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Magnetization reversal by superconducting current in φ_0 Josephson junctions

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We study magnetization reversal in a φ_0 Josephson junction with direct coupling between magnetic moment and Josephson current. Our simulations of magnetic moment dynamics show that by applying an electric current pulse, we can realize the full magnetization reversal. We propose different protocols of full magnetization reversal based on the variation of the Josephson junction and pulse parameters, particularly, electric current pulse amplitude, damping of magnetization, and spin-orbit interaction. We discuss experiments that can probe the magnetization reversal in φ_0 -junctions. *Published by AIP Publishing.*

Spintronics, which deals with an active control of spin dynamics in solid state systems, is one of the most rapidly developing fields of condensed matter physics.¹ An important place in this field is occupied by superconducting spintronics dealing with the Josephson junctions (JJ) coupled to magnetic systems.² The possibility of achieving electric control over the magnetic properties of the magnet via Josephson current and its counterpart, i.e., achieving magnetic control over Josephson current, recently attracted a lot of attention.^{3–5} Spin-orbit coupling plays a major role in achieving such control. For example, in superconductor/ferromagnet/superconductor (S/F/S) JJs, its presence in a ferromagnet without inversion symmetry provides a mechanism for a direct (linear) coupling between the magnetic moment and the superconducting current. In such junctions, called hereafter φ_0 -junction, time reversal symmetry is broken, and the current phase relation is given by $I = I_c \sin(\varphi - \varphi_0)$, where the phase shift φ_0 is proportional to the magnetic moment perpendicular to the gradient of the asymmetric spin-orbit potential and also to the applied current.^{6–8} Thus, such JJs allow one to manipulate the internal magnetic moment by Josephson current.^{6,9} The static properties of S/F/S structures are well studied both theoretically and experimentally; however, the magnetic dynamics of these systems has not been studied in detail beyond a few theoretical works.^{6,9–14}

The spin dynamics associated with such φ_0 -junctions was studied theoretically in Ref. 9. The authors considered a S/F/S φ_0 -junction in a low frequency regime, which allowed the usage of the quasi-static approach to study magnetization dynamics. It was demonstrated that a DC superconducting current produces a strong orientation effect on the magnetic moment of the ferromagnetic layer. Thus, the application of a DC voltage to the φ_0 -junction is expected to lead to current oscillations and consequently magnetic precession. This precession can be monitored by the appearance of higher harmonics in the current-phase relation; in addition, it also leads to the appearance of a DC component of the current which

increases near a ferromagnetic resonance.⁹ It is then expected that the presence of external radiation in such a system would lead to several phenomena such as the appearance of half-integer steps in the current-voltage (I-V) characteristics of the junction and generation of an additional magnetic precession with the frequency of external radiation.⁹

In this paper, we study the magnetization reversal in the φ_0 -junction with direct coupling between magnetic moment and Josephson current and explore the possibility of electrically controllable magnetization reversal in these junctions. We carry out investigations of the magnetization dynamics for two types of applied current pulses: rectangular and Gaussian forms. An exact numerical simulation of the dynamics of magnetic moment of the ferromagnetic layer in the presence of such pulses allows us to demonstrate complete magnetization reversal in these systems. Such reversal occurs for specific parameters of the junction and the pulse. We chart out these parameters and suggest a possible way for the determination of the spin-orbit coupling parameter in these systems. We discuss the experiment that can test our theory.

In order to study the dynamics of the S/F/S system, we use the method developed in Ref. 9. We assume that the gradient of the spin-orbit potential is along the easy axis of magnetization taken to be along \hat{z} . The total energy of this system can be written as

$$E_{\text{tot}} = -\frac{\Phi_0}{2\pi} \varphi I + E_s(\varphi, \varphi_0) + E_M(\varphi_0), \quad (1)$$

where φ is the phase difference between the superconductors across the junction, I is the external current, $E_s(\varphi, \varphi_0) = E_J[1 - \cos(\varphi - \varphi_0)]$, and $E_J = \Phi_0 I_c / 2\pi$ is the Josephson energy. Here, Φ_0 is the flux quantum, I_c is the critical current, $\varphi_0 = l v_{so} M_y / (v_F M_0)$, v_F is the Fermi velocity, $l = 4hL / \hbar v_F$, L is the length of the F layer, h is the exchange field of the F layer, $E_M = -K \mathcal{V} M_z^2 / (2M_0^2)$, the parameter v_{so}/v_F characterizes a relative strength of the spin-orbit interaction, K is the anisotropic constant, and \mathcal{V} is the volume of the F layer.

