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## ▶ To cite this version:

Guido Schreurs, Susanne J.H. Buiter, Jennifer Boutelier, Caroline Burburry, Jean-Paul Callot, et al.. Benchmarking analogue models of brittle thrust wedges. Journal of Structural Geology, 2016, 92, pp.116-139. 10.1016/j.jsg.2016.03.005 . hal-01449311

## HAL Id: hal-01449311 https://hal.science/hal-01449311

Submitted on 7 Jan 2021

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## Benchmarking analogue models of brittle thrust wedges

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#### Abstract :

We performed a quantitative comparison of brittle thrust wedge experiments to evaluate the variability among analogue models and to appraise the reproducibility and limits of model interpretation. Fifteen analogue modeling laboratories participated in this benchmark initiative. Each laboratory received a shipment of the same type of quartz and corundum sand and all laboratories adhered to a stringent model building protocol and used the same type of foil to cover base and sidewalls of the sandbox. Sieve structure, sifting height, filling rate, and details on off-scraping of excess sand followed prescribed procedures.

Our analogue benchmark shows that even for simple plane-strain experiments with prescribed stringent model construction techniques, quantitative model results show variability, most notably for surface slope, thrust spacing and number of forward and backthrusts. One of the sources of the variability in model results is related to slight variations in how sand is deposited in the sandbox. Small changes in sifting height, sifting rate, and scraping will result in slightly heterogeneous material bulk densities, which will affect the mechanical properties of the sand, and will result in lateral and vertical differences in peak and boundary friction angles, as well as cohesion values once the model is constructed. Initial variations in basal friction are inferred to play the most important role in causing model variability.

Our comparison shows that the human factor plays a decisive role, and even when one modeler repeats the same experiment, quantitative model results still show variability. Our observations highlight the limits of up-scaling quantitative analogue model results to nature or for making comparisons with numerical models. The frictional behavior of sand is highly sensitive to small variations in material state or experimental set-up, and hence, it will remain difficult to scale quantitative results such as number of thrusts, thrust spacing, and pop-up width from model to nature.

#### Highlights

A quantitative comparison of thrust wedge models from 15 analogue modeling laboratories is presented.
 Analogue models show variability, most notably for surface slope, thrust spacing and number of forward and backthrusts.
 Model variability is most likely controlled by initial variations in basal friction.
 Our comparison highlight the limits of up-scaling quantitative analogue model results to nature.

**Keywords** : Thrust wedges, Brittle wedges, Shear zones, Analogue modeling, Benchmarking, Critical taper, Sand, Friction, Cohesion

#### 240 **1. Introduction**

241

242 Scaled analogue experiments have a long history of modeling geological processes. Analogue 243 models built of materials such as sand, silicone or clay have helped geoscientists to gain 244 insights into the kinematic and dynamic evolution of a wide variety of geological structures. 245 However, as for all models, their results reflect the initial boundary conditions, the choice of 246 materials, the modeling apparatus and the technique of building the model. Unfortunately, 247 many publications on analogue modeling do not adequately record experimental details and 248 material properties, making a detailed comparison of model results among different 249 laboratories simulating similar geological processes difficult. Additionally, experiments are 250 rarely re-run to test the reproducibility and to determine the intrinsic variability of model 251 results.

252

253 Schreurs et al. (2006) were the first to report a direct comparison of scaled analogue 254 experiments to test the reproducibility of model results amongst ten analogue modeling 255 laboratories. One of the two experimental set-ups chosen in their comparison was a brittle 256 thrust wedge experiment (Fig. 1). The experimental set-up, the model-building technique, and 257 the material covering walls and base were all prescribed. However, each laboratory used its 258 own granular material to simulate brittle deformation. Consequently, in the comparison of 259 Schreurs et al. (2006) the material properties can be considered as extrinsic and were a major 260 source of model variability.

261

The qualitative evolution of all models was broadly similar (Fig. 2) with the development of a thrust wedge characterized by in-sequence forward thrusting and by minor back thrusting. However, significant quantitative variations existed between models in parameters such as the spacing between thrusts, their dip angles, number of forward and back thrusts and surface slopes.

267

INSERT Fig. 1. Experimental set-up used in model comparison experiments by Schreurs et al., (2006). Model
consists of a 3.5 cm-thick sand layer with an embedded microbeads layer and an overlying sand wedge with a
surface slope of 10° adjacent to the mobile wall. All walls are covered by Alkor foil. Figure reproduced from
Schreurs et al. (2006) with permission from the Geological Society of London.

273 274

275 INSERT Fig. 2. Model comparison showing crosssections through thrust wedge after 2, 6 and 14 cm of 276 shortening. The experimental set-up is shown in Fig. 1. The sections of Bern and IFP Rueil Malmaison are X-ray 277 computer tomography (XRCT) images through the center of the model, whereas the remaining sections are 278 sidewall observations. Microbeads layer indicated by "m". Figure modified after and reproduced from Schreurs 279 et al. (2006) with permission from the Geological Society of London.

280

281 In the analogue modeling comparison by Schreurs et al. (2006), each laboratory used its own 282 granular material and differences existed in terms of material properties such as grain size, 283 grain shape and grain size distribution. Hence, we suspect that the resulting inherent 284 variations in material properties between the different labs may have been responsible for 285 differences in the evolution of the experimental models. Lohrmann et al. (2003), for example, 286 determined that the kinematics of thrust wedges is largely a function of their material 287 properties. Differences in the observation techniques used to monitor the evolution of 288 structures also contributed to model variability. Some research groups observed structures 289 through transparent sidewalls, where sidewall friction is highest, whereas other labs used X-290 ray CT (XRCT) techniques to observe model evolution at the center of the model, where the 291 effects of sidewall frictional stresses are less.

292

293 The outcome of the analogue comparison study by Schreurs et al. (2006) motivated us to 294 propose new comparison experiments, with the aim to better understand the variability 295 between models by discriminating extrinsic versus intrinsic variability. The main differences 296 with the previous analogue model comparison are that in the present study we not only 297 prescribe stringent model-building techniques, but all participating laboratories use exactly 298 the same type of analogue materials for their experiments. By harmonizing boundary 299 conditions and material properties we isolate intrinsic variability related to sources such as 300 inherent randomness or other less obvious conditioning parameters (e.g., air humidity).

301

302 We also decided to choose simple experimental designs using brittle frictional materials only 303 to minimize structural complexity and to better assess structural variability. Our new 304 experiments are thrust wedge experiments that have frequently been performed in the analog 305 modeling community. We choose three different experiments, referred to as experiment 1, 2 306 and 3, respectively. In each of these experiments deformation is imposed by displacement of 307 one mobile, vertical wall. For practical reasons the maximum shortening is limited to 10 cm. 308 This allowed sand box dimensions to be smaller than for larger amounts of shortening, and 309 thereby allowed more labs to participate. Fifteen analogue modeling laboratories joined in this 310 comparison conducting the experiments in their local laboratory environment. In order to 311 isolate the personal impact on experiments, two researchers ran models using the 312 experimental apparatus from the laboratory in Bern. These models are referred to as "Bern" 313 and "GFZ@Bern", respectively.

314

In a companion paper, Buiter et al. (2016) present the results of a comparison of up to 11 numerical codes, simulating the same experimental set-ups, with the numerical material properties following the analogue material properties as closely as possible. Major sources of variability here are differences in the implementation of boundary conditions and subtle differences between numerical solvers.

320

321

#### 322 **2. Modeling approach**

- 323
- 324 2.1. Material properties

325

Each laboratory received a shipment of the quartz and corundum sand that is routinely used at the analogue modeling laboratory of the Institute of Geological Sciences at the University of Bern. Laboratories were asked to store the sands in a dry place for at least one month before conducting experiments and to record room temperature and humidity during experimental runs.

- 331
- 332 2.1.1. Physical characteristics
- 333

The physical characteristics of the sands are summarized in Figure 3. The quartz sand is a natural Triassic sand from a quarry at Schnaittenbach (Germany), whereas the corundum sand is derived from bauxite. The quartz sand has a fairly homogeneous grain size distribution with 90% of the grains falling within the 125 - 175 µm fraction. The brown corundum sand has a 338 more heterogeneous grain size distribution with 70% of the grains falling between 88 and 125 339 um. Bulk density depends both on the material and on the physical handling technique, i.e. 340 whether material is sieved or poured. As shown previously by Krantz (1991), Schellart 341 (2000), Lohrmann et al. (2003), Panien et al. (2006), Gomes (2013) and Maillot (2013) the 342 bulk density of sieved granular materials is higher than the bulk density of poured granular 343 materials. In our experiments, the sands are sieved from a height of 20 cm using prescribed 344 sieve (Appendix A-1) and sieving rates. The bulk densities of quartz and corundum sand sieved from 20 cm height are 1.6 g/cm<sup>3</sup> and 1.9 g/cm<sup>3</sup>, respectively. 345

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- 347
- 348

349 INSERT Fig. 3. Physical characteristics of the quartz and corundum sand used in the experiments (modified
350 after Panien et al., 2006). Upper and lowermost images are photographs and SEM images, respectively. Width
351 of each SEM image is 1740 µm.

