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On the environment surrounding close-in exoplanets

A. A. Vidotto,¹★ R. Fares,² M. Jardine,² C. Moutou^{3,4} and J.-F. Donati⁵

¹Observatoire de Genève, Université de Genève, Chemin des Maillettes 51, CH-1290 Versoix, Switzerland

²SUPA, School of Physics and Astronomy, University of St Andrews, North Haugh, St Andrews KY16 9SS, UK

³Canada–France–Hawaii Telescope Corporation, CNRS, 65-1238 Mamalahoa Hwy, Kamuela, HI 96743, USA

⁴Aix Marseille Université, CNRS, LAM (Laboratoire d’Astrophysique de Marseille) UMR 7326, F-13388 Marseille, France

⁵LATT-UMR 5572, CNRS and Univ. P. Sabatier, 14 Av. E. Belin, F-31400 Toulouse, France

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ABSTRACT

Exoplanets in extremely close-in orbits are immersed in a local interplanetary medium (i.e. the stellar wind) much denser than the local conditions encountered around the Solar system planets. The environment surrounding these exoplanets also differs in terms of dynamics (slower stellar winds, but higher Keplerian velocities) and ambient magnetic fields (likely higher for host stars more active than the Sun). Here, we quantitatively investigate the nature of the interplanetary media surrounding the hot Jupiters HD 46375b, HD 73256b, HD 102195b, HD 130322b and HD 179949b. We simulate the three-dimensional winds of their host stars, in which we directly incorporate their observed surface magnetic fields. With that, we derive mass-loss rates ($1.9\text{--}8.0 \times 10^{-13} M_{\odot} \text{yr}^{-1}$) and the wind properties at the position of the hot Jupiters’ orbits (temperature, velocity, magnetic field intensity and pressure). We show that these exoplanets’ orbits are supermagnetosonic, indicating that bow shocks are formed surrounding these planets. Assuming planetary magnetic fields similar to Jupiter’s, we estimate planetary magnetospheric sizes of 4.1–5.6 planetary radii. We also derive the exoplanetary radio emission released in the dissipation of the stellar wind energy. We find radio fluxes ranging from 0.02 to 0.13 mJy, which are challenging to be observed with present-day technology, but could be detectable with future higher sensitivity arrays (e.g. Square Kilometre Array). Radio emission from systems having closer hot Jupiters, such as from τ Boo b or HD 189733b, or from nearby planetary systems orbiting young stars, are likely to have higher radio fluxes, presenting better prospects for detecting exoplanetary radio emission.

Key words: MHD – methods: numerical – stars: magnetic field – planetary systems – stars: winds, outflows.

1 INTRODUCTION

The interplanetary medium that surrounds exoplanets is filled by stellar wind particles and the embedded stellar magnetic field. The large majority of exoplanets found so far are orbiting cool stars at the main-sequence phase. Although the winds of these stars have proven quite challenging to observe (Mullan et al. 1992; Wargelin & Drake 2001; Wood et al. 2005), the interaction between exoplanets and their surrounding medium (i.e. the host star’s wind) may give rise to observable signatures, such as planetary radio emission (Zarka 2007), enhancement of stellar activity (Cuntz, Saar & Musielak 2000; Shkolnik, Walker & Bohlender 2003; Shkolnik et al. 2005), bow shock formation (Vidotto, Jardine & Helling 2010b; Bisikalo et al. 2013; Llama et al. 2013), charge exchange between stellar wind protons and planetary neutral hydrogen (Holmström et al. 2008;

Ekenbäck et al. 2010; Bourrier & Lecavelier des Etangs 2013; Kislyakova et al. 2014) and formation of comet-like tail structures (Mura et al. 2011; Rappaport et al. 2012; Budaj 2013; Villarreal D’Angelo et al. 2014), all of which can provide invaluable insights into the system, such as the intensity of the planetary magnetic field, velocity and temperature of the local stellar wind, etc.

By studying stellar winds, we are able to make quantitative predictions about the interplanetary medium. A significant improvement on our understanding of the interaction between a planet and the wind of its host star has been achieved in the past decade. Traditionally, these works have been based on simplified treatments of the winds (e.g. Ip, Kopp & Hu 2004; Grießmeier et al. 2005; Preusse et al. 2005; Stevens 2005; Lovelace, Romanova & Barnard 2008; Vidotto, Jardine & Helling 2011a; See et al. 2014; Strugarek et al. 2014). For example, simplified wind approaches might assume an isothermal wind structure, or that stars are non-rotating and/or non-magnetized bodies, among others. However, stellar winds are three-dimensional (3D) in nature, where complex interactions of

* E-mail: aline.vidotto@unige.ch

a rotating, magnetized plasma take place. In view of that, more recently, new generations of 3D, magnetohydrodynamical (MHD) models have started to be employed in the studies of interactions between stars/winds and their planets (e.g. Cohen et al. 2009, 2014; Vidotto et al. 2009a,b, 2010a, 2011b, 2012, 2014b; Llama et al. 2013).

The advantage of using simplified treatments of the wind is that these works rely on analytical and low-dimensional (1D, 2D) numerical studies, which are significantly faster and do not demand extensive computational resources as 3D models do. Because of that, 1D works can investigate a much wider range of stellar wind parameters (e.g. Cranmer & Saar 2011; See et al. 2014) than more complex, computationally expensive 3D models can. The disadvantage, on the other hand, is that the simplified models cannot capture the 3D structure of stellar winds. Combined with modern techniques to reconstruct stellar magnetic fields, some 3D models are able to provide a more realistic account of the stellar magnetic field topology embedded in the wind, recognized to be essential to interpret and predict signatures of star–planet interactions (McIvor, Jardine & Holzwarth 2006; Fares et al. 2010; Vidotto, Jardine & Helling 2011c; Lanza 2012; Llama et al. 2013).

1.1 Interactions with magnetized planets

As the wind outflows from the star, it interacts with any planet encountered on its way. If these planets are magnetized, their magnetic fields can act as shields, which prevent stellar wind particles from reaching all the way down to the surface or atmosphere of these objects (e.g. Khodachenko et al. 2007; Lammer et al. 2007; Driscoll & Bercovici 2013; Kislyakova et al. 2014). This is in particular the case of the Earth and, more generally, of planets with dipolar field configurations. For these objects, the solar and stellar winds are deflected around the magnetospheric cavity, potentially helping the planet to retain its atmosphere. However, atmospheric escape can still occur at high magnetic latitudes through polar flows, as is the case of the Earth (e.g. Seki et al. 2001; Moore & Horwitz 2007) and predicted for exoplanets (Owen & Adams 2014; see also Section 5.2). Part of this planetary outflow can return from the magnetosphere back into atmospheric regions of low-magnetic latitudes, reducing the total net loss rate of atmospheric escape, as suggested for the Earth scenario (Seki et al. 2001). The detailed process of atmospheric dynamics and escape is certainly complex and not examined here.

In the present work, only magnetized exoplanets are considered. This means that the cross-section of the ‘obstacle’ is not that of the planet itself, but rather takes into account the magnetospheric size of the planet. The magnetospheric size of the planet depends both on the characteristics of the local environment surrounding the planet (interplanetary density, velocity, magnetic field, temperature) and on its own magnetic field. On the theoretical side, some models suggest that the strength of the planetary magnetic field is dependent on the rotation rate of the planet (Farrell, Desch & Zarka 1999). In this situation, close-in planets that are tidally locked could have a reduced magnetic moment (Grießmeier et al. 2004). Other models advocate that the planetary magnetic field is related to the energy flux coming from the planetary core and does not depend on the rotation rate of the planet (Christensen, Holzwarth & Reiners 2009). Recent studies indicate that the planetary field strength is independent of rotation rate, which instead plays a role in the geometry of the generated magnetic field (Zuluaga & Cuartas 2012).

Although planetary magnetism has been observed in several Solar system planets, such as in the Earth and the giant planets, the

presence of exoplanetary magnetic fields is much more elusive. Vidotto et al. (2010b) suggested that the close-in giant planet WASP-12b hosts a bow shock that surrounds its magnetosphere at a distance of about 4–5 planetary radii. Their suggestion was motivated by transit observations of the close-in giant planet WASP-12b by Fossati et al. (2010), who, based on space-borne spectroscopic observations in the near-ultraviolet (UV), showed that the transit light curve of WASP-12b presents both an early ingress when compared to its optical transit, as well as excess absorption during the transit (see also Haswell et al. 2012). Vidotto et al. (2010b) attributed this signature to an absorption of the material in the bow shock (see also Llama et al. 2011). If confirmed, this technique should provide a useful tool for determining planetary magnetic field intensities for hot Jupiter transiting systems. In the case of WASP-12b, Vidotto et al. (2010b) derived an upper limit of 24 G for the planetary field. Vidotto et al. (2011a) later proposed other targets with good prospects to hosting observable early ingresses. Unfortunately, the near-UV (254–258 nm) early-ingress signature of WASP-12b observed with (expensive) space-based spectroscopic observations (Fossati et al. 2010; Haswell et al. 2012) does not seem to be observable with ground-based, broad-band photometry in the wavelength range ~340–540 nm (Haswell et al. 2012), and neither in the range of 303–417 nm (Turner, private communication; for other transiting exoplanets see Turner et al. 2013; Pearson, Turner & Sagan 2014). Observations from Fossati et al. (2010) indicate that the material surrounding WASP-12b absorbs at certain resonance lines in the near-UV (in particular in Mg II lines). The lack of absorption from broad-band photometric observations of WASP-12b possibly indicates that either the material is not absorbing at the observed photometric wavelengths (~303–540 nm), or that the absorption occurs only at some specific spectral lines, but gets diluted over the much wider spectral region.