The magnetization dynamics is described by the Landau-Lifshitz-Gilbert equation³ (see also [supplementary material](#)), which can be written in the dimensionless form as

$$\begin{aligned}\frac{dm_x}{dt} &= \frac{1}{1+\alpha^2} \left\{ -m_y m_z + Gr m_z \sin(\varphi - r m_y) \right. \\ &\quad \left. - \alpha \left[m_x m_z^2 + Gr m_x m_y \sin(\varphi - r m_y) \right] \right\}, \\ \frac{dm_y}{dt} &= \frac{1}{1+\alpha^2} \left\{ m_x m_z \right. \\ &\quad \left. - \alpha \left[m_y m_z^2 - Gr (m_z^2 + m_x^2) \sin(\varphi - r m_y) \right] \right\}, \\ \frac{dm_z}{dt} &= \frac{1}{1+\alpha^2} \left\{ -Gr m_x \sin(\varphi - r m_y) \right. \\ &\quad \left. - \alpha \left[Gr m_y m_z \sin(\varphi - r m_y) - m_z (m_x^2 + m_y^2) \right] \right\},\end{aligned}\quad (2)$$

where α is a phenomenological Gilbert damping constant, $r = l v_{so} / v_F$, and $G = E_J / (K V)$. The $m_{x,y,z} = M_{x,y,z} / M_0$ satisfies the constraint $\sum_{\alpha=x,y,z} m_\alpha^2(t) = 1$. In this system of equations, time is normalized to the inverse ferromagnetic resonance frequency $\omega_F = \gamma K / M_0$: ($t \rightarrow t \omega_F$), γ is the gyromagnetic ratio, and $M_0 = \|\mathbf{M}\|$. In what follows, we obtain the time dependence of magnetization $m_{x,y,z}(t)$, phase difference $\varphi(t)$, and normalized superconducting current $I_s(t) \equiv I_s(t) / I_c = \sin(\varphi(t) - r m_y(t))$ via the numerical solution of Eq. (2).

Let us first investigate an effect of superconducting current on the dynamics of magnetic momentum. Our main goal is to search for cases related to the possibility of the full reversal of the magnetic moment by superconducting current. In Ref. 9, the authors have observed a periodic reversal, realized in a short time interval. But, as we see in Fig. 1, during a long time interval the character of m_z dynamics changes crucially. At long times, \vec{m} becomes parallel to the y-axis, as seen from Fig. 1(b) demonstrating dynamics of m_y . The situation is reminiscent of the Kapitza pendulum (a pendulum whose point of suspension vibrates) where the external sinusoidal force can invert the stability position of the pendulum.¹⁵ Detailed features of Kapitza pendulum manifestation will be presented elsewhere.

The question we put here is the following: is it possible to reverse the magnetization by the electric current pulse and then preserve this reversed state. The answer may be found by solving the system of equation (2) together with Josephson relation $d\varphi/dt = V$, written in the dimensionless form. It was demonstrated in Ref. 13 that using a specific time dependence of the bias voltage applied to the weak link leads to the reversal of the magnetic moment of the nanomagnet. The authors showed the reversal of the nanomagnet by linearly decreasing bias voltage $V = 1.5 - 0.00075t$ (see Fig. 3 in Ref. 13). The magnetization reversal, in this case, was accompanied by complex dynamical behavior of the phase and continued during a sufficiently long time interval.

In contrast, in the present work we investigate the magnetization reversal in the system described by Equation (2) under the influence of the electric current pulse of rectangular and Gaussian forms. The effect of the rectangular electric current pulse is modeled by $I_{pulse} = A_s$ in the Δt time interval ($t_0 - \frac{\Delta t}{2}, t_0 + \frac{\Delta t}{2}$) and $I_{pulse} = 0$ in other cases. The form of the current pulse is shown in the inset to Fig. 2(a).

