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Nonlinear optical response of low loss silicon germanium waveguides in the mid-infrared

L. Carletti,^{1,*} P. Ma,² Y. Yu,² B. Luther-Davies,² D. Hudson,³ C. Monat,¹ R. Orobtchouk,¹ S. Madden,² D. J. Moss,⁴ M. Brun,⁵ S. Ortiz,⁵ P. Labeye,⁵ S. Nicoletti,⁵ and C. Grillet¹

¹University of Lyon, Institut des Nanotechnologies de Lyon, Ecole Centrale de Lyon, 36 Avenue Guy de Collongue, 69134 Ecully, France

²CUDOS, Laser Physics Centre, Australian National University, Canberra, ACT 0100, Australia

³CUDOS, School of Physics, University of Sydney, NSW 2006, Australia

⁴School of Electrical and Computer Engineering, RMIT University, Melbourne, Victoria 3001, Australia

⁵CEA-Leti MINATEC Campus, 17 rue des Martyrs 38054 GRENOBLE Cedex 9, France

⁸luca.carletti@ec-lyon.fr

Abstract: We have investigated the nonlinear optical response of low loss $Si_{0.6}Ge_{0.4}$ / Si waveguides in the mid-infrared wavelength range from 3.25-4.75µm using picosecond optical pulses. We observed and measured the three and four-photon absorption coefficients as well as the Kerr nonlinear refractive index. The dynamics of the spectral broadening suggests that, in addition to multiphoton absorption, the corresponding higher order nonlinear refractive phenomena also needs to be included when high optical pulse intensities are used at mid-infrared wavelengths in this material.

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References and links

- 1. B. Jalali, "Nonlinear optics in the mid-infrared," Nat. Photonics 4(8), 506–508 (2010).
- 2. R. Soref, "Mid-infrared photonics in silicon and germanium," Nat. Photonics 4(8), 495-497 (2010).
- J. Leuthold, C. Koos, and W. Freude, "Nonlinear silicon photonics," Nat. Photonics 4(8), 535–544 (2010).
 C. Monat, C. Grillet, M. Collins, A. Clark, J. Schroeder, C. Xiong, J. Li, L. O'Faolain, T. F. Krauss, B. J.
- C. Monat, C. Grillet, M. Collins, A. Clark, J. Schroeder, C. Xiong, J. Li, L. O'Faolain, T. F. Krauss, B. J. Eggleton, and D. J. Moss, "Integrated optical auto-correlator based on third-harmonic generation in a silicon photonic crystal waveguide," Nat. Commun. 5, 3246 (2014).
 B. Corcoran, C. Monat, C. Grillet, D. J. Moss, B. J. Eggleton, T. P. White, L. O. Faolain, and T. F. Krauss,
- B. Corcoran, C. Monat, C. Grillet, D. J. Moss, B. J. Eggleton, T. P. White, L. O. Faolain, and T. F. Krauss, "Green light emission in silicon through slow-light enhanced third-harmonic generation in photonic-crystal waveguides," Nat. Photonics 3(4), 206–210 (2009).
- C. Grillet, L. Carletti, C. Monat, P. Grosse, B. Ben Bakir, S. Menezo, J. M. Fedeli, and D. J. Moss, "Amorphous silicon nanowires combining high nonlinearity, FOM and optical stability," Opt. Express 20(20), 22609–22615 (2012).
- X. Liu, R. M. Osgood, Jr., Y. A. Vlasov, and W. M. J. Green, "Mid-infrared optical parametric amplifier using silicon nanophotonic waveguides," Nat. Photonics 4(8), 557–560 (2010).
- 8. G. Z. Mashanovich, M. M. Milošević, M. Nedeljkovic, N. Owens, B. Xiong, E. J. Teo, and Y. Hu, "Low loss silicon waveguides for the mid-infrared," Opt. Express 19(8), 7112–7119 (2011).
- 9. P. Y. Yang, S. Stankovic, J. Crnjanski, E. J. Teo, D. Thomson, A. Bettiol, M. B. H. Breese, W. Headley, C. Giusca, G. T. Reed, and G. Z. Mashanovich, "Silicon photonic waveguides for mid- and long-wave infrared region," J. Mater. Sci. Mater. Electron. 20(S1), 159–163 (2009).
- B. Kuyken, X. Liu, R. M. Osgood, Jr., R. Baets, G. Roelkens, and W. M. J. Green, "Mid-infrared to telecomband supercontinuum generation in highly nonlinear silicon-on-insulator wire waveguides," Opt. Express 19(21), 20172–20181 (2011).
- R. Shankar, I. Bulu, and M. Lončar, "Integrated high-quality factor silicon-on-sapphire ring resonators for the mid-infrared," Appl. Phys. Lett. 102(5), 051108 (2013).
- 12. X. Gai, Y. Yu, B. Kuyken, P. Ma, S. J. Madden, J. Van Campenhout, P. Verheyen, and R. Baets, "Nonlinear absorption and refraction in crystalline silicon in the mid-infrared," Laser Photonics Rev. 7, 1–11 (2013).
- M. Muneeb, X. Chen, P. Verheyen, G. Lepage, S. Pathak, E. Ryckeboer, A. Malik, B. Kuyken, M. Nedeljkovic, J. Van Campenhout, G. Z. Mashanovich, and G. Roelkens, "Demonstration of Silicon-on-insulator mid-infrared spectrometers operating at 3.8 μm," Opt. Express 21(10), 11659–11669 (2013).
- C. Grillet, P. Ma, B. Luther-Davies, D. Hudson, C. Monat, S. Madden, D. J. Moss, M. Brun, P. Labeye, S. Ortiz, and S. Nicoletti, "Low loss SiGe waveguides in the MID-IR," in 2013 Conference on Lasers and Electro-Optics International Quantum Electronics Conference (Optical Society of America, 2013), paper CK 2 6.

