

# Decreasing the Electronic Confinement in Layered Perovskites through Intercalation

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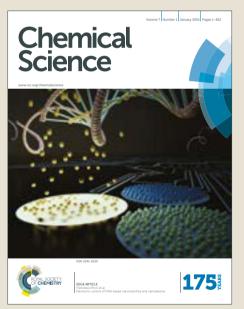
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Chemical Science Accepted Manuscript

# Decreasing the Electronic Confinement in Layered Perovskites through Intercalation<sup>†</sup>

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We show that post-synthetic small-molecule intercalation can significantly reduce the electronic confinement of 2D hybrid perovskites. Using a combined experimental and theoretical approach, we explain structural, optical, and electronic effects of intercalating highly polarizable molecules in layered perovskites designed to stabilize the intercalants. Polarizable molecules in the organic layers substantially alter the optical and electronic properties of the inorganic layers. By calculating the spatially resolved dielectric profiles of the organic and inorganic layers within the hybrid structure, we show that the intercalants afford organic layers that are more polarizable than the inorganic layers. This strategy reduces the confinement of excitons generated in the inorganic layers and affords the lowest exciton binding energy for an n = 1perovskite of which we are aware. We also demonstrate a method for computationally evaluating the exciton's binding energy by solving the Bethe-Salpeter equation for the exciton, which includes an ab initio determination of the material's dielectric profile across organic and inorganic layers. This new semi-empirical method goes beyond the imprecise phenomenological approximation of abrupt dielectric-constant changes at the organic-inorganic interfaces. This work shows that incorporation of polarizable molecules in the organic layers, through intercalation or covalent attachment, is a viable strategy for tuning 2D perovskites towards mimicking the reduced electronic confinement and isotropic light absorption of 3D perovskites while maintaining the greater synthetic tunability of the layered architecture.

#### Introduction

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The remarkable optoelectronic properties of organic-inorganic metal-halide perovskites have recently come to light. Notably, these properties can be synthetically modulated by altering the dimensionality of the anionic inorganic lattice. Small organic cations allow for the self-assembly of threedimensional (3D) frameworks, whereas larger organic cations partition the inorganic lattice into two-dimensional (2D) sheets.<sup>1</sup> Recently, 3D Pb–I perovskites have been employed as low-cost absorbers in high-efficiency solar cells.<sup>2-4</sup> Here, the weak binding energy between photogenerated electrons and holes allows for charge carriers to easily separate and migrate towards their respective current collectors. The high dielectric constant of the 3D Pb-I lattice shields the coulombic attraction between photogenerated electrons and holes.<sup>5, 6</sup> This results in free charge carriers that are ideal for solar-cell absorbers. On the other hand, typical 2D n = 1 perovskites (where n is the number of metal-halide sheets in each inorganic layer) are not

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suitable for standard photovoltaic devices, owing to the presence of strongly bound electron-hole pairs, or excitons. The quantum confinement of the 2D inorganic sheets increases the bandgap  $(E_g)$  and exciton binding energy  $(E_b)$ relative to the 3D materials. The  $E_{\rm h}$  in these materials is further enhanced by the dielectric mismatch between organic and inorganic layers.<sup>7-12</sup> Here, the low dielectric constant of the adjacent organic layers provides poor shielding of the electrons and holes in the inorganic layers leading to the exciton's dielectric confinement. The  $E_b$  values for n = 1perovskites are typically above 300 meV,<sup>13</sup> comparable to those of certain organic molecules.<sup>14</sup> These tightly bound excitons in 2D perovskites have enabled varied applications in luminescence. The high oscillator strength of the excitons affords strong excitonic luminescence, which has been used in green phosphor<sup>15</sup> and light-emitting-diode<sup>16</sup> applications, and we proposed that white-light emission from 2D perovskites stems from strongly bound excitons stabilized (or self-trapped) through lattice distortions.<sup>17, 18</sup> Furthermore, perovskites with  $1 < n < \infty$  values provide access to intermediate  $E_{g}$  and  $E_{h}$ values,<sup>19-21</sup> while the organic layers bring new functionality. For example, the n = 3 2D Pb–I perovskite exhibits sufficiently low  $E_g$  and  $E_b$  values to absorb sunlight and generate photocurrent in a solar cell, while hydrophobic organic layers provide enhanced moisture resistance.<sup>22, 23</sup> Owing to the greater stability and structural diversity of the layered framework compared to the 3D perovskite, we investigated

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how the common n = 1 Pb–I perovskites can be modified to mimic the optoelectronic properties of their 3D congeners.

Herein we demonstrate that post-synthetic intercalation of highly polarizable molecules into 2D Pb–I perovskites can significantly decrease their electronic confinement and optical anisotropy, enabling new functionality in these materials. Using experimental and theoretical methods, we explain the structural, optical, and electronic consequences of intercalating I<sub>2</sub> molecules in the perovskite's organic layers. Furthermore, using in situ powder X-ray diffraction (PXRD) and in situ optical absorption spectroscopy, we monitor the dynamics of halogen intercalation and release. We further extend halogen intercalation to halogen-mediated reactivity to access novel Pb–halide perovskites that cannot be synthesized from solution.

