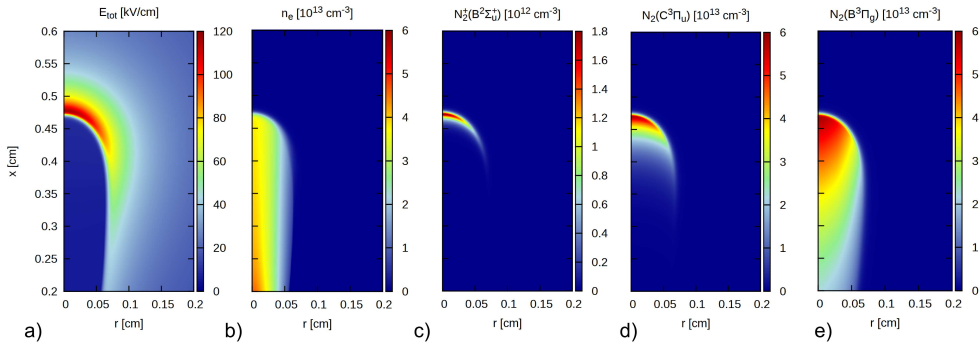


Figure 5: Cross sectional views of electric field (a), electron density (b), FNS (c), SPS (d) and FPS (e) for a positive streamer at time $t = 10.0 \text{ ns}$ when it approaches the middle of the simulation domain, see Fig. 4.

To calculate the optical emissions of the SPS, FNS and also FPS (first positive system) band systems, we use a model similar to the one given in [50]. The population of the excited

species $N_2(C^3\Pi_u)$, $N_2^+(B^2\Sigma_u^+)$ and $N_2(B^3\Pi_g)$ is governed by:

$$\frac{\partial n_k}{\partial t} = -\frac{n_k}{\tau_k} + \nu_k n_e, \quad (4)$$

where n_k [cm^{-3}] is the population of excited state k , and ν_k is the frequency of creation of excited state k by electron impact, $\tau_k = [A_k + \alpha_{N_2}^k N_{N_2} + \alpha_{O_2}^k N_{O_2}]^{-1}$ is the total lifetime of k -state, α_X^k is a quenching rate of k due to collisions with molecule of type X of density N_X and A_k [s^{-1}] is the Einstein coefficient. The quenching rates and Einstein coefficient sets from [51] are used throughout this work. The equation (4) for excited states is solved with the streamer equations (2)–(3). This gives a full time-dependent solution of optical emissions in the modelling of the streamer processes, see Fig. 5.

Intensity of light emission I_k of a state k is proportional to radiative dexcitation rate A_k (s^{-1}):

$$I_k = A_k n_k. \quad (5)$$

Intensity of light emitted from a discharge is usually line-of-sight (LoS) integrated, then the LoS optical emission intensity of state k is given by

$$\Psi_k = 10^{-6} \int_{\mathcal{L}} I_k dl, \quad (6)$$

where I_k is in $\text{cm}^{-3}\text{s}^{-1}$, length l of the optical path \mathcal{L} is in cm and Ψ_k is in Rayleighs. The effect of radiative transfer between the source of the emission and the detector is not taken into account.

4 Results and discussion

4.1 Causes of the emission delays

The two-dimensional plots of the development of the electric field, FNS and SPS emission and electron density were evaluated from the simulations (see Fig. 5). For these conditions, 10 ns after ignition, the positive streamer is propagating in homogeneous electric field of 12 kVcm^{-1} with velocity of about $5 \cdot 10^5 \text{ ms}^{-1}$. In two dimensions (axial and radial), streamer head distributions of SPS and FNS emission intensities together with electric field and electron density in the $x - r$ plane are shown in Fig. 6. The position of the signal and parameter maxima in 2D streamer head profile are denoted. From Fig. 6 one can see that as the streamer head, i.e. the maximum of the electric field, passes the spatial coordinate, the FNS maximum follows with the delay of 100 ps ($83 \mu\text{m}$ at given velocity) and after next 50 ps ($55 \mu\text{m}$) the maximum of SPS emission follows. Note that these are axial values obtained from radially resolved simulations thus not directly comparable to the experimentally obtained (radially unresolved) ones.