352

#### 353 2.1.2. Friction angles and cohesion

354

355 The mechanical properties of the sands have been determined with a ring-shear tester, model 356 RST-01.pc (Schulze, 2008), at the GFZ in Potsdam. The sands were stored for one month 357 prior to testing to adapt to the air-conditioned environment. Sand storage and ring-shear 358 testing occurred at temperatures of  $23 \pm 1^{\circ}$  C and atmospheric humidity of  $45 \pm 5\%$ . The 359 ring-shear tester allows the determination of the internal and boundary friction angles of 360 granular materials at low normal stresses similar to those observed in analog model 361 experiments (< 20 kPa). The ring-shear tester consists of an annular shear cell holding the 362 tested material, a normal loaded shear lid placed onto the cell, and tie rods measuring the 363 shear stress. Using a ring-shear tester, Lohrmann et al. (2003) could show that granular 364 materials such as quartz sand do not have constant frictional properties. Upon loading the 365 granular materials undergo initially a limited elastic deformation, which is followed by strain 366 hardening preceding failure at peak strength and subsequent strain softening until a stable 367 strength value is reached (Fig. 4). The strain localisation at peak strength is associated with a 368 material compaction-decompaction cycle as inferred from volumetric changes, with 369 maximum dilation rates close to peak strength when faults form (Lohrmann et al., 2003). 370

- 371 INSERT Fig. 4. Shear stress plotted versus shear strain for quartz sand (modified from Lohrmann et al., 2003;
- 372 Panien et al., 2006). Strain softening from peak strength to stable strength correlates with dilation of sand.
- 373

374 The ring-shear tests for measuring internal friction and boundary friction differ in the design 375 of the shear cell and lid. The setup for measuring internal friction ensures that shear 376 displacement occurs entirely within the sand such that only intergranular deformation occurs, 377 whereas the setup for measuring boundary friction ensures that deformation occurs between 378 sand and a surface with controlled roughness, in our case a transparent and super polished 379 self-adhesive foil (brand Alkor-Venilia, article nr. 120010; this foil has been renamed, and is 380 now available as Gekkofix article nr. 11325 from Van Merksteijn Plastics B.V. in the 381 Netherlands, www.gekkofix.nl).

382

The physical handling technique used to fill the annular cell of the ring-shear tester was identical to the one used to determine the bulk density and to the one prescribed in our thrust wedge experiments, i.e. material was sifted through a prescribed mesh sieve from c. 20 cm height into the shear cell at a filling rate of c. 250 ml/min. Excess material was subsequently scraped off before assembling shear cell and shear lid.

388

Ring-shear measurements were performed at a shear velocity of 3 mm/min for 4 minutes at a given normal load. For each test, measurements were done for different normal stresses ranging from c. 500 Pa to c. 2240 Pa in steps of c. 435 Pa, and for each particular normal stress, peak strength and stable strength values were determined. Each ring-shear test was repeated three times for both quartz sand and corundum sand.

394

395 Measured shear stress values at peak strength and at stable strength are plotted against the 396 applied normal stresses and a linear regression analysis is applied to the data, to obtain the 397 friction coefficient,  $\mu$ , which corresponds to the slope of the line and the friction angle,  $\phi$ , 398 which is tan<sup>-1</sup> $\mu$ . The cohesion is the linearly extrapolated value at zero normal stress. We 399 report the range of friction angles and (apparent) cohesion values in Table 1.

- 400
- 401
- 402 INSERT Table 1. Range of mechanical properties of quartz and corundum sand obtained with a ring-shear
- 403 tester. Values are rounded to nearest degree for friction angles and to nearest whole number for cohesion. n is
- 404 *number of ring-shear tests at normal stresses ranging from c. 500 to 2240 Pa.*

405 406

407 The angle of internal friction at peak strength ( $\phi_p$ ) of the tested quartz and corundum sand are 408 about 35-36°. The angles of internal friction at stable strength ( $\phi_s$ ) are in both cases lower, 409 with values around 30-31°. The angle of boundary friction ( $\phi_b$ ) varies more for quartz sand on Alkor foil, with values between 15° and 21°, than for corundum sand on Alkor foil with 410 values of  $24^{\circ} \pm 1^{\circ}$ . At the range of applied normal stresses the cohesion at peak strength (C<sub>p</sub>) 411 412 for both granular materials is in the order of a few tens of Pa. Boundary cohesion values  $(C_b)$ 413 range from 14 to 141 Pa for quartz sand and from 23 to 44 Pa for corundum sand. The large 414 spread in cohesion values is due to the linear extrapolation to zero normal stress on shear 415 stress versus normal stress curves. Strain softening corresponds to the weakening of the shear 416 zone after its formation. By comparing the mean values of the peak internal friction 417 coefficient and the stable friction coefficient for each granular material, the mean strain 418 softening can be determined, which amounts to c. 15-20% for both quartz and corundum 419 sand.

420

421 Panien et al. (2006) used the same ring-shear tester at identical laboratory climatic conditions 422 to determine the material properties of the same quartz and corundum sand as used in this model comparison. Their filling procedure (filling height and rate) is identical to ours, albeit 423 424 with a slightly different sieve. The obtained values for repeated measurements correspond closely to ours. Their mean values for  $\phi_p$  of quartz and corundum sand are 36° and 37°, 425 respectively and their mean values for  $\phi_s$  are 31° and 32°, respectively. Using the same Alkor 426 427 foil, Panien et al. (2006) also found that boundary friction angles at peak strength and at stable 428 strength are lower for quartz sand than for corundum sand.

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## 431 *2.1.3. Dilation and elasticity*

432

Deformation of the granular materials used in our experiments occurs by localization along shear zones in combination with dilation. The dilation angles at peak strength for our dry quartz and corundum sand are difficult to determine with a ring-shear tester. It requires measurements of the changes in volumetric strain, but the volumetric strain depends on the width of the initial shear zone that forms. Assuming an initial shear zone width of about 10 times the average grain size (Panien et al., 2006), we obtain very small dilation angles of less
than 2°. Measurements of shear zone formation in dry sands indicate that dilation approaches
zero once the shear zone has formed (Lohrmann et al., 2003; Bernard et al., 2007).

441

442 The elastic behaviour of the granular materials is characterized by at least two elastic 443 parameters, e.g. Young's modulus E and Poisson's ratio v. Young's modulus is the ratio of 444 uniaxial stress and strain:  $E = \sigma/e$ , while Poisson's ratio is the negative ratio of transverse strain (e<sub>x</sub>) to longitudinal strain (e<sub>z</sub>) under conditions of uniaxial stress, i.e.  $v = -e_x/e_z$ . Another 445 446 elastic parameter is the bulk modulus K defined by the ratio of mean stress over volumetric 447 strain. K is related to E and v and can be expressed as K = E/(3(1-2v)). Importantly, one has 448 to differentiate between the elasticity of individual granular particles (which is in the order of 449 tens of GPa for sand) and the elasticity of the bulk solid, i.e. the structure made by many 450 grains in contact, which is generally much lower and the one relevant in our modelling 451 approach.

452

453 The bulk moduli (K) of dry quartz and corundum sand were measured performing loading-454 unloading cycles (maximum load: 20 kPa) on sieved sand samples with a uniaxial confined 455 compression tester at GFZ Potsdam. The values vary depending on the degree of compaction, 456 which increases mainly during the first few loading-unloading cycles. Linear regression 457 analysis of the stress-strain curves (up to a strain of 0.00003) during loading of the first ten 458 cycles suggests an effective bulk modulus of around 200 MPa for both sands under laboratory 459 conditions. Assuming a Poisson's ratio, v, of about 0.25 results in a Young's modulus E of 460 300 MPa. Though orders of magnitude smaller than for single grains these values are so high 461 that elastic deformation in the experiments is expected to be below the detection threshold of 462 even sophisticated optical strain measurement systems (e.g. microns when applying subpixel-463 resolution particle image velocimetry, Adam et al., 2005). Stress is therefore expected to 464 accumulate and relax without obvious deformation in sandbox experiments. This is in contrast 465 to more elastic modelling approaches where proper scaling of elasticity from nature to the 466 analogue model yields observable elastic effects (Rosenau et al., 2009).

467

468

469 2.2. Brittle thrust wedges

471 The formation of fold-and-thrust belts and accretionary wedges in compressional settings is 472 comparable to the process of forming a wedge of snow in front of a moving bulldozer with a 473 taper angle described by the critical taper theory (e.g. Davis et al., 1983; Dahlen et al., 1984; 474 Zhao et al., 1986; see Buiter et al., 2012 for an extensive review of brittle compressional 475 wedge models). The material being pushed will reach an equilibrium angle, the so-called 476 critical taper angle, which is the sum of the surface slope angle ( $\alpha$ ) and the basal dip angle of 477 the wedge ( $\beta$ ). The critical taper angle depends on the material properties within the wedge, 478 the pore fluid pressure and the strength of the decollement along the base of the wedge.

479

480 Under the assumption that the material deforms according to the Coulomb failure criterion 481 and that the base of the wedge is cohesionless (i.e.,  $C_b = 0$ ), the critical taper theory permits 482 the derivation of the critical taper angle for a dry sand wedge (pore fluid pressure is zero) 483 knowing the angle of internal friction, the internal cohesion and the angle of basal friction 484 (Fig. 5). Dahlen et al. (1984) show that a cohesionless wedge results in a perfectly triangular 485 form, whereas a wedge with a constant internal cohesion will acquire a concave upward 486 surface.

487

Fig. 5 shows wedge stability fields for cohesionless and internal cohesive sands with frictional properties that closely correspond to those obtained from ring-shear tests on our sands: for a cohesionless sand at peak strength and at stable strength, and for a cohesive sand at peak strength with depth-dependent internal cohesion (Buiter et al., 2016).

492

493 INSERT Fig. 5. Zoom of critical taper curves for cohesionless sand at peak strength ( $\phi_p = 36^\circ$ ,  $\phi_b = 15^\circ$  and C =494 0 Pa), cohesionless sand at stable strength ( $\phi_s = 31^\circ$ ,  $\phi_b = 15^\circ$  and C = 0 Pa), and a cohesive sand at peak 495 strength with depth-dependent cohesion ( $\phi_p = 36^\circ$ ,  $\phi_b = 15^\circ$  and C = 20 Pa cm<sup>-1</sup> times z, with z = depth, following 496 Zhao et al. (1986)).

497

498

Wedges in the stable field will slide stably without internal deformation as long as no new material is accreted. This is our experiment 1, which has an initial wedge shape with a horizontal base and a 20° surface slope (Fig. 5). Unstable, subcritical wedges will deform internally upon compression towards the critical taper angle. Our experiment 2 and 3 models with initial horizontal layering start out as subcritical wedges (Fig. 5).