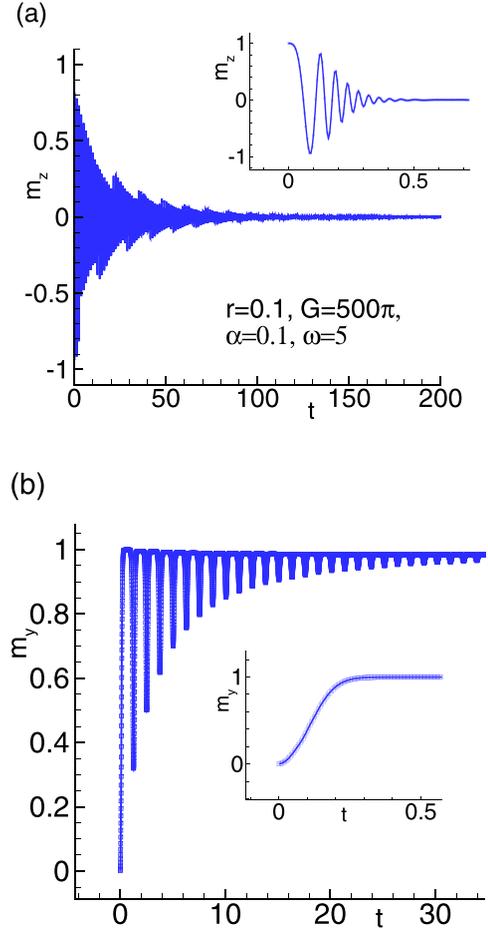


FIG. 1. (a) Dynamics of m_z in the case of $\omega_J = 5$, $G = 500\pi$, $r = 0.1$, and $\alpha = 0.1$. The inset shows the character of time dependence in the beginning of the time interval; (b) The same as in (a) for m_y .

Here, we consider the JJ with low capacitance C ($R^2 C / L_J \ll 1$, where L_J is the inductance of the JJ and R is its resistance), i.e., we do not take into account the displacement current. So, the electric current through JJs is

$$I_{pulse} = w \frac{d\varphi}{dt} + \sin(\varphi - r m_y), \quad (3)$$

where $w = \frac{V_F}{I_c R} = \frac{\omega E}{\omega_R}$, $V_F = \frac{\hbar \omega E}{2e}$, I_c – critical current, R – resistance of JJ, and $\omega_R = \frac{2e I_c R}{\hbar}$ – characteristic frequency. We solved the system of equation (2) together with Equation (3) and describe the dynamics of the system. The time dependence of the electric current is determined through the time dependence of phase difference φ and magnetization components m_x , m_y , and m_z .

We first study the effect of the rectangular pulse shown in the inset to Fig. 2(a). It is found that the reversal of magnetic moment can indeed be realized at optimal values of JJ (G , r) and pulse (A_s , Δ , t_0) parameters. An example of the transition dynamics for such reversal of m_z with residual oscillation is demonstrated in Fig. 2(a); the corresponding parameter values are shown in the figure.

Dynamics of the magnetic moment components, the phase difference, and superconducting current is illustrated in Fig. 2(b). We see that in the transition region, the phase difference changes from 0 to 2π and, correspondingly, the

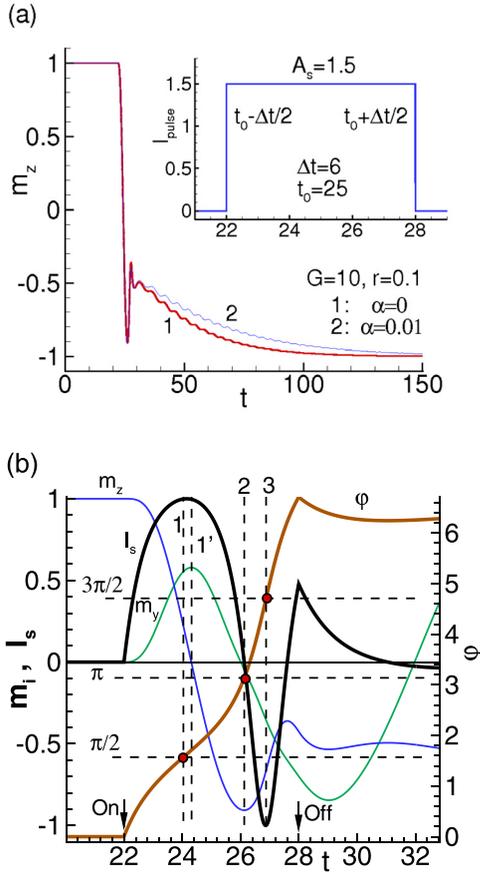


FIG. 2. Transition dynamics of the magnetization component m_z for a system with the rectangular current pulse shown in the inset; (b) Dynamics of magnetization components together with the phase difference φ and superconducting current I_s . Arrows indicate the beginning and end of the electric current pulse. Vertical dashed lines indicate the common features, while the horizontal ones mark the corresponding values of the phase difference.

