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# Model-based Investigation of the Circadian Clock and Cell Cycle Coupling in Mouse Embryonic Fibroblasts: Prediction of *RevErb- $\alpha$* Up-Regulation during Mitosis

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## Abstract

Experimental observations have put in evidence autonomous self-sustained circadian oscillators in most mammalian cells, and proved the existence of molecular links between the circadian clock and the cell cycle. Some mathematical models have also been built to assess conditions of control of the cell cycle by the circadian clock. However, recent studies in individual NIH3T3 fibroblasts have shown an unexpected acceleration of the circadian clock together with the cell cycle when the culture medium is enriched with growth factors, and the absence of such acceleration in confluent cells. In order to explain these observations, we study a possible entrainment of the circadian clock by the cell cycle through a regulation of clock genes around the mitosis phase. We develop a computational model and a formal specification of the observed behavior to investigate the conditions of entrainment in period and phase. We show that either the selective activation of *RevErb- $\alpha$*  or the selective inhibition of *Bmal1* transcription during the mitosis phase, allow us to fit the experimental data on both period and phase, while a uniform inhibition of transcription during

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mitosis seems incompatible with the phase data. We conclude on the arguments favouring the *RevErb- $\alpha$*  up-regulation hypothesis and on some further predictions of the model.

*Keywords:* Quantitative biology, Circadian clock, Cell cycle, Model coupling, Data fitting, Oscillations, Formal methods, Model Checking

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## 1. Introduction

In most organisms, from bacteria to plants and animals, spontaneous gene expression oscillations with a period close to 24 hours have been observed. A biochemical circadian clock present in each cell is responsible for maintaining these oscillations at this period, generally in the form of a self-sustained genetic oscillator entrained by the day/night cycle through various input pathways.

This circadian clock has many effects on cell signaling and metabolism [1]. Experimental results have also shown a regulation of the cell division cycle by the circadian clock [2, 3, 4], in particular in mammalian cells with possible applications to cancer chronotherapies [5, 6]. Molecular links between these two cycles have been exhibited to explain this regulation. In particular the regulation of Wee1, an inhibitor of the G2/M transition, by the clock genes has been proposed to explain the circadian gating of mitosis during the liver regeneration process [2] with 48 hours period doubling phenomena for the cell cycle [7]. Other similar molecular links going in the same direction, through p21 [8] and Chk1 and Chk2 [4, 9], have been shown in different cells in the literature. A few models have also been developed to further investigate those hypotheses, by coupling a model of the cell cycle with a model of the circadian clock through those direct molecular links, and analyzing the conditions of entrainment in period [10, 11, 12].

However, in mouse embryonic fibroblasts NIH3T3, several studies using large-scale time-lapse microscopy to monitor circadian gene expression and cell division events in real time and in individual cells during several days have unveiled unexpected behaviors, hinting that the relationship might be more

complex. Nagoshi et al. [7], have first shown that circadian gene expression in fibroblasts continues during mitosis, but with a consistent pattern in circadian period variation relatively to the circadian phase at division, leading them to hypothesize that mitosis elicits phase shifts in circadian cycles. A more recent study of Bieler et al. [13] relating the same experiments on dividing fibroblasts found the two oscillators synchronized in 1:1 mode-locking leading the authors to hypothesize a predominant influence of the cell cycle on the circadian clock in NIH3T3 cells. This is in agreement with another detailed experimental study of Feillet et al. [14] which found several synchronization states in NIH3T3 fibroblasts in different conditions of culture. In particular, it was observed in [14] that enriching the culture medium with growth factors by increasing the concentration of Foetal Bovine Serum (FBS) not only accelerates the cell division cycle but also the circadian clock. For cells cultured in 10% FBS, both distributions of the cell cycle length and the circadian clock are centered around 22h. For cells cultured in 15 % FBS, both the cell cycle and the circadian clock accelerate, with period distributions centered around 19 hours. However, when cells reach confluence and stop dividing, the circadian clock slows down and the period distribution is then centered around 24 hours. None of the currently available models coupling the cell cycle and the circadian clock can explain these observations since they are based on an unidirectional influence of the circadian clock on the cell cycle [10, 11] and not on the other direction.

In this paper, in order to explain these observations, we investigate the reverse influence of the cell cycle on the circadian clock, using computational modeling tools. We develop a mathematical model of the influence of the cell cycle on the circadian clock through the differential regulation of clock genes around the mitosis phase, and study the conditions in which the cycles are entrained in period and phase as observed in [14]. For this, we use the circadian clock model of Relogio et al. [15] which has been carefully fitted to phase data on suprachiasmatic cells, and a simple model of the cell cycle by Qu et al. [16] which focuses on the mitosis phase. In [17], we have already shown that the uniform inhibition of transcription during mitosis, as observed in eukaryotes [18], could

explain the acceleration of the circadian clock in non-confluent cells when the concentration of FBS increases [14]. In particular, our model could reproduce the same periods for the cell cycle and the circadian clock for different levels of FBS, modeled by different values for the synthesis parameters of the cell cycle model, but with an incorrect time delay between the cell division and the peak of *Reverb- $\alpha$* , which seemed impossible to fix under the hypothesis of a uniform inhibition of transcription during mitosis.

Here, we show that these difficulties can be resolved, using a different hypothesis of selective regulation of one clock gene during the M phase, either the activation of *Reverb- $\alpha$*  or the inhibition of *Bmal1*. Our coupled model under one of these hypotheses is able to reproduce the experimental measures on periods and phases made by Feillet et al. [14] in individual unperturbed fibroblasts. Furthermore we argue that the complex behaviors observed with high variability after a treatment by dexamethasone to synchronize cellular clocks, modeled by the induction of a high level of *Per* and the inhibition of the other clock core genes, can be explained by the perturbation of the clock after this treatment. Indeed, our model shows that the stabilization time after that pulse appears to be greater than the time horizon of 72 hours used in those experiments.

This computational model has been built using the Biocham modeling software [19] for

1. importing and exporting models in SBML, and modeling the molecular interactions of the coupling of the models,
2. specifying the observed behavior in quantitative temporal logic using pattern formulae for periods and phases [20, 21],
3. searching parameter values [22] and measuring robustness and parameter sensitivity indices [23] with respect to the temporal logic specification of the dynamical behavior<sup>1</sup>.

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<sup>1</sup>The models and the formal specifications used in this paper are available on <http://lifeware.inria.fr/wiki/software/biosystems16>.

## 2. Experimental Data and their Formal Specification in Temporal Logic

### 2.1. Experimental Observations and Measurements

In this section we explain the single cell experiments and analyses performed in [14] and the conclusions drawn by the authors. The reported experiments have been done using time lapse videomicroscopy and cell tracking using different fluorescent reporters for the cell cycle and the circadian clock observed during 72 hours in proliferating NIH3T3 embryonic mouse fibroblasts. This cell line was modified to include three fluorescent markers of the circadian clock and the cell cycle: the RevErb- $\alpha$ ::Venus clock gene reporter [7] for measuring the expression of the circadian protein<sup>2</sup> RevErb- $\alpha$ , and the Fluorescence Ubiquitination Cell Cycle Indicators (FUCCI), Cdt1 and Geminin, two cell cycle proteins which accumulate during the G1 and S/G2/M phases respectively, for measuring the cell cycle phases [24].

The cells were left to proliferate in regular medium supplemented with different concentrations of FBS (10% and 15%). Long-term recording was performed in constant conditions with one image taken every 15 minutes during 72 hours. The lengths of the cell cycles were measured as the time interval between two consecutive cell divisions.

