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Deterioration modelling of contact surfaces for a friction drive system

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ABSTRACT: This article presents a novel model of surface deterioration for a friction drive. For this basic transmission system, the difference between tangential speeds is linked with the production of contact force and at the same time with an energy transfer that deteriorates the contact surfaces. Thus, an optimal management between health state of components and use of energy resources is required. In a first step, the physics of the system is modeled in a deterministic way. Then, considering either random system parameters or random system inputs and usage, a complete stochastic model for the system deterioration is proposed. The developed model allows to link the deterioration evolution to the inputs and operating modes of the system; to assess the behavior of deterioration in critical stages, such as sharp motion and smooth motion. The advantages to design and to analyze such a model are finally discussed in terms of reliability-adaptive systems.

1 INTRODUCTION

The Remaining Useful Life (RUL) of an asset or system is defined as the time left from the current time to the end of the useful life. Prognosis of RUL is a widely studied topic in health management of resources for automated engineered. RUL prognosis has also an important role in the management of energy resources for e.g. autonomous devices. A good overview over existing methods for RUL prognosis is given in (Si, Wang, Hu, & Zhou 2011). Note that the meaning of “useful life” varies according to the studied engineering field, thus the owner of the asset is the one who defines the sense of useful life and its management.

Deterioration of components and failures affects directly the lifetime of assets, and consequently their usability and/or productivity. On the other hand, energy consumption is another critical variable to manage in relation with the deterioration behavior. For this reason, nowadays manufacturers or end users are becoming increasingly motivated to manage the complete life-cycle of an asset and to optimize the production process and its energy consumption using proactive strategies. Thus, an optimal management between health state of components and use of energy resources is required, which is defined in this paper as a “RUL-aware” operation.

The aim of this work is to develop a mathematical model for the deterioration of the contact surfaces of a friction drive system, which is a type of transmission

that uses two circular devices to transfer mechanical power by friction, used e.g. in some electrical bikes with two main components: wheel and DC-motor. The basic model of friction drive transmission relies on the assumption of equal tangential speeds of wheel and motor surfaces. However, the difference between speeds can not be always neglected because this is linked with the efficiency of mechanical transmission that drives the wheel and the production of contact force, which is associated with a transfer of energy that also deteriorates the contact surfaces. Then, the energy transfer is at the same time, the useful phenomenon and the source of deterioration and as such it requires to be properly modeled; thus, allowing an optimal control ensures both a sufficient drive power and an acceptable deterioration. As explained in Section 4, this work can then be seen as a required step towards developing a complete Reliability Adaptive Systems or RAS according to (Meyer & Sextro 2014).

We consider a special case of a friction drive system (roller-on-tire system) and we develop an analytical physics-based model for the deterioration of the driving contact surfaces. The developed model integrates the deterioration as one of the states of the system, thus it allows: a) to link the deterioration evolution to the inputs and operating modes of the system, b) to assess the behavior of deterioration in critical stages, such as sharp motion and smooth motion and c) to predict analytically an interval of useful lifetime before the total-failure-time of actuator, taking into account stochastic perturbations.

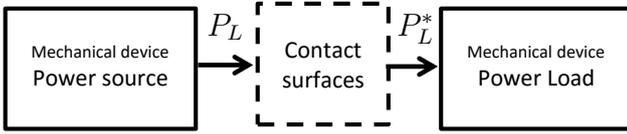


Figure 1: Losses of power in contact

The remainder of this paper is organized as follows. Section 2 presents the design and analysis of the deterioration model of the considered friction drive system. Section 2.1 contains the general definition of the particular friction drive which here is called “roller-on-tire” system. In a first step, in Section 2.2, the physics of the system, and in particular the link between deterioration dynamics and energy transfer at the friction surface, is modeled in a deterministic way. In Section 2.3 an useful space state representation is presented. Then, considering either random system parameters or random system inputs and usage, a complete stochastic model for the system deterioration is proposed in Section 2.4.

Section 3 shows the analysis of simulations for a case study. Finally, plans for future work directions are given in Section 4 in the framework of RAS.

2 FRICTION DRIVE SYSTEM MODELLING

Figure 1 presents the basic principles of the mechanical devices considered in this work: a power transmitted from the source to the load, P_L , is higher than the power which actually causes the motion, P_L^* . This phenomenon is modeled under the general hypothesis that the loss of efficiency in the conversion from energy to motion can be an estimable image of the deterioration of materials in contact.

2.1 Roller-on-tire system description

The “roller-on-tire” system is a friction drive composed by a driven device and a motor, as depicted in figure 2, for which it is supposed that: a) both contact surfaces, the rotor of the motor and the external part of the driven device, deteriorate, b) both surface deterioration of the motor and the tire reach eventually a threshold above which the system is considered failed, and c) an inversion of motion sense cannot occur at any time.

Symbols of the equations and units are shown in Table 1.

