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Behavior modelling and microstructural evolutions of Ti-6Al-4V alloy under hot forming conditions

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Abstract

Ti-6Al-4V alloy is widely used in superplastic forming process. The conventional conditions require high forming temperatures $(T \ge 900^{\circ}C)$ and low strain rates $(\dot{\varepsilon} \le 10^{-3}s^{-1})$. In order to reduce the costs of the industrial process, recent investigations focus on the micro-structural refinement of the material. It allows an improvement of the forming conditions which makes lower forming temperatures and higher strain rates eligible whereas low strain rates ($\dot{\varepsilon} \leq 10^{-3} s^{-1}$) and high temperatures $(T \ge 800^{\circ}C)$ are particularly suitable for conventional superplastic forming conditions. However, the mechanical response of the Titanium alloy strongly depends on the starting micro-structure considered and on its evolution with the temperature and the deformation. The objective of the present investigation is to observe the micro-structural evolutions of Ti-6Al-4V alloy under thermal and mechanical loadings from different starting micro-structures. Hence, an internal grain growth variable is identified by the use of these observations. Then, it is introduced into the behavior model and its influence on the mechanical response of the material is analysed. The final constitutive equations are able to take into account viscosity, strain hardening and grain size evolution for a wide range of strain rates and forming temperatures $(10^{-4}s^{-1} \le \dot{\varepsilon} \le 10^{-2}s^{-1}; 650^{\circ}C \le T \le 870^{\circ}C).$ Moreover, the model is able to consider several starting microstructures (different initial grain sizes) and to predict their influence on the viscous flow and the strain hardening. At last, some model verifications are conducted to check the validity of the non-isothermal model formulation. Some predictions are also performed by considering several starting microstructures.

Keywords: Behavior modelling, Micro-structural evolutions, Viscoplastic material, Mechanical testing, Hot and superplastic forming conditions, Ti-6Al-4V alloy

1. Introduction

Ti-6Al-4V alloy is one of the most popular Titanium alloy, it is commonly used in superplastic forming process due to its high strength combined with an important ductility [1]. It exhibits a

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very large amount of starting microstructures regarding different heat treatments and processing

practises. It can result lamellar, equi-axed or bi-modal microstructures. Moreover, combined heat treatments and mechanical processes also allow a grain refinement of the microstructure which is a well known method for enhancing the superplastic properties of Titanium alloys [2, 3]. Thus, lower temperature and higher strain rate conditions become eligible for superplastic deformation[4, 5, 6, 7]. These test conditions strongly influence the mechanical behavior of the material. And each particular starting microstructure may induce complex mechanisms as grain growth [8, 9, 10], 10 dynamic recrystallization [11, 12, 13], cavity and void nucleation [14, 15, 16] in addition with grain boundary sliding [17], each mechanism respectively suggesting hardening, softening or damage.

The present work intends to analyse the thermo-mechanical behavior of Ti-6Al-4V alloy under hot forming conditions (650° $C \leq T \leq 870°C$ and $10^{-4}s^{-1} \leq \dot{\varepsilon} \leq 10^{-2}s^{-1}$). It considers two different equi-axed starting microstructures with initial average α grain sizes of 0.5 μm and 3 μm . 15 Previous investigations show that void nucleation is not responsible for the necking phenomenon. Moreover, dynamic recrystallization can be assumed negligible whereas, in contrast, grain boundary sliding and grain growth have a preponderant role on the occurring flow stress and hardening [18, 19]. From these observations, constitutive equations are identified in order to consider the influence of the starting microstructure and its evolution on the mechanical behaviour of Ti-6Al-4V alloy. The grain growth effect is taken into account through the evolution laws of the literature [15, 20]. But, the law parameters have been identified for the temperature range investigated in the present study. Moreover, the results provided have been successfully compared with experimental observations. A part of them comes from the present work, another part is provided by the work

- of Semiatin [2, 21, 22] where the established law was extrapolated to our temperature and strain 25 rate conditions. Hence, the grain growth evolution equations are introduced into the mechanical constitutive equations. The influence of the starting microstructure and its evolution is considered through a modification of the viscosity parameters of the model dependent on the initial grain size and on the grain growth. Moreover, a hardening variable depending on the grain size range is
- introduced and permits an accurate assessment of the stress increase. Afterwards, this approach is formulated under non isothermal conditions and a validation stage is performed at an intermediate test temperature and for different starting microstructures. Some model predictions are then possible in a range of grain sizes, temperature and strain rate conditions where any additional phenomenon occurs. At the end, the stability of the constitutive equations are analysed under uni-axial conditions by predicting the reduction rate of the cross-sectional area of a specimen.
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2. Material and Methods