The expression traces of RevErb- $\alpha$  proteins were detrended and smoothed. Spectrum resampling was used to estimate the clock period. Cells with less than two RevErb- $\alpha$  peaks within their lifetime, a period length outside the interval between 5 hours and 50 hours or a relative absolute error (RAE) bigger than 0.25 (showing a confidence interval wider than twice the estimated period) were classified as non-rhythmic and discarded, assuming that they do not have a functioning clock. Finally, the delay between cell division and the next clock marker peak was measured. It revealed that RevErb- $\alpha$ -Venus peaked about 7 h after cell division in all conditions, quite consistently with the delay of 5 hours

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<sup>2</sup>In this paper, the genes are distinguished from the proteins by writing the names of the genes in italics and the proteins in normal text.

for *Reverb- $\alpha$*  without *Venus* observed in [25] and [13].

The quantitative data on the periods of the cell cycle and the circadian clock and the phase between them are summarised in Table 1 [14]. Surprisingly, increasing FBS from 10% to 15%, not only decreases the mean period of the cell cycle from 21.3 hours to 18.6 hours, but also the clock period from 21.9 hours to 19.4 hours, i.e. to essentially the same period. This shows that both oscillators remain unexpectedly in 1:1 mode locking. While the speedup of the cell cycle can be directly attributed to the growth factors in increasing concentration of FBS, it can not account for the speedup of the clock the same way, since confluent cells keep a 24-hours period for the circadian clock independently of the FBS concentration [14].

Medium	Clock period	Division period	Mean delay
<b>FBS 10%</b>	21.9 h $\pm$ 1.1 h	21.3 h $\pm$ 1.3 h	8.6 h
<b>FBS 15%</b>	19.4 h $\pm$ 0.5 h	18.6 h $\pm$ 0.6 h	7.1 h

Table 1: Estimated periods of the circadian molecular clock and the cell division cycle measured in [14] in fibroblast cells without treatment by dexamethasone, for two concentrations of FBS. The time delay is between the cell division time and the next peak of *RevErb- $\alpha$*  protein.

## 2.2. Experimental Observations after Treatment by Dexamethasone

Furthermore, a series of experiments were done with a pulse of dexamethasone (abbreviated in the rest of this paper as *Dex*) before recording. This glucocorticoid agonist is known to exert a resetting/synchronizing effect on the circadian molecular clocks in cultured cells through the induction of *Per* genes. In that case, the cells were incubated for 2 hours in the same medium supplemented with *Dex*, just before returning to a *Dex*-free medium for the recording.

The resulting dynamics in *Dex* pulsed cells are more complex. Table 2 summarizes the observed period and phase values reported in [14]. The cells in 10% FBS show an increased clock period and a low cell cycle period, with an overall ratio of 5:4. In 20% FBS the cell lineages are dominated by two groups. The first group shows close periods, i.e. a 1:1 mode-locking similarly to the experiments without dexamethasone. The second group shows a high clock

period and a fast cell cycle, with an overall ratio close to 3:2 between the clock and cell cycle, explaining the three-peaks distribution of the circadian phase at division, as already observed by Nagoshi et al.[7] ten years before. It has to be noted that the 20% FBS dexamethasone-synchronized experiment was repeated with similar results available in the Supplementary Information of [14], although the distribution of the period ratios for the second group is wider in the interval ranging from 1.2 to 2.

Medium	Clock period	Division period	Mean delay
<b>FBS 10%</b>	24.2 h $\pm$ 0.5 h	20.1 h $\pm$ 0.94 h	10.7 h
<b>FBS 20%</b>	21.25 h $\pm$ 0.36 h	19.5 h $\pm$ 0.42 h	8.3 h
	29 h $\pm$ 1.05 h	16.05 h $\pm$ 0.48 h	6h/12h/22h

Table 2: Estimated periods of the circadian molecular clock and the cell division cycle measured in [14] in fibroblast cells after treatment by dexamethasone, for two concentrations of FBS. The time delay is between the cell division and the next peak of RevErb- $\alpha$  protein. The experiment done with 20% FBS have been clustered by the authors of [14] in two groups with different periods.

In [14], the authors suggest that these observations might be interpreted by the existence of distinct oscillatory stable states coexisting in the cell populations, in particular with 5:4 and 1:1 phase-locking modes for the condition 10% FBS, and 3:2 and 1:1 phase-locking modes for the condition 20% FBS, and that the dexamethasone could knock the state out of the 1:1 mode toward other attractors.

### 2.3. Formal Specification of Oscillation Properties in Quantitative Temporal Logic

For the analysis of the dynamical behavior of this complex system, we shall make use of a temporal logic language which allows us to express the relevant system’s oscillatory properties to fit, instead of over-specifying them by providing a precise curve to fit. This allows us to combine qualitative properties of oscillations and quantitative properties on the shapes of the traces such as distances between peaks or peak amplitudes. This is useful to capture the periods on either experimental and simulated traces, even when the traces are irregular and noisy. We use formal constraints on the amplitudes and regularity of the



peaks to filter out ambiguous traces, keeping only sustained oscillations with small irregularities, as depicted for instance in Fig. 10.

More precisely, we use the temporal logic formula patterns described in [20, 21] and implemented in our modeling software Biocham [19] to specify the constraints about the successive peaks of concentrations between either the same molecular species (period constraints) or different molecular species (phase constraints). Biocham then provides commands for automatically

- extracting periods and phases from either simulation or experimental numerical data time series [26],
- searching the space of the unknown parameters of the model for satisfying period and phase constraints [22],
- measuring parameter sensitivity indices and robustness with respect to period and phase constraint [23].

For instance, the following command (used in Section 3) computes the validity domain of the variables of a formula pattern used to extract the period of the mitosis promoting factor (MPF) for the cell cycle, and of RevErb- $\alpha$  for the circadian clock, in a trace, together with their relative phase:

```
validity_domain(
  Exists([e1,e2,e3],
    periodErrors([RevErb_nucl],[periodselect,e1,e2,e3],100)
    & e1<2 & e2<2 & e3<2))
  & period([MPF],[periodMPF])
  & phase([MPF,RevErb_nucl],[phase])).
```

The result for the simulation trace displayed on the bottom of Fig. 6 is

```
periodselect = 20.023, periodMPF = 20.046, phase = 6.765
```

Since the trace of MPF shows sustained and regular oscillations in all simulations, the simple predicate *period* is used here to extract the mean of the last two peak-to-peak intervals. The predicate *phase* similarly captures the mean of the last two time intervals between MPF and RevErb- $\alpha$  peaks. On the other hand, the period constraint on the oscillations of RevErb- $\alpha$  is expressed by the

predicate *periodErrors* which deals with irregular traces. The validity domains of its variables provide the mean of the last two RevErb- $\alpha$  peak-to-peak intervals in the variable *periodselect*, along with several variables characterizing irregularity features of the trace, namely *e1* for the irregularities in distances between peaks (it denotes the maximum difference between two intervals), *e2* for the irregularities in the amplitudes of the peaks (it quantifies the differences between the amplitudes of the peaks), and *e3* being a non-null error if the concentration amplitude is too small (below 0.1). Setting thresholds on these variables ensures that irregular traces are filtered out. Furthermore, a transient time of 100h is used to avoid the irregularities caused by the initial state. The logical quantifier *Exists* projects the validity domain of the variables on the single dimension for *periodselect* for the answer, and eliminates the other dimensions for *e1*, *e2* and *e3*.

