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# Resolution and reconciliation of non-binary gene trees with transfers, duplications and losses

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## Abstract

**Motivation:** Gene trees reconstructed from sequence alignments contain poorly supported branches when the phylogenetic signal in the sequences is insufficient to determine them all. When a species tree is available, the signal of gains and losses of genes can be used to correctly resolve the unsupported parts of the gene history. However finding a most parsimonious binary resolution of a non binary tree obtained by contracting the unsupported branches is NP-hard if transfer events are considered as possible gene scale events, in addition to gene origination, duplication and loss.

**Results:** We propose an exact, parameterized algorithm to solve this problem in single-exponential time, where the parameter is the number of connected branches of the gene tree that show low support from the sequence alignment or, equivalently, the maximum number of children of any node of the gene tree once the low-support branches have been collapsed. This improves on the best known algorithm by an exponential factor. We propose a way to choose among optimal solutions based on the available information. We show the usability of this principle on several simulated and biological data sets. The results are comparable in quality to several other tested methods having similar goals, but our approach provides a lower running time and a guarantee that the produced solution is optimal.

**Availability:** Our algorithm has been integrated into the ecceTERA phylogeny package, available at [http://mbb.univ-montp2.fr/MBB/download\\_sources/16\\_\\_ecceTERA](http://mbb.univ-montp2.fr/MBB/download_sources/16__ecceTERA) and which can be run online at <http://mbb.univ-montp2.fr/MBB/subsection/softExec.php?soft=ecceTERA>.

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## 1 Introduction

Constructing good gene trees is both crucial and very challenging for molecular evolutionary studies. The most common way to proceed is to compute a multiple alignment of nucleotide or protein sequences from a gene family, and search for an evolutionary tree that is most likely to produce this alignment (under some evolutionary model). Additionally, it is strongly advised to compute statistical supports on the branches of the output tree, as this tells whether they are inferred from the signal of mutations contained in the alignment or are chosen at random in the absence of signal (Felsenstein, 2004). Commonly, it is very rare that the gene sequences contain enough mutations, but not too many, to support all the branches of a gene phylogeny (Mossel and Steel, 2005).

In consequence, it is very rare that a maximum-likelihood tree computed from a multiple alignment reflects the true history of the genes.

A way to approach this true history is to use the information contained in a species tree to correct the branches of the gene tree that are not supported by the alignment. Understanding a gene tree, given its species tree, requires the introduction of gene scale events, as the birth of the gene, its death, its replication and diversification by speciation, duplication, and horizontal gene transfer (Szöllősi *et al.*, 2015). Such a complete history is called a *reconciliation* and, if costs are assigned to each gene scale event, it has a total cost. Binary gene trees reconstructed with the additional information of this reconciliation cost show a higher quality, according to all tests on methods that are able to perform such a construction: MowgliNNI (Nguyen *et al.*, 2013), ALE (Szöllősi *et al.*, 2013), TERA (Scornavacca *et al.*, 2015), TreeFix-DTL (Bansal *et al.*, 2014) and JPrIME-DLTRS (Sjöstrand *et al.*, 2014) (we enumerate only the methods allowing

horizontal gene transfers). However, these methods generally require intensive computation time.

Here, we provide an algorithm that, given a species tree  $S$  and a gene tree  $G$  with supports on its branches, computes a modified gene tree  $G'$  such that all well-supported branches of  $G$  are in  $G'$  and no other gene tree modified in such a way has a lower reconciliation cost than  $G'$ . “Well supported” is defined by a threshold chosen by the user, or by an adaptive method which sets this support according to the algorithm complexity. This problem reduces to the reconciliation of non-binary gene trees with binary species trees. Although optimal and practical methods are known in the absence of gene transfers (Noutahi *et al.*, 2016), this problem has been shown to be NP-hard (Kordi and Bansal, 2015) with gene transfers. Letting  $k$  be the maximum number of children of any node of the gene tree after collapsing branches of low support, the problem can be solved in  $2^k \cdot k^k \cdot (|S| + |G|)^{O(1)}$  time (Kordi and Bansal, 2016). We employ amalgamation principles (David and Alm, 2011; Szöllösi *et al.*, 2013; Scornavacca *et al.*, 2015) to provide an algorithm with a time complexity of  $(3^k - 2^{k+1}) \cdot (|S| + |G|)^{O(1)}$ , which gives access to a wider range of data. This, however, comes at the price of using  $\Theta(2^k)$  space while the algorithm of Kordi and Bansal (2016) runs in polynomial space. We provide an implementation of our algorithm and we propose a way to choose among all optimal solutions according to the supports of the branches of the input tree. We show on both simulated and real data sets that our method produces gene trees whose quality is similar to those constructed by competitive methods, often in a smaller amount of time.

The novelties of this method compared to the previous ones are: (1) a lower running time, allowing it to run on larger datasets; (2) guaranteed optimal solutions; and (3) a simpler input – the input data consists of a gene tree with supports and a species tree, without the need to supply a gene alignment or a sample of gene trees that other methods rely on. Moreover, our method is integrated into the user-friendly ecceTERA package so that anyone having a gene tree with supports – output by standard ML software such as PhyML or RAxML – and a species tree (with or without dates), can quickly obtain a better-quality gene tree, or even correct a whole database in reasonable time.