Another hint that close-in planets may also harbour intrinsic magnetic fields, similar to the Earth and the giant planets of the Solar system, was found by Shkolnik et al. (2003, 2005, 2008), who observed modulations of chromospheric spectral lines in phase with orbital periods on a few systems. Such modulations were interpreted as induced activity on the stellar surface due to magnetic interactions between star and planet. Shkolnik et al. (2008) showed that there exists a correlation between the night-to-night stellar activity variation with the ratio between the planetary mass to orbital period, used as a proxy for the magnetic moment of a tidally locked planet. Although unfortunately this correlation does not provide the intensity of the planetary magnetic field, it offers a way to measure the relative field strength among the different exoplanets in their sample. Therefore, once magnetism is assessed for one of their targets (by a different method), the magnetic field strength of their remaining targets could be derived.

These two suggestions (early ingress and activity enhancement), however, cannot be used as conclusive evidence of the presence of planetary magnetic fields, as alternative, non-magnetic explanations for the observations exist (Preusse et al. 2006; Lai, Helling & van den Heuvel 2010; Bisikalo et al. 2013; Vidotto et al. 2014a). A conclusive way to probe the presence of exoplanetary magnetic fields could be achieved by the detection of radio emission from the planet. The stellar wind that impacts on the planet produces energetic particles that are captured by the planet’s magnetic field, emitting cyclotron radiation at radio wavelengths. This emission depends on the planet’s magnetic field intensity and on the stellar wind power: it implies that the stronger is the stellar wind, the more luminous is the planet. As such radio emission is observed in the Solar system (Zarka 2007), there are expectations that close-in

exoplanets will exhibit comparable radiation (see Nichols 2012 for the case of planets that are not necessarily close-in). In particular, hot Jupiters are expected to be much more luminous than the most luminous planet in our Solar system, Jupiter (e.g. Farrell et al. 1999; Grießmeier et al. 2005; Zarka 2007; Jardine & Cameron 2008; Vidotto et al. 2010a). This is because hot Jupiters are located much closer to their stars, interacting with portions of the host star’s wind that has larger kinetic and magnetic energies available to power planetary radio emission. So far, radio signatures of close-in exoplanets have not yet been detected (e.g. Bastian, Dulk & Leblanc 2000; Lazio et al. 2004; Smith et al. 2009; Hallinan et al. 2013) and one possible reason for that may be due to the lack of instrumental sensitivity in the appropriate frequency range of the observations (Bastian et al. 2000). This picture, however, might be changing, as possible hints of exoplanetary radio emission have recently been reported (Lecavelier des Etangs et al. 2013; Sirothia et al. 2014).

The theoretical estimates of the radio flux emitted by extrasolar planets carry a large uncertainty due to the fact that the stellar wind properties are poorly constrained. In this work, we model the 3D structure of the stellar wind of a sample of five planet-hosting stars, whose 3D winds have not yet been studied to date. We investigate the nature of the interplanetary media of these exoplanetary systems and how different they are from the environment surrounding our own Solar system planets. The stars used in this study, described in Section 2, have had their surface magnetic field recently reconstructed by means of tomographic techniques (Fares et al. 2012, 2013). These surface fields are used as boundary conditions for our data-driven simulations of stellar winds. Our model is described in Section 3. The derived global characteristics of the stellar winds are presented in Section 4, and the properties of the local environment surrounding the exoplanets in our sample are described in Section 5. We then use these computed quantities to calculate the strengths of the interactions between the stellar wind and the planetary system, making it possible to quantitatively predict planetary radio emission and bow shock formation. Our discussion is shown in Section 6, and summary and conclusions are presented in Section 7.

2 THE SAMPLE OF STARS

The stars considered in this study consist of five solar-type stars of spectral types F8 to K1, namely: HD 46375, HD 73256, HD 102195, HD 130322 and HD 179949. All these stars host a gaseous planet at very close orbit (i.e. a hot Jupiter). Table 1 presents a summary of the observationally derived characteristics of the host stars and also

of their hot Jupiters (planet ‘b’). The large-scale surface magnetic field maps of the planet hosts have been reconstructed by Fares et al. (2012, 2013) from a series of circular polarization spectra [acquired at Canada–France–Hawaii Telescope (CFHT)/Echelle SpectroPolarimetric Device for the Observation of Stars (ESPaDOs) and T eloscope Bernard Lyot (TBL)/NARVAL] using the Zeeman–Doppler Imaging (ZDI) technique (e.g. Donati & Brown 1997; Donati et al. 2006). Fig. 1 presents the radial component of the reconstructed surface field of these stars. Our targets present surface magnetic fields with a variety of topologies and intensities. For instance, HD 46375 presents a magnetic field that is mostly dipolar, whose axis is slightly tilted with respect to the rotation axis. HD 73256, on the other hand, has a magnetic field topology that is less axisymmetric.

3 STELLAR WIND MODEL

The stellar wind model we use here is identical to the one presented in Vidotto et al. (2014b). We use the 3D MHD numerical code BATS-R-US (Powell et al. 1999; T oth et al. 2012) to simulate the stellar winds. BATS-R-US solves the set of ideal MHD equations for the mass density ρ , the plasma velocity $\mathbf{u} = \{u_r, u_\theta, u_\phi\}$, the magnetic field $\mathbf{B} = \{B_r, B_\theta, B_\phi\}$ and the gas pressure P :

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0, \quad (1)$$

$$\frac{\partial (\rho \mathbf{u})}{\partial t} + \nabla \cdot \left[\rho \mathbf{u} \mathbf{u} + \left(P + \frac{B^2}{8\pi} \right) \mathbf{I} - \frac{\mathbf{B} \mathbf{B}}{4\pi} \right] = \rho \mathbf{g}, \quad (2)$$

$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{u} \mathbf{B} - \mathbf{B} \mathbf{u}) = 0, \quad (3)$$

$$\frac{\partial \varepsilon}{\partial t} + \nabla \cdot \left[\mathbf{u} \left(\varepsilon + P + \frac{B^2}{8\pi} \right) - \frac{(\mathbf{u} \cdot \mathbf{B}) \mathbf{B}}{4\pi} \right] = \rho \mathbf{g} \cdot \mathbf{u}, \quad (4)$$

where

$$\varepsilon = \frac{\rho u^2}{2} + \frac{P}{\gamma - 1} + \frac{B^2}{8\pi}. \quad (5)$$

We assume the wind is polytropic, in which $P \propto \rho^\gamma$ and γ is the polytropic index. To derive the temperature, we consider an ideal gas, so $P = nk_B T$, where k_B is the Boltzmann constant, T is the temperature, $n = \rho/(\mu m_p)$ is the particle number density of the stellar wind, μm_p is the mean mass of the particle. In this work, we

Table 1. Observationally derived characteristics of the exoplanets and planet-host stars of our sample. The columns are the following: the host-star name, spectral type, mass (M_\star), radius (R_\star), effective temperature (T_{eff}), rotation period (P_{rot}), Rossby numbers (Ro), distance (d), inclination between the stellar rotation axis and the line-of-sight (i) estimated from ZDI, unsigned surface magnetic flux (Φ_0), date of the spectropolarimetric observations, projected mass of the planet ‘b’ ($M_p \sin i$) and semimajor axis of the planetary orbit (a). For uncertainties in the quantities below, we refer the reader to the following literature. All the values listed below were compiled by Fares et al. (2013), except for d , whose references are listed in the footnote of the table, and Ro, which was derived by Vidotto et al. (2014c) using the models of Landin, Mendes & Vaz (2010).

Star ID	Spectral type	M_\star (M_\odot)	R_\star (R_\odot)	T_{eff} (K)	P_{rot} (d)	Ro	d (pc)	i ($^\circ$)	Φ_0 (10^{23} Mx)	Date	$M_p \sin i$ (M_{Jup})	a (R_\star)
HD 46375	K1IV	0.97	0.86	5290	42	2.340	33.4 ^a	45	0.85	2008 Jan	0.2272	10.0
HD 73256	G8	1.05	0.89	5636	14	0.962	36.5 ^b	75	2.1	2008 Jan	1.869	9.0
HD 102195	K0V	0.87	0.82	5290	12.3	0.473	29.0 ^c	50	2.1	2008 Jan	0.453	12.6
HD 130322	K0V	0.79	0.83	5330	26.1	0.782	30.0 ^d	80	0.74	2008 Jan	1.043	23.2
HD 179949	F8V	1.21	1.19	6168	7.6	>1.726	27.0 ^e	60	1.3	2007 June	0.902	7.9

Notes. ^aMarcy, Butler & Vogt (2000); ^bUdry et al. (2003); ^cGe et al. (2006); ^dUdry et al. (2000); ^eHolmberg, Nordstr om & Andersen (2007).

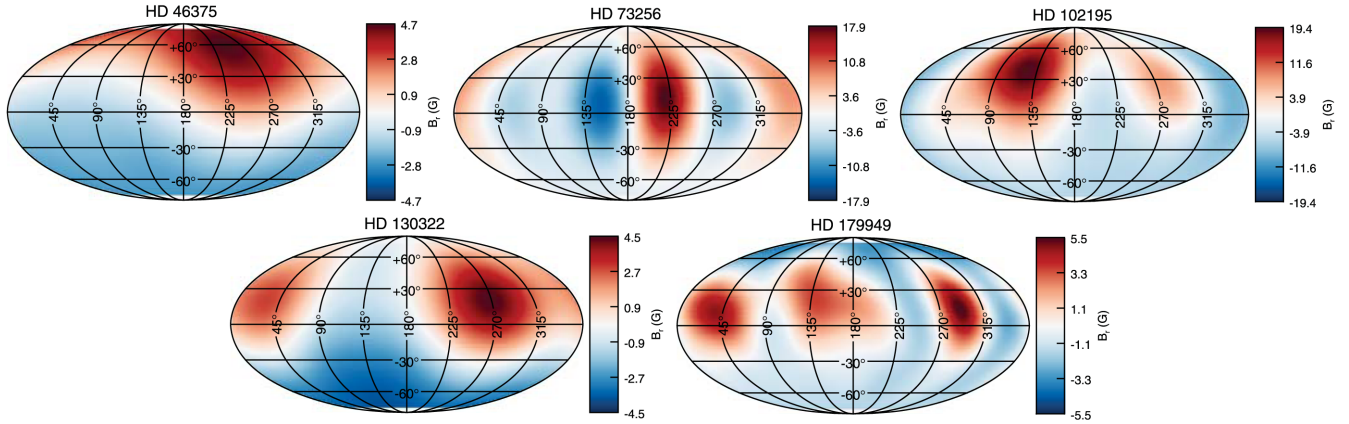


Figure 1. Mollweide projection of the radial component of the stellar surface magnetic field (from Fares et al. 2012, 2013). These observed magnetic maps are included as boundary conditions in our data-driven simulations.

adopt $\gamma = 1.1$, similar to the effective adiabatic index measured in the solar wind (Van Doorselaere et al. 2011), and $\mu = 0.5$, for a fully ionized hydrogen plasma.

