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Article

Experimental and Numerical Simulation of the Dynamic Frictional Contact between an Aircraft Tire Rubber and a Rough Surface

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Abstract: This paper presents a numerical simulation of an aircraft tire in contact with a rough surface using a variable friction coefficient dependent on temperature and contact pressure. A sliding facility was used in order to evaluate this dependence of the friction coefficient. The temperature diffusion throughout the tire cross-section was measured by means of thermocouples. Both frictional heating and temperature diffusion were compared to numerical two- and three- dimensional simulations. An adequate temperature prediction could be obtained. In future simulations, wear should be taken into account in order to have a more accurate simulation especially in the case of high pressures and slipping velocities. A 3D finite element model for a rolling tire at a velocity of 37.79 knots (19.44 m/s) and in a cornering phase was investigated using a variable friction coefficient dependent on temperature and pressure. The numerical simulation tended to predict the temperature of the tire tread after a few seconds of rolling in skidding position, the temperature of the contact zone increases to 140 °C. Further investigations must be carried out in order to obtain the evolution of the temperature observed experimentally. The authors would like to point out that for confidentiality reasons, certain numerical data could not be revealed.

Keywords: tire; modeling; finite element; friction coefficient; contact pressure; temperature

1. Introduction

Aircraft tires are subject to very high performance requirements when providing directional control and braking during the maneuvering of the airplane on the ground. The tires must not only support the aircraft's weight, and transmit acceleration and braking forces to the runway surface, but also supply the forces necessary for the directional control of the aircraft [1]. It is well known that the directional capacity of an aircraft is measured by the friction coefficient [2]; this is the measurement of the contact area forces as a fraction of the aircraft's weight. In the field of aeronautics, NASA carried out the first experimental and related studies [3–5] on the thermal aspect (influence of temperature and its distribution) of the evolution of the friction coefficient between the tire and the ground. Subsequently, many other studies also investigated the interaction of various phenomena in the contact area, with the friction coefficient [6–8]. As friction is the major factor for generating forces on the aircraft through the tire, it is extremely important to have an accurate characterization of the magnitude and direction of the frictional force generated at the ground/tire interface. Generally, the normalized tire friction coefficient $\mu = F_y / F_z$ is used in most tire friction models, where F_y is the tangential friction force at the tire/runway interface and F_z is the vertical loading on the tire (Figure 1). Thus, μ is the sliding friction coefficient,

1). Thus, μ is the sliding friction coefficient, this being a nonlinear function depending principally on the velocity of the tire. Grosch [9] studied different vulcanized rubber tires and described the dependence of the friction coefficient on sliding velocity, temperature and surface roughness. He explained that friction is due to energy dissipation when rubber is compressed and released by asperities. The friction coefficient also depends on several airplane factors (loading, velocity, slip ratio, slip angle) [10–12], tire factors (tire type, inflation pressure, tread design, rubber composition) [13], runway surface conditions (roughness, dryness and wetness) [14] and also environmental factors (weather conditions and contamination) [15,16].

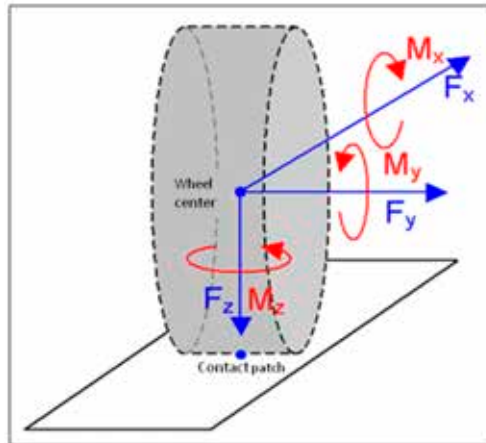


Figure 1. Forces and moments definitions on a tire.

Pearson studied tire rubber friction in the context of road vehicle tires and also the role of surfaces in contact [17–19]. He developed a theory on the influence of temperature on the rubber friction coefficient called flash temperature [19]. He showed that rubber friction depends on the sliding history (effects), which is difficult for an accurate description of friction. Friction for sliding on rough surfaces, the rate of change of friction is due mainly to heating and heating of the rubber/surface contact region. Most real surfaces have asperities of many different orders of magnitude. When calculating the friction forces, it is necessary to include the deformation and formation of stable ripples. The energy dissipation results in localized heating of the rubber. Since the viscoelastic properties of rubber are extremely temperature dependent, it is necessary to include the localized temperature increase in the analysis. At very low sliding velocities, the temperature increase is negligible due to heat diffusion. However, for velocities of the order of 0.1 m/s or higher, the localized heating plays a role. Pearson showed that at a typical ramp the temperature increase results in a decrease of rubber friction with increasing sliding velocity (if the sliding velocity is above 0.5 m/s).