#### **Results and discussion**

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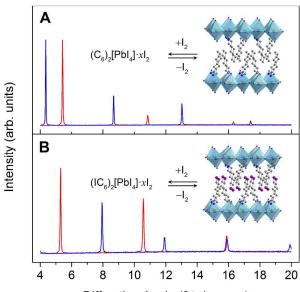
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We recently showed that upon exposure to halogen gas, layered perovskites containing terminal alkynes or alkenes topotactically expand by up to 36% of their original volume to form perovskites containing dihaloalkenes or dihaloalkanes, respectively.<sup>24, 25</sup> During our experiments with I<sub>2</sub> chemisorption, we hypothesized that intercalation precedes halogenation of these nonporous solids. Here, the organic layers may stabilize I2 incorporation similar to halogen solvation in organic liquids. A paraffin-like quality has been previously ascribed to organic layers containing long-chain alkyl groups in hybrid perovskites<sup>26, 27</sup> and binding sites in the organic layers have been shown to stabilize electrochemical ion insertion in these materials.<sup>28</sup> We therefore sought to assess if intercalation of highly polarizable molecules could provide a facile method for tuning the electronic structure of 2D perovskites.

#### 1. Structural effects of iodine intercalation

Weak electrostatic interactions have been previously leveraged to reversibly intercalate nonpolar aliphatic and aromatic hydrocarbons into layered perovskites containing long alkyl chains such as  $(C_{10}H_{21}NH_{3})_2[CdCl_4]$  and



Diffraction Angle (20 degrees)

Figure 1. (A) Powder X-ray diffraction (PXRD) patterns of  $(C_6)_2[Pbl_4]$  (red) and  $(C_6)_2[Pbl_4] \cdot xl_2$  (blue). Inset: X-ray crystal structure of  $(C_6)_2[Pbl_4]$ .<sup>30</sup> (B) PXRD patterns of  $(IC_6)_2[Pbl_4]$  (red) and  $(IC_6)_2[Pbl_4] \cdot xl_2$  (blue). Inset: X-ray crystal structure of  $(IC_6)_2[Pbl_4]$ . Green, purple, blue, and grey spheres represent Pb, I, N, and C atoms, respectively. Disordered atoms and hydrogen atoms are omitted for clarity.

(C<sub>9</sub>H<sub>19</sub>NH<sub>3</sub>)<sub>2</sub>[PbI<sub>4</sub>].<sup>27</sup> Stronger fluoroaryl-aryl interactions have been subsequently used to stabilize and isolate the guestintercalated perovskites  $(C_6H_5(CH_2)_2NH_3)_2[SnI_4]\cdot(C_6F_6)$  and  $(C_6F_5(CH_2)_2NH_3)_2[SnI_4] \cdot (C_6H_6)$ .<sup>29</sup> In order to investigate the consequences of I<sub>2</sub> intercalation in 2D perovskites, we first chose  $(C_6H_{13}NH_3)_2[PbI_4]^{30}$  (hereafter denoted as  $(C_6)_2[PbI_4]$ ) in order to provide a well-defined organic bilayer with some structural flexibility (Figure 1A, inset). Perovskite films were deposited on substrates through spincoating and then thermally annealed. Flowing air over the spinning sample improved film quality (further details are provided in the Supplementary Information). Exposing a  $(C_6)_2[PbI_4]$  film to a dry, inert carrier gas (N<sub>2</sub> or Ar) containing I<sub>2</sub> vapor results in a color change from orange to red and an expansion of the unit cell by ca. 4 Å along the c axis (perpendicular to the inorganic sheets) to yield the perovskite we formulate as

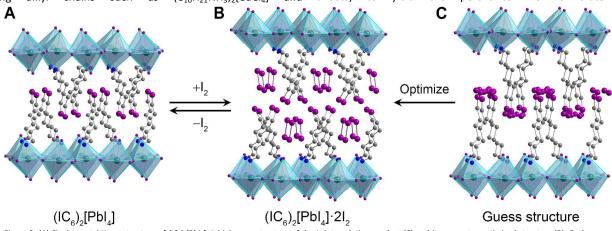


Figure 2. (A) Single-crystal X-ray structure of (IC<sub>6</sub>)<sub>2</sub>[PbI<sub>4</sub>]. Initial guess structure of the I<sub>2</sub> intercalation product (C) and its geometry-optimized structure (B). Dark green, purple, blue, and grey spheres represent Pb, I, N, and C atoms, respectively. Disordered atoms and hydrogen atoms are omitted for clarity.

