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First vs second order magnetocaloric material for thermomagnetic energy conversion

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Abstract—We estimate the power and efficiency of a thermal energy harvesting thermodynamic Brayton cycle using a first and second order magnetocaloric materials as active substance. The thermodynamic cycle was computed using a simple thermal exchange model and an equation of state deduced from a phenomenological Landau model. For the first and second order materials, narrow and high frequency cycles are optimum and give similar performances. Considering technological issues hindering the increase of frequency, we introduced a more detailed approach where we take into account the time needed to switch the material between two heat reservoirs. We show that the first order material equation of state leads thermodynamic cycle shape keeping it closer to the optimum cycle. Conditions to improve the performance of second order materials are discussed. In addition, we infer key remarks for prototype design regarding the power density and efficiency reachable in different configurations.

Index Terms—magnetocaloric materials, thermal energy harvesting, thermomagnetic cycle, simulation.

The supply of waste heat represents a huge and freely available amount of energy that makes it a key target for energy conversion technologies, notwithstanding the small thermodynamic efficiency to be expected because of the limited working temperature difference. Energy harvesting systems from waste heat based on thermomagnetic generation (TMG) have been studied since the 1948 paper by Brillouin and Iskenderian [1]. The new generation of magnetocaloric materials (MCM) raised a renewed interest towards this technology [2]. Recently we published numerical simulations of isofield-isotemperature and adiabatic-isotemperature cycles using a finite-time thermodynamics approach [3] (i.e. where thermal exchange is taken into account in a non-quasistatic regime). This allowed to estimate the efficiency at maximum power (EMP) using the first and second order phase transition magnetocaloric materials as active substance. Our preliminaries results made possible the comparison with thermoelectric generators [4]–[6], showing a similar power density for temperature span below 10°C, but a much higher relative efficiency from 0.05 to 0.2 is attained in the case of thermomagnetic cycles. However, these cycles are still highly idealized as we assume a perfect control of their shapes based on field feedback. Indeed, the isotemperature transformations (i.e. a finite-time heat exchange where the temperature difference between the engine and the source is kept constant) used in [3] to work out best efficiency can be hardly achieved in an actual device that would more easily work on an isofield-adiabatic cycle (i.e. a Brayton cycle).

Here we will show how the constitutive relation (equation of state) of the material leads the actual shape of a finite-time thermodynamic cycle. Our main result is that in the first order MCM the isofield transformation stays closer to the

isotemperature one allowing a significant efficiency improvement with respect to the second order MCM. Using the method presented in [3], we study the potential benefit of the first order MCM in terms of power density and efficiency as compared to the second order MCM for a cycle with adiabatic and isofield processes. In other words, we study how the shape of the cycle resulting from the state function of the MCM affects the efficiency at maximum power of the system.

I. SYSTEM AND MATERIAL MODELING

Two approaches are commonly envisaged to harvest the magnetic energy produced by cycling of the active material around a temperature induced ferromagnetic-paramagnetic transition. The first one uses the magnetization change in time to drive electric current [7], [8], whereas the second one uses the mechanical work associated with the difference of magnetic force due to magnetization change [9], [10]. Because of design constraints, a thermodynamic cycle composed by two isofield and two adiabatic processes (Brayton cycle) is a common choice for systems of the latter class.