In precedent papers [20–22], FEM models are proposed to simulate the aircraft tire behavior in contact with the runway and coupled to the mechanical analysis procedures described. The frictional work is converted to heat. The contact/friction state is governed by a variable friction coefficient depending on the sliding velocity, contact pressure and temperature. The present paper presents the numerical simulation of an aircraft tire in contact with a rough surface, using a variable friction coefficient dependent on temperature and contact pressure. Firstly, a sliding facility with rubber block samples under sliding conditions is used, under different fixed vertical pressures, with a constant sliding velocity. The friction coefficient was determined and the thermal evolution of the rubber samples discussed. Secondly, experimental tests were carried out in order to simulate the frictional heating phenomenon developed in the tire tread, using an external heat source. In these studies, experimental parameters corresponding to the real parameters of an aircraft tire in rolling conditions (vertical loading, velocity, inflation pressure and sliding angle) have been used. Two- and three-dimensional numerical simulations were carried out for sliding and thermal diffusion. Finally, a three-dimensional finite element model for a rolling tire at a velocity of 37.79 km/h (10.44 m/s) in a cornering mode was investigated using a variable friction coefficient dependent on

a cornering mode was investigated using a variable friction coefficient dependent on temperature and pressure. The thermal evolution of the tire rubber during this rolling phase was compared to experimental data.

Rubber Block Frictional Heat

Tread rubber characteristics play a crucial role in tire force generation; they describe tread stiffness, friction properties and heat generation. Energy loss and modulus vary, not only from one compound to another, but also depending on stress frequency and on temperature. Tread rigidity is directly related to the rubber shear modulus G'' , as rubber becomes softer when its bulk temperature increases; tread rigidity will depend on the tire temperature increase. Higher cornering stiffness is obtained at a lower tire tread temperature [23]. Fevrier et al. demonstrate the mechanisms involved in the relative slippage between the tire tread and runway. The first mechanism is the frequency excitation of the material by the runway surface texture. The rubber is distorted when it comes into contact with rough spots on the runway, thus leading to energy loss (hysteresis). The second mechanism is molecular adhesion. As regards the energy balance, both hysteresis and adhesion result from the transformation of mechanical energy in the contact zone. Thus, friction is not only a mechanical process but is also related to the thermal evolution of the rubber, which means that a thermo-mechanical contact model is essential for a reliable description of the frictional behavior.

Kainradl et al. [24] also studied the thermal evolution of the tire tread in a rolling phase. They demonstrate that the tire tread temperature rise is due to frictional heating, which does not significantly affect the temperature profiles within the tire carcass structure. However, these tread temperature peaks probably have a significant influence on tread wear rates. It is well known that the maximum friction level developed by a worn tire is shown to be more sensitive to variations in tread temperature and velocity. It was observed that a tire in cornering or braking conditions at a high angle produced molten rubber deposits on the runway surface and tread temperatures high enough to cause the rubber to undergo changes in its chemical composition [3]. For all these reasons, a profound study of tread rubber in skidding positions is primordial, in order to establish a dynamic friction coefficient dependence on contact pressure, sliding velocity and temperature. In the literature, few experiments have been realized to determine the temperature rise in the contact area between an aircraft tire rubber and a rigid, rough runway [4,5].

2. Experimental and Numerical Studies: Materials and Methods

2.1. Experimental Study: Frictional Heating

The aim of this study is to identify tire tread behavior in a sliding situation. It was therefore important to design an experiment that could provide necessary data for comparison with numerical simulation. The experimental investigations were performed on the High Speed Linear Friction Tester (HiLiTe), (Figure 2a) at the Institute of Dynamics and Vibration Research (IDS) at Leibniz Universität Hannover, Germany. With this test rig, sliding friction and sticktion measurements can be performed over a wide velocity range (0.1–10 m/s) and with vertical forces up to 1 kN. The ambient temperature can be controlled between $-20\text{ }^{\circ}\text{C}$ and $+55\text{ }^{\circ}\text{C}$. Typically, the sliding friction of tire tread samples is tested on several surfaces, such as asphalt or concrete test tracks, and also on snow and ice. Experiments at positive ambient temperatures can be carried out in dry, damp or wet conditions. Whilst friction and vertical force are measured with standard equipment, additional test equipment must be used to measure the sample temperature and contact temperature. The experiments for this study were performed on a concrete test track, the rubber tread samples measured $20 \times 20\text{ mm}$ on the contact area and 10 mm in thickness. The sample was bonded onto the sample mounting plate and fitted with a thermocouple 6 mm from the contact area, which was implanted into a borehole and thermally connected by heat conductive paste, Figure 2b. The velocity profile is trapezoidal; it is formed in a short acceleration phase, then a phase of constant velocity $v = 4\text{ m/s}$ followed by a short

deceleration phase. The overall track length is 2 m (Figure 2c). The experiments were realized at 20 °C. As well as the measurement of friction force, normal force, and the sample core temperature, the temperature in the contact area was measured with an infrared camera, at the end of the track, see Figure 2b. Simultaneously, a high speed camera was used to record lateral images of the deformed block while sliding.