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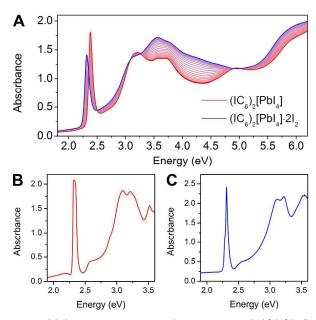
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#### **Chemical Science**

To stabilize the I2-intercalated material, we then focused on the perovskite  $(IC_6H_{12}NH_3)_2[PbI_4]$  (hereafter denoted as (IC<sub>6</sub>)<sub>2</sub>[PbI<sub>4</sub>]) containing terminal alkyl iodides (Figure 1B, inset). The structure of  $(IC_6)_2[PbI_4]$  at 173 K has been reported;<sup>31</sup> however, we collected single-crystal XRD data at 298 K to gain a better match with our room-temperature PXRD patterns. The 298-K crystal structure (Figure 2A) shows a partially interdigitated organic layer with I---I distances of 5.017(1) Å between organoiodines that run parallel to the inorganic sheets. Iodine-iodide interactions of 3.955(1) Å are also evident between the organoiodines and terminal iodides of the inorganic sheets. We envisioned that halogen-halogen interactions<sup>32, 33</sup> between the organoiodines and inorganic iodides could stabilize I<sub>2</sub> intercalation in the organic layers. Exposing  $(IC_6)_2[PbI_4]$  thin films to  $I_2$  vapor also results in a color change from orange to red. PXRD data show that I<sub>2</sub> exposure causes the inter-layer spacing in  $(IC_6)_2[PbI_4]$  to increase by 5.5 Å (33%) (Figure 1B). Indeed, the iodine retention time is increased more than four-fold in  $(IC_6)_2[PbI_4] \cdot xI_2$  compared to  $(C_6)_2[PbI_4] \cdot xI_2$ . Because films of  $(C_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4]$  are similar in both quality and thickness (250  $\pm$  20 nm), we attribute the difference in  $I_2$  retention to stabilization of  $I_2$ molecules by the iodoalkyl groups in  $(IC_6)_2[PbI_4]$ .

To elucidate the structure of  $(IC_6)_2[PbI_4] \cdot xI_2$ , we performed structural optimization at the DFT level in two steps. First, we used the local density approximation (LDA) for both  $(IC_6)_2[PbI_4]$ and  $(IC_6)_2[PbI_4] \cdot xI_2$ . Then, we re-optimized the LDA-optimized structure using the generalized gradient approximation (GGA) corrected to take into account van der Waals (vdW) interactions (hereafter GGA+vdW; see Supplementary Information and Table S2 for details). The alkyl chain of the  $IC_6^+$  cation in  $(IC_6)_2[PbI_4]$  is disordered across two positions. For the calculations we used only the atomic positions of the major disorder component. This final geometry-optimized structure of  $(IC_6)_2[PbI_4]$  is consistent with the roomtemperature single-crystal XRD structure, with differences ranging from ca. 1.5% to 3.8% for the *a* and *b* lattice parameters, respectively (Table S2). Note that our structure optimizations do not include temperature effects. In layered hybrid perovskites, the evolution of unit-cell parameters with temperature is not necessarily systematic because of the rotational flexibility of the metal-halide octahedra.

In order to simulate the  $I_2$ -intercalated perovskite structure, we expanded the inter-layer spacing by the experimentally observed 5.5 Å. We then positioned two intercalated  $I_2$  molecules per formula unit with their internuclear axes aligned parallel to the inorganic sheets to simulate their possible configuration as the molecules enter the perovskite (Figure 2C). During geometry optimization, no constraints were placed upon the added iodine atoms, which were allowed to move freely and independently. Upon reaching an optimized configuration at the LDA level of theory, we continued the optimization at the GGA+vdW level of



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Figure 3. (A) Change in room-temperature absorption spectra as  $(IC_6)_2[PbI_4]$  (red) absorbs  $I_2$  to form  $(IC_6)_2[PbI_4]\cdot 2I_2$  (blue). Absorbance spectra collected at 5 K for  $(IC_6)_2[PbI_4]$  (B) and  $(IC_6)_2[PbI_4]\cdot 2I_2$  (C).

theory. We find that the iodine atoms arrange as I<sub>2</sub> molecules with their inter-nuclear axes nearly perpendicular to the inorganic sheets (Figure 2B). The I<sub>2</sub> molecules are flanked on either side by halogen-halogen interactions from both inorganic iodides (in the inorganic layer) as well as organoiodines (in the organic layer) with short I---I distances of 3.32–3.33 Å (Table S2). The computed c lattice parameter (double the inter-layer spacing) for  $(IC_6)_2[PbI_4] \cdot 2I_2$  compares well with that obtained from PXRD, with a difference of ca. 1% (Table S2) of the experimental value determined at room temperature. We therefore assign the I2-intercalated perovskite as  $(IC_6)_2[PbI_4] \cdot 2I_2$ . Interestingly, the  $I_2 \cdots I^-$  fragment in  $(IC_6)_2[PbI_4] \cdot 2I_2$  exhibits a similar geometry to the triiodide anion found in  $Csl_3$ <sup>34</sup> indicating that the inorganic lattice may now be thought to contain axial triiodides bound to the Pb<sup>2+</sup> centers to give the perovskite  $(IC_6)_2[PbI_2(I_3)_2]$ . Therefore, we post-synthetically access a lead-iodide-triiodide perovskite, which is structurally related to the mixed-ligand 2D perovskites  $(H_3N(CH_2)_8NH_3)_2[(Au^{I}I_2)(Au^{III}I_4)(I_3)_2]^{35}$ and  $(CH_3NH_3)_2[PbI_2(SCN)_2]^{36}$ and the 1D structure  $(H_3N(CH_2)_2SS(CH_2)_2NH_3)_4[Pb_3I_{14}] \cdot I_2^{37}$  that contains  $I_2$  molecules interacting with the lead-iodide chains.