- 15. M. Brun, P. Labeye, G. Grand, J. M. Hartmann, F. Boulila, M. Carras, and S. Nicoletti, "Low loss SiGe graded index waveguides for mid-IR applications," Opt. Express 22(1), 508–518 (2014).
- N. K. Hon, R. Soref, and B. Jalali, "The third-order nonlinear optical coefficients of Si, Ge, and Si1-xGex in the midwave and longwave infrared," J. Appl. Phys. 110(1), 011301 (2011).
- 17. K. Hammani, M. A. Ettabib, A. Bogris, A. Kapsalis, D. Syvridis, M. Brun, P. Labeye, S. Nicoletti, D. J. Richardson, and P. Petropoulos, "Optical properties of silicon germanium waveguides at telecommunication wavelengths," Opt. Express 21(14), 16690–16701 (2013).
- 18. K. Hammani, M. A. Ettabib, A. Bogris, A. Kapsalis, D. Syvridis, M. Brun, P. Labeye, S. Nicoletti, and P. Petropoulos, "Towards nonlinear conversion from mid- to near-infrared wavelengths using Silicon Germanium waveguides," Opt. Express 22(8), 9667–9674 (2014).
- P. Ma, D. Y. Choi, Y. Yu, X. Gai, Z. Yang, S. Debbarma, S. Madden, and B. Luther-Davies, "Low-loss chalcogenide waveguides for chemical sensing in the mid-infrared," Opt. Express 21(24), 29927–29937 (2013).
- 20. G. P. Agrawal, Nonlinear Fiber Optics (Academic, 2001).
- L. Yin and G. P. Agrawal, "Impact of two-photon absorption on self-phase modulation in silicon waveguides," Opt. Lett. 32(14), 2031–2033 (2007).
- C. Monat, B. Corcoran, M. Ebnali-Heidari, C. Grillet, B. J. Eggleton, T. P. White, L. O'Faolain, and T. F. Krauss, "Slow light enhancement of nonlinear effects in silicon engineered photonic crystal waveguides," Opt. Express 17(4), 2944–2953 (2009).
- B. Corcoran, C. Monat, D. Pudo, B. J. Eggleton, T. F. Krauss, D. J. Moss, L. O'Faolain, M. Pelusi, and T. P. White, "Nonlinear loss dynamics in a silicon slow-light photonic crystal waveguide," Opt. Lett. 35(7), 1073–1075 (2010).
- C. Husko, S. Combrié, Q. V. Tran, F. Raineri, C. W. Wong, and A. De Rossi, "Non-trivial scaling of self-phase modulation and three-photon absorption in III-V photonic crystal waveguides," Opt. Express 17(25), 22442– 22451 (2009).
- B. S. Wherrett, "Scaling rules for multiphoton interband absorption in semiconductors," J. Opt. Soc. Am. B 1(1), 67–72 (1984).
- T. Wang, N. Venkatram, J. Gosciniak, Y. Cui, G. Qian, W. Ji, and D. T. H. Tan, "Multi-photon absorption and third-order nonlinearity in silicon at mid-infrared wavelengths," Opt. Express 21(26), 32192–32198 (2013).
- D. Seo, J. M. Gregory, L. C. Feldman, N. H. Tolk, and P. I. Cohen, "Multiphoton absorption in germanium using pulsed infrared free-electron laser radiation," Phys. Rev. B 83(19), 195203 (2011).