## 2 An FPT algorithm for reconciling gene trees with polytomies

### 2.1 Reconciliation of binary gene trees

For our purposes, a *rooted phylogenetic tree*  $T = (V(T), E(T), r(T))$  is an oriented tree, where  $V(T)$  is the set of nodes,  $E(T)$  is the set of arcs, all oriented away from  $r(T)$ , the root. For an arc  $(x, y)$  of  $T$ , we call  $x$  the *parent* of  $y$ , and  $y$  a *child* of  $x$ . The number of children of  $x$ , denoted by  $k_x$ , is called the *out-degree* of  $x$ . If a path from the root to  $y$  contains  $x$ , then  $x$  is an *ancestor* of  $y$  and  $y$  is a *descendant* of  $x$ . This defines a partial order denoted by  $y \leq_T x$ , and  $y <_T x$  if  $x \neq y$ . The subtree of  $T$  that is *rooted at* a node  $u$  of  $T$  (denoted by  $T_u$ ) is the result of deleting all nodes  $v$  with  $v \not\leq_T u$  from  $T$ . Nodes with no children are *leaves*, all others are *internal nodes*. The set of leaves of a tree  $T$  is denoted by  $L(T)$ . The leaves of  $T$  are bijectively labeled by a set  $\mathcal{L}(T)$  of labels. A tree is *binary* if  $k_x = 2$  for all internal nodes  $x$ . A tree  $T$  is *dated* if a total order  $\leq_\theta$  on internal nodes that extends  $\leq_T$  is given. Each internal node then implies a *date* between 1 and  $|V(T)| - |L(T)|$  (the root) and all the leaves are assumed to have date 0. The *dated subdivision*  $T'$  of a dated tree  $T$  is obtained by replacing each arc  $(x, y)$  by a path containing  $d$  additional nodes, where  $d+1$  is the difference between the date of  $x$  and the date of  $y$ .

A reconciliation involves two rooted phylogenetic trees, a *gene tree*  $G$  and a *species tree*  $S$ , both binary. Their relation is set by a function  $s : \mathcal{L}(G) \rightarrow \mathcal{L}(S)$ , which means that each extant gene belongs to an extant species. Note that  $s$  does not have to be injective (several genes

of  $G$  can belong to the same species) or surjective (some species may not contain any gene of  $G$ ). A *reconciliation*  $\alpha$  of  $G$  in  $S$  is a mapping of each internal node  $u$  of  $G$  to a sequence  $(\alpha(u)_1, \alpha(u)_2, \dots)$  of nodes of  $S$  if  $S$  is undated or nodes of the dated subdivision  $S'$  of  $S$  if  $S$  is dated. Herein, for each  $i \geq 1$ , we have  $\alpha(u)_{i+1} \leq_T \alpha(u)_i$  and  $\alpha(u)_i$  satisfies the constraints of any one of the possible events among duplication ( $\mathbb{D}$ ), transfer ( $\mathbb{T}$ ), loss ( $\mathbb{L}$ ), or speciation ( $\mathbb{S}$ ) – see the appendix in the supplementary material for more details. This ensures that a coherent gene history can be extracted from  $\alpha$ . Given costs for individual  $\mathbb{D}$ ,  $\mathbb{T}$  and  $\mathbb{L}$  events (it is usually assumed that speciation does not incur cost), denoted respectively  $\delta$ ,  $\tau$  and  $\lambda$ , a reconciliation  $\alpha$  is assigned the cost  $c(\alpha) := d\delta + t\tau + l\lambda$ , where  $d$ ,  $t$  and  $l$  denote the respective numbers of events of type  $\mathbb{D}$ ,  $\mathbb{T}$  and  $\mathbb{L}$  implied by  $\alpha$ . We denote by  $\mathcal{R}(G, S)$  the set of all possible reconciliations of  $G$  in  $S$  and define  $c_{\mathbb{DTL}}(G, S) := \min_{\alpha \in \mathcal{R}(G, S)} c(\alpha)$ , that is, the minimum cost over all possible reconciliations of  $G$  in  $S$ . We call  $c_{\mathbb{DTL}}(G, S)$  the *cost* of  $G$  with respect to a species tree  $S$ . A reconciliation  $\alpha$  achieving this cost is called *most parsimonious reconciliation* (MPR).

#### Problem 1. Most Parsimonious Reconciliation

**Instance:** a (dated) binary species tree  $S$ , a binary gene tree  $G$ , costs  $\delta$ ,  $\tau$ ,  $\lambda$  for respective  $\mathbb{D}$ ,  $\mathbb{T}$ ,  $\mathbb{L}$  events

**Output:** a reconciliation of  $G$  in  $S$  of minimal cost

This problem can be solved in  $O(|S|^2 \cdot |G|)$  time (Doyon *et al.*, 2010) for dated trees, and  $O(|S| \cdot |G|)$  time for undated ones (Bansal *et al.*, 2012). In the following, we turn our attention to non-binary gene trees and we consider the species tree as dated. Nevertheless, every result is also valid for the undated case with better complexity, see Section 3.3.

### 2.2 Resolution of non-binary gene trees

If a node in a tree  $T$  has more than two children, we call this node a *polytomy*. Note that a node  $a$  of  $T$  partitions  $L(T)$  into two sets, the descendants of  $a$  and all others. Given a gene tree  $G$  with at least one polytomy, a binary tree  $G'$  is called a *binary resolution* of  $G$  if  $G$  can be obtained from  $G'$  by contracting edges. We denote by  $\text{BR}(G)$  the set of all binary resolutions of  $G$ .

#### Problem 2. Polytomy Solver under the $\mathbb{DTL}$ framework

**Instance:** a dated binary species tree  $S$ , a gene tree  $G$ , costs  $\delta$ ,  $\tau$ ,  $\lambda$  respectively for  $\mathbb{D}$ ,  $\mathbb{T}$ ,  $\mathbb{L}$  events

**Output:** a binary resolution  $G'$  of  $G$  minimizing  $c_{\mathbb{DTL}}(G', S)$

This problem – introduced by Chang and Eulenstein (2006) – is known to be NP-hard (Kordi and Bansal, 2015), and can be solved in time  $O(|G| + |S|)$  for  $\tau = \infty$  (Zheng and Zhang, 2014b).

A brute-force approach would need to generate all binary resolutions. There are  $(2n - 3)!! \approx \sqrt{2} \left(\frac{2}{e}(n - 1)\right)^{n-1}$  different rooted binary trees on  $n$  leaves, which gives  $|\text{BR}(G)| \sim \prod_{u \in V(G) \setminus L(G)} \sqrt{2} \left(\frac{2}{e}(k_u - 1)\right)^{k_u - 1}$  different binary resolutions of  $G$ . This yields an algorithm with time complexity  $O(|S|^2 \cdot |G| \cdot |\text{BR}(G)|)$ . Using the following result, we can improve on the brute-force approach.