#### 2. Optical and electronic effects of iodine intercalation

The 2D Pb–I perovskites are medium-bandgap semiconductors with significant absorption in the visible range. The 298-K absorption spectrum of  $(IC_6)_2[PbI_4]$  shows an excitonic absorption at 2.38 eV (521 nm), similar to other layered Pb–I perovskites (Figure 3A).<sup>38</sup> Iodine intercalation causes a redshift of this absorption band by 60 meV to 2.32 eV (535 nm), as well as an increase in absorption between 3 and 5 eV. Furthermore, the intensity ratio between the excitonic absorption peak and the above bandgap (continuum) absorption is reduced upon  $I_2$  intercalation. The high oscillator strength and temperature-

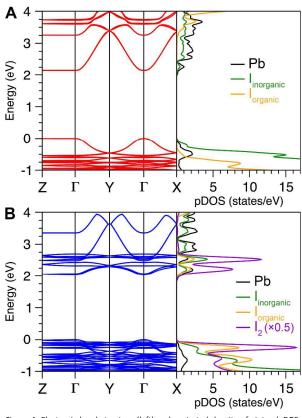


Figure 4. Electronic band structure (left) and projected density of states (pDOS, right) for (A)  $(IC_6)_2[PbI_4]$  and (B)  $(IC_6)_2[PbI_4] \cdot 2I_2$ . The  $I_2$  pDOS was halved to bring into scale.

induced broadening of the excitonic absorbance in lead-halide perovskites<sup>13, 38</sup> obscure the bandgap onset at room temperature. However, at 5 K we were able to resolve the bandgap in both  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$  as linear steplike absorption features (Figures 3B, 3C and S2) characteristic of a 2D material.<sup>39</sup> We estimate  $E_g$  for  $(IC_6)_2[PbI_4]$  to be ca. 2.56 eV. lodine intercalation redshifts the  $E_g$  to ca. 2.49 eV in  $(IC_6)_2[PbI_4]\cdot 2I_2$ , a decrease of ca. 70 meV. Importantly, the perovskite's  $E_{\rm b}$  substantially decreases upon I<sub>2</sub> intercalation. Using the difference between the bandgap and the exciton peak energy in the 5-K absorption spectra, we estimate that  $E_{\rm b}$ for  $(IC_6)_2[PbI_4]$  is ca. 230 meV, which is significantly lower than typical perovskites likely owing to the polarizability of the organoiodines. This  $E_b$  value further drops in  $(IC_6)_2[PbI_4] \cdot 2I_2$  to only 180 meV (a decrease of 50 meV). To our knowledge, this is the lowest  $E_{\rm b}$  value reported for an n = 1 Pb–I perovskite. Most 2D lead-iodide perovskites have  $E_{\rm b}$  values higher than 300 meV.<sup>7</sup> The perovskite  $(C_6H_5(CH_2)_2NH_3)_2[PbI_4]$  has been reported to have a notably low  $E_{\rm b}$  of 220 meV, attributed to the polarizability of the aromatic organic cations.<sup>21</sup>

Small-molecule intercalation can cause both structural and electronic changes in perovskites. As the inorganic sheets are pushed apart to accommodate the intercalants, small distortions in the metal-halide sheets can slightly alter  $E_g$ .<sup>40</sup> However, this effect alone cannot explain the significant reduction in both  $E_b$  and  $E_g$  we observe upon I<sub>2</sub> intercalation. In fact, the computed crystal structure reveals a sizeable increase

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of in-plane octahedral rotations (Table S2) that should lead to an increase in  $E_{g}$ ,<sup>41-43</sup> in contradiction with our experimental findings. Therefore, intercalation-induced electronic effects should play the dominant role in the observed changes in the perovskite.

