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# Safe Navigation in Urban Environments 

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#### Abstract

Advancements in mobile technology and computing have fostered the collection of a large number of civic datasets that capture the pulse of urban life. Furthermore, the open government and data initiative has led many local authorities to make these datasets publicly available, hoping to drive innovation that will further improve the quality of life for the city dwellers. In this paper, we develop a novel application that utilizes crime data to provide safe urban navigation. Given a model that allows us to estimate the relative probability of a crime on any road segment, we define two variants of the SAFEPATHS problem where the goal is to find a short and low-risk path between a source and a destination locations. Since both the length and the risk of the path are equally important and they cannot be combined into a single objective, we approach the urban-navigation problem as a biobjective shortest path problem. Our algorithms aim to output a small set of paths that provide tradeoffs between distance and safety. While the solution space of such biobjective problems can be exponentially large, we design efficient algorithms that effectively exploit its structure and geometry. We enhance these algorithms with early-stopping criteria, which in practice lead to four times shorter running times with minimal sacrifices in the information content they provide to the user. In addition, using crime data from Chicago and Philadelphia we develop the required risk model for their street urban networks. Our experiments with this data demonstrate the efficacy of our algorithms and their practical applicability.


## 1. INTRODUCTION

A recent United Nations report states that more than $50 \%$ of the world's population currently lives in cities. This percentage is projected to increase to $70 \%$ by 2050 [6]. One of the main reasons for these levels of urbanization is the long-lived thought of cities as the paramount instrument for innovation and wealth creation. Nevertheless, there are side effects attached to this phenomenon. Cities have become the

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main source of crimes, diseases and pollution, significantly deteriorating the quality of life of their dwellers.

During the last years, local authorities have collected a large number of civic datasets that capture various aspects of urban life. These datasets include information for street constructions, crimes, bicycle routes, etc. The open government and data initiative from President Obama's administration [5] has further led many local authorities to systematically collect, organize and publicize such datasets. Besides the transparency of federal and local government operations, this initiative seeks the development of innovative services that will impact people's lives, from the people themselves.
In this paper, we take steps towards this direction. In particular, we focus on one of the major aforementioned problems present in almost every megacity today: crimes and public safety. We develop a novel application aiming to identify safe and short paths for people to take when they navigate the city. For this purpose, we take into consideration both the spatial constraints imposed by the structure of the city's road network as well as the criminal activity in the city. Ideally, prioritizing the safety of dwellers, one would like to provide the user with the safest path from origin $s$ to destination $t$. However, such a path may incur a significant penalty in the total distance that needs to be traveled. Conversely, the shortest path between $s$ and $t$ may be risky. Therefore, we approach the problem of safe urban navigation as a bicriteria optimization problem where the goal is to provide users with a small collection of paths, each offering a different tradeoff between distance and safety.
As an example, consider the scenario illustrated by Figure 1: a city dweller is at the Philadelphia Museum of Art ( $s$ ) and wants to return to her home on Wharton Street $(t)$. Her shortest way to home is given by Path 1 . However, according to the crime model we develop in Section 4, the itinerary indicated as Path 5 constitutes her safest option, which is also about 1.5 times longer than Path 1. Instead, our art lover may prefer one of the intermediate routes (Paths 2-4), that offer various tradeoffs between distance and risk.

Our approach in a nutshell: Our approach includes an algorithmic and a modeling component. As part of the former, we define the SAFEPATHS problem as a biobjective shortest path problem where the goal is to output a collection of paths that offer different tradeoffs between their length and the associated risk. Of course the space of all possible paths can be extremely large and showing all such paths to the users may be overwhelming. Thus, our goal is to select a small subset of paths that gives a good summary


Path 1 Path 2 Path 3 Path 4 Path 5

| Length $\ell(\mathrm{m})$ | 3955 | 4027 | 4060 | 4922 | 5988 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Risk $r\left(\times 10^{-3}\right)$ | 2.32 | 2.02 | 2.01 | 1.71 | 1.70 |

Figure 1: An illustrative example of safe urban navigation. The routes depicted as Paths $1-5$ offer various compromises between distance and risk for traveling between $s$ and $t$.
of the solution space and the available tradeoffs. We study two variants of this generic problem that differ on their definition of the risk of a path. In the first variant, the risk of the path is defined as the total probability of a crime happening along all its segments. In the second variant, the risk of the path is defined as the maximum risk to which the user is exposed on any segment. The key challenge in designing algorithms for these problems stems from the fact that they aim to explore and summarize a possibly exponential solution space. The algorithms we present effectively exploit the structure and the geometry of the underlying solution space and can report a representative set of paths in a matter of seconds. Moreover, we enhance these algorithms with early-stopping criteria which, in practice, lead to 4-fold reduction of the running time with minimal sacrifices in the information content they provide to the user.

As part of the modeling component, we develop a framework for the crime risk on street urban networks. We focus on the US cities of Chicago and Philadelphia. After exporting their street networks from OpenStreetMap (OSM) into a graph format we use publicly available crime datasets to assign a risk score to each edge (i.e. street segment).
Roadmap: The rest of the paper is organized as follows. Section 2 provides the necessary notation and formally defines the SafePaths problem while Section 3 describes our algorithms to solve two specific instances of the problem. Section 4 describes the civic datasets as well as the risk model we developed for the urban road networks. In Section 5 we present our experimental results, and after reviewing the related work in Section 6, we conclude in Section 7.

## 2. PROBLEM DEFINITION

In this section, we start by presenting the necessary notation and then formally define the SAFEPATHS problem and its variants.

### 2.1 Preliminaries

Throughout the paper, we will represent the road network using an undirected graph $G=(V, E)$. The nodes of the graph, $V$, represent intersections and the edges, $E$, represent the road segments that connect intersections. The focus on undirected graphs is due to the fact that our framework is targeted primarily to pedestrians, since they are more exposed to risks in urban areas. Clearly, such users can traverse street segments in both directions. However, we emphasize that this assumption is not restrictive and the proposed framework can also be used with directed graphs.