1. Introduction

There is a strong interest in expanding the spectral window of operation of group IV material platforms for integrated photonics in the mid-infrared (mid-IR - at wavelengths between 2 µm and 20 µm) for a vast range of applications relating directly to our everyday life, such as chemical and biological sensing, active imaging, tissue ablation, secure free-space communication, multi-wavelength light sources, and many others [1,2]. Many molecules exhibit strong fundamental rotational-vibrational absorption lines in the mid-IR, which has motivated the development of integrated molecular sensing platforms in this wavelength range with unprecedented sensitivity. However, the lack of low-cost and easily deployable photonic technologies that operate in this wavelength range constitute a major roadblock to achieving these devices. Sensing applications require compact and low-cost optical devices and, most importantly, optical sources that are widely tuneable or yield broadband emission to access the whole mid-IR band. There have been a number of approaches, particularly within the silicon photonics community [3–6], to adapt technologies developed for the near-IR to the mid-IR for both linear [1,2,7–11] and nonlinear photonic devices. For nonlinear devices, the issue of two-photon absorption (TPA) that limits device performance in the near-infrared region, vanishes at longer wavelengths (>2.2 µm) [1,3], and this has motivated some impressive nonlinear optical demonstrations in silicon on insulator (SOI) waveguides near 2 μm [7,10], as well as in silicon on sapphire (SOS) [11]. However, it has recently been shown that, although TPA vanishes beyond 2 µm, higher order (3 and 4) photon absorption and the ensuing free carrier absorption (FCA) in Si remain far from negligible [12]. Therefore, a careful design is needed for applications requiring a strong nonlinear response, such as for supercontinuum generation, in this wavelength range.

The SOI platform has attracted significant interest for on-chip integrated waveguides that can operate in the mid-IR since the CMOS compatible fabrication process offers the same advantages as for telecom band devices. However, the dramatic increase in absorption of the silica cladding layer at wavelengths longer than 3.5 µm significantly limits the performance of devices in this material platform [8,13]. It is, therefore, crucial to explore other material platforms, and in this context SiGe alloys on Si are an attractive alternative platform to SOI.

The transparency window of this material platform expands more deeply in the mid-IR as compared to other CMOS compatible platforms that have already been proposed for operation in this wavelength region such as SOI, SOS or silicon nitride on silicon [2]. The much lower propagation losses of SiGe/Si waveguides compared to SOI in the mid-IR have enabled some very promising results [14,15]. Furthermore, the optical nonlinear response of SiGe alloys is predicted to be higher than Si [16], although this has yet to be exploited except for only one report in the near-IR [17] and another one out to a wavelength of 2.6 μ m [18]. A recent study [17] has shown that the nonlinear parameter (γ) of SiGe waveguides may indeed exceed 30 W⁻¹m⁻¹, based on results obtained in a 0.8 x 1.4 μ m² cross-section waveguide at telecom wavelengths.

Here, we report the first experimental measurements of the nonlinear optical response of SiGe/Si waveguides in the mid-IR obtained by measuring self-phase modulation (SPM) and the nonlinear transmission of these waveguides at high optical intensities (up to 45 GW/cm²) with picosecond optical pulses centred at wavelengths between 3 μ m and 5 μ m. Our results show that not only can we achieve significant spectral broadening in a region where multiphoton absorption exists, but that the dynamics are such that there is strong evidence for a significant presence of higher order nonlinear refraction beyond the Kerr effect.

2. Experiment

The devices (Fig. 1) consisted of ridge waveguides with a Si_{0.6}Ge_{0.4} core encapsulated in a Si cladding, grown on a silicon substrate. Mode confinement was obtained by exploiting the refractive index difference between Si and the SiGe alloy of about 0.17 in the wavelength range used for the experiments. Fabrication was performed onto a 200 mm CMOS pilot line at CEA-LETI. A 1.4 μm Si_{0.6}Ge_{0.4} layer was deposited by reduced pressure-CVD (RP-CVD) directly on a 200 mm Si wafer. A conventional deep UV (193nm) stepper mask aligner based photolithography, together with reactive ion etching techniques were used to define the core of the SiGe waveguides. The ridges were encapsulated with a 12 μm thick Si cladding layer using the same RP-CVD technique. More detail about the fabrication procedure can be found in [17], where it is pointed out that epitaxial growth allows for the realization of low-loss fully crystalline structures, while preserving IC (CMOS) processing compatibility. SEM pictures of a waveguide before encapsulation and of the device cross-section after encapsulation (inset) are shown in Fig. 1(a).

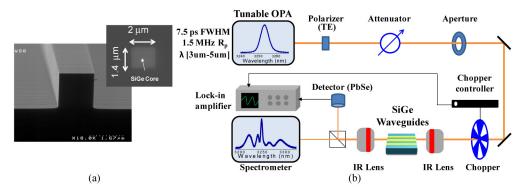


Fig. 1. (a) Scanning Electron Microscopy (SEM) image of a SiGe waveguide before encapsulation. A cross section of a SiGe waveguide after encapsulation is shown in the inset. (b) Schematic view of the experimental setup.

Waveguides with widths of 2 μm and 1.9 μm were fabricated with the goal of characterizing the nonlinear response of $Si_{0.6}Ge_{0.4}$. The waveguide dispersion was not engineered, and so, by considering the material dispersion of Si [3] and $Si_{0.6}Ge_{0.4}$ (measured at CEA-LETI), the estimated β_2 value associated with the GVD is normal and larger than + 1 ps²/m over the wavelength range probed experimentally here. Accordingly, the dispersion

length varies from 4.5 m at 4.75 μ m up to 11.3 m at 3.25 μ m, which is much longer than any waveguide (between 1 cm and 8 cm long) used for the experiments.