Two cooperative electronic effects greatly modify the  $E_{\rm b}$  of 2D perovskites relative to the 3D analogues: i) quantum and ii) dielectric confinement.<sup>13, 38</sup> i) Quantum confinement arises from the 2D structure of the lead-halide layers, causing greatly reduced band dispersion perpendicular to the inorganic sheets.<sup>38, 39</sup> In the ideal limit of a single n = 1 lead-halide layer confined by potential barriers of infinite height, purely 2D quantum confinement enhances  $E_{\rm b}$  by a factor of four compared to the analogous 3D perovskite.<sup>39, 44</sup> Therefore, to parse the contribution of quantum confinement to the 2D perovskite's E<sub>b</sub>, we first considered a hypothetical 3D perovskite with the same dielectric constant and exciton reduced mass as the 2D perovskite. Here, the 3D material's  $E_{\rm b}$ can be calculated as the Rydberg energy in the hydrogenic Bohr model modified by the dielectric constant of the inorganic layers (measured at the middle of an inorganic sheet in the 2D perovskite, close to the Pb atoms) and exciton reduced mass (details in the Supplementary Information). Using our computed values of the 3D Rydberg energies of the excitons  $E_{b,3D}$ , and calculating  $E_{b,2D} = 4E_{b,3D}$  gives values of 204 and 142 meV for  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$ , respectively. These values are lower than the corresponding experimental values (230 and 180 meV, respectively), indicating significant additional contributions from the exciton's dielectric confinement to its  $E_{\rm h}$ . ii) Dielectric confinement<sup>11</sup> is a result of the dielectric mismatch between the inorganic (high dielectric constant)<sup>5, 45</sup> and organic (low dielectric constant)<sup>38</sup> layers. Here, the high-frequency dielectric constant  $(\varepsilon_{\infty})$  is an appropriate descriptor of the charge-screening ability of the layers, owing to the small exciton Bohr radius and faster timescales of electronic polarization compared to lattice vibrations.<sup>5, 46</sup> The organic layer poorly screens the electric field between the electron and hole in the inorganic laver. thereby further enhancing  $E_{\rm b}$  over the conventional limit of a 2D quantum well.9, 13

We reasoned that  $I_2$  intercalation could lessen the quantum confinement (the  $I_2$  molecules that orient perpendicular to the sheets could reduce its 2D nature), reduce the dielectric confinement (by increasing the polarizability of the organic layers), or both. To parse out these contributions to the exciton's confinement we turned to electronic-structure calculations.

#### **Electronic structure**

Starting from the geometry-optimized structures for  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4]\cdot 2I_2$  (optimized at the GGA+vdW level of theory), we investigated the electronic consequences of  $I_2$  intercalation. Since this level of theory cannot accurately calculate semiconductor bandgaps, we used the Heyd, Scuseria, and Ernzerhof (HSE) hybrid functional.<sup>47-49</sup> This functional is known to improve accuracy without reaching the

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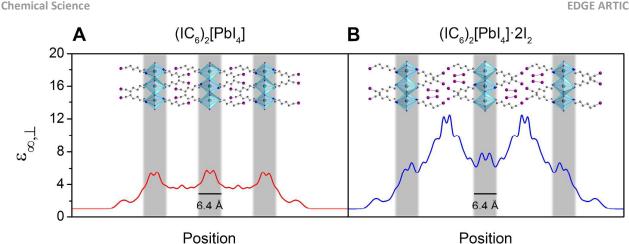


Figure 5. Slabs of  $(IC_6)_2[PbI_4]$  (A) and  $(IC_6)_2[PbI_4]\cdot 2I_2$  (B) and their corresponding calculated high-frequency dielectric profiles  $\varepsilon_{\infty,\perp}$ . Here,  $\varepsilon_{\infty,\perp}$  is the high-frequency dielectric constant perpendicular to the direction of layer propagation. Green, purple, blue, and grey spheres represent Pb, I, N, and C atoms, respectively. Hydrogen atoms omitted for clarity.

performance of GW calculations that remain computationally unaffordable for this type of large, low-symmetry system. We also included spin-orbit coupling (SOC), which is essential for correctly evaluating the band structures of lead-halide perovskites (Table S3 and Figure S3).<sup>12</sup> The HSE+SOC band structure of  $(IC_6)_2[PbI_4]$  (Figure 4A) shows a direct bandgap at the Brillouin zone center with an  $E_g$  of 2.15 eV. Consistent with prior reports, hybridization of the I 5p and Pb 6s orbitals leads to a large in-plane dispersion of the valence-band (VB) maximum, while the Pb 6p orbitals provide for the in-plane dispersion of the conduction-band (CB) minimum.<sup>12, 50</sup> The negligible band dispersion along the  $\Gamma$ -Z direction indicates the 2D nature of the electronic structure responsible for quantum confinement. A similar VB and CB composition is found for  $(IC_6)_2[PbI_4] \cdot 2I_2$  (Figure 4B) with a direct bandgap at  $\Gamma$ . The calculated  $E_{g}$  decreases by 110 meV upon  $I_{2}$  intercalation. Including self-energy corrections that account for interactions of charge carriers with the potential of the surrounding medium (including dielectric effects), the calculated decrease in Eg upon intercalation is 230 meV (details in the Supplementary Information). In contrast to the band structure of  $(IC_6)_2[PbI_4]$ , a set of narrow bands appear close to the Fermi level for the I2-intercalated perovskite. From the projected density of states (pDOS), we see that these originate from the guest I<sub>2</sub> molecules (Figure 4). The highest-energy valence bands stemming from the inorganic sheets lie about 200 meV below the Fermi level. Solid  $(IC_6)_2[PbI_4] \cdot 2I_2$  can be regarded as a weakly coupled composite system with limited interaction between the narrow bands arising from the intercalated I<sub>2</sub> molecules and the original energy levels of (IC<sub>6</sub>)<sub>2</sub>[PbI<sub>4</sub>]. The bands derived from the intercalated  $I_2$  molecules decrease the dispersion of the original CB minimum by ca. 30%, although the dispersion of the original VB maximum is mostly unaffected.

