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Giant Drag Reduction in Complex Fluid Drops on Rough Hydrophobic Surfaces

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We describe a new spreading regime during the drop impact of model yield-stress fluids (Carbopol microgel solutions) on rough hydrophobic surfaces, in a range of parameters where classical Newtonian drops usually splash. For large surface roughness and high impact velocity, we observe that the maximal inertial spreading diameter of the drops can be as much as twice larger than on smooth surfaces in the same conditions, corresponding to apparent basal friction reductions of more than 80%. We interpret this large drag reduction using a simple energy balance model and a dynamic slip length that depends on both the surface roughness and the drop's dynamics.

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In fluid dynamics, microscopic details at the solid-liquid interface can have a dramatic influence on the macroscopic flow behavior. Wetting and roughness properties of solid surfaces play a key role in many phenomena involving the static and dynamics of the contact line [1,2], from coating flows to fast inertial flows like drop impact [3,4], penetration of solid bodies into liquids [5], or flow separation from solid surfaces [6]. Surface properties can also affect the classical no-slip hydrodynamic boundary condition at a solid surface [7]. Of particular interest is the possibility to achieve a large effective slip length using textured superhydrophobic surfaces, owing to the strong reduction of the solid-liquid contact area when the liquid is in a 'fakir' or Cassie state [8]. This strategy has proven successful to produce significant skin-friction drag reduction in microfluidic flows or in macroscale turbulent channel flows [9], when the size of the flow gradients becomes comparable to the slip length. However, the extension of this drag-reduction mechanism to other macroscale hydrodynamic configurations-a central issue in many applications—remains largely unexplored.

In this Letter, we address this question in the context of drop impact. When a drop hits a solid surface, a very thin lamella is generated that rapidly spreads radially, providing a unique means to probe the friction drag between a freesurface boundary layer and a solid surface. With Newtonian drops, this goal is however hampered by the instability and splashing of the lamella as the velocity increases, especially on textured nonwetting surfaces [3]. Here we show that the use of highly elastic complex fluids (Carbopol microgel solutions) enable us to overcome this splashing limit, giving rise to a new spreading regime. At high impact velocities, Carbopol drops impacting a rough hydrophobic surface (RH) can spread twice farther than when they hit a smooth surface in the same conditions (see Fig. 1 and the movie in the Supplemental Material [10]). This observation strongly contrasts with the case of impacting drops of Newtonian fluids or dilute polymer solutions, for which the maximal (inertial) spreading

diameter L_m is found to be almost independent of the surface wetting properties [3,11,12] or surface microstructure [13]. Such an increase of spreading, called 'superspreading' in the following, can be interpreted as an apparent reduction of the basal friction between the spreading lamella and the rough hydrophobic surface. Assuming that the initial kinetic energy of the drop $\sim \rho L_0^3 V_0^2$ (ρ is the mass density of the drop, L_0 the drop diameter, and V_0 the impact velocity) is balanced by the work of the basal shear stress $\sim \sigma_b L_m^2 L_m (L_m \gg L_0)$ gives $\sigma_b \propto L_m^{-3}$, where σ_b is the typical magnitude of the basal shear stress. In our case, a twofold increase of the maximal spreading diameter thus corresponds to an apparent drag reduction ($\sigma_b^{\mathrm{smooth}}$ - $\sigma_{h}^{\text{RH}}/\sigma_{h}^{\text{smooth}} \sim 85\%$, a value that greatly exceeds drag reductions reported previously in steady flow configurations using microfabricated superhydrophobic surfaces [9,14].

To study this phenomenon in detail, we measure the maximal spreading diameter as a function of the impact velocity for a wide range of Carbopol concentrations and drop sizes [15], both on a smooth surface (glass) and on a



FIG. 1 (color online). Spreading of a microgel drop (Carbopol ETD 2050 1 wt%, drop size $L_0 = 22$ mm) impacting at high velocity ($V_0 = 6.15$ m/s) a glass surface (left) or a rough hydrophobic surface (Teflon-coated sandpaper surface *P*120 grit size) (right). On the coated sandpaper, the maximal spreading diameter L_m is about twice that on glass (see also the movie in the Supplemental Material [10]).