The experimental setup is shown in Fig. 1(b). We performed optical transmission measurements between 3.2 μm and 4.75 μm using a tunable optical parametric amplifier (OPA) that emitted transform limited Gaussian pulses with a full-width at half maximum (FWHM) duration of about 7.5 ps at a 1.5 MHz repetition rate. The input light was TE polarized and coupled from free-space in and out of the waveguide using molded chalcogenide lenses. The transmitted power was measured using a PbSe detector. A chopper and lock-in amplifier were used to discriminate against the thermal background from the environment [19]. To measure the transmitted spectrum a Newport Cornerstone 260 1/4m monochromator with a 1501/mm grating was used. The average powers derived by integrating the spectral power density recorded with the spectrometer over the spectral window of interest were compared with the powers measured with the photodetector used in combination with the lock-in amplifier. The good agreement found between the two signals at all powers indicates the negligible contribution of the environmental noise (i.e. between subsequent pulses) to the measurements and the reliability of the results.

3. Linear measurement results

The propagation losses were estimated from cut-back measurements on waveguides with different lengths between 1 to 8 cm and using an average input power of less than 1 mW (i.e. coupled peak intensity between 1 GW/cm² and 3 GW/cm²) in order to avoid any nonlinear effects. The results are shown in Fig. 2. From the cut-back measurements we were able to estimate the total coupling loss to be about 7 dB (i.e. 3.5 dB per facet), fairly independent of wavelength over the range studied. The measured linear loss decreased monotonically for increasing wavelengths down to 0.5 dB/cm at 4.75 μ m, which, to our knowledge, is the lowest propagation loss that has been measured so far for strip waveguides fabricated using group IV materials platforms in the mid-IR. In the inset of Fig. 2, the propagation loss of a waveguide with a cross section 1.4 x 1.9 μ m² was measured and the results were similar to the ones obtained for the 1.4 x 2 μ m² waveguide, indicating a good reproducibility of the fabrication process. The scattering loss for the 1.4 x 1.9 μ m² was calculated numerically and is shown along with the experimental results in the inset of Fig. 2.

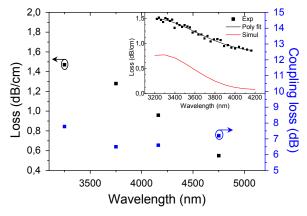


Fig. 2. Propagation loss and coupling loss as a function of wavelength for a waveguide with a cross section of 1.4 x 2 μ m². In the inset the propagation loss of a waveguide with a 1.4 x 1.9 μ m² cross section is shown along with simulation results.

The dependency of the propagation loss as a function of the wavelength is best reproduced by the numerical calculations when using a coherence length of 50 nm and an RMS roughness value of 4 nm, which is in agreement with the RMS value derived from TEM image analysis of the SiGe waveguides. However, no scattered light from the waveguides was observable

using a mid-infrared (InSb) camera, hence the difference in the losses might be in part due to absorption from defects states in the $Si_{0.6}Ge_{0.4}$.

4. Nonlinear measurement results

The nonlinear optical response of the SiGe was analyzed by performing systematic transmission and SPM measurements at increasing peak powers on a 8cm long, 1.4 x 2 μ m² cross-section waveguide using optical pulses centered at four different wavelengths (3250 nm, 3750 nm, 4162 nm, and 4750 nm). The spectra measured at the output of the waveguide with the scanning monochromator are shown in Figs. 3(a)-3(d) for increasing powers. It can be seen that as the peak coupled intensity increased, more and more side lobes appeared, which is characteristic of SPM. In Fig. 3(e), the experimental spectral broadening calculated from the spectra [20], was found to be a sub-linear function of the coupled peak intensity, which indicated the presence of nonlinear losses [20]. Furthermore, as the coupled peak intensity increased, the spectra in Figs. 3(a)-3(d) became asymmetrical and the mean wavelength, calculated in Fig. 3(f), was slightly blue shifted with respect to that at low power. This was also observed in Si waveguides using picosecond pulses in the near-infrared where it was attributed to free-carriers generated by two-photon absorption [21,22].

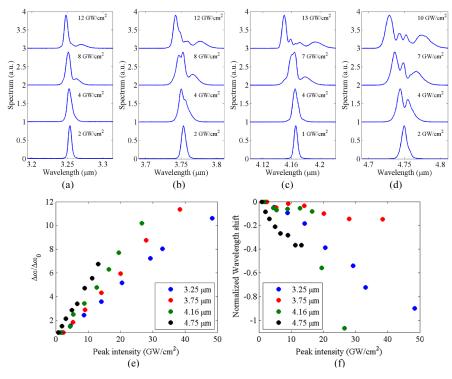


Fig. 3. (a-d) Normalized transmitted spectrum as a function of the coupled peak intensity for picosecond pulses centered at wavelengths between 3.25µm and 4.75µm. (e) and (f) Spectral broadening and normalized mean wavelength shift (i.e. $(\lambda_c-\lambda_0)/\lambda_0$ where λ_c is the mean wavelength of the spectrum and λ_0 is the low power mean wavelength) as a function the coupled peak intensity.