Each road segment $e \in E$ is associated with two (unrelated) types of weights: its length, denoted by $\ell(e)$, and its risk, denoted by $r(e)$. To reiterate, the length of edge $e$ corresponds to the actual distance between the two intersections connected by the associated street segment, while the risk of edge $e$ should be interpreted as the probability that a crime will be committed on that segment. The exact details of how this model is obtained are given in Section 4.
A path $P$ on $G$ is defined as a connected sequence of edges; a path $P$ from a particular source, $s$, to a particular destination $t$ is a connected sequence of edges such that the first edge in the sequence has its starting point in $s$ and the last edge in the sequence has its ending point in $t$. When we want to specify the source and destination nodes of a path $P$, we denote it by $P_{s, t}$.

Clearly, the length of a path $P$ is the sum of the lengths of its edges; that is, $\ell(P)=\sum_{e \in P} \ell(e)$. The risk of a path $P, r(P)$, is also a function of the risks of its edges, but we consider two alternative definitions for it: the total-risk, denoted by $r_{t}(P)$ and the max-risk, denoted by $r_{m}(P)$.

On one hand, $r_{t}(P)$ is the probability of a crime happening anywhere along the path, or in other words, on any edge of $P$. More specifically, it is defined as follows:

$$
\begin{equation*}
r_{t}(P)=1-\prod_{e \in P}(1-r(e)) \tag{1}
\end{equation*}
$$

On the other hand, $r_{m}(P)$ is the highest crime probability encountered on any single edge along the path $P$, that is,

$$
\begin{equation*}
r_{m}(P)=\max _{e \in P} r(e) \tag{2}
\end{equation*}
$$

Note that both $r_{t}(P)$ and $r_{m}(P)$ have a probability interpretation. However, while $r_{m}(P)$ depends only on the most risky edge of the path, $r_{t}(P)$ involves the risk of all the edges in $P$. In both cases, we look for safe paths. That is, we want to minimize $r(P)$, whether it is instantiated as $r_{t}(P)$ or $r_{m}(P)$.

### 2.2 The SafePaths problem

At a high level, the SaFePaths problem takes as input the road network $G=(V, E)$ together with a pair of sourcedestination nodes, $(s, t)$, and its goal is to provide to the user a (set of) short and safe paths between $s$ and $t$.

The difficulty with this high-level problem definition is that clearly, the shortest path (in terms of length) is not necessarily the one with the smallest risk and vice versa. Therefore, the problem we actually want to solve is a bicriteria optimization problem, where the goal is to minimize both the length as well as the risk of the reported path. Of course, there are multiple ways of formalizing, and subsequently, solving such a bicriteria optimization problem. One way to approach it is by combining the two objectives, the
length and the risk of the path, into a single objective and ask for the path $P_{s, t}$ minimizing the weighted combination:

$$
P_{s, t}=\arg \min _{P_{s, t}^{\prime}}\left(\alpha \times \ell\left(P_{s, t}^{\prime}\right)+\beta \times r\left(P_{s, t}^{\prime}\right)\right)
$$

where $\alpha$ and $\beta$ are appropriately-tuned real-valued coefficients and $r(P)$ encodes the max or the total risk of $P$.
Although such a formulation could be an option, it has its shortcomings. First, it is not straightforward to appropriately define the parameters $\alpha$ and $\beta$ since they depend on the user preference. In this particular case, setting them is even more difficult because $\ell(P)$ and $r(P)$ are not measured in comparable units. This latter point also highlights that finding a single path that optimizes the above objective does not have a direct and intuitive interpretation since it is a single solution that optimizes a summation of distances and probabilities.
Exploring the set of all possible paths $\mathcal{P}$ : Instead of combining the two objectives into a single one and finding a unique solution with respect to that composite objective, we take a different approach. We look for a small set of paths that provide tradeoffs between the two objectives.
Every path $P$ from $s$ to $t$ is a 2-dimensional point with its $x$-coordinate corresponding to $\ell(P)$ and its $y$-coordinate corresponding to $r(P)$ (see Figure 2 for an example). Clearly, there are many paths from $s$ to $t$, corresponding to different 2-dimensional points. Therefore, in order to exhaustively explore the solution space one needs to consider all possible paths and investigate the tradeoffs they offer in terms of length versus risk. From a practical perspective, such an exhaustive exploration of the solution space is infeasible, simply because the number of possible paths can be exponential in the input size.
However, if $\mathcal{P}$ is the set of all possible paths from $s$ to $t$, then not all of these paths are of interest to the user. For instance, consider two paths $P_{1}$ and $P_{2}$, such that $\ell\left(P_{1}\right) \leq$ $\ell\left(P_{2}\right)$ and $r\left(P_{1}\right)<r\left(P_{2}\right): P_{1}$ is better than $P_{2}$ both in terms of length and risk. In this case, we say that $P_{2}$ is dominated by $P_{1}$. Obviously, solutions in $\mathcal{P}$ that are dominated by other solutions need not be considered. Since the notion of domination of paths is important for the rest of the discussion we provide a formal definition below.

Definition 1. Given two paths $P$ and $P^{\prime}$ and assuming that their lengths and risks can be computed using functions $\ell()$ and $r()$, respectively, which are to be minimized, we say that $P$ dominates $P^{\prime}$ if $\ell(P) \leq \ell\left(P^{\prime}\right)$ and $r(P) \leq r\left(P^{\prime}\right)$ and at least one of the two inequalities is strict, that is, either $\ell(P)<\ell\left(P^{\prime}\right)$ or $r(P)<r\left(P^{\prime}\right)$.

We are also not interested in returning equivalent paths, i.e. paths $P$ and $P^{\prime}$ for which $\ell(P) \leq \ell\left(P^{\prime}\right)$ and $r(P) \leq$ $r\left(P^{\prime}\right)$. In such cases we break ties arbitrarily.
Given the above, we are now ready to define the SafePaths problem:

Problem 1 (SafePaths). If $\mathcal{P}$ is the set of all possible paths from s to $t$, our goal is to select a small subset of these paths $\mathcal{S} \subseteq \mathcal{P}$ such that for every path $P \in \mathcal{S}, P$ is neither dominated by nor equivalent to any other path $P^{\prime} \in \mathcal{S}$.