506

507 Although each lab used its own experimental apparatus, all labs applied the same type of self-508 adhesive Alkor foil to cover the base and the four vertical walls of their experimental 509 apparatus in order to guarantee identical shear stresses at the boundaries. In addition, each lab 510 received a detailed document outlining the prescribed model-building techniques including 511 details on mesh sieve structure for model construction and leveling techniques (Appendix A). 512 The model was built by sifting sand through a sieve with specified mesh sieve from a height 513 of 20 cm at a filling rate of c. 250 ml/min. This procedure is identical to the one used to fill 514 the test cell during ring-shear test measurements. The minimum width of the model (measured 515 along the mobile wall) was prescribed at 20 cm. Model widths as well as laboratory 516 temperature and relative humidity are shown in Table 2.

- 517
- 518

519 INSERT Table 2. Overview of laboratory climatic conditions and model widths. Most laboratories performed
520 experiments 2 and 3 twice, and range of values for room temperature and relative humidity are indicated.
521 Exceptions to the prescribed modeling procedure are also given.

522 523

## 524 2.4. Model analysis

525

526 We analyse our models in a qualitatitave way by comparing cross-sectional views and top 527 views and in a quantitative way by cross section measurements. As boundary stresses created 528 significant drag of structures along the sidewalls, our visual comparison is done for sections 529 away from the sidewalls. Consequently, for models analysed in a conventional way by 530 physically cutting the model, we only show cross sections through the final stage of 531 deformation. However, for models analysed by X-ray computed tomography (XRCT) we 532 show the cross-sectional evolution at successive increments of mobile wall displacement, 533 hereafter termed shortening.

534

535 Our quantitative analysis consisted of measuring surface slope (Fig. 6a), thrust spacing 536 between forward thrusts (Fig. 6b), dip angle of newly formed forward thrusts at base, mid and 537 top (Fig. 6c), thrust initiation (i.e. at how much shortening a particular thrust forms) and 538 number of thrusts at the end of the experiment. We define a thrust as formed when it shows a 539 small, visible offset in cross section. As in the previous model comparison (Schreurs et al., 540 2006), two of us (Guido Schreurs and Susanne Buiter) performed the quantitative analysis by 541 measuring the aforementioned parameters in the same manner and averaging the obtained 542 values. In general the differences between the two measurers were small, with average 543 difference in slope values of 1-2° and maximum difference in dip values of 3°. Also 544 differences in measured distance values were generally small. In models analysed by XRCT 545 all parameters were measured using cross-sectional images taken at 0.5 cm increments of displacement for Experiment 1, and at 0.2 cm increments of displacement until 1 cm and 546 547 subsequently at 0.5 cm increments until 10 cm shortening for Experiments 2 and 3. 548 549 550 INSERT Fig. 6. Schematic illustration of measurements of a) surface slope, b) forward thrust spacing, and c) 551 thrust dip angles. Surface slope is measured as the best fitting line through the valleys (Stockmal et al., 2007) 552 and can only be determined once at least 2 thrusts have formed. Thrust spacing is measured horizontally from a 553 newly initiated in-sequence forward thrust to the previously formed forward thrust. 554 555 556 To document lateral variations of structures, we compared sections at five different positions. 557 As model width varied between laboratories, we defined the five sections in terms of along-558 strike model width at 25%, 50% - 2 cm, 50%, 50% + 2 cm, and 75% positions (see Fig. 7). 559 560 561 INSERT Fig. 7. Top view photograph illustrating position of cross sections at 25% (1), 50%-2 cm (2), 50% (3), 562 50% + 2 cm (4), and 75% (5) of model width (measured parallel to mobile wall, which moves here from bottom 563 to top). Model width is 80 cm in this particular experiment. 564

565

#### 566 **3. Experiment 1**

567

- 568
- 569 3.1. Experiment 1: Model set-up
- 570

571 In the first experimental set-up, a quartz sand wedge with a horizontal base ( $\beta = 0^{\circ}$ ) and a 572 surface slope ( $\alpha$ ) of c. 20° was constructed adjacent to the mobile wall (Fig. 8). The height of 573 the wedge immediately adjacent to the mobile wall is 3 cm. INSERT Fig. 8. Model set-up for experiment 1. Model building consisted of two steps (Fig. 9). In a first step quartz sand was sieved in the sandbox partly sloping towards the fixed wall (Fig. 9a). In a second step a template with a 20° slope-angle was attached onto each sidewall and excess material was scraped towards the tip of the wedge and taken out (Fig. 9b). Adjacent to the fixed wall, there was at least 5 cm space where no sand covered the base. The model was shortened 4 cm by inward movement of the mobile wall. Eleven analogue modeling laboratories ran experiment 1 once. INSERT Fig. 9. Model building procedure for experiment 1 shown in cross section. A template with the shape of the final wedge is attached on top of each sidewall to guide the scraper (see Appendix A-2). Stippled line indicates sand wedge before final scraping. 3.2. Experiment 1: Results Three intrinsic material parameters are important in the critical taper theory: the internal peak friction, internal cohesion, and basal friction. Of these three parameters, the basal friction of quartz sand is the least constrained, varying between 15 and 21° (Table 1). However, even when taking into account this uncertainty, the quartz sand wedge of experiment 1 is well within the stable domain. Hence, the wedge should slide stably without internal deformation and consequently the surface slope should remain constant throughout the experiment. All experiment 1 models do conform to the critical taper theory and are stable. The quartz sand wedge is translated along the horizontal base and is not affected by internal localized deformation. Apart from a slight slope change in the extreme front region of the wedge in a number of experiments, the overall surface slope remains constant (Fig. 10 and 11). 

608

609

610	INSERT Fig. 10. Evolution of experiment 1 model run at Bern after 0, 2 and 4 cm of shortening (a) XRCT
611	sections through centre of model, (b) top view photographs of model.
612	
613	
614	INSERT Fig. 11. Cross sections through centre of experiment 1 models after 4 cm of shortening. Sections of

- 615 Bern, GFZ@Bern, and IFP are XRCT images. Note that Toronto and Uppsala laboratories added extra sand on
- 616 the wedge before cutting cross section.

618	4. Experiment 2
619	
620	
621	4.1. Experiment 2: Model set-up
622	
623	In experiment 2 alternating horizontal layers of quartz and corundum sand are shortened by
624	inward movement of a mobile wall (Fig. 12). Both the base and the surface of the model are
625	horizontal ( $\alpha = \beta = 0^{\circ}$ ) and the "wedge" starts in the unstable field (Fig. 5). The minimum
626	length of the undeformed model, measured parallel to the movement direction of the mobile
627	wall, was 35 cm. The model had an initial thickness of 3 cm and directly overlies the base of
628	the model. Total shortening of the model by inward displacement of the mobile wall was 10
629	cm. No exit slot existed below the mobile vertical wall and the base of the model.
630	
631	
632	INSERT Fig. 12. Model set-up for experiment 2.
633	
634	Fourteen laboratories participated in experiment 2, running a total of 25 models, of which five
635	were analysed by XRCT.
636	
637	
638	4.2. Experiment 2: Results
639	
640	4.2.1. Evolution of models analysed by XRCT
641	
642	Fig. 13 shows the cross-sectional evolution through the centre of five thrust wedge models
643	analysed by XRCT after 1, 2, 6 and 10 cm of shortening. Movies showing additional stages in
644	the cross-sectional evolution are given in the journal's repository. Shortening is
645	accommodated by forward thrusts, which propagate in-sequence towards the foreland, and by
646	back thrusts.
647	
648	The first pop-up structure develops between 0.5 and 1 cm of shortening (Fig. 14) adjacent to
649	the mobile wall. The dip of the first forward thrust steepens slightly upwards, with dips

650 varying between 22° and 25° at the bottom, between 27° and 31° at the middle, and between (51 - 26) and 22° at the tag (Fig. 15c). The head there is first new an attraction of the first set of the fi

 $26^{\circ}$  and  $32^{\circ}$  at the top (Fig. 15a). The back thrust of the first pop-up strucure generally dips

steeper than the forward thrust, in particular near the base of the model. The variation in dip of the first-formed back thrust is large, with dip angles between 26° and 46° at the bottom, and between 27° and 45° at the middle and at the top (Fig. 15b). The width of the pop-up at the surface varies because of the considerable variation in dip of the back thrust. Models with a steep back thrust (Bern 2B and IFP 2A) have a narrower pop-up width than models with a shallow-dipping back thrust (Fig. 13; 1 cm of shortening).

658

659 After 2 cm of shortening a second back thrust has formed in all models, except in model Bern 660 2A. The first-formed forward thrust takes up most of the initial shortening and the first-661 formed back thrust is displaced along it (Fig. 13; 2 cm of shortening). A second in-sequence 662 forward thrust forms between 3 and 5.5 cm of shortening and further in-sequence forward 663 thrusts develop with progressive shortening. The spacing to the previously formed forward 664 thrust at the moment of initiation of a new forward thrust tends to increase for subsequent 665 thrusts (Fig. 14b). In general the dip of newly formed in-sequence thrusts near the base of the 666 model becomes shallower with progressive deformation

667

A second pop-up structure forms in all XRCT models, albeit at different stages: at 5.5 cm of
shortening for Bern 2A, at 6.5 cm for GFZ@Bern, and at 9 cm for Bern 2B, IFP 2A and IFP
2B. Back thrusts associated with this second pop-up generally cross-cut earlier-formed, now
inactive forward thrusts.

- 672
- 673

674 INSERT Fig. 13. Cross-sectional evolution through centre of experiment 2 models after 1, 2, 6 and 10 cm of
675 shortening as observed in XRCT images.

676

The surface slope evolution of the wedge for models analysed by XRCT is shown in Fig. 16
Oscillations in surface slope angles reflect the formation of new thrusts. All models except
Bern 2A show these oscillations. The Bern 2A model shows instead a steady increase in
surface slope.

