

Decay of the I $\pi = 8$ – isomeric state in Nd 134 and Pt 184 studied by electron and γ spectroscopy

J. Perkowski, J. Andrzejewski, Ch. Droste, Ł. Janiak, E. Grodner, S. G.

Rohoziński, L. Próchniak, J. Srebrny, J. Samorajczyk-Pyśk, T. Abraham, et

al.

► To cite this version:

J. Perkowski, J. Andrzejewski, Ch. Droste, Ł. Janiak, E. Grodner, et al.. Decay of the I $\pi = 8$ – isomeric state in Nd 134 and Pt 184 studied by electron and γ spectroscopy. Physical Review C, 2017, 95 (1), pp.014305. 10.1103/PhysRevC.95.014305. hal-01465731

HAL Id: hal-01465731 https://hal.science/hal-01465731

Submitted on 13 Feb 2017

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Decay of the $I^{\pi} = 8^{-}$ isomeric state in ¹³⁴Nd and ¹⁸⁴Pt studied by electron and γ spectroscopy

J. Perkowski* and J. Andrzejewski

Faculty of Physics and Applied Informatics, University of Łódź, 90-236 Łódź, Poland

Ch. Droste, Ł. Janiak, E. Grodner, and S. G. Rohoziński Faculty of Physics, University of Warsaw, 02-093 Warsaw, Poland

L. Próchniak, J. Srebrny, J. Samorajczyk-Pyśk, T. Abraham, K. Hadyńska-Klęk, M. Kisieliński, M. Komorowska,

M. Kowalczyk, J. Kownacki, T. Marchlewski, J. Mierzejewski, P. Napiorkowski, and A. Stolarz

Heavy Ion Laboratory, University of Warsaw, 02-093 Warsaw, Poland

A. Korman

National Centre for Nuclear Research, 05-400 Otwock, Świerk, Poland

M. Zielińska

Irfu, CEA, Université Paris-Saclay, F-91191 Gif-sur-Yvette, France (Received 7 June 2016; revised manuscript received 25 October 2016; published 5 January 2017)

The properties of the *K*-isomer decays in the ¹³⁴Nd and ¹⁸⁴Pt nuclei have been investigated. Measurements were carried out in $e-\gamma$ and $\gamma-\gamma$ coincidence modes using electron spectrometers coupled to the central European Array for Gamma Levels Evaluations at the Heavy Ion Laboratory of the University of Warsaw. Internal conversion coefficients were obtained for transitions relevant to the decay of the isomeric states, allowing the determination of multipolarities and mixing ratios as well as hindrance factors. Two possible causes of the weakening of the *K* forbiddenness, namely rotational *K* mixing (Coriolis interaction) and triaxiality, are briefly discussed using schematic theoretical models.

DOI: 10.1103/PhysRevC.95.014305

I. INTRODUCTION

Nuclear isomerism is a frequently observed phenomenon. According to a recent compilation [1], there are 2469 isomers with half-life $T_{1/2} \ge 10$ ns. They are classified into five groups [1], including the group of K isomers. The mechanism of electromagnetic decay of these isomers, in spite of being the subject of extensive studies, is still frequently discussed [2-8]. K-isomeric states with spin/parity $I^{\pi} = 8^{-}$ and quantum number K equal to 8 (where K is the projection of the total angular momentum onto the symmetry axis of the nucleus) are found in nuclei from the mass regions around A = 130, 180,and 250. These isomeric states are observed in even-even nuclei with neutron numbers N = 74, 106, and 150 and in some isotopes of hafnium (Z = 72) and tungsten (Z = 74). They often decay many orders of magnitude slower than expected from the Weisskopf single-particle estimate. As an example, the $I^{\pi} = 8^{-}$, K = 8, 2340 keV, $T_{1/2} = 9.4$ ms isomeric state in ${}^{132}_{58}$ Ce₇₄ [9] decays, among other ways, to the 6^+ state (a member of the ground-state band with K = 0) via mixed E3/M2 transitions. For this decay the hindrance factors defined as $F = T_{1/2}^p/T_{1/2}^W$ (where $T_{1/2}^p$ is the partial half-life of the isomeric state and $T_{1/2}^W$ is the corresponding Weisskopf estimate) are equal to $2.5(4) \times 10^3$ and $4(1) \times 10^6$ for the E3 and M2 transitions [9], respectively.

Within the model of axially symmetric deformed (prolate) nuclei the isomeric $I^{\pi} = 8^{-}$, K = 8 states in ¹³⁴Nd and ¹⁸⁴Pt can be described by the following two quasiparticle configurations: $v7/2[404] \otimes v9/2[514]$ (N = 74) and $\nu 7/2[514] \otimes \nu 9/2[624]$ (N = 106) [1], with a single value of K = 8. These isomeric states decay via E1 transitions to the $I^{\pi} = 8^+$ state belonging to the ground-state band. For an axially symmetric nucleus this state has a value of K equal to 0. Such E1 transitions have been found in, among others, ¹³⁴Nd (N = 74) and ¹⁸⁴Pt (N = 106) [10–14]. Additionally, E3/M2 or E3 transitions are observed in nuclei with neutron number N = 74, where they connect the isomeric state with the $I^{\pi} = 6^+$ state [9–15] of the rotational band with K = 0as well as with the $I^{\pi} = 5^+$ state [9–15] belonging to the γ band with K = 2. According to the selection rules, 2^{λ} -pole transitions between initial (i) and final (f) states with quantum numbers K_i and K_f , respectively, are allowed if the condition $\Delta K = |K_i - K_f| \leq \lambda$ is fulfilled. Therefore, in an axially symmetric deformed nucleus where the K quantum number is a good one, the above-mentioned transitions (E1, M2, E3)between states with $K_i = 8$ and $K_f = 0$ or 2 should be forbidden. In fact, however, they are observed as strongly slowed down but not truly forbidden. This suggests that in these cases K is not a good quantum number and that the isomeric states and/or the final states have (in addition to the main value of K) some admixtures of other K components. The presence of these admixtures enables the decay of the K-isomeric state. One possible reason for the K admixtures is the Coriolis interaction that can modify the wave function

2469-9985/2017/95(1)/014305(10)

^{*}jarekper@uni.lodz.pl



FIG. 1. The decay scheme of the $I^{\pi} = 8^{-}$, K = 8 isomeric state in ¹³⁴Nd (N = 74) [10,11].

of the states to which an isomer decays, adding to the main value of *K* some additional high-*K* components [2–4]. There is another possible source of such admixtures, namely a deviation of the nuclear shape from axial symmetry. In such a case the nuclear-state wave functions are obviously combinations of components with different *K* values. To evaluate quantitatively the contribution of higher-*K* components, we have applied the simple phenomenological Davydov-Filippov model [16] of a triaxial rigid rotor. The estimated value of the triaxiality parameter γ [17] for the nuclei considered is around 20°–25° (see Sec. III), which causes the higher-*K* contribution to be quite substantial. Hence, both mechanisms of the *K* mixing should be taken into account for transitional nuclei such as 134 Nd and 184 Pt.