Here we compute the thermodynamic cycle following [3], namely using an equation of state deduced from a phenomenological Landau model with magnetoelastic coupling [12] (for a review of similar approaches see also [11]). This model was developed to describe the first order phase transition in the $\text{Mn}_{1.3}\text{Fe}_{0.65}\text{P}_{0.5}\text{Si}_{0.5}$ magnetocaloric compound. The equation of state is presented in a dimensionless form, and the scale parameters connecting the internal variables with observed temperature, field and magnetization are roughly fitted to the real material. As for the second order transition, we use the fact that the magnetic behavior of this thermodynamic system is affected by the Landau coefficient related to strain. By modifying this coefficient, we can change the order of temperature-induced phase transition. Therefore, we slightly modify this parameters to be at the limit where we obtain a continuous transition i.e. a second order transition. The obtained equation of state still may (or may not) correspond to a real material as, depending on the chemical composition, both first and second order transitions are observed in the Mn-Fe-P-Si system. In any case, this comparison is useful to emphasize the differences between sharp and smooth phase transitions. Because Landau model does not fit the total thermal capacity, a logarithmic term $C \ln(T)$ is added to the entropy to introduce a constant C (lattice contribution) in the thermal capacity [3]. Here we use C values similar to those encountered in most MCM ($3.9 \text{ J} \cdot \text{K}^{-1} \cdot \text{cm}^{-3}$).

Figure 1 and Figure 2 show two examples of thermodynamic Brayton cycles, calculated using the equation of state of the first order MCM, represented in the $T(S)$ (temperature-entropy) and $M(H)$ (magnetization-field) planes, respectively. In Figure 2,

during adiabatic magnetization (process 1), the cycle crosses the isotherms (thin lines) as the temperature of the MCM increases. Figure 3 shows an example of the second order MCM.

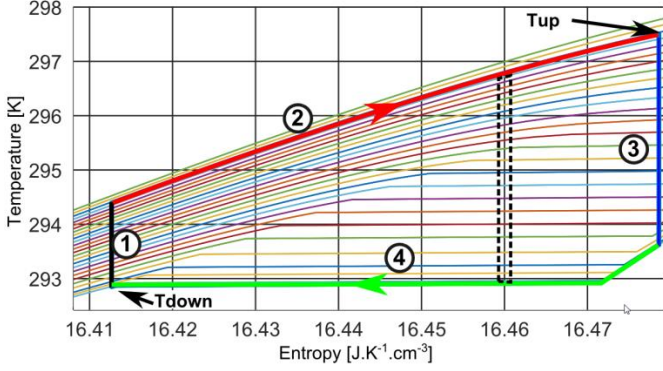


Figure 1. Two Brayton cycles on $T(S)$ diagram for the first order MCM with isofields in thin lines. Numbers from 1 to 4 indicate respectively the adiabatic magnetization, the isofield heat exchange with the hot reservoir, the adiabatic demagnetization, the isofield heat exchange with the cold reservoir.

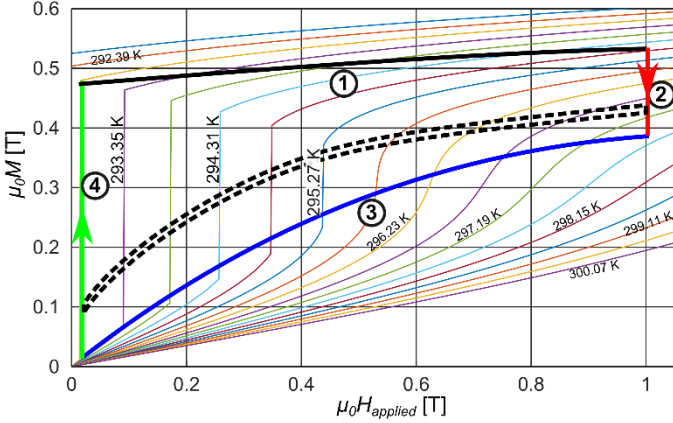


Figure 2. $M(H)$ cycle for a first order material. Thin lines represent isotherms from 291.91 K to 300.07 K with step of 0.48 K. Numbers from 1 to 4 have the same meaning as in Fig. 1. The dashed thick lines represent a loaded cycle as described in section IV.

