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Improvement of signal to noise ratio in Electro Optical Probing technique by wavelets filtering

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Abstract

Electro Optical Probing (EOP) technique is an efficient backside contactless technique to measure waveforms in modern VLSI circuits. The signal related intensity variation of the reflected beam is very weak therefore, to acquire a signal with enough Signal to Noise Ratio, averaging techniques are usually performed. Resulting acquisition time for one waveform are too long to implement point to point probing to image mode. To overcome this limitation, we have developed a new filtering by wavelets approach to keep a good SNR while significantly reducing this acquisition time. It opens the doors to new multipoint probing applications. In this paper, we describe the technique, its efficiency in terms of SNR, execution time and limits.

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1. Introduction

In addition to light emission techniques, methods based on laser exploit optical stimulation or optical properties of reflected beam [1]. Electro Optical Probing is a popular timing-analysis laser-based technique [2], using Franz-Keldysh effects and free carrier absorption. Heinrich was the precursor of EOP approach [3] by proposing a non-invasive method which uses an infrared laser measuring the modulation of the free carrier density induced by the variation of electric potentials inside bipolar transistors. At the end of the nineties, a commercial application of the LVP technique was developed by Schlumberger Technologies Inc [4]. The source used was a pulsed laser, wavelength of 1.06 microns, 35 ps pulse duration.

Since its introduction, Electro Optical Probing has become an essential tool to the failure analysis (FA) and design debug communities [2]. In backside EOP analysis, pulsed or continuous laser beam is focused on a node of the chip which has been thinned. Thereafter, the reflected beam properties are analyzed.

The reflected signal mostly contains usual optical reflection from metal lines and a very weak signal related to free carrier absorption and bandgap modulation difficult to extract from noise. Techniques such as averaging [5] and frequency-domain measurements [6] have been implemented in probing and image modes. Averaging process is quite efficient in probing mode but it results at least in seconds duration to probe each node. This single waveform acquisition duration prevents EOP to probe each point of the device to build a waveform database of the full device. It will last from days to weeks to do it. Using frequency analysis in image mode is pretty fast but timing information is lost as a scan gives only amplitude information on one frequency inside the device. Therefore, in order to build a waveform database of the full device or just to reduce acquisition time to acquire thousands of nodes in a batch process (automatically moves to the next node, focus, slightly defocus up and down and each time scans a small area to finally extract the best waveform), it is mandatory to reduce processing time for each waveform while keeping a reasonable SNR. This paper introduces a new processing scheme based on wavelet transform to achieve this goal. We firstly remind some EOP background. The second section is dedicated to the description of EOP acquisition setup. The third section introduces the complete processing sequence. The fourth section exhibits the SNR improvement by wavelets transform. A fifth section concerns examples of results. And before a conclusion a sixth section tells about the level of decomposition and the choice of the wavelet used for the filtering.

2. Electro Optical probing

EOP technique is still based on analysis of the reflected beam properties [7]. Intensity varies with temperature

change [8], charge density [4] or electric field [9]. The analyze of the properties of the reflected laser beam can be traced back to its origin, in order to obtain information on the physical parameter studied. Two wavelengths have been used for EOP, also known as LVP (Laser Voltage Probing, [10] [11]) : 1064 and 1340 nm. 1064 gives a better spatial resolution (shorter wavelength) and the laser beam absorption is sensitive to carrier density (free carrier absorption) and to small bandgap (Franz Keldish) variations. Nevertheless, absorption is important (less reflected beam intensity) and it induces slight Optical Beam Induced Current (OBIC) that could bias a little bit the measurements. 1340 nm is less absorbed, is not sensitive to Franz Keldish effect. Considering the free carrier absorption mechanism, EOP is based on the very weak useful part of the reflected signal. It means that noise coming from various sources (thermal, shotky, electronic ...) is often order of magnitude higher than this useful part of the signal. During the acquisition, a signal with a weak amplitude drowned in noise is measured. If the waveform is directly acquired without processing, the SNR is extremely low. The absorption coefficient varies according to equation (1) [12]. According to M. Rebai [12], the relative changes are often less than 10^{-3} less than those induced by temperature changes.