superconducting current changes its direction twice. This is followed by damped oscillation of the superconducting current. There are some characteristic time points in Fig. 2(b), indicated by vertical dashed lines. Line 1 corresponds to a phase difference of $\pi/2$ and indicates the maximum of superconducting current I_s . The line 1', which corresponds to the maximum of m_y and $m_z=0$, has a small shift from line 1. This fact demonstrates that, in general, the characteristic features of m_x and m_y time dependence do not coincide with the features on the $I_s(t)$, i.e., there is a delay in reaction of magnetic moment to the changes of superconducting current. Another characteristic point corresponds to the $\varphi = \pi$. At this time, line 2 crosses points $I_s=0$, $m_y=0$, and minimum of m_z . At time moment when $\varphi = 3\pi/2$, line 3 crosses the minimum of I_s . When the pulse is switched off, the superconducting current starts to flow through the resistance, demonstrating damped oscillations and causing residual oscillations of magnetic moment components. Note also that the time at which the current pulse ends ($t=28$) actually does not manifest itself immediately in the m_y (and not shown here m_x) dynamics. They demonstrate continuous transition to the damped oscillating behavior.

Fig. 2(b) provides us with a direct way of determining the spin-orbit coupling strength in the junction via estimation of r . For this, we note that $\varphi(t) = \varphi_{00} + \int_0^t V(t')dt'$ can be

determined, up to an initial time-independent constant φ_{00} , in terms of the voltage $V(t)$ across the junction. Moreover, the maxima and minima of I_s occur at times t_{\max} and t_{\min} (see Fig. 2(b)) for which $\sin[\varphi_{00} + \int_0^{t_{\max}} V(t')dt' - r m_y(t_{\max})] = +[-]1$. Eliminating φ_0 from these equations, one gets

$$\sin \frac{1}{2} \left[\int_{t_{\max}}^{t_{\min}} V(t')dt' + r[m_y(t_{\max}) - m_y(t_{\min})] \right] = 1, \quad (4)$$

which allows us, in principal, to determine r in terms of the magnetization m_y at the position of maxima and minima of the supercurrent and the voltage V across the junction. We stress that for the experimental realization of the proposed method, one would need to resolve the value of the magnetization at the time difference of the order of $10^{10} - 10^9 c$. At the present stage, the study of the magnetization dynamics with such a resolution is extremely challenging. To determine the spin-orbit coupling constant r experimentally, it may be more convenient to vary the parameters of the current pulse $I(t)$ and study the threshold of the magnetic moment switching.

The dynamics of the system in the form of magnetization trajectories in the planes $m_y - m_x$ and $m_z - m_x$ during a transition time interval at the same parameters of the pulse and JJ at $\alpha=0$ is presented in Fig. 3. We see that magnetic moment makes a spiral rotation approaching the state with $m_z = 1$ after switching off the electric current pulse. The figures show clearly the specific features of the dynamics around points B, A', and Q and damped oscillations of the magnetization components (see Figs. 3(b) and 3(d)). The cusps at point B in Fig. 3(a) correspond just to the change from an increasing absolute value of m_x to its decreasing and, opposite, at point A' in Fig. 3(c). The behavior of the magnetic system happens to be sensitive to the parameters of