**Theorem 2.1.** *Let  $S$  be a species tree, let  $G$  be a gene tree, and let  $u$  be a polytomy in  $G$ . Let  $G' \in \text{BR}(G)$  and let  $\alpha \in \mathcal{R}(G', S)$  such that  $\alpha$  is an MPR between  $S$  and  $G'$  and no MPR between  $S$  and any other binary tree in  $\text{BR}(G)$  is strictly cheaper than  $\alpha$ . Let  $G_u^* \in \text{BR}(G_u)$  and let  $\beta \in \mathcal{R}(G_u^*, S)$  such that  $\beta(u)_1 = \alpha(u)_1$ . Then,  $c(\alpha_u) \leq c(\beta)$ , where  $\alpha_u$  is the restriction of  $\alpha$  to  $G_u^*$ . Less formally, a binary resolution of  $G$  allowing a globally optimal reconciliation  $\alpha$  is also locally optimal for each subtree rooted at a polytomy  $u$  (provided that  $u$  is mapped to the same species  $v$ ).*

This implies that an MPR  $\alpha$  on the whole tree  $G$  always yields an MPR on a subtree  $G_u$  (where the first node in the mapping of  $u$  is constrained to be the same as in  $\alpha$ ); so we can progressively reconstruct a global solution by amalgamating MPRs on subtrees. We do not give a proof of Theorem 2.1 here because it will be a consequence of our main Theorem 2.2. Nevertheless, we note here that the dynamic programming algorithm by Doyon *et al.* (2010) with the help of Theorem 2.1 permits us to solve Problem 2 with a lower complexity: Whenever we encounter a polytomy  $u$  in its bottom-up approach, we store, for each  $v \in V(S)$ , the minimum cost of a reconciliation associating  $u$  with  $v$  over all binary resolutions of  $G_u$ .

**Observation 2.1.** *A solution for Problem 2 can be found by solving polytomies one by one in a bottom-up approach, with a time complexity of  $O(|S|^2 \cdot |G| \cdot (\frac{2}{e}(k-1))^{k-1})$ , where  $k$  is the maximum number of children of any node in  $G$ .*

Note that this has been independently observed by Kordi and Bansal (2016), who presented an algorithm having the same asymptotic time complexity as the approach described in Observation 2.1.

While Observation 2.1 already implies that Problem 2 is fixed-parameter tractable<sup>1</sup> (FPT) with respect to the maximum out-degree in  $G$ , it remains interesting to search for a single-exponential-time algorithm that could process larger gene trees and even genome-wide data. The idea for such an algorithm comes from the amalgamation principle.

### 2.3 Amalgamation of gene trees

A node  $u$  of a binary tree  $T$  is said to generate the *clade*  $C(u) = \mathcal{L}(T_u)$ . If  $u$  has distinct children  $u_r$  and  $u_l$ , we also say that  $u$  generates the tripartition  $(C(u), \{C(u_l), C(u_r)\})$ , otherwise,  $u$  generates the *trivial* tripartition  $(C(u), \{\emptyset, \emptyset\})$ . Herein, we call  $C(u)$  the *domain* of the tripartition. A binary tree  $T$  generates a set of clades and tripartitions, respectively denoted  $\mathcal{C}(T)$  and  $\Pi(T)$ , which are the clades and tripartitions generated by its nodes.

More generally, for a set of labels  $L$ , a clade is a subset of  $L$  and a tripartition is a tuple  $(C, \{C_r, C_l\})$  such that the clades  $C_r, C_l$  partition the clade  $C$ . Let  $\Pi$  be a set of tripartitions on  $L$ . We denote the set of clades present in  $\Pi$  by  $\mathcal{C}(\Pi)$ . Further,  $\Pi$  is said to be *complete* if it contains  $L$  as the domain of some tripartition, and for each tripartition  $(A, \{B, C\})$  either  $B = C = \emptyset$  or  $\Pi$  contains tripartitions with  $B$  and  $C$  as respective domains. It is easy to see that the set of tripartitions generated by a binary tree is always complete, and conversely, for any complete set of tripartitions  $\Pi$  on  $L$ , there is at least one binary tree  $G$  with  $\mathcal{L}(G) = L$ , which generates a subset of  $\Pi$ . The amalgamation problem is to generate one minimizing the reconciliation cost with respect to a species tree:

**Problem 3.** Amalgamation under the DTL framework

**Input:** a complete set of tripartitions  $\Pi$  on a set of labels  $L$ , a dated binary species tree  $S$ , a labeling function  $s : L \rightarrow \mathcal{L}(S)$  and costs  $\delta, \tau, \lambda$  respectively for  $\mathbb{D}, \mathbb{T}, \mathbb{L}$  events

**Output:** a binary gene tree  $\bar{G}$  minimizing  $c_{\text{DTL}}(\bar{G}, S)$  over all binary gene trees  $G'$  with  $\mathcal{L}(G') = L$  and such that the set of tripartitions generated by  $G'$  is a subset of  $\Pi$

This problem can be solved in  $O(|S|^2 \cdot |\Pi|)$  time (Scornavacca *et al.*, 2015). Given a non-binary tree  $G$ , we can generate a complete set of tripartitions containing all tripartitions of any binary resolution of  $G$  as follows: for each node  $u$  of  $G$  with child set  $\{u_1, \dots, u_t\}$ , and for each  $I \subseteq \{u_1, \dots, u_t\}$ ,  $u$  generates a tripartition  $(A, \{B, C\})$  such that

$B \cup C = A \subseteq \bigcup_{i \in I} C(u_i)$  and none of  $B$  or  $C$  overlap any  $C(u_i)$  (overlapping means containing some elements but not all). The union of all these tripartitions is the set of tripartitions of  $G$ , noted  $\Pi(G)$  as in the binary case. Now, if the set  $\Pi$  in Problem 3 is set to  $\Pi(G)$  and the labelling function  $s$  associates the genes in  $G$  to the correct species in  $S$ , then Problems 2 and 3 are equivalent: indeed, it is easy to see that any binary resolution  $G'$  of  $G$  is such that the set of tripartitions generated by  $G'$  is a subset of  $\Pi(G)$ , and that the converse holds too. Thus, the known dynamic programming algorithm solving Problem 3 (Scornavacca *et al.*, 2015) yields a novel algorithm for the resolution of polytomies.