$$\alpha_{fc} = A \frac{\lambda^2 q^3}{4\pi^2 c_0^3 \epsilon_0 n_0} \left[\frac{N_e}{m_e^2 \mu_e} + \frac{N_h}{m_h^2 \mu_h} \right], \quad (1)$$

with α_{fc} = absorption coefficient variation, A = refinement coefficient, λ = wavelength, q = elementary charge, c_0 = celerity of light in vacuum, ϵ_0 = permittivity in vacuum, n_0 = refractive index in silicon, $[m_e, m_h]$ = concentration of electrons and holes, $[\mu_e, \mu_h]$ = mobility of electrons and holes, $[N_e, N_h]$ = number of electrons and holes.

3. Acquisition setup

To solve this problem and improve the SNR, our existing acquisition setup integrates signals by averaging. Experimentations were done on Tri-Phemos, device designed by HAMAMATSU Photonics.

The signal of the reflected beam is acquired by a photodiode and amplified. The output signal of the amplifier is sent to an oscilloscope which proceeds in 512 averages to improve the SNR in a first time. In a second time, this averaged signal is sent to a computer (with LABVIEW interface) which integrates by averaging several acquisitions (one acquisition corresponds to 512 oscilloscope averages). FIGURE 1a shows that the signal is submerged in noise if only one acquisition is taken into account. Our setup needs several averages, by consequences a lot of time is necessary to significantly improve SNR. To illustrate these explanations, an example of probing on a microcontroller STM32 was chosen. After some averages (10 averages in our case), we obtain the waveform in FIGURE 1b. We can notice that

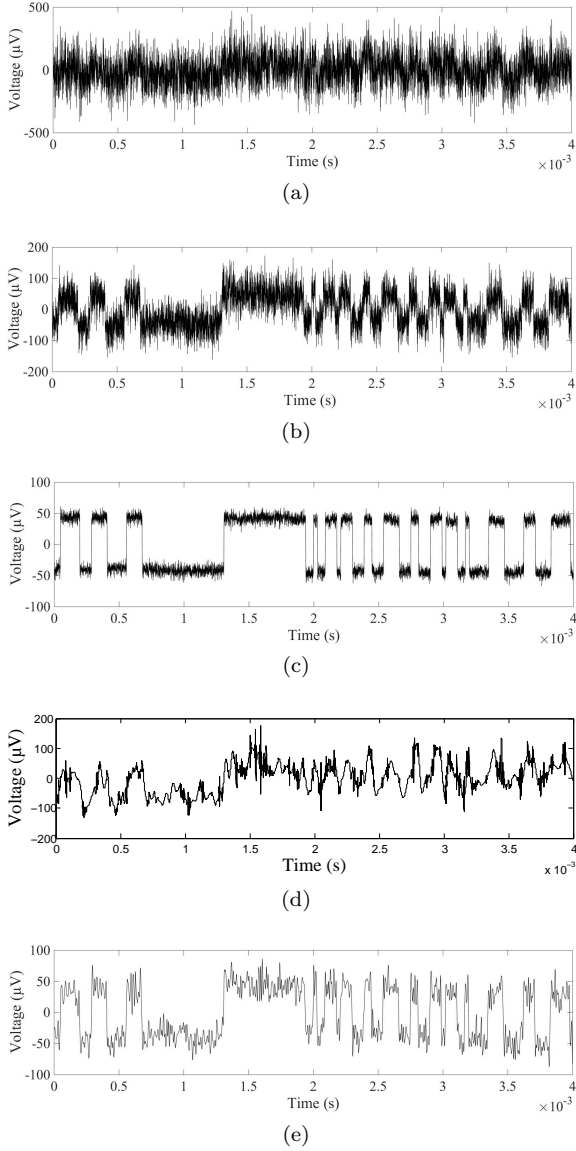


FIGURE 1: Probing on Digital/Analog converter STM32 : (a) One acquisition of EOP signal / Computing Time : ≈ 0.7 s / SNR = -19.96 dB. (b) Signal rebuild with 10 averages / Computing Time : ≈ 7 s / SNR = 3.09 dB. (c) Signal rebuild with 418 averages / Computing Time : ≈ 292 s / SNR = 37.39 dB. (d) Signal rebuild with wavelets transform and 1 average / Computing Time : ≈ 0.8 s / SNR = 1.9 dB. (e) Signal rebuild with wavelets transform and 10 averages / Computing Time : ≈ 8 s / SNR = 22.9 dB.

the SNR is very low. The number of averages has been increased to decrease the SNR. FIGURE 1c is the result after 418 averages.