The asymmetry in the transmitted pulses is actually more pronounced than one would expect for only multi photon effects and the derived mean wavelength shift seems to increase with the wavelength. Although, at a fixed light intensity, one would expect that fewer free carriers are generated as the wavelength increases, the free carrier dispersion coefficient, k_c , scales as λ^2 [12], therefore leading to a stronger effect at longer wavelengths and thus potentially explaining the stronger asymmetry and the larger mean wavelength shift observed.

In order to obtain the multi-photon absorption coefficients of Si_{0.6}Ge_{0.4}, the average output power was measured as a function of the coupled peak intensity and the results are shown in Fig. 4(a). The nonlinear, normalized, transmission (T_{NL}) through the waveguide as a function of coupled peak intensity is also shown in Fig. 4(b). It is estimated from T_{NL} = P_{out}/[P_{in}*exp(- αL)], where P_{out} and P_{in} are the output and input coupled powers, α is the propagation loss coefficient and L is the waveguide length. From Fig. 4(a) we observed that the output power increased almost linearly with the input power at low intensities. The slope is in agreement with the wavelength dependence of the linear losses measured on Fig. 2, i.e. a decrease of the linear loss for increasing wavelengths. This behavior confirms that the contribution of the nonlinear absorption remains negligible for coupled peak intensities below about 3 GW/cm², as was used earlier for the cut-back measurements. As the coupled peak intensity increased further, the output power from the waveguide saturated and eventually decreased for the two longest wavelengths. Accordingly, the nonlinear transmission in Fig. 4(b) shows a rapid drop as the input pulse intensity increased. This behavior is a clear indication of the presence of nonlinear losses in the waveguide. This trend is similar to the one observed in the case of optical limiting in the near-infrared region [21,23], which is caused by two-photon absorption and the subsequent absorption by the generated free-carriers. As the wavelength range used in our experiment is beyond the two-photon absorption threshold of $Si_{0.6}Ge_{0.4}$ (i.e. $\lambda_{th} \approx 2.45~\mu m$ [16]) the nonlinear transmission observed in Fig. 4 is necessarily due to higher order multiphoton absorption, such as three- and four-photon absorption, as well as the resulting freecarrier absorption [12].

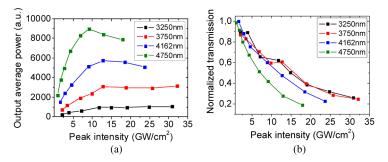


Fig. 4. (a) Output power from the Si/SiGe waveguide as a function of the coupled peak intensity for all the wavelengths used in the experiments. (b) Normalized transmission as a function of the coupled peak intensity.

5. Discussion

We used the nonlinear Schrödinger equation (NLSE) to model the nonlinear response of the SiGe/Si waveguides. The standard NLSE was modified in order to include higher order multiphoton absorption as well as free-carrier effects [20]. For example, if we were considering both three- and four-photon absorption, the NLSE would be given by

$$\frac{\partial A}{\partial z} + \frac{i}{2} \beta_2 \frac{\partial^2 A}{\partial t^2} + \frac{\alpha}{2} A = i \frac{k_0 n_2}{A_{3eff}} |A|^2 A - \frac{\alpha_{3PA}}{2A_{5eff}^2} |A|^4 A - \frac{\alpha_{4PA}}{2A_{7eff}^3} |A|^6 A - \frac{\sigma}{2} (1 - i\mu) N_c A$$
 (1)

where A is the slowly varying envelope of the pulse electric field amplitude; β_2 is the group velocity dispersion; α is the linear loss parameter; k_0 is the wavenumber; n_2 is the nonlinear refractive index; α_{3PA} and α_{4PA} are the three and four-photon absorption coefficients; A_{3eff} , A_{5eff} and A_{7eff} are the effective mode areas related to the nonlinear phenomena of different orders [24]; σ is the free-carrier absorption parameter; and $\mu = 2k_ck_0/\sigma$ with k_c the free-carrier dispersion parameter. The rate equation of the free-carrier density, N_c , in the case described by Eq. (1) is given by

$$\frac{\partial N_c}{\partial t} = \frac{\alpha_{3PA}}{3\hbar\omega} \left(\frac{\left| \mathbf{A} \right|^2}{A_{5eff}} \right)^3 - \frac{\alpha_{4PA}}{4\hbar\omega} \left(\frac{\left| \mathbf{A} \right|^2}{A_{7eff}} \right)^4 - \frac{N_c}{\tau_c}$$
 (2)