In order to understand these delays the population evolutions of the radiative states, their source terms (see equation 4) and other related characteristics are visualised in figure 7. There, the development of electron density and electric field is shown in panels a) and e). Optical emissions rise sharply reaching peak values after the E_{max} together with an increase of n_e , because the population of corresponding excited states is determined by the product of n_e and excitation rate. The characteristic energy ε^* of electrons (see panel e)) evolves quickly achieving its maximum of approx. 5 eV nearly synchronously with the peak of electric field E_{max} and decreasing towards streamer channel stationary value of approx. 1.3 eV within 200 ps. Such a drop implies significant variations of the EEDF characterized by a much faster disappearance of high energy (tail) electrons and, in general, determines characteristic timescale of the population dynamics of electronically excited states. The position of FNS and SPS maxima is governed by the balance established between gain and loss terms. Behind the streamer head (i.e. the coordinate E_{max}) where both E and ε^* decrease, the creation frequency for FNS ν_{FNS} decreases faster (insufficient electrical field for accelerating electrons

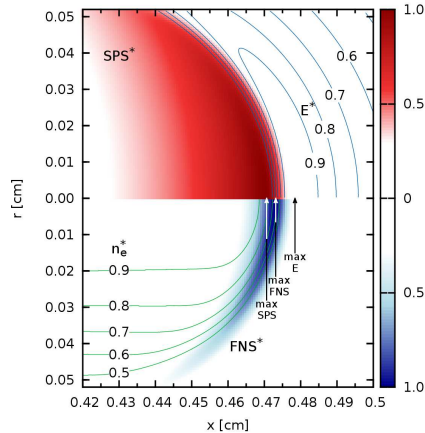


Figure 6: Detailed view on the positive streamer head structure obtained from 2D axisymmetric simulation. In upper part, electric field isolines and emission profile of SPS (red) are shown. In the part below, electron density isolines and emission profile of FNS (blue) are presented. The star-signs denote a normalised value. Note, that while the results of measurements on the streamer discharge are typically represented in the time scale of measured temporal development, i.e. from left to the right as in Fig. 2 or in [16,29,36,38], the results of numerical modelling are presented in opposite direction [15,17], which is also the case further in this article.

over the FNS excitation threshold of 18.8 eV) than ν_{SPS} (SPS threshold 11 eV), see panel d). The difference between two excitation thresholds is imprinted via different rates for FNS and SPS excitations (panel d). Consequently, the SPS remains sufficiently excited even in low field region where the FNS source term vanishes. Moreover, FNS has much shorter effective lifetime than SPS (effective lifetime of SPS is 0.61 ns and 0.12 ns for FNS under given conditions [51] or even shorter for FNS as reported in [42]). This scenario results in sharper FNS emission peak which appears closer to the electric field maximum than more distant and broader peak of SPS.

For comparison, in Fig. 7, the development of $N_2(B^3\Pi_g)$ axial population (FPS emission) is presented as well. Comparing FPS, SPS and FNS maxima delays, the delay of FPS emission maximum with respect to the peak of electric field is the longest one (about 200 ps). This is because the threshold for electron impact excitation of the $N_2(B^3\Pi_g)$ state (FPS emission) is significantly lower (7.4 eV) compared with excitation threshold of $N_2(C^3\Pi_u)$ and $N_2^+(B^2\Sigma_u^+)$. Moreover, the lower excitation threshold of the $N_2(B^3\Pi_g)$ is responsible for much higher population density than in the case of $N_2^+(B^2\Sigma_u^+)$. The form of the FPS emission correlates with the electron density distribution more closer than any other presented spectral system emission, compare the sub-figures b), c), d) and e) in Fig. 5.

To summarise, sub-nanosecond delays of peak intensities of the SPS, FNS and FPS systems with respect to E_{\max} signal maxima behind the streamer head are caused by different excitation threshold energies of excited states, different radiative and collisional quenching, as well as by fast decrease of characteristic energy of electrons ε^* and slowly increasing electron density n_e behind the streamer head.

4.2 Streamer geometry and its fingerprint in spectral signatures

The dependence of the computed delays (SPS and FNS) on the ratio of the streamer radius and velocity r/v at given moments of its development are shown for different values of the homogeneous ambient electric field (Fig. 8). Individual points in the figure represent

