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▶ To cite this version:

Edouard Canot, Renaud Delannay. Liquid menisci equilibrium in a wet granular medium in pendular regime – Cohesive strength estimation for random smooth spheres packings. Condensed Matter in Groningen (CMD26), Sep 2016, Groningue, Netherlands. . hal-01398312

HAL Id: hal-01398312 https://hal.science/hal-01398312

Submitted on 17 Nov 2016

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Liquid menisci equilibrium in a wet granular medium in pendular regime – Cohesive strength estimation for random smooth spheres packings



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1 – Can a simple model well represent the cohesion? Expected Cohesive Strength



Sandcastle: a small water content gives strong capillary forces!





2 – Two smooth spherical grains' system

Control parameters: R radius of the spherical grains ϵ half of the gap between them κ total curvature of the meniscus surface σ surface tension θ contact angle liquid-solid

Variables obtained after computation: r_o radius of the neck $r_{\rm B}$ radius of the wet surface of the solid part V volume of the liquid meniscus



come from surface tension

Maximum of this cohesive strength should occur at the end of the pendular regime... (see Richefeu et al., 2016, for a realistic 2D simulation)

3 – Statistics for random spheres' packings

 \rightarrow numerically obtained via DEM (L. Oger, IPR)





S surface area of the liquid meniscus F attractive force between the two grains

$F = \sigma \left(2 \pi r_0 + \kappa \pi r_0^2 \right)$

Meniscus shape computed numerically: integration of an ODE system, in an axisymmetric coord. system, specifying a constant total curvature κ Numerical results for r_0 , V, S, F: stored in a database

frontières

Main tendencies for the behaviour of the capillary force $F(\varepsilon,V)$



With respect to the volume V: \rightarrow force ~ Cst for contact (ϵ =0) (even for infinitesimal volume!)

Energy approach: Gibbs free potential

Defining the Gibbs free energy as: (P. Attard, 2000; Elliott & Voitcu, 2007) With respect to the gap ϵ : \rightarrow force is always decreasing

Leads to *unstable situation* as the following:



 \rightarrow Easy to parameterize – isotropic case: median of log(gap) + sharpness - anisotropic case: % of true contacts + distribution width

5 – Results and Conclusion

- \rightarrow Strong dependency with the contact angle, as expected
- \rightarrow Plots w.r.t. saturation (strongly linked to Relative Humidity and curvature κ via the Kelvin equation)



 \rightarrow Good behavior but not realistic packing (because lot of true contacts must occur!)

Advantages of roughness introduction:

 \rightarrow already emphasized by Bocquet *et al.*, 2002 \rightarrow avoids true contacts between smooth spheres

Funicular **Behaviour not expected!** Smooth spheres model not appropriate! → Needs introduction of roughness

Pendular



 $G(\varepsilon,\kappa) = \sigma (A_{LV} - A_{SL} \cos \theta - 2 V \kappa)$ where A_{IV} and A_{SI} are the liquid-vapor and solid-liquid surface area

then $F = \frac{\partial G}{\partial \epsilon}$ with κ fixed (not V!)

4 – Computing the cohesive strength

Density of Gibbs free energy: $\bar{G}(\kappa) = N_g \int_{-\infty}^{-\infty} D(\epsilon) G(\epsilon, \kappa) d\epsilon$

The Cohesive Strength χ :

of a tension N/m^2

- \rightarrow average of the normal components of the tensile tensor (Richefeu *et al.*, 2016); (avoid the full tensile tensor, as in Scholtès et al., 2009)
- → computed via a Uniform Volumetric Expansion $\chi(\kappa) = \frac{\partial G}{\partial \beta}$ where β is the dilatation
- \rightarrow doesn't need the direction of the contacts, uses only statistical information (see below)

Equilibrium \rightarrow all liquid menisci have the same curvature κ

 κ related to Relative Humidity via Kelvin equation

Recast in terms of $\frac{\partial D(\epsilon)}{\partial \epsilon}$ instead of $\frac{\partial G(\epsilon)}{\partial \epsilon}$ because $D(\epsilon)$ is well approximated by a

mathematical function: \rightarrow needs to work with a shifted distribution of gaps

The cohesive strength $\chi(\kappa)$ has the dimension





kappa = -4.3e3

Shifted distribution of gaps

- \rightarrow allows the decreasing of the cohesive strength w.r.t. liquid volume (or saturation): see the regime II of Halsey & Levine, 1998
- \rightarrow another possibility is the cone-plane contact model of Albert et al., 1997

Three-regime model of Halsey & Levine, 1998 \rightarrow capillary force decrease as liquid volume tends to zero

References

Albert et al., 1997, Maximum angle of stability in wet and dry spherical granular media, Phys. Rev. E, 56, 6, pp 6271-6274 Halsey & Levine, 1998, How sandcastles fall, Phys. Rev. Letters, 80, 14, pp 3141-3144 P. Attard, 2000, Thermodynamics analysis of bridging bubbles..., Langmuir, 16, pp 4455-4466 Bocquet et al., 2002, *Physics of humid granular media*, C. R. Physique 3, pp 207-215 Staron et al., 2005, *Multi-scale analysis of the stress state in a granular slope...*, Eur. Phys. J. E, 18, pp 311-320 Elliott & Voitcu, 2007, On the thermodynamics stability of liquid capillary bridges, Canadian J. of Chem. Engng, 85, pp 692-700 Scholtès et al., 2009, On the capillary stress tensor in wet granular materials, Int. J. Num. Anal. Meth. Geomech., 33, pp 1289-1313 Richefeu et al., 2016, Lattice Boltzmann modelling of liquid distribution in unsaturated granular media, Comput. Geotech., in press, DOI:10.1016/j.compgeo.2016.02.017

Non constant shift due to the volumetric dilatation of the grains' packing

Boundary effect at the origin, comes from the integration by parts