**Theorem 2.2.** *Let  $G$  be a non-binary gene tree. An amalgamation solution on  $\Pi(G)$  is an optimal binary resolution of  $G$ .*

The complexity of this algorithm is  $O(|S|^2 \cdot |\Pi(G)|)$ . We can bound the size of  $\Pi(G)$  using the following statement.

**Lemma 2.3.** *For any gene tree  $G$ ,  $|\Pi(G)| = O(|G| \cdot (3^k - 2^{k+1}))$ , where  $k$  is the maximum out-degree of any node in  $G$ .*

**Proof.** Let  $u$  be a node of  $G$ , and  $u_1, \dots, u_t$  its children. Recall that, for each  $I \subseteq \{u_1, \dots, u_t\}$ ,  $u$  generates a tripartition  $(A, \{B, C\})$  such that  $B \cup C = A \subseteq \bigcup_{i \in I} C(u_i)$  and none of  $B$  or  $C$  overlap any  $C(u_i)$ . Any tripartition  $(A, \{B, C\})$  generated by  $u$  is isomorphic to a partition of  $\{C(u_1), \dots, C(u_t)\}$  into three sets,  $B, C$ , and  $\bigcup_i C(u_i) \setminus A$  with  $B \neq \emptyset$  and  $C \neq \emptyset$ . There are  $3^t$  partitions of  $t$  elements into three sets, with  $2 \cdot 2^t$  of them having  $B = \emptyset$  or  $C = \emptyset$ . If the (unique) partition with  $B = C = \emptyset$  is not counted twice, we get  $3^t - 2^{t+1} + 1$  such partitions. Finally, we can remove half of the remaining partitions by the symmetry of  $B$  and  $C$  and arrive at a count of  $1/2(3^t - 2^{t+1} + 1)$ . Thus, there are  $1/2(3^t - 2^{t+1} + 1)$  such partitions and, hence, this is also an upper bound on the number of tripartitions generated by  $u$ . Summing over all vertices of  $G$ , the total number of tripartitions generated by  $G$  is then bounded by  $|G| \cdot 1/2(3^k - 2^{k+1} + 1)$  where  $k$  is the maximum out-degree in  $G$ .  $\square$

This leads to the main theoretical result of the paper

**Proposition 2.4.** *For any gene tree  $G$ , Problem 2 can be solved in  $O(|S|^2 \cdot |G| \cdot (3^k - 2^{k+1}))$  time for dated species trees, where  $k$  is the maximum out-degree in  $G$ .*

The running-time in Proposition 2.4 improves on the previous result (see Kordi and Bansal (2016) or Observation 2.1) by an exponential factor, allowing us to optimally reconcile gene trees with out-degrees of  $O(\log |G|)$  in polynomial time.

## 3 Practical issues

In order to turn the algorithmic principle described in the previous section into a workable method for biological datasets, we have to handle three issues: one is that the position of the root in the gene tree is usually unknown; a second is that species trees are usually undated; the last and most difficult one is the choice between multiple solutions. Indeed, in some cases the solution space of the problems defined in the previous sections is huge and two different solutions can be far apart. But some information from branch supports – encoded in the tripartitions to be used in the amalgamation algorithm – can be used to efficiently find a good solution. We address this issue first.

### 3.1 Scoring tripartitions as a guide in the solution space

Given a multiset of tripartitions  $\Pi$  on  $L$ , the *conditional probability* of a tripartition  $\pi = (C_1, \{C_2, C_3\})$  in  $\Pi$  is the ratio  $f_{\Pi}(\pi)/f_{\Pi}(C_1)$ , where, for each clade and tripartition in  $\Pi$ ,  $f_{\Pi}(\cdot)$  denotes its frequency in  $\Pi$  (Höhna and Drummond, 2012). The *conditional clade probability* of a

<sup>1</sup> An algorithm is FPT with respect to  $p$  if its running time is  $f(p) \cdot \text{poly}(n)$  where  $f$  is some function that only depends on  $p$  and  $n$  is the size of the instance.

binary tree  $G$  such that  $\mathcal{L}(G) = L$ , denoted by  $P_{\text{CCP}}(G)$ , is defined as the product of the conditional probabilities of all tripartitions in  $\Pi(G)$ .

Problem 2 admitting a multitude of optimal solutions, Kordi and Bansal (2016) propose to enumerate them all. We propose to exploit the support of the branches in the input tree to evaluate each solution and reduce the size of the output. To this end, we construct an artificial probability space, where the conditional probability of a tripartition  $\pi = (C_1, \{C_2, C_3\})$  is still  $f_{\Pi}(\pi)/f_{\Pi}(C_1)$ , but where  $f$  is redefined using information from branch supports of the input tree. The rationale is that for the clades present in the input tree we use the supports of the corresponding branches to approximate the frequency in an imaginary sample  $\mathcal{G}$  of binary resolutions, while the clades that are not present in the input tree are considered equiprobable. So we have to assign a probability to each clade and, in the following, we explain precisely how.