In this work both conversion electrons and γ rays were studied, which allowed the internal conversion coefficients (ICCs) and, as a consequence, the multipolarities to be determined. This information can be further used for measuring absolute transition probabilities. The experiment and results are described in Sec. II. Theoretical considerations and a summary are given in Secs. III and IV, respectively.

II. EXPERIMENTS

The half-lives of the studied $I^{\pi} = 8^{-}$, K = 8 isomeric states in the ¹³⁴Nd and ¹⁸⁴Pt nuclei are of the order of 1 ms; hence, the measurements were carried out during "beam-off" time intervals in electron- γ and γ - γ coincidence modes. The decay schemes of the $I^{\pi} = 8^{-}$, K = 8 isomeric states for the measured nuclei are presented in Fig. 1 for ¹³⁴Nd [10,11] and Fig. 2 for ¹⁸⁴Pt [13]. $E1 (8^- \rightarrow 8^+)$ and $E3 (8^- \rightarrow 6^+)$ transitions with a degree of K forbiddenness $\nu = |K_i - K_f| - \lambda = 7$ and 5 leading directly to the 8⁺ and 6^+ states of the ground-state band with K = 0 are present in ¹³⁴Nd (see Table I). Also, in the ¹⁸⁴Pt decay scheme an E1 transition connects the $I^{\pi} = 8^{-}$, K = 8 isomeric state with the 8^+ state belonging to the ground-state rotational band (K = 0). All these γ transitions severely violate the purity of the K-quantum number. Admixtures of K-quantum numbers are important for the description of configurations of excited states in both nuclei.

The decays of the isomeric states in ¹³⁴Nd and ¹⁸⁴Pt were studied using the EAGLE array [18] and conversion-electron spectrometers. The EAGLE array (central European Array for Gamma Levels Evaluations), located at the Heavy Ion Laboratory of University of Warsaw, has been designed as a multidetector setup for in-beam nuclear spectroscopy studies. In our experiments the array was equipped with 15



FIG. 2. The decay scheme of the $I^{\pi} = 8^{-}$ isomeric state in ¹⁸⁴Pt (N = 106) [13]. The width of the solid rectangles at the top of the arrows is proportional to the relative γ intensity from a given level.

TABLE I. Summary of data for the 8⁻ isomeric state in ¹³⁴Nd. The table contains information about energies (E_{γ}) , intensities (I_{γ}) , spins (I_i, I_f) , multipolarities $(\sigma\lambda)$, partial half-lives $(T_{1/2}^p)$, reduced transition probabilities $[B(\sigma\lambda, i \to f)]$, hindrance factors (F), degree of K forbiddenness (ν) , and reduced hindrance factors $f_{\nu} = F^{1/\nu}$ in the convention used in our work and in Ref. [8] (see the penultimate and the last column, respectively).

E_{γ} (keV)	I_{γ}^{a}	I_i^{a}	$I_f{}^{a}$	σλ	$T_{1/2}^{p}$ (ms)	$B(\sigma\lambda, i \to f)$	F^{b}	ν	$f_{\nu}{}^{b}$	$f_{\nu}^{\ c}$
168	93(7)	8-	8+	<i>E</i> 1	0.47(5)	$2.0(2) \times 10^{-10} \ (e^2 \ \text{fm}^2)$	8.4(9)×10 ⁵	7	$7.0^{+0.1}_{-0.1}$	$26.2^{+0.4}_{-0.4}$
596	0.6(2)	8-	(5 ⁺)	E3 ^d	73(25)	$0.6^{+0.3}_{-0.16} \ (e^2 \ {\rm fm}^6)$	$1.7(6) \times 10^3$	3	$11.9^{+1.2}_{-1.6}$	$11.9^{+1.2}_{-1.6}$
874	7(2)	8-	6+	E3 ^e	7^{+10}_{-3}	$0.5^{+0.4}_{-0.3} \ (e^2 {\rm fm}^6)$	$2^{+3}_{-1} \times 10^3$	5	$5^{+0.9}_{-0.5}$	$5^{+0.9}_{-0.5}$

^aIntensities I_{γ} of the 168- and 874-keV γ transitions and all spin values (I_i, I_f) were taken from Ref. [11].

^bConvention used in this work; see text.

^cConvention used in Ref. [8].

^dSpin/parity $I_f^{\pi} = 5^+$ was assumed.

^eOnly pure E³ multipolarity is considered; however, in the limit of experimental uncertainty an M2 admixture is possible (see text in Sec. II).

Compton-suppressed Ge detectors and was coupled to a conversion-electron spectrometer. The conversion-electron spectrometer used in the ¹³⁴Nd experiment was constructed at the University of Łódź [19] for "in-beam" studies. The spectrometer utilizes a combination of two magnetic fields for separation and transportation of electrons from the target position to the silicon detectors. Separation of electrons from positrons is achieved in a simplified miniorange setup. The transportation field is produced by a set of permanent magnets arranged in the form of coaxial rings. The background from δ electrons and γ rays is greatly reduced. A new version of the spectrometer University of Lodz an Electron SpEctrometer (ULESE) [20] was used in the ¹⁸⁴Pt experiment. The ULESE spectrometer is characterized by a very high efficiency, up to 9% at an energy of 300 keV, and good energy resolution, $\approx 1\%$ at \sim 500 keV for a thin calibration source and, which is very important, good suppression of δ electrons, positrons, and photons emitted by the targets. This achievement was obtained using a combination of magnetic fields in two different layouts: perpendicular and parallel to the axis of the spectrometer, which is orthogonal to the beam line. Both spectrometers were designed to be coupled to the EAGLE array.

Internal conversion coefficients α were determined based on the formula [9]

$$\alpha = \frac{N_e}{N_\gamma} \frac{\epsilon_\gamma}{\epsilon_e},\tag{1}$$

where N_e and N_{γ} are the numbers of conversion electrons and γ 's for a given transition, ϵ_e and ϵ_{γ} are the detection efficiencies of the electron and γ spectrometers, respectively.