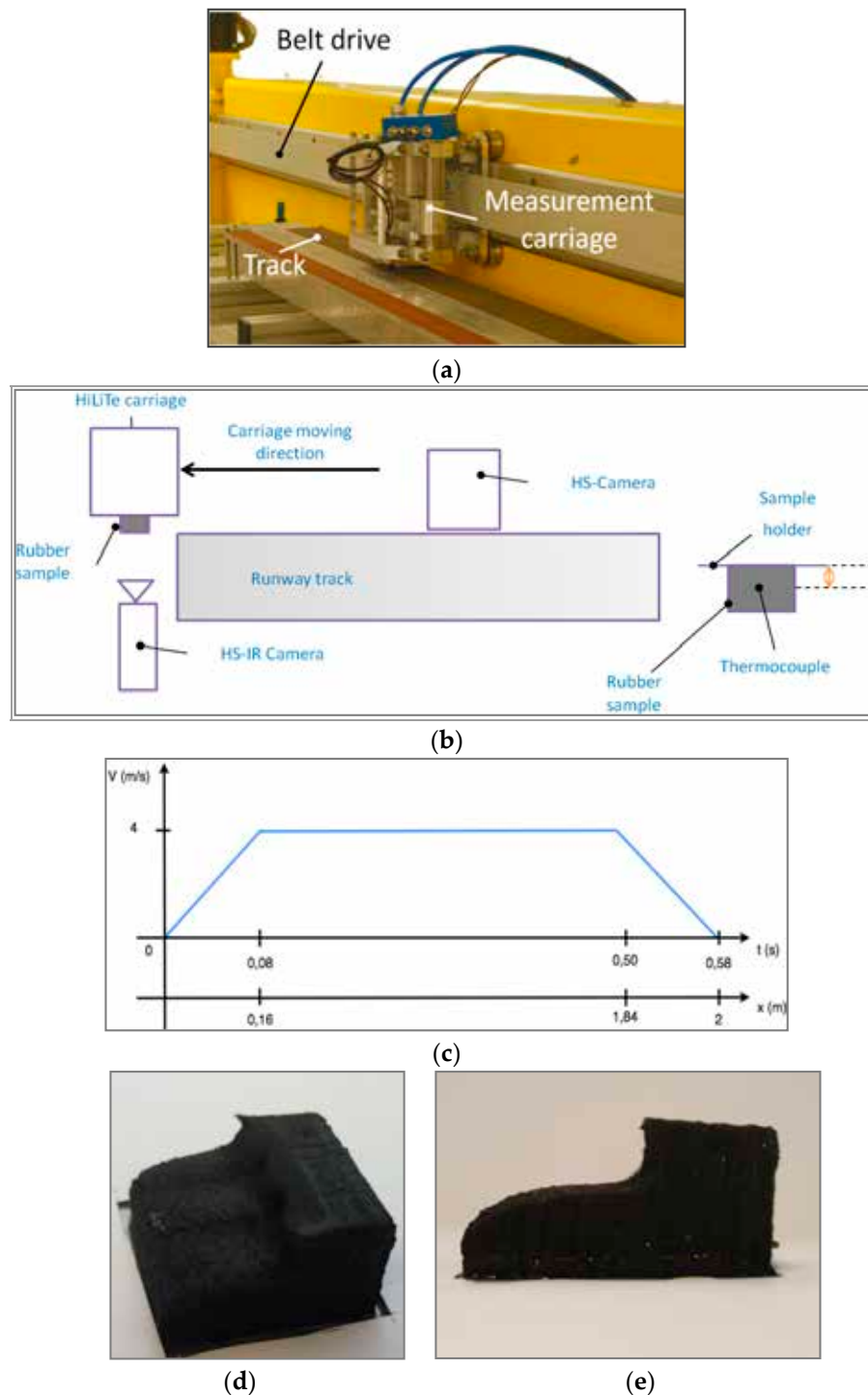


Figure 2. (a) High Speed Linear Tester (HiLiTe); (b) test set-up for contact temperature and deformation measurements; (c) test phases; (d,e) final sample shape after sliding phase on concrete test track.

Figure 2d,e present, respectively, the final shape and the profile of the rubber sample after sliding. The rubber sample was subject to considerable wear; such a high level degradation could not be achieved without taking into account a strong link between the heating history and wear, which is a highly non-linear phenomenon. Another parameter to take into account is the split coefficient of the heat generated by friction between the rubber, the sample and the track surface.

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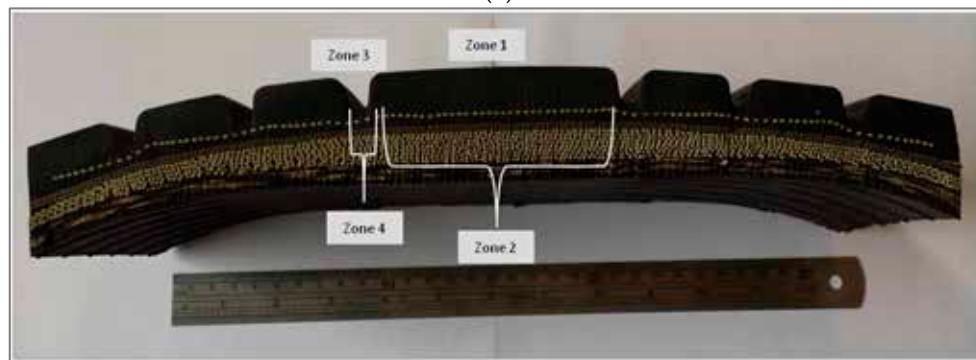
5 of 14

2.2. Experimental Study: Simulated Frictional Heating of the Tire Tread by an External Heat Source

The main objective of this test is to determine the temperature evolution of the tire tread by means of a simple temperature increase experiment. The frictional heating of the tire tread is replaced by a heated heat source, after which the thermal diffusion through the tire cross-section is studied. The experimental test consists of increasing the temperature of the tire using a heat source (Figure 3a) and a pre-determined temperature. The temperature evolution is simulated by a series of sensors (see Figure 3b) and a data acquisition system (see Figure 3c) facing the tire tread (zone 1) and the groove (zone 2). (Zone 1) and (zone 2) are the internal part of the tire tread (zone 1) and the groove (zone 2). The thermal evolution is recorded (zone 1) and (zone 2) by means of a data acquisition system (see Figure 3c) and a data acquisition system (see Figure 3c). The heat flow is vertical to the tire tread surface.