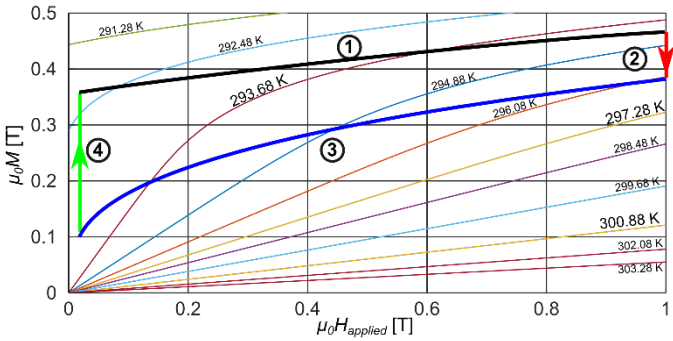


Figure 3. Cycle on $M(H)$ diagram for the second order MCM with isotherms from 291.28 K to 303.28 K with step of 1.2 K, numbers 1 to 4 have the same meaning as in Fig. 1.

The MCM exchanges heat with reservoirs at the temperature T_{res} , where $T_{res} = T_{hot}$ or $T_{res} = T_{cold}$ when it is in contact with the heat source or with the heat sink, respectively. The heat exchange model, used to mimic the finite-time heat exchange, is given by

$$\delta Q = [-k_{high}(T - T_{res})]dt \quad (1)$$

where the heat exchange coefficient k_{high} is chosen as $1 \text{ W} \cdot \text{cm}^{-3} \cdot \text{K}^{-1}$. It is estimated by considering a 1 mm thickness sheet of MCM separated from the reservoir by an air layer of $25 \mu\text{m}$ due to bad mechanical contact associated with surface roughness. The thermal conductance of a typical metallic MCM is much higher than the air gap conductance.

II. THERMODYNAMIC SIMULATIONS

Considering the MCM at thermodynamic equilibrium $\delta Q = Tds$ and the equation of state $s(T, H)$, integration of (1) gives the time of exchange $t_{exchange}$:

$$t_{exchange} = \int_{cycle} dt = \int_{cycle} \frac{Tds}{[-k_{high}(T - T_{res})]} \quad (2)$$

In the first approximation we assume $t_{period} = t_{exchange}$, namely the time $t_{switching}$ spent along the adiabatic processes is assumed to be negligible. For example, if the temperature was fixed during the isofield process, then the time of exchange would be proportional to the entropy span. Therefore, the size of the cycle is correlated to the time of exchange, i.e. wider cycle has greater exchange time (dashed lines in Figure 2 show a tiny cycle associated with small $t_{exchange}$). Given the power density, the maximum relative efficiency η_{rel} , with respect to the Carnot efficient η_{Carnot} , is achieved by minimizing the entropy production s_i as shown in the following equation:

$$\eta_{rel} = \frac{\eta}{\eta_{Carnot}} = 1 - \frac{s_i T_{cold}}{\eta_{Carnot} Q_{hot}} \quad (3)$$

where Q_{hot} is the heat exchanged with the hot reservoir. Here we take into account only the entropy production associated with the finite-time heat exchange (i.e. the hysteresis and kinetics associated with the magnetic transition are neglected, a state of things often referred to as endoreversibility), which defines the degree of departures from thermal equilibrium. We have:

$$\delta s_i(T, H) = \left(\frac{1}{T} - \frac{1}{T_{res}(H)} \right) \delta Q(T, H) \quad (4)$$

Using the heat exchange model (1), the entropy produced is given by the following expression:

$$s_i = k_{high} \int_{t_{period}} \frac{(T_{res}(t) - T(t))^2}{T_{res}(t)T(t)} dt \quad (5)$$

therefore the efficiency and power are deduced from (3) and

$$P = \eta_{rel} \eta_{Carnot} Q_{hot} / t_{period} \quad (6)$$

It can be shown using (5) that s_i is minimum when the heat exchange takes place at a constant temperature difference (HECTD). This means that efficiency is maximum when the difference between the temperature $T(t)$ of the MCM as a function of time t and the temperature of the reservoirs, T_{hot} or T_{cold} , respectively for the hot and cold reservoirs, are constant during the heat exchange process. That is why we use the term isotemperature rather than isotherm to name this process.