The efficiency curve $(\epsilon_{\gamma}/\epsilon_e)$ as a function of electron energy was obtained based on transitions with well-known multipolarity or known ICC. The GF3 program from the RADWARE package [21] was used to analyze the γ and electron lines. For the fitting procedure of electron peaks a step function and an asymmetric Gaussian were used in addition to the usual Gaussian shape.

A. Decay of the $I^{\pi} = 8^-$, K = 8 isomeric state in ${}^{134}_{60}$ Nd₇₄

The ¹³⁴Nd nucleus was produced in the ¹²²Te(¹⁶O,4n)¹³⁴Nd reaction at a beam energy of 90 MeV and an intensity of about 10 pnA. The ¹⁶O beam was delivered by the U-200P cyclotron of the Heavy Ion Laboratory (HIL) of the University of

Warsaw. The ¹²²Te target (with thickness of about 3 mg/cm²) was evaporated onto a Au backing foil (2.5 mg/cm²) thick enough to stop all recoils. The target preparation is described in Ref. [22].

The efficiency curve (Fig. 3) of our setup was obtained using an internal calibration based on the γ transitions accompanying the ^{134m}Nd \rightarrow ¹³⁴Nd and ¹³⁴Nd \rightarrow ¹³⁴Pr \rightarrow ¹³⁴Ce decays. The following lines with well-known multipolarities were used: 495, 631, and 706 keV from ¹³⁴Nd and 409, 556, 639, 677, 965, and 973 keV from the ¹³⁴Pr \rightarrow ¹³⁴Ce decay.

One of the main goals of this experiment was to determine the internal conversion coefficient for the 874-keV transition which connects the isomeric state with the 6⁺ level in the ¹³⁴Nd nucleus (Fig. 1). To clean up the γ and electron spectra from long-lived ($T_{1/2} \ge 1$ ms) lines which do not originate from the isomeric state decay ($T_{1/2} \approx 0.4$ ms), events collected between 2.1 and 3.6 ms after the end of the cyclotron beam pulse were subtracted from the events collected in the time span between 0.2 and 1.7 ms. This method could be used owing to the millisecond time structure of the cyclotron beam at the HIL ("beam-on," 2 ms; "beam-off," 4 ms). The electron spectrum (the sum of three spectra gated on the 294-, 495-, and 631-keV



FIG. 3. The efficiency curve $(\epsilon_{\gamma}/\epsilon_e)$ of the experimental setup for the ¹³⁴Nd measurement. The linear fit to the experimental points and the error band are indicated by solid and dashed lines, respectively.



FIG. 4. The summed electron spectrum in coincidence with the 294-, 495-, and 631-keV γ transitions accompanying the decay of the isomeric state in ¹³⁴Nd (see also Fig. 1). The experimental (thick solid line) and simulated (for more details, see text) K874 lines, for *M*2 and *E*3 multipolarities, are shown for comparison in the inset.

 γ lines) is presented in Fig. 4. By analyzing this spectrum, the value of the conversion coefficient for the $8^- \rightarrow 6^+$, K874 line was determined to be $\alpha_K = 0.005(2)$. Comparison of this value with theoretical conversion coefficients ($\alpha_K(E3) = 0.00551$, $\alpha_K(M2) = 0.0103$ [23]) suggests that the studied transition has a pure E3 or mixed E3/M2 character in the limit of experimental uncertainty. It is worth adding that previously available information suggesting an M2 multipolarity for the 874-keV transition [12] was based purely on systematics. For a better visualization of our result, the inset in Fig. 4 shows the part of the electron spectrum relevant to the K874 line. The experimental spectrum can be compared with the simulated electron peaks for M2 and E3 multipolarities. The simulated electron spectra were calculated taking into account the experimentally obtained intensity of the γ 's, the efficiency of the experimental setup and the experimental energy resolution of the electron spectrometer.

The possibility that the 8^- isomeric state decays to the (5^+) level via the 596-keV transition (see Fig. 1) was pointed out in Ref. [10]. To check this suggestion, the γ -ray spectrum gated on the 294-keV line was analyzed (see Fig. 5). Thanks to the time-cleaning procedure (described above) a very weak 596-keV γ line was observed (Fig. 5), showing that this isomer decays to the (5^+) , 1698-keV level belonging to the γ band and then via the 609- and 795-keV transitions to the 2^+ state of the rotational band. The decay path of the (5^+) level via emission of the 609-, 795-, and 294-keV γ 's is well established [10–12]. Our observation supports the result that the 596-, 609-, and 795-keV transitions are not present in the γ spectrum gated on the 495-keV line. The intensity of the 596-keV line was estimated at 0.6(2)%. For comparison, the γ intensities of the 168- and 874-keV transitions connecting the 8⁻ state with the 8^+ and 6^+ states are 93% and 6.5%, respectively [12]. In this experiment the half-life of the $I^{\pi} = 8^{-}$, K = 8 isomeric state in ¹³⁴Nd was measured as 0.38(2) ms and this value agrees perfectly with the value of 0.41(3) ms given in Ref. [12].



FIG. 5. The γ spectra (thin solid lines, left ordinate) gated on the 294-keV line collected during two time spans (see text) after the end of the cyclotron beam pulse. The weak 596-keV γ line is visible in the difference spectrum (thick solid line, right ordinate). This proves that the 8⁻ isomeric state in ¹³⁴Nd also decays to the γ band, as was suggested in Ref. [10].

B. Decay of the $I^{\pi} = 8^-$, K = 8 isomeric state in ${}^{184}_{78}$ Pt₁₀₆

The study of the decay of the $I^{\pi} = 8^{-}$, K = 8isomeric state in ¹⁸⁴Pt was performed by measuring $e - \gamma$ and $\gamma - \gamma$ coincidences. The ¹⁸⁴Pt isotope was produced in the ¹⁷⁵Lu(¹⁴N,5*n*)¹⁸⁴Pt reaction at a beam energy of 90 MeV and intensity of about 1 pnA. The ¹⁴N beam was delivered by the U-200P cyclotron of the Heavy Ion Laboratory, Warsaw. In the experiment natural lutetium foil (2.5 mg/cm² thick) was used as a target. The Lu foil was backed by a gold layer (~1 mg/cm²) to stop all the reaction products. Therefore, electrons as well as γ rays were emitted from a well-defined spot. The chosen thickness of the target was a compromise between the energy loss of electrons traveling through the target and the efficiency of ¹⁸⁴Pt production.