At the initial state of the simulations, we assume that the wind is thermally driven (Parker 1958). The stellar rotation period P_{rot} , M_* and R_* are given in Table 1. At the base of the corona ($r = R_*$), we adopt a wind coronal temperature $T_0 = 2 \times 10^6$ K and wind number density $n_0 = 10^9 \text{ cm}^{-3}$ (Section 6.1 discusses the choices of n_0 and T_0 and how they affect our results). With this numerical setting, the initial solution for the density, pressure (or temperature) and wind velocity profiles is fully specified. The radial component of the magnetic field B_r , anchored at the base of the wind, is reconstructed from observations (Fig. 1). The other two components of the surface field are assumed to be potential ($\nabla \times \mathbf{B} = 0$), as it has been shown that stellar winds are largely unaffected by the non-potential part of the observed surface field (Jardine et al. 2013). At the initial state, we assume that the field considered in the simulation box is potential up to a radial distance $r = r_{\text{SS}}$ (known as the source surface) and, beyond that, the magnetic field lines are considered to be open and purely radial. As the simulation evolves in time, the wind particles interact with the magnetic field lines (and vice versa), removing the field from its initial potential state. For all the cases studied here, we take $r_{\text{SS}} = 4R_*$, but we note that different values of r_{SS} produce similar final steady-state solutions for the simulations (Vidotto et al. 2011b, 2014b).

Once set at the initial state of the simulation, the values of the observed B_r are held fixed at the base of the wind throughout the simulation run, as are the coronal base density and thermal pressure. A zero radial gradient is set to the remaining components of \mathbf{B} and $\mathbf{u} = 0$ in the frame corotating with the star. The outer boundaries at the edges of the grid have outflow conditions. The rotation axis of the star is aligned with the z -axis, and the star is assumed to rotate as a solid body. Our grid is Cartesian and the star is placed at the origin of the grid, which extends in x , y and z from -20 to $20R_*$, except for HD 102195, whose simulation box extends from -24 to $24R_*$, as to extend out to the orbit of the planet. BATS-R-US uses block adaptive mesh refinement. The finest resolved cells are located close to the star (for $r \lesssim 2R_*$), where the linear size of the cubic cell is $0.0097R_*$ (or $0.012R_*$ for the simulation of HD 102195). The coarsest cell has a linear size of $0.31R_*$ (or $0.37R_*$ for HD 102195) and is located at the outer edges of the grid. The total number of cells in our simulations is around 40 million. As the simulations evolve in time, both the wind and magnetic field lines are allowed

to interact with each other. The resultant solution, obtained self-consistently, is found when the system reaches steady state in the reference frame corotating with the star.

4 DERIVED PROPERTIES OF THE STELLAR WINDS

Table 2 presents the properties of the stellar winds obtained in our simulations. The unsigned observed surface magnetic flux is

$$\Phi_0 = \oint_{S_*} |B_r(R_*, \theta, \varphi)| dS_*, \quad (6)$$

and the unsigned open magnetic flux is

$$\Phi_{\text{open}} = \oint_{S_{\text{sph}}} |B_r(r, \theta, \varphi)| dS_{\text{sph}}. \quad (7)$$

The surface flux (Table 1) is integrated over the surface of the star S_* and the open flux (Table 2) over a spherical surface S_{sph} at a distance r from the star, where all the magnetic field lines are open. The mass-loss rate \dot{M} of the stellar wind, which outflows along open magnetic field lines, can be calculated as the flux of mass integrated across S_{sph} :

$$\dot{M} = \oint \rho u_r dS_{\text{sph}}, \quad (8)$$

where \dot{M} is a constant of the wind. Similarly, the angular momentum loss rates can be calculated as the angular momentum flux across S_{sph} :

$$\dot{J} = \oint_{S_{\text{sph}}} \left[-\frac{\varpi B_\varphi B_r}{4\pi} + \varpi u_\varphi \rho u_r \right] dS_{\text{sph}} \quad (9)$$

(Mestel & Selley 1970; Mestel 1999; Vidotto et al. 2014b), where $\varpi = (x^2 + y^2)^{1/2}$ is the cylindrical radius. In our simulations, we find that \dot{M} ranges from ~ 2 to $8 \times 10^{-13} M_\odot \text{ yr}^{-1}$ and \dot{J} between ~ 0.14 and $2.4 \times 10^{31} \text{ erg}$ for the stars in our sample. The open flux ranges from 26 to 69 per cent of the large-scale unsigned surface flux. These values are within the range $(4.4\text{--}8.4) \times 10^{22} \text{ Mx}$. For the solar wind, Wang, Sheeley & Rouillard (2006) obtained magnetic field values at the orbit of the Earth in the range between 0.01 and 0.05 mG, or in terms of open magnetic fluxes, in the range $(2.8\text{--}14) \times 10^{22} \text{ Mx}$, depending on the phase of the solar activity cycle. Although the range of open fluxes calculated for the simulations presented here fall within the values of the solar wind, we show in Section 5 that

Table 2. Characteristics of the stellar winds. The columns are the following: the star name, the stellar wind mass-loss rate (\dot{M}), angular momentum loss rate (\dot{J}), unsigned open magnetic flux (Φ_{open}), average radii of the Alfvén surfaces ($\langle r_A \rangle$), its minimum and maximum value (r_A^{min} and r_A^{max}) and the effective radius of the source surface derived from the MHD models ($r_{\text{SS}}^{\text{eff}}$). In our simulations, \dot{M} , \dot{J} and Φ_{open} are conserved within 0.03, 3 and 4 per cent, respectively.

Star ID	\dot{M} ($10^{-13} M_{\odot} \text{ yr}^{-1}$)	\dot{J} (10^{31} erg)	Φ_{open} (Φ_0)	$\langle r_A \rangle$ (R_{\star})	$[r_A^{\text{min}}, r_A^{\text{max}}]$ (R_{\star})	$r_{\text{SS}}^{\text{eff}}$ (R_{\star})
HD 46375	1.9	0.14	0.52	5.1	[3.0, 6.1]	2.7
HD 73256	2.1	2.3	0.26	6.2	[1.8, 8.1]	5.6
HD 102195	3.2	2.0	0.41	6.4	[2.3, 7.5]	5.6
HD 130322	5.8	0.36	0.69	3.5	[1.6, 4.2]	1.9
HD 179949	8.0	2.4	0.34	2.8	[1.0, 3.7]	3.0

Table 3. Derived characteristics of the hot Jupiters and of their local environments. The columns are, respectively, the planet name, the averages of the local velocity of the wind in the reference frame of the planet, wind density, magnetic field strength, wind temperature, total pressure, planetary magnetospheric radius, shock angle, auroral oval opening angle and fractional area of the polar cap. These quantities were averaged over the subplanetary longitude. Values in brackets represent the minimum and maximum values of the averaged quantity.

Planet ID	$\langle \Delta u \rangle$ (km s^{-1})	$\langle n \rangle$ (10^5 cm^{-3})	$\langle B \rangle$ (mG)	$\langle T \rangle$ (10^6 K)	$\langle p_{\text{tot}} \rangle$ ($10^{-4} \frac{\text{dyn}}{\text{cm}^2}$)	$\langle r_M \rangle$ (R_p)	$\langle \theta_{\text{shock}} \rangle$ ($^{\circ}$)	$\langle \alpha_0 \rangle$ ($^{\circ}$)	$\langle A_{\text{auroral}} \rangle$ (A_{planet})	$\langle \phi_{\text{radio}} \rangle$ (mJy)
HD 46375b	234 [228, 242]	1.8 [1.7, 2.0]	8.8 [0.55, 11]	0.87 [0.86, 0.91]	1.1 [1.0, 1.2]	5.1 [5.0, 5.2]	52 [50, 53]	26.2 [26.0, 26.6]	0.10 [0.10, 0.11]	0.037 [0.036, 0.043]
HD 73256b	263 [217, 345]	2.0 [1.6, 2.6]	17 [2.6, 26]	1.1 [0.91, 1.6]	1.6 [1.0, 2.7]	4.8 [4.4, 5.2]	57 [44, 67]	27.1 [26.1, 28.5]	0.11 [0.10, 0.12]	0.045 [0.027, 0.081]
HD 102195b	288 [240, 338]	1.5 [1.1, 2.0]	14 [3.6, 18]	0.96 [0.87, 1.2]	1.3 [1.1, 1.6]	5.0 [4.8, 5.1]	65 [61, 69]	26.6 [26.2, 27.1]	0.11 [0.10, 0.11]	0.067 [0.054, 0.086]
HD 130322b	322 [316, 334]	0.6 [0.6, 0.7]	2.3 [0.36, 2.9]	0.78 [0.77, 0.79]	0.62 [0.58, 0.69]	5.6 [5.5, 5.7]	74 [74, 75]	25.0 [24.8, 25.2]	0.09 [0.09, 0.10]	0.055 [0.053, 0.061]
HD 179949b	243 [225, 257]	5.9 [5.5, 6.2]	9.6 [1.4, 15]	0.97 [0.96, 0.99]	3.8 [3.1, 4.1]	4.2 [4.1, 4.3]	53 [51, 55]	29.3 [28.9, 29.6]	0.13 [0.12, 0.13]	0.112 [0.092, 0.127]

the values of the interplanetary magnetic field at the orbits of the hot Jupiters are more than 100 times larger than the interplanetary magnetic field at the Earth’s orbit (compare 0.01 to 0.05 mG to the values presented in Table 3).