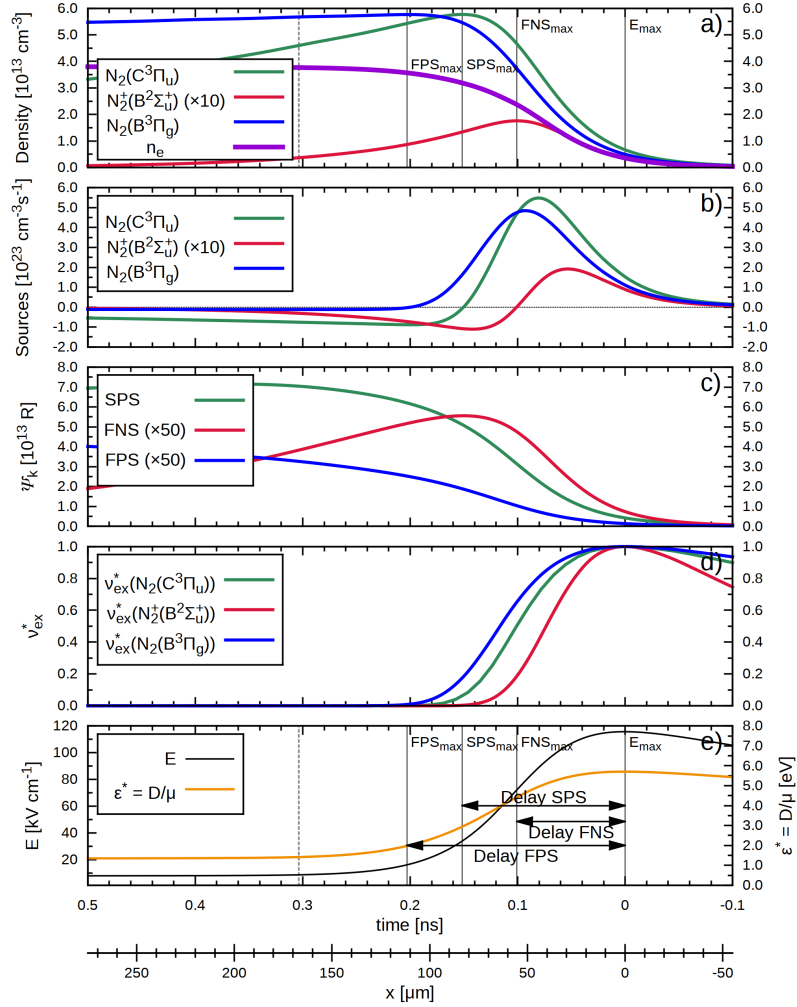


Figure 7: Time (space) evolution of the axial densities of $\text{N}_2(\text{C}^3\Pi_u)$, $\text{N}_2^+(\text{B}^2\Sigma_u^+)$ and $\text{N}_2(\text{B}^3\Pi_g)$ states and electrons n_e are shown in panel (a). Source terms $\partial n_k/\partial t$, Ψ_k (line-of-sight) intensities and normalized excitation rates ν_{ex}^* for all three excited states are given in panel (b), (c) and (d), respectively. In the panel (e), development of x -component of the electric field E and characteristic electron energy $\epsilon^* = D/\mu$ is shown. Full vertical lines indicate positions of peak axial values of the electric field (E_{max}) and emission intensities (SPS_{max} , FNS_{max} and FPS_{max}). The delays marked by horizontal arrows have values of 150 ps (83 μm), 100 ps (55 μm) and 200 ps (112 μm) for SPS, FNS and FPS signal maxima, respectively. Vertical dashed line marks a position where a radially resolved spectrum is analysed in Section 4.3. The spatial and time coordinates are linked via streamer velocity of $5 \cdot 10^5 \text{ ms}^{-1}$.

individual instants of the streamer propagation. Generally all points for each set are ordered in time when seen from left to right. In other words, points of given colour lying more on the left correspond to the earlier phases of the streamer development. Clearly, a linear trend can be observed for the set of ‘axial’ values (local emission from the axis of the propagating streamer).

Considering first the delays of peak densities of excited states on the axis of the discharge,

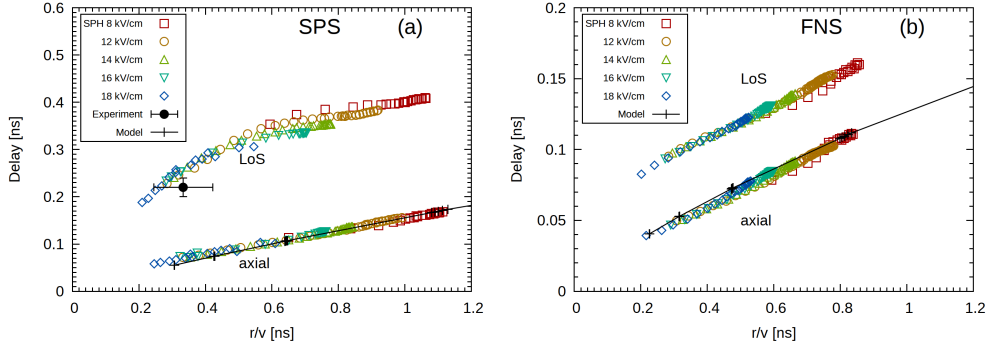


Figure 8: Delays of optical emission peaks for SPS (a) and FNS (b) for positive streamer as a function of streamer radius r and streamer velocity v ratio for different values of the homogeneous ambient electric field (see Fig. 4). Streamer radius is determined as: 1) the (radiation) radius where density of excited states is 1/2 the value on the axes for ‘axial’ group of points; 2) the radius where the line-of-sight (LoS) radially integrated intensity is 1/2 of the maximum value for ‘LoS’ group of points. Points are results of 2D axi-symmetric simulation and lines are modelled by eq.(13), see further in the text.