where \hbar is the reduced Plank constant; ω is the central angular frequency of the input pulse; and τ_c is the free-carrier lifetime. Since the range of values for τ_c reported for integrated waveguides is much longer than our pulse duration and much shorter than the time period between two subsequent pulses, we can neglect the last term on the right hand side of Eq. (2) [20]. As a starting point, we used the values of Si for the free-carrier absorption and dispersion parameters and we applied the scaling rules for the wavelength used in [12]. Thus we defined $\sigma(\lambda) = 1.45 \times 10^{-21} \text{ x } (\lambda/1.55)^2 \text{ m}^2$ and $k_c(\lambda) = 1.35 \times 10^{-27} \text{ x } (\lambda/1.55)^2 \text{ m}^3$, where λ is the wavelength (in μ m).

The NLSE in Eq. (1) was solved numerically using the Split-Step Fourier Method. We began by estimating the multi-photon absorption coefficients from the nonlinear transmission measurements that were shown in Fig. 4(b). In this step the Kerr effect and the free-carrier dispersion were neglected because they only affect the pulse phase and do not contribute to the nonlinear losses under our experimental conditions. The multi-photon absorption phenomenon considered at each of the experimental wavelengths was chosen following the model developed by Wherrett [25], i.e. by considering the ratio between the indirect bandgap energy of Si_{0.6}Ge_{0.4} (E_g = 1.01 eV) and the photon energy. Additionally, the different trends of the nonlinear transmission that are observed in Fig. 4(b) confirm that the regimes associated with the four investigated wavelengths are dominated by different multi-photon absorption orders. Therefore, up to a wavelength of 3750 nm, only three-photon absorption (α_{3PA}) is considered. At a wavelength of 4162 nm both three- and four-photon absorption are taken into account while at 4750 nm only four-photon absorption (α_{4PA}) is considered. In Figs. 5(a)-5(d) the transmission predicted by the model (continuous line) is compared to the experimental results (circles) and good agreement between the theory and the experiment is obtained. The multi-photon absorption coefficients that were estimated from our model are summarized and compared to the ones of Si and Ge in Fig. 5(e). The uncertainty in the values is mainly due to the uncertainty in the power that was coupled to the waveguides. We note that the estimated multi-photon absorption coefficients of SiGe are on the same order of magnitude as those for crystalline Si when the same order of multi-photon process is considered [12,26].

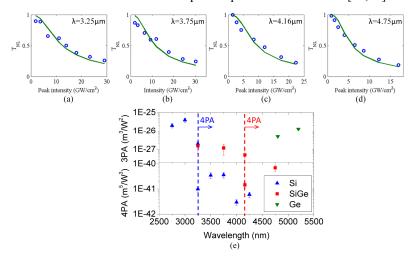


Fig. 5. (a-d) Nonlinear transmission deduced from the measurements as a function of the coupled peak intensity (circles) at different wavelengths. The nonlinear transmission predicted by solving the NLSE (continuous line) is shown along with the experimental results. (e) Comparison of three- and four-photon absorption coefficients of our SiGe waveguides (estimated in this work), along with that of Si [12], and Ge [27].

After obtaining the multi-photon absorption coefficients, we used the NLSE to estimate the nonlinear refractive index, n₂, of our SiGe/Si waveguides in the mid-IR. The best fits with the experimental data are obtained for numerical calculations with an n₂ of 0.75x10⁻¹⁸ m²/W at 3.25 μ m and of $2x10^{-18}$ m²/W at 4.75 μ m (see Figs. 6(a) and 6(b)). These values of n_2 are similar to that of crystalline Si in the same wavelength range (i.e. $n_2 \approx 2.7-5.8 \times 10^{-18} \text{ m}^2/\text{W}$) [12,26]. A similar analysis was carried out at all wavelengths used in these experiments and the value of the nonlinear refractive index found was 1.75×10^{-18} m²/W at 3.75 μm and 1.5×10^{-18} m²/W at 4.162 µm. The estimated value of n₂ as a function of wavelength is reported in Fig. 6(c). To first order, it is roughly constant over the wavelength range of the experiment, which is consistent with the negligible dispersion of the susceptibility of Si_{0.6}Ge_{0.4} in the mid-IR [16]. From a direct comparison of the spectra shown on Figs. 3(a)-3(d), one might have expected a clear increase in n₂ with wavelength because the number of peaks at the same coupled peak intensity increases. This apparent increase ends up being moderated by the decrease in the propagation loss for longer wavelengths (Fig. 2), and the impact of the different multi-photon absorption and effective areas, which are all taken into account in the simulations.

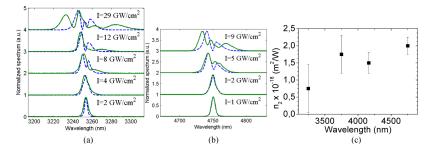


Fig. 6. Experimental (continuous line) and numerical (dashed line) transmission spectrum due to SPM as a function of the coupled peak intensity for a pulse centered at a wavelength of 3250nm, (a), and 4750nm, (b). (c) Nonlinear refractive index as a function of wavelength.