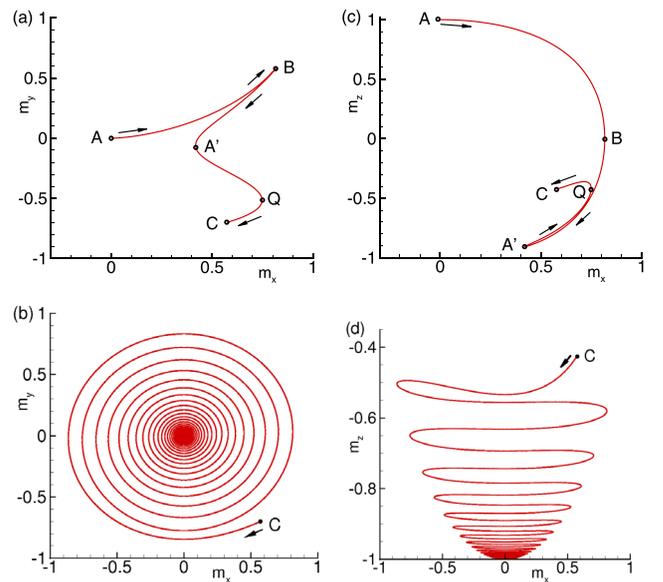


FIG. 3. Trajectories of magnetization components in the planes $m_y - m_x$ in the transition region: (a) during electric pulse action (between points A and C) and (b) after switching the pulse off; In (c) and (d), the same is shown for the $m_y - m_z$ plane. Parameters of the pulse and the JJ are the same as in Fig. 2(a) at $\alpha = 0$.

the electric current pulse and JJ. In the [supplementary material](#), we show three additional protocols of the magnetization reversal by the variation of A_s , G , and r .

It is interesting to compare the effect of the rectangular pulse with the Gaussian one of the form

$$I_{pulse} = A_s \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(t-t_0)^2}{2\sigma^2}\right), \quad (5)$$

where σ denotes the full width at half-maximum of the pulse and A is its maximum amplitude at $t=t_0$. In this case, we also solve numerically the system of equation (2) together with Equation (3) using (5). An example of magnetic moment reversal in this case is presented in Figure 4, which shows the transition dynamics of m_z for the parameters $r=0.1$, $G=10$, $A_s=5$, and $\sigma=2$ at small dissipation $\alpha=0.01$. We see that the magnetization reversal occurs more smoothly in comparison with a rectangular case.

We also note that a very important role in the reversal phenomena belongs to the effect of damping. It is described by the term α in the system of equation (2), where α is a damping parameter. The examples of the magnetization reversal at $G=50$ and $r=0.1$ and different values of α are presented in Fig. 5. We see that dissipation can bring the magnetic system to full reversal; even if at $\alpha=0$ the system does not demonstrate reversal. Naturally, the magnetic moment, after reversal, shows some residual oscillations as well. We stress that the full magnetization reversal is realized in some fixed intervals of the dissipation parameter. As expected, the variation of the phase difference by π reflects the maxima in the time dependence of the superconducting current. Fig. 6 demonstrates this fact. The presented data show that the total change of phase difference consists of 6π , which corresponds to the six extrema in the dependence $I_s(t)$. After the full magnetization reversal is realized, the phase difference shows the oscillations only.

One of the important aspects of the results that we obtain here is the achievement of a relatively short switching time interval for magnetization reversal. As we have seen in Figs. 2(a) and 4, the time taken for such reversal is $\omega_F t \simeq 100$, which translates to 10^{-8} s for typical $\omega_F \simeq 10$ GHz. We note that this amounts to a switching time which is 1/20th of that obtained in Ref. 13.

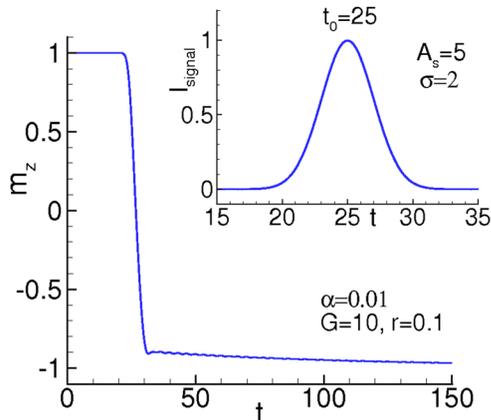


FIG. 4. Demonstration of transition dynamics of m_z for a Gaussian electric current pulse (shown in the inset).