Materials. Typical chemical composition for Ti-6Al-4V titanium alloy investigated in the present work is referred to table 1. Two different starting microstructures are considered, both of them consist of equiaxed α grains. They are produced using a combined forging-rolling process providing



Figure 1: SEM image (a) and EBSD-grain boundary (b) of the starting microstructure with a grain size of $3\mu m$

- ⁴⁰ plates with a thickness between 1.4 mm and 3 mm and an Ultra Fine grain (UFG) microstructure with a mean α grain size of 0.5 μm [18] and a Fine Grain microstructure (FG) with a mean α grain size of 3 μm [23] respectively. Priorly, the first type of microstructure was solution treated at 1125°C for 3.6ks, quenched in ice water to get an acicular α' martensite microstructure and then hot-rolled to obtain a final UFG microstructure consisting of equiaxed α grains. The second type
 ⁴⁵ of micro-structure consists in α grain phase with small amounts of intergranular β phase (< 10%).
- Fig. 1 shows a SEM (a) and a EBSD-grain boundary (b) images of the starting microstructure with an initial grain size of $3\mu m$.

| Al | V | Ο | Ν | Ti |
|------|------|------|-------|------|
| 6.50 | 4.24 | 0.17 | 0.004 | Bal. |

Table 1: General chemical composition wt.%.

Microstructural Evolutions. Microstructures are identified by conducting Electron Back-Scatter Diffraction (EBSD) analysis and Scanning Electron Microscopy (SEM) observations [24]. It allows

- the analysis of each starting microstructure but also its evolution with the temperature and the deformation. Indeed, in hot forming and superplastic forming processes, the control of grain growth is important and the grain size dynamically affects the viscoplastic flow of the material [25, 26], it can also acts on the hardening as discussed in the sequel. Thus, grain growth is investigated by conducting static and dynamic tests. The static tests consider different temperature exposure
- time regarding to the forming time during the process. In this case, no mechanical deformation is considered. The dynamic tests are based on high temperature tensile tests ($650^{\circ}C \leq T \leq 870^{\circ}C$) and consider different deformation conditions corresponding to several strain rates between $10^{-4}s^{-1}$ and $10^{-2}s^{-1}$. Fig. 2 and Fig 3 concern the starting microstructure with an initial α grain size of



Figure 2: Grain growth evolution observed by SEM micrographs (BSE mode) in the case of the static tests at $T = 840^{\circ}C$ and several temperature exposure times t = 1000s (a), t = 5000s (b), t = 10000s (c) and t = 30000s (d).

 $3\mu m$. Fig. 2 illustrates the grain growth evolution for the static tests at $T = 840^{\circ}C$ and several temperature exposure times (t = 1000s (a), t = 5000s (b), t = 10000s (c) and t = 30000s (d)), whereas Fig. 3 shows the grain growth evolution in the case of the dynamic tests at $T = 870^{\circ}C$ and several strain rates ($\dot{\varepsilon} = 10^{-2}s^{-1}$ (a), $\dot{\varepsilon} = 10^{-3}s^{-1}$ (b) and $\dot{\varepsilon} = 10^{-4}s^{-1}$ (c)).

The results are compared with the works of Semiatin [21, 22, 27] regarding a Ti-6Al-4V titanium alloy with an initial grain size of 2.5 μm . In this study, several tests and observations allow to determine dynamic ($K = K_d$, for a strain rate of $10^{-4}s^{-1}$ and $10^{-3}s^{-1}$) and static ($K = K_s$) coarsening rate constants at 775°C and 815°C using the equation 1.

$$r^3 = r_0^3 + Kt (1)$$

where r and r_0 denoted the current and the initial average α grain radii respectively.

In the present work, this evolution law is slightly modified to consider not the radius but the diameter of the grain. Then, it is extended to the temperature range $650 - 870^{\circ}C$ by defining the evolution of the coarsening rate constants $\{K_s, K_{d10^{-4}s^{-1}}, K_{d10^3s^{-1}}\}$ versus temperature as an



Figure 3: Grain growth evolution observed by SEM micrographs (SE mode) in the case of the dynamic tests at $T = 870^{\circ}C$ and several strain rates $\dot{\varepsilon} = 10^{-2}s^{-1}$ (a), $\dot{\varepsilon} = 10^{-3}s^{-1}$ (b) and $\dot{\varepsilon} = 10^{-4}s^{-1}$ (c).