Considering our hardware, an acquisition is achieved in 0.7s. It is very long in some cases as shown with the previous example. An approach with simple filters (Median, FIR, IIR) has been tested to improve the SNR and reduce acquisition time. If this kind of process is applied with a large scale, the signal will be indeed smoothed but short duration signals can be lost because of mandatory sample size (up to tens of samples) to get a reasonable noise re-

duction. That is why a process based on filtering by wavelets was implemented to improve both acquisition times and SNR. Example of result is represented in FIGURE 1. We precise that the aim of this process is to decrease the number of averages in order to reduce acquisition time while having a good SNR. For this example we have taken the same signal as previously but only 10 averages are used. Visually, we can notice the improvement of the SNR. In addition the acquisition time is reduced due to the decreasing of averages. For the same acquisition time (7 s here), the SNR is significantly improved. The computing time for wavelet transform can be evaluated in few *ms*. The filtering process by wavelets transform is explained below.

4. SNR improvement by wavelets transform

4.1. Multiresolution analysis : discrete wavelet transform

Since few years, several approaches have emerged in signal processing in order to remove the noise in signals. In [13], it is said that these new methods with wavelets give better results than Wiener filtering. Wavelets transform can be adapted to the discrete set. The size of the information could be reduced by choosing a level of detail. In our case, we use one aspect of wavelets : the multiresolution decomposition, which is very used in image processing because of its performance [14]. It is recalled that in failure analysis, wavelets have ever been applied to perform the approach by Time-Resolved Imaging in light emission [15]. This reference used the Continuous Wavelet Transform to determine a frequency while we use the discrete wavelet transform (DWT) to filter the signal. [16] and [17] explain the theory of the DWT. Given a signal \mathbf{s} of length N , the DWT consists of $\log_2 N$ stages at most. The first step produces, starting from \mathbf{s} , two sets of coefficients : approximation coefficients CA_i , and details coefficients CD_i , with $i = [1, \dots, n]$. These vectors are obtained by convoluting \mathbf{s} with an expression equivalent to a low-pass filter (l_d) for approximation, and with another equivalent to an high-pass filter (h_d) for details, followed by under-sampling [16]. (l_d) and (h_d) correspond exactly with impulse response of low and high-pass filter respectively. These coefficients are described such as

$$CD_i[n] = \sum_{k=-\infty}^{\infty} h_d[k]s[2n - k], \quad (2)$$

$$CA_i[n] = \sum_{k=-\infty}^{\infty} l_d[k]s[2n - k], \quad (3)$$

where n and k denote discrete time coefficient, and $i \in \mathbb{Z}$. In this way, the signal \mathbf{s} can be written as

$$s[n] = \sum_{k=-\infty}^{\infty} (CD_i[k]h_r[2k - n] + CA_i[k]l_r[2k - n]), \quad (4)$$

where l_r and h_r are reconstitution filters. Next step splits the approximation coefficient CA_1 in two parts using the

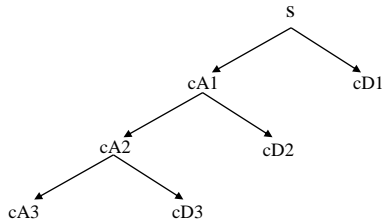


FIGURE 2: Multiresolution decomposition tree for level $L = 3$.

same scheme, replacing s by CA_1 , and producing CA_2 and CD_2 , and so on. The wavelet decomposition at level L has the following structure : $[CA_i, CD_i, \dots, CD_1]$. FIGURE 2, represents this structure with terminal nodes.