we see that no matter what model or external field, all points fit a single line (‘axial’). Clearly the ratio r/v is a key characteristic of a streamer for discussing the excitation delay. Obviously, both the delay and r/v are linked characteristics of the streamer head geometry and thus connected to more fundamental features of the streamer structure. On the other head, the so called line-of-sight (LoS, i.e., intensity integrated through the whole streamer diameter at selected x, r -coordinate) delays dependence on r/v is a bit more complex. We see convergence to a single path for the LoS points that correspond to instants of early streamer development (points more on the left for each set). For more developed streamers (points more on the right of each set) a dispersion of the delays obtained for various simulation conditions is observed.

Even though we do not intend to simulate in this work the particular case of the Trichel pulse streamers presented in Section 2, from Fig. 8 one can see that the experimentally observed delay value (at least for SPS, as we have no experimental value for the FNS emission radius) is not far from the simulated one when we consider the both streamers, the measured and the simulated one, in their early development stage. Note that in the experiment the emission is projected and integrated over the whole streamer diameter (direct Abel transformation) at selected x -coordinate, while for LoS emission the emission is integrated through the projection along single line-of-sight which is passing streamer axis ($r = 0$). To radially resolve the $40 \mu\text{m}$ thin streamer by maintaining the high temporal resolution simultaneously is over the possibilities for given setup.

From the results presented in Fig. 8 one can also conclude that the later is the stage of streamer development the longer are the delays of the peak emissions. SPS recordings for the positive streamer propagating along the 1 mm long gap in dielectric barrier discharge [39] was analysed in previous section (see Fig. 3). Indeed, a delay dilatation was observed. After $500 \mu\text{m}$ of the streamer propagation the dilatation was $+50 \text{ ps}$ and $100 \mu\text{m}$ in front of the cathode reaching already $+70 \text{ ps}$ for the SPS delay. The obtained result is consistent with the simulated delay dilatations. This is due to the spatial scale of the streamer head which expands in time both in the experiment as well as in presented models.

Strongly nonlinear features of streamers are well known and thoughtfully discussed in many works, see, e.g., in [54, 55]. Nevertheless in this work, based on the results of 2D axisymmetric simulations, the dependence of the delays on the streamer radius to velocity ratio r/v is found to be linear for the emissions on the streamer axis. In order to explain this

surprising linearity, in the following we analyze the positive streamer in the framework of a 1D analytical approximation. This model is capable to mimic basic features of the streamer propagation [15, 31, 56] and through its obvious simplicity to explain in very comprehensive manner the meaning of the observed linearity. Dependence of E on z along the axis in the vicinity of the streamer head may be reasonably approximated by an expression

$$E(z) = \begin{cases} E_s(1 + z/l_f)^{-1} & \text{for } z > 0, \\ E_s(1 + 2z/l_f) & \text{for } -l_f < z < 0, \end{cases} \quad (7)$$

where E_s is the peak electric field in the streamer head at position $z = 0$, and l_f is the axial width of the streamer high field region [31]. The simplest equation describing a streamer propagation is based on a fluid approximation, neglecting photoionization and diffusion and has a form:

$$\frac{\partial n_e}{\partial t} + \nabla \cdot (n_e \mathbf{w}_e) = \alpha_{\text{eff}} w_e, \quad (8)$$

where \mathbf{w}_e is the electron drift velocity, α_{eff} is the effective ionization coefficient, both functions of E . Assuming that the streamer is propagating with a constant velocity v_s , then, following [15], we can integrate (8) in the framework of a 1D approximation by using (7) for $z > 0$ to get

$$n_{\text{es}}(v_s + w_{\text{es}}) = n_{\text{eb}}(v_s + w_{\text{eb}}) \exp \left(l_f E_s \int_{E_b}^{E_s} \frac{\alpha_{\text{eff}} w_e}{v_s + w_e} \frac{dE}{E^2} \right), \quad (9)$$