III. PARAMETERS AFFECTING THE POWER DENSITY AND THE EFFICIENCY

A sound comparison between materials with the first and second order transitions needs a careful definition of the relevant parameters affecting the efficiency and the power density. We first define the maximum power conditions and eventually work out the efficiency at maximum power (EMP). In section IV we will argue that, when the period $t_{exchange}$ tends to zero, all the cycles approach the isothermality and isofield ones, whatever the order of the transition. For this class of cycles we worked out an analytical expression in [3], allowing easy determination of the relevant parameters. The power will be considered negative using standard thermodynamic convention. Maximum power is achieved when thermodynamic cycles are centered between the temperatures of the reservoirs to ensure the same driving temperature difference $T - T_{res}$ during heat exchange processes. Using the results presented in [3], we write:

$$\eta_{rel} = \frac{\Delta T_{adia}}{\Delta T_{res}} \quad (7)$$

$$P(\eta_{rel}) = -\frac{\Delta T_{res}^2 k_{high}}{4T_{hot}} \eta_{rel}(1 - \eta_{rel}) \quad (8)$$

Here $\Delta T_{adia}(T, H_f, H_i)$, where H_f and H_i are the final and initial applied fields, depends on the equation of state [13] and $\Delta T_{res} = T_{hot} - T_{cold}$. Indeed, the maximum power is achieved when the temperature span of the reservoir is twice the adiabatic temperature change (i.e. $\Delta T_{adia} = \Delta T_{res}/2$). As long as the field available is strong enough to reach this condition, the power increases proportionally to ΔT_{res}^2 with

$$P = -\frac{\Delta T_{res}^2 k_{high}}{16T_{hot}} \quad (9)$$

keeping the relative efficiency around 50 %. This is a key technological issue inciting researches towards materials showing high ΔT_{adia} under low applied fields as in an actual device fields higher than 1 T can be hardly achieved. When the maximum field is reached, the system does not work anymore with the best cycle, i.e. with the maximum power cycle among all. The system works at its maximum power for its maximum ΔT_{adia} and the power increases proportionally to ΔT_{res} with

$$P = -\frac{(\Delta T_{res} - \Delta T_{adia})\Delta T_{adia}k_{high}}{4T_{hot}} \quad (10)$$

In addition, the EMP decreases as indicated in (7). These expressions are useful tools to estimate the harvested power. In the following, we numerically find the maximum power cycle keeping constant ΔT_{adia} and ΔT_{res} . But we should be aware that for a given isothermality, isofield cycle, an increase of k_{high} will increase the performance (power density and/or efficiency) whereas an increase of temperature span ΔT_{res} will increase the power density but also decrease the efficiency unless accompanied by equal ΔT_{adia} increase. In our simulations, the applied field for the first and second order MCM is chosen in order to have the same maximum adiabatic temperature change ΔT_{adia} .

IV. CYCLE SHAPE FOR THE FIRST AND SECOND ORDER MATERIALS

In Figure 4 we show the calculated cycles with $T_{hot} = 298 K$, $T_{cold} = 291 K$. Full line cycles, corresponding to $t_{exchange} = 10 s$ (the wide cycles in the figure) give for first order $P_{mag} = -9.2 mW.cm^{-3}$ and $\eta_{rel} = 0.41$, and for second order $P_{mag} = -8.2 mW.cm^{-3}$ and $\eta_{rel} = 0.41$. Tiny cycles, corresponding to $t_{exchange} = 0.1 s$ (dashed line in the figure), give the same results for the first and second order MCM, namely $P_{mag} = -10 mW.cm^{-3}$, $\eta_{rel} = 0.45$. Figure 4 shows that the first order MCM in isofield processes keeps closer to a HECTD (i.e. closer to the optimum cycle) than the second order MCM. The difference is apparent when comparing the low temperature isofield line in Figure 4, the first order material (red line, right) shows a horizontal line (a perfect isothermality process) whereas the second order one (black line, left) shows a steeper slope. Results for the same $t_{exchange}$ show the same efficiency but not the same power density. Therefore, considering cycles with the same power density, the efficiency will be lower for the second order MCM as expected.