It is worth noting that for the purpose of parameter search, irregular traces after transient time should not be filtered out in order to orient the search algorithm in a promising direction, when oscillations begin to appear for instance. The formula below specifies a constraint on period and phase for parameter search, without constraint on the period errors:

```
add_search_condition(
  periodErrors([RevErb_nucl], [period, e1, e2, e3], 100)
  & Exists([phase], phase([MPF, RevErb_nucl], [phase])
           & phase > minphase & phase < maxphase),
  [period, e1, e2, e3, minphase, maxphase], [21.3, 0, 0, 0, 3, 5.5],
  300, [(kdie, kdie21)]).
```

This formula is used by the parameter search procedure for testing the parameter values in different conditions. The condition expressed here, *kdie=kdie21*, fixes a particular value for the parameter *kdie* which determines the period of the cell cycle model (detailed in the next Section) in accordance with one of the experimental values for FBS. A time horizon of 300h is specified for the simulation. The validity domains for the variables [*period, e1, e2, e3, minphase, maxphase*] are compared to the objective values [21.3, 0, 0, 0, 3, 5.5] in order to determine a score for the constraint (as the Euclidean distance to the objective values). The addi-

tional variables *minphase* and *maxphase* are used to score the distance from the phase to the objective interval [3,5.5], enabling some flexibility in the searched value for the phase. For instance, the best set of parameters found as a solution after the calibration procedure detailed in 4.2 has the score 0.54 for this constraint..

Furthermore, the difference between the periods of the cell cycle and the circadian clock is used to score the entrainment in period of the circadian clock by the cell cycle. This is achieved by the following formula with the variable *diff* :

```
satisfaction_degree(
  Exists([p1,p2],
    Exists([e1,e2,e3],
      periodErrors([RevErb_nucl],[p1,e1,e2,e3],100)
      & e1<3 & e2<3 & e3<3)
    & period([MPF],[p2]) & diff=p2-p1),
  [diff],[0],300).
```

This formal specification of entrainment in period is used to compute the satisfaction degrees displayed in Fig. 7. Each value scores the difference between the two periods with a continuous satisfaction degree between 0 (no entrainment) to 1 (null difference, perfect entrainment).

### 3. Cell Cycle and Circadian Clock Models

#### 3.1. Model of the Cell Cycle

The cell cycle of mammalian cells is composed of five phases: the quiescent phase G0 where cells can stay without dividing, the growth phase G1 for entering the cell cycle, the DNA replication phase S, the gap phase G2, and the chromosome segregation and mitosis phase M phase. Each phase is characterized by a particular protein of the cyclin family, which forms a complex with a cyclin-dependent-kinase (CDK) and determines the activity of the phase. The mouse embryonic fibroblast cells considered in this paper are quickly dividing cells. However, those cells with growth factors also reach confluence and the G0 quiescent phase when they have no more space to divide, i.e. G0 by contact inhibition.

For our purpose of investigating the hypothesis of a regulation of some clock genes around mitosis, it is sufficient to use a cell cycle model focusing on the mitosis phase. We use a model proposed by Qu et al. [16] in which the cell cycle is divided in two different phases: the G1/S/G2 phase and the M phase. Of course, more detailed models distinguishing the four phases of the cell cycle exist, e.g. [10], making possible to represent various regulations of the cell cycle by the circadian clock genes, for instance through p21 and c-Myc on G1, and Wee1 on the G2/M transition. However, since the consequences of those regulations have not been observed in the experimental data considered in this paper, those extra details are irrelevant for our focus on the reverse effect of the cell cycle on the circadian clock by the regulation of clock genes around mitosis. The simpler two phase model of Qu et al. [16] is thus sufficient to investigate this hypothesis.

In this model, the M phase is triggered by the complex Cdk1/Cyclin-B. This complex appears in two forms, an active form called MPF (M-phase Promoting Factor) and a phosphorylated, inactive form called preMPF. MPF is phosphorylated and inactivated by the kinase Wee1, and dephosphorylated and activated by the phosphatase Cdc25. Both the kinase and phosphatase activities are themselves regulated by MPF, respectively inactivated and activated by the complex, as depicted in Fig. 1.

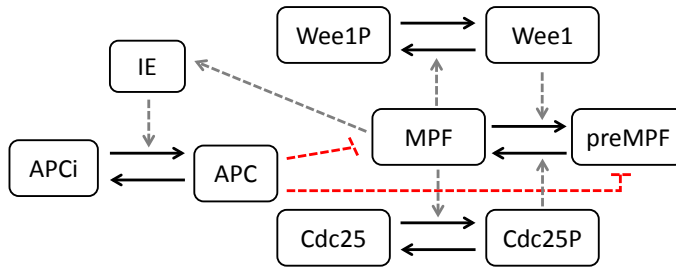


Figure 1: Schema of the cell cycle model of Qu et al. [16]. Solid arrows represent biochemical reactions while dashed arrows denote enzyme catalysis. Red arrows denote an inhibition through activation of the degradation.

In this model, we assessed the effect of the different reaction rate constants on the period of the cell cycle using sensitivity analysis. We found that two

parameters are able to change widely the range of the cell cycle period without changing significantly the strength of the coupling:  $k_{die}$ , the degradation rate constant of the intermediary enzyme involved in the negative feedback loop between MPF and the proteasome APC, particularly important in G1/S, and  $k_{ampf}$ , the activation rate constant of MPF by Cdc25p, which plays a role in G2/M. In the supplementary material of [14], both the phases G1 and S/G2/M seem to be shortened in enriched FBS. Therefore there is no reason to prefer  $k_{die}$  (active in G1) or  $k_{ampf}$  (active in G2/M) to modulate the cell cycle period. We choose  $k_{die}$  as varying parameter affected by FBS because its activity is during the cell growing phase G1. The same results could be obtained with  $k_{ampf}$ .

A simple parameter search gives the following values for  $k_{die}$ : 0.147 for a cell division period of 21.3 hours corresponding to 10% FBS, and 0.23 for a period of 18.6 hours corresponding to 15% FBS).

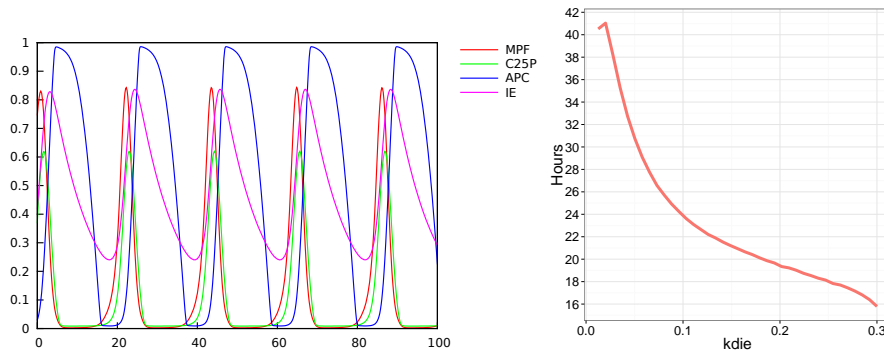


Figure 2: **Left:** Simulation of the cell division cycle model of Qu et al. **Right:** Period of the cell division cycle (measured as the distance between successive peaks of MPF) as a function of the parameter  $k_{die}$  for MPF activation by Cdc25p in the model of Qu et al.

### 3.2. Model of the Circadian Clock

It has been shown in mice that in absence of synchronisation by a central clock, autonomous circadian oscillators are maintained in peripheral tissues, although they are progressively desynchronized [27] because each one of them has its own period, that varies slightly from 24h. This has been confirmed in cultured NIH3T3 cells first in [7] and then in [13] and [14]. In each of those

studies, confluent fibroblasts have a circadian clock period close to 24 hours regardless of the medium concentration.