Figure 4: Identification of the coarsening rate constants based on the values provided by Semiatin et al at $775^{\circ}C$ and $815^{\circ}C$ and $\dot{\varepsilon} = \{0, 10^{-4}, 10^{-3}\}s^{-1}$ (a); Simulated grain growth obtained with the identified values versus time



Figure 5: Tensile tests conducted under small deformation conditions at several temperatures and a strain rate of $10^{-2}s^{-1}$ (a); at $650^{\circ}C$ and a strain rate of $10^{-3}s^{-1}$ (b)

exponential form (see Fig. 4a). Hence, grain growth can be simulated for different temperatures, different initial grain sizes and for strain rates of $\dot{\varepsilon} = \{0, 10^{-4}, 10^{-3}\}s^{-1}$ as illustrated in Fig. 4(b-d).

High temperature tensile Testing for elastic properties. The elastic properties are assessed using
⁷⁵ tensile test under small deformation conditions (see Fig. 5). In order to obtain accurate values of the Young modulii, an extensioneter is used to calculate the deformation. However, at these temperatures, the small values of the elasticity limits make these measurements difficult. Tab. 2 gives the values provided by the tensile tests.

| $T \{^{\circ}C\}$ | 650 | 730 | 750 | 770 | 800 | 840 | 870 |
|-------------------|-------|-------|-------|-------|-------|-------|-------|
| $E \{MPa\}$ | 70000 | 58000 | 50000 | 42000 | 30000 | 20000 | 15000 |

Table 2: Evolution of the Young modulii with the test temperature

| $T \circ C$ | 650 | 700 | 730 | 750 | 770 | 800 | 840 | 870 |
|--|-----|-----|-----|-----|-----|-----|-----|-----|
| $\dot{\varepsilon} = 10^{-4} s^{-1}$ | ✓ X | ✓ X | X | ✓ X | × | × | × | × |
| $\dot{\varepsilon}=5.10^{-4}s^{-1}$ | × | 1 | × | 1 | | | | × |
| $\dot{\varepsilon} = 10^{-3} s^{-1}$ | ✓ X | ✓ X | X | ✓ X | × | × | × | × |
| $\dot{\varepsilon} = 5.10^{-3} s^{-1}$ | × | 1 | × | 1 | | | | × |
| $\dot{\varepsilon} = 10^{-2} s^{-1}$ | √ X | √ X | × | √ X | × | × | × | × |

Table 3: Tensile test conditions, \checkmark for an initial grain size of $d_0 = 0.5 \mu m$ and \bigstar for $d_0 = 3 \mu m$.

- High temperature tensile Testing for superplastic properties. The mechanical tensile tests were performed using a servo-hydraulic testing machine and a furnace accurate for the very large elongations. It includes three heating zones controlled by S-thermocouples and allows to maintain a constant temperature during all the sample deformation. As the use of a classical extensometer was not possible due to the very large elongation, a non linear crosshead displacement can be considered in order to obtain a constant target strain rate $\dot{\varepsilon}$ at the middle of the specimen [8, 28, 29].
- ⁸⁵ However, it is important to notice that such a strain rate controlled test is only performed on the starting microstructure of 3 μm . Thus, in the case of the initial grain size of 0.5 μm , a constant cross head displacement is considered which induces a slight decrease of the target strain rate with the sample elongation. Regarding the definition of the tensile test conditions, the typical superplastic properties for Ti-6Al-4V alloy are enhanced at a temperature around $870^{\circ}C$ and a strain rate

⁹⁰ between $10^{-4}s^{-1}$ and $10^{-3}s^{-1}$. The fine grain starting microstructure of $3\mu m$ is presently certified in the aircraft industry. Hence, the test conditions are defined to investigate the superplastic capabilities of an ultra fine grain microstructure of $0.5\mu m$ by decreasing the test temperature (forming temperature) and by increasing the strain rate. The test conditions considered for each starting microstructure have been selected to be close or similar in order to compare their strain-stress ⁹⁵ responses. Table 3 summarizes all the tensile test conditions.