Now the important step, is to understand how to denoise the signal S . For that purpose, an approach by coefficients thresholding was chosen [18] and described in the next section.

4.2. Coefficients thresholding

According to the literature, it exists different kinds of thresholding for the wavelets coefficients [13] :

- **Soft thresholding** : The absolute value of all the wavelets coefficients is compared to a threshold T . If this value is greater than T the threshold is subtracted from any coefficient that is greater than the threshold. Others are set to zero.
- **Hard thresholding** : Hard thresholding sets any coefficient less than or equal to the threshold T to zero. Others are preserved.
- **Universal thresholding** : the value called *universal*, is defined by :

$$T_{thresh} = \sigma \sqrt{2 \log(N)} \quad (5)$$

where N is the length of the signal and σ the noise's standard deviation. Here, T_{thresh} is used with hard thresholding. In several applications, noise is most of the time white and gaussian. This kind of white gaussian noise (WGN) is a random signal with constant power spectral density. WGN whose representation is given by (6), is independent and identically distributed (i.i.d) and drawn from a zero-mean normal distribution with variance σ^2 .

$$WGN \sim N(0, \sigma^2) \quad (6)$$

According to (6), only σ^2 is unknown. That is why wavelets are useful in our study. Here, only the standard deviation could be estimated. In rarely cases the noise is assumed but in others, it can be estimated by using the Median Absolute Deviation (MAD). This method has been introduced by Donoho and Johnstone in 1994 [19]. MAD is the median absolute deviation of the empirical wavelet coefficients corresponding to the highest level j_1 . The reason for using these highest level coefficients for the variance estimation, is that they are mostly constituted of noise [20]. By consequences the estimated variance is given by

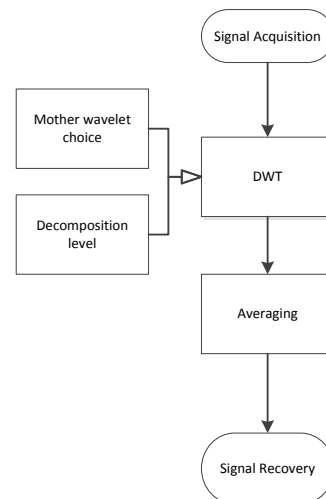


FIGURE 3: Flowchart of the filtering by wavelets.

$$\sigma^2 = \left(\frac{MAD}{0.6745} \right)^2 \quad (7)$$

where 0.6745 is the 0.75- quantile of the standard normal distribution and

$$MAD((w_j)) = Median((|w_j|)_j) \quad (8)$$

with w_j , the wavelets coefficients. Thus, σ^2 is now known and the threshold given in (5) can be computed. For a better understanding, a flowchart of our new process is illustrated in FIGURE 3.

5. Application, results and discussion

5.1. Results on STM32 microcontroller

The process is applied on digital signal acquired on a 90 nm microcontroller STM32, more precisely on the digital analog converter. The topographic image is reported in FIGURE 4. On this picture, we can notice a yellow cross which represents the pointer where the probing is applied. FIGURE 5 illustrates the acquired waveform and its wavelets coefficients decomposition. For this example we have decomposed with four levels with an *Haar* mother wavelet. On this picture we start by decomposing the original signal with wavelets. The next step consists to apply a threshold for the coefficients. And finally we go back to the time domain. As you can see at the right in FIGURE 5, we can considerably denoise the signal.

5.2. Signal to Noise Ratio

Previously, it has been seen that it was possible to denoise the signal. It could be interesting to compare this new method with available filtering method in the LVP field. Our filtering by wavelets is compared to filtering by

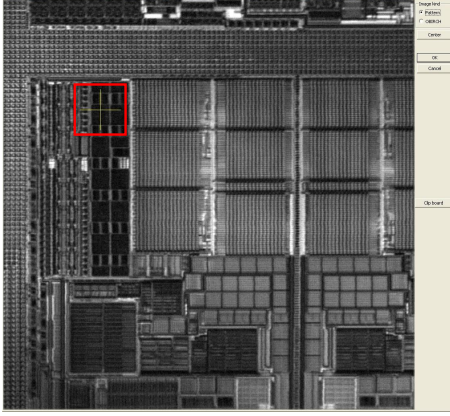


FIGURE 4: Pattern of microcontroller Digital/Analog converter (DAC) STM 32 and probing area symbolized by the yellow cross.