rough hydrophobic surface made with hydrophobic sand particles [see Fig. 2(a)]. At low velocities and/or high concentrations, the normalized maximal drop deformation $(L_m - L_0)/L_0$ is the same on both kinds of surfaces, as observed with Newtonian fluids [11]. However, at large velocities and/or low concentrations, the drop deformation is systematically larger on the rough hydrophobic surface. Note that in most experiments, the maximal drop extension is well below the capillary limit controlled by the Weber number We = $\rho L_0 V_0^2 / \gamma$, where γ is the surface tension of the drop [11]. This means that bulk rheological properties and not surface tension are responsible for the arrest of the spreading in our study. In a previous work [16], we have shown that for a soft yield-stress fluid like Carbopol, elasticity controls the impact dynamics even above the yield stress, because the impact time is much shorter than the fluid relaxation time (large Deborah numbers). In Fig. 2(c), we plot the maximal drop deformation for all data as a function of the elastic Mach number M = $V_0/\sqrt{G/\rho}$, where G is the typical elastic shear modulus



FIG. 2 (color online). (a) Normalized maximal drop deformation $(L_m - L_0)/L_0$ as a function of the impact velocity on a glass surface (left) and a rough hydrophobic surface made of 222 μ m mean diameter hydrophobic sand (right) for different drop sizes and Carbopol concentrations (0.2-3 wt%). (b) Same data as a function of the Weber number We = $\rho L_0 V_0^2 / \gamma$ (taking ρ = 1015 kg m⁻³ and $\gamma = 0.07$ J m⁻², see Ref. [16]). The solid line gives the law $L_m/L_0 = 0.9 \,\mathrm{We}^{1/4}$ found for low viscosity Newtonian drops impacting solid surfaces in the capillary regime [11]. (c) Rescaling of the data using the elastic Mach number $M = V_0 / \sqrt{G/\rho}$, where G is the low-frequency elastic shear modulus of the fluids. The black squares give the maximum sheet extension for a Carbopol drop (0.5 wt%, $L_0 = 9$ mm) impacting a small disc (15 mm in diameter) at different velocities (pictures). The solid and dotted lines give the model prediction [Eq. (1)] for b = 0 and $b = \infty$, respectively.

of the material (see Fig. 1 in the Supplemental Material [17] for typical rheological curves and a definition of *G*). A collapse of the data for each impacted surface is observed, confirming the dominant role of elasticity in our study. At low Mach numbers, both master curves coincide. However, above $M \sim 10$ a transition is observed and the maximal diameter increases much more rapidly on the rough hydrophobic surface than on the glass surface.

When seeing pictures of the drop's dynamics in the superspreading regime [see Fig. 1], one may wonder to what extent the fluid lamella actually touches the solid surface or simply floats over an air layer. Such a thin air cushion is present during the early time dynamics of low viscous drops hitting smooth [18] or micrometer textured surfaces [13], and is believed to play an important role in the splashing transition [19]. Although our very rough surfaces prevent a precise visualization of the contact area, it is possible to test the role of the surface on the spreading by performing impact experiments on small targets [see the inset of Fig. 2(c)]. In this case, the basal friction is negligible during most of the spreading dynamics and the drop's extension is solely controlled by extensional elasticity and/or capillary effects [20,21]. Figure 2(c) shows that the maximal drop extension on the solid surfaces is always smaller than on the small targets, even in the superspreading cases. Air friction alone cannot explain this difference, as shown by estimation of the bottom viscous drag created by an air layer of thickness $\sim R_a$ [rms surface roughness] trapped between surface asperities [22]. It is also unlikely that the superspreading comes from a squeezed air effect between the drop and the solid surface that would push the lamella outward, since the spreading is maximal on the small targets for which squeezed air effects are minimized.

Systematic experiments using coated sandpaper surfaces over a wide range of grit sizes [23] reveal that surface roughness is actually the key parameter in our study. By increasing the surface roughness ξ [defined as the mean peak spacing] while keeping all other parameters fixed, it is possible to continuously tune the maximal drop extension between the low value obtained on the glass surface to the superspreading case observed previously on a very rough surface [see Fig. 3(a)]. Importantly, shifting the surface from hydrophobic ($\theta > 90^\circ$) to hydrophilic ($\theta < 90^\circ$) does not suppress the superspreading effect, although hydrophobicity tends to enhance the maximal drop extension for a given roughness [see Fig. 3(a)]. This crucial role of surface roughness points to the question of the relevant length scale needed to rescale ξ . To investigate this, we performed experiments with different drop sizes, impact velocities, and elasticities, while keeping the Mach number fixed. Figure 3(b) shows large dispersion between the three sets of experiments when the surface roughness is simply normalized by the drop size, which means that ξ/L_0 (and any of its combinations with the Mach number) is not the