In this experiment the EAGLE array and the ULESE conversion-electron spectrometer were used. As an example of the data obtained from this electron spectrometer, spectra of electrons emitted from the target during "beam-off" periods are shown in Fig. 6.

In this experiment the efficiency curve (see Fig. 7) was obtained using an internal calibration based on the γ transitions accompanying the ¹⁸⁴mPt \rightarrow ¹⁸⁴Pt and ¹⁸⁴Pt \rightarrow ¹⁸⁴Ir \rightarrow ¹⁸⁴Os decays. The following lines with well-known multipolarities were used: 163, 273, 362, 432, and 610 keV from ¹⁸⁴Pt and 120, 264, 390, 493, and 539 keV from the ¹⁸⁴Ir \rightarrow ¹⁸⁴Os decay. A third-order polynomial function was fitted to the experimental points. The result is shown in Fig. 7.

One of the goals of the ¹⁸⁴Pt experiment was the determination of the conversion coefficient for the $(6^-) \rightarrow (5)^-$, 119-keV transition (see Fig. 2). For that purpose the electron spectra in coincidence with the 441- and 1071-keV γ rays were summed. The resulting spectrum is shown in Fig. 8 as the thin solid line. A conversion coefficient for the $L + M + \cdots$ lines equal to $\alpha_{L+M+\cdots} = 1.2(2)$ was obtained. This value agrees with



FIG. 6. The total electron spectrum (dotted line, left ordinate) and the spectrum gated on the 163-keV γ line (solid line, right ordinate) for the ¹⁸⁴Pt "beam-off" measurement.

 $\alpha_{L+M+\dots}(E2) = 1.5(3)$ published in Ref. [14]. A comparison of our result with theoretical conversion coefficients for the 119-keV transition ($\alpha_{L+M+\dots}(E1) = 0.05$, $\alpha_{L+M+\dots}(E2) =$ 1.87, $\alpha_{L+M+\dots}(M1) = 0.72$, $\alpha_{L+M+\dots}(M2) = 9.4$ [23]) implies an E2/M1 mixed transition with $\delta^2 = 0.7^{+0.9}_{-0.4}$. The E2/M1 transition is consistent with the level scheme (Fig. 2) proposed in Ref. [13]. An M2/E1 solution with a substantial contribution from the M2 transition (our result $\delta^2 = 0.14(3)$ and the result from Ref. [14] $\delta^2 = 0.19$) is also possible.

Another important transition in the decay of the $I^{\pi} = 8^-$, K = 8 isomeric state in ¹⁸⁴Pt is the (6⁻) \rightarrow (5)⁺, 488-keV line. From the electron spectrum presented in Fig. 9 it was only possible to obtain an upper limit for the internal conversion coefficient of the studied transition: $\alpha_K \leq 0.028(2\sigma)$. By comparing this result with the calculated ICCs ($\alpha_K(E1) = 0.0073$, $\alpha_K(M1) = 0.069$, $\alpha_K(E2) = 0.019$ and $\alpha_K(M2) = 0.20$ [23]) one can draw the conclusion that the following solutions,



FIG. 7. The efficiency curve $(\epsilon_{\gamma}/\epsilon_e)$ vs electron energy for the experimental setup (¹⁸⁴Pt experiment). The third-order polynomial fit to the experimental points and the error band are denoted by solid and dashed lines, respectively.



FIG. 8. Sum of the electron spectra (thin solid line) in coincidence with the 441- and 1071-keV γ rays from the ¹⁸⁴Pt experiment. For the 119-keV transition the experimental spectrum may be compared with the simulated one (thick solid line) for $\delta^2 = 0.7$.

namely E1 (or E1/M2) and E2 (or E2/M1), should be considered. The E1 or E1/M2 multipolarities agree with the assignment of spins/parities proposed in Ref. [13] for the $(6^-) \rightarrow (5)^+$ transition, whereas the E2 (or E2/M1) multipolarity requires $\Delta I = |I_{\text{initial}} - I_{\text{final}}| = 2$ or 1 and $\Delta \pi = \pi_{\text{initial}} \times \pi_{\text{final}} = +1$ for the spins/parities of the studied transition.

In the case of the $(7)^+ \rightarrow (5)^+$, K424-keV line the situation is more complicated. One broad electron peak at an energy of 350 keV in the sum of the electron spectra gated by the 163-, 273-, and 871-keV transitions consists of the K432keV ($E_e = 354$ keV), L362-keV ($E_e = 349$ keV), and K424keV ($E_e = 346$ keV) lines. Fortunately, the multipolarities of the 362- and 432-keV transitions are known from Ref. [13]



FIG. 9. The sum of the electron spectra gated on the 163- and 871-keV γ lines from ¹⁸⁴Pt. The thick solid line represents a Gaussian function (superimposed on a constant background) fitted to the experimental points. All peak parameters were fixed except the area.

E_{γ} (keV)	$I_{\gamma}{}^{\mathrm{a}}$	I_i	I_f	σλ	$T_{1/2}^{p}$ (ms)	$B(\sigma\lambda, i \to f)$	F^{b}	ν	$f_{v}{}^{b}$	$f_{\nu}^{\ c}$
49	0.79(8)	8-	(6 ⁻)	$E2^{d}$	300(40)	$6.7(9) \times 10^{-3} \ (e^2 \ \text{fm}^4)$	$9(1) \times 10^3$	1	$9^{+1}_{-1} \times 10^3$	$9^{+1}_{-1} \times 10^3$
112	12(4)	8-	$(7)^+$	E1	19(7)	$1.6^{+0.9}_{-0.4} \times 10^{-11} \ (e^2 \ {\rm fm}^2)$	$1.2(4) \times 10^7$	5	$26.2^{+1.6}_{-2.1}$	165^{+10}_{-13}
610	100(16)	8^{-}	8^+	$E1^{d}$	2.3(4)	$8.0(1.5) \times 10^{-13} \ (e^2 \ \text{fm}^2)$	$2.6(5) \times 10^8$	7	$15.9^{+0.4}_{-0.5}$	$59.2^{+1.4}_{-1.7}$

TABLE II. The same as Table I but for the 8⁻ isomeric state in ¹⁸⁴Pt.

^aIntensities of listed γ transitions (I_{γ}) were taken from Ref. [13] except for the 49-keV line.

^bConvention used in this work; see text.

^cConvention used in Ref. [8].