The left-hand panels in Fig. 2 show the final configuration of the magnetic field lines obtained through self-consistent interaction between magnetic and wind forces after the simulations reached steady state. Although we assume the magnetic field is current-free in the initial state of our simulations, this configuration is deformed when the interaction of the wind particles with the magnetic field lines (and vice versa) takes place (currents are created in the system). The right-hand panels of Fig. 2 show the Alfvén surface S_A of each simulation. This surface is defined as the location where the wind velocity reaches the local Alfvén velocity ($v_A = B(4\pi\rho)^{-1/2}$). Inside S_A , where the magnetic forces dominate over the wind inertia, the stellar wind particles are forced to follow the magnetic field lines. Beyond S_A , the wind inertia dominates over the magnetic forces and, as a consequence, the magnetic field lines are dragged by the stellar wind. In models of stellar winds, the Alfvén surface has an important property for the characterization of angular momentum losses, as it defines the lever arm of the torque that the wind exerts on the star (e.g. Weber & Davis 1967). Its location is also relevant in the studies of magnetic interactions with planets (e.g. Cohen et al. 2014; Strugarek et al. 2014). As shown in Vidotto et al. (2014b), the Alfvén surfaces of the objects investigated here have irregular, asymmetric shapes as a consequence of the irregular distribution of the observed magnetic field. To illustrate the difference in sizes of these surfaces, we show in the right-hand panels of Fig. 2 the scales of the images plotted (red lines). We find that the average radius

of the Alfvén surfaces range between $2.8 R_{\star}$ (for HD 179949) and $6.4 R_{\star}$ (for HD 102195).

In order to provide constraints for analytical methods of extrapolation of magnetic field lines, we also compute here the MHD equivalent of the source surface. In particular, the potential field source surface (PFSS) method has proven to be a fast and simple way to extrapolate surface magnetic fields into the stellar coronal region (Jardine et al. 1999; Jardine, Collier Cameron & Donati 2002; Vidotto et al. 2013). It is also used here as the initial conditions for our simulations. However, the PFSS method has an unconstrained parameter: the radius r_{SS} of the source surface, beyond which the magnetic field lines are assumed open and purely radial, as a way to mimic the effects of a stellar wind. Because of stellar rotation and magnetic field stresses, in the MHD solutions, the surface where all magnetic field lines are purely radial does not exist – even in the region of open field lines, there is always B_{θ} and, especially, B_{φ} components that are non-null. Therefore, we define here an ‘effective radius of the source surface’ $r_{\text{SS}}^{\text{eff}}$ as the radius of the spherical surface where 97 per cent of the average magnetic field is contained in the radial component (i.e. $\langle |B_r| \rangle / \langle |B| \rangle = 0.97$, based on Riley et al. 2006). For some of the stars in our sample (HD 73256 and HD 179949), the ratio $\langle |B_r| \rangle / \langle |B| \rangle$ does not reach the 97 per cent level and in such cases, we take $r_{\text{SS}}^{\text{eff}}$ to be the position where $\langle |B_r| \rangle / \langle |B| \rangle$ is maximum. Table 2 shows that $r_{\text{SS}}^{\text{eff}}$ is in the range between $1.9 R_{\star}$ and $5.6 R_{\star}$, indicating a compact region of closed field lines. We note that this size is similar to the usual adopted size of $2.5 R_{\odot}$ from PFSS methods of the solar coronal magnetic field and also similar to the values obtained in other MHD simulations of winds (Riley et al. 2006; Vidotto et al. 2011b, 2014b).

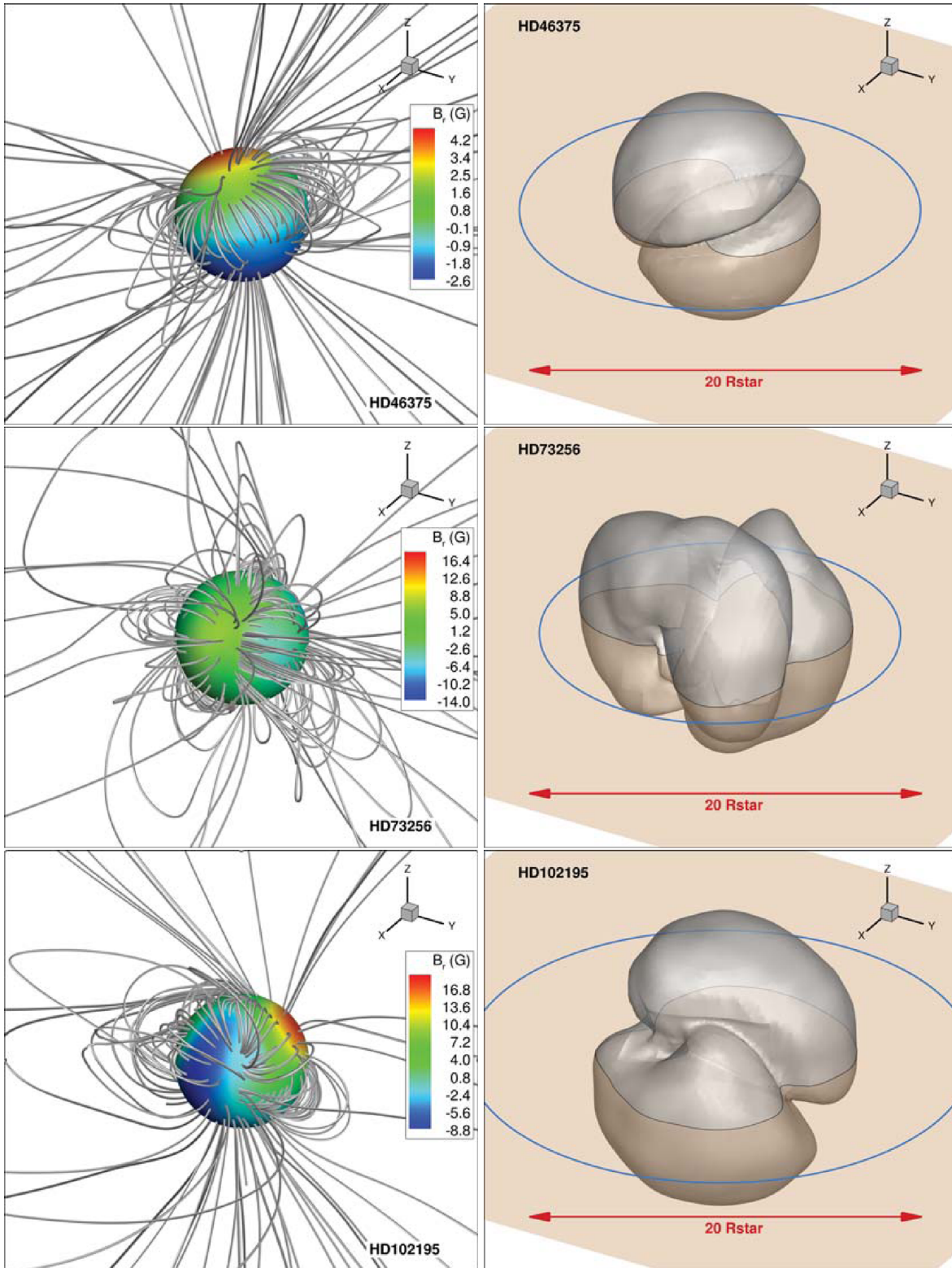


Figure 2. Left: the final configuration of the magnetic field lines after the wind solution has relaxed in the grid. Overplotted at the surface of the star is the observationally reconstructed stellar magnetic field (Fares et al. 2012, 2013), used as boundary condition for the radial magnetic field. Right: the Alfvén surfaces are shown in grey. Note their irregular, asymmetric shapes due to the irregular distribution of the observed field. The equatorial (xy) planes of the star, assumed to contain the orbits of the planet, are also shown, as are the intersections between the xy plane and the Alfvén surface (thin black contour) and the orbital radius of the planet (thick blue contour).