Observe that in the above discussion we kept the definition of the risk of the path generic, using $r(P)$ to denote indistincly the max risk as well as the total risk. We call the


Figure 2: The 2-dimensional representation of paths from the solution space $\mathcal{P}$ of a SafePaths instance.
instance of the SafePaths problem where the risk of the path is computed using $r_{t}(P)$ (Equation (1)) the TotalPaths problem. On the other hand, when the risk of $P$ is computed using $r_{m}(P)$ (Equation (2)), we call the corresponding problem the Max-Paths problem.
Observe that Problem 1 asks for a "small" subset of nondominated paths. One can naturally wonder what the right number of paths is. Here we aim to provide the end user with a set of paths that she can easily parse. At the same time, this set should adequately represent the space of nondominated paths.

## 3. ALGORITHMS

In this section, we present our algorithms for TotalPaths and Max-Paths. Given a source-destination pair ( $s$, $t$ ), the common goal of our algorithms for both problems is to efficiently explore the space of nondominated paths from $s$ to $t$.
Our algorithms can be more easily understood if we visualize every path $P \in \mathcal{P}$ as a 2 -dimensional point, with its $x$-coordinate corresponding to $\ell(P)$ and its $y$-coordinate corresponding to $r(P)$. An example of a 2 -dimensional representation of some of the paths of $\mathcal{P}$ is shown in Figure 2.
For a fixed $(s, t)$ pair, there are two important paths: the shortest path, denoted by $P_{\ell}^{*}$, and the safest path, denoted by $P_{r}^{*}$. If they two coincide, then the point that corresponds to the shortest and safest solution dominates all others, and our algorithms report this as the only solution.
When these two paths are distinct, they are both nondominated. Furthermore, they define the "region" of our solutions in their 2-dimensional representation. In fact, all the nondominated solutions will have lengths in the interval $\left[\ell\left(P_{\ell}^{*}\right), \ell\left(P_{r}^{*}\right)\right]$ and risks in the interval $\left[r\left(P_{r}^{*}\right), r\left(P_{\ell}^{*}\right)\right]$.

We propose recursive algorithms for both versions of the SafePaths problem that share the same high-level principle. Starting with the shortest and the safest paths, $P_{\ell}^{*}$ and $P_{r}^{*}$, they consider in each iteration a pair of nondominated paths $P_{u}$ and $P_{l}$ and search for an intermediate nondominated path $P_{i}$ inside the subintervals $\left[\ell\left(P_{l}\right), \ell\left(P_{u}\right)\right]$ and [ $\left.r\left(P_{u}\right), r\left(P_{l}\right)\right]$ that they define within the original intervals. This process is repeated recursively with the pairs ( $P_{u}, P_{i}$ )
and $\left(P_{i}, P_{l}\right)$ until convergence.
Despite their common high-level description, the details of our algorithms for Total-Paths and Max-Paths differ. We describe them in turn in Sections 3.1 and 3.2. We also present speedups which can be applied to both algorithms and lead to significant computational savings, in Section 3.3
Computing shortest paths: In all our algorithms we will often use the Dijkstra shortest path routine. We use the notation Dijkstra $(G, f())$ to indicate that we run the Dijkstra shortest-path algorithm on input graph $G$ with weights on edges defined by function $f()$. That is, the output of Dijkstra $(G, f())$ is a path $P$ in $G$ minimizing $\sum_{e \in P} f(e)$.

### 3.1 Algorithms for the Total-Paths

First, let us take a closer look at the two objectives of the Total-Paths problem. For every path $P$ the length of the path, $\ell(P)$, is written as a summation of the lengths of the edges in $P$. Moreover, the total risk of the path, $r_{t}(P)$, given in Equation (1), can equivalently be minimized as a summation, namely, as the sum of the negative logarithms of one minus the risk of the edges along the path. Therefore, both our objectives can be computed as summations of (appropriately-defined) weights of the graph edges.
The solution space: Exploring the solution space of such "sum-sum" biobjective shortest path problem is a long-studied research topic and there exist many approaches that aim to find nondominated points [23] under given thresholds, or identify $\epsilon$-pareto sets of points [15, 28]. By definition, an $\epsilon$ pareto set has the following property: every nondominated point is within $\epsilon$ distance in each of the dimensions from a point in the $\epsilon$-pareto set. The problem with identifying all nondominated paths is that there can be exponentially many of them. As a result, finding them can be computationally expensive. Furthermore, reporting an exponential number of solutions to the end user can be very overwhelming in practice and thus, unrealistic and impractical. The advantage of reporting the $\epsilon$-pareto set of paths is that they contain a polynomial number of points. However, the known algorithmic techniques for computing them can lead to fairly inefficient algorithms in practice.

In order to avoid such impractical algorithms and outputs, we consider the following alternative: if $\mathcal{P}$ is the set of all paths between $s$ and $t$, we are content with reporting the lower convex hull of $\mathcal{P}$, defined with respect to the 2 dimensional representation of the points. We denote the set of points in the lower convex hull as $\mathcal{H}$. Clearly, $\mathcal{H} \subseteq \mathcal{P}$ and all points in $\mathcal{H}$ correspond to nondominated paths.
The Sum-Recursive algorithm: The pseudocode of SumRecursive, our algorithm for finding the paths in $\mathcal{H}$, is given in Figure 3. At a high level, the algorithm is a recursive algorithm that repeatedly calls the sum-rec routine. This routine takes as input two nondominated paths $P_{u}$ and $P_{l}$ and assigns to every edge $e$ of the original graph a composite weight $f(e)=r(e)-\lambda \ell(e)$, where $\lambda$ is a real number that depends on the length and the total risk of paths $P_{u}$ and $P_{l}$ according to the following rule:

$$
\lambda=\frac{r\left(P_{u}\right)-r\left(P_{l}\right)}{\ell\left(P_{u}\right)-\ell\left(P_{l}\right)}
$$

The shortest path $P_{i}$ of graph $G$ with weights assigned by $f()$ is computed by Dijkstra $(G, f())$. This new path is added to the set $\mathcal{H}$ and is used for recursively calling the sum-rec