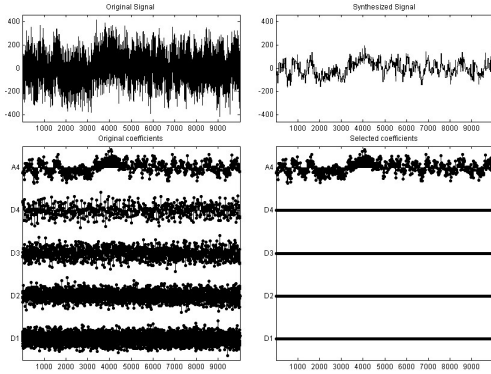


FIGURE 5: Wavelets decomposition with four levels. Top left : Noised signal/ Bottom left : Wavelets coefficients/Top right : Denoised signal/Bottom right : Thresholded coefficients.

averaging and median filter. FIGURE 6 represents the evolution of the SNR in function of the number of averages for each case. Here SNR is given by the following equation :

$$SNR_{(dB)} = 10 \log_{10} \frac{\text{Var}(\text{Signal})}{\text{Var}(\text{Noise})} \quad (9)$$

where $\text{Var}(\text{Signal})$ and $\text{Var}(\text{Noise})$ correspond to the signal and noise variance respectively.

For each values of average, the SNR with filtering by wavelets is always higher than the SNR computed with average and median filter. It proves the efficiency of the filtering to reconstitute the signal with a good SNR. Now we will focus on the other key aspect of this study, more precisely the execution time and the reconstitution error (mean square error).

5.3. Acquisition time

After the examination of the SNR, we give some results concerning the acquisition time which is not a negligible parameter. In fact, by decreasing the number of averages, the acquisition time decreases. Different acquisitions have

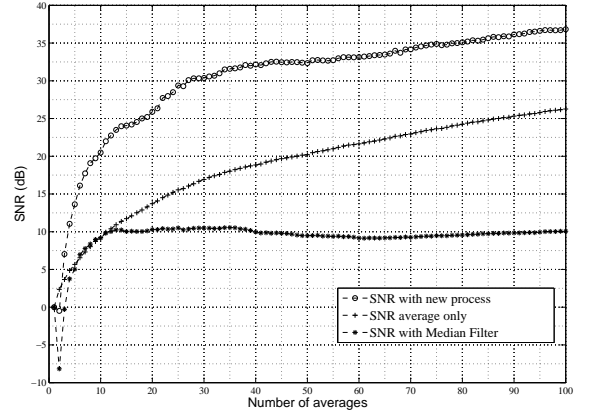


FIGURE 6: SNR evolution with wavelets, average and median filtering.

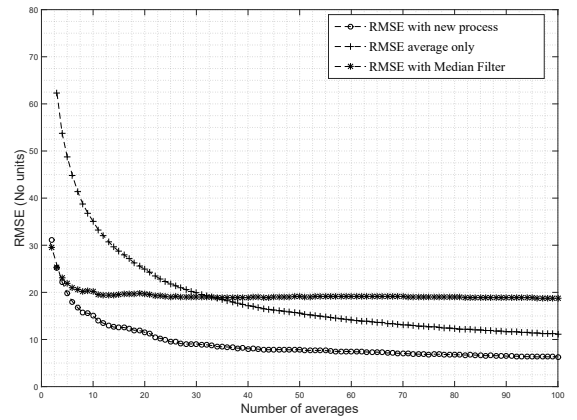


FIGURE 7: Mean Square Error evolution with new filtering process, averaging and median filtering.

been realized on some analogue or digital signals. For a same SNR, we have reported the execution time for all the signals. Results are referred in TABLE 1. In all cases, the execution time with only average and median filter is always higher than the computing time with wavelets. We notice a gain between 10 and 30 dB, depending on cases.