FIG. 3. (a) Maximal drop deformation as a function of the surface roughness ξ (defined as the mean peak spacing measured by optical profilometry) for a given set of impact parameters (Carbopol 0.5 wt%, $V_0 = 4.35 \text{ m/s}$, $L_0 = 8.5 \text{ mm}$) (filled circles: Teflon-coated sand paper, apparent advancing contact angle $\theta = 130^{\circ} \pm 3^{\circ}$; open circles: uncoated sandpaper, $\theta =$ $50^{\circ} \pm 5^{\circ}$). Picture: scanning electron microscopy of a P1200 grit size sandpaper ($\xi = 17 \ \mu$ m). (b) Maximal drop deformation as a function of ξ/L_0 for three sets of parameters at a given Mach number M = 19.3 (filled circles: $L_0 = 8.5$ mm, $V_0 = 4.35$ m/s, G = 52 Pa; filled squares: $L_0 = 13$ mm, $V_0 =$ 4.25 m/s, G = 50 Pa; filled triangles: $L_0 = 21.7$ mm, $V_0 =$ 6 m/s, G = 98 Pa). (c) Same data when the roughness is normalized by the capillary length scale: (ξ/L_0) We. The solid line gives the prediction of the model [Eq. (1)] using a dynamic slip length $b = AWe\xi$ with A = 0.0045.

relevant dimensionless parameter that captures the effect of roughness. There exist however two other length scales in the problem. The first one is the capillary length scale $\gamma/\rho V_0^2$. The second is a viscous length scale defined as L_0/Re [24], where Re is an effective Reynolds number of the Carbopol drops computed from the steady-state rheology of the fluid [16]. Figure 3(c) shows a good collapse of the data when ξ is normalized by the capillary length scale, that is, using a Weber number based on the roughness size: $\rho \xi V_0^2 / \gamma = (\xi / L_0)$ We. By contrast, no collapse is obtained when using the viscous length scale (see Fig. 2 in the Supplemental Material [25]). This result suggests that the interaction between the drop's lamella and the surface roughness is dynamic and involves the balance at the asperity scale between the lamella inertia and the capillary pressure.

In the following, we interpret this roughness-induced basal drag reduction in terms of dynamic slip length. Our picture is that at large impact velocity, the inertia of the spreading lamella overcomes capillary adhesion at small scales, thus preventing the fluid lamella to follow the surface corrugation and impregnate the surface [26]. In this dynamic 'fakir' state, the lamella only touches the

highest asperities and the solid-liquid contact area is strongly reduced, yielding large slip lengths. To quantify this idea, we assume that when the drop reaches its maximal extension, the fluid lamella is both sheared across its thickness h and stretched along its length L_m . The shearing comes from the partial adhesion of the lamella with the bottom solid surface during the spreading, while the top surface is stress free. The typical shear deformation is then written as $\epsilon_{\text{shear}} \sim (1/2)(L_m - L_0)/(h + b)$, while the typical stretching deformation is $\epsilon_{\text{stretch}} \sim (L_m - L_0)/L_0$. Here b is an effective 'elastic' slip length, defined by analogy with the classical Navier hydrodynamic slip length by $b = u_{\rm slip}/\epsilon_{\rm shear}$, where $u_{\rm slip}$ is the finite slip displacement occurring at the solid boundary condition. Assuming that the initial kinetic energy of the drop $(1/2)(\pi L_0^3/6)\rho V_0^2$ is fully converted in elastic energy, written as $(1/2) \times$ $(\pi L_0^3/6)(G\epsilon_{\text{shear}}^2 + 3G(4\epsilon_{\text{stretch}}^2))$ for an incompressible medium [27], and using volume conservation [h = $(2/3)L_0^3/L_m^2$, we obtain the following implicit relation for the normalized maximal drop deformation $x = (L_m - L_m)$ $L_0)/L_0$ as a function of the elastic Mach number M and normalized slip length b/L_0 :

$$M^{2} = \frac{9}{16} \frac{x^{2}(x+1)^{4}}{[1+(3/2)(b/L_{0})(x+1)^{2}]^{2}} + 12x^{2}.$$
 (1)

For b = 0 (no slip) and large Mach numbers $(L_m \gg L_0)$, shear dominates over stretch yielding $(L_m - L_0)/L_0 \sim M^{1/3}$, in good agreement with experiments on the glass smooth surface [see Fig. 2(c)]. Conversely, for $b \to \infty$ (perfect slip), the drop is only stretched and $(L_m - L_0)/L_0 \sim M$, as observed on small targets [see Fig. 2(c)].