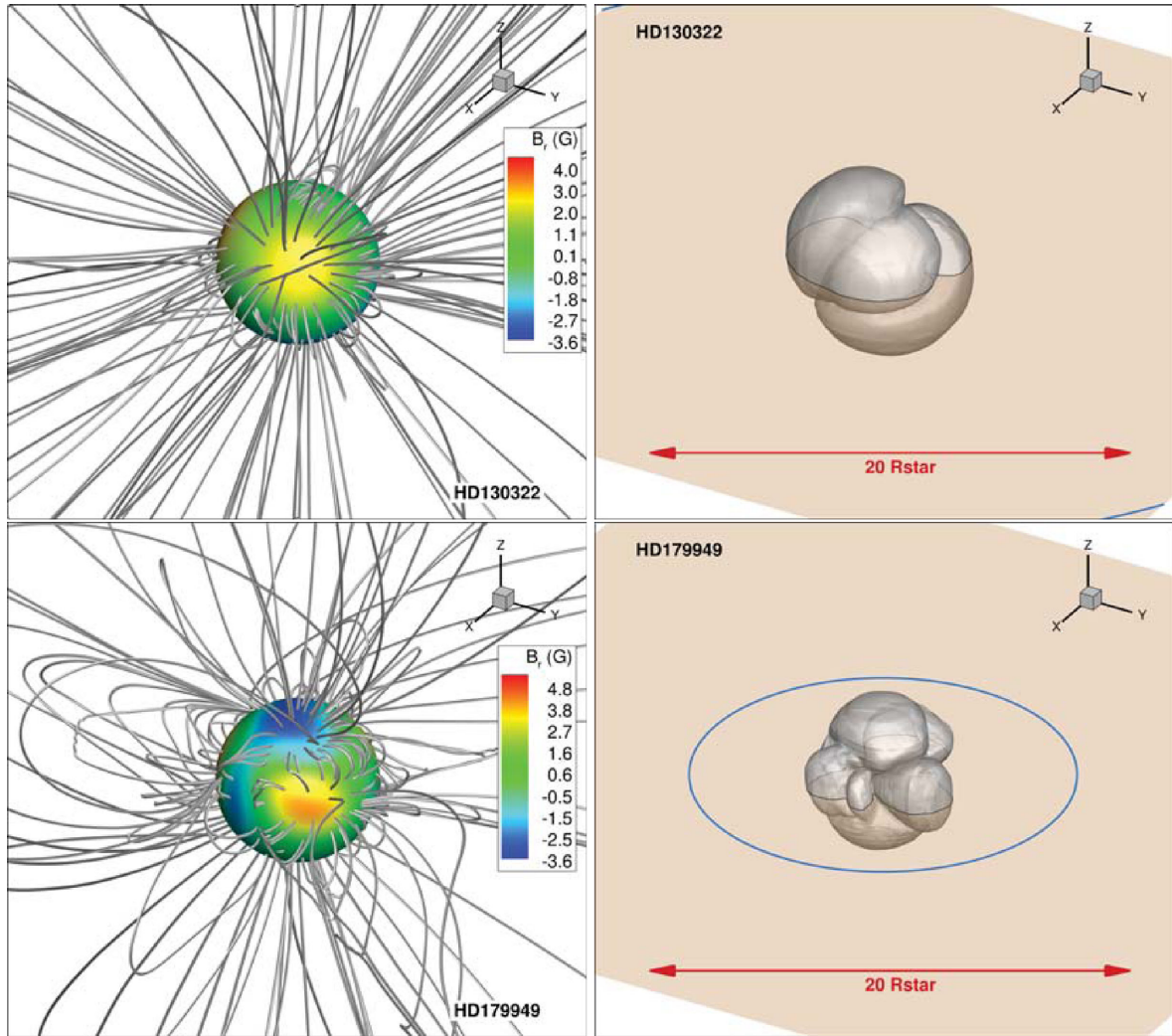


Figure 2 – continued.

5 CHARACTERIZING THE LOCAL ENVIRONMENT SURROUNDING HOT JUPITERS AND RESULTANT INTERACTIONS

All the stars in our sample host giant planets orbiting at close distances. Mercury, the closest planet to our Sun, has a semimajor orbital axis of about 0.39 au, or equivalently, of about $83 R_{\odot}$. The hot Jupiters in our sample have considerably closer orbits, with semimajor axes of about $9\text{--}23 R_{\star}$ (i.e. about 9–4 times closer than Mercury). As a consequence, the hot Jupiters in our sample interact with much denser winds that have larger ram pressures than those typically found around the planets in the Solar system. In addition, because the hot Jupiters are located much closer to the star, the large-scale magnetic field at the orbit of these planets has also a larger strength compared to the interplanetary magnetic field strength of our Solar system planets.

The orbital planes of the planets considered in this work are not known. Here, we assume their orbits lie in the equatorial plane of the star. This seems to be a reasonable hypothesis for our targets (cf. Table 1), as planets orbiting stars cooler than 6200 K have been observed to have small (projected) obliquities (Winn et al. 2010). Fig. 3 shows the total pressure p_{tot} (i.e. the sum of thermal, magnetic and ram pressures) experienced by a planet as it orbits at

the equatorial plane of the stars. Note that the ram pressure term must take into account the relative motion of the planet through the interplanetary medium. Here, we assume prograde motion of the planetary orbit relative to the stellar rotation. The white circles indicate the orbital radii of each hot Jupiter, taken here to be circular (note that for the systems investigated here the eccentricities are rather small, <0.06). The colour bar is the same for the five images, illustrating that the total pressure varies from planet to planet. The last panel in Fig. 3 shows the total *local* pressure at the planetary orbits as a function of subplanetary longitude (see also Table 3). For the cases studied here, at these orbital distances, the dominant term in the total pressure is the ram pressure of the relative motion of the planet through the wind. The values of the local total pressure are within $(0.58\text{--}4.1) \times 10^{-4} \text{ dyn cm}^{-2}$, which are about four orders of magnitude larger than the ram pressure of the solar wind at the Earth’s orbit ($1.8 \times 10^{-8} \text{ dyn cm}^{-2}$; See et al. 2014). We also note that there is some variability in the local total pressure, showing that the planets interact with the varying environment of the star along their orbits. In the case of HD 73256, the amplitude of this variability is the highest among the cases studied here and is due to the peak (which is a factor of 1.9 above the average value of p_{tot} of HD 73256) at $\sim 220^{\circ}$. This peak is caused by a fast wind stream, associated with the magnetic feature seen in the surface magnetograms at

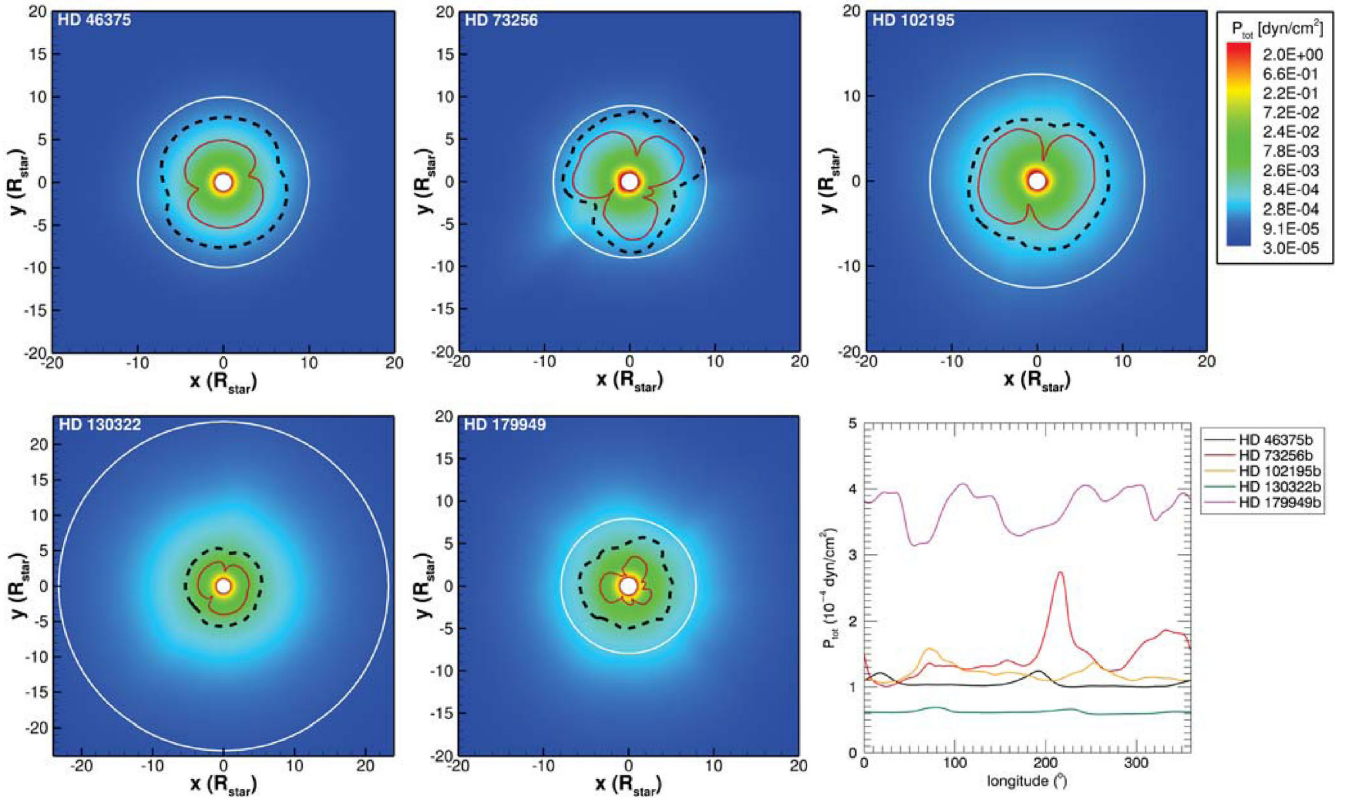


Figure 3. Distribution of the total pressure p_{tot} experience by a planet as it orbits at the equatorial plane of each star in our simulations. The black dashed and solid red contours are cuts of the fast magnetosonic and Alfvén surfaces of the stellar wind, respectively, at the equatorial plane. The white lines indicate the orbital radii, taken to be circular, of the hot Jupiters. The last panel shows the total local pressure at these orbits as a function of subplanetary longitude.

longitude $\sim 225^\circ$ (Fig. 1). A similar feature appears in Figs 4 and 5 that we present later. Variability on larger time-scales due to intrinsic variations of the stellar magnetic field can also alter the environment of surrounding planets (Vidotto, Jardine & Helling 2011c; Vidotto et al. 2012; Llama et al. 2013), but it is not considered in the present work.

5.1 Exoplanetary bow shocks: sizes and orientations

If a planet is magnetized, its magnetic field can act as shield for the stellar wind, deflecting the wind particles and potentially preventing the wind from reaching down to the planetary atmosphere. A way to estimate the size of this stand-off distance is by pressure balance between the local total pressure of the interplanetary medium (i.e. the stellar wind) and the planet total pressure. Thus, at the interaction zone, we have

$$p_{\text{tot}} = \frac{B_{p,r_M}^2}{8\pi}, \quad (10)$$

where B_{p,r_M} is the planetary magnetic field intensity at a distance r_M from the planet centre. Equation (10) neglects the planetary thermal pressure component on the right-hand side. Because of the exponential decay of planetary densities, at the height of a few planetary radii, the thermal pressure is usually negligible compared to the planetary magnetic pressure. If we assume the planetary magnetic field is dipolar, we have that $B_{p,r_M} = B_{p,\text{eq}}(R_p/r_M)^3$, where R_p is the planetary radius and $B_{p,\text{eq}}$ its surface magnetic field at the equator (half the value of the intensity at the magnetic pole). For a

planetary dipolar axis aligned with the rotation axis of the star, the magnetospheric size of the planet is given by

$$\frac{r_M}{R_p} = \left[\frac{B_{p,\text{eq}}^2}{8\pi p_{\text{tot}}} \right]^{1/6}. \quad (11)$$

In the absence of observational constraints, we assume the hot Jupiters studied here to host magnetic fields similar to Jupiters. Fig. 4(a) shows the magnetospheric sizes of these hot Jupiters assuming $B_{p,\text{eq}} = 7$ G (i.e. half of the maximum observed field of Jupiter of ~ 14 G; Smith et al. 1975; Bagenal 1992). The average estimated magnetospheric sizes range from about $\langle r_M \rangle = 4.2R_p$ for HD 179949b to $\langle r_M \rangle = 5.6R_p$ for HD 130322b (see Table 3). Variations in r_M along the planetary orbit are roughly ~ 10 per cent. This variation occurs because, as the planet goes along its orbit and probes regions with different p_{tot} , its magnetospheric size reacts accordingly, becoming smaller when the external p_{tot} is larger and vice versa.