- 681
- 682
- 683
- 684

685 686 687	INSERT Fig. 14. Quantitative comparison of experiment 2 models analysed by XRCT. (a) Amount of shortening at which a forward thrust forms at centre of model. (b) Spacing to previously formed forward thrust at the moment of initiation of a new, in-sequence forward thrust.
688	
689	
690 691	INSERT Fig. 15. Dip angles of successive in-sequence forward (a) and back thrusts (b) in centre of experiment 2 XRCT models, measured at ton, middle and bottom
692	
693	
694	INSERT Fig. 16. Surface slope evolution at centre of experiment 2 XRCT models. Only values that could be
695	reliably measured in XRCT images are given.
696	
697	4.2.2. Final deformation stage
698	
699	Cross sections through the centre of all experiment 2 models after 10 cm of shortening show a
700	series of forward and back thrusts directly adjacent to the mobile wall (Fig. 17). In addition,
701	most models show a second pop-up structure that formed in front. However, the models of
702	Kyoto, Parma, Piscataway 2A and 2B, and Stanford 2A lack this second pop-up structure and
703	consequently have higher surface slopes.
704	
705	
706	INSERT Fig. 17. Cross sections through centre of experiment 2 models after 10 cm of shortening. Width of each
707	panel shown is 25 cm. Note that some labs added a layer of sand before cutting the model. Cross sections from
708	Lille 2A and 2B are at 50%-2cm position. Image quality of cross sections from Stanford 2A and 2B was not good
709	enougn jor reproduction.
711	The top views for experiment 2 after 10 cm shortening are shown in Fig. 18 Approaching the
712	sidewalls of the models, thrusts are convex to the hinterland with the thrust wedge becoming
713	narrower and steeper. Along-strike structural changes are present in all models away from the
714	sidewalls with curved thrust segments and along-strike merging of thrusts. The along-strike
715	changes are also well visible in the cross-sectional wedge geometries shown for 5 different
716	locations in Fig. 19
717	100001010 III 1 IS. 17.
718	The surface slope is measured in cross sections at the 25% 50% and 75% positions and varies
710	hetween 4° and 24° (Fig. 20). Surface slones measured along one sidewall (0% position) are
11)	outreen i und 21 (115. 20). Surface stopes measured along one sidewan (070 position) are

shown for comparison and are, for one particular model, generally considerably higher than those measured at the other three positions. Variations in surface slope along strike within one model are generally small, with most models showing along-strike differences between maximum and minimum surface slope of less than 4° (Fig. 20). Only the Lille 2B model and Melbourne 2A model have higher along-strike differences of 6° and 11°, respectively.

725

The number of thrusts has also been measured at the 25%, 50% and 75% positions (Fig. 21). Models have between 3 and 5 forward thrusts at the end of the experimental run (10 cm of shortening), except Mexico 2A and 2B, and Piscataway 2A, which have a higher number of thrusts (up to 9), and Bern, which has only two forward thrusts (Fig. 21a). The number of backthrusts varies between 1 and 9, and in comparison with the forward thrusts, there is an overall higher along-strike variability in the number of backthrusts within one particular model.

- 733
- 734

735 INSERT Fig. 18. Top views of experiment 2 models after 10 cm of shortening showing along-strike structural 736 variability. Movement of mobile wall is from bottom to top Note that Lille 2A and 2B models have a grid of 737 corundum sand imprinted on the surface, whereas Mexico 2A and 2B models used prescribed sand mixed with 738 dark sand particles. All photos are shown at the same scale, given in the top left photo.

- 739
- 740

741 INSERT Fig. 19. Cross sections after 10 cm shortening for experiment 2 models at positions 25%, 50%-2 cm,
742 50%, 50%+2 cm and 75% (see Fig. 6) showing along-strike structural variability. Note that some laboratories
743 added a post-kinematic sand layer before wetting and sectioning.

744

745 INSERT Fig. 20. Surface slope after 10 cm of shortening at 25%, 50% and 75% positions for experiment 2 746 models. The surface slope could not be reliably measured on all cross-sectional images. Surface slopes for Lille 747 2A and Lille 2B models were measured at 50%-2cm position. Numbers above symbols indicate difference 748 between maximum and minimum slope angle within one particular model and are only given for those models in 749 which the surface slope could be determined at all three positions. Surface slope values along one sidewall (0% 750 position) are given for comparison and are generally higher.

- 751
- 752

753 INSERT Fig. 21. Number of forward and back thrusts at 25%, 50% and 75% position after 10 cm of shortening

- 754 for experiment 2 models. Numbers above symbols indicate along-strike differences in number of thrusts and are
- 755 only given for those models, in which thrusts could be reliably determined at all three positions.

756	
757	
758	4.2.3. Model similarities and variability
759	
760	The experiment 2 models share a number of similarities:
761	
762	(1) the development of forward thrusts propagating in-sequence and the formation of back
763	thrusts,
764	(2) the formation of a first pop-up adjacent to the mobile wall forming in all models before 1
765	cm of shortening
766	(3) the fairly uniform dip of the first forward thrust, which steepens slightly upwards,
767	resulting in a slightly listric thrust plane
768	(4) the first backthrust that forms close to the mobile backwall dips steeper than the first
769	forward thrust
770	(5) in top views thrust wedges are curved with a convex to the hinterland shape. Sidewall
771	friction results in a narrower and steeper wedge immediately along the sidewall when
772	compared to sections through the center of the model
773	
774	However, our quantification of experiment 2 model results shows that there are also important
775	variations, notably:
776	
777	(1) The number of forward thrusts and backthrusts that formed after a certain amount of
778	shortening is variable when comparing all models (Fig. 14a). For example, the number of
779	forward thrusts through the centre of the model after 10 cm shortening varies between 2 and
780	9, wheras the number of back thrusts varies between 1 and 9 (Fig. 21). Variability in the
781	number of thrusts within one particular model is less with a difference in number of thrusts
782	along strike varying from 0 to 3 (Fig. 21).
783	(2) The surface slope of the thrust wedge is highly variable. Whereas four out of the five
784	models analysed by XRCT show an oscillating behaviour in surface slope, reflecting new
785	thrust formation, Bern 2A model shows a steady increase in surface slope. After 10 cm of
786	shortening the surface slope through the centre (50% position) of all models varies between $4^\circ$
787	and 24°.
788	(3) Not all models develop a second pop-up structure. In case a second pop-up forms, the
789	associated back-thrusts cut in most cases previously formed forward thrusts in the hinterland.

790

The variations in overall wedge geometry result from local scale variations in thrust dips. Notably, the variability in dip of newly formed back thrusts is large, with dip angles ranging from 26° to 50°, and also the width of the initial pop-up structure through the centre of the models (Fig. 13) varies considerably due to varying dip angles of forward and in particular back thrusts.

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### 798 *4.3. Experiment 2 model and the critical taper theory*

799

800 The internal peak friction angles of the quartz and corundum sand used in experiment 2 are 801 nearly identical (Table 1) and a value of  $\phi_p = 36^\circ$  is considered a good approximation for the entire sand wedge. If we take into account the uncertainty in the basal friction angle  $(\phi_b)$  of 802 the quartz sand layer, ranging between 15° to 21°, the analytical solutions derived from the 803 804 critical taper theory indicate that the critical taper angle, which equals the surface slope for 805 experiment 2 with a horizontal base, would be between c. 4 and 6° (taking only the lowest of 806 the two permissible critical taper angles) for a sand wedge with depth-dependent cohesion of 807  $20 \text{ Pa cm}^{-1}$ .

808

The initial horizontally layered models of experiment 2 start out as a sub-critical wedge and deform by in-sequence thrusting. After 10 cm of shortening sections through the centre of the models show a wide spread in surface slope, ranging between 4° and 24°. Only the surface slopes of models GFZ@Bern, Taipei 2A, Uppsala 2B, with slopes of 5°, 6°, and 4°, respectively, are within the predicted range of values for a cohesionless wedge. The fact that a few models do reach a critical taper could suggest that at 10 cm shortening the wedges are at the verge of transition from an immature, subcritical wedge to a critical one.

816

817 The discrepancy between most model surface slopes and analytical predictions of the critical
818 taper theory are possibly related to a combination of factors described below:

819

(1) After 10 cm shortening, the surface slope in the deforming thrust wedge might not
have yet stabilised and more shortening might be needed in order for the sand wedge
to achive steady state and reach its critical taper. It has also to be kept in mind that the

critical taper theory assumes a perfect, infinite length wedge, with a sharp tip. Here,
the wedge tip is replaced by a flat layer of thickness (3 cm), which is as much as half
the maximum wedge height (about 6 cm) at the end of experiments. Departures from
the assumptions of the theory are therefore substantial.

827

828 (2) Compaction and dilation of sand during localization of deformation along faults. 829 which is not considered in the critical taper theory, also affects the frictional strength 830 of the wedge. Lohrmann et al. (2003) show that the frictional strength of the wedge 831 changes as faults form in the wedge, and that the behaviour of the wedge is controlled 832 by the frictional strength of these faults, which have angles of stable sliding. Hence, in 833 our case it would be more appropriate to take the internal angle of friction at stable 834 sliding strength ( $\phi_s$ ) which is 31°, instead of the internal angle of friction at peak 835 strength ( $\phi_p$ ), which is c. 36°, and also the boundary friction angle at stable sliding strength of quartz sand ( $\phi_{bs}$ ), which is between 9 and 14° instead of the boundary 836 friction angle at peak strength ( $\phi_b$ ), which is between 15 and 21° (Table 1). Using 837 838 stable sliding internal friction values (neglecting cohesion), the critical surface slopes range between  $3^{\circ}$  and  $5.2^{\circ}$ , i.e. essentially the same as using the peak values ( $3^{\circ}$  to  $6^{\circ}$ ), 839 840 because the loss of strength in the bulk material and at the base partly counteract each 841 other.