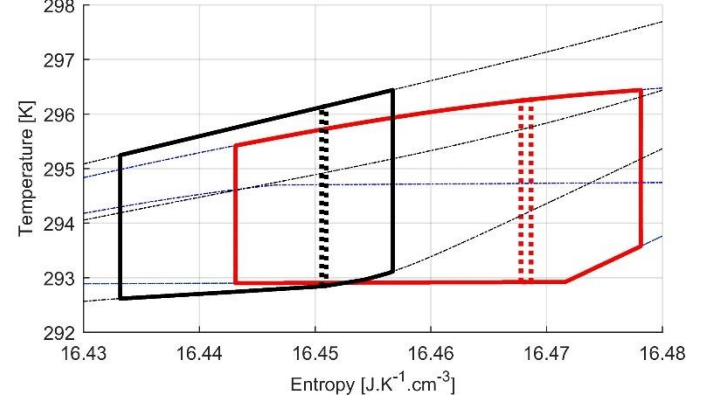


Figure 4. Brayton cycles on $T(S)$ diagram for the second order MCM (black) on the left and the first order MCM (red) on the right for large (solid line) and small cycles (dotted line). Thin lines represent three isofields in black for the second order MCM and in blue for the first order MCM.

Nevertheless, it is worth noting that both second and first order MCM can approach HECTD by drastically reducing the entropy span of the isofield process, as in the dashed line cycles in Figure 4. This means EMP for the first and second order materials will be very similar when working on tiny cycles at a rather high frequency. We shall use the term *low loaded cycle* to describe tiny cycles close to the HECTD. Indeed, only for a given heat exchange coefficient and temperatures of the reservoirs, low loaded cycles correspond to higher frequency than high loaded cycles.

V. MAXIMUM POWER CYCLE FOR DIFFERENT EXCHANGE TIMES

Low loaded cycles deal with small amount of energy including heat exchanged, that is why exchange time (2) is also small. It is not trivial to estimate the power density, especially as the cycles are not always close to isothermality processes. An algorithm, based on simulations at constant reservoir temperatures, explores all possible cycles, i.e. all possible T_{up} and T_{down} , the temperatures of the ascending and descending adiabatics processes (as shown in Figure 1), to find the

maximum power cycle for different $t_{exchange}$. Results are shown in Figure 5 for the first and second order MCM. The choice of $t_{exchange}$ as a variable to study the power density will be discussed in the next section. In Figure 5 a slight increase of the power density for the first order MCM for longer periods is apparent. Cycles corresponding to exchange time of 0.1 s and 10 s are shown in Figure 4.

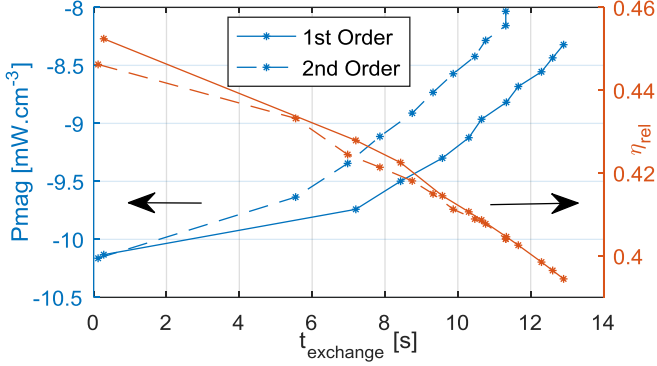


Figure 5. Maximum magnetic power and its relative efficiency for different exchange times for the first order in solid line ($H_{applied} = 0.67 T, \max(\Delta T_{adia}) = 3.4 K$) and for the second order in dashed line ($H_{applied} = 1 T, \max(\Delta T_{adia}) = 3.4 K$) with $\Delta T_{res} = 6.8 K, T_{hot} = 298 K$ and $T_{cold} = 291 K$.