In this paper we use the circadian clock model of Religio et al. [15] which has been fitted on mouse suprachiasmatic neurons with precise data on the amplitude and phases of the different components. This model is composed of 20 species, 71 parameters, and several feedback loops. Two major transcription factors, Clock and Bmal1 heterodimerize and activate the transcription of the period (*Per1* and *Per2*), cryptochrome (*Cry1* and *Cry2*), *RevErb- $\alpha$*  and *Ror* clock genes. The Per and Cry proteins associate and inhibit their own expression and that of the *RevErb- $\alpha$*  and *Ror* through direct inhibition of the *Clock/Bmal1* transcriptional activity. Furthermore, the antagonistic *RevErb- $\alpha$*  and *Ror* transcription factors regulate the rhythmic transcription of *Bmal1* and *Clock*. These interlocked feedback loops generate robust 24 hours self-sustained oscillations that in turn control the expression of a large set of downstream clock-controlled genes. A simulation trace of this model is shown in Fig. 3.

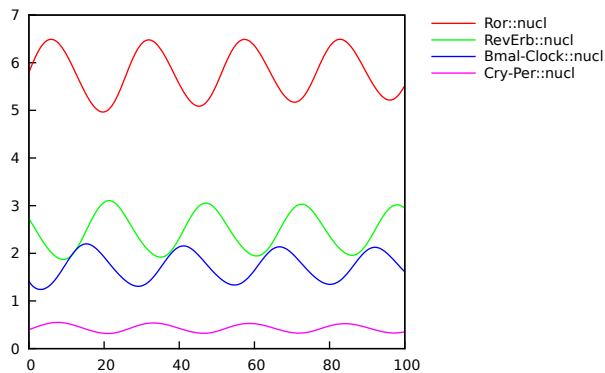


Figure 3: Simulation trace of the concentrations of the clock gene products in the nucleus over a time horizon of 100h in the model of Religio et al. [15].

## 4. Coupled Model

### 4.1. Hypothesis of a Selective Regulation of Clock Gene Transcription triggered by Mitosis

In this paper, we investigate the hypothesis that a differential inhibition/activation of some clock genes around the M phase could explain the observations made and reproduce consistent values for the period of the circadian clock and the delay between the divisions and RevErb- $\alpha$ -Venus peaks for the different values of FBS.

To assess this hypothesis, we model the inhibition or activation of clock genes transcription with five multiplicative coefficients  $L_i$  ( $i \in [1..5]$ ), associated to the synthesis rate parameters of the model of Relegio et al. [15] for each of the five clock genes. Each coefficient takes the value 1, except during a window starting at the beginning of the M phase, where its value is changed with an event triggered by the decrease of MPF. Another event is triggered at the end of the regulation window to reset the coefficient. During this window, whose length is defined by a parameter *duration*, the coefficient for the circadian core gene  $i$  takes the value of the dimensionless parameter *coefsynth<sub>i</sub>*, that defines the inhibition/activation strength of this clock gene. This value is included in the interval  $[0, 3]$ , where 0 denotes a full inhibition (i.e., strong coupling), 1 marks no effect of the mitosis on the synthesis (no coupling), and more than 1 induces some activation (coupling again). The value of the regulation *duration* parameter is also considered in the interval  $[0, 3]$  hours.

Our coupled model of the cell cycle and the circadian clock thus uses six parameters: the regulation strengths of the clock genes (*coefsynth<sub>i</sub>* ( $i \in [1..5]$ )) and the duration of the regulation.

```
parameter(duration,2).
parameter(endMitosis,0).

For each clock gene i:
parameter(I_i,1).
parameter(coefsynth_i,0).

add_event([MPF]<0.5,endMitosis,Time+duration).
add_event([MPF]<0.5, I_i, coefsynth_i).
```

```
add_event(Time>=endMitosis, I_i, 1).
```

It is worth noting that this way of coupling the models enforces the fact that for quiescent cells, whatever the FBS concentration is, the transcription rate is unaffected by mitosis. As a consequence, the clock necessarily returns to a period of 24 hours in confluent cells, as observed in the experiments.

#### 4.2. Coupling Parameters

In our coupled model, the influence of the cell cycle on the circadian clock is modeled by a set of parameters that express the regulation coefficient (activation or inhibition) of clock gene synthesis during mitosis. We use the parameter search procedure of Biocham based on stochastic optimization [22] to find the sets of values for the coupling parameters that reproduce the entrainment in period and phase observed in the data. Using the behavior specification detailed in Section 2.3, we define a multi-condition objective for the four conditions  $k_{die}=0.1$ ,  $k_{die}=0.147$ ,  $k_{die}=0.18$  and  $k_{die}=0.23$ : the period of the circadian clock must be equal to the period of the cell cycle, respectively 24 hours, 21.3 hours, 20h and 18.6 hours. Furthermore, in each condition, the delay between MPF and RevErb- $\alpha$  peaks must be between 6.5 hours and 8.6 hours.

Coupling parameters	First set	Second set
Synthesis coefficient for <i>Per</i>	2.40	0.66
Synthesis coefficient for <i>Cry</i>	0.67	2.30
Synthesis coefficient for <i>RevErb-<math>\alpha</math></i>	1.92	1.04
Synthesis coefficient for <i>Ror</i>	1.51	2.1
Synthesis coefficient for <i>Bmal1</i>	0.78	0
Duration	2.81	2.97 hours

Table 3: Two sets of synthesis regulation coefficients during mitosis, found by Biocham’s calibration procedure for satisfying the temporal logic specification of period and phase data. The first set was found with initial values equal to 1 for all synthesis coefficients, while the second was found with null initial values.

Essentially, two types of solutions, shown in Table 3, are found. If the initial values are 1 for all synthesis coefficients, corresponding to no inhibition during mitosis, the best result found after 55 iterations on a population of 95 sets of



parameters gives the first set of parameters reported in Table 3. This solution corresponds to an activation of *RevErb- $\alpha$* , *Per* and *Ror*, while *Bmal1* and *Cry* transcription is weakly inhibited. If the parameter search starts from a full inhibition triggered by mitosis for all clock genes, corresponding to initial values of 0 for all synthesis coefficients, the second set is the best result found after 260 iterations on a population of 95 sets of parameters. In this parameter set, a full inhibition is found for *Bmal1* transcription, and a smaller inhibition for *Per* transcription. *Cry* and *Ror* transcriptions are activated while the *RevErb- $\alpha$*  transcription is mostly unaffected.

The simulation of the model with any of these two sets of parameters shows a delay between the starting time of the mitosis effect and the circadian clock consistent with the experimental data (close to 7 hours for the first set, and between 7 and 8.5 hours for the second one), as well as consistent period values. The stochastic optimization procedure for parameter search returns numerical values for all coupling parameters, however one must check which parameter values are necessary for the correct entrainment, and which parameters have no impact on the satisfaction of the specification of the behavior. To this end, we perform a sensitivity analysis by computing the response curves for the period of the circadian clock and the delay between mitosis and the next *RevErb- $\alpha$*  peak by varying each coupling parameter, in the condition where the cell cycle has a period of 21 hours.