*Frequency of clades.* Let  $G^B$  be a rooted binary tree with supports on its branches and let  $G$  be the multifurcated gene tree obtained from  $G^B$  by contracting unsupported branches (according to a given threshold), we define a support  $f(C_1)$  for each clade  $C_1$  generated by  $G$ . If  $C_1 \in \mathcal{C}(G^B)$ , then  $f(C_1)$  is its support, i.e. the support of the branch leading to the clade<sup>2</sup>. Otherwise, there is a clade in  $G^B$  that is incompatible with  $C_1$ . Among all such clades, let  $C_0$  be one that maximizes  $f(C_0)$ . Then, we use the knowledge of the frequency of  $C_0$  to infer the frequency of  $C_1$  in our imaginary sample  $\mathcal{G}$  by assuming that the ratio of trees generating  $C_1$  to trees not generating  $C_0$  is the same in  $\mathcal{G}$  as in  $BR(G)$ . Thus, the support of  $C_1$  is defined as  $f(C_1) := (1 - f(C_0)) \cdot \frac{g(C_1)}{1 - g(C_0)}$ , where  $g(C)$  is the frequency of a clade  $C$  in  $BR(G)$ . To compute  $g(C)$ , suppose  $C$  is generated by a vertex  $u$  of  $G$  with  $n(u)$  children, and that  $n(C)$  is the number of children of  $u$  ‘‘contained’’ in  $C$ . Then:

$$g(C) := \frac{\#T(n(C)) \cdot \#T(n(u) - n(C) + 1)}{\#T(n(u))}$$

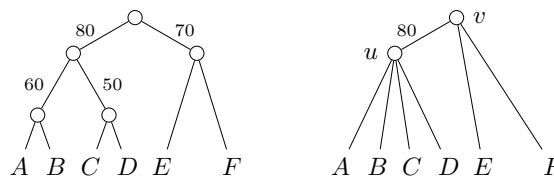
where  $\#T(k)$  is the number of rooted binary trees with  $k$  leaves, i.e.  $(2k - 3)!!$ . For example, given the trees in Figure 1, the support of the clade  $\{C, D\}$  is 0.5 (i.e. 50/100), while the support of  $\{A, B, C\}$  (which conflicts with  $\{C, D\}$ ) is  $0.5 \cdot \frac{1}{4} = \frac{1}{8}$  (note that  $g(\{C, D\}) = g(\{A, B, C\}) = \frac{3}{15}$ ).

*Frequency of tripartitions.* Let  $\pi = (C_1, \{C_2, C_3\})$  be a tripartition. Let  $BR(G)_1$  be the set of binary resolutions of  $G$  that generate  $C_1$  and let  $\mathcal{G}_1 = \mathcal{G} \cap BR(G)_1$  be the part of our imaginary sample whose trees generate  $C_1$ . If  $\pi \in \Pi(G^B)$ , we define  $f(\pi) := \min(f(C_1), f(C_2), f(C_3))$ . Otherwise, either  $G^B$  generates  $C_1$  and a tripartition  $\pi'$  on the same domain  $C_1$  as  $\pi$ , or  $G^B$  does not generate  $C_1$ . In the first case, we use the knowledge of the frequency of  $\pi'$  and  $C_1$  to infer the frequency of  $\pi$  in our imaginary sample by assuming that the ratio of trees generating  $\pi$  to trees not generating  $\pi'$  is the same in  $\mathcal{G}_1$  as in  $BR(G)_1$ . Thus,  $f(\pi) := (f(C_1) - f(\pi')) \cdot \hat{g}(\pi) / (g(C_1) - \hat{g}(\pi'))$ , where  $\hat{g}(\pi)$  is the frequency of  $\pi$  in  $BR(G)$ . In the second case, we assume that the frequency of trees generating  $\pi$  is the same in  $\mathcal{G}_1$  as in  $BR(G)_1$ . Thus,  $f(\pi) := f(C_1) \cdot \hat{g}(\pi) / g(C_1)$ , where  $\hat{g}(\pi)$  is the frequency of  $\pi$  in  $BR(G)$ .

The frequencies  $\hat{g}$  can be computed as follows. If  $\pi = (C_1, \{C_2, C_3\})$  is generated by  $u$ , then we denote by  $n(C_i)$  the number of children of  $u$  whose clades are contained in  $C_i$ . We define  $\hat{g}(\pi)$  as

$$\frac{\#T(n(C_2)) \cdot \#T(n(C_3)) \cdot \#T(n(u) - (n(C_2) + n(C_3)) + 1)}{\#T(n(u))}.$$

<sup>2</sup> Note that supports have to be numbers between 0 and 1, and thus bootstrap values should be divided by the size of the bootstrap sample.



**Fig. 1.** A binary gene tree  $G^B$  (left) and a non-binary one (right) obtained from  $G^B$  by suppressing edges with a support lower than 80.

For example, given the trees in Figure 1, we have the following:

$$\begin{aligned} f(\{A, B, C, D\}, \{\{A, B\}, \{C, D\}\}) &= 0.5, \\ f(\{A, B, C, D\}, \{\{A, C\}, \{B, D\}\}) &= 0.3 \cdot 1/14 \text{ and} \\ f(\{A, B, C\}, \{\{B, C\}, \{A\}\}) &= 1/8 \cdot 1/3. \end{aligned}$$

Finally, conditional clade probability and reconciliation cost can be combined by weighting their ratio (see Scornavacca *et al.* (2015)).

$$c_{\text{joint}}(G', S) = c_{\text{DTL}}(G', S) + c_A N_A(G')$$

where  $G'$  is a gene tree in  $BR(G)$  and the parameter  $c_A$  weights the ‘‘sequence contribution’’  $N_A(G') := -\log(P_{\text{CCP}}(G'))$ . Formally, we have the following problem:

**Problem 4.** Polytoxy Solver with CCPs under the  $\mathbb{DTL}$  framework

**Instance:** a dated binary species tree  $S$ , a gene tree  $G$ , costs  $\delta, \tau, \lambda$  respectively for  $\mathbb{D}, \mathbb{T}, \mathbb{L}$  events

**Output:** a binary resolution  $G'$  of  $G$  minimizing  $c_{\text{joint}}(G', S)$

Note that Problems 2 and 4 coincide when  $c_A = 0$ . In experiments with real-world data, choosing  $c_A > 0$  gives better results (Scornavacca *et al.*, 2015), so we used such a joint score in the experiments (see Section 4).