where $E_b = 30 \text{ kVcm}^{-1}$ is the magnitude of the electric field on the edge of the ionization region, n_{es} and n_{eb} are electron densities at the position of the peak electric field ($z = 0$) and on the edge of the ionization region where $E = E_b$, respectively. Similarly w_{es} and w_{eb} denote electron drift velocities where the electric field value equals E_s and E_b . Similarly by using (7) for $z < 0$ one gets electron density on the axis of streamer behind the electric peak:

$$n_{\text{ec}}(v_s + w_{\text{ec}}) = n_{\text{es}}(v_s + w_{\text{es}}) \exp \left(\frac{l_f}{2E_s} \int_{E_c}^{E_s} \frac{\alpha_{\text{eff}} w_e}{v_s + w_e} dE \right), \quad (10)$$

where n_{ec} is electron density behind the electric field peak where the magnitude of the field diminished to value E_c and w_{ec} is corresponding electron drift velocity. Equation (9) allows to obtain a condition that relates the axial streamer width l_f to the streamer velocity v_s through the streamer peak field E_s :

$$l_f E_s \int_{E_b}^{E_s} \frac{\alpha_{\text{eff}} w_e}{v_s + w_e} \frac{dE}{E^2} = \ln \left(\frac{n_{\text{es}}}{n_{\text{eb}}} \right) + \ln \left(\frac{v_s + w_{\text{es}}}{v_s + w_{\text{eb}}} \right), \quad (11)$$

which allows one to obtain for a given E_s and l_f coherent values of streamer velocity v_s , see [15].

Observed linear dependence of delays of maximum intensity of SPS and FNS emission on the ratio r_s/v_s can be explained on the basis of equation (7). Considering the dependence $E(z) = E_s(1 + 2z/l_f)$, an observer at a fixed point would find that when the streamer is passing its location with velocity v_s , then after the peak, the electric field decays linearly with time

$$E(t) = E_s(1 - 2v_s t/l_f). \quad (12)$$

Note also that most of the excitation of radiating states, in fact, takes place after the passage of the peak electric field, when the electric field starts to diminish. Therefore after some time, the lost of excited states overcomes their production. The maximum of the emission occurs when lost and gain terms in equation (4) are equal, i.e. when $n_k/\tau_k = n_e \nu_k$. The time lag t_{lag} between the maximum of the electric field and the maximum of emission defines the delay and may be estimated by simply recasting the equation (12) for time:

$$t_{\text{lag}} = \left(1 - \frac{E(t_{\text{lag}})}{E_s} \right) \frac{l_f}{2v_s}. \quad (13)$$

Taking into account coherent combination of streamer parameters $\{E_s, l_f, v_s\}$ obtained from condition (11) with electron density variation as given by (10), then (4) can be integrated to find time t_{lag} (or electric field $E(t_{\text{lag}})$ in (13)) when loss and gain terms of (10) equal. This model was evaluated for α_{eff} and w_e from [47] and for $\ln(n_{\text{es}}/n_{\text{eb}}) = 8$ (see [15]) for E_s in the range between 100 and 200 kVcm $^{-1}$ with step of 20 kVcm $^{-1}$ and l_f in between 0.05 to 0.125 cm with a step of 0.015 cm. Note that according to [15, 31, 46, 57] ratio of radiation radius r of the streamer to the width l_f ranges between $\xi = 1.5$ –2.5. Time delays resulting from the model (13) for $\xi = 1.7$ in case of FNS and $\xi = 2.3$ in case of SPS (solid lines with points) together with data obtained from 2D axi-symmetric simulations (coloured symbols) are presented in Figure 8. Finally one can observe that, despite the fact that the slope $(1 - E(t_{\text{lag}})/E_s)$ in equation (12) generally depends on a set of $\{E_s, l_f, v_s\}$ values, the overall dependence of t_{lag} on the radiation radius to velocity ratio is not far from linear.

4.3 Spectrometric representation of the streamer head structure

Concentrations of $\text{N}_2(\text{C}^3\Pi_u)$, $\text{N}_2^+(\text{B}^2\Sigma_u^+)$ and $\text{N}_2(\text{B}^3\Pi_g)$ species (i.e. SPS, FNS and FPS respectively, see figure 5) calculated at any spatial coordinate (x, r) in the $x - r$ plane can be represented by corresponding synthetic emission spectrum $i(\lambda, x, r)$ calculated assuming fixed spectral resolution (given by instrumental function of spectrometer) and certain characteristics of emitting states (rotational temperatures and vibrational distributions). Integration of $i(\lambda, x, r)$ synthetic spectra along r (assuming cylindrical symmetry) and/or x coordinates allows evaluating instrumental effects associated with spatial, temporal and spectral resolution limits occurring in real experiments. For example, streamer emission is usually detected through projected luminosity of the streamer filament determined by the unknown radial distributions of various radiating species. Integrating $i(\lambda, x, r)$ along the plane perpendicular to the direction of the streamer propagation ($x = \text{const.}$) therefore simulates radially integrated spectra $I(\lambda, x)$ which are usually used to evaluate streamer parameters. Integrating $I(\lambda, x)$ along x -coordinate then allows accounting for limited temporal resolution of real ICCD or PMT detectors.