Fig. 6 illustrates the strain-stress curves at different temperatures and strain rates. Fig. 6a-b shows the strain rate sensitivity induced at $750^{\circ}C$ for both starting microstructures. As expected, the viscoplastic flow is greatly influenced by the starting microstructure and a decrease of the stress level with the grain size is observed whatever the test temperature. Moreover, Fig. 6a

¹⁰⁰ presents a decrease of the stress level at $\dot{\varepsilon} = \{10^{-2}, 10^{-3}\}s^{-1}$ due to the necking of the specimen whereas the failure does not occur at the lower strain rate ($\dot{\varepsilon} = 10^{-4}s^{-1}$). A slight increase of the stress is observed due to the grain growth effect which initiates flow hardening into the



Figure 6: Strain rate sensitivity observed on experimental strain-stress curves at $750^{\circ}C$ for both starting microstructures $d_0 = 3\mu m$ (a) and $d_0 = 0.5\mu m$ (b); Temperature effect observed on both starting microstructures $d_0 = 3\mu m$ (c) and $d_0 = 0.5\mu m$ (d).

material. Fig.6b shows the same results for the initial grain size of $0.5\mu m$. The decrease of the stress at the higher strain rate is not only due to necking but also to the loading rate which ¹⁰⁵ considers a constant cross head displacement as explained above. At the lower strain rates, flow behavior in steady state region indicates that grain boundary sliding occurs. Then, the pronounced flow hardening observed implies that deformation mode dynamically changes during straining and hardening becomes predominant certainly because of a grain growth effect (dislocation slips govern plastic deformation). Fig.6c-d shows the temperature effect on the mechanical behavior for both starting microstructures at $10^{-4}s^{-1}$. The flow hardening is initiated at the higher temperature for the initial grain size of $3\mu m$, this effect significantly increases for the initial grain size of $0.5\mu m$.

3. Modelling methods

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Grain Growth. The grain growth is defined as an internal variable of the behaviour model. In this section, the grain growth evolution based on the works of Semiatin (see Fig. 4) are used for the coefficient identification of the grain growth evolution law. Moreover, the results obtained are compared with the observations performed in the present study.

The grain size model which accounts for the effect of static and dynamic grain growth is

illustrated by Eq.2 [15, 26].

$$\dot{d} = \dot{d}_s + \dot{d}_d \tag{2}$$

The static grain growth (Eq.3) describes the atomic diffusion process affected by temperature and related to the grain boundary mobility and boundary energy density [30, 31]. 120

$$\dot{d}_s = A_1 d^{-m_1} \tag{3}$$

The dynamic grain growth (Eq. 4) allows to reproduce grain growth kinetics over a range of temperatures and strain rates [32].

$$\dot{d}_d = A_2 \dot{p}^{n_1} d^{-m_2} \tag{4}$$

where A_i , m_i (i = 1, 2) and n_1 are temperature dependent parameters and p is the effective inelastic strain. In the sequel, $m_1 = m_2 = 2$.

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Eq. 2-4 have ever successfully applied on Ti-6Al-4V Titanium alloy at $900^{\circ}C$ and $927^{\circ}C$ [33, 34]. In the present work, Eq.4 is slightly modified by introducing the parameter n_1 in order to better match with the experimental grain growth evolution provided by Semiatin [2, 22] and this study. The identification process of the model parameters was performed into two steps. First, the static and dynamic tests are considered separately (see Eq. 3-4). Second, it considers both equations simultaneously (see Eq.2) using the previous identified set of parameters as initial guess 130 of the optimization problem. The parameters are determined using experimental curves provided by Semiatin law [2, 21, 27]. Fig. 7a-b and Fig. 7c-d give the computed grain growth-time and the computed grain growth-strain curves respectively for each starting microstructure at different temperature levels. These results are compared, on the one hand, to the results provided by the Semiatin law [2] (used to identify the parameters) and, on the other hand, by the grain size 135 measurements performed in the present study. The results obtained are in a very good agreement with experiment. Hence, the differential equations allow to simulate the static and dynamic grain growth for different starting microstructure, different temperature levels and different strain rates. Table 4 gives the parameters of the grain growth evolution with the temperature.

| $T \{^{\circ}C\}$ | 650 | 700 | 730 | 750 | 770 | 800 | 870 |
|---|-------|-------|------|-------|-------|-------|-------|
| $A_1 \times 10^{-13} \{mm^3.s^{-1}\}$ | 1.24 | 2.01 | 2.71 | 3.31 | 4.05 | 5.46 | 10.75 |
| $A_2 \times 10^{-11} \{mm^3.s^{-1+n_1}\}$ | 1.38 | 3.08 | 4.95 | 6.72 | 9.19 | 14.7 | 45 |
| n_1 | 0.331 | 0.356 | 0.37 | 0.379 | 0.388 | 0.402 | 0.48 |