#### **Reduced optical anisotropy**

We computed the frequency-dependent dielectric matrix elements in order to calculate the perovskites' absorption

spectra. Figure S4 shows absorbance spectra calculated for  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$ . Absorption of light propagating perpendicular to the inorganic sheets (given by the imaginary component of the frequency-dependent dielectric constant parallel to the inorganic sheets  $\varepsilon_{\parallel}^{\prime\prime}$ ) remains nearly unaffected by the presence of I<sub>2</sub>. However, absorption of light propagating parallel to the inorganic sheets (given by the imaginary component of the frequency-dependent dielectric constant perpendicular to the inorganic sheets  $\varepsilon_{\perp}^{\prime\prime}$ ) is dramatically altered upon I<sub>2</sub> insertion. Pristine (IC<sub>6</sub>)<sub>2</sub>[PbI<sub>4</sub>] shows a strongly anisotropic optical response with minimal absorbance of lowenergy light incident parallel to the inorganic sheets, which is characteristic of 2D materials with no electronic communication between layers.<sup>12</sup> Upon I<sub>2</sub> intercalation, we see a large decrease in this anisotropy. This likely causes the new above-gap absorption features we observe upon  $I_2$ intercalation in the experimental spectrum of  $(IC_6)_2[PbI_4]$ (Figure 3A). Therefore, although the perovskite retains the 2D nature of its electronic structure near the band edges (Figure 4B), I<sub>2</sub> intercalation produces new electronic transitions making it a more isotropic light absorber.

#### **Reduced dielectric confinement**

We then computed the real component of the materials' frequency-dependent dielectric constant  $\varepsilon'$  (Figure S5). Here also, only small changes occur in the plane parallel to the inorganic sheets ( $\varepsilon'_{\parallel}$ ) upon I<sub>2</sub> intercalation whereas the dielectric response in the direction perpendicular to the inorganic sheets ( $\varepsilon'_{\perp}$ ) is strongly modulated. Therefore, not only is the  $\varepsilon'$  of (IC<sub>6</sub>)<sub>2</sub>[PbI<sub>4</sub>]·2I<sub>2</sub> increased compared to that of (IC<sub>6</sub>)<sub>2</sub>[PbI<sub>4</sub>] but it also shows significant anisotropy with a higher perpendicular component ( $\varepsilon'_{\perp}$ ) than a parallel component ( $\varepsilon'_{\parallel}$ ). This is also likely a result of the orientation of the I<sub>2</sub> molecules, which provide polarizable electron density perpendicular to the inorganic sheets.

The bulk high-frequency dielectric response  $(\varepsilon_\infty)$  corresponds to an average response over all layers of the perovskite and is not suited to describe the difference in

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dielectric constant between the organic and the inorganic layers. We therefore used a method designed to compute  $\varepsilon_\infty$ profiles for nanoscale slabs and composite systems<sup>10, 51</sup> to estimate the respective contributions from the organic and inorganic layers to the bulk  $\varepsilon_\infty$  value. Profiles of the highfrequency dielectric constant perpendicular to the layers ( $\varepsilon_{\infty,\perp}$ ) in  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$  are shown in Figure 5. The behavior of  $\epsilon_{\infty,\perp}$  changes substantially when  $\mathsf{I}_2$  molecules intercalate. The average  $\varepsilon_{\infty, \perp}$  dielectric profile stemming from the inorganic layers increases from 5.4 to 7.0 when including  $I_2.$  For the  $\epsilon_{\varpi, \perp}$  dielectric profile associated with the organic layers, we see a dramatic three-fold increase from 3.7 to 11.1 upon I<sub>2</sub> intercalation. Therefore, I<sub>2</sub> intercalation significantly decreases the dielectric confinement of excitons in the inorganic layers by better screening electric field lines in the organic layer.

Layered perovskites have been considered as quantumwell-like structures where the more polarizable (higher dielectric constant) inorganic sheets form the "wells" and the less polarizable organic layers (low dielectric constant) form the "barriers".<sup>8, 38</sup> Notably, I<sub>2</sub> intercalation completely inverts this dielectric profile to yield the first example of a 2D perovskite containing organic layers with a higher dielectric constant than the inorganic layers. The exciton's dielectric confinement is thus substantially reduced, though not completely eliminated because the exciton is likely screened only by the immediately adjacent portion of the organic layer.