5.4. Reconstitution error : Mean Square Error

In this kind of study, it is interesting to compare quantitatively each method. That is reason the Mean Square Error (MSE) is used here. If \hat{x} is a vector of n predictions, and x is the vector of the true values, then the MSE of the predictor is given by :

$$MSE = \frac{1}{n} \sum_{i=1}^n (\hat{x} - x)^2 \quad (10)$$

Thus, the MSE evolution is computed for each kind of filter, average, median and wavelets and is represented in FIGURE 7. We can notice immediately that the MSE is minimized in the case of wavelets filtering for each number of

TABLE 1: Results of execution time on seven signals (analogue/digital) with wavelets and averaging, with median filter and with averaging only.

SNR = 30 db	Signal 1	Signal 2	Signal 3	Signal 4	Signal 5	Signal 6	Signal 7
Number of acquisitions with wavelets	5	15	10	20	14	25	6
Time with wavelets and averaging (s)	3.5	10.5	7	14	9.8	17.5	4.2
Number of acquisitions with averaging	20	70	50	100	40	120	25
Time with averaging (s)	14	49	35	70	28	84	17.5
Number of acquisitions with median filter	10	35	34	60	22	80	17
Time with median filter (s)	8	25	19	42	15	56	12

TABLE 2: Mean Square Error (MSE) in function of the mother wavelet choice.

Wavelet	MSE									
	Sig 1	Sig 2	Sig 3	Sig 4	Sig 5	Sig 6	Sig 7	Sig 8	Sig 9	Sig 10
1 Sym 2	0.0163	0.0166	0.0143	0.0157	0.0153	0.0148	0.0157	0.0164	0.0131	0.0139
2 Sym 4	0.0144	0.0149	0.0132	0.0144	0.0149	0.0142	0.0152	0.0161	0.0129	0.0133
3 Sym 8	0.0155	0.0152	0.0143	0.0167	0.0157	0.0138	0.0148	0.0168	0.0123	0.0128
4 Sym 16	0.0142	0.0145	0.0131	0.0154	0.0144	0.0153	0.0149	0.0157	0.0117	0.0129
5 Sym 32	0.0152	0.0153	0.0147	0.0153	0.0162	0.0149	0.0162	0.0159	0.0135	0.0134
6 Db 2	0.0151	0.0147	0.0152	0.0164	0.0156	0.0154	0.0153	0.0165	0.0141	0.0145
7 Db 4	0.0162	0.0155	0.0158	0.0163	0.0155	0.0168	0.0172	0.0176	0.0152	0.0148
8 Db 8	0.0161	0.0164	0.0167	0.0171	0.0166	0.0176	0.0175	0.0181	0.0164	0.0156
9 Db 16	0.0182	0.0178	0.0169	0.0159	0.0184	0.0194	0.0154	0.0189	0.0172	0.0157
10 Db 32	0.0193	0.0187	0.0184	0.0198	0.0193	0.0197	0.0156	0.0194	0.0184	0.0161
11 Coif 1	0.0161	0.0165	0.0162	0.0169	0.0158	0.0168	0.0171	0.0178	0.0154	0.0166
12 Coif 2	0.0144	0.0152	0.0154	0.0157	0.0152	0.0155	0.0169	0.0159	0.0147	0.0163
13 Coif 3	0.0155	0.0153	0.0162	0.0162	0.0164	0.0167	0.0173	0.0175	0.0149	0.0159
14 Coif 4	0.0145	0.0141	0.0144	0.0165	0.0150	0.0153	0.0156	0.0163	0.0137	0.0154
15 Coif 5	0.0152	0.0159	0.0157	0.0164	0.0163	0.0166	0.0169	0.0168	0.0142	0.0156
16 Haar	0.0198	0.0196	0.0214	0.0189	0.0221	0.0217	0.0198	0.0243	0.0197	0.0211
17 Meyer	0.0151	0.0153	0.0164	0.0158	0.0168	0.0174	0.0175	0.0172	0.0156	0.0158

average. The quantitative analysis with SNR and execution time is reinforced by the MSE to prove the efficiency of our process.