(a)



(b)

Figure 3: (a) Heating setting; (b) tire tread and sensors positions; zone (1) presents the tire tread zone where the heating was applied; zone (2) presents the internal part of tire tread where an infrared sensor was installed; zone (3) presents the groove area where an external sensor is used to measure the temperature; zone (4) presents the internal part of the groove where an infrared sensor was used to measure the thermal evolution.

Figure 4 presents the temperature evolution of various tire tread zones. As can be observed, for the thermal evolutions corresponding to the heated zone (zone (1), triangles), the time shifted increases compared to the temperature inside the tire tread (zone (2)), and smaller values were noted compared to the temperature inside the tire tread (zone (2)), and smaller values were noted (blue solid). Concerning the grooves, the evolution profile appears very similar to that of the tread (red solid). However, we can notice that, after the end of the heating, marked by the vertical line (Figure 4), the groove temperature continues to rise for a short time before reaching a plateau. This proves that the temperature is “stored” and “diffused” throughout the tire rubber and, at the same time, that the rubber has a very low conductivity coefficient.

However, we
groove temp
temperature
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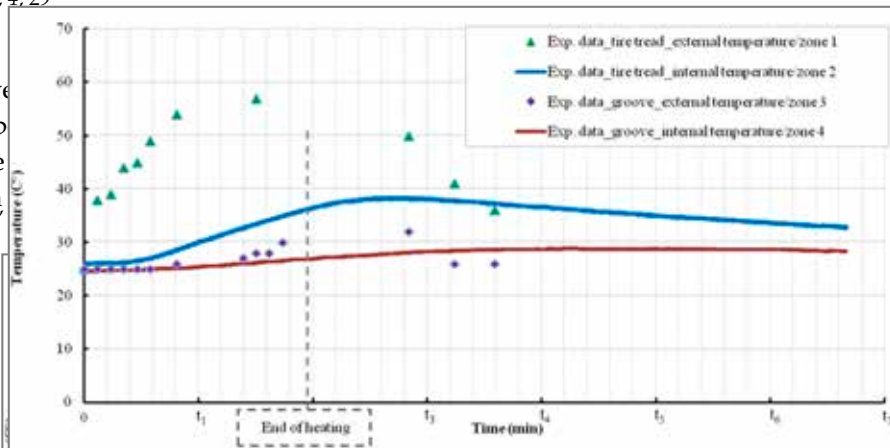


Figure 4. Thermal evolution of tire tread zones for 60 °C of external heating.

2.3. Numerical Simulation/Heating of the Tire Tread

Figure 5 illustrates a comparison between the experimental measurements and the simulated temperature evolution of the tire tread rubber (zone (2), Figure 3b) for an equivalent external heat source. The numerical simulation was carried out using a numerical specimen identical to the physical specimen.

A good correlation is obtained between the simulated temperature of the tire tread and that actually measured. Figure 6 presents the internal thermal evolution of the rubber block observed during sliding (IDS test, Figure 2b). As can be observed, the core temperature increases during the first instants of sliding; a plateau is rapidly attained. It can be concluded that the temperature increase of rubber produced by sliding on a rough surface, or by heat diffusion, leads to a similar evolution in the tire tread rubber (Figures 5 and 6). Whatever the mechanism of heating, by friction or by heat diffusion, the thermal evolution of the rubber remains identical.

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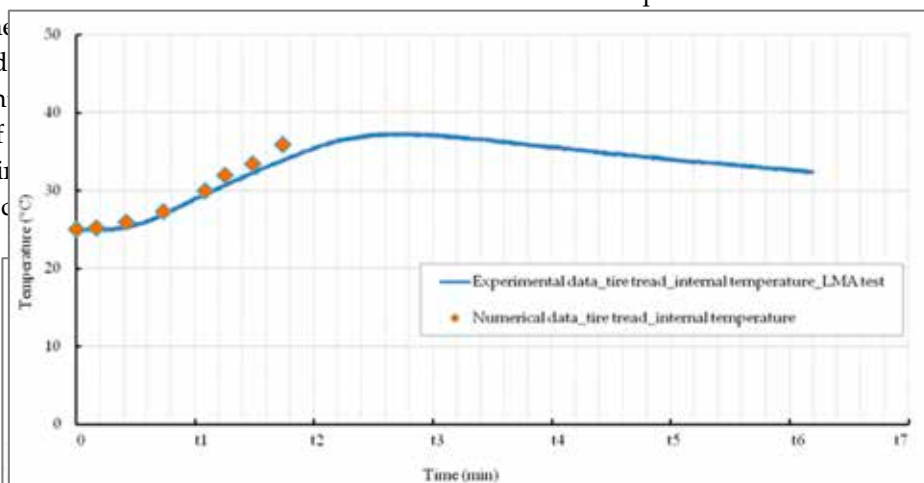


Figure 5. Comparison between experimental and numerical simulation heating of tire tread by external heat source (LMA data).