842

(3) Ring-shear tests show that our analog model materials have a basal cohesion that is not taken into account in the critical taper theory. With uniform basal and peak cohesion, a critical taper would assume a concave surface shape. Estimates using the limit analysis method (Mary et al., 2013b) yield surface slopes around 5° to 6° for  $\phi_p =$  $36^\circ$ ,  $\phi_b = 15^\circ$ ,  $C_p = 20$  Pa and  $C_b = 15$  Pa ; and in a higher range of 11° to 13° for  $\phi_p$  $= 36^\circ$ ,  $\phi_b = 21^\circ$ ,  $C_p = 70$  Pa and  $C_b = 140$  Pa. Therefore, cohesion of the materials could in part explain the discrepancy with the critical taper theory.

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- 851
- 852 5. Experiment 3
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- 854 5.1. Experiment 3: Model set-up
- 855

856	In the set-up of experiment 3 a thin rigid sheet, 1 mm thick, and 12 cm in length is attached to
857	the mobile wall and underlies part of the model. The tip of the rigid sheet has a perpendicular
858	cut. Displacement of the mobile wall creates a moving basal velocity discontinuity where
859	deformation localizes away from the mobile wall during shortening of the model (Fig. 22).
860	The thin sheet is covered by Alkor foil, as are the base and the four vertical walls of the
861	experimental apparatus. The model consists of three 1-cm-thick layers of quartz and
862	corundum sand. Minimum prescribed model length parallel to the movement direction is 35
863	cm.
864	
865	INSERT Fig. 22. Model setup for experiment 3.
866	
867	Experiment 3 was done by 14 laboratories, and a total of 22 models were run, of which five
868	were analysed by XRCT.
869	
870	
871	5.2. Experiment 3: Results
872	
873	5.2.1. Evolution of models analysed by XRCT
874	
875	The cross-sectional evolution through the centre of experiment 3 models reveals that in all
876	five models analysed by XRCT a pop-up structure has formed at the tip of the moving basal
877	sheet after 1 cm of shortening (Fig. 23). At this stage the overall dip of the backthrust is
878	somewhat steeper than the forward thrust (Fig. 24). Both forward thrust and backthrust have a
879	slightly listric shape with dips between 26° and 32° at the top, and between 17° and 23° near
880	the base (Fig. 25).
881	
000	

With continuing shortening the first-formed forward thrust is advected upward along the backthrust, and new in-sequence forward thrusts initiate at the base, propagate upward and either merge with the pre-existing forward thrust at depth or reach all the way to the surface. This process is repeated during continuing shortening: previously formed forward thrusts are displaced along the backthrust and new in-sequence forward thrusts form in the footwall. The dip of new in-sequence forward thrusts is in general shallower than the first-formed forward thrust and their dip near the surface varies between 22° and 27°.

890

891 INSERT Fig. 23. Cross sections at 1, 2, 6 and 10 cm for all experiment 3 models analysed by XRCT.

892

893

894 INSERT Fig. 24. Dip of successive forward thrusts at time of initiation through centre of model, measured at
895 bottom, middle and top in experiment 3 XRCT models.

896

897

898 INSERT Fig. 25. Evolution of surface slope through centre of experiment 3 XRCT models. The lines connecting
899 measurements illustrate the oscillating behaviour of the surface slope, which tends to become less with
900 increasing shortening. Numbers above symbols indicate the difference in maximum and minimum surface slope
901 between the five models at a specific shortening increment.

902

After 3.5 cm of shortening, the surface slope of the five XRCT models, measured in sections through the centre of the model, varies between 5° and 16° (Fig. 25). During initial shortening the surface slope in each model increases, and then shows an oscillating behaviour which tends to become less important with increasing shortening. Comparing the XRCT models indicates that the spread in surface slope values tends to diminish with increasing shortening. At 10 cm of shortening surface slopes range between 16° and 22° (Fig. 25).

909

910 5.2.2. Final deformation stage

911

A comparison of all cross sections at the 50% position after 10 cm shortening (Fig. 26) shows
very similar geometries: a series of forward thrusts with relatively small, individual offsets,
and one backthrust with a large offset, except for the Lille and Melbourne 3A models which
show an additional backthrust.

916

917 Top views of all models indicate slight lateral variations in the strike of forward thrusts and 918 lateral merging of forward thrusts (Fig. 27). In top views, both forward thrusts and 919 backthrusts have a convex to the hinterland shape as a result of friction along the sidewalls.

920

921 Cross sections at five different positions after 10 cm of shortening (Fig. 28) show minor922 lateral variations, which mainly relate to surface slope and number of forward thrusts.

The surface slope for all models at the 25%, 50% and 75% positions is quite uniform, with values between 16° and 24° (Fig. 29). The Uppsala 2B model is the only exception. It has a shallower surface slope ranging between 12° and 14° at all three positions. Lateral differences in surface slope within one model are minor, mostly only between 1 and 3°. Only the Bern 3B and Lille models show larger along-strike variations with differences in values of surface slope up to 5°.

930

The number of forward thrusts was determined in cross sections at the 25%, 50% and 75% positions and only thrusts that produced a noticeable offset at the surface were considered (Fig. 30). The number of forward thrusts varied between 4 and 9 among all models. Within one particular model the difference in thrust number along strike is small, between 1 and 2 for most models, with only the Bern 3B, GFZ@Bern and Piscataway 3A models showing a difference in thrust number of 3.

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- 938

939 INSERT Fig. 26. Cross sections after 10 cm of shortening through centre of experiment 3 models. Cross section
940 of Stanford 3A is not shown, because image quality was insufficient for reproduction.

- 941
- 942

943 INSERT Fig. 27. Top views after 10 cm of shortening for experiment 3 models. Lille model has a surface grid of
944 corundum sand.

- 945
- 946

947 INSERT Fig. 28. Cross sections after 10 cm shortening for experiment 3 models at positions 25%, 50%-2 cm,
948 50%, 50%+2 cm and 75% of model width (see Fig. 7).

- 949
- 950

951 INSERT Fig. 29. Surface slope after 10 cm of shortening at 25%, 50% and 75% position for experiment 3 952 models

953

954

955 INSERT Fig. 30. Number of forward thrusts after 10 cm of shortening at 25%, 50% and 75% position for 956 experimental 3 models. Note that only those thrusts were considered that produced a noticeable offset at the 957 surface. The number of thrusts in Stanford 3A and 3B models could not be reliably determined due to poor 958 image quality.

- 960
- 961

## 962 5.2.3. Model similarities and differences

963

964 Visual comparison of all experiment 3 models shows that the evolution of structures both in 965 cross section and top view is very similar. A pop-up structure forms initially above the 966 moving basal velocity discontinuity, with subsequent in-sequence forward thrusts being 967 advected along the backthrust and becoming sucessively inactive when a new forward thrusts forms at the tip of the moving basal sheet. The backthrust, however, remains active 968 969 throughout the shortening and accommodates much more fault displacement than individual 970 forward thrusts. Nearly all models have only one backthrust and between 4 and 9 forward 971 thrusts.

972

973 The surface slope of the models at 10 cm shortening varies between 12 and 24°. These values are well above the predicted critical taper angles (c. 4-6°) for sand with  $\phi_p = 36^\circ$ ,  $\phi_b$  between 974  $15^{\circ}$  and  $21^{\circ}$  and C = 0. However, the particular set-up of experiment 3 probably does not 975 976 warrant a direct comparison with the critical taper theory. The critical taper theory accounts 977 for a situation in which the velocity discontinuity (between mobile wall and material) is 978 adjacent to the wedge, whereas in experiment 3 the velocity discontinuity is below the sand 979 wedge. The pop-up that forms at the tip of the rigid basal sheet results in a wedge of material 980 in the footwall of the backthrust that remains undeformed and is passively displaced along 981 with the basal sheet. As a result the backthrust remains active throughout the experiment, 982 advecting material and forward thrusts upward, but at the same time preventing propagation 983 of forward thrusts away from the velocity discontinuity towards the foreland.

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### 986 6. Discussion of model results

- 987
- 988 6.1. The effect of sidewall friction
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990 Sidewall friction in sandbox models has an influence on thrust wedge geometry (e.g. Costa 991 and Vendeville, 2004; Schreurs et al., 2006; Souloumiac et al., 2012). Thrust wedges are 992 generally narrower and steeper near the sidewalls and shallower and wider in the centre of the

993 model. This is caused by sidewall drag causing rotation of the stress field within the sand.. In 994 our models with fixed sidewalls and a mobile backstop, the lateral effects due to sidewall 995 friction result in a convex-to-the-backstop shape of the thrust wedge in top view. This is 996 largely consistent with the analysis of Souloumiac et al. (2012), who measured the effect of 997 sidewall friction in experiments in which a sand wedge undergoes plane-strain shortening. 998 They varied the surface  $S_L$  of sand in contact with the sidewalls, and the surface  $S_B$  in contact 999 with the base plate of the sandbox. For initial ratios  $S_L/S_B$  between 0.1 and 0.35, Souloumiac 1000 et al. (2012) found that sidewall friction during shortening of the sand wedge causes thrust 1001 curvature near the side walls, whereas for  $S_L/S_B$  ratios < 0.1 sidewall friction has negligible 1002 effects. At  $S_L/S_B$  ratios > 0.35, thrusting occurs at different locations throughout the box, 1003 revealing a major experimental bias (Souloumiac et al., 2012). For the experiment 2 and 3 1004 models presented here, S<sub>L</sub>/S<sub>B</sub> varies between 0.075 and 0.3, and all models show thrust 1005 curvature near the sidewalls (Figs. 18 and 29). The fact that the Bern and IFP models, with 1006  $S_L/S_B$  ratios < 0.1 still show thrust curvature near the sidewalls might be related to the 1007 difference in the nature of the walls, i.e. foil-covered walls in the experiments presented here and glass walls in the experiments of Souloumiac et al. (2012). From an inspection of top 1008 1009 views, we estimate that sidewall friction only plays a role on thrust wedge curvature until c. 5 1010 cm away from the sidewalls. All our quantified parameters are measured in sections that are at 1011 least 5 cm away from the sidewalls (except IFP exp 1), and hence our results are not expected 1012 to be affected by the effects of sidewall friction.