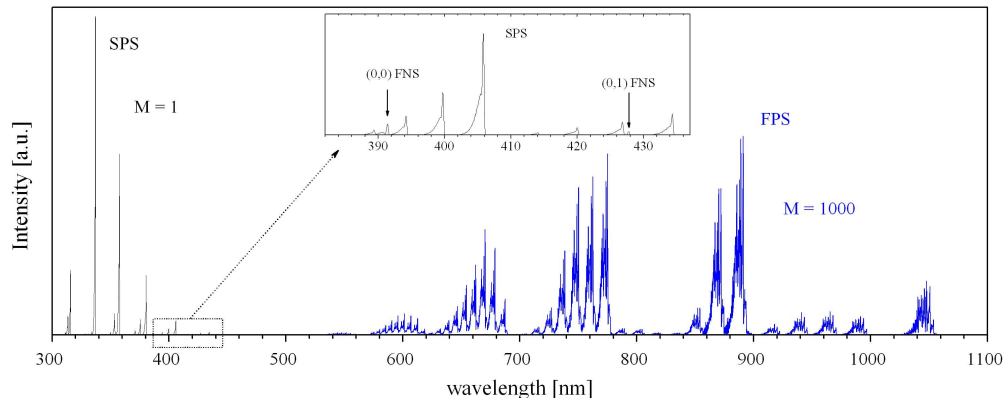


Figure 9: Synthetic streamer head emission spectrum integrated over the whole $x - r$ plane displayed in Fig. 6. Calculated assuming $T_{\text{rot}} = 300$ K and using triangular instrumental function (FWHM = 0.2 nm). The value M denotes the multiplication factor.

We applied an approach detailed in [58, 59] to construct synthetic SPS, FNS and FPS emission spectra occurring in the 300–1100 nm spectral range by fixing rotational temperature of 300 K for all emitting states and using line-shape defined by triangular instrumental function (spectral resolution of 0.2 nm), for axially and spectrally integrated signal see Fig.

9. Because the code which was used to simulate populations of excited electronic states of N_2 and N_2^+ species does not include vibrational kinetics, i.e. populations obtained represent sum over all vibrational levels of a given state, corresponding data (such as shown in Fig.6) can be therefore represented by emission spectra only after assuming certain vibrational distribution for each electronic state. In the case of the FNS we assumed that electron-impact ionization populates exclusively $v = 0$ vibrational level of the $N_2^+(B^2\Sigma_u^+)$ state, whereas the $N_2(C)$ and $N_2(B^3\Pi)$ state populations were distributed among $v = 0-4$ (1 : 0.18 : 0.06 : 0.015 : 0.002) and $v = 0-12$ (0.64 : 1.00 : 0.98 : 0.47 : 0.39 : 0.26 : 0.12 : 0.073 : 0.041 : 0.022 : 0.011 : 0.0055 : 0.0028) vibrational levels, respectively. Final $i(\lambda, x, r)$ spectra were constructed by blending SPS, FPS and FNS systems according to calculated local (x, r) populations of individual $N_2(C^3\Pi, v)$, $N_2(B^3\Pi, v)$ and $N_2^+(B^2\Sigma, v)$ vibrational levels, respectively.