^dMultipolarity taken from Ref. [13].

and the γ lines of these peaks are easily identified in the γ spectrum; therefore, the ICC for the 424-keV transition could be calculated from the equation

$$\alpha_{K}^{424} = \frac{N_{e}^{424+362+432}(\epsilon_{\gamma}/\epsilon_{e}) - \alpha_{K}^{432}N_{\gamma}^{432} - \alpha_{L}^{362}N_{\gamma}^{362}}{N_{\gamma}^{424}}$$
$$= -0.09 \pm 0.08, \tag{2}$$

where α_K and α_L are the internal conversion coefficients for the given transition, N_e and N_γ are the numbers of conversion electrons and γ 's for the transitions of interest, and $\epsilon_{\gamma}/\epsilon_e$ is the detection efficiency of the experimental setup.

In this equation the efficiency ratios were assumed to be the same for all transitions considered. As a result, it was only possible to obtain an upper limit for the ICCs of the studied transition: $\alpha_K \leq 0.07(2\sigma)$. A comparison of this result with the calculated ICCs ($\alpha_K(E1) = 0.0098$, $\alpha_K(M1) = 0.10$, $\alpha_K(E2) = 0.027$ and $\alpha_K(M2) = 0.31$ [23]) suggests that the studied (7)⁺ \rightarrow (5)⁺, 424-keV transition has *E*2 multipolarity (in agreement with Ref. [13]) or *E*2/*M*1. The *E*1 or *E*1/*M*2 multipolarities are excluded because of the parities of the initial and final states. There are no other data concerning the ICCs for the 424- and 488-keV transitions that can be compared with our results.

In our experiment the γ -ray intensity of the $8^- \rightarrow (6^-)$, 49keV transition was determined to be $I_{\gamma} = 0.79(8)\%$, assuming that the intensity of the $8^- \rightarrow 8^+$, 610-keV γ transition equals 100% (see Table II). This result was obtained based on a comparison of the 119- and 112-keV line intensities in the γ spectrum with a gate set on the ($2^+ \rightarrow 0^+$), 163-keV transition. The accepted values of the ICCs for the 49-, 119-, and 488-keV transitions were used in this calculation. In this experiment the half-life of the $I^{\pi} = 8^{-}$, K = 8 isomeric state in ¹⁸⁴Pt was measured to be 0.86(10) ms. This value agrees with the value of 1.01(5) ms given in Ref. [13].

The experimental results (present work and also results taken from Ref. [11]) for the $I^{\pi} = 8^{-}$, K = 8 isomeric state in ¹³⁴Nd are summarized in Table I. The results for the E1 transitions in ¹³⁴Nd as well as in ¹⁸⁴Pt require some additional comments. In our work, for E1 transitions the Weisskopf estimates of $T_{1/2}^W$ (used to calculate the value of F) were multiplied by a factor of 10^4 to take into account the generally higher hindrance for such transitions [5,24,25]. It should be noted that Kondev et al. in their recent comprehensive review [8] did not use this correction factor. Hence, F(E1; Kondev, Ref. [8]) = $10^4 \times F(E1; \text{ our work})$ and the reduced hindrance factor per degree of K forbiddenness $f_{\nu}(E1; \text{ Kondev, Ref. } [8]) =$ $(10^4)^{1/\nu} \times f_{\nu}(E1; \text{ our work});$ see Table I for the definition of f_{ν} . To avoid misunderstanding, in the last and penultimate columns of Tables I (¹³⁴Nd) and II (¹⁸⁴Pt) the same sets of experimental data are presented using both our and Kondev's conventions. The experimentally determined values of the internal conversion coefficients (taken from the present work and from Ref. [14]) for the $I^{\pi} = 8^{-}$, K = 8 isomeric state in 184 Pt are summarized in Table III.

III. THEORETICAL CONSIDERATIONS

Below we briefly discuss the two mechanisms which can be invoked to explain a reduction in the hindrance of a K-isomer decay. The first is the influence of the Coriolis interaction on nuclear states with increasing rotational frequency [3,7]. The second is deviation of the nuclear shape from axial symmetry, which can induce substantial higher K-number admixtures to nuclear wave functions [5,26]. In both cases we use simple phenomenological models which can give, we hope, some

TABLE III. Internal conversion coefficients (ICCs), multipolarities ($\sigma\lambda$), and mixing parameters (δ^2) for transitions accompanying the decay of the $I^{\pi} = 8^{-}$, K = 8 isomeric state in ¹⁸⁴Pt. The ICCs measured in the present work (second column) may be compared with the data of Ref. [13] (last column).

E_{γ} (keV)	ICC	$\sigma\lambda,\delta^2$	ICC from Ref. [14]		
119	$\alpha_{L+M} = 1.2(2)$	$E2/M1$, ^a $\delta^2 = 0.7^{+0.9}_{-0.4}$ or $M2/E1$, $\delta^2 = 0.14(3)$	$\alpha_{L+M} = 1.5(3)$		
424	$\alpha_K \leqslant 0.07(2\sigma)$	$E2 \text{ or } E2/M1^{\text{b}}$	No data		
488	$\alpha_K \leqslant 0.028(2\sigma)$	$E1$ or $M2/E1$, $E2$ or $E2/M1^{\circ}$	No data		

^aMultipolarity E2/M1 agrees with the (6⁻) \rightarrow (5)⁻ assignment given in Ref. [13].

^bMultipolarity E2 agrees with the $(7)^+ \rightarrow (5)^+$ assignment given in Ref. [13].

^cMultipolarities E1 or E1/M2 agree with the $(6^-) \rightarrow (5)^+$ assignment given in Ref. [13].



FIG. 10. Experimental alignments for ¹³⁴Nd and ¹⁸⁴Pt. Harris reference parameters of $\mathcal{I}_0 = 17.0\hbar^2 \text{ MeV}^{-1}$ and $\mathcal{I}_1 = 25.0\hbar^2 \text{ MeV}^{-1}$ (the same as in Ref. [3]) were used for both nuclei.

hints on the nature and decay of the *K* isomers discussed even if the employed approximations are rather crude.

A high rotational frequency leads to changes of in the nuclear shell structure [27], and at some point the Coriolis force can break a correlated nucleon pair, which causes the creation of the so-called *s* band. This effect can be seen, e.g., on a plot of the experimental alignments vs rotational frequency (Fig. 10). Other broken-pair excitations may have a substantial spin component along the symmetry axis, and as a result *K*-isomeric states emerge. However, the Coriolis effect can perturb the states to which an isomer decays and introduce higher-*K* components into the wave function describing these states. These admixtures play the main role in the weakening of the hindrance of transitions from the *K*-isomeric state [3,8].