The results for the first set of parameters are shown in Fig. 4. These simulation results reveal that the entrainment in period and phase of the circadian clock depends only on the effect of mitosis on *RevErb- $\alpha$*  and *Bmal1*, and on the duration of this effect. In the first parameter set, the activation of *RevErb- $\alpha$*  is crucial for the entrainment in period. On the other hand, varying the synthesis coefficients during mitosis for *Per*, *Cry* or *Ror* has no significant effect on the entrainment in period and phase. More specifically, the clock is entrained to the cell cycle period of 21 hours if the coefficient multiplied to the synthesis rate of *RevErb- $\alpha$*  is at least 1.7, and the inhibition lasts at least 2 hours. In this condition the time delay between divisions and *RevErb- $\alpha$*  peaks is consistent with

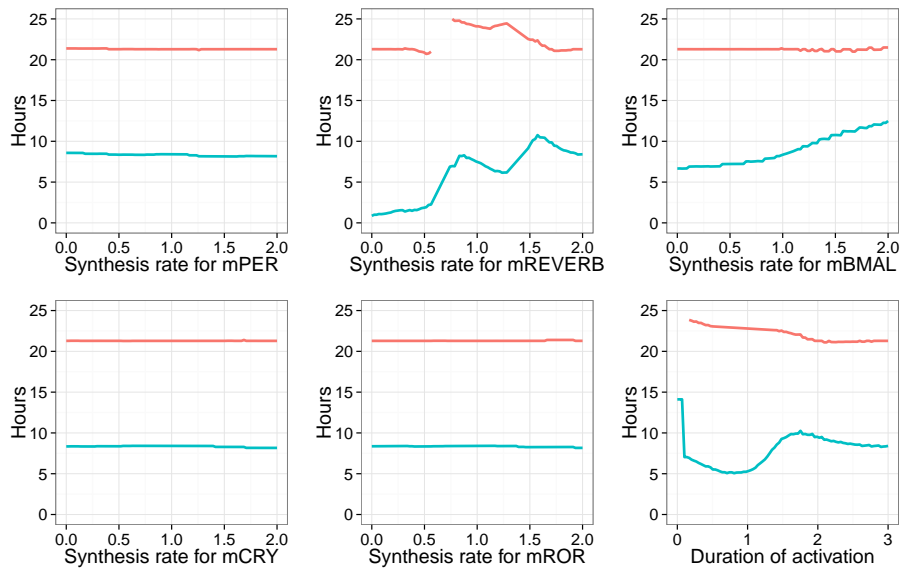


Figure 4: Period of the circadian clock (red) and time delay between MPF and RevErb- $\alpha$  proteins peaks (blue) in the coupled model calibrated with the first set of parameters, and when the cell cycle has a period of 21 hours. The peaks on the blue curves on the right figures characterize irregular oscillating traces (due to a partial entrainment in period).

the data, with RevErb- $\alpha$  peaks occurring 7 hours after division. An inhibition of *RevErb- $\alpha$*  would also preserve the entrainment in period, but the circadian phase at division would become inconsistent with the data, with RevErb- $\alpha$  peaks occurring just after mitosis. One can notice that an activation on *Bmal1* would also increase the time delay of RevErb- $\alpha$  peaks after division.

The results for the second set of parameters are shown in Fig. 5. These simulation results reveal similarly that the entrainment in period and phase of the circadian clock depends only on the effect of mitosis on *Bmal1* and *RevErb- $\alpha$* , and not on *Per*, *Cry* or *Ror*. However in this case the entrainment in period depends on the effect on *Bmal1* which has to be inhibited with a coefficient smaller than 0.2 in order for the circadian clock to be entrained at 21 hours with a correct delay after division.

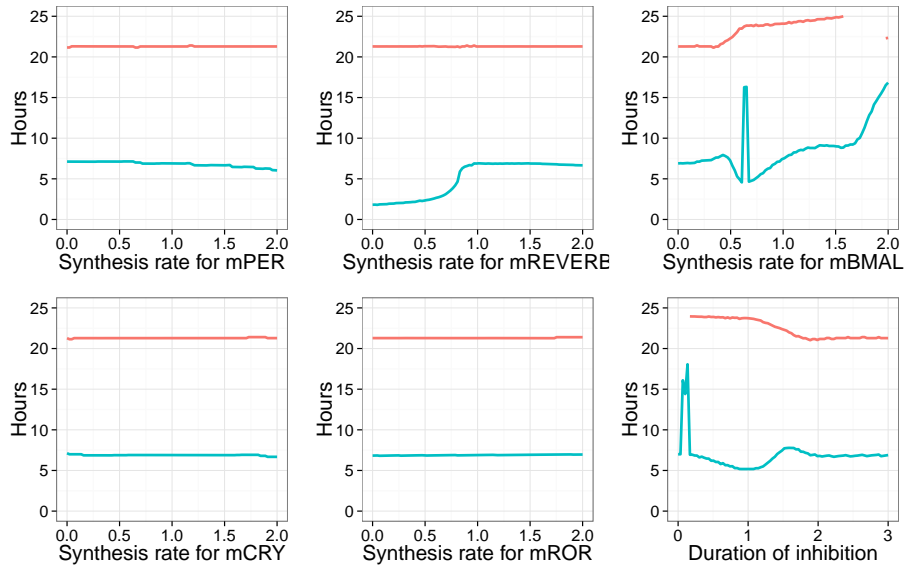


Figure 5: Period of the circadian clock (red) and phase between the division and RevErb- $\alpha$  protein (blue) in the coupled model calibrated with the second set of parameters, and when the cell cycle has a period of 21 hours.

### 4.3. Simulation Results for the Selective Activation of *RevErb- $\alpha$* during Mitosis

The first set of coupling parameter values points toward the hypothesis of a selective activation of the circadian clock gene *RevErb- $\alpha$*  triggered by mitosis. Thanks to the previous sensitivity analysis, the first coupling parameter set can be simplified to consider a single activation of *RevErb- $\alpha$*  (corresponding to a coefficient equal to 2), and no effect on the other clock genes.

It is worth noting that an up-regulation of *RevErb- $\alpha$*  translation during the M phase has already been observed in a genome-wide experimental study interrogating the translational landscape during cell cycle progression using ribosome profiling [28]. This provides one first argument for considering this hypothesis in the first place.

<i>kdie</i>	FBS %	Circadian clock period (h)	Cell division period (h)	Phases (h)
0.077	5	26.14	26.12	6.1
0.147	10	21.52	21.28	8.5
0.229	15	18.48	18.60	7.2

Table 4: Periods and time delays measured in the coupled model with different values of *kdie* for modeling the different culture conditions (the correspondance with 5% FBS is speculative since no significant experiment was done in this condition). The delays are the time observed by simulation between the peaks of concentration of MPF and *RevErb- $\alpha$* .

Table 4 shows the periods of the circadian clock and the cell division cycle and the delay between the starting time of the inhibition of *RevErb- $\alpha$* , when the peak of MPF overtakes the threshold 0.5, and the following peak of *RevErb- $\alpha$*  in our model with different values of *kdie* corresponding to the different culture conditions. As shown in the right panel of Fig. 2, it is possible to simulate the experimental medium enrichment with 10 or 15% FBS by varying the parameter *kdie* of the cell cycle model to obtain the same values for the period of the cell division cycle. In all cases, the cell division manages to entrain the circadian clock (that has a free period around 24 hours) to its period, simply through this mechanism of selective transcription activation, as depicted in Fig. 6. These simulation results reproduce quite well the data of Table 1 when there is no treatment by Dex.