Table 4: Temperature evolution of the identified parameters for the grain growth equations



Figure 7: Comparison of computed grain growth-time (a,b) and computed grain growth-strain (c,d) curves using the evolution law identified with the coarsening rate constants by Semiatin et al and experimental measurements performed in the present work at {650, 700}°C and $d_0 = 3\mu m$ (a,c); at {730, 840}°C and $d_0 = 0.5\mu m$ (b,d)

- Unified Elasto-viscoplastic model. Unified constitutive equations for modelling the multiaxial superplastic and hot forming deformation can be formulated by assuming an energy dissipation potential Ω. This thermodynamic framework has been adopted for many metallic materials [30, 35, 36, 37, 38, 39] under small as well under large deformation conditions[40], including the thermo-mechanical behavior of hot forming tools [41, 42]. The potential can be written as Eq. 5.
 The model formulation has to take into account the following considerations. On the one hand, superplastic forming conditions occur at low stress levels and long time periods inducing high temperature deformation process controlled by diffusion. On the other hand, hot forming conditions
- at higher stress levels and lower temperature coupled with high strain rates can be defined by a predominant dislocation controlled deformation. Thus, an accurate thermo-mechanical behavior ¹⁵⁰ model requires a coupling between the different induced mechanisms (lattice and grain boundary diffusion, grain boundary sliding and dislocation climb)[32].

$$\Omega(f) = \left\langle \frac{f}{K} \right\rangle^n; \ f = \sigma_{eq} - R - \sigma_0 \tag{5}$$

K and n define the viscous parameters able to describe the strain rate sensitivity of the material, $\sigma_{eq} = \sqrt{\frac{3}{2} \mathbf{S} : \mathbf{S}}$ and \mathbf{S} is the deviatoric part of the Cauchy stress $\boldsymbol{\sigma}$. σ_0 is the yield stress and R is an isotropic hardening variable related to the dislocation density in the plastic deformation. This variable is not significant under superplastic deformation mechanisms but can become predominant for the low temperatures or for an important grain growth. Its formulation is given by Eq. 6.

$$R = Q(1 - e^{-bp}) \tag{6}$$

p is the effective strain, Q and b are material parameters. Assuming normality and the associated flow rule, the multiaxial viscoplastic strain rates for materials implemented within a large strain deformation is given by Eq. 7.

$$\boldsymbol{D_p} = \frac{\partial\Omega}{\partial\boldsymbol{\sigma}} = \Omega'(f)\frac{\partial f}{\partial\boldsymbol{\sigma}} = \frac{3}{2}\dot{p}\frac{\boldsymbol{S}}{\sigma_{eq}}$$
(7)

where $\dot{p} = \Omega'(f) = \left\langle \frac{f}{K} \right\rangle^n = \sqrt{\frac{2}{3}D_p : D_p}$. Moreover, the corotational stress rate is given by Hooke's law (see Eq. 8).

$$\stackrel{\nabla}{\boldsymbol{\sigma}} = 2G\boldsymbol{D}_{\boldsymbol{e}} + \lambda Tr(\boldsymbol{D}_{\boldsymbol{e}}) \tag{8}$$

in which $G = \frac{E}{2(1+\nu)}$ is the shear modulus defined by the Young modulus E and the Poisson ratio ν as the lame elasticity constant $\lambda = \frac{E\nu}{(1-2\nu)(1+\nu)}$. D_e is the rate of the elastic deformation which can be expressed as $D_e = D_t - D_p$ with D_t is the rate of the total deformation.

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The deformation gradient F can be defined together with the velocity gradient L and can be decomposed as the rate of the deformation tensor D and the spin tensor W as described in Eq. 9.

$$\boldsymbol{L} = \dot{\boldsymbol{F}}\boldsymbol{F}^{-1} = \boldsymbol{D} + \boldsymbol{W} \tag{9}$$

with $\boldsymbol{D} = \frac{1}{2}(\boldsymbol{L} + \boldsymbol{L}^T)$ and $\boldsymbol{W} = \frac{1}{2}(\boldsymbol{L} - \boldsymbol{L}^T)$.