We performed band-mixing-type calculations according to the method described in Ref. [3]. In the first step the groundstate and *s*-band energies were parametrized using the wellknown formula from the variable-moment-of-inertia (VMI) model [28],

$$E(I) = \frac{I(I+1)}{2J} + \frac{[(I(I+1)]^2}{8CJ^4} + E_0,$$
 (3)

where I is the spin of a given level, C and E_0 are constants, and the moment of inertia (depending on the spin) fulfills the equation

$$J^{3} - J_{0}J^{2} + I(I+1)/2C = 0,$$
(4)

with another constant J_0 . The results of fitting the VMI parameters to experimental data and values of interaction matrix elements are given in Table IV. The calculations for *s* bands were performed taking the value of the alignment as equal to $10\hbar$ for both nuclei (see Fig. 10). Final results for the distribution of *K* values (after mixing the ground-state band and the *s* band) are given in Table V. Let us mention that in the case of ¹³⁴Nd a similar approach was used in Ref. [3] but with a different value for the alignment of the *s* band (6 \hbar).

The occurrence of higher-K components in the final states of the decay of K isomers in the considered nuclei as a consequence of nonaxial deformation (triaxiality) is studied using the simple phenomenological Davydov-Filippov model [16], which describes the energy of excited rotational states and electromagnetic transition probabilities for nonaxial nuclei. An important parameter of the model is the value of the γ deformation which can be estimated, e.g., from the ratio of the excitation energies of the 2^+_1 (yrast band) and of the 2^+_2 level. From the experimental data we obtained values for the γ deformation equal to 24° for ¹³⁴Nd and 20° for ¹⁸⁴Pt. An additional argument for considering the nonaxiality of the nuclei under study comes from our microscopic self-consistent calculations using the Sly4 Skyrme interaction and the δ -type pairing. The calculations were made along the same lines as in Refs. [29,30]. The collective potential energy obtained for both nuclei is plotted in Fig. 11. One can observe a significant softness against nonaxial deformation, especially in the case of the ¹³⁴Nd nucleus. In both cases the minimum of the collective energy corresponds to a nonzero γ deformation.

The elaborate theoretical model used in Refs. [29,30], based on the generalized Bohr Hamiltonian, can also give more detailed information on collective states. One of the results obtained is the average value of the γ deformation in the ground state, equal to 22° in the case of ¹³⁴Nd and 18° in the case of ¹⁸⁴Pt. These values are quite close to those calculated in the Davydov-Filippov (DF) model and we confine ourselves to the simpler DF approach because of several rather crude approximations employed in the subsequent discussion.

The following discussion is based mainly on the analysis of the distribution of wave-function components with different *K* numbers of the 5⁺, 6⁺, 8⁺ (in ¹³⁴Nd), 7⁺, 8⁺ (in ¹⁸⁴Pt), and 8⁻ (for both nuclei) states. The results for the positive-parity states obtained from the two theoretical approaches mentioned previously are presented in Table V. Calculations for the Davydov-Filippov model were performed using the DF code [31]. In the case of the γ -vibrational band, owing to the lack of sufficient experimental information, we cannot apply the approach based on band mixing; hence, for the 5⁺ (¹³⁴Nd) and

TABLE IV. Parameters of the VMI model [28] and results of band mixing calculations for the considered nuclei.

		$C (10^6 \text{ keV}^3 \hbar^{-4})$	$J_0 (10^{-3} \text{ keV}^{-1}\hbar^2)$	E_0 (keV)	V (keV) ^a	s band $(\%)^{b}$
¹³⁴ Nd	ground-state band	4.9	7.8	0	275	2.8
	s band	14.5	13	3634		
¹⁸⁴ Pt	ground-state band	1.6	19.6	24	114	0.6
	s band	5.5	25	2669		

^aInteraction matrix element.

^bProbability of admixture of the *s* band in the 8⁺ yrast state.

KI ^π			¹³⁴ Nd			Ref. [7]			
		DF model		Coriolis		DF model		Coriolis	
	5+	6+	8+	6+	8+	7+	8+	8+	8-
0	_	61.3	52.4	99.14	97.7	_	65.5	99.5	0
1	_	_	_	0.335	0.893	_	_	0.187	0
2	96.5	37.5	44.1	0.251	0.669	96.4	33.6	0.140	0
3	_	_	_	0.154	0.412	_	_	0.086	0
4	3.5	1.2	3.4	0.077	0.206	3.6	0.9	0.043	6.3×10^{-4}
5	_	_	_	0.031	0.082	_	_	0.017	0.014
6	_	2.5×10^{-3}	0.05	9.63×10^{-3}	0.026	8.2×10^{-3}	3.2×10^{-3}	5.4×10^{-3}	0.35
7	_	_	_	_	6.0×10^{-3}	_	_	1.3×10^{-3}	7
8	_	_	5×10^{-5}	-	1.0×10^{-3}	-	8×10^{-7}	0.2×10^{-3}	92.6

TABLE V. Distributions of the *K*-number values calculated within the models discussed in the text for the relevant states in ¹³⁴Nd and ¹⁸⁴Pt. Each entry corresponds to the square of the amplitude (expressed in %) of a component of the wave function with a given *K*.

 7^+ (¹⁸⁴Pt) states we show only results from the DF model. The composition of the 8⁻ state cannot be predicted by the simple models presented; therefore, the *K* distribution for this state was taken from calculations performed for ¹⁸²Os [7], where the same $I^{\pi} = 8^-$, K = 8 isomeric state is observed. The authors of Ref. [7] claim that for other nuclei with N = 106 the results are very similar. We also used these results in the discussion of the ¹³⁴Nd nucleus, where the 8⁻ isomeric state has an analogous structure (two quasineutron $v7/2 \otimes v9/2$ state).

As can be seen from Table V the Coriolis (rotational K-mixing) and DF models give quite different distributions of the K components in the wave functions of the positive-parity states. To estimate the relative importance of the effects taken into account by the two models, we simply consider the products of the probabilities of the K components in the wave function of the isomeric state and the state into which the

isomer decays. The considered K values take into account the experimental transition multipolarities discussed in this work and the K selection rule.

Of course, such an analysis can yield only qualitative conclusions.