Overplotted to Fig. 3 are the contours at the equatorial plane of the Alfvén surface (red lines) and the magnetosonic surface (black lines) of the stellar wind. In all the cases studied here, the planets orbit at regions of superfast magnetosonic velocities of the stellar wind. One exception is the case of HD 73256b, in which a small part of its orbit (white circle) lies within the fast magnetosonic surface of the wind. This does not necessarily mean that at these orbital positions a bow shock will not be formed surrounding HD 73256b’s magnetosphere. Rather, it is the relative velocity of the planet orbiting through the stellar wind:

$$\Delta \mathbf{u} = \mathbf{u} - u_K \hat{\phi}, \quad (12)$$

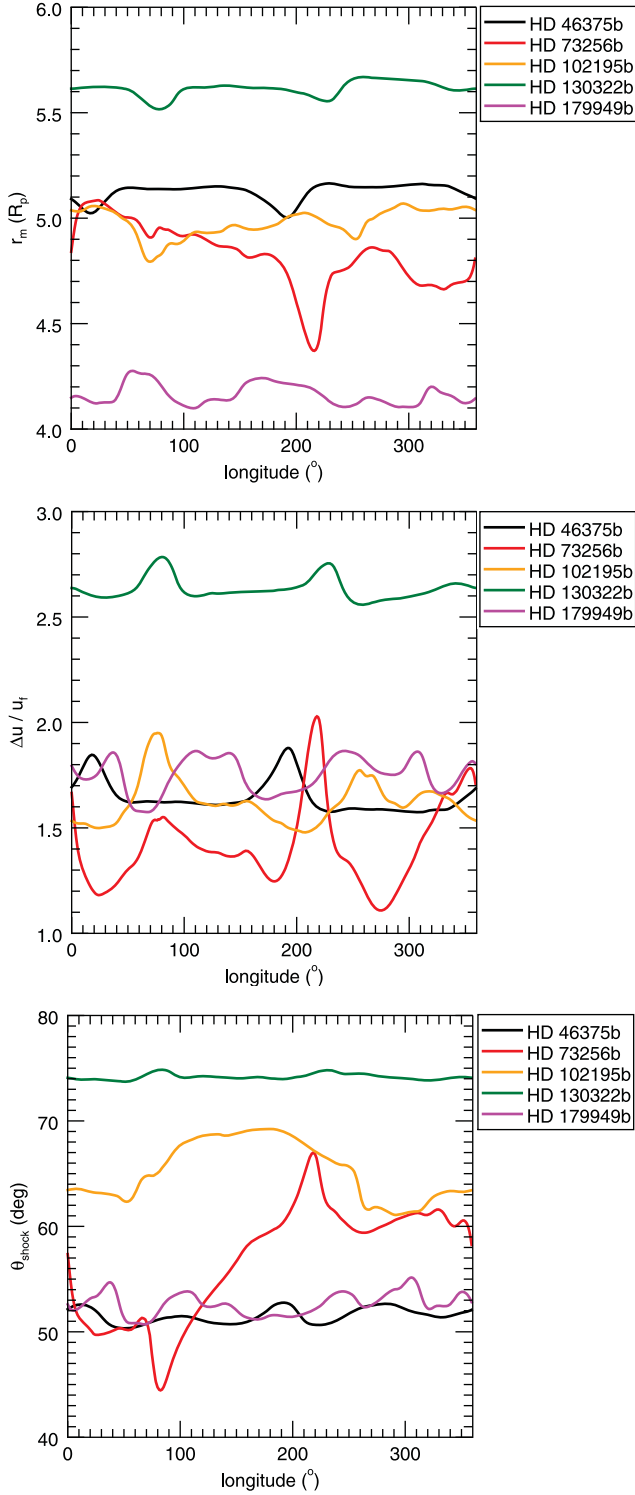


Figure 4. As a magnetized planet orbits around its host star, it probes regions of the stellar wind with different properties. As a consequence, its magnetospheric size and shock orientation change. Upper panel: the magnetospheric stand-off distance for the hot Jupiters studied here as a function of subplanetary longitude. Middle panel: the ratio between the relative velocity of the planet and the local fast magnetosonic velocity. Bottom panel: the angle formed between the shock normal and the tangent of a circular orbit. The top and bottom figures assume the hot Jupiters have a dipolar field of 7 G at their equator.

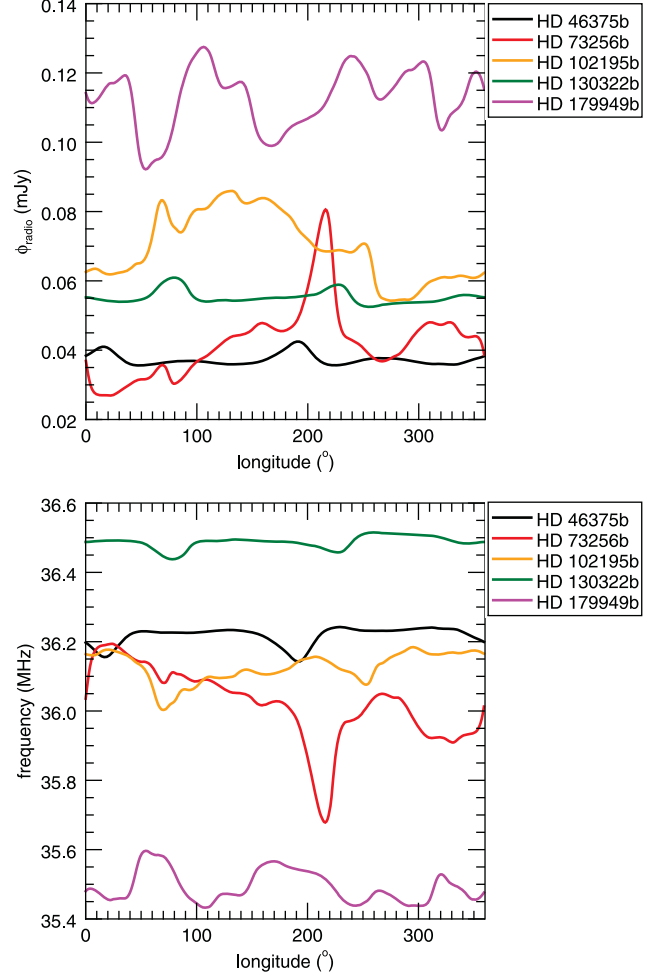


Figure 5. The predicted radio flux (equation 16) computed using the results of our wind simulations (top) and associated frequency of emission (bottom) assuming the emission bandwidth is the cyclotron frequency (equation 17). These results assume a dipolar exoplanetary magnetic field, whose intensity is 7 G at the equator.

where u_K is the (purely azimuthal) Keplerian velocity of the planet that should be compared to the fast magnetosonic velocity of the local plasma $v_f = (c_s^2 + v_A^2)^{1/2}$, where c_s is the local sound speed. Fig. 4(b) shows the fast magnetosonic Mach number ($\Delta u/v_f$) calculated at the orbital radii of the hot Jupiters, where we see that the relative planetary velocity is always superfast magnetosonic (i.e. $\Delta u/v_f > 1$), indicating that the magnetosphere of these planets are surrounded by bow shocks.

It has been proposed that these bow shocks might absorb at specific wavelengths, generating asymmetric transit light curves (Vidotto et al. 2010b). This is particularly relevant for the case of hot Jupiters, in which the orientation of the bow shock is shifted towards the direction of planetary motion (as opposed to the bow shocks surrounding the Solar system planets, which are largely formed facing the Sun). These ‘sideways’ bow shocks present the best conditions for detection during planetary transits (Llama et al. 2011, 2013). Although the hot Jupiters investigated here are not transiting and do not have constrained orbital inclinations, there have been cases in the literature of non-transiting (but grazing) exoplanets whose extended atmospheres might undergo partial transit (Ehrenreich et al. 2012). Likewise, combined with the orbital

inclinations, it is possible that bow shocks of non-transiting planets might be visible if they graze the stellar disc. We, here, do not model the 3D extent of bow shocks, as done in Llama et al. (2011, 2013), but we can calculate the angle between the shock normal and the tangent of a circular orbit:

$$\theta_{\text{shock}} = \arctan\left(\frac{u_r}{|u_K - u_\phi|}\right) \quad (13)$$

(Vidotto et al. 2010b). Along its orbital path, the planet probes regions of the wind with different velocities, which implies that the orientation of the bow shock that forms surrounding planetary magnetospheres changes along the planetary orbit. This can be seen in Fig. 4(c) and Table 3, where we present θ_{shock} as a function of the subplanetary longitude. We present in Table 3 the average shock angle ($\langle\theta_{\text{shock}}\rangle$) of the bow shock of each of these hot Jupiters, where we note that they range from about 52° to 74° .