As we argued in the previous section, both first and second order MCM show maximum power density and efficiency close to the optimum cycle for exchange time that tends to zero, i.e. for a low loaded cycles.

To emphasize the difference between the second and first order transitions, the adiabatic temperature change from now on is changed from 3 to 1.5 K, accordingly ΔT_{res} is changed from 6.8 to 3.7 K in order to keep in same configuration. Power density and efficiency for this case are shown in Figure 6

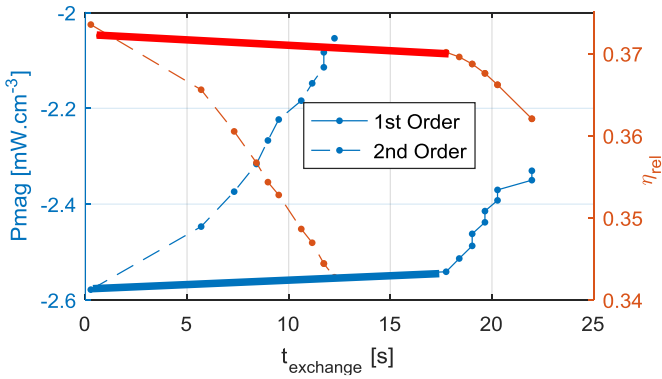


Figure 6. Maximum magnetic power and its relative efficiency for different time periods for the first order in solid line ($H_{applied} = 0.28 T, \max(\Delta T_{adia}) = 1.5 K$) and for the second order in dashed line ($H_{applied} = 0.33 T, \max(\Delta T_{adia}) = 1.5 K$) with $\Delta T_{res} = 3.75 K, T_{hot} = 295.53 K$ and $T_{cold} = 291.8 K$.

A careful analysis of the results reveals some subtle details. The relative efficiency does not reach 0.5 because the system does not work exactly at $2\Delta T_{adia} = \Delta T_{res}$, using (7) the relative efficiency is estimated around 0.4. For the first order MCM, where isofield lines are horizontal in the TS diagram, the power density and the efficiency are nearly constant whatever the exchange time (highlighted line in Figure 6). Because $T(H)$ isofield lines are not perfectly horizontal due to the lattice

thermal capacity, the power and relative efficiency are slightly decreasing (highlighted line in Figure 6). Eventually, the relative efficiency does not exactly follow (7), because of not ideal isotherm process.

VI. SWITCHING TIME

In a real device the period t_{period} of the cycle is the sum of the time spent to exchange heat $t_{exchange}$ (phases 2 and 4 in Figure 1) and the time spent along the two adiabatic branches (phases 1 and 3 in Figure 1), we refer to the latter as the switching time $t_{switching}$. The switching time has been hitherto neglected assuming $t_{switching} \ll t_{exchange}$ so that $t_{exchange} \sim t_{period}$. Now we would like to briefly discuss the case where the switching time cannot be neglected.

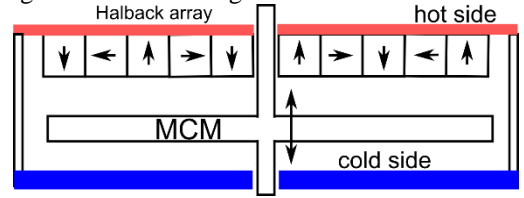


Figure 7. Example of thermomagnetic generator converting magnetization change to mechanical power (motion-force).