1013

1014 Friction on the moving back wall also has an effect. In the previous analogue model 1015 comparison (Schreurs et al., 2006, Fig. 2b), six models developed a pop-up against the back 1016 wall, and two models developed a single forward thrust rooted at the back wall-base plate 1017 corner. Souloumiac et al. (2010, Fig. 11 and 14) showed that this difference is due to the 1018 friction on the back wall: at high friction, a pop-up develops in order to reduce sliding on the 1019 back wall, whereas at low friction we observe a single forward thrust and vertical slip on the 1020 back wall. Here, sands and sidewall materials are identical in all models, and all models 1021 develop the same initial structure: a pop-up. This is a substantial improvement compared to the previous comparison (Schreurs et al., 2006), and a confirmation that the pop-up / forward 1022 thrust discrepancy is due to differences in friction of sand against the back wall material, 1023 1024 provided other parameters like basal friction are fixed.

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- 1027 6.2. Influence of experimental set-up on model reproducibility
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1029 The results of our three different thrust experiments demonstrate that the set-up itself has an 1030 influence on model reproducibility with experiment 1 showing the highest degree of 1031 similarity, followed by experiment 3 and then by experiment 2.

1032

1033 All experiment 1 models show exactly the same evolution, i.e. stable sliding of a triangular 1034 sand wedge without significant internal deformation and a surface slope that remains nearly 1035 constant throughout the experiment. Experiments 2 and 3 consist of horizontally layered 1036 models that are shortened by inward movement of a mobile wall. The undeformed models in 1037 both experiments represent subcritical wedges. The only difference between the two 1038 experimental setups is the presence of a thin, rigid basal sheet attached to the mobile wall in 1039 experiment 3. Hence, in experiment 3 a singularity is stationary with respect to the moving 1040 sheet tip and displacement of the mobile wall forces deformation to remain localized at the 1041 singularity resulting in a good similarity among all models with only minor variations in 1042 quantitative parameters such as surface slope, and thrust dip. In contrast, in experiment 2, the 1043 singularity is located at the active forward thrust, which is less constrained in space, and 1044 consequently models show a larger variability, in particular with regard to the number of 1045 forward thrusts, which in experiment 2 varies from 2 to 9 for forward thrusts and from 1 to 9 1046 for backthrusts.

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- 1048

## 1049 6.3. Variations within and between models

1050

Both experiments 2 and 3 models show similar cross-sectional evolutions demonstrating reproducibility of first-order experimental results. However, for both experiments we do observe variations of structures both in map view and in cross sections. Thrusts merge along strike and show slight variations in their surface strike. Quantification of parameters in crosssections also documents variations among models and lateral variations within one model, in particular for experiment 2. Possible explanations for these variations are discussed below:

1057

(1) Even though the prescribed model construction techniques were stringent concerning
 sieve mesh size, sifting height, and sifting rate, it is unlikely in practice that the initial
 undeformed model is perfectly homogeneous and has constant values of internal

1061 friction, basal friction, internal cohesion and basal cohesion throughout. Slight 1062 variations in these values might be caused by small changes in sifting height or sifting 1063 rate during model construction or might have occurred during off-scraping of excess 1064 material. An inspection of the first-formed pop-up structure in the centre of XRCT 1065 experiment 2 models shows that those of Bern 2B and IFP 2A are quite asymmetric, with a steep backthrust dipping at c. 45° and a relatively shallow forward thrust. The 1066 1067 other three models (Bern 2A, GFZ@Bern, and IFP 2B) have a more symmetric pop-up structure. Analogue models testing the influence of basal friction on the thrust wedge 1068 shape (e.g. Colletta et al., 1991; Huigi et al., 1992) reveal that initially horizontally 1069 1070 layered models with a low basal friction have a more symmetric style of thrusting than 1071 models with a high basal friction, which have a more asymmetric thrust style. This 1072 would suggest a variability in initial basal friction between the models, at least near the moving wall with models Bern 2B and IFP 2A having higher values of basal 1073 1074 friction. This variability, as well as the variability of the measured friction of sand on 1075 Alkor foil in ring-shear tests (boundary friction, Table 1), could be due to repeated use 1076 of the Alkor foil, which would thus change (probably increase) basal frictional 1077 properties during repeated tests, as sand grains scratch its surface. In our experiments 1078 electrostatic forces will occur at the interface Alkor foil / sand, but their magnitudes 1079 are difficult to determine and their effect on the structures remains unknown. 1080 Variability in model results might also be caused by the presence of tiny air pockets 1081 trapped below the Alkor foil during adhesion to the base of the sandbox resulting in a 1082 slightly uneven surface and varying basal friction conditions.

1083

1084 (2) During the initial stages of the experiment, shortening of the model will result in 1085 compaction of the sand grains close to the mobile wall, and hence compaction 1086 gradients will form. Adam et al. (2013) could visualize this diffuse, non-localised 1087 deformation in analogue models using digital image correlation techniques applied on 1088 XRCT images. The lateral variations in compaction might enhance or reduce the 1089 initial variations in mechanical properties introduced during model construction. The 1090 spatial and temporal evolution of the compaction gradients will depend on the 1091 experimental set-up. For experiments 1 and 2, initial compaction occurs adjacent to 1092 the mobile wall, whereas in experiment 3, it starts near the tip of the basal sheet.

1094 (3) Laboratory climatic conditions varied and in particular the relative humidity might 1095 have an influence on the cohesion of the sands, and thus on model results. Forsyth et 1096 al. (2002) investigated the influence of atmospheric humidity on glass spheres with 1097 different sizes. For the range of grain size used in our experiments (c. 80-200 µm), 1098 Forsyth et al. (2002) could show that glass spheres only start to show cohesive or 1099 stick-slip behaviour at relative humidities > 65%. As most laboratories reported 1100 humidities below 65%, humidity is probably not a major factor influencing model 1101 results. However, it has to be kept in mind that Forsyth et al. (2002) only investigated 1102 the influence of humidity on perfectly spherical grains with identical grain size. Our quartz and corundum sands have an angular grain shape and a heterogeneous grain 1103 1104 size distribution, and an uncertainty remains with regard to the role of humidity on the 1105 cohesion of our material.

1106

1107 (4) One of the striking results of the present comparison is the large variability in surface 1108 slopes, thrust dips, and particularly numbers of thrusts. Large variations occur even 1109 between repetition of experiments in the same laboratory. They also do occur along 1110 strike of single models. Details of each thrust is little reproducible after substantial 1111 shortening, despite our present efforts to remove experimental imperfections. This 1112 variability is a feature of the localisation process in frictional materials that cannot be 1113 completely removed by an improvement of experimental protocols. The exact location 1114 and dip of a thrust depend on minute changes in the distribution of sand grains that 1115 promote or delay the onset of dilatation, which has a long term effect upon further 1116 shortening. This can also be understood theoretically by recalling the central argument 1117 of the critical taper theory: that the wedge will deform to maintain the stress field 1118 everywhere on the verge of Coulomb failure. Any model imperfection ruins this 1119 simplicity and triggers the next failure, resulting in a system that is highly sensitive to 1120 initial conditions and to external perturbations (Mary et al., 2013a).

- 1121
- 1122 6.4. Recommendations and potential improvements
- 1123

We recommend that a minimum standard be adhered for experimental descriptions. Often analogue model materials are inadequately characterized and model building and experimental procedures are incomplete. Experimental descriptions should include the physical characteristics (e.g. grain size, grain size distribution, grain shape) of the analogue materials, the mechanical properties (e.g. cohesion and angles of internal friction at peak and stable strength, basal friction) and how measured, model construction technique (e.g., physical handling technique, size of sieve mesh, sifting rate, scraping details) and laboratory climatic conditions (temperature, humidity).

1132

1133 In order to reduce the influence of the human factor and minimize initial heterogeneities in 1134 material properties introduced during model construction, one could consider using a special 1135 sedimentation device for sifting sands. Maillot (2013) built a sedimentation device in an 1136 attempt to produce uniform sand packs. For Fontainebleau sand with a 250 µm median grain 1137 size, Maillot (2013) could show that the density of the resulting sandpack is close to its 1138 maximum value, reproducible and uniform. Although the sedimentation device surely 1139 presents an advantage in terms of model homogeneity, it requires extensive testing to produce 1140 relatively level sand packs. Spatial variations in the thickness of the sand layers cannot be 1141 avoided due to downward air currents during infill resulting in a central depression and excess 1142 thickness near the four walls. Whereas thickness variations in the centre of the sandbox are 1143 mostly below 4% for a model thickness of c. 3 to 4 cm, variations near the lateral walls are 1144 more important (Maillot, 2013). Although a best value of +6% is reached, the excess 1145 thickness near the walls can be larger than 100% depending on the type of sand, the 1146 sedimentation flux and the number of sieves used (Maillot, 2013). In any case, the sieving process is a central ingredient in model construction. Other devices could be developed for 1147 1148 special setups or for producing layered models consisting of different granular materials.

1149 Cubas et al. (2010) performed analogue model experiments using such a sedimentation device 1150 to quantify the intrinsic variability of model results. The experiments consisted of shortening 1151 an initially subcritical sand wedge resting on a flat sand layer by translating the wall on the 1152 wedge side over a distance of 30 mm. By repeating experiments and applying statistical 1153 methods to observables measured in final-state cross sections through the central part of the 1154 box (where side-wall effects did not play a role), they could for example show that the error 1155 bar for fault dips are c. 3.3° for the first pop-up that forms, with forward thrusts dipping at 38° 1156  $\pm$  3.2° and backthrusts at 41  $\pm$  3.3°. These values are of course dependent on the granular 1157 material used, the experimental protocol and the set-up. Although our experiments 2 and 3 1158 consisted of a different set-up (our models are initially horizontal), used different granular 1159 materials and did not involve the sedimentation device of Maillot (2013), a comparison of the error bars for fault dips of forward and backthrusts measured at the top in XRCT sections through the centre of the model shows largely comparable error bars, with forward thrusts dipping at  $29 \pm 3^{\circ}$  in both experiments 2 and 3. Backthrusts in experiment 2 have a larger error bar with faults dipping at  $36 \pm 9^{\circ}$ , whereas backthrusts in experiment 3 show a smaller error bar with faults dipping at  $30 \pm 2^{\circ}$ .