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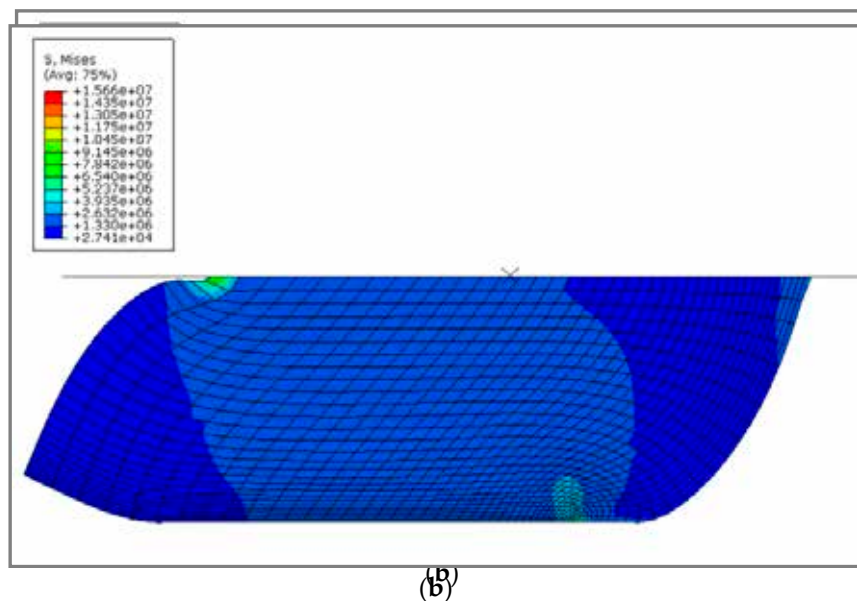


Figure 7: (a) The 2D numerical specimen; (b) specimen shape after sliding. Von Mises's stress distribution.

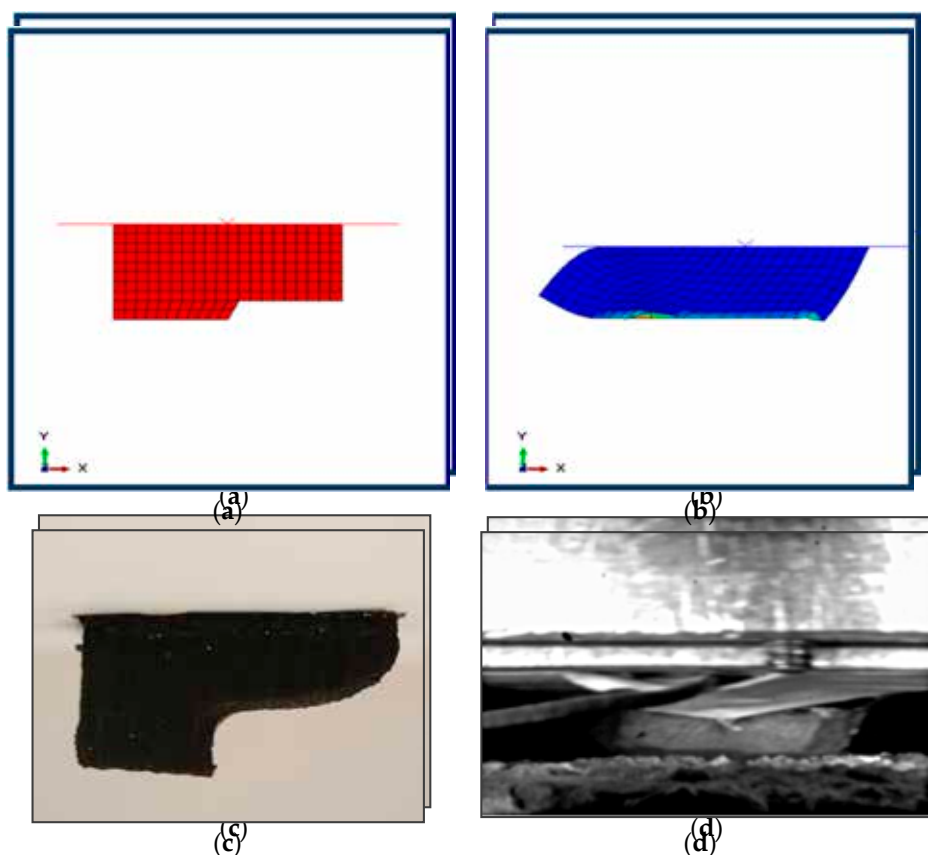


Figure 8: (a) Numerical specimen, rubber sample shape with initial eroded zone; (b) typical lateral view of deformed, worn sample form; (c) rubber sample final shape; (d) rubber test sample during sliding at the liner friction tester.

Figure 8a presents a full 2D image of the eroded initial shape of the rubber sample corresponding to the experimental specimen (Figure 8c). Figure 8b shows the numerical results with respect to the same rubber sample, while taking into account the final eroded shape of the specimen by means of an eroded initial shape. In this case, the rubber block is loaded with 2.5 MPa and sliding at 4 m/s. This deformed shape is in good correlation with the rubber block tested using the Hannover facility (Figure 8d).

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Figure 9 presents a full 3D numerical simulation for a rubber block loaded with 2.5 MPa and sliding on a deformable concrete track at a fixed velocity of 4 m/s. Coupled temperature-displacement elements (C3D8RHT, eight-node tri-linear displacement and temperature, reduced integration with hourglass control, hybrid with constant pressure) were used in this simulation.