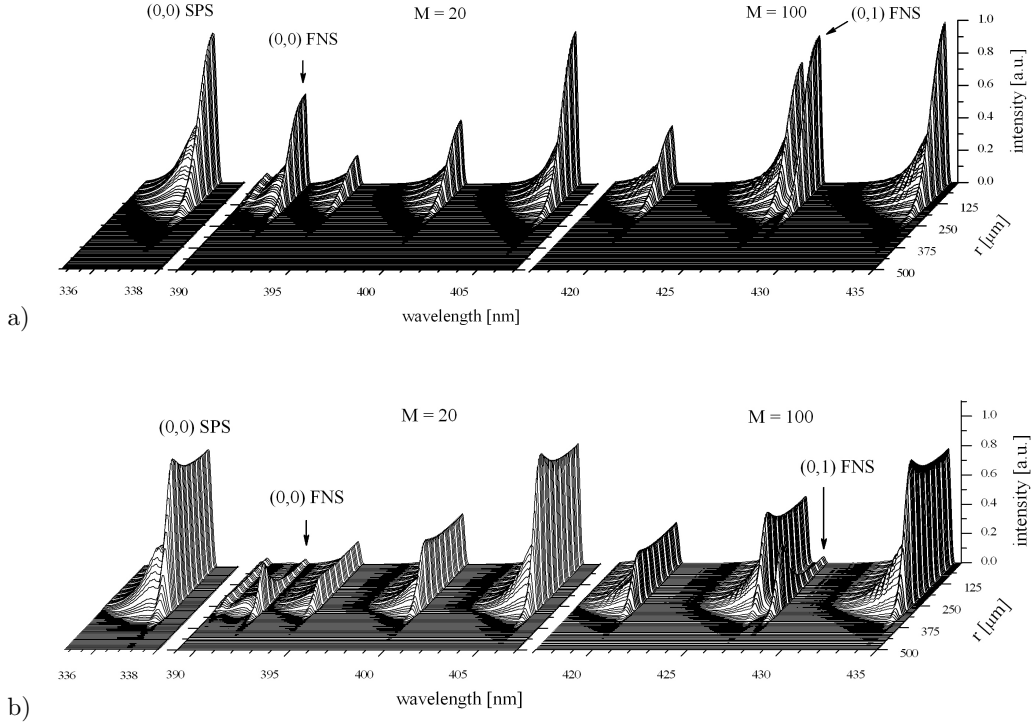


Figure 10: Synthetic streamer head emission distribution evaluated along the radius from the data shown in Fig. 6. Calculated assuming $T_{rot} = 300$ K and using triangular instrumental function (FWHM = 0.2 nm). Radially resolved spectra simulated at two ($x = \text{const.}$) positions corresponding to maximum axial population (indicated as FNS_{max} in Fig.6) of the $N_2^+(B^2\Sigma)$ state (a) and position slightly shifted ($\Delta x = 112 \mu\text{m}$, i.e. approx. 200 ps delay) behind the FNS_{max} position (b). The value M denotes the multiplication factor.

Because obtaining emission data with sufficient spatio-temporal resolution from streamer experiments is very difficult and in most cases impossible due to instrumental limitations, in the next part of this paper we will focus on the radially resolved as well as radially-integrated emission spectra discussing possible effects connected with determination of basic streamer parameters (emission delays, electric field etc.) from real (experimental) spectra. In figure 10, the radially resolved spectra of the streamer head are shown for two selected ($x = \text{const.}$) positions behind E_{max} . The first position (a) coincides with the maximum intensity of the

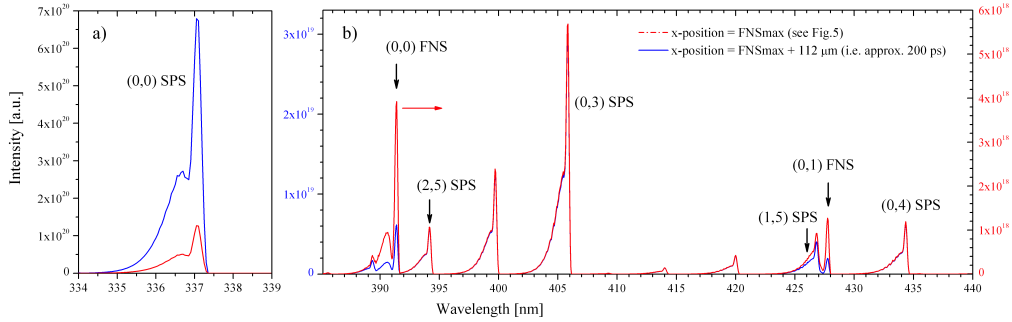


Figure 11: Selected parts of synthetic FNS and SPS spectra occurring in UV (a) and vis (b) ranges at two different axial positions averaged over the radius (evaluated from the data shown in Fig. 6). Calculated assuming $T_{\text{rot}} = 300$ K and using triangular instrumental function (FWHM = 0.2 nm). Radially integrated spectra simulated at a position ($x = \text{const.}$) corresponding to maximum axial population of the N_2^+ ($\text{B}^2\Sigma$) state (FNS_{max}) and position slightly shifted ($\Delta x = 112 \mu\text{m}$) behind the FNS_{max} position (i.e. 200 ps later). Note that two different y-axis scales are used in panel (b) to display the two spectra with overlapped (0,3) SPS bands.