¹³⁴Nd, $8^- \rightarrow 6^+$, 874-keV E3 transition. For this transition we also consider the M2 multipolarity, not excluded by the experimental data. First we discuss the DF model. In the case of the E3 branch the greatest probability products give two combinations, $(8^-, K = 7) \rightarrow (6^+, K = 4)$ and $(8^-, K = 5) \rightarrow$ $(6^+, K = 2)$, with respective values of 8.4 and 0.54. For the M2 branch there are also two important combinations, $(8^-, K =$ $6) \rightarrow (6^+, K = 4)$ and $(8^-, K = 8) \rightarrow (6^+, K = 6)$, with respective values of 0.42 and 0.2. Within the Coriolis model and for the E3 branch one should consider two combinations, $(8^-, K = 8) \rightarrow (6^+, K = 5)$ and $(8^-, K = 7) \rightarrow (6^+, K = 4)$, with values of 2.9 and 0.54. For the M2 branch there are again



FIG. 11. Mean-field collective potential energy (relative to a spherical shape) for ¹³⁴Nd and ¹⁸⁴Pt (see text).

two combinations, $(8^-, K = 8) \rightarrow (6^+, K = 6)$ and $(8^-, K = 7) \rightarrow (6^+, K = 5)$, with values of 0.89 and 0.22.

¹³⁴Nd, $8^- \rightarrow 8^+$, 168-keV E1 transition. In the DF model the best combination $(8^-, K = 7) \rightarrow (8^+, K = 6)$ gives a value of the product equal to 0.32, while other combinations can be neglected. In the Coriolis model there are again two relevant combinations, $(8^-, K = 8) \rightarrow (8^+, K = 7)$ and $(8^-, K = 7) \rightarrow (8^+, K = 6)$, with values of 0.56 and 0.18.

¹⁸⁴Pt, $8^- \rightarrow 8^+$, 610-keV E1 transition. The DF model gives the biggest product for the combination $(8^-, K = 7) \rightarrow (8^+, K = 6)$ but with a value of only 0.023, while within the Coriolis model for the combination $(8^-, K = 8) \rightarrow (8^+, K = 7)$ the probability product is equal to 0.12.

The general qualitative conclusion is that both rotational K mixing and triaxiality effects should be taken into account in explaining the reduction of the hindrance of the K-isomer decay. To get a quantitative interpretation of the experimental results, one needs a more complete theory for both the isomers and the states into which they decay.

IV. SUMMARY

The decays of two $I^{\pi} = 8^{-}$, K = 8 isomeric states in ${}^{134}_{60}$ Nd₇₄ and ${}^{184}_{78}$ Pt₁₀₆ have been studied. The experiments were carried out in $e - \gamma$ and $\gamma - \gamma$ coincidence mode using electron spectrometers coupled to the EAGLE array. As a result of these measurements the internal conversion coefficients, multipolarities, and absolute transition probabilities were obtained.

In the case of ¹³⁴Nd the internal conversion coefficient $[\alpha_K = 0.005(2)]$ for the $8^- \rightarrow 6^+$, 874-keV transition from the decay of the 8^- isomeric state was measured. The result implies a pure *E*3 or, in the limit of the experimental uncertainty, a mixed *E*3/*M*2 character. A previous suggestion [12] of an *M*2 multipolarity for this transition was based only on systematics. The very weak 596-keV γ line accompanying the 8^- isomeric state decay to the (5⁺) state (a member of the γ band) was observed in the present work for the first time. Its intensity is equal to 0.6(2)%, while the total intensity of all

 γ transitions deexciting the 8⁻ isomeric state equals 100%; see Fig. 1 and Table I. The presence of the 596-keV transition was postulated in Ref. [10] but not experimentally proved. In our experiment the half-life of the 8⁻ isomeric state was determined as 0.38(2) ms.

In the case of ¹⁸⁴Pt the internal conversion coefficients, multipolarities, and mixing parameters were determined for 119-keV transition. For the weak transitions, namely the 424- and 488-keV γ lines, only upper limits for the ICCs were obtained. Nevertheless, these data allowed us to obtain information about the transition multipolarities. In all the cases studied (see Tables II and III) the results do not contradict the spins and parities proposed in Ref. [13], but for the 424and 488-keV transitions other, additional solutions shown in Table III are possible. The half-life of the 8⁻ isomeric state measured in our experiment equals 0.86(10) ms.

Schematic theoretical models (VMI plus two band mixing and the Davydov-Filippov model) were applied to investigate the role of the Coriolis interaction (rotational K mixing) and triaxiality in the weakening of the K forbiddenness in the decay of the considered isomeric states. An analysis utilizing the transition multipolarities determined in this work and those taken from the literature shows that, besides the widely discussed rotational K mixing, nonaxiality of the nucleus should also be taken into account in the theoretical description of the K-isomer decay.

ACKNOWLEDGMENTS

We are grateful to Alison Bruce for very helpful discussions, in particular of the Coriolis *K*-mixing mechanism. The authors wish to thank the staff of the Heavy Ion Laboratory of the University of Warsaw for providing excellent beam conditions and for their support at each stage of this work. The possibility to use the Phase I ACS Ge detectors loaned by the GAMMAPOOL is gratefully acknowledged. This project was supported by grants from the Polish National Science Centre (Grants No. 2011/03/B/ST2/02660 and No. 2013/10/M/ST2/00427).

- A. K. Jain, B. Maheshwari, S. Garg, M. Patial, and B. Singh, Nucl. Data Sheets 128, 1 (2015).
- [2] P. M. Walker, G. Sletten, N. L. Gjorup, M. A. Bentley, J. Borggreen, B. Fabricius, A. Holm, D. Howe, J. Pedersen, J. W. Roberts, and J. F. Sharpey-Schafer, Phys. Rev. Lett. 65, 416 (1990).
- [3] A. M. Bruce, A. P. Byrne, G. D. Dracoulis, W. Gelletly, T. Kibèdi, F. G. Kondev, C. S. Purry, P. H. Regan, C. Thwaites, and P. M. Walker, Phys. Rev. C 55, 620 (1997).
- [4] P. M. Walker and G. D. Dracoulis, Nature (London) 399, 35 (1999).
- [5] T. Morek, J. Srebrny, C. Droste, M. Kowalczyk, T. Rzaca-Urban, K. Starosta, W. Urban, R. Kaczarowski, E. Ruchowska, M. Kisieliński, A. Kordyasz, J. Kownacki, M. Palacz, E. Wesołowski, W. Gast, R. M. Lieder, P. Bednarczyk, W. Męczyński, and J. Styczeń, Phys. Rev. C 63, 034302 (2001).
- [6] A. P. Robinson, T. L. Khoo, I. Ahmad, S. K. Tandel, F. G. Kondev, T. Nakatsukasa, D. Seweryniak, M. Asai, B. B. Back,

M. P. Carpenter, P. Chowdhury, C. N. Davids, S. Eeckhaudt, J. P. Greene, P. T. Greenlees, S. Gros, A. Heinz, R.-D. Herzberg, R. V. F. Janssens, G. D. Jones, T. Lauritsen, C. J. Lister, D. Peterson, J. Qian, U. S. Tandel, X. Wang, and S. Zhu, Phys. Rev. C 78, 034308 (2008).