#### Synergistic effects of intercalation

An accurate determination of  $E_{\rm b}$  in a single quantum well with finite barriers or in a composite layered heterostructure can be calculated by including dielectric effects in the resolution of the Bethe-Salpeter equation (BSE) for the exciton to account for the abrupt interfaces between organic and inorganic components.<sup>52, 53</sup> Taking advantage of our ab initio determination of the perovskites' nanoscale dielectric profiles<sup>10, 51</sup> (Figure 5), we refined this abrupt dielectricinterface approximation of the BSE for the first time to estimate the electron-hole Coulombic interaction without experimental inputs, while simultaneously avoiding an unphysical divergence of the self-energy.<sup>54</sup> This semi-empirical method (details in the Supplementary Information) allows us to simulate the absorption spectra of large composite systems, in principle without experimental inputs, using the bandgaps and effective masses computed at the ab initio level. Here, we used the  $E_{a}$  values calculated at the HSE+SOC level of theory for  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$  including the self-energy corrections obtained from the computed dielectric profiles (Figure S6; details in the Supplementary Information). We also take into account the increase of the exciton's reduced mass upon  $I_2$  intercalation (from 0.11 to 0.13) predicted from the computed electronic band structures.

The resulting  $E_b$  values for  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$  are 288 and 171 meV, respectively. These numbers compare well with the experimental  $E_b$  values of 230 and 180 meV for  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$ , respectively (determined using



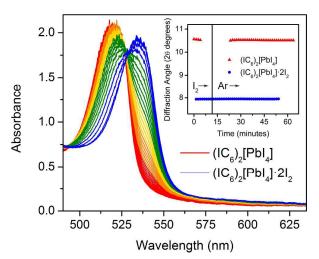


Figure 6. In situ optical absorbance spectra acquired as  $(IC_6)_2[PbI_4]$ - $2I_2$  (blue) desorbs  $I_2$  to yield  $(IC_6)_2[PbI_4]$  (red). Inset: Position of the (004) reflection in the powder X-ray diffraction pattern as  $(IC_6)_2[PbI_4]$  absorbs and then desorbs  $I_2$  vapor.

the exciton peak positions and bandgaps from the 5-K absorption spectra in Figures 3B and 3C). Similar to our experimental absorption spectrum, the calculated spectrum for  $(IC_6)_2[PbI_4]\cdot 2I_2$  (Figure S7) also shows a reduction in the ratio between the excitonic absorption peak and the above bandgap continuum compared to that of  $(IC_6)_2[PbI_4]$ , which is a good indicator of decreased dielectric confinement upon  $I_2$  intercalation (Figures 3 and 5).<sup>55</sup> The difference between the exciton peak positions in the computed absorption spectra for  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4]\cdot 2I_2$  relative to experiment result from the difference between experimental and computed  $E_g$  and  $E_b$  values.

The experimentally observed reduction in the exciton's confinement upon I<sub>2</sub> intercalation is therefore well supported by theory. Our calculations further indicate that the dominant contribution to this effect is the decrease in the exciton's dielectric confinement upon inclusion of the polarizable I<sub>2</sub> molecules in the organic layers, which results in an inversion of the pseudo-quantum-well dielectric profile. The intercalating I<sub>2</sub> molecules extend perpendicular to the inorganic sheets and further mitigate the 2D nature of the material's optical properties leading to more isotropic light absorption.

#### 3. Dynamics of halogen intercalation

The foregoing calculations assumed that we experimentally accessed a single product through  $I_2$  intercalation:  $(IC_6)_2[PbI_4]\cdot 2I_2$ , with no intermediate species with varying  $I_2$  content. To test this assumption, we studied the dynamics of  $I_2$  intercalation. Because reaction with  $I_2$  vapor occurs in seconds, we designed in situ PXRD and electronic absorption spectroscopy cells for use with halogen gas to track potential reaction intermediates (see Supplementary Information for details and Figure S8).

We first studied the reaction between the alkyl perovskite  $(C_6)_2$ [PbI<sub>4</sub>] and I<sub>2</sub>. Here, we see evidence for reaction intermediates in both PXRD and optical absorption spectroscopy (see Supplementary Information for details). The

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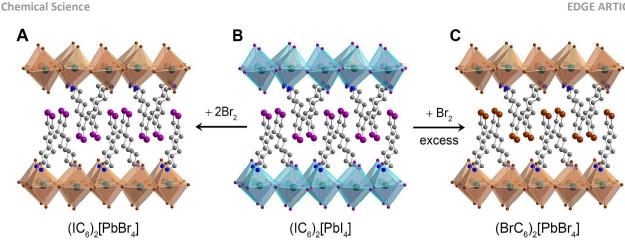


Figure 7. Schematic of products obtained through reaction of (IC<sub>6</sub>)<sub>2</sub>[Pbl<sub>4</sub>] (B) with a stoichiometric amount of Br<sub>2</sub> (A) and with excess Br<sub>2</sub> (C). Turquoise and brown polyhedra represent Pb–I and Pb–Br octahedra, respectively. Dark green, purple, brown, blue, and grey spheres represent Pb, I, Br, N, and C atoms, respectively. Hydrogen atoms omitted for clarity.