In Figure 7 we show a typical device to harvest the energy due to the difference of magnetic force during displacement between the hot and cold reservoirs [9]. If we assume $t_{switching} \sim 0$, the power transfer through the mechanical force and motion is infinite because the MCM passes between from one magnetic state to another in zero time, which is not physically possible. A finite switching time is needed to properly model the actual harvesting process. Therefore, we write $t_{period} = t_{exchange} + t_{switching}$. The power density being the area of the cycle divided by the period

$$P = \frac{1}{t_{period}} \int_{Cycle} T dS \quad (11)$$

for a fixed cycle, the power density depends only on t_{period} . Because in the previous part we considered $t_{period} = t_{exchange}$, we can deduce the power as a function of switching time by replacing the period $t_{exchange}$ with $t_{exchange} + t_{switching}$. Therefore, the previous power density has to be multiplied by the switching factor

$$c_{switching} = \frac{t_{exchange}}{t_{exchange} + t_{switching}} \quad (12)$$

Taking into account the switching time defines an upper bound to the maximum power that becomes relevant in the case of low loaded cycles where $t_{exchange}$ is vanishing and therefore $t_{switching}$ cannot be neglected.

Thin solid lines in Figure 8 show the power density as a function of $t_{switching}$, normalized to its low loaded cycle value, calculated for different fixed periods (i.e. fixed $t_{exchange}$). It is worth noting that, in this case, normalizing to the low loaded cycle power makes the first and second order lines collapse on the same curve. In the same figure we show the maximum normalized power density as a function of the switching time (dashed lines). In this case, our algorithm selects the maximum power cycle given $t_{switching}$ (dashed line in Figure 8) by

changing the exchange time; namely, each point on the dashed lines corresponds to a cycle with different period using power maximization as a constraint. The set of cycles found for different switching times considered, limits the decrease of the power density as shown by dashed line in Figure 8.

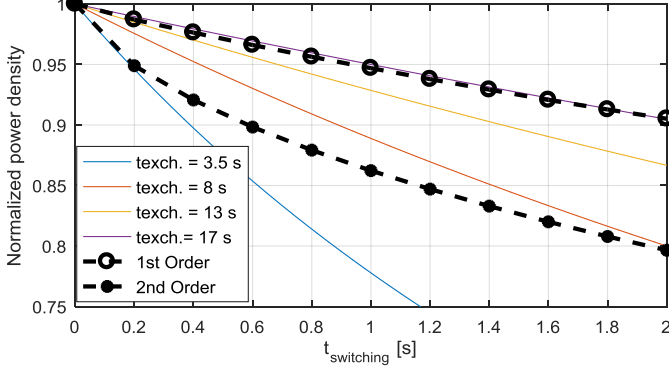


Figure 8. Effect of the switching time on the power density normalized with respect to the low loaded cycle, with $\Delta T_{adia} = 1.5 K$. Dashed lines are the maximum power cycle for different $t_{switching}$. Solid lines represent the normalized power density for a fixed $t_{exchange}$.

The power maximization algorithm tends to compensate the switching time decrease by selecting cycles with larger $t_{exchange}$ (i.e. larger periods, as shown in Figure 9). However, as discussed in the previous sections, larger $t_{exchange}$ is getting the isofield transformations away from the isotherm curves drastically reducing the cycle relative efficiency for the second order MCM.

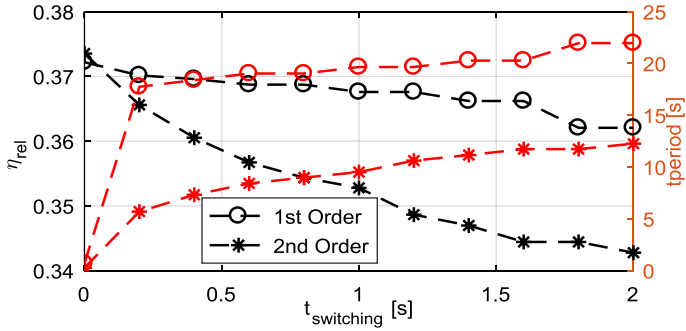


Figure 9 Relative efficiency (black) and period (red) of the maximum power cycle for different $t_{switching}$ with $\Delta T_{adia} = 1.5 K$ for the first order (circles) and for the second order (asterisks).