To predict the drop deformation in the general case requires an expression for the 'elastic' slip length b. In our experiments, the normalized deformation is controlled by the Mach number M and the dimensionless length (ξ/L_0) We [see Fig. 3(c)]. In the framework of the model, this means that the normalized slip length b/L_0 depends on (ξ/L_0) We. Figure 3(c) shows that taking the simplest dependence $b/L_0 \propto (We/L_0)\xi$ enables us to correctly fit our data for a given M, yielding an effective slip length as large as millimeters for the largest Weber numbers and surface roughness. The complete comparison between the model's prediction and measurements for a wide range of Mach numbers, Weber numbers, drop sizes, and surface roughnesses is presented in Fig. 4, with no further fitting parameter. The agreement is reasonable [coefficient of determination R = 0.95 and gives, both in the model and experiments, a transition at $M \sim 10$ for the dependence of the deformation with the Mach number [see Fig. 2(c)and the inset of Fig. 4].

Our simple model using a dynamic elastic slip length therefore captures our main observation, namely the superspreading and strong apparent basal reduction observed during the impact of a Carbopol drop on rough hydrophobic surfaces. However, the phenomenological



FIG. 4 (color online). Comparison between the model and experiments for a wide range of impact parameters and surface roughnesses (0.5 < M < 32; 20 < We < 11250; $8 \times 10^{-4} < \xi/L_0 < 2 \times 10^{-2}$), with $b = AWe\xi$ and A = 0.0045. The inset gives the maximal drop deformation predicted by the model as a function of the elastic Mach number for a typical Carbopol drop (G = 50 Pa, $\gamma = 0.07$ N m) and different surface roughnesses ($\xi = 15, 30, 45, 75, 120, 200 \ \mu$ m) between $\xi = 0$ (red line) and $\xi = \infty$ (black dotted line).

dependence of the slip length with the surface roughness and Weber number remains to be understood. For classical liquids flowing at low Reynolds numbers over composite slip and no-slip surfaces, the effective hydrodynamic slip length is given by $b_{\text{hydro}} \sim f(\phi_s)\xi$, where ξ is the typical pitch of the surface and $f(\phi_s)$ is a function that increases when the fraction of solid-liquid contact area ϕ_s decreases [28]. In our case of the drop impact of complex fluids, we also find a slip length proportional to the surface pitch ξ , but with a dependence with the Weber number suggesting a reduction of the solid-liquid contact area as the Weber number increases. Such behavior is reminiscent of the loss of adhesion observed in fast film flows over curved solid surfaces, due to the competition between inertia and capillary pressure [6]. In our case, the flow is furthermore highly unsteady and finding the precise relationship between the slip length, the Weber number, and the surface roughness would require more investigation and the use of more controlled surfaces. It is also important to note that our experiments have been conducted in ambient pressure. As shown in previous studies [13,29], air pressure can have a strong influence on the dynamic wetting property of an impacting drop on textured surfaces. We have shown that air itself cannot explain our observation of a decrease of the basal drag when the surface roughness increases. However, air pressure could play an indirect role in our phenomena by affecting the solid-liquid contact area ϕ_s , in addition to the Weber number. During the spreading, resistance to air flow at the edge of the liquid lamella could detach the lamella from the solid surface [30], and help to maintain the liquid sheet in a dynamic fakir state.

To conclude, we note that the dynamic mechanism of drag reduction reported here is *a priori* not peculiar to complex fluids and could apply to Newtonian drops hitting rough surfaces in the viscous regime. However, our results show that the superspreading occurs in a regime of high Reynolds and Weber numbers for which Newtonian drops are usually unstable and splash [3,29,31] (see Fig. 3 in the Supplemental Material [32]). For Carbopol, this splashing threshold is likely postponed due to the strong elasticity of the fluid [20,33], allowing us to explore extreme flow conditions difficult to achieve with classical fluids.

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