1165

1166 Compaction of the granular model material prior to deformation might also reduce variability 1167 in model results. Compaction, however, would need to be done in a systematic and 1168 reproducible way, e.g. by shaking or tapping. In addition, one would need to determine the 1169 mechanical properties of compacted granular material using an apparatus in which 1170 compaction is achieved in an identical way as for the analogue model.

1171

1172 In our model comparison we choose to use quartz and corundum sand used at the laboratory 1173 in Bern. These sands have their own specific physical characteristics and mechanical 1174 properties. It can not be excluded that the use of another type of sand, with different grain 1175 shape, grain size, and grain size distribution, might improve experimental reproducibility. 1176 This would require further testing.

1177

Finally, repeating experiments should be performed in order to ensure that intrinsic variability
(in identical setups) is properly defined and smaller than the expected effects related to
(extrinsic) "controlling" factors.

- 1181
- 1182

#### 1183 7. Concluding remarks

1184

1185 We have made a quantitative comparison of brittle thrust experiments to evaluate the 1186 variability among analogue models and to appraise reproducibility and limits of model 1187 interpretation. The reasons for variability in analogue model experiments boils down to the 1188 system-wide effectiveness of small disturbances. Bearing this in mind the philosophy behind 1189 our benchmark was to minimize this by choosing the most simple and most insensitive setups, 1190 boundary conditions and materials keeping them as homogeneous as possible in the different 1191 laboratories. For three different thrust wedge experiments, we quantified parameters such as 1192 fault dip, fault spacing, thrust number, thrust formation and surface slope. In contrast to the 1193 model comparison of Schreurs et al. (2006) we made quantitative comparisons of model

results in sections at least 5 cm away from the sidewalls, to avoid non-representative results due to complex interactions between sidewall friction and basal friction.

1196

1197 Our model comparison suggests that one of the sources of experimental variability is related 1198 to slight variations in how material is deposited in the sandbox and how scraping of material 1199 occurred to flatten the surface. Small changes in sifting height, sifting rate, and scraping will 1200 result in slightly heterogeneous material densities, which will affect the mechanical properties 1201 of the granular material, and result in lateral and vertical differences in peak and basal friction 1202 angles, as well as cohesion values once the model is constructed. Initial variations in basal 1203 friction are most likely responsible for most of the variability in model results. Part of the 1204 variability might also be explained by our choice not to compact models prior to deformation. 1205 In our benchmark, shortening causes compaction of the granular materials leading to 1206 compaction gradients that are superposed on previous heterogeneities introduced during 1207 model construction. Differences in relative humidity between participating laboratories might 1208 also have an effect on granular material cohesion and hence on model variability. The 1209 influence of humidity on the cohesion of the sands used in our model comparison remains 1210 poorly known. Taking into account the experimental studies of Forsyth et al. (2002), however, 1211 we consider that its influence on model variability is most likely minimal.

1212

Our observations highlight the limits of up-scaling quantitative analogue model results to nature or for making comparisons with numerical models (Buiter et al., 2016). It will remain difficult to scale quantitative results such as number of thrusts, spacing between forward thrusts, or width of pop-up structures from model to nature. The way forward is perhaps to build statistical descriptions of the measured parameters rather than using single values. These would in turn provide more reliable data for a comparison to numerical simulations.

1219

1220 Our model comparison shows that even for simple plane-strain experiments with prescribed 1221 stringent model construction techniques, the human factor plays a decisive role, and even 1222 when one modeler repeats the experiment, the quantitative model results show considerable 1223 variability. Although this might at first seem a discouraging conclusion, the failure of the 1224 models to achieve perfect replicability despite our precautions can be considered a success in 1225 documenting the importance of initial model heterogeneity. As is the case for natural thrust 1226 wedges, the initial undeformed sand model is not perfectly homogeneous throughout, but 1227 already has slight variations in mechanical properties such as internal friction, basal friction,

internal cohesion and basal cohesion. Small differences in these parameters will affect how,
where and when the first thrusts form and will affect the details of the timing and location of
subsequent thrusts.

1231

1232 The variability reported in our benchmark is considerable and should serve the analogue 1233 modeling community as a constraint on the best expected "precision" of models. We can 1234 assume that as model setups become more complex (e.g. by introducing detachment layers, 1235 erosion, sedimentation, lateral and vertical changes in material geometry, etc.) the "precision" 1236 will drop drastically. We hope that this benchmark serves to sensitize the community and 1237 helps to prevent over-interpretation of analogue models especially in view of recent 1238 developments that allow quantitative measurements to be made easily at high precision using 1239 laser scanning or image correlation techniques.

- 1240
- 1241

### 1242 Acknowledgments

1243

This study was supported by SNF Grant 200020-109320, 200020-122143 and 200021-140608 (Guido Schreurs), Discovery and Equipment grants from the Natural Sciences and Engineering Research Council of Canada, NSERC (Alexander Cruden), the Fundação de Amparo à Pesquisa do Estado de Minas Gerais (Fapemig), CRA 871/06 (Caroline J.S. Gomes), and the Swedish Research Council, Grant 2008-3443 (Faramarz Nilfouroushan).

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Fig. 1. Experimental set-up used in model comparison experiments by Schreurs et al., (2006). Model consists of a 3.5 cm-thick sand layer with an embedded microbeads layer and an overlying sand wedge with a surface slope of 10° adjacent to the mobile wall. All walls are covered by Alkor foil. Figure reproduced from Schreurs et al. (2006) with permission from the Geological Society of London.

1343

Fig. 2. Model comparison showing cross sections through thrust wedge after 2, 6 and 14 cm of shortening. The experimental set-up is shown in Fig. 1. The sections of Bern and IFP Rueil Malmaison are X-ray computer tomography (XRCT) images through the center of the model, whereas the remaining sections are sidewall observations. Microbeads layer indicated by "m". Figure modified after and reproduced from Schreurs et al. (2006) with permission from the Geological Society of London.

1350

Fig. 3. Physical characteristics of the quartz and corundum sand used in the experiments (modified
after Panien et al., 2006). Upper and lowermost images are photographs and SEM images,
respectively. Width of each SEM image is 1740 μm.

1354

Fig. 4. Shear stress plotted versus shear strain for quartz sand (modified from Lohrmann et al., 2003;
Panien et al., 2006). Strain softening from peak strength to stable strength correlates with dilation of
sand.

1358

Fig. 5. Zoom of critical taper curves for cohesionless sand at peak strength ( $\phi_p = 36^\circ$ ,  $\phi_b = 15^\circ$  and C = 1360 0 Pa), cohesionless sand at stable strength ( $\phi_s = 31^\circ$ ,  $\phi_b = 15^\circ$  and C = 0 Pa), and a cohesive sand at peak strength with depth-dependent cohesion ( $\phi_p = 36^\circ$ ,  $\phi_b = 15^\circ$  and C = 20 Pa cm<sup>-1</sup> times z, with z = 1362 depth, following Zhao et al. (1986)).

1363

Fig. 6. Schematic illustration of measurements of a) surface slope, b) forward thrust spacing, and c) thrust dip angles. Surface slope is measured as the best fitting line through the valleys (Stockmal et al., 2007) and can only be determined once at least 2 thrusts have formed. Thrust spacing is measured horizontally from a newly initiated in-sequence forward thrust to the previously formed forward thrust.

1369	Fig. 7. Top view photograph illustrating position of cross sections at 25% (1), 50%-2 cm (2), 50% (3),
1370	50% + 2 cm (4), and 75% (5) of model width (measured parallel to mobile wall, which moves here
1371	from bottom to top). Model width is 80 cm in this particular experiment.
1372	
1373	Fig. 8. Model set-up for experiment 1.
1374	
1375	Fig. 9. Model building procedure for experiment 1 shown in cross section. A template with the shape
1376	of the final wedge is attached on top of each sidewall to guide the scraper (see Appendix A-2).
1377	Stippled line indicates sand wedge before final scraping.
1378	
1379	Fig. 10. Evolution of experiment 1 model run at Bern after 0, 2 and 4 cm of shortening (a) XRCT
1380	sections through centre of model, (b) top view photographs of model.
1381	
1382	Fig. 11. Cross sections through centre of experiment 1 models after 4 cm of shortening. Sections of
1383	Bern, GFZ@Bern, and IFP are XRCT images
1384	
1385	Fig. 12. Model set-up for experiment 2.
1386	
1387	Fig. 13. Cross-sectional evolution through centre of experiment 2 models after 1, 2, 6 and 10 cm of
1388	shortening as observed in XRCT images.
1389	
1390	Fig. 14. Quantitative comparison of experiment 2 models analysed by XRCT. (a) Amount of
1391	shortening at which a forward thrust forms at centre of model. (b) Spacing to previously formed
1392	forward thrust at the moment of initiation of a new, in-sequence forward thrust.
1393	
1394	Fig. 15. Dip angles of successive in-sequence forward (a) and back thrusts (b) in centre of experiment
1395	2 XRCT models, measured at top, middle and bottom.
1396	
1397	Fig. 16. Surface slope evolution at centre of experiment 2 XRCT models. Only values that could be
1398	reliably measured in XRCT images are given.
1399	
1400	Fig. 17. Cross sections through centre of experiment 2 models after 10 cm of shortening. Width of
1401	each panel shown is 25 cm. Note that some labs added a layer of sand before cutting the model. Cross
1402	sections from Lille 2A and 2B are at 50%-2cm position. Image quality of cross sections from Stanford
1403	2A and 2B was not good enough for reproduction.
1404	
1405	

Fig. 18. Top views of experiment 2 models after 10 cm of shortening showing along-strike structural variability. Movement of mobile wall is from bottom to top Note that Lille 2A and 2B models have a grid of corundum sand imprinted on the surface, whereas Mexico 2A and 2B models used prescribed sand mixed with dark sand particles. All photos are shown at the same scale, given in the top left photo.