Input: A graph $G$ with edge weights $\ell()$ and $r()$.
Output: The lower convex hull $\mathcal{H}$ of bicriteria paths for Total-Paths.
$P_{\ell}^{*} \leftarrow \operatorname{Dijkstra}(G, \ell())$
$P_{r}^{*} \leftarrow \operatorname{Dijkstra}(G, r())$
$\mathcal{H} \leftarrow\left\{P_{\ell}^{*}, P_{r}^{*}\right\}$
$\operatorname{sum-rec}\left(P_{\ell}^{*}, P_{r}^{*}, \mathcal{H}\right)$
return $\mathcal{H}$
Routine sum-rec $\left(P_{u}, P_{l}, \mathcal{H}\right)$
$\lambda \leftarrow\left(r\left(P_{u}\right)-r\left(P_{l}\right)\right) /\left(\ell\left(P_{u}\right)-\ell\left(P_{l}\right)\right)$
$\forall e \in E: f(e)=r(e)-\lambda \ell(e)$
$P_{i} \leftarrow \operatorname{Dijkstra}(G, f())$
if $P_{i} \neq P_{u}$ and $P_{i} \neq P_{l}$ then
$\mathcal{H} \leftarrow \mathcal{H} \cup\left\{P_{i}\right\}$
sum-rec $\left(P_{u}, P_{i}, H\right)$
sum-rec $\left(P_{i}, P_{l}, H\right)$

Figure 3: The Sum-Recursive algorithm for the TotalPaths problem.
routine using as input the pair of paths $\left(P_{l}, P_{i}\right)$ and the pair $\left(P_{i}, P_{u}\right)$. Paths $P_{\ell}^{*}$ and $P_{r}^{*}$ are used as the initial pair, and they are also members of $\mathcal{H}$. By the results of Mehlhorn and Ziegelmann [23] we have:

Proposition 1. The set of paths $\mathcal{H}$ reported by the SumRecursive algorithm upon termination is the lower convex hull of the solution space $\mathcal{P}$.
If the Sum-Recursive reports $|\mathcal{H}|$ points, it further requires $O(|\mathcal{H}|)$ calls to the Dijkstra routine. Thus, the worst-case running time of Sum-Recursive is $O(|\mathcal{H}|(|E|+|V| \log |V|))$.

### 3.2 Algorithms for the Max-Paths

Again, let us take a closer look at the two objectives of the Max-Paths problem. For every path $P$ the length of the path $\ell(P)$ is again the summation of the lengths of the edges in $P$. However, now the max-risk of the path, $r_{m}(P)$, is the maximum of the risks of the edges in $P$ (cf. Equation (2)). Therefore, one of our objectives can be written as a summation of edge lengths and the other as the max of the edges risks, resulting in a "sum-max" biobjective problem.
The solution space: This "sum-max" biobjective problem turns out to have a more structured solution space than the "sum-sum" problem we studied in the previous section. More specifically, we have the following observation:

Proposition 2. Any set of nondominated and nonequivalent paths in the solution space of the MAX-Paths has size polynomial to the size of the input.

The proof is based on the following fact: since the risk of a path corresponds to the risk of a single edge along the path, there can be only as many distinct values for the path risks as there are edges in the network and there can be at most one nondominated path for every such distinct value.
The Max-Exhaustive algorithm: The exhaustive algorithm for finding the nondominated paths is straightforward: first, find $P_{\ell}^{*}$ and report this as a nondominated path. Then, identify in $P_{\ell}^{*}$ the edge with the maximum risk and remove from the original graph all edges with risk greater or equal to that value. Find again the shortest path in this reduced subgraph and add the new path into the set of nondominated solutions. Iterate the above process until the source and target are no longer connected. This algorithm, that

Input: A graph $G$ with edge weights $\ell()$ and $r()$.
Output: The set $\mathcal{S}$ of nondominated bicriteria paths for Max-Paths.
$P_{\ell}^{*} \leftarrow \operatorname{Dijkstra}(G, \ell())$
$P_{r}^{*} \leftarrow \operatorname{Safest}(G, r())$
$\mathcal{S} \leftarrow\left\{P_{\ell}^{*}, P_{r}^{*}\right\}$
$\max -\operatorname{rec}\left(P_{\ell}^{*}, P_{r}^{*}, \mathcal{S}\right)$
return $\mathcal{S}$
Routine max-rec $\left(P_{u}, P_{l}, \mathcal{S}\right)$
$\rho \leftarrow\left(r\left(P_{u}\right)+t\left(P_{l}\right)\right) / 2$
if $\exists e \in E, t\left(P_{l}\right)<r(e)<\rho$ then $P_{i} \leftarrow \operatorname{Dijkstra}\left(G_{r(e)<\rho}, \ell()\right)$ if $P_{i} \neq P_{l}$ then $\mathcal{S} \leftarrow \mathcal{S} \cup\left\{P_{i}\right\}$ $\max -\operatorname{rec}\left(P_{i}, P_{l}, \mathcal{S}\right)$
$\max -\operatorname{rec}\left(P_{u}, P_{i}, \mathcal{S}\right)$

Figure 4: The Max-Recursive algorithm for the Max-Paths problem.
we call Max-Exhaustive, has at most $O(|E|)$ repetitions and each repetition requires running Dijkstra on the remaining graph, resulting in an $O\left(|E|^{2}+|E||V| \log |V|\right)$ running time.
The Max-Recursive algorithm: Instead of going over possible risk thresholds in decreasing order, like Max-Exhaustive, Max-Recursive proceeds by recursion. The pseudocode is given in Figure 4.