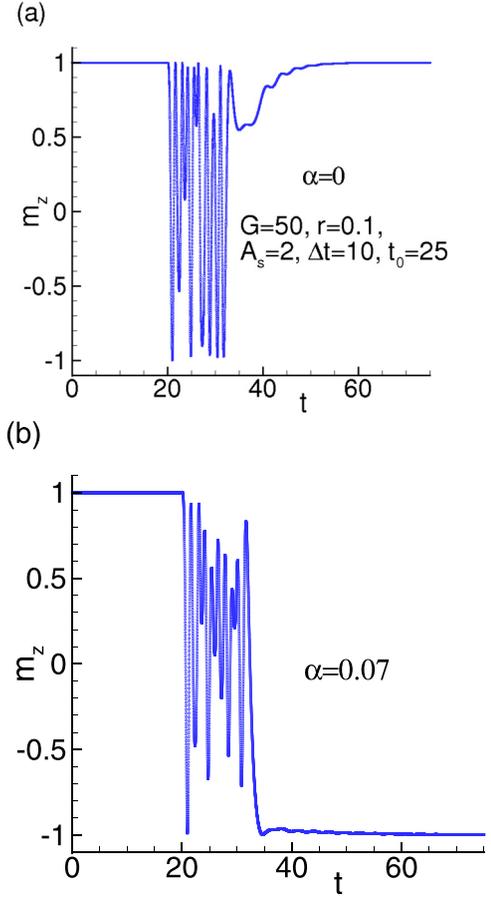


FIG. 5. Magnetization dynamics under the rectangular pulse signal in the system at different values of the dissipation parameter α .

Experimental verification of our work would involve measurement of $m_z(t)$ in a φ_0 junction subjected to a current pulse. For appropriate pulse and junction parameters as outlined in Figs. 4 and 5, we predict the observation of reversal of m_z at late times $\omega_F t \geq 50$. Moreover, the measurement of m_y at times t_{max} and t_{min} where I_s reaches maximum and minimum values and the voltage $V(t)$ across the junction between these times would allow for the experimental determination of r via Eq. (4).

As a ferromagnet, we propose to use a very thin F layer on the dielectric substrate. Its presence produces the

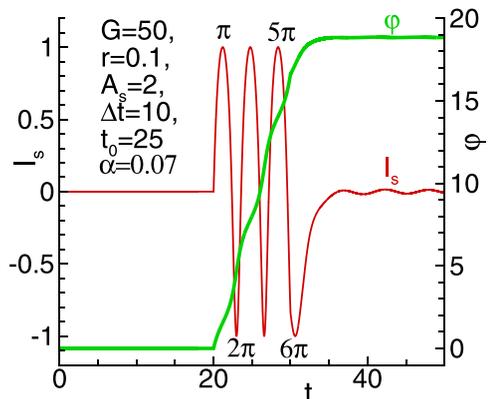


FIG. 6. Transition dynamics of the phase difference and the superconducting current for the case presented in Fig. 5(b).

Rashba-type spin-orbit interaction, and the strength of this interaction will be large in metal with large atomic number Z . The appropriate candidate is a permalloy doped with Pt .¹⁶ In Pt , the spin-orbit interaction plays a very important role in electronic band formation and the parameter v_{so}/v_F , which characterizes that the relative strength of the spin-orbit interaction is $v_{so}/v_F \sim 1$. On the other hand, the Pt doping of the permalloy up to 10% did not influence significantly its magnetic properties¹⁶ and then we may expect v_{so}/v_F to reach 0.1 in this case also. If the length of the F layer is of the order of the magnetic decaying length $\hbar v_F/h$, i.e., $l \sim 1$, we have $r \sim 0.1$. Another suitable candidate may be a Pt/Co bilayer, ferromagnet without inversion symmetry like $MnSi$ or $FeGe$. If the magnetic moment is oriented in plane of the F layer, then the spin-orbit interaction should generate a φ_0 Josephson junction⁶ with a finite ground phase difference. The measurement of this phase difference (similar to the experiments in Ref. 17) may serve as an independent way for the parameter r evaluation. The parameter G has been evaluated in Ref. 9 for weak magnetic anisotropy of permalloy $K \sim 4 \times 10^5 \text{K}\text{\AA}^3$ (see Ref. 18) and $S/F/S$ junction with $l \sim 1$ and $T_c \sim 10 \text{K}$ as $G \sim 100$. For stronger anisotropy, we may expect $G \sim 1$.

In summary, we have studied the magnetization reversal in the φ_0 -junction with direct coupling between magnetic moment and Josephson current. By adding the electric current pulse, we have simulated the dynamics of magnetic moment components and demonstrated the full magnetization reversal at some parameters of the system and external signal. Particularly, the time interval for magnetization reversal can be decreased by changing the amplitude of the signal and spin-orbit coupling. The observed features might find an application in different fields of superconducting

spintronics. They can also be considered as a fundamental basis for memory elements.

See [supplementary material](#) for the demonstration of different protocols of the magnetization reversal by variation of Josephson junction and electric current pulse parameters.

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