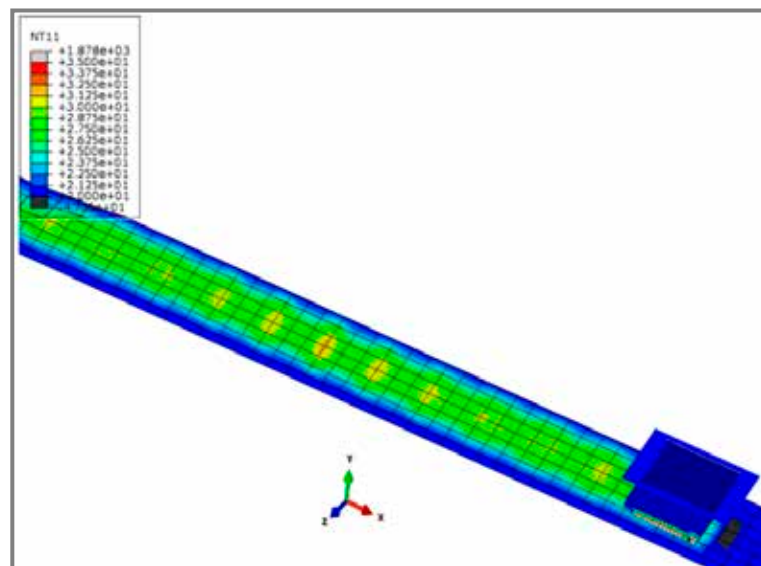


Figure 9: The 3D view of a rubber block on a runway track, thermal evolution of the contact zone; the temperatures are presented in °C (NT11).

As already mentioned, the numerical simulation of a sliding rubber sample demonstrates the same tendencies as the friction rig results. Figure 10a presents the profile of an experimental specimen of a rubber sample observed after the first sliding step. The thermal evolution of the contact zone of the rubber sample was measured using an infrared camera (Figure 2b), and the temperature of each area of the contact zone is shown in Figure 10b. The numerical simulation presented in Figure 10d, shows the temperature variations between 170 °C and 195 °C (orange code) in the upper part of the contact zone which can also be observed on the experimental block (orange patch, Figure 10b). However, a very high temperature was noted at the edge of the numerical rubber block (Figure 10b, red zone); it appears to reveal the first abrasion zone. The sliding sample is subject to several mechanical and thermal mechanisms: the heating of the sliding surface leads to wear. The contact rubber layer of the rubber sample wears out and a new undamaged surface comes into contact. This new surface undergoes a temperature rise until wear appears again and thus the process of repeated (heating/wearing) leads to the final eroded shape shown in Figure 10a. The numerical simulation results shown in Figure 10c do not take into account this erosion mechanism, as the temperature of the leading edge rises to 1800 °C. As previously mentioned, the experimental test shows a very high level of abrasion and this phenomenon needs to be taken into consideration. Within the ABAQUS code [30], a method could be adopted, based on a new modified geometry (new mesh) for each step of sliding. This method will be discussed in a future study.

From these present studies, it can be concluded that pressure and temperature have a considerable influence on the aircraft tire wear phenomenon which needs to be taken into account in future simulations. It must also be mentioned that a specific mesh could be used in the case of a constant wear ratio and a constant number of elements, and the rubber block could be divided into sub-zones, each zone having its own heating history.