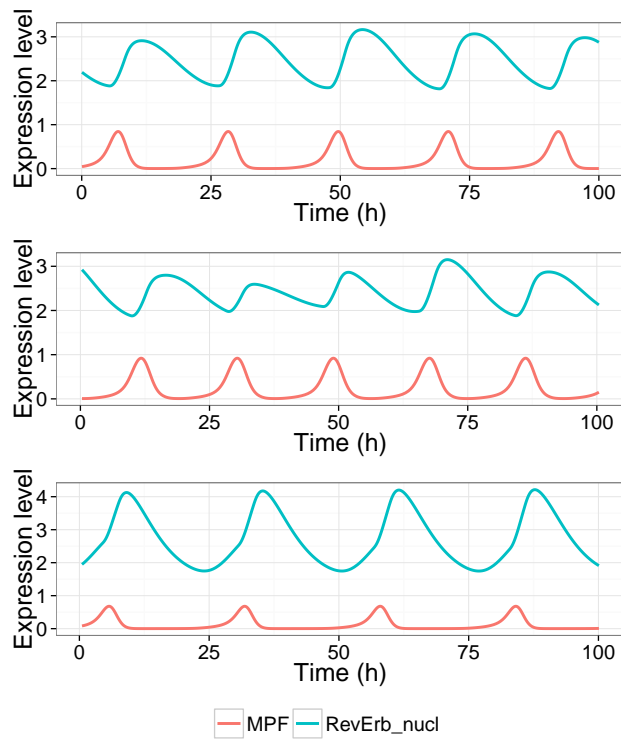


Figure 6: Simulation of the model with the activation of the transcription of *RevErb- $\alpha$*  triggered by mitosis, during 72 hours. Top: the cell cycle has a period of 21.3 hours. Middle: the cell cycle has a period of 20.1 hours. Bottom: the cell cycle has a period of 26 hours.

Interestingly, our model can also have a cell division time higher than 24 hours, for instance with  $kdie=0.077$  which might correspond to a concentration of FBS around 5%. In that case the model predicts that the cell cycle will still entrain the circadian clock, lowering its period. Moreover, RevErb- $\alpha$  peaks are predicted to stay just after the mitosis.

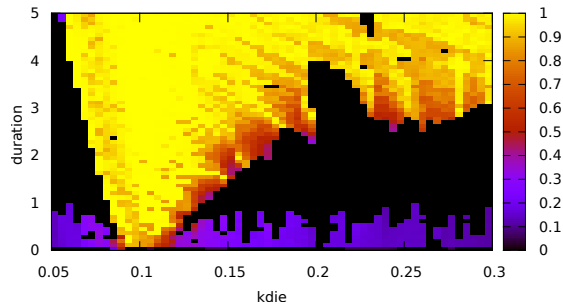


Figure 7: Absolute difference between the periods of the circadian clock and the cell cycle, as a function of  $kdie$  for varying the cell cycle period,  $duration$ , the duration of the activation of *RevErb- $\alpha$*  transcription triggered by mitosis. The landscape is computed as the satisfaction degree of the third formula detailed in 2.3. The color translates the distance from the value found for the period difference  $diff$  to the objective 0. Full satisfaction in yellow indicates equal periods for MPF and RevErb- $\alpha$  proteins, while the other colours indicate the absolute difference. Black indicates an absence of result for the specification, meaning that the regularity constraints set on the trace of RevErb- $\alpha$  with the function *periodErrors* were not met.

The landscape in Fig. 7 is computed to assess the role of the inhibition or activation duration. It shows the variation of the difference between the periods of RevErb- $\alpha$  for the circadian clock and MPF for the cell cycle when the two parameters  $kdie$  and  $duration$  vary. The value of each period is captured with a temporal logic specification as seen in the subsection 2.3. The result for the activation of *RevErb- $\alpha$* . is shown in Fig. 7. Three domains can be distinguished in this parameter space. In the domain in yellow, the circadian clock is entrained to the same period as the cell cycle. This domain of entrainment is wider for a long duration of activation. For a short duration, the circadian clock can only be entrained by the cell cycle if the entraining period is close to 24 hours (corresponding to  $kdie=0.1$ ). In the purple domain at the bottom (for a low value of  $duration$ ), the difference between the two periods is high because the

clock is not entrained, hence it keeps its period constant and close to 24 hours. Finally, these two domains are separated by a black domain where the clock oscillations are partially entrained and become irregular.

One can notice that the longer the activation of *RevErb- $\alpha$* , the wider the range of values of *kdie* over which the circadian clock can be entrained. In particular, the clock can be entrained by the cell cycle when *kdie* = 0.23, corresponding to the smallest period (18 hours) reported in the data, if the duration of the activation is at least 3 hours.

The entrainment both in period and phase with an activating effect during 3 hours is visualized in Fig. 8. It shows the response curve for the periods of the cell cycle and the circadian clock, and the time delay between the peaks of MPF and *RevErb- $\alpha$*  in the simulations when the parameter *kdie* varies.

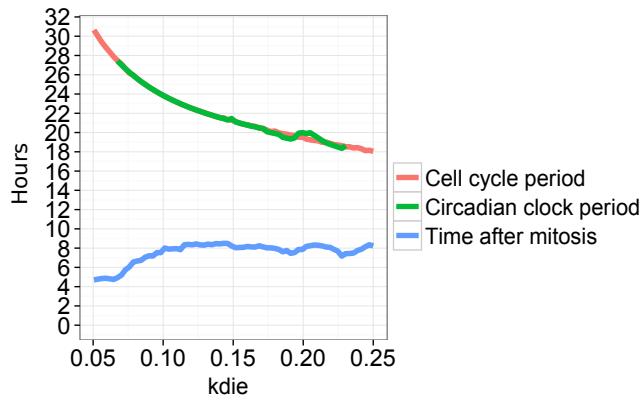


Figure 8: Entrainment in period and phase of the circadian clock when the period of the cell cycle varies with the parameter *kdie*, with the activation of *RevErb- $\alpha$*  triggered by mitosis. The blue curve depicts the time delay between peaks of MPF and *RevErb- $\alpha$*  in the simulations.

#### 4.4. Predictions on the phases in the clock

The experimental data on the phases between clock components in proliferating cells are sparse. The model allows us to investigate whether the coupling from the cell cycle affects the phases between clock mRNAs and proteins. The following *in silico* experiment has been performed to this end: in the coupled

model with a fast cell cycle (21 hours), the strength of the activation of *RevErb- $\alpha$*  is changed in a set of simulations and the phases between clock components are captured in each simulation, normalised by the clock period. The results are shown in Fig. 9.

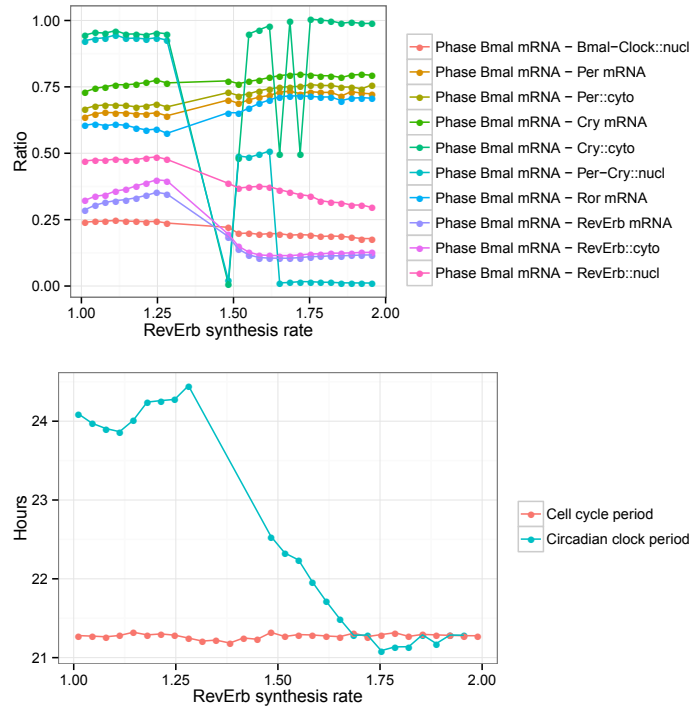


Figure 9: Circadian clock phases in the coupled model when the cell cycle has a period of 21 hours and the activation of *RevErb- $\alpha$*  varies. Note that the deep variations between synthesis rates 1.25 and 1.75 can be explained by irregular oscillations caused by partial entrainment, on which measured phases are not reliable.