### 3.2 Unrooted gene trees

Phylogenetic trees are always rooted, but often the position of the root is unknown. The method in the previous section can be used on an unrooted gene tree  $G$  to account for the uncertainty on the position of the root, without additional complexity as follows. First, we call  $G_r$  the rooted tree obtained by rooting  $G$  arbitrarily on an internal edge  $e$ , and  $G_r^B$  the rooted version of  $G^B$ , also rooted on  $e$ . Then we compute the set  $\Pi(G_r)$  of tripartitions as defined in Section 2.3. To obtain  $\Pi(G)$ , we also consider, for each non-trivial tripartition  $(C_1, \{C_2, C_3\}) \in \Pi(G_r)$ , the two other possible tripartitions on  $\mathcal{L}(G)$  that are implied by a different placement of the root, namely  $((\mathcal{L}(G) \setminus C_1) \cup C_2, \{\mathcal{L}(G) \setminus C_1, C_2\})$  and  $((\mathcal{L}(G) \setminus C_1) \cup C_3, \{\mathcal{L}(G) \setminus C_1, C_3\})$ . To these tripartitions, we add the set  $\Pi' := \{(\mathcal{L}(G), \{\{l\}, \mathcal{L}(G) \setminus \{l\}\}) \mid l \in \mathcal{L}(G)\}$  of all trivial tripartitions.

Each edge  $e = (u, v)$  of the rooted binary tree  $G_r^B$  induces two clades  $C_u(e)$  and  $C_v(e)$ , which correspond to the label sets of the leaves of the two subtrees created by removing  $e$ . We say that  $C_u(e)$  is generated by  $u$  and  $C_v(e)$  by  $v$ , and we associate to them the support of  $e$ . Then, we redefine the set  $\mathcal{C}(G_r^B)$  as the set of clades induced by all edges of  $G_r^B$ . Given the set  $\mathcal{C}(G_r^B)$  defined in this way, the support of each clade of  $\mathcal{C}(G_r)$  is then computed as in the rooted case.

Finally, we describe how to give a support value to each tripartition of  $G$  in the unrooted case: The support of each tripartition  $\pi \in \Pi(G_r)$  is computed w.r.t.  $G_r^B$  as described in the previous section, and the support of the two other possible tripartitions on  $\mathcal{L}(G)$  that are implied by a different placement of the root is the same as the support of  $\pi$ . All tripartitions in  $\Pi'$  have support equal to 1.

### 3.3 An undated variant

The method discussed by Scornavacca *et al.* (2015) has been conceived for dated binary species trees, but can easily be adapted to undated ones, while respecting all previously mentioned results, with a slight correction concerning the complexity.

Indeed, reconciliations for undated species trees can be computed in  $O(|S| \cdot |G|)$  time with an algorithm described by Bansal *et al.* (2012). Adapting this algorithm to the amalgamation framework can be done by the same technique used to adapt the  $O(|S|^2 \cdot |G|)$ -time algorithm of Doyon *et al.* (2010) for dated species trees reconciliation to the amalgamation framework as done in (Jacox *et al.*, 2016). Thus, our result translates to an  $O(|S| \cdot |G| \cdot |II|)$ -time algorithm – by Lemma 2.3, an  $O(|S| \cdot |G| \cdot (3^k - 2^{k+1}))$ -time algorithm – for undated species trees.

### 3.4 Adaptive compromise between the amount of correction and the computational complexity

The threshold for deciding if a branch is well-supported or not is, in principle, user-defined. However, in the experiments, we required that, in the multifurcated tree resulting from the contraction of unsupported branches, an internal node has at most 12 children. This is done to avoid the combinatorial explosion and to keep the method fast. So we adopted a strategy of increasing the threshold until the 12 maximum children property was satisfied.

## 4 Application on simulated and biological data

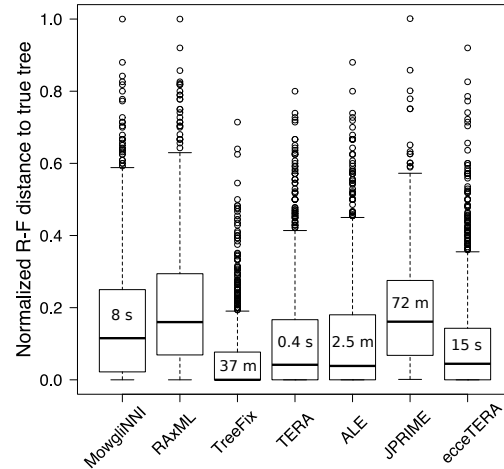
In this section, we use three different data sets, two simulated and one from microbial genomes, to compare the performance of our algorithm with seven different gene tree reconstruction methods: TERA (Scornavacca *et al.*, 2015), ALE (Szöllösi *et al.*, 2013), TreeFix-DTL (Bansal *et al.*, 2014), MowgliNNI (Nguyen *et al.*, 2013), JPrIME-DLTRS (Sjöstrand *et al.*, 2014), RAxML (Stamatakis, 2014) and PhyML (Guindon *et al.*, 2010). The first five use information from the sequences and the species tree, while the last two use only information from the sequences. The method described in this paper has been integrated to the ecceTERA package and thus it is called ecceTERA in the comparisons. TERA has also been implemented in the same package, but it is a different method, described in (Scornavacca *et al.*, 2015). The method presented by Kordi and Bansal (2016) has not been tested because no implementation was available at the time of writing. However, as it also solves Problem 2 (with a higher time complexity than our method), it will give the same results as our method for  $c_A = 0$ , but with a higher running time.

### 4.1 Simulated Proteobacteria Data Set

The proteobacteria data set is the one constructed to test MowgliNNI and made available by Nguyen *et al.* (2013). Starting with a dated phylogeny of 37 proteobacteria (David and Alm, 2011):

- 1000 evolutionary histories comprising  $\mathbb{D}$ ,  $\mathbb{T}$ , and  $\mathbb{L}$  events were simulated along the species tree according to a birth and death process;
- sequences were simulated along these true gene trees under the GTR (General Time Reversible) model using Seq-Gen (Rambaut and Grass, 1997);
- RAxML (Stamatakis, 2014) was used to estimate gene trees (along with 100 bootstrap trees) from these sequences under the GTR model.