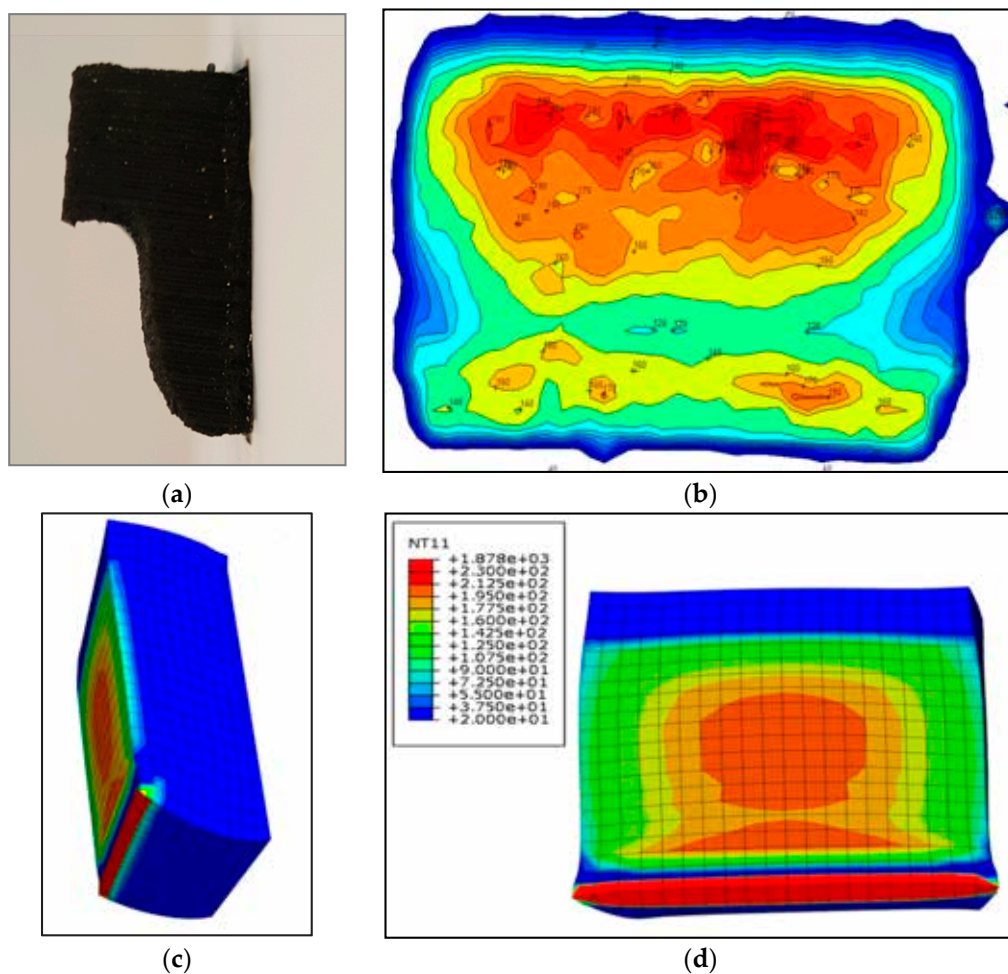


Figure 10. (a) Experimental specimen, a rubber sample shape after the sliding step; (b) experimental measurement, thermal evolution of a rubber sample/contact zone at the end of the sliding step (in °C); (c) numerical specimen, rubber sample shape after first sliding; (d) numerical simulation typical lateral view of the deformed specimen's final shape appearance, thermal evolution in the contact zone, the temperatures are presented in °C (NT11).

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3. Finite Element Model of a Rolling Tire

FEM of a Rolling Tire Using a Variable Friction Coefficient

In a precedent study, a purely mechanical finite element analysis of a rolling tire was investigated [22]. The model was able to predict the cornering behavior of an aircraft tire in contact with a flat rigid body. The Coulomb friction was modeled using a stiffness method [12] that permits some relative motion of the surfaces.

In this section, a thermo-mechanical model was proposed in order to predict the friction coefficient μ , the self-aligning torque M_z and the thermal evolution of a rolling tire. A classical rolling (CR) method based on the Lagrangian formulation was used along with a variable friction coefficient $\mu(P,T)$ dependent on the contact pressure and temperature. The contact aspect is modeled in a soft-contact

manner using exponential pressure-overclosure regularization, where the clearance C_0 and the contact pressure at zero clearance λ_0 are defined, based on a numerical sensitivity study. A Prony model was used for the viscoelastic behavior of the rubber. Concerning the friction coefficient, the IDS facility (High Speed Linear Friction Tester, Figure 2b) was used once more in order to identify the dependence of the friction coefficient on temperature and pressure. The experiments for this study were performed on an asphalt test track, and rubber tread samples measuring 20×20 mm on the contact area and 10 mm in thickness were used. Experimental results are shown in Figure 11 which presents the variation of the friction coefficient as a function of the ambient temperatures of the test track, for different given contact pressures (corresponding to the real pressures applied on the aircraft tire). As can be noted, for a given contact pressure, the temperature increase results in a decrease in the friction coefficient values. Figure 12 illustrates the variation of the friction coefficient as a function of the contact pressure for different given ambient temperatures of the test track. Here, for a given contact temperature, the friction coefficient decreases with the increase of the contact pressure. These variations of the friction coefficient were taken into account and applied in the numerical simulations.

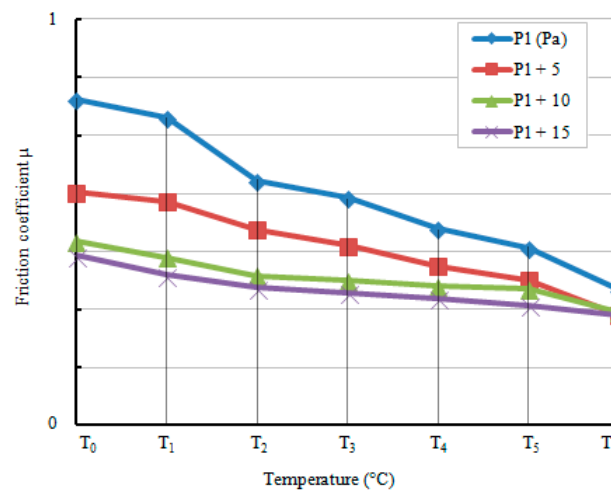


Figure 11. IDS experimental results, variation of friction coefficient as function of the ambient temperature of the test track, for different given contact pressures.

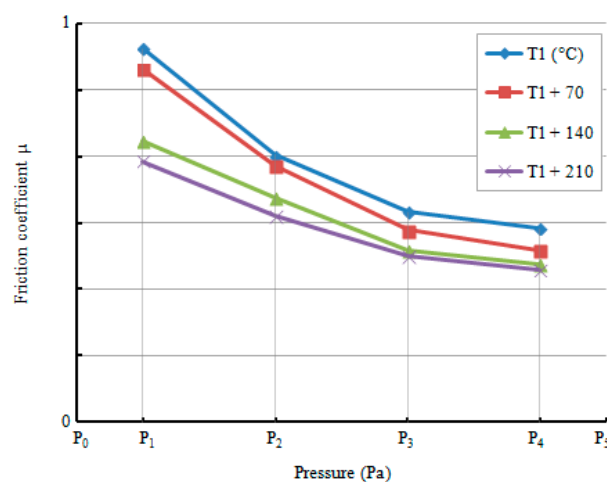


Figure 12. IDS experimental results, variation of friction coefficient as function of contact pressure for different given ambient temperatures.