The simulations reveal that in the entrained condition (when the synthesis rate of *RevErb- $\alpha$*  is activated with a coefficient higher than 1.75), the phases between clock components are impacted by the periodic activation of *RevErb- $\alpha$*  resulting from the coupling with the cell cycle, compared to their values in the free clock (when the synthesis rate of *RevErb- $\alpha$*  is activated with a coefficient close to 1). In particular, the phase between *Bmal1* and *RevErb- $\alpha$*  mRNAs shows a small advance, that impacts similarly the phases between Bmal1 and



RevErb- $\alpha$  in the cytoplasm and in the nucleus. Notably, the other clock genes and proteins targeted by Bmal1 exhibit a phase delay when the synthesis of *RevErb- $\alpha$*  is activated during mitosis.

The prediction is thus that in dividing cells, the phases between the clock proteins slightly but significantly differ from the phases in quiescent cells.

#### 4.5. Comparison to Experimental Data after Treatment by Dexamethasone

In order to take into account the experiments with dexamethasone, the model can be extended with an event, lasting for two hours, and inducing *Per* mRNA while inhibiting the other clock genes.

Fig. 10 shows that in our models, regardless of the growth factors in the medium (i.e. of the value of *kdie*), the Dex pulse results in a perturbation of the clock and then returns to the observed entrainment.

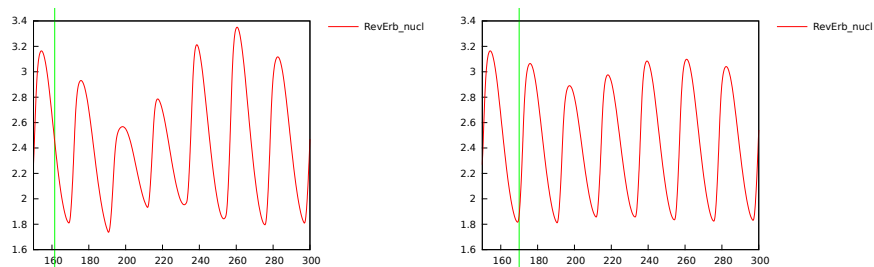


Figure 10: Effect of a dexamethasone pulse on the entrainment resulting from the periodic activation of *RevErb- $\alpha$*  synthesis by the cell cycle. The pulse alters the clock before returning to the previously observed entrainment regime. In the left panel the pulse is from time 162 to 164 while on the right it is from 170 to 172. The left panel’s peak-to-peak distance is in the [18.8; 22.7] interval, while the right one remains in the [20.9; 21.7] interval. This might correspond to the two groups observed in [14]. The time to recover normal entrainment varies but is often larger than 72 hours.

These simulations point us to the possibility that the noisy data reported in Table 1 after the Dex pulse might simply be due to the various cellular states in which the pulse happened and to the time necessary for the cells to recover their clock entrainment, rather than to two different oscillatory attractors of the system. A pulse at time 170h disrupted only slightly our clock, leading to mostly remaining in mode-locking 1 : 1, whereas advancing that same pulse by 8 hours (corresponding to giving the pulse to a cell in a different state) leads

to a bigger disturbance, some peak-to-peak distances close to 23 hours, others to 18 hours, and even if this is transitory, this might correspond to the type of data observed in the Group 2 of Table 1.

One can remark that an alternative hypothesis could be that Dex causes a stress response linked to the cell cycle and the circadian clock. This would still look like noise, but there could be a mechanistic explanation for this effect which could be investigated with a modeling approach. However, to our knowledge, a short treatment by Dex is not known to cause a stress response.

#### 4.6. Simulation Results for the Selective Inhibition of *Bmal1* during Mitosis

The second solution found by the calibration procedure in section 4.2 is discussed here. Like the activation of *RevErb- $\alpha$*  transcription, the inhibition of *Bmal1* during 3 hours, triggered at mitosis, is able to entrain the circadian clock in a wide range of periods (18-28 hours). The results summarized in Table 5 show a similarly good fit to the experimental data on periods and phases. The resulting traces are displayed in Fig. 11 for different cell cycle length conditions.

The entrainment in phase, ie. the duration between mitosis and the following *RevErb- $\alpha$*  peak, differs between the two couplings, as shown in Fig. 12. In both cases, when the cell cycle has a period smaller than 24 hours, the circadian clock marker *RevErb- $\alpha$*  peaks 6 hours to 8 hours after mitosis. When the cell cycle period is greater than 24 hours, a notable difference can be seen for the predicted phase: with an activation of *RevErb- $\alpha$* , *RevErb- $\alpha$*  still peaks just after the mitosis. But with an inhibition of *Bmal1*, *RevErb- $\alpha$*  peaks 18 to 24 hours after the mitosis. No experimental observations exist in a slowed down cell cycle condition, but [7] and [13] report some cells dividing not long after the circadian peak where the circadian clock was found to be slowed down. On the other hand, the large translational landscape of gene expression during cell-cycle progression reported in [28] does not consider *Bmal1* nor any clock gene other than *RevErb- $\alpha$* .

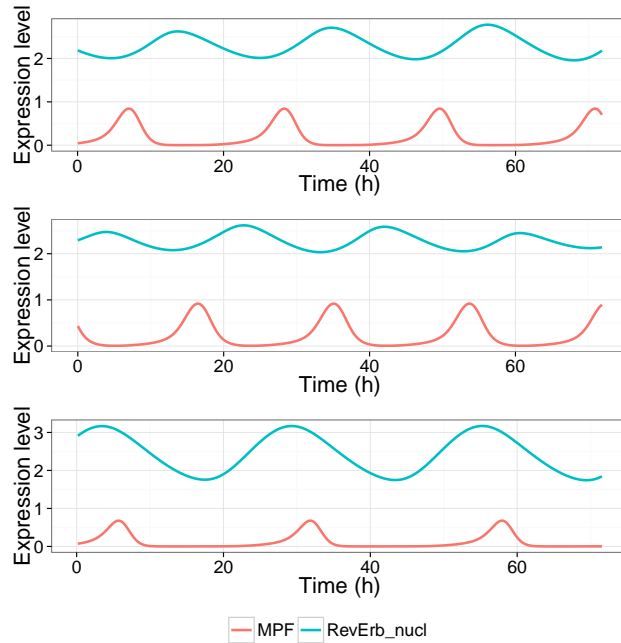


Figure 11: Simulation of the model with the the periodic transcription of *Bmal1* activated by mitosis, during 72 hours. Top: the cell cycle has a period of 21.3 hours. Middle: the cell cycle has a period of 20.1 hours. Bottom: the cell cycle has a period of 26 hours.