- [7] G. D. Dracoulis, G. J. Lane, F. G. Kondev, H. Watanabe, D. Seweryniak, S. Zhu, M. P. Carpenter, C. J. Chiara, R. V. F. Janssens, T. Lauritsen, C. J. Lister, E. A. McCutchan, and I. Stefanescu, Phys. Rev. C 79, 061303 (2009).
- [8] F. G. Kondev, G. D. Dracoulis, and T. Kibedi, At. Data Nucl. Data Tables 103–104, 50 (2015).
- [9] J. Perkowski, J. Andrzejewski, J. Srebrny, A. M. Bruce, C. Droste, E. Grodner, M. Kisieliński, A. Korman, M. Kowalczyk, J. Kownacki, A. Krol, J. Marganiec, J. Mierzejewski, T. Morek, K. Sobczak, W. H. Trzaska, and M. Zielińska, Eur. Phys. J. A 42, 379 (2009).
- [10] T. Morek and the Warsaw OSIRIS II Collaboration, Acta Phys. Pol. B 32, 2537 (2001).

- [11] E. A. McCutchan, R. F. Casten, V. Werner, R. J. Casperson, A. Heinz, J. Qian, B. Shoraka, J. R. Terry, E. Williams, and R. Winkler, Phys. Rev. C 87, 057306 (2013).
- [12] A. A. Sonzogni, Nucl. Data Sheets 103, 1 (2004).
- [13] C. M. Baglin, Nucl. Data Sheets 111, 275 (2010).
- [14] J. Burde, R. M. Diamond, and F. S. Stephens, Nucl. Phys. 85, 481 (1966).
- [15] J. Perkowski, J. Andrzejewski, T. Abraham, W. Czarnacki, C. Droste, E. Grodner, L. Janiak, M. Kisieliński, M. Kowalczyk, J. Kownacki, J. Mierzejewski, A. Korman, J. Samorajczyk, J. Srebrny, A. Stolarz, and M. Zielińska, Acta Phys. Pol. B 43, 273 (2012).
- [16] A. S. Davydov and G. F. Filippov, Nucl. Phys. 8, 237 (1958).
- [17] A. Bohr and B. R. Mottelson, *Nuclear Structure* (World Scientific, London, UK, 1999).
- [18] J. Mierzejewski, J. Srebrny, H. Mierzejewski, J. Andrzejewski, W. Czarnacki, C. Droste, E. Grodner, A. Jakubowski, M. Kisieliński, M. Komorowska, A. Kordyasz, M. Kowalczyk, J. Kownacki, A. Pasternak, J. Perkowski, A. Stolarz, M. Zielińska, and R. Anczkiewicz, Nucl. Instrum. Methods Phys. Res., Sect. A 659, 84 (2011).
- [19] J. Andrzejewski, A. Krol, J. Perkowski, K. Sobczak, R. Wojtkiewicz, M. Kisieliński, M. Kowalczyk, J. Kownacki, and A. Korman, Nucl. Instrum. Methods Phys. Res., Sect. A 585, 155 (2008).
- [20] J. Perkowski, J. Andrzejewski, L. Janiak, J. Samorajczyk, T. Abraham, C. Droste, E. Grodner, K. Hadyńska-Klek, M. Kisieliński, M. Komorowska, M. Kowalczyk, J. Kownacki, J. Mierzejewski, P. Napiorkowski, A. Korman, J. Srebrny, A. Stolarz, and M. Zielińska, Rev. Sci. Instrum. 85, 043303 (2014).

- [21] D. C. Radford, Nucl. Instrum. Methods Phys. Res., Sect. A 361, 297 (1995).
- [22] J. Samorajczyk, J. Andrzejewski, L. Janiak, J. Perkowski, J. Skubalski, and A. Stolarz, Acta Phys. Pol. B 43, 325 (2012).
- [23] T. Kibedi, T. W. Burrows, M. B. Trzhaskovskaya, P. M. Davidson, C. W. Nestor, and C. W. Nestor, Nucl. Instrum. Methods Phys. Res., Sect. A 589, 202 (2008).
- [24] T. Venkova, T. Morek, G. V. Marti, H. Schnare, A. Kramer-Flecken, W. Gast, A. Georgiev, G. Hebbinghaus, R. M. Lieder, G. Sletten, K. M. Spohr, K. H. Maier, and W. Urban, Z. Phys. A 344, 417 (1993).
- [25] G. D. Dracoulis, P. M. Walker, and F. G. Kondev, Rep. Prog. Phys. 79, 076301 (2016).
- [26] B. Crowell, P. Chowdhury, D. J. Blumenthal, S. J. Freeman, C. J. Lister, M. P. Carpenter, R. G. Henry, R. V. F. Janssens, T. L. Khoo, T. Lauritsen, Y. Liang, F. Soramel, and I. G. Bearden, Phys. Rev. C 53, 1173 (1996).
- [27] S. Nilsson and I. Ragnarsson, *Shapes and Shells in Nuclear Structure* (Cambridge University Press, Cambridge, UK, 1995).
- [28] M. A. J. Mariscotti, G. Scharff-Goldhaber, and B. Buck, Phys. Rev. 178, 1864 (1969).
- [29] L. Próchniak and S. Rohoziński, J. Phys. (London) G 36, 123101 (2009).
- [30] K. Wrzosek-Lipska, L. Próchniak, M. Zielińska, J. Srebrny, K. Hadyńska-Klek, J. Iwanicki, M. Kisieliński, M. Kowalczyk, P. J. Napiorkowski, D. Pietak, and T. Czosnyka, Phys. Rev. C 86, 064305 (2012).
- [31] P. J. Napiorkowski, DF code, accessible online at http://www.slcj.uw.edu.pl/~pjn/DF/DF.htm.