At line 8, Max-Recursive runs the Dijkstra routine on $G_{r(e)<\rho}$, the subgraph obtained from $G$ after removing all edges with risk greater or equal to $\rho$. By doing so, it identifies the shortest path $P_{i}$ in $G$ such that $r_{m}(P)<\rho$. For algorithmic purposes, we need to remember the threshold with which a path $P$ has been discovered, which we denote by $t(P)$. Indeed, upon finding $P_{i}$, we know that there is no nondominated path with risk between $t\left(P_{l}\right)$ and $r\left(P_{i}\right)$, so we can leave out that range. Given two paths $P_{u}$ and $P_{l}$, max-rec considers as risk threshold $\rho$ the mean of $r\left(P_{u}\right)$ and $t\left(P_{l}\right)$. If there exist edges with risk between $t\left(P_{l}\right)$ and $\rho$, and hence potentially paths with $r_{m}$ inside that range, the Dijkstra routine is run to identify the shortest such path. max-rec iterates with $P_{u}$ and the new path, as well as with the new path and $P_{l}$, if they differ.
With Max-Recursive, we need to compute the safest path in the input graph $G$ upfront in order to initiate the recursions. This is done by the Safest routine in the pseudocode of Max-Recursive as follows. First, we compute the minimum spanning tree (MST) of the graph considering the risks of the edges as the weights. The risk $\rho_{s, t}^{*}$ of the safest path between a given pair $(s, t)$ is the maximum risk encountered along the unique path from $s$ to $t$ in this spanning tree. Then, we compute the shortest path verifying this risk threshold by running the Dijkstra routine on $G_{r(e) \leq \rho_{s, t}^{*}}$ to obtain $P_{r}^{*}$. Note that its length will generally differ from the length of the path connecting $s$ and $t$ in the spanning tree.
Figure 2 illustrates a run of this algorithm. First, the shortest path $\left(P_{\ell}^{*}\right)$ and safest path $\left(P_{r}^{*}\right)$ are found, then $\rho_{1}$ is used as threshold, finding $P_{1}$. The next thresholds are $\rho_{4}$ and $\rho_{2}$ in the upper and lower side respectively, and so on.
Since we are not looking for a unique solution we explore both sides after a binary split. Thus, the worst-case complexity of this approach is the same as the exhaustive search. In fact, the advantage of Max-Recursive only appears when combined with the approximation speedup discussed in the


Figure 5: Illustration of the Ellipse pruning.
next section, which cannot be applied to Max-Exhaustive.

### 3.3 Computational speedups

In this section we describe our strategies for speeding up the above algorithms, applicable to both versions of the SafePaths problem.
Approximation via early stopping: The running time of our algorithms for both versions of the SAFEPATHS problem depend linearly on the number of points in the set of paths returned by the algorithms. Therefore, one way of speeding up the algorithms is by reporting a subset of those paths. Hence, by restricting the number of iterations of the SumRecursive and the Max-Recursive we contribute to both of our aforementioned objectives, i.e., reducing the runtimes and limiting the size of the reported solution sets.

Specifically, consider the shortest and the safest paths with 2-dimensional representations $\left(\ell\left(P_{\ell}^{*}\right), r\left(P_{\ell}^{*}\right)\right)$ and $\left(\ell\left(P_{r}^{*}\right)\right.$, $r\left(P_{\ell}^{*}\right)$ ) respectively, defining a rectangle of area $A$. Before calling the recursive routine with two paths $P_{u}$ and $P_{l}$, we check the area of the unexplored rectangle between them. If this area becomes smaller than a chosen fraction $\gamma$ of $A$ we stop the iteration. With sum-rec, the unexplored rectangle for paths $P_{u}$ and $P_{l}$ is delimited by $\left(\ell\left(P_{u}\right), r\left(P_{u}\right)\right)$ and $\left(\ell\left(P_{l}\right)\right.$, $\left.r\left(P_{l}\right)\right)$. With max-rec, it is delimited by $\left(\ell\left(P_{u}\right), r\left(P_{u}\right)\right)$ and $\left(\ell\left(P_{l}\right), t\left(P_{l}\right)\right)$, since we know there is no nondominated path with risk between $t\left(P_{l}\right)$ and $r\left(P_{l}\right)$. In Figure 2 for instance, with $\gamma=0.1$, since the hatched area is smaller than onetenth of $A$, the total area of the solution space (delimited by a grey solid line), the recursive routine is not called for $P_{3}$ and $P_{2}$. In summary, the choice of $\gamma$ directly limits the number of iterations and the number of paths in the solution; larger $\gamma$ results in fewer paths returned and shorter runtimes.
Pruning: Our pruning strategy, which we call the Ellipse pruning, is based on the following observation: any path between $s$ and $t$ that is longer than the safest path, will be dominated by it.

This observation has the following consequence: if $L$ is the length of the safest path between $s$ and $t$, then any node $u$ such that the sum of the distances "as the crow flies" from $s$ to $u$ and $u$ to $t$ is greater than $L$ cannot be part of the solution. This criterion defines an ellipse with foci $s$ and $t$ and major axis of length $L$. Hence, after finding $P_{r}^{*}$ we can safely remove any node that lies outside the ellipse, thereby reducing the size of the graph processed in subsequent calls to the Dijkstra routine.

This observation is pictorially depicted in Figure 5. The safest path between $s$ and $t$ is shown in green and its length $L$ defines the length of the major axis of the ellipse drawn in
red. Any node located outside this ellipse can be discarded from further computations for the pair $(s, t)$.

We combine the Ellipse pruning with another simple pruning technique: we split the area that corresponds to the city (or neighborhood) of interest into a grid and project the graph $G$ on this grid. Then, instead of considering the original graph we only consider the grid cells that are included into or overlap with the ellipse, for instance, the eleven cells marked with a star in the example shown in Figure 5.

Note that the Ellipse pruning reduces the size of the input graph, without sacrificing the accuracy. That is, the set of nondominated paths before and after the Ellipse pruning remains the same.

## 4. MODELING CRIME DATA

In this section, we describe the civic datasets that we will use in our experiments. More specifically we explain how we combined data from different sources in order to form the input to our algorithms.
Urban road network: We extract the actual road network of a city using OpenStreetMap (OSM) [1]. OSM is a crowdsourcing-based open platform, which aims to make the world map freely available. The OSM community has developed a number of tools that facilitate the integration of OSM maps with a variety of applications. For our purposes we make use of the osm4routing parser [3], that exports the map of interest from an OSM format (appropriate for traditional GIS systems) to a graph-based format (appropriate for graph-based algorithms).
In particular, each node $v$ in the exported graph $G$ corresponds to an intersection, while each edge $e$ represents a street segment that connects two intersections. osm4routing provides additional information about the intersections and the street segments as node and edge attributes. Specifically, the geographical location (latitude/longitude pair) of each node is provided. Each edge $e$ is annotated with a variety of features. The following ones are of particular interest for our study:

- Length $\ell(e)$, the physical length of the corresponding street segment. It is the length value we associate with every edge in our input graph.
- Geometry $\Gamma(e)$, a sample set of discrete latitude/longitude points from the street segment. It essentially provides information about the actual geographic shape of the street segment.
- Accessibility flags, indicators that capture the accessibility of a street segment by car, bicycle and foot.
Here, we consider the pedestrian street network of Chicago and Philadelphia. We obtained the OSM maps for the metropolitan areas of these two cities from Metro Extracts [2].
Crime datasets: In addition to the above, we also use two civic datasets made available by the cities of Chicago ${ }^{1}$ and Philadelphia ${ }^{2}$ that encode information about crimes in the two cities for the one year period between October 2012 and September 2013. Their formats do not align, as it is true with the majority of civic datasets made available from different cities even when they aim to convey the same information. Nevertheless, some basic information that both

[^0]

Figure 6: KDE for crime activity in Chicago (left) and Philadelphia (right).
of our datasets include are encoded in the tuple:

## $<$ Date, Time, Latitude, Longitude, TypeofCrime $>$.

Risk model: A risk model for the urban road network is essentially an assignment of a risk score $r$ to each edge that is proportional to the probability of a crime happening on the corresponding street segment. Note that we do not intend to infer the exact risk probability of individual edges with this model. Rather, we are interested in the relative values of $r$ for different edges and the fact that they can be interpreted as probabilities.

Our model is built in a two-step process. First, we use the geographic coordinates of the crime incidents to compute a spatial density for the crime activity by applying a Gaussian kernel density estimation (KDE). Given $n$ points of crime incidents $\mathbf{c}_{1}, \mathbf{c}_{2}, \ldots, \mathbf{c}_{n}$ on a 2-dimensional plane, the Gaussian kernel estimates the density of crime activity at point p as:

$$
\begin{equation*}
\lambda(\mathbf{s})=\frac{1}{n h^{2}} \sum_{i=1}^{n} \frac{1}{\sqrt{2 \pi}} \exp \left(-\frac{\left\|\mathbf{c}_{i}-\mathbf{p}\right\|_{2}^{2}}{2 h^{2}}\right) \tag{3}
\end{equation*}
$$

where $\left\|\mathbf{c}_{i}-\mathbf{p}\right\|_{2}$ is the euclidean distance between points $\mathbf{c}_{i}$ and $\mathbf{p}$ and $h$ is the bandwidth used. The bandwidth $h$ dictates the spread of the Gaussian kernel that is centered at each datapoint and hence, it controls the smoothness of the estimated density. Small values of $h$ can capture more detail while large values of $h$ lead to smoother estimation. In other words, it is the analogue of the bin width of a histogram. We determine $h$ according to Scott's rule [25]. Figure 6 visualizes the estimated densities for the two cities. As we can observe, crimes are not uniformly distributed over the metropolitan areas of the two cities but there are hotspots of crimes, something expected based both on our experience as city-dwellers as well as on existing literature in a variety of fields (e.g. [11, 24]).
Once the density function is estimated, we evaluate it on the actual road segments. For this purpose, we make use of the geometry $\Gamma(e)$ of each edge $e$ of the road network. Evaluating Equation (3) on every point $\boldsymbol{\xi}_{i} \in \Gamma(e)$ and summing up we obtain the crime density $\Lambda(e)$ on road segment $e$ : $\Lambda(e)=\sum_{\boldsymbol{\xi}_{i} \in \Gamma(e)} \lambda\left(\boldsymbol{\xi}_{i}\right)$. Finally, we compute the risk weights for every edge $e$ as the normalized densities:

$$
\begin{equation*}
r(e)=\frac{\Lambda(e)}{\sum_{e^{\prime} \in G} \Lambda\left(e^{\prime}\right)} . \tag{4}
\end{equation*}
$$

Networks statistics: We obtain two graphs, Chicago and Philadelphia, representing the street networks of the


Figure 7: Empirical probability density functions of edge lengths (left) and risks (right) for Chicago (blue dashed line) and Philadelphia (green solid line).

Table 1: Statistics of the road networks.

|  | $\|V\|$ | $\|E\|$ |
| :--- | :---: | :---: |
| Chicago | 57998 | 91695 |
| Philadelphia | 55234 | 82676 |

metropolitan areas of Chicago and Philadelphia, respectively. Their node and edge counts are given in Table 1 and as we can see they are fairly similar.
Figure 7 depicts the empirical distributions of edge lengths (left) and risks (right) over the two networks. In both cities, most edges span a short geographic distance, that is, less than 250 m . There are few edges spanning long distances, 4 km and above (not shown), that most likely correspond to highways. Similarly, the distributions of risks are highly right-skewed for both cities, which essentially indicates that while most edges are assigned low risk values, there exist street segments that are comparatively dangerous and exhibit much higher risk values.
We point out that our model does not involve time, but can be easily extended with a temporal dimension. In particular, we can quantize the time depending on the granularity required by the application (e.g. hourly bins) and consider separately crimes that happened during each time period. Then the density (Equation (3)) and the final risk values (Equation (4)) will also be functions of time, and we will be able to set the weights according to the time of the query from the user, resulting in a time dependent version of the SafePaths problem. Nevertheless, handling the temporal dimension is beyond the scope of our work and we ignore it in our experiments.

## 5. EXPERIMENTS

In this section, we present an experimental assessment of our proposed methods. Our main objective is to evaluate the practical utility of our algorithms. We focus on two aspects: (i) the representativeness of the small set of nondominated paths that our algorithms return and (ii) their runtime.
We build our evaluation benchmark by sampling node pairs from both cities. To ensure a good coverage of scenarios involving short distances, which are of particular interest for a pedestrian urban navigation system, we perform distance-aware sampling. More specifically, we sample 100 nodes for each city. Then, for each of these source nodes, we divide the remaining nodes into classes based on their distance "as the crow flies" from the source. Considering

Table 2: Summary of the solution sizes. We indicate the total number of solutions, number of singletons and of twopaths solutions $(|\mathcal{S}|=1$ and $|\mathcal{S}|=2)$ and number of approximations multi-paths solutions identical to the exact solution.

|  | Total-Paths |  | Max-Paths |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Chicago | Philadelphia | Chicago | Philadelphia |
| Total | 2400 | 2400 | 2400 | 2400 |
| $\|\mathcal{S}\|=1$ | 111 | 407 | 263 | 562 |
| $\|\mathcal{S}\|=2$ | 182 | 148 | 317 | 253 |
| Ident. $\mathrm{A}_{5}$ | 520 | 476 | 398 | 424 |
| Ident. $\mathrm{A}_{10}$ | 420 | 407 | 340 | 351 |
| Ident. $\mathrm{A}_{20}$ | 337 | 327 | 14 | 49 |

distances of $1,2,3,4$ and 5 kilometers we have five concentric circles around the source that divide the plane into six distance classes further denoted by $D_{0}, D_{1}, \ldots D_{5}$. With this setting we sample 4 targets from each class, obtaining a total of $2400(s, t)$ pairs for each city.