In Figs. 6(a) and 6(b), a clear deviation between the experiments and simulations is seen beyond intensities greater than $5 \, \text{GW/cm}^2$, with the simulated spectral broadening underestimating the experimental one. Considering the results obtained at 3250 nm, for instance, we first investigated if this discrepancy could be due to an incorrect value for the free-carrier dispersion. The results shown in Fig. 7(a) were obtained by increasing the free-carrier dispersion parameter by a factor 3, i.e. up to $k_c = 1.78 \times 10^{-26} \, \text{m}^3$. Due to the blue shift induced by the free-carrier dispersion, the blue part of the spectrum seems to be in slightly better agreement with the experimental results. However, the red side does not agree well with the experiment. This observation is corroborated by calculating the shift in the average wavelength of the spectrum [20], shown in Fig. 8(a). The blue shift generated by high free-carrier dispersion is too strong compared to that derived from the experimentally measured spectra (circles). Therefore, we conclude that free-carrier dispersion alone cannot explain the experimentally observed features.

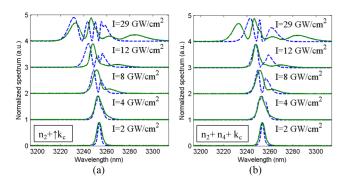


Fig. 7. Experimental (continuous line) and numerical (dashed line) transmission spectrum due to SPM as a function of the coupled peak intensity. For both scenarios $n_2 = 0.75 \times 10^{-18} \text{ m}^2/\text{W}$, then on the left $k_c = 1.78 \times 10^{-26} \text{ m}^3$ while on the right $n_4 = 5 \times 10^{-33} \text{m}^4/\text{W}^2$ and $k_c = 5.95 \times 10^{-27} \text{m}^3$

A second possible reason for discrepancy with our experimental results could be the presence of higher order nonlinear refractive phenomena. The polarization, P(t), induced by an intense electric field, E(t), in a centro-symmetric nonlinear medium is

$$P(t) = \varepsilon_0 \left[\chi^{(1)} E(t) + \chi^{(3)} E^3(t) + \chi^{(5)} E^5(t) + \chi^{(7)} E^7(t) + \cdots \right]$$
 (3)

where the $\chi^{(n)}$ terms correspond to the n-th order susceptibility. For instance, the two-photon absorption and the quadratic intensity dependent refractive index (Kerr nonlinearity) are related to the imaginary and the real part of $\chi^{(3)}$ respectively [20]. In our experimental conditions, three- and four-photon absorption are present. These nonlinear losses arise from the imaginary parts of the $\chi^{(5)}$ and $\chi^{(7)}$ susceptibilities. Therefore, as for $\chi^{(3)}$, the real part of these higher order susceptibilities might have an impact at high field intensities in this wavelength range. These nonlinear phenomena would induce a change in the refractive index given by

$$\Delta n = n_2 I + n_4 I^2 + n_6 I^3 \tag{4}$$

where n_4 and n_6 are associated with the real parts of $\chi^{(5)}$ and $\chi^{(7)}$, respectively. Therefore, Eq. (1) is modified to take into account the effect of the real parts of $\chi^{(5)}$ and $\chi^{(7)}$ and we obtain in the general case:

$$\frac{\partial A}{\partial z} + \frac{i}{2} \frac{\partial^{2} A}{\partial t^{2}} + \frac{\alpha}{2} A = ik_{o} \left(\frac{n_{z} |A|^{2}}{A_{sof}} + \frac{n_{s} |A|^{4}}{A_{sof}^{2}} + \frac{n_{s} |A|^{4}}{A_{sof}^{2}} + \frac{n_{s} |A|^{4}}{A_{sof}^{2}} \right) A - \frac{\alpha_{srs}}{2A_{sof}^{2}} |A|^{4} A - \frac{\alpha_{srs}}{2A_{sof}^{3}} |A|^{6} A - \frac{\sigma}{2} (1 - i\mu) N_{s} A$$
 (5)

where the effects of the real parts of $\chi^{(5)}$ and $\chi^{(7)}$ are given by $n_4|A|^4$ and $n_6|A|^6$ respectively. At 3250 nm, only three-photon absorption is considered and thus the terms relative to $\chi^{(7)}$ (i.e. n_6 and α_{4PA}) are both dropped in Eqs. (2) and (5). We simulated the pulse propagation through the $Si_{0.6}Ge_{0.4}$ waveguide at wavelength 3250 nm and adjusted the n_4 parameter to improve the agreement between theory and experiment. We kept the same value of n_2 as before, considering that this term dominates the pulse spectral broadening at low intensities. The results shown in Fig. 7(a) were obtained using $n_4 = 5 \times 10^{-33} \text{ m}^4/\text{W}^2$ along with the same value of $k_c = 5.95 \times 10^{-27} \text{ m}^3$ as in the initial simulation (Fig. 6(a)). From the results shown in Fig. 7(b) we obtained a better agreement between the experimental and numerical results than with standard theory shown in Fig. 6(a). Thus, the evolution of the spectral broadening is better reproduced by the model developed in Eq. (5) rather than the model of Eq. (1). This can also be seen by calculating the mean wavelength shift as shown in Fig. 8(a).