In Figure 10, maximum power cycles for $t_{switch} \sim 0$ and 0.8 s show that the first order cycles are closer to HECTD compared to the second order ones when t_{switch} equals 0.8 s. This is a key point to compare the first and second order MCM performances. First order materials can increase the $t_{exchange}$ without reducing significantly the efficiency of the cycle, because they keep closer to HECTD (Figure 10). As shown in Figure 8 and Figure 9, EMP and power density of the first order MCM are less sensitive to the effect of increasing $t_{switching}$.

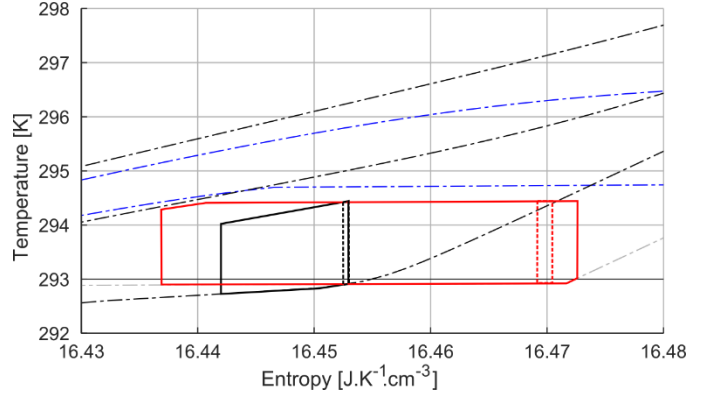


Figure 10. Maximum power Brayton cycles for $t_{switch} \sim 0$ i.e. small cycles (dotted line) and $t_{switch} = 0.8 s$ i.e. large cycles (solid line) on $T(S)$ diagram for the second order MCM (black) around $16.45 J.K^{-1}cm^{-3}$ and the first order MCM (red) around $16.47 J.K^{-1}cm^{-3}$. Thin lines represent three isofields in black for second order and in blue for first order.

VII. CONCLUSION

This study evaluates the benefit of using MCM with high ΔT_{adia} and systems with high heat exchange coefficient k_{high} for thermomagnetic energy conversion. Our simulations reveal that low loaded cycles are beneficial in terms of efficiency and power density but involve an increase of the operating frequency. At low frequency, the time taken along the adiabatic processes can be neglected. Because of the frequency increase and considering technical constraints, the model needs to take into account the time to switch between the reservoirs, called the switching time.

The first order MCM shows its robustness to the introduction of the switching time as compared to the second order MCM in terms of power and relative efficiency. An increase of the heat exchange coefficient k_{high} paves the way to potentially much higher power densities, due to a decrease of $t_{exchange}$. However, in this case, the reduction of the switching time becomes a key technological issue.

In section V we did show that, when the switching time can be neglected, the first and second order MCM may show similar performances only in the case of low loaded cycles when $t_{exchange}$ becomes small. However, in section VI we argued that in low loaded cycle case $t_{switching}$ can hardly be neglected and, also in this case, the power density at maximum efficiency of the second order materials is drastically reduced, with respect to the first order ones, when switching time is relevant.

However, high frequency excitations will very possibly increase the role of transition kinetics (neglected in our approach) and tiny thermodynamic cycles will be more affected by hysteresis. Both effects have been neglected in our discussion and can be relevant in the case of the first order MCM.

Small period cycles are expected to be achievable mostly in micro-systems where a fast heat exchange and a fast switching are expected. We can conclude that, while the first order materials are definitely better suited for bulk applications, further investigations must be devoted to the case of high-frequency micro-systems, taking into account the possible shortcomings of the first order materials associated with the role of non-equilibrium phenomena in the phase transitions.

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