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Thus, the material stress rate can be expressed from the corotational stress rate, the spin tensor and the Cauchy stress (see Eq. 10).

$$\dot{\boldsymbol{\sigma}} = \overset{\nabla}{\boldsymbol{\sigma}} + \boldsymbol{W}\boldsymbol{\sigma} - \boldsymbol{\sigma}\boldsymbol{W} \tag{10}$$

Introduction of the grain growth effect on the viscosity and the hardening. As mentioned previously, the model formulation aims to take into account the initial grain size and its evolution with the temperature and the deformation. The initial grain size effect is introduced into the model formulation through the viscous parameters K and n as formulated in Eq. 11.

$$K = K_r \left(\frac{d}{\chi(d_0)}\right)^{\frac{\mu}{n}}; \ n = n_r \left(\frac{d}{\chi(d_0)}\right)^{\alpha} \tag{11}$$

where d is the average grain size of the grain growth model given by Eq. 2-4. μ and α are material constants which characterise the continuous material hardening due to grain growth. The ¹⁸⁰ initial grain size is taken into a account by the parameter χ written as a function of the initial grain size d_0 , $\chi(d_0) = \chi_1 e^{-\chi_0 d_0}$, χ_0 and χ_1 are constant parameters. The evolution law translates that the more important the initial grain size will be the more promptly its effect on the viscous flow will vanish. These equations can reproduce the continuous increase of the viscous flow due grain growth, but can not describe the drastic increase of the stress level which operates at low strain rate and a

long time period. In such a case the grain growth induces a change in the deformation mechanisms (dislocation glide) which could be reproduced through a modified isotropic hardening variable as mentioned in Eq.11. Then, the asymptotic value of the hardening variable Q is considered to be dependent on the grain growth variable d.

$$Q = Q_0 e^{\gamma \Delta d} \tag{12}$$

where $\Delta d = d - d_0$, Q_0 and γ are constant parameters. Thus, the hardening will be important for the significant increase of the grain size and reduced for a slight growth.

4. Results and discussion

Identification methodology. The identification of the model parameters is performed into 3 stages.

- The parameters identification of the grain growth model is first performed, the values A_1 , A_2 , n_1 , m_1 and m_2 are determined.
- The parameters identification of the viscous law for each starting microstructure is performed without introducing the grain growth model, different values of K and n are identified for each starting microstructure. Constant values are considered for the parameters Q and b of the isotropic hardening variable.
 - An unique set of parameters is adjusted, it describes the strain-stress response of both microstructures, K_r , n_r , μ , α and $\chi(d_0)$ are determined in this stage.
 - The introduction of the hardening due to the deformation mechanism change is added through the parameters Q_0 , γ and the hardening variable is modified.

The final mechanical parameters set is defined in table 5, these values has to used in conjunction with the results provided in table 4.

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The following parameters are set to be constant, $\mu = 0.004$, b = 0.5, $\chi_0 = 760$ and $\chi_1 = 0.03$.

Fig. 8 illustrates computed strain-stress curves compared to the experimental results at $650^{\circ}C$ and $750^{\circ}C$. Fig. 8a does not show a deformation mechanism change for an initial grain size of $d_0 = 3\mu m$ whereas this effect is observed and well assessed at low strain rate $(10^{-4}s^{-1})$ for an initial grain size of $d_0 = 0.5\mu m$ (Fig. 8b). This phenomenon increases with the temperature. At

| $T \{^{\circ}C\}$ | 650 | 700 | 730 | 750 | 770 | 800 | 870 | |
|-------------------------|-------|-------|-------|------|-------|--------|------|--|
| $\sigma_0 \{MPa\}$ | 10 | 8 | 6 | 5 | 4 | 3 | 0.2 | |
| $K_r \{MPa.s^{1/n_r}\}$ | 1608 | 1750 | 1757 | 1700 | 1457 | 1250 | 1000 | |
| n_r | 3.71 | 2.8 | 2.4 | 2.31 | 2.25 | 2.1 | 1.9 | |
| α | 0.128 | 0.095 | 0.088 | 0.08 | 0.764 | 0.0691 | 0.06 | |
| $Q_0 \{MPa\}$ | 5 | 6.9 | 8.4 | 9.5 | 10.6 | 12.5 | 17.2 | |
| $\gamma \{mm^{-1}\}$ | 850 | 700 | 595 | 530 | 460 | 356 | 140 | |

Table 5: Temperature evolution of the identified parameters for the mechanical behavior model



Figure 8: Computed Strain-Stress datas compared to Experimental results at a temperature of $650^{\circ}C$ and an initial grain size of $d_0 = 3\mu m$ (a) and $d_0 = 0.5\mu m$ (b); at a temperature of $750^{\circ}C$ and a initial grain size of $d_0 = 3\mu m$ (c) and $d_0 = 0.5\mu m$ (d).