We run our algorithms for the Total-Paths and the Max-Paths problems for each of the pairs on their respective road network. For each run, we obtain a set of paths offering different tradeoffs between distance and safety. For instance, Figure 1 depicts an actual solution of 5 paths to the Total-Paths problem for a pair of nodes in Philadelphia.

The 2-dimensional representation of a solution consisting of 8 paths to Max-Paths for a pair of nodes in Chicago is plotted in blue in Figure 2. As we explained previously, a path $P$ can be represented in a 2 -dimensional space by a point whose $x$ and $y$-coordinates correspond to $\ell(P)$ and $r(P)$ respectively. Given a pair of nodes, the shortest and safest paths joining them, $P_{\ell}^{*}$ and $P_{r}^{*}$, define a rectangle $R$. A solution to the SafePaths problem is a set of paths $\mathcal{S}$ including $P_{\ell}^{*}$ and $P_{r}^{*}$. In the 2-dimensional space, $\mathcal{S}$ can be represented with a curve that starts from $P_{\ell}^{*}$, ends at $P_{r}^{*}$ and passes through intermediate nondominated paths in $\mathcal{S}$ across $R$. Formally, given a solution $\mathcal{S}=\left(P_{\ell}^{*}, P_{1}, P_{2}, \ldots, P_{r}^{*}\right)$, where the paths are ordered by increasing length, the corresponding curve is defined by: $\left(\ell\left(P_{\ell}^{*}\right), r\left(P_{\ell}^{*}\right)\right),\left(\ell\left(P_{1}\right), r\left(P_{\ell}^{*}\right)\right)$, $\left(\ell\left(P_{1}\right), r\left(P_{1}\right)\right),\left(\ell\left(P_{2}\right), r\left(P_{1}\right)\right), \ldots\left(\ell\left(P_{r}^{*}\right), r\left(P_{r}^{*}\right)\right)$.

Based on this representation, each solution is associated with an area: the area of $R$ located under the curve. Continuing on our example in Figure 2, the area associated with the 8-paths solution is colored in blue. Paths offering good tradeoffs correspond to points close to the bottom left corner of $R$. Hence, solutions containing good tradeoffs are associated with small areas (relative to the total area of $R$ ).
Approximations: The representativeness of our algorithms can be captured through their goodness of approximation as compared to the exact algorithms for the corresponding problems. In particular, we compare the exact algorithms Sum-Recursive (for Total-Paths) and Max-Exhaustive (for MAX-PATHS), to both recursive algorithms with applying the approximation via early stopping - described in Section 3.3. For the latter we use three different values for the stopping criterion $\gamma$, namely, $0.05,0.10$ and 0.20 . We denote each of the above four runs for either problem by $E, A_{5}, A_{10}$ and $\mathrm{A}_{20}$, respectively.

Our goal is to evaluate the ability of our proposed approx-


Figure 8: Results for Total-Paths on Chicago.


Figure 9: Results for Max-Paths on Chicago.
imations to capture the landscape of nondominated paths. When the shortest and the safest paths coincide (i.e. $|\mathcal{S}|=1$ ) or when there are no intermediate paths between $P_{\ell}^{*}$ and $P_{r}^{*}$ (i.e. $|\mathcal{S}|=2$ ), the approximations trivially return the same solution as the exact algorithms. Solutions containing intermediate paths (i.e. $|\mathcal{S}|>2$ ) are called multi-paths solutions. The counts of singletons and two-paths solutions found for both cities and both problems are reported in Table 5 . In addition, we also report the number of multi-paths solutions found with the approximations that are identical to the exact solutions. For instance, with the stricter approximation $\mathrm{A}_{5}$ for the Total-Paths problem in Chicago, $111+182+520=813$ solutions out of 2400 obtained are identical to the exact solutions, as compared to only 630 with the looser approximation $\mathrm{A}_{20}$. The difference is even more pronounced for the Max-Paths problem.

Still, we would like to measure the quality of the approximations beyond strict equality of the solution sets. For this purpose, we compare the area associated with the solution obtained with an approximation, denoted as $S_{\mathrm{A}}$, with the area associated with the solution returned by the exact algorithm, denoted as $S_{\mathrm{E}}$. Note that since the approximate solution is a subset of the exact solution, we have $S_{\mathrm{E}} / S_{\mathrm{A}}$ and


Figure 10: Results for Total-Paths on Philadelphia.


Figure 11: Results for Max-Paths on Philadelphia.
the equality holds if and only if the solutions are identical. Thus, we use the ratio $S_{\mathrm{E}} / S_{\mathrm{A}}$ to measure the quality of the approximations. It takes values in the unit interval, with values closer to one indicating better approximations.
The statistics of our results, grouped by distance classes, are presented as box plots in Figures 8-11. In each figure, the three lines of plots depict from top to bottom the distribution of (i) area ratios $\left(S_{\mathrm{E}} / S_{\mathrm{A}}\right)$, (ii) solution sizes $(|\mathcal{S}|)$ and (iii) runtimes in seconds ( $T$ ) across the 400 pairs from each distance class. Note the different scale used for the last column in each figure (for $D_{5}$ ).
While remaining of high quality (average area ratios $S_{\mathrm{E}} / S_{\mathrm{A}}$ almost always lie above 0.8 ), the approximations clearly deteriorate for larger distances and especially for $\mathrm{A}_{20}$. This is due to the fact that the average number of paths in the solutions returned by the exact algorithms increases as distances expand while the number of paths in the solutions with approximations is capped. The number of paths per solution averages between 7.83 and 16.33 and reaches up to 144 for the exact algorithms, while approximate solutions never contain more than 8 paths, with an average between 2.93 and 4.3 depending on the scenario. As expected, the runtime scales linearly with the size of the solution. Hence, com-
bining the algorithms with approximations yields notable reductions in the runtimes, especially for larger distances.