We refer to the section “Simulated gene trees and evolutionary histories” of Nguyen *et al.* (2013) for more details on how the data set was composed. Some of the test results are taken from the same procedure proposed by Scornavacca *et al.* (2015).

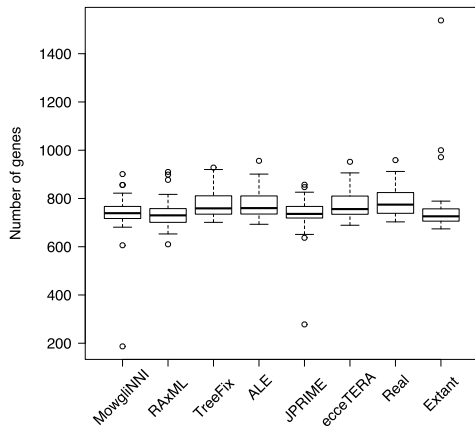


**Fig. 2.** Accuracy of several methods on the simulated proteobacteria data set: we measure the normalized Robinson-Foulds distance of the reconstructed tree to the true gene tree for all 1000 gene trees, for 7 methods. Computing times – except for the computation of the RAxML trees – are given in the boxes (s=seconds, m=minutes). In terms of quality, TreeFix-DTL achieves the best accuracy but is relatively slow. ecceTERA is comparable with the second best methods, both in accuracy and computing time.

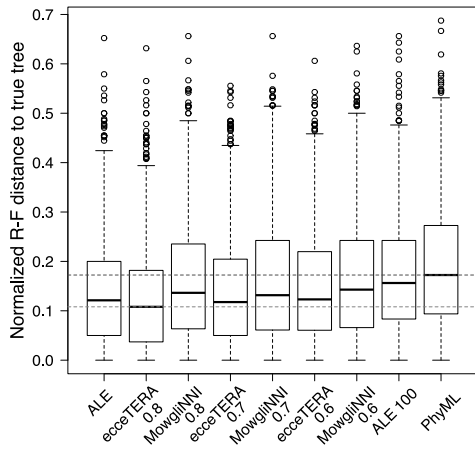
We ran TreeFix-DTL with default parameters, GTR with a gamma distribution as models of evolution, and as a starting tree the RAxML tree. The RAxML tree (with bootstrap values) was also the input given to MowgliNNI and ecceTERA that were run with a threshold for weak edges equal to 70. As in Scornavacca *et al.* (2015), JPrIME-DLTRS was run on the sequence alignments with JC69 with a gamma distribution as model of evolution (GTR is not available in JPrIME-DLTRS), 100 000 iterations, a thinning factor of 10 and a time out of 10h. Finally, TERA and ALE were run on the set of bootstrap trees with default parameters, except for the weight of amalgamation  $c_A$ , fixed to 0.1 for TERA as for ecceTERA.

The accuracy – defined as normalized Robinson-Foulds distance to the true gene tree – of TERA, ecceTERA and ALE is comparable and higher than the one of JPrIME-DLTRS and RAxML (see Figure 2). The method that outperforms the others in this case is TreeFix-DTL. This is possibly due to the fact that the synthetic data set was simulated on the same model used to estimate the gene trees with TreeFix-DTL, making the task easier for the method. Another reason may be the fact that TreeFix-DTL can show signs of significant overfitting of the species tree (Scornavacca *et al.*, 2015). Note also that TreeFix-DTL is slower than ecceTERA, with an average runtime of 37 minutes versus 15 seconds. Interestingly, the accuracy of ecceTERA does not vary if we consider the species tree as undated, while the average runtime decreases considerably (6 seconds). Note that the normalized Robinson-Foulds distance is not fine-grained and it is not necessarily correlated with reconciliation measures, as noted by Zheng and Zhang (2014a). This is why we also compared trees using the (more fine-grained) normalized triplet distance, with similar results (see Figure 1 of the Appendix).

We also counted the number of genes present in ancestral species according to reconciled gene trees. All gene trees, reconstructed from different methods, are reconciled with TERA to have access to the ancestral gene content, considering trees as rooted for all methods but RAxML (RAxML is the only method tested here that outputs unrooted gene trees). We compared it with the number of genes present in extant species. The results are shown in Figure 3.



**Fig. 3.** Number of genes for extant species (“Extant”), or ancestral species reconstructed with reconciled real trees (“Real”) or inferred trees from several methods (the others).



**Fig. 4.** Accuracy of some methods on the sim. cyanobacteria data set. The accuracy of TERA, TreeFix-DTL and JPRIME-DLTRS are depicted in Figure 2(a) of Scornavacca *et al.* (2015).

We see that the genome histories are close to the ones inferred from the real trees according to ecceTERA trees, ALE being equivalent in this view. Note that gene trees reconstructed from RAXML only do not yield a correct ancestral genome content. This result argues for the correction step, quickly achieved by ecceTERA, for every evolutionary study.

## 4.2 Cyanobacteria Data sets

The biological and simulated cyanobacteria data sets used here have been made public by Szöllősi *et al.* (2013) at <http://datadryad.org/resource/doi:10.5061/dryad.pv6df>. Their construction consisted in selecting 1099 gene families from 36 cyanobacteria species, related by a known dated species tree. These families were retrieved from HOGENOM (Penel *et al.*, 2009), and selected for their reasonable size and representativity. To obtain the biological data set, multiple-alignments on these families were computed with Muscle (Edgar, 2004).

To obtain the simulated data set, from each multiple-alignment of the real data set, a sample of 1000 trees was computed with PhyloBayes (Lartillot *et al.*, 2009), and an amalgamated tree was

reconstructed with ALE (Szöllősi *et al.*, 2013). This tree was used to simulate multiple-alignments of artificial sequences evolved along this tree under an LG model with a gamma distribution. This multiple-alignment is the input of our simulated data set. See (Szöllősi *et al.*, 2013) for more detail on how the data sets were generated.

*Tests on the simulated data set.* A tree was computed for each simulated multiple-alignment using PhyML (Guindon *et al.*, 2010), with an LG+ $\Gamma$ 4+I model and SH branch supports.