²¹⁰ 750°C, a slight increase of the stress level is induced at the lower strain rate and for an initial grain size of $d_0 = 3\mu m$ (Fig. 8c). Last, for the same test temperature, the rapid grain growth for an initial grain size of $d_0 = 0.5\mu m$ implies an increase of the hardening and an acceleration of the deformation mechanism changes at higher strain rate (Fig. 8d at $10^{-3}s^{-1}$). These analyses are confirmed by Fig.9 where the hardening flow increases with the test temperature and it is all the more significant as a small initial grain size is considered. For the case of the starting of 0.5 μm , one can notice that the behavior model predicts a stress decrease under certain conditions (see Fig



Figure 9: Computed Strain-Stress datas compared to Experimental results: (a) at a temperature of $870^{\circ}C$ and an initial grain size of $d_0 = 3\mu m$ and (b) at a temperature of $700^{\circ}C$ and a initial grain size of $d_0 = 0.5\mu m$.

Model verification. The evolutions of each model parameter with the temperature are addressed. Thus, both non isothermal and isothermal loadings at intermediate temperature, but not used in 220 the preliminary experimental database, can easily be simulated.

Table 6 gives the temperature evolution laws for each model parameters. The interpolation function coefficients are given in appendix 1 and their evolutions as well (see Table 7 and Fig. 13-15).

| Parameters | (A_i, n_1, Q_0) | E | σ_0 | K_r | $(n_r, \ \gamma, \ \alpha)$ |
|-----------------|-------------------|---|--------------------------|--|-----------------------------|
| Considered laws | $ae^{b/T}$ | | $\frac{a}{b+e^{c(T-d)}}$ | $\frac{a}{1 + \left(\frac{T-b}{c}\right)^2}$ | $\frac{a}{b+e^{c(T-d)}}+e$ |

Table 6: Temperature evolution laws for each model parameters

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In order to verify the accuracy of the non isothermal model response, tensile tests are conducted at $T = 840^{\circ}C$ for both starting microstructures $(d_0 = \{0.5, 3\}\mu m)$. Computed and experimental strain-stress responses are compared. Fig. 10 shows that the obtained results are in a good agreement. For the case of the starting microstructure of 0.5 μm at $10^{-2}s^{-1}$ (Fig. 10b), the model strain rate sensitivity associated with the non constant applied strain rate with the sample elongation can explain a part of the predicted stress decrease. 230

Fig.11 illustrates the capabilities of the behaviour model in the prediction of the strain-stress response at different temperatures and different starting microstructures.

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Necking prediction. The stability of the previous constitutive equations is analysed under uniaxial loading [20, 31]. In the sequel, A is the cross-sectional area of the sample and P is the force applied. The incompressibility assumption under a superplastic deformation leads to the following expression for the reduction rate of the cross-sectional area (see Eq. 13).

$$\frac{dA}{dt} = -A \left(\frac{P/A - R - \sigma_0}{K}\right)^n \tag{13}$$



Figure 10: Computed Strain-Stress datas compared to Experimental results at a temperature of $840^{\circ}C$ and an initial grain size of $d_0 = 3\mu m$ (a) and $d_0 = 0.5\mu m$ (b)



Figure 11: Model prediction for different test conditions (a) $d_0 = 0.5 \mu m$ and different temperatures; (b) at $T = 750^{\circ}C$ and different starting microstructures

where K and n (see Eq.11) and R though the parameter Q (see Eq. 12) depend on the grain growth d and on the initial grain size d_0 .

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If the yield stress σ_0 , the isotropic hardening R and the grain growth d are omitted, Eq. 13 can be reduced as Eq. 14.

$$\frac{dA}{dt} = -A \left(\frac{P/A}{K_0}\right)^{n_0} \tag{14}$$

where $K_0 = K(d_0)$ and $n = n(d_0)$ are constant values for a fixed grain size d_0 , in this case, these values only depend on the temperature.