1411

Fig. 19. Cross sections after 10 cm shortening for experiment 2 models at positions 25%, 50%-2 cm,
50%, 50%+2 cm and 75% (see Fig. 6) showing along-strike structural variability. Note that some
laboratories added a post-kinematic sand layer before wetting and sectioning.

1415

Fig. 20. Surface slope after 10 cm of shortening at 25%, 50% and 75% positions for experiment 2 models. The surface slope could not be reliably measured on all cross-sectional images. Surface slopes for Lille 2A and Lille 2B models were measured at 50%-2cm position. Numbers above symbols indicate difference between maximum and minimum slope angle within one particular model and are only given for those models in which the surface slope could be determined at all three positions. Surface slope values along one sidewall (0% position) are given for comparison and are generally higher.

1423

Fig. 21. Number of forward and back thrusts at 25%, 50% and 75% position after 10 cm of shortening
for experiment 2 models. Numbers above symbols indicate along-strike differences in number of
thrusts and are only given for those models, in which thrusts could be reliably determined at all three
positions.

1428

1429 Fig. 22. Model setup for experiment 3.

1430

1431 Fig. 23. Cross sections at 1, 2, 6 and 10 cm for all experiment 3 models analysed by XRCT.

1432

Fig. 24. Dip of successive forward thrusts at time of initiation through centre of model, measured atbottom, middle and top in experiment 3 XRCT models.

1435

Fig. 25. Evolution of surface slope through centre of experiment 3 XRCT models. The lines connecting measurements illustrate the oscillating behaviour of the surface slope, which tends to become less with increasing shortening. Numbers above symbols indicate the difference in maximum and minimum surface slope between the five models at a specific shortening increment.

1440

Fig. 26. Cross sections after 10 cm of shortening through centre of experiment 3 models. Cross section
of Stanford 3A is not shown, because image quality was insufficient for reproduction.

1443	
1444	Fig. 27. Top views after 10 cm of shortening for experiment 3 models. Lille model has a surface grid
1445	of corundum sand.
1446	
1447	Fig. 28. Cross sections after 10 cm shortening for experiment 3 models at positions 25%, 50%-2 cm,
1448	50%, 50%+2 cm and 75% of model width (see Fig. 7).
1449	
1450	Fig. 29. Surface slope after 10 cm of shortening at 25%, 50% and 75% position for experiment 3
1451	models
1452	
1453	Fig. 30. Number of forward thrusts after 10 cm of shortening at 25%, 50% and 75% position for
1454	experimental 3 models. Note that only those thrusts were considered that produced a noticeable offset
1455	at the surface. The number of thrusts in Stanford 3A and 3B models could not be reliably determined
1456	due to poor image quality.
1457	
1458	Appendix A: Model construction techniques
1459	Appendix A-1: Mesh sieve
1460	Appendix A-2: Scraper to remove excess sand
1461	
1462	
1463	
1464	
1465	Table 1. Range of mechanical properties of quartz and corundum sand obtained with a ring-shear tester. Values
1466	are rounded to nearest degree for friction angles and to nearest whole number for cohesion. n is number of ring-
1467	shear tests at normal stresses ranging from c. 500 to 2240 Pa.
1468	
1469	Table 2. Overview of laboratory climatic conditions and model widths. Most laboratories performed experiments
1470	2 and 3 twice, and range of values for room temperature and relative humidity are indicated. Exceptions to the
1471	prescribed modeling procedure are also given.
1472	
1473	

## Shortening experiment - Mobile back wall

Foil	Initial width > 35 cm	10 cm	Mobile back wall
		10° sand	
1.0	cm sand		、
0.5	cm sand		
1.0	cm sand		N
	0.5 cm microbeads		•
0.5	cm sand		
		base of sandbox is covered with Foil	

Foil

Fig. 1









Parma

Pavia

Toronto



















		Quartz sand	Corundum sand
		<u>100 µт</u>	1 <u>00 μ</u> m
origin:	Ті	iassic quartz sand	bauxite
composition:		99 % Si0 <sub>2</sub>	95 % Al <sub>2</sub> O <sub>3</sub>
grain size rang	le li v	80-200 μm	88-125 μm
(as indicated b grain size distr (μm)	y supplier) ibution % 10 8 6 4 2	α α α α α α α α α α α α α α	0.61-088 0.61-0880000000000000000000000000000000000
bulk density: s p	ieved oured	1.56 g/cm <sup>3</sup> 1.32 g/cm <sup>3</sup>	1.89 g/cm <sup>3</sup> 1.55 g/cm <sup>3</sup>
porosity: si po	ieved oured	41.8 % 50.7 %	53.0 % 61.7 %
grain shape: te	exture	irregular surfaces	conchoidal fractures
r	oundness	angular	very angular
	2.584		







γ shear strain















GFZ@Bern



Melbourne



Piscataway



Cergy-Pontoise



Kyoto

Ouro Preto

Uppsala



Bern



Mexico



Toronto















25%	50%-2cm	50%	50%+2cm	75%
Bern 2A				
Bern 2B				
Buenos Aires	Carlos and	Sec.		<u> </u>
Cergy Pontoise		TIT		
GFZ@Bern				
IFP 2A			n.a	
IFP 2B				
Kyoto			(Action)	re-
Lille 2A		n.a		- FT
Lille 2B		n.a		
Melbourne 2A		The second second	and the second s	Contraction of the second
Melbourne 2B				





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1	-											Δ													
0	Bern 2A	Bern 2B	Buenos Aires	Cergy-Pontoise	GFZ@Bern	IFP 2A	IFP 2B	Kyoto	Lille 2A	Lille 2B	Melbourne 2A	Melbourne 2B	Mexico 2A	Mexico 2B	Parma	Piscataway 2A	Piscataway 2B	Stanford 2A	Stanford 2B	Taipei 2A	Taipei 2B	Toronto 2A	Toronto 2B	Uppsala 2A	I Inscala 2B



































































IFP 3B

Melbourne 3A



































25%	50%-2cm	50%	50%+2cm	75%
Mexico				
Parma 3A		-22		- 12
Parma 3B	-22			
Piscataway 3A	16	15	12	7
Piscataway 3B	7	8	9	15
Taipei 3A	and the second s		and the second s	Selection of the Party of the P
Taipei 3B		and the second second		
Toronto 3A	Sem	5 cm	5cm	5cm
Toronto 3B	5 cm	5 cm	Sen	5 cm
Uppsala 3A	22	-72		-72
Uppsala 3B	-	-72	- 82	-










Side view (lateral sidewall omitted for clarity)



Frontal view (vertical mobile wall omitted for clarity)

Mechanical parameter	Quartz sand	Corundum sand		
	n = 3	n = 3		
Angle of internal friction at peak strength $(\phi_p)$	34° - 37°	35° - 36°		
Cohesion at peak strength (C <sub>p</sub> ) in Pa	19 – 69	15 – 28		
Angle of internal friction at stable strength $(\phi_s)$	30° - 31°	31°		
Angle of boundary friction $(\phi_b)$	15° - 21°	23° - 25°		
Boundary cohesion (C <sub>b</sub> ) in Pa	14 – 141	23 - 44		
Angle of boundary friction at stable strength ( $\phi_{bs}$ )	9° - 14°	22° - 24°		

Table 1. Range of mechanical properties of quartz and corundum sand obtained with a ring-shear tester. Values are rounded to nearest degree for friction angles and to nearest whole number for cohesion. n is number of ring-shear tests at normal stresses ranging from c. 500 to 2240 Pa.

Laboratory Exp.	Roo	Room temperature*		Relative humidity			Model width			
		(°C)			(%)			(cm)		
	1	2	3	1	2	3	1	2	3	
Bern	23	23-24	23-24	60	59-60	54-60	80	80	80	
Buenos Aires <sup>1</sup>	23	25	x	53	29	x	32	32	x	
Cergy-Pontoise	17-20	17-20	x	60-80	60-80	x	20	20	x	
GFZ@Bern <sup>2</sup>	24	23	23	54-55	63	57-59	80	80	80	
IFP <sup>3</sup>	21	21	21	n.d.	n.d.	n.d.	13#	74	74	
Kyoto	21	21-22	21	60	55-60	50	30	30	30	
Lille	n.d.	n.d.	x	n.d.	n.d.	x	60	60	x	
Melbourne	24	24	24	33	32	30-31	60	60	60	
Mexico	21	24-26	22	58	57-58	66	20	20	20	
Ouro Preto <sup>4</sup>	20	x	x	56	x	x	30	x	x	
Parma <sup>5</sup>	23	22	22	41	40	40	40	40	40	
Piscataway	23	20-25	20-24	n.d.	n.d.	n.d.	61	61	61	
Stanford	21-22	21-22	21-22	40-50	40-50	40-50	30.5	30.5	30.5	
Taipei	x	19	19	х	58-67	58-60	x	20	20	
Toronto	24	24	25	44	45-49	51-53	45	45	45	
Uppsala	21	21	21	n.d.	n.d.	n.d.	30	30	30	

\* rounded to nearest degree, <sup>x</sup> experiment not done, <sup>#</sup>width less than prescribed minimum width of 20 cm, <sup>1</sup> velocity of mobile wall was 4 cm/h, <sup>2</sup> researcher (MR) of Helmholtz Centre Potsdam (GFZ German Research

Centre for Geosciences) performed experiments 1, 2 and 3 using experimental apparatus from Bern, <sup>3</sup> transverse walls in experiment 3 consisted of rubber sheets, <sup>4</sup> velocity of mobile wall 2.3 cm/h, <sup>5</sup> velocity of mobile wall 5 cm/h, n.d. = not determined

Table 2. Overview of laboratory climatic conditions and model widths. Most laboratories performed experiments 2 and 3 twice, and range of values for room temperature and relative humidity are indicated. Exceptions to the prescribed modeling procedure are also given.