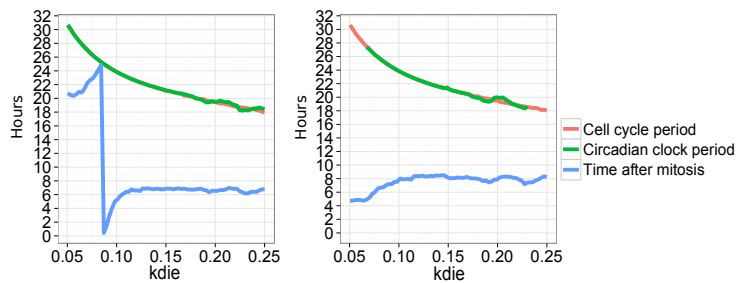


Figure 12: Entrainment in period and phase of the circadian clock when the period of the cell cycle varies with the parameter  $k_{die}$ , with the inhibition of *Bmal1* (left) or the activation of *RevErb- $\alpha$*  (right) triggered by mitosis. In the right panel, the circadian clock period is missing for low  $k_{die}$  values because the oscillations are irregular. The blue curves depict the time delay between peaks of MPF and RevErb- $\alpha$  in the simulations.

$k_{die}$	FBS %	Circadian clock period (h)	Cell division period (h)	Phases (h)
0.077	5	26.09	26.10	23.2
0.147	10	21.28	21.28	6.8
0.229	15	17.99	18.60	6.3

Table 5: Periods and time delays reproduced by the coupled model with different values of  $k_{die}$  for modeling the different culture conditions (the correspondance with 5% FBS is speculative since no experiment was done in this condition). The delays are the time observed by simulation between the peaks of concentration of MPF and RevErb- $\alpha$ .

#### 4.7. Uniform Inhibition of Transcription during Mitosis

It has been shown that in eukaryotes, gene transcription can be significantly inhibited during mitosis [18]. The impact of a global transcription inhibition of clock genes during mitosis on the circadian oscillator has been studied by modeling in [29]. In this study, the authors found that a periodic inhibition of transcription during one hour was able to entrain a model of the mammalian circadian clock, but only when the inhibition period was close to one half, twice or equal to the intrinsic circadian model period. In these cases, a phase locking between the circadian clock and the periodic inhibition was observed, albeit with one or two preferential circadian phases for the inhibition and values that varied greatly with the inhibition period. The discrepancies with the recent data could come from the short inhibition duration considered or from the arbitrarily parameterised model used for the circadian clock, taken from [30].

In [17], we also investigated the uniform inhibition of all clock genes and found that it was sufficient to reproduce the entrainment of the circadian clock by the cell cycle in period, but *not in phase*. The delay between MPF and RevErb- $\alpha$  remained inconsistent with the data, as depicted in Fig. 13, i.e. the mitosis triggered by MPF occurs just after the peaks of RevErb- $\alpha$ , while the experimental studies consistently report the opposite: peaks of RevErb- $\alpha$  5-7 hours after divisions. Furthermore, it seemed impossible to find parameter values to reproduce the observed delay under that hypothesis of a uniform inhibition of transcription during mitosis, which thus cannot explain the experimental data in mouse embryonic fibroblasts NIH3T3 measured in [14].

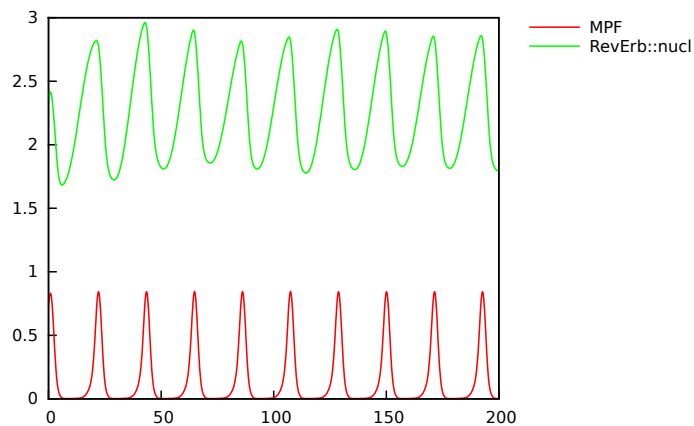


Figure 13: Entrainment to a period around 21.3 hours with  $kampf = 3.75$  corresponding to a medium enriched with 10% FBS, found in [17].

## 5. Conclusion

By hypothesizing a selective activation of *RevErb- $\alpha$*  or a selective inhibition of *Bmal1* triggered at the beginning of mitosis, we have been able to build a mechanistic dynamical model which reproduces the somewhat surprising numerical data reported in [13, 14] about the acceleration of the circadian clock observed in dividing fibroblasts with high FBS concentrations. These observations suggest that the primary coupling between the cell division cycle and the circadian clock results from an influence of the cell cycle on the circadian clock in those cells. While considering a uniform inhibition of the transcription during mitosis [18] was shown to be sufficient to fit the period data in [17], the phase data reported in [14] seemed to be impossible to reproduce under that uniform inhibition hypothesis. The use of Biocham search algorithms for computing transcription inhibition parameters satisfying the period and phase observations formalized in quantitative temporal logic, led us to the hypothesis that around mitosis, either the transcription of *RevErb- $\alpha$*  has to be strongly activated, or *Bmal1* strongly inhibited with no inhibition of *RevErb- $\alpha$* . These two hypotheses differ by their predictions on slow cell cycle cells, possibly obtained with low levels of FBS, but for which no quantitative data are currently

available.

Since RevErb- $\alpha$  is a repressor of *Bmal1* and Bmal1 an activator of *RevErb- $\alpha$* , these two hypotheses correspond to two alternative mechanisms for a similar effect. Interestingly, an experimental study investigating the translational landscape of dividing cells reported an up-regulation of *RevErb- $\alpha$*  translation during the M phase [28].

This is one reason to favour this hypothesis. Furthermore, the activation of *RevErb- $\alpha$*  might be caused by various mechanisms [31]. For instance, the transcription factor c-Myc displays bursts of transcriptional activity during G1 phase just after mitosis and the S to G2/M transition of the cell cycle [32]. The c-Myc protein regulates its target genes through the same E-box DNA response element as the Clock/Bmal1 heterodimer. It is therefore conceivable that during the G2/M phase of the cell cycle, *RevErb- $\alpha$*  is positively regulated by c-Myc leading to the transcriptional repression of *Bmal1* [33]. In this scenario the E-box regulated *Per* and *Cry* genes are expected to be also up-regulated by the higher transcriptional activity of c-Myc. This is compatible with our simulations which show that the phase and period are resilient to variation of the coefficient synthesis for *Per* and *Cry*. An additional potential link between RevErb- $\alpha$  and the cell cycle machinery is provided by the recent observation that the Cyclin B-CDK complex can phosphorylate RevErb- $\alpha$  [34].

Our model also postulates a different interpretation of some of the results presented in [14] when cells are treated by a 2 hours pulse of dexamethasone. Indeed, instead of different autonomous cycling regimes, the model predicts temporary perturbations leading to shorter or longer peak-to-peak distances, but returning to the previous entrainment regime after some time, longer than the horizon used in the experiments.

Furthermore, in our coupled model, the phases between some of the clock gene products are shifted when entrained by a fast cell cycle. We are able to quantify these phase shifts and show that they concern mainly RevErb- $\alpha$  whose mRNA peaks are advanced by the periodic activation during mitosis. Other clock mRNAs and proteins are slightly delayed compared to their activator

Bmall. A prediction of the model is therefore that in quickly dividing cells, these protein peaks are shifted with respect to quiescent cells where such a phenomenon should not be observed.

*Acknowledgements.*

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