5.2 Exoplanetary auroral ovals: escape channels and radio emission

As the planetary magnetosphere extent is reduced, the size of the ‘auroral oval’, which is the amount of planetary area with open magnetic field lines, increases. Along these open field lines, particles can be transported to/from the interplanetary space, affecting, for instance, the amount of atmospheric mass loss (Adams 2011). We estimate here the size of the auroral region of the planet as follows. Assuming the planet to have a dipolar magnetic field, aligned with the planetary orbital spin axis, the colatitude of the largest closed field line of the planet, which defines the boundary between open- and closed-field line regions, can be estimated as $\alpha_0 = \arcsin(R_p/r_M)^{1/2}$ (Siscoe & Chen 1975; Tarduno et al. 2010). This implies in a fractional area of the planetary surface that has open magnetic field lines:

$$\frac{A_{\text{polar cap}}}{A_{\text{planet}}} = (1 - \cos \alpha_0) \quad (14)$$

(Vidotto et al. 2013). Therefore, in addition to making r_M smaller, a stronger external pressure of the stellar wind exposes a larger area of the polar cap of the planet. Table 3 shows the average, minimum and maximum angles of the auroral ovals (α_0) and fraction of open area ($\langle A_{\text{polar cap}} \rangle$) as calculated by equation (14). For the hot Jupiters analysed here, (α_0) ranges between 25° and 29° , and $\langle A_{\text{polar cap}} \rangle$ ranges between 9 and 13 percent. For comparison, the size of the auroral oval in Saturn is $\alpha_0 \simeq 10^\circ$ – 20° (Clarke et al. 2005) and at the Earth it is $\alpha_0 \simeq 17^\circ$ – 20° (Milan et al. 2009). Using equation (14), a rough estimate indicates that the open-field-line region covers ~ 1.5 – 6 per cent of Saturn’s surface and ~ 4.5 – 6 per cent of Earth’s surface. This is a factor of ~ 2 smaller than the values we derive for the hot Jupiters in our sample, but not as extreme as the cases of planets orbiting at the habitable zone of more active stars (Vidotto et al. 2013).

Planetary radio emission takes place in a hollow cone of half-aperture angle given by the auroral oval colatitude α_0 . It has been recognized that the radio emission of the Earth and the four giant planets of the Solar system correlates to the local characteristics of the solar wind (e.g. Zarka 1998), an indication that radio emission is powered by the local solar wind. Analogously, it is expected that when exoplanets interact with the wind of their host stars, they would also be sources of radio emission.

We use the results of our stellar wind simulations to calculate the kinetic power of the wind, at the orbital radii of the hot Jupiters studied here. Our approach follows closely the one in Vidotto et al.

(2012). The kinetic power P_k of the impacting wind on the planet is approximated as the ram pressure of the particles $\rho(\Delta u)^2$ impacting on the planet, with effective cross-section πr_M^2 , at a relative velocity Δu :

$$P_k \simeq \rho(\Delta u)^3 \pi r_M^2. \quad (15)$$

The radio flux can be written as

$$\phi_{\text{radio}} = \frac{P_{\text{radio}}}{d^2 \omega \Delta f} = \frac{\eta_k P_k}{d^2 \omega \Delta f}, \quad (16)$$

where d is the distance to the system, $\omega = 2 \times 2\pi(1 - \cos \alpha_0)$ is the solid angle of the hollow emission cone (defined by the auroral oval) and Δf is the frequency of emission. In the last equality, we assumed a linear efficiency η_k in converting the power released from the dissipation of kinetic wind energy to radio emission (‘radiometric Bode’s law’). We adopt $\eta_k = 10^{-5}$, as derived from observations of the Solar system planets (Zarka 2007). Here, we assume that the emission bandwidth Δf is approximately the cyclotron frequency (Grießmeier et al. 2007):

$$\Delta f = \frac{e B_p(\alpha_0)}{m_e c} = 2.8 \left[\frac{B(\alpha_0)}{1 \text{ G}} \right] \text{ MHz}, \quad (17)$$

where m_e is the electron mass and c the speed of light. $B_p(\alpha_0)$ is the planet’s magnetic field strength at colatitude α_0 of the auroral ring. For a dipolar field, $B_p(\alpha_0) = B_{p, \text{eq}}(1 + 3\cos \alpha_0)^{1/2}$.

To compute the radio flux (equation 16), we need to know the physical size of r_M . This value, normalized to the planet’s radius, is given in Fig. 4(a) and we further assume planetary radii of $1.5R_{\text{Jup}}$ for all the hot Jupiters analysed in this work (note that they are non-transiting planets and therefore do not have observationally determined radii). Equation (16) is the only place where the physical size of the exoplanet is required and different choices of R_p influence the estimated radio flux as $\phi_{\text{radio}} \propto r_M^2 \propto R_p^2$.

Fig. 5(a) shows the radio flux computed using the results of our wind simulations and Fig. 5(b) shows the calculated frequency of emission. We find that the predicted emission frequency occurs at ~ 36 MHz and the radio fluxes range between 0.02 and 0.13 mJy among all the cases studied here (see also Table 3). Values of radio fluxes such as these (including the peak values that occur at favourable phases) should be challenging to be observed with present-day technology, such as with Low-Frequency Array (LOFAR), whose sensitivity at 20–40 MHz is $\gtrsim 30$ – 3 mJy, respectively, for a 1-h integration time (Grießmeier, Zarka & Girard 2011). It is likely, however, that even these small radio fluxes will be detectable with future higher sensitivity arrays, such as the Square Kilometre Array (SKA)-low array system.

Among the systems studied here, HD 179949b has the highest estimated radio flux. This occurs for two reasons. First, this exoplanet has the closest orbital radius and, because of that, $\rho \Delta u^3$ is the largest among our sample; for the same reason, it also has the smallest r_M (cf. Tables 1 and 3). In spite of the smallest cross-section πr_M^2 , the large $\rho \Delta u^3$ term is more important in equation (15), which results in the largest stellar wind kinetic power impacting on the magnetosphere of the exoplanets studied here. Second, the closest distance to the HD 179949 system also favours a larger radio flux (equation 16).

It is also worth comparing the emission calculated here and the values calculated for τ Boo b and HD 189733b.¹ Using the same

¹ Note that the stellar wind simulations presented in Vidotto et al. (2012) and Llama et al. (2013) have the same assumptions as the ones shown in the present work.

radio emission model presented here, Vidotto et al. (2012) estimated the radio flux of τ Boo b at different epochs of the host star's magnetic cycle. They found the radio flux of τ Boo b to be of the order of 0.5–0.9 mJy. We can also use the simulations presented in Llana et al. (2013) to compute the radio flux of HD 189733b. Assuming a planetary radius of $R_p = 1.15 R_{\text{Jup}}$ and a distance of 19.3 pc, we calculate the radio flux of HD 189733b to be on average 0.47 mJy (peak at 0.98 mJy) for the case where the observed stellar magnetic map is derived from the 2007 June observations and 0.23 mJy (peak at 0.51 mJy) for the 2008 July map (cf. Fares et al. 2010).

The radio fluxes computed for τ Boo b and HD 189733b are therefore considerably larger than the values computed for the exoplanets presented here, having better prospects for being detected. The reason why these two systems have higher radio fluxes is similar to the reasons discussed for the case of HD 179949b: a combination of closer orbital radii ($6.8 R_*$ and $8.6 R_*$ for τ Boo b and HD 189733b, respectively) and closer distances to the systems (15.6 and 19.3 pc). It is also expected that exoplanets orbiting young stars (with denser stellar winds) are likely to produce higher radio fluxes (Grießmeier et al. 2005; Vidotto et al. 2010a), presenting also better prospects for detection of exoplanetary radio emission.

Radio fluxes estimated for the five hot Jupiters studied here have been estimated by other authors. For instance, Grießmeier et al. (2011) predicted radio fluxes that are larger than the values predicted here by a factor of 500–2000 (compared to the case for their rotation-independent planetary magnetic field model). Although our radio emission model is similar to the one used in Grießmeier et al. (2011) (i.e. both our models assume a ‘radiometric Bode’s law’, in which a fraction of the dissipation of the wind power is converted into planetary radio emission), we attribute the difference found between their work and the present one due to the different models assumed for the stellar wind and stellar magnetic field, as well as for the assumed planetary magnetic field intensities. For the stellar wind, Grießmeier et al.’s work assumes a spherically symmetric, isothermal wind model (Parker 1958). The velocity and density structures are scaled with respect to the age of the system, based on the age relations found by Newkirk (1980) and Wood et al. (2005). For the planetary magnetic field, Grießmeier et al.’s work assumes either a case where the planetary dynamo is independent (Reiners & Christensen 2010) or dependent (Grießmeier et al. 2004) on the planetary rotation. Grießmeier et al. (2011) showed that the intensity of the planetary magnetic field affects the frequency of the emission (as in our model) and that the radio flux has a strong dependence with the intensity of the planetary magnetic field (contrary to our model). More recently, See et al. (2015) studied the variability of exoplanetary radio emission for a sample of planet host stars, which includes the objects studied in the present work. Similar to our model, their model incorporates the realistic large-scale geometry of the stellar magnetic field, but their radio emission model differs from ours. Instead, their study was based on the model developed by Jardine & Cameron (2008), which computes the radio emission generated by energetic electrons released in the reconnection between stellar and exoplanetary magnetic field lines, without assuming the a priori relation of the ‘radiometric Bode’s law’. Despite the differences in these models, the radio fluxes estimated by See et al. (2015) and by us are very similar, within a factor of 1–4, except for HD130322, in which we estimate radio fluxes that are 100 times larger than theirs. In addition to providing information on exoplanetary’s magnetic field, detection of exoplanetary radio emission would clearly provide invaluable constraints to stellar wind models as well.

6 DISCUSSION

6.1 Limitations of the models

The stellar wind models presented in this paper use as input the observationally reconstructed stellar magnetic field and are, therefore, more realistic (and provide an advance) compared to models that are non-magnetized or that assume simplified stellar magnetic field topologies. In spite of that, our wind models share the limitations of global, polytropic wind models. In particular, these types of models have three parameters that are poorly constrained by observations, namely, the wind base density and temperature and the temperature profile (i.e. the profile of energy deposition through the parameter γ). In this work, we have chosen to set all these three parameters to be the same for all the stars in our sample. On the other hand, parameters such as the stellar mass, radius, rotation period and magnetic field differ for each object and are constrained to values observationally derived for each stars (Table 1).