5.5. Other Example

To illustrate graphically our results, FIGURE 8 represents a comparison between the different kinds of filters used in LVP. This example has been realized on digital signal acquired on a 90 nm microcontroller STM32. In a first time, one acquisition is realized, see FIGURE 8(a), and then wavelets filtering is applied on 5 averaging, see FIGURE 8(b). Five averaging are represented in FIGURE 8(c) and finally median filter is applied on 5 averaging FIGURE 8(d) in order have a comparison. Each signal has been averaged five times in order to reduce the computing time. For a same number of averages, the signal in FIGURE 8(b) has clearly the best SNR.

6. Discussion

6.1. Decomposition Level

In this paper, prior parameters must be chosen, more precisely the decomposition level (DL) and the mother wa-

velet (MW). In fact the aim is to automate the filtering process. Concerning the decomposition level, it is possible to compute it automatically.

In the wavelets theory the DL_{max} is given by the following equation :

$$DL_{max} = \log_2 N \quad (11)$$

with N the signal length. Thus, if the signal length is known, DL_{max} can be computed easily.

6.2. Mother wavelet

Selection of mother wavelet (MW) could be based on qualitative or quantitative approaches. The chosen database are ten signals (analogue and digital). In this study, different MW with different vanishing moments were used : Symmlet(Sym), Daubechises(Db), Haar, Meyer and Coiflet (Coif). Instead of using qualitative approach such as similarity between signal and MW , this discussion will be based on the MSE value in function of the MW , i.e. the MSE is computed for each mother wavelet and for each vanishing moment. In fact for transient signals, using Haar wavelet could be pointed because its shape is similar to

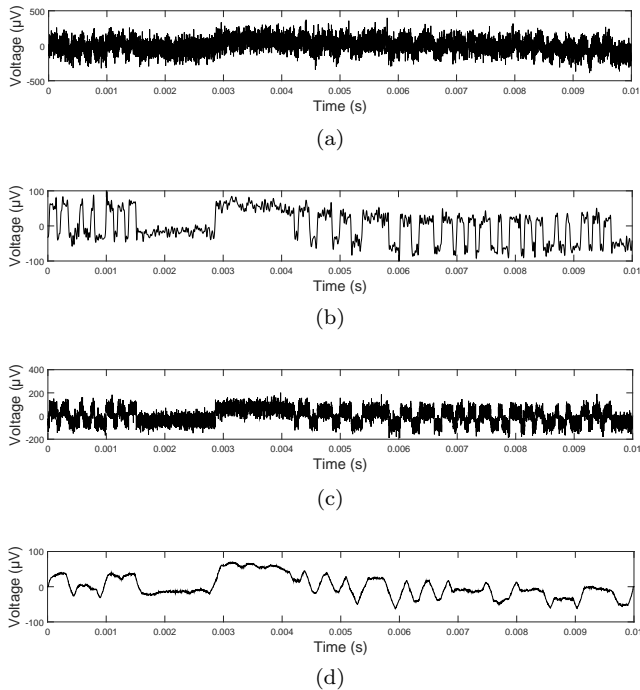


FIGURE 8: (a) Signal with one acquisition. (b) Signal with wavelets filtering (c) Signal with averaging filter (d) Signal with median filtering (size 50)

numeric signal. But it does not prove that it is the good choice, that is the reason a quantitative approach has been chosen. Results are listed in TABLE 2. In 80% of cases the *Sym16* mother wavelet gives the best results. These results give credit to the idea of choosing a mother wavelet to minimize the MSE.

Conclusion and perspectives

Rebuild a weak signal is a real challenge especially when it is drowned in noise. In this paper, a new method based on compression has been reported. This process could be useful for the FA community because it allows the expert to significantly save time during the acquisition. Therefore it is partially automated, in fact the mother wavelet choice is a key step of the process and the most difficult. If the MW is chosen at the beginning, the process is completely automated. In the event the expert is not satisfied with result, he can manually adjust all the parameters to optimize the final SNR.

In terms of perspectives, this process opens the door to new multipoint probing applications and allows the FA community to use signal processing techniques instead of expensive hardware.

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