N_2^+ -FNS system (FNS_{max} position) occurring with the shift of $55 \mu\text{m}$ (i.e. approx. 100 ps) behind the E_{max} (compare to figures 6 and 7). Radial distributions of emission spectra peak at $r = 0$ with the (0,0) FNS band intensity exceeding amplitudes of both (2,5) and (1,4) SPS bands occurring in the 390–400 nm region. The second position (b) is shifted only by next $112 \mu\text{m}$ (200 ps) with respect to the FNS_{max} , see the dashed line in Fig. 7. Radial distributions in the latter case clearly show a shallow dip towards $r = 0$ and a small peak at the periphery of the cylindrically symmetric streamer. The (0,0) FNS band intensity significantly decreases with respect to SPS bands. The main part of the FNS emission is shifted to the side while the SPS emission intensity is nearly constant along the radius with just a small hump occurring at the edge of the streamer channel. The possible uncertainties of the electric field determination via FNS/SPS ratio method by analysing insufficiently resolved (spatially or temporally) streamer head emission are obvious. When comparing SPS and FNS amplitudes of radially integrated spectra from two above mentioned axial positions (shown in Fig. 11), one can clearly see that when detecting streamer head emission with axial spatial resolution about 0.1 mm, most of the integrated emission comes from regions behind FNS_{max} coordinate and therefore FNS/SPS ratio is far from being representative for the electric field estimation at E_{max} or even at FNS_{max} positions.

The determination of the three SPS, FNS and FPS axial delay parameters therefore seems to be a crucial step for selecting suitable spatial/temporal resolutions for investigating fine structure of the streamer head. Using SPS-to-FNS delay measurement one can check the relevance of the electric field estimation method. The use of the FPS delay parameter together with FNS and SPS ones could be a further improvement of delay-coupled streamer diagnostics. While the FNS and SPS are due to their relatively high excitation thresholds coupled to the streamer head, the FPS is more related to the environment in plasma channel behind the streamer head (see Fig. 4).

Additionally, in synthesised spectra in Fig. 10 and 11 another band of the FNS is visible: the (0,1) band. As its intensity is scalable with the usually used (0,0) FNS band only through the ratio of corresponding radiative transition probabilities, it can be easily used for the estimation of the electric field together with neighbouring (1,5) and (0,4) SPS bands which are scalable in the same way (considering fixed vibrational distribution of the $\text{C}^3\Pi_u$ state) with the (0,0) SPS band. This approach has an important advantage because both bands are placed on close wavelengths so there is usually no need to make correction for

spectral response of the spectrometric system. It is similar as in [18] where the (0,0) FNS and (2,5) SPS bands at 391 nm and 394 nm, respectively were used for the same reason as well. However in both cases, a possible overlap of FNS band with the tail of SPS band occurring to the next at higher wavelengths has to be carefully evaluated and subtracted (if not negligible).

5 Summary and conclusion

In this paper, delays of several tens-of-picoseconds for emission maxima of dominant N_2 and N_2^+ band systems developing behind the positive streamer head are reported and thoroughly analyzed. In surprising contrast to highly-nonlinear behaviour of streamer events a linear dependence was found using 2D axi-symmetric simulations as well as 1D analytic models for the emission maxima delays as a function of the streamer radius to velocity ratio r/v . We concluded that the coupling of the delay and the r/v parameter represents an intrinsic characteristic of the streamer head and we proposed an analytical model for this coupling. A dilatation of these delays of few tens-of-picoseconds during the early-stage streamer evolution was observed both experimentally and theoretically with good agreement. The SPS delay can reach the value of up to 400 ps at given conditions which can cause an error in the discharge analysis by correlating electrical measurements (current and voltage waveforms for instantaneous power and energy estimation) to the early-stage streamer emission development only. As shown, the detected emission just represents populations of excited states formed behind the running streamer head, giving only delayed information about the streamer head position. It is reasonable to expect that similar phenomena occurs in other streamer-mechanism driven discharges, too. Presumably, it can be described by similar analytical approach.

For the first time, based on the results of a 2D axi-symmetric model, a spectral representation of the whole streamer head area is visualised. It is shown that for short delays, the FNS emission peaks at the axis of the streamer while several tens of picoseconds later more complex FNS intensity distributions appear. Also, by understanding the spectra structure in the streamer head, one can assess that the radial averaging of the streamer emission will cause smaller distortion of the further processed signal as the axial signal integration.

Finally, we suggest to consider these delays in advanced emission-based streamer diagnostics. Analysing accurately this effect for selected case and using the analytical expression for the delay parameter derived in this article, we see possibilities to assess more easily the basic plasma parameters of the propagating streamer, based on the measurements of these delays and other macroscopic streamer parameters only.

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