Johnstone & Guedel (2015) recently showed that the average temperature of X-ray coronae (T_{cor}) is a weak function of X-ray flux F_X : $\langle T_{\text{cor}}[\text{MK}] \rangle = 0.11(F_X/[\text{erg s}^{-1} \text{cm}^{-2}])^{0.26}$ (see also Telleschi et al. 2005). Using their relation, the X-ray luminosities compiled in Vidotto et al. (2014c) and the stellar radii from Table 1, we estimate $\langle T_{\text{cor}} \rangle$ to be in the range between 2 and 3.6 MK for the stars in our sample. Naively, one could expect that the temperature at the base of the wind is related to the temperature of the closed X-ray corona (and this is the case for our Sun), but it is not clear if this relation is true for other stars. Therefore, in the absence of a stronger constraint, in our models, we adopt a wind base temperature of 2 MK, typical of stellar coronae of solar-type stars. We adopt γ that is the same as the effective adiabatic index measured in the solar wind (Van Doorsselaere et al. 2011). For the base density, we adopted a value of 10^9 cm^{-3} . Ideally, observations of mass-loss rates of cool dwarf stars would allow us to place better constraints on the densities. However the lack of, or difficult-to-obtain, observational signatures of these winds make constraints of base density (or mass-loss rates) challenging to be obtained.

To investigate how our results change with the change in the wind base density, we performed a stellar wind simulation of HD 46375 that results in a mass-loss rate ($\dot{M} = 2.9 \times 10^{-14} M_{\odot} \text{ yr}^{-1}$) that is similar to the one observed in the solar wind ($\dot{M} = 2 \times 10^{-14} M_{\odot} \text{ yr}^{-1}$). Compared to the values of HD 46375 reported in Table 2, in this simulation, we found a mass-loss rate that is a factor of 6.5 smaller, \dot{J} that is a factor of 3 smaller and Φ_0 that is a factor of 1.3 smaller.

Locally, the hot Jupiter HD 46375b experience a total external pressure whose average value (averaged over the longitude of the subplanetary point) is a factor of 5.6 smaller than the value presented in Table 3. Because r_M is weakly dependent on p_{tot} ($r_M \propto p_{\text{tot}}^{-1/6}$), the value of r_M we estimated before is smaller by a factor of only 1.3. In spite of the larger the cross-section of the planetary magnetosphere, the radio flux decreased by a factor of 2.3, caused by the decrease in the ram pressure (equation 15).

Another parameter we have assumed in our models is the planetary magnetic field intensity. As discussed in Section 1.1, this is a quantity that has yet not been measured in exoplanets. Here, we adopted a magnetic field intensity which is similar to the value of Jupiter. We can also estimate how the magnetospheric size we presented in Fig. 4(a) would have changed if a different field strength were to be adopted. Because $r_M \propto B_p^{1/3}$, a strength that is a factor of 2 smaller would decrease the reported values of r_M by $2^{1/3}$ (i.e. only 25 per cent). In spite of that, this would not have significantly altered

the computed radio flux (our radio flux model is weakly dependent on the planetary field strength; see discussion in Vidotto et al. 2012), but would have decreased the frequency of the emission by a factor of 2, making it not possible to be observed from the ground, due to the Earth’s ionospheric cut-off in frequencies. Indeed, one of the possibilities that exoplanetary radio emission has not been detected so far might be due to a frequency mismatch between the emission source and that of the search instruments (Bastian et al. 2000).

6.2 Exoplanetary system conditions for detectability at radio wavelengths

Because of the cyclotron nature of the magnetospheric radio emission, exoplanets with higher magnetic field strengths emit at higher frequencies, where the detection sensitivity is larger. For instance, an exoplanet with a magnetic field of about 40–50 G emits at the frequency range between 110 and 140 MHz. The sensitivity of LOFAR at 100–200 MHz is roughly about 0.05 mJy (cf. fig. 1 in Grießmeier et al. 2011). This indicates that, except for HD 46375b, all the remaining exoplanets studied here could in principle be detectable with LOFAR, if their magnetic field strengths were about 40–50 G. Compared to Jupiter’s maximum field intensity, these field strengths are about ~ 3 times higher.

We can also estimate what would be the required dissipated stellar wind power to generate detectable radio signatures from the exoplanets studied here. In this exercise, we take the same exoplanetary magnetic field assumed in Section 5 (i.e. $B_{p,eq} = 7$ G). With such a magnetic field intensity, the frequency of emission is around 36 MHz, where the LOFAR sensitivity for a 1-h integration time is about a few mJy. The radio power calculated in Section 5 yielded values of about $(1.6\text{--}5.6) \times 10^{25}$ erg s $^{-1}$. For a radio flux of a few mJy, the required radio power of the exoplanets studied here should be higher, on the range of $(1.1\text{--}2.1) \times 10^{27}$ erg s $^{-1}$. To have a radio power (or, equivalently, a wind kinetic power) that is roughly two orders of magnitude larger, the stellar wind characteristics need to change – either by increasing the density of the stellar wind or its velocity or both, as demonstrated next.

From equations (11), (15) and (16), and assuming a ram-pressure-dominated wind, one can show that

$$\rho^2 \Delta u^7 \sim \frac{8P_k^3}{\pi^2 R_p^6 B_p^2}, \quad (18)$$

such that the ratio between the values required for a radio flux of about 3 mJy to the ratio of the values calculated in Section 5 is

$$\frac{[\rho^2 \Delta u^7]_{(3\text{mJy})}}{[\rho^2 \Delta u^7]_{(\text{Section 5})}} \sim \left(\frac{P_{k(3\text{mJy})}}{P_{k(\text{Section 5})}} \right)^3 \sim (0.5\text{--}3.3) \times 10^5. \quad (19)$$

A very crude estimate² then tells us that either the wind density needs to increase by a factor of at least $\sim 300\text{--}600$ (i.e. the square root of the values derived in equation 19) or the velocity requires an increase of a factor of at least $\sim 5\text{--}7$ (i.e. the 7th root of the values

in equation 19). Or, alternatively, density and velocity should both change such that they obey the relation (19).

From Table 3, a five to seven times increase in the wind velocity implies a relative velocity $\gtrsim 1200$ km s $^{-1}$, which is 50 per cent larger than the speed of the fast solar wind and three times larger than the slow solar wind speed. In terms of density, an increase of $\sim 300\text{--}600$ roughly implies a similar increase in mass-loss rates and, from Table 2, this would result in \dot{M} of at least $(2.9\text{--}24) \times 10^4$ times the solar wind mass-loss rates. Such mass-loss rates are typical of very young stars, indicating that exoplanets orbiting young suns are more likely to produce detectable levels of radio fluxes (Grießmeier et al. 2005; Vidotto et al. 2010a).

7 SUMMARY AND CONCLUSIONS

In this work we have investigated the interplanetary media surrounding five hot Jupiters, namely: HD 46375b, HD 73256b, HD 102195b, HD 130322b and HD 179949b. For that, we carried out 3D MHD stellar wind simulations, which incorporate as boundary conditions the surface magnetic field of the star reconstructed by Fares et al. (2012, 2013) using the ZDI technique. The global characteristics of our wind models are presented in Table 2.

We then calculated the *local* characteristics of the stellar winds at the orbital radius of the hot Jupiters, in order to characterize the interplanetary medium surrounding these exoplanets. In particular, we calculated the total pressure of the interplanetary medium and estimated what would be the size of planetary magnetospheres in case these hot Jupiters had a magnetic field similar to Jupiter’s field. We found that magnetospheric sizes range between 4.1 and $5.6R_p$ and that they can vary by a few per cent due to variations in the external environment of the planets, as they orbit around their parent stars. We also demonstrated that these planets orbits are superfast magnetosonic, indicating that bow shocks should be formed around their magnetospheres. The bow shock orientations (i.e. the angle between the shock normal and the tangent of the circular orbit) are of intermediate type, in which the shock forms at intermediate angles from the one of a shock facing the motion of the planet (‘ahead shock’) and the one connecting the star–planet centres (‘dayside shock’).

We also calculated the size of the auroral ovals of these planets. Inside these ovals, the planetary magnetic field lines are open, through which particles from the star and from the cosmos can penetrate as well as planetary atmospheric particles can escape through polar flows. On average, the auroral ovals we calculated have a half-opening angle of about $25^\circ\text{--}29^\circ$, leaving exposed about 9–13 per cent of the planetary area, which is a factor of ~ 2 larger than estimates for the Earth’s and Saturn’s auroral caps. Finally, we estimated the radio flux of these planets, using the analogy observed in the Solar system, in which the radio emission from the magnetized planets is correlated to the solar wind power. We found small radio fluxes ranging from 0.02 to 0.13 mJy, which should represent a challenge to be observed with present-day technology (e.g. LOFAR; Grießmeier et al. 2011), but could be detectable with higher sensitivity arrays, such as the SKA-low array system. Radio emission from systems having closer hot Jupiters, such as from τ Boo b (radio flux of the order of 0.5–0.9 mJy; Vidotto et al. 2012), HD 189733b (0.5–1 mJy, calculated using the simulations from Llama et al. 2013 and the same model as presented here) or from nearby planetary systems orbiting young stars (Grießmeier et al. 2005; Vidotto et al. 2010a), is likely to have higher radio fluxes, presenting thus better prospects for detection of exoplanetary radio emission.

² Note that this approach is not a self-consistent one, because in this scenario the structures of the wind temperature, velocity and magnetic fields are not modified (i.e. we are assuming they remain unchanged as the structures derived in Section 4). In the self-consistent approach, if either the density of the wind or its velocity is modified, one needs to solve the coupled MHD equations to derive all the remaining quantities of the wind. However, this back-of-the-envelope calculation can give a rough estimate of how larger should the stellar wind power be in order for the radio emission to reach values above the sensitivity limit of a couple of mJy.

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