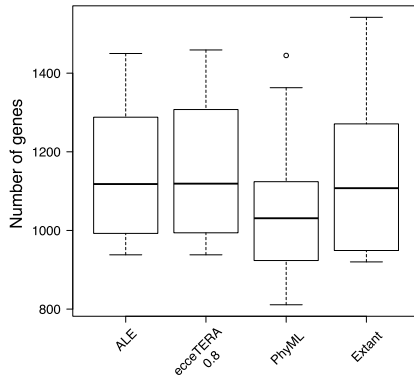
For this data set, the accuracy of TERA, ALE, TreeFix-DTL, MowgliNNI, JPRIME-DLTRS and PhyML were compared by Scornavacca *et al.* (2015, Figure 2(a)) (See Section 2.5 of the same paper for more details on the input/parameters used to generate the results), TERA and ALE giving the best results. In Figure 4, we compare these results with those of ecceTERA, again on unrooted gene trees and dated species tree, for three different thresholds of weakly supported edges (0.8, 0.7 and 0.6). We report the results of ALE and PhyML from Scornavacca *et al.* (2015), plus the results for MowgliNNI for the same thresholds used for ecceTERA. Both ecceTERA and Mowgli were given the “simulated” PhyML trees with SH branch supports. Finally, we report the accuracy of ALE when using as input 100 sample trees (ALE 100 in Figure 4) among the 10k trees provided, mimicking the information contained in a set of bootstrap trees.

Figure 4 shows that, for this data set, ecceTERA with a threshold of 0.8 achieves a slightly better accuracy than all other methods, while with a threshold of 0.7-0.6 the accuracy is comparable to that of ALE. Moreover, the accuracy of ecceTERA increases with the threshold for weak edges, while this is not the case for MowgliNNI. It is also worth noting that the accuracy of ALE decreases considerably when used on small samples of trees. These results are even more interesting when considering that ecceTERA is the fastest method of the bundle (see Table 1 and Figure 2(a) of (Scornavacca *et al.*, 2015)). Although ecceTERA has similar running times as TERA, it requires much less time to construct the input (as its input is the PhyML tree with SH branch supports). Thus, the ecceTERA strategy is the fastest (considering computation + input preparation time) among all compared strategies. Again, comparing the trees using the normalized triplet distance yielded similar results (see Figure 2 of the Appendix). Note that scoring tripartitions as described in Section 3.1 and the choice of the costs have impact on the accuracy: running ecceTERA with unitary costs for  $\mathbb{D}$ ,  $\mathbb{T}$ ,  $\mathbb{L}$  events yields to an average normalized R-F distance of 0.134 for a threshold of 0.8 for weakly supported edges (the average is 0.24 if the costs are respectively 2,3 and 1, see Figure 4); the average stays at 0.133 if the costs are 2,3 and 1 but all tripartitions are considered equiprobable, while it goes down to 0.151 for unitary costs and equiprobable tripartitions.

*Tests on the biological data set.* From each multiple alignment, a maximum-likelihood tree was computed with PhyML (Guindon *et al.*, 2010) with SH branch supports. These PhyML trees were corrected using ecceTERA with a threshold for weak edges equal to 0.8. The weight of amalgamation  $c_A$  was estimated, with starting value 1. Gene trees were considered as unrooted and the species tree as dated.

We measured the quality of the corrected trees compared to that of the maximum-likelihood trees in two ways. First, we compared the likelihoods according to the multiple-alignments. Of course, the PhyML trees always have a better likelihood because they are optimized with respect to this criterion. But it is interesting to note that for 80% of the trees, an Approximate Unbiased (AU) test performed with Consel (Shimodaira and Hasegawa, 2001) did not reject the ecceTERA tree. So, in a vast majority of the cases, the ecceTERA and PhyML trees are equivalent regarding their sequence likelihoods.

Second, we compared the two sets of trees with respect to their implications for the evolutionary dynamics of genomes: we counted the



**Fig. 5.** Number of genes for extant species ("Extant"), or ancestral species reconstructed with reconciled trees from ALE, ecceTERA and PhyML. Better trees yield more plausible genome histories.

number of genes present in ancestral species according to reconciled gene trees (again all gene trees were reconciled *a posteriori* with TERA, considering gene trees as rooted for ALE and ecceTERA, and unrooted for PhyML), and compared it with the number of genes present in extant species. The results are shown in Figure 5.

Genome histories are much more stable according to ecceTERA and, equivalently, ALE. According to PhyML trees, ancestral genomes were much smaller than extant genomes, which is not a plausible hypothesis, regarding the theoretical performances of sequence-based constructions, and regarding the same study on simulated genomes (Figure 5).

All results tend to show that the gene tree quality is comparable to that of the best available methods, ALE, TERA and TreeFix-DTL, while solving exactly the non binary gene tree species tree reconciliation, being faster and simpler to use.

## 5 Conclusions

Gene trees are a precious resource for biologists. They allow us to annotate genomes, to define species taxonomies, and to understand the evolution of traits, adaptation, and modes of genome evolution. They are also used to reconstruct ancestral genomes and understand the history of relations between organisms and their environment on a long time scale. Thus, reliable gene trees are crucial for many biological results (see for example Groussin *et al.* (2015)).

Standard tools constructing gene trees from multiple sequence alignments are widely used. Although species tree aware methods provide better quality gene trees, they have not been as popular. First because a species tree is not always available, and second because of the computational investment most methods require to output a gene tree.

We propose a method that can be easily used by biologists to quickly correct the output of a gene tree computed from a multiple sequence alignment, provided that branch supports and a species tree are available. The software is built on an FPT algorithm which is derived from recent advances in gene tree amalgamation principles. Its complexity is single exponential in the maximum degree of the input tree, which reduces to the maximal number of connected branches with low support. What a low support is depends on a threshold chosen by the user. Thus, a compromise between the extent of the correction and the computing time is easily achieved. On all of our data sets, on several dozens of species and several thousand of genes, we arrived quickly at a result that is always significantly better than methods based on multiple sequence alignments

only, and whose quality is equivalent to the computationally more intensive integrated methods.

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