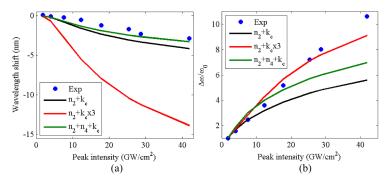


Fig. 8. (a) and (b) Mean wavelength shift and spectral broadening as a function of the coupled peak pulse intensity for the three simulation scenarios. For all the curves $n_2 = 0.75 \times 10^{-18} \text{ m}^2/\text{W}$. For the black curve $k_c = 5.95 \times 10^{-27} \text{ m}^3$ as in Fig. 6(a), for the red $k_c = 1.78 \times 10^{-26} \text{ m}^3$ as in Fig. 7(a), while for the green $n_4 = 5 \times 10^{-33} \text{m}^4/\text{W}^2$ and $k_c = 5.95 \times 10^{-27} \text{m}^3$ as in Fig. 7(b).

We see that for low peak intensities, up to about 5 GW/cm², the numerical results do not differ significantly depending on whether n_4 is included or not. On the other hand, at high peak intensities the wavelength shift is reduced when both n_2 and n_4 are considered due to the quadratic dependence of the induced refractive index change with pulse intensity arising from n_4 . The RMS spectral broadening calculated from the different simulation scenarios are compared to the experimental ones in Fig. 8(b) and demonstrate that including both n_2 and n_4 gives the better agreement with the experimental results of both Figs. 8(a) and 8(b).

Similar results were found also for the pulse centered at 4750 nm. In this case, since the four-photon absorption process is present, from Eq. (5), both n_4 and n_6 were considered but α_{3PA} is neglected in both Eqs. (2) and (5) as three-photon absorption is considered to be negligible at this wavelength. From the results shown in Fig. 9 we found that, once again, the evolution of the spectral broadening is better described when the real parts of $\chi^{(5)}$ and $\chi^{(7)}$ are included.

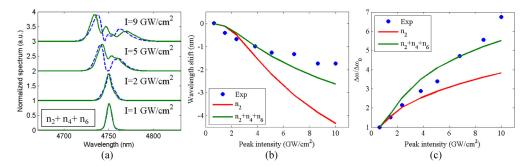


Fig. 9. (a) Experimental (continuous line) and numerical (dashed line) transmission spectrum as a function of the coupled peak intensity calculated considering the real parts of $\chi^{(5)}$ and $\chi^{(7)}$. The values used are $n_2=2x10^{-18}\ m^2/W,\ n_4=1x10^{-34}\ m^4/W^2,\ n_6=5x10^{-46}\ m^6/W^3$ and $k_c=1.27x10^{-26}\ m^3$. (b) and (c) Mean wavelength shift and spectral broadening as a function of the coupled peak pulse intensity. For both curves $n_2=2x10^{-18}\ m^2/W$ and $k_c=1.27x10^{-26}\ m^3$. For the green curve $n_4=1x10^{-34}\ m^4/W^2$ and $n_6=5x10^{-46}\ m^6/W^3$.

6. Conclusions

We report measurements of the nonlinear optical response of low-loss $Si_{0.6}Ge_{0.4}/Si$ waveguides in the mid-IR between 3250 nm and 4750 nm. In this wavelength range, nonlinear losses due to multi-photon absorption and the associated generation of free-carriers are observed at high peak intensities. The three- and four-photon absorption coefficients of $Si_{0.6}Ge_{0.4}$ were estimated and were found to be comparable to those of crystalline Si and Si

Furthermore, the nonlinear refractive index, n_2 , was estimated from spectral broadening measurements. We found that theory that accounts for free-carrier effects, multi-photon absorption and the Kerr effect was able to correctly predict the experimental results for peak intensities up to at least 5 GW/cm², while by including higher-order nonlinear refractive effects arising from the real parts of $\chi^{(5)}$ and $\chi^{(7)}$ we obtained a better agreement with experiments for higher pulse intensities. This suggests that the effect of these phenomena is not negligible in the wavelength range considered and at the pulse intensity levels used in the experiments. This could be caused by the fact that in the mid-IR we are close to the resonance frequencies of these higher order susceptibilities, which is also consistent with our observation of three- and four-photon absorption. These results represent the first experimental characterization of the nonlinear optical response of $Si_{0.6}Ge_{0.4}/Si$ waveguides in the mid-IR and they will be useful for the design of future photonic devices based on this material platform and go a long way to understanding the optical nonlinear response of this material in the mid-IR wavelength range.

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