In summary, by using moderate approximations (e.g. $\mathrm{A}_{10}$ ) we obtain very satisfactory solutions containing a small number of paths, with shorter and more predictable runtimes, supporting the practical utility of our algorithms.
For the same problem, discrepancies arise between the two cities due to characteristics of their respective road networks and crime distributions. For instance, because of the Delaware river that runs through Philadelphia, the walking distance between nodes on either side of the river is much greater than their distance "as the crow flies". Hence, the closer distance classes contain pairs for which the shortest path is much longer than expected. Besides, crime locations are more spatially clustered in Chicago (see Figure 6) so the KDE for the crime activity is less regular, yielding a greater variety of risk thresholds in the Max-Paths problem.
Pruning: Next, we investigate the benefits of applying the Ellipse pruning described in Section 3.3. These pruning techniques discard nodes that are too far away from $s$ and $t$ to be part of nondominating solutions. The first pruning technique, denoted by $\mathrm{L}_{\mathrm{N}}$, filters individual nodes while the second, denoted by $L_{G}$ uses a grid and filters entire cells at once. Both techniques only affect the runtime of the algorithms without impacting the solutions.
For this experiment, we focus on the Sum-Recursive and Max-Recursive algorithms combined with approximation using $\gamma=0.10$, as they represent the most practical scenario. The runtimes in seconds on the Chicago network for these algorithms with and without the pruning techniques are reported in Figure 5.
$\mathrm{L}_{\mathrm{N}}$ drastically reduces the size of the input graph of the Dijkstra routines, as witnessed by the very short span of runtimes. However, the pruning operation itself imposes a large overhead which takes away most of the benefits of using this method. This is particularly evident for the TotalPaths problem, where the average runtime with the pruning is almost equivalent to the average runtime of the original algorithm, if not greater.
On the contrary, $\mathrm{L}_{\mathrm{G}}$ does not suffer from this drawback. While selecting whole cells at once is suboptimal in terms of the reduction of the graph, it can be performed more efficiently, resulting in an overall gain for both problems. Tuning the size of the grid provides a means to adjust the balance between stringency and speed of pruning. Here, after a short exploration, we chose a grid of $20 \times 20$ cells.
When the source and target nodes are far apart, the ellipse covers the graph almost entirely. Then, no node can be discarded and pruning only adds overhead runtime. However, such situations can be easily detected and the pruning can be abandoned.

## 6. RELATED WORK

Our work is related to research on modeling crime events and on recommending routes to city dwellers, as well as to theoretical work on biobjective optimization problems. Here, we review these lines of research and their connections to our framework.
Crime event models: Crime events are neither random nor uniform [24], but they exhibit spatial and temporal patterns. Large research efforts focus on the development of specialized systems for crime mapping $[21,10,26]$ that can


Figure 12: Runtime for pruning on Chicago.
be used by law enforcement agencies to study and analyze crime patterns and to inform their decisions on strategies against crime. While these methods can visualize events in the physical urban environment, there is also a large volume of urban and social literature that attempts to explain the reasons behind the observed patterns of crimes [9, 12, 13]. Such theories can also provide guidelines for policies that aim to prevent crimes. For instance, environmental criminology studies the relation between crime events and the spatio-temporal context of people's activities [9]. Apart from these theories, there is a surge in studies that aim to identify and exploit patterns in historical crime data, hoping to forecast crimes (e.g. [29, 30, 20, 8]). These efforts have produced an arsenal of software tools that is available to law enforcement for proactive policing (e.g. COPLINK [18], ESRI's GIS platform [4]).
While we are unable to present an exhaustive account of the corresponding literature, we emphasize here that our study is complementary in two ways: firstly, we propose computational methods relying on combinatorial algorithms that use crime data to recommend routes. Secondly, our algorithms could be combined with forecasting systems that project/update the probabilities of crime in the various street segments for upcoming path queries.
Urban navigation: Systems with new navigation objectives that go beyond the shortest path have recently appeared in the literature [ $7,22,14,16,17,19,27,31]$. Such objectives include the recommendation of healthy routes (i.e. maximizing physical activity) [27], routes tailored to the personal interests and spatiotemporal constraints of users [7, 22, $14,16]$, or routes that take into account traffic information gathered from historical speed patterns and GPS devices [17, 19, 31]. To the best of our knowledge we are the first to consider the biobjective problem of safe and short routes.
Biobjective shortest paths: From a computational viewpoint, our work is related to research on biobjective optimization and, more specifically, biobjective shortest paths [15, 23, 28]. Such methods either aim to identify the optimal path with respect to one objective given a threshold on the other, a problem known as the resource constrained shortest path [23], or they try to report a polynomial number of points that are close enough to all nondominated points [15, 28]. The Total-Paths problem could potentially benefit from the above studies, had the existing methods been more
efficient in practice. Thus, while we acknowledge this literature, we resort to an algorithm that only explores the lower convex hull of the solution space. In fact, this algorithm was proposed as a subroutine to the enumeration methods of Mehlhorn and Ziegelmann [23]. On the other hand, the Max-Paths problem proves to have a much more structured solution space, allowing us to identify complete sets of nondominated paths.

## 7. CONCLUSIONS

In this paper, we developed practical algorithms for safe urban navigation. In particular, we formalized the SAFEPATHS problem as a biobjective optimization problem and set as our goal to identify a small collection of nondominated paths that provide different tradeoffs between distance and safety. We explored two variants of this problem and designed efficient algorithms for solving them involving approximation and pruning techniques.

Based on civic datasets from Chicago and Philadelphia, we built a crime event model for the urban road networks of these two cities, which was obtained from OpenStreetMap. Our experimental evaluations showed the efficacy and the efficiency of our algorithms and demonstrated the practicality of biobjective optimization formulations in this setting.

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