excitonic absorption band continuously redshifts upon I2 intercalation and it continuously blueshifts upon I<sub>2</sub> release, indicating an evolving structure (Figures S9 and S10). In contrast, we did not observe any crystalline intermediates in the PXRD patterns during I<sub>2</sub> absorption or desorption from the iodoalkyl perovskite  $(IC_6)_2[PbI_4] \cdot 2I_2$  (Figure 6, inset). The absence of intermediates is further supported by optical absorption spectroscopy. When we plot the exciton's spectral progression during I2 intercalation and deintercalation for  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$ , respectively, we do not observe a continuous shift of the excitonic absorption energy (Figures 6 and S11). Instead, at intermediate scan times, the excitonic absorbance contains only contributions from the excitonic bands of  $(IC_6)_2[PbI_4]$  and  $(IC_6)_2[PbI_4] \cdot 2I_2$ . The absence of intermediates in both the PXRD and absorption data suggests that I<sub>2</sub> molecules that enter the perovskite rapidly localize to the binding sites provided by the organoiodines and inorganic iodides. Compared to  $(C_6)_2[PbI_4]$ , the organic layers in  $(IC_6)_2[PbI_4]$  should interact more strongly with the inorganic sheets. Upon  $I_2$  loss from  $(IC_6)_2[PbI_4] \cdot 2I_2$ , the organic layers may more rapidly find their equilibrium positions in  $(IC_6)_2[PbI_4]$ aided by iodine-iodine interactions between the organic and inorganic layers. Such halogen-halogen interactions have been previously invoked as structure-directing agents during the assembly of layered lead-halide perovskites.<sup>41</sup> To further test if I<sub>2</sub> molecules intercalate between the organic bilayers, we synthesized the alkyldiammonium perovskite (H<sub>3</sub>NC<sub>6</sub>H<sub>12</sub>NH<sub>3</sub>)[PbI<sub>4</sub>],<sup>56</sup> which contains an organic monolayer that forms hydrogen bonds at both ends with adjacent inorganic sheets. We did not observe any new phases in the PXRD patterns during I<sub>2</sub> exposure, indicating that an organic bilayer is necessary for I<sub>2</sub> intercalation (Figure S12).

#### 4. Halogen exchange

We finally turned our attention to reactivity that may follow halogen intercalation. As we reported previously,  $Br_2$  exposure converts Pb–I perovskites to Pb–Br perovskites through redox-mediated halogen exchange.<sup>25</sup> To further extend this reactivity, we investigated the reaction product of  $(IC_6)_2[PbI_4]$ 

with Br<sub>2</sub>. In addition to inorganic halide substitution (95% conversion), analysis of the digested product by <sup>1</sup>H NMR shows that the organoiodines have also been converted (90% conversion) to organobromines to yield the new perovskite: (BrC<sub>6</sub>H<sub>12</sub>NH<sub>3</sub>)<sub>2</sub>[PbBr<sub>4</sub>] (Figures 7C, S13 and S17). While atypical, few examples of solution-state halogen-mediated organohalogen substitution reactions are known.<sup>57, 58</sup> To further parse the reactivity of the organic and inorganic components, we then studied the reaction between a 1:2 molar ratio of  $(IC_6)_2[PbI_4]$  and  $Br_2$ . The major product of this reaction (95% yield) was  $(IC_6)_2$ [PbBr<sub>4</sub>] (identified through <sup>1</sup>H NMR, inductively coupled plasma mass spectrometry, and PXRD), where the organoiodines remain unsubstituted (Figures 7A, S14 and S18). This indicates that inorganic halide substitution precedes organohalogen exchange in the organic layer. Notably, we could not form this perovskite through solution-state reactions. When we combined  $IC_6^+$  salts and PbBr<sub>2</sub> in solution, Br<sup>-</sup> ions partially displaced the organoiodines to form organobromines (Figure S16).

#### Conclusions

We demonstrate that small molecules can be stabilized in binding pockets designed into 2D perovskites. Notably, placing highly polarizable molecules in the organic layers can cause large changes in the electronic and optical properties of the inorganic sheets. Here we show that I<sub>2</sub> intercalation results in more polarizable organic layers compared to the inorganic lavers. which considerably decreases the dielectric confinement of excitons generated in the inorganic layers. Control over the exciton binding energy in 2D perovskites can enable their application in a broad range of optoelectronic technologies. Although the I<sub>2</sub> intercalated perovskite studied here is metastable, our studies show that incorporation of polarizable functionalities through intercalation or covalent attachment in the organic layers is a viable approach for substantially decreasing the electronic confinement of these layered materials.

We further extend halogen intercalation to halogenmediated reactivity where our studies show that inorganic halide exchange precedes organohalogen exchange. This gassolid reaction allows us to synthesize perovskites that cannot be formed through traditional solution-state routes.

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