A cornering tire loaded at vertical force F_z , running at a velocity of 37.79 knots (19.44 m/s) and a fixed skidding angle, is presented. The temperature of the tire tread increases significantly after a few

seconds of cornering, and the rubber reaches an external high temperature which is close to the critical temperature at which the rubber is deposited on the concrete surface [3]. An experimental test was realized on an aircraft tire, and the thermal evolution of the contact zone of the aircraft tire tread was recorded during both rolling and skidding phases using an infrared camera (Figure 13a). Figure 13b shows the experimental data of the thermal evolution of the contact zone in the cornering conditions of an aircraft tire under load, running at a velocity of 37.79 knots and for a given slip angle β_1 for a given time (t_6). The blue solid presents the three stages of the skidding test. In the first stage, the tire is skidded from 0° to β_1° . In the second stage, the tire is kept rolling at β_1° for a given time, and in the last stage, the tire is moved from the skidding position (at β_1°) to the initial position (at 0°). The red line (Figure 13b,d) reveals the heating of the tire tread after a few seconds of skidding, during the first stage of the skidding test.

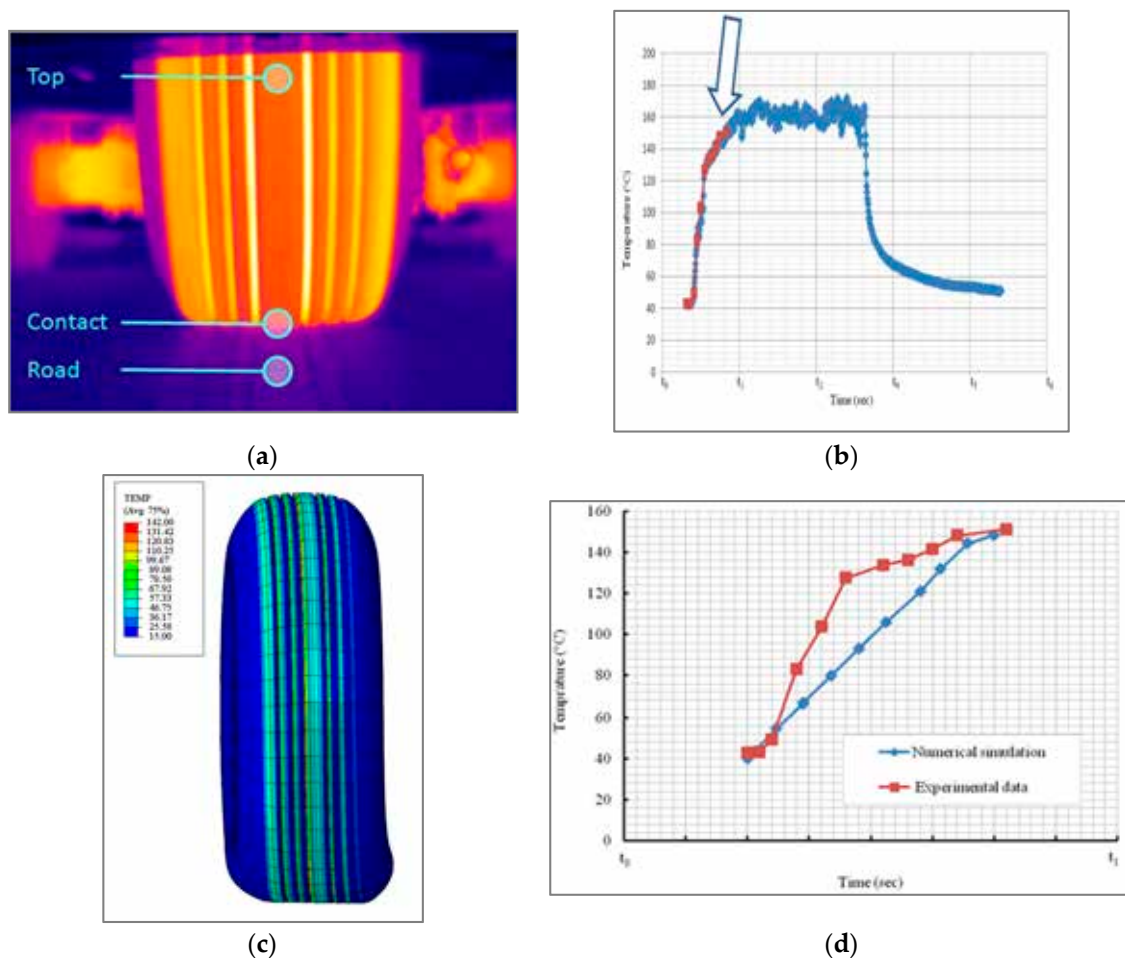


Figure 13. (a) Experimental measurement; (b) experimental data, thermal evolution of the contact zone during the skidding test for a given skidding angle β_1 ; (c) numerical simulation, thermal evolution of the contact zone of the tire during a cornering stage (the temperatures are presented in $^\circ\text{C}$ (TEMP); (d) thermal evolution of the contact zone during the first seconds of skidding (first stage of skidding test), comparison between experimental test and numerical simulation.

Figure 13d presents the thermal evolution in contact zone of tire tread during the first seconds of skidding (between t_0 and t_1 seconds). As can be noted, the numerical simulation tends to predict the maximum temperature of the tire tread after a few seconds of rolling in skidding mode (first stage of the skidding test). Even if the temperature of the contact zone increases to 140°C , the experimental data shows a different tendency for the initial gradient. That difference could be related to the rolling

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