An analytical solution can be determined for Eq.14 whereas a numerical method is required 245 to solve the Eq. 13, a Runge-Kutta method is used in the present work. Fig. 12 illustrates the shrinkage rate against the normalised cross-section area. Fig. 12a shows results at $750^{\circ}C$ and an initial grain size of $0.5\mu m$, several initial stresses between 20 MPa and 65 MPa are considered related to several constant loads P. At the lower stress levels, the reduction rate of the cross-section area remains constant. It means that the shrinkage rate is not dependent on the cross section and necking is limited whereas at the higher stress levels, the shrinkage rate greatly increases as the cross-section decreases. It means that necking occurs leading to an elongation to failure [20]. Fig. 12b (resp. Fig. 12c) gives the same observations at several temperatures and an initial grain size of $0.5\mu m$ (resp. $3\mu m$). These figures show the influence of the strain rate parameter n = 1/m on necking where m increases with the temperature. For the initial grain size of $0.5\mu m$, the shrinkage 255 rate remains constant with the cross-section reduction, it means that the local strain concentration is prevented and a large elongation is expected. This phenomenon is observed whatever the test temperature considered between $650^{\circ}C$ and $750^{\circ}C$. On the contrary, for an initial grain size of $3\mu m$, a significant increase of the shrinkage rate is observed. For the same test conditions, an increase of the initial grain size leads to an increase of the n parameter and a partial loss of the 260 superplastic properties. On Fig. 12b-c, the dashed line illustrates the shrinkage rate against the cross-section reduction in the case where the hardening, the yield stress and the grain growth effects are neglected (see Eq. 14). In this case, a more important effect of the strain rate parameter n is observed on the shrinkage rate. Thus, the introduction of the hardening and grain growth effects

improves the superplastic properties and limits the necking [20]. 265



Figure 12: Shrinkage rate predicted against the normalised cross-section area at $750^{\circ}C$, an initial grain size of $3\mu m$ and different stress levels (a); at different temperatures and an initial grain size of $0.5\mu m$ (b); an initial grain of $3\mu m$ (c); the dashed lines represents the curves obtained when hardening, yield stress and grain growth are omitted.

5. Conclusions

The following conclusions can be drawn from this work.

- The superplastic behaviour of Ti-6Al-4V Titanium alloy was investigated under hot forming conditions regarding both different starting microstructures with an average α grain size of 0.5 μm and 3 μm . A temperature range $650^{\circ}C \leq T \leq 870^{\circ}C$ and strain rates between
 - $10^{-4}s^{-1}$ and $10^{-2}s^{-1}$ were considered.
- The strain-stress response exhibits a viscous flow dependent on the test temperature, the initial microstructure and the grain growth.
- A strain hardening is observed for the long time period test due to the grain growth evolution.

• The parameters of a grain growth model are identified, it successfully describes the evolutions predicted by the works of Semiatin et al and the measurements performed in the present study.

- The internal variable related to grain growth was introduced into the mechanical model through the viscous flow and the hardening. The stability of the constitutive equations are investigated under uni-axial conditions by the prediction of the necking and by the analysis of the shrinkage rate against the normalised cross-sectional area.
- A non isothermal formulation of the model allows to accurately predict test conditions not considered in the identification process. Moreover, some predictions with different initial grain sizes are addressed.

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Appendix

| Parameters | a | b | с | d | е |
|------------|-----------------|-------|----------------|------|----------------|
| A_1 | $1.406.10^{-9}$ | -6252 | - | - | - |
| A_2 | $1.19.10^{-5}$ | -8921 | - | - | - |
| n_1 | 0.993 | -719 | - | - | - |
| Q_0 | 725 | -3254 | - | - | - |
| α | 33.1 | -0.3 | $9.49.10^{-3}$ | 10.9 | $5.01.10^{-2}$ |
| γ | 549 | 0.469 | $1.2.10^{-2}$ | 795 | - |
| σ_0 | 156 | 0.223 | 0.024 | 550 | - |
| K_r | 1767 | 714 | 153 | - | - |
| n_r | 414 | 14.75 | 0.0175 | 345 | 1.95 |

Table 7: Interpolation function coefficients of the model parameters with the temperature



Figure 13: Evolution of the model parameters A_1, A_2, n_1 and α with temperature



Figure 14: Evolution of the model parameters $E,\ \sigma_0,\ K_r$ and n_r with temperature



Figure 15: Evolution of the model parameters Q_0 and γ with temperature

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