2.2 Analytical physics-based modelling

The mechanical analysis is based on the Dahl model and LuGre model of friction, which are widely studied in the literature of mechanics. A good overview about those models can be read in (Geffen 2009) and (Armstrong-Helouvy & Canudas de Wit 1996). These models represent the friction force with the components of the Stribeck friction effect, for which

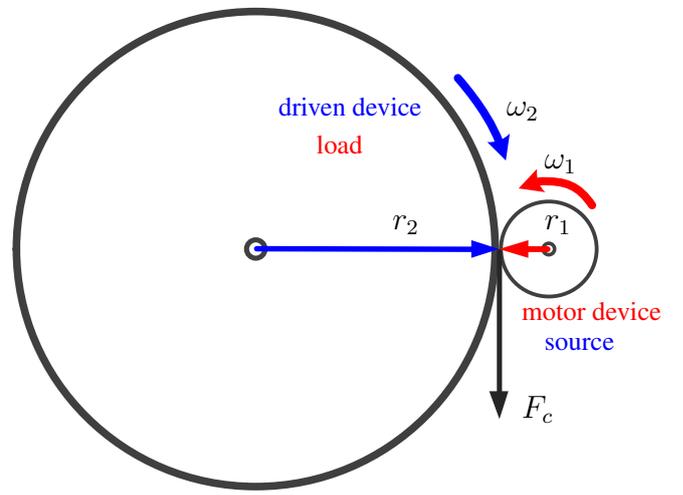


Figure 2: Basic roller-on-tire motor system

Table 1: Parameters, units and symbols

Symbol	Units	Physical meaning
v_1	$[m/s]$	Tangential speed of the motor
v_2	$[m/s]$	Tangential speed of the driven device
ω_1	$[rad/s]$	Angular speed of the motor
ω_2	$[rad/s]$	Angular speed of the driven device
$\dot{\omega}_1$	$[rad/s^2]$	Angular acceleration of the motor
$\dot{\omega}_2$	$[rad/s^2]$	Angular acceleration of the driven device
r_1	$[m]$	External radius of the motor
r_2	$[m]$	External radius of the driven device
B_1	$[Kgm^2/s]$	Viscous damping coefficient of the motor
B_2	$[Kgm^2/s]$	Viscous damping coefficient of the driven device
J_1	$[Kgm^2]$	Moment of inertia of the motor
J_2	$[Kgm^2]$	Moment of inertia of the driven device
T_m	$[Nm]$	Torque of the motor
T_L	$[Nm]$	Load torque seen by the motor
T_L^*	$[Nm]$	Source torque observed by the driven device
K_m	$[Vs/rad]$	Motor back electromotive force constant
I	$[A]$	Electrical current of the motor
α	$[Ns/m]$	Contact quality coefficient

the friction force has an inverse relation with respect to the speed; the Coulomb friction, for which the force remains as a constant with respect to the speed at the beginning of motion; and the viscous friction, for which the friction force is proportional to the speed. In the present contribution, Stribeck friction effect and Coulomb friction are considered negligible; that is, only the viscous friction is taken into account, due to the fact that it does not exist any possibility of inversion of the motion sense.

Here F_c is assumed as a frictional force, tangential to both the motor and the driven devices, which causes a rotational torque over the driven device. A similar approximation of the law of friction by a continuous function of velocity is analysed in (Popov 2010). Consequently, the friction force component depicted in Equation (1), depends on the difference Δ_v between the tangential speeds of motor and driven device, v_1 and v_2 respectively, and the coefficient α , which in this paper is called contact quality coefficient and that corresponds to the viscous friction coefficient in the classic context of friction components modelling.

$$F_c = \alpha(v_1 - v_2) = \alpha(r_1\omega_1 - r_2\omega_2) = \alpha\Delta_v \quad (1)$$

The parameter α is classically considered to be constant, but in this paper it is treated as a time-varying parameter. In some sense, this α gives an initial idea about the quality of contact between both

rolling devices in each time of the motion. Then, because of the frictional phenomena, the condition of contact depends on the deterioration of materials and varies with time, i.e. $\alpha = f(D, t) \succ 0$.

Thus both the torque produced by the motor and transferred to the load $T_L(t)$ and the torque observed by the driven device $T_L^*(t)$ depend on $F_c(t)$ according to equations (2) and (3). In this paper, dependence on time is not written for convenience.

$$T_L = F_c r_1 \quad (2)$$

$$T_L^* = F_c r_2 \quad (3)$$

The system dynamics using Newton's laws of motion can be written as follows:

$$\Sigma T_1 = J_1 \dot{\omega}_1 = T_m - T_L - B_1 \omega_1 \quad (4)$$

$$\dot{\omega}_1 = \frac{1}{J_1} (K_m I - r_1 \alpha (r_1 \omega_1 - r_2 \omega_2) - B_1 \omega_1)$$

$$\Sigma T_2 = J_2 \dot{\omega}_2 = T_L^* - B_2 \omega_2 \quad (5)$$

$$\dot{\omega}_2 = \frac{1}{J_2} (r_2 \alpha (r_1 \omega_1 - r_2 \omega_2) - B_2 \omega_2)$$

Equations (4) and (5) can be rewritten in terms of power multiplying them by ω_1 and ω_2 respectively as follows:

$$J_1 \dot{\omega}_1 \omega_1 = K_m I \omega_1 - T_L \omega_1 - B_1 \omega_1^2 \quad (6)$$

$$J_2 \dot{\omega}_2 \omega_2 = T_L^* \omega_2 - B_2 \omega_2^2 \quad (7)$$

where terms in equations are shown in Table 2:

Table 2: Terms of power equations

Term	Physical meaning	Symbol
$J_1 \dot{\omega}_1 \omega_1$	Total power in the motor	P_{TM}
$K_m I \omega_1$	Electric power in the motor	P_{motor}
$T_L \omega_1$	Power transferred to the load	P_L
$B_1 \omega_1^2$	Power caused by viscous damping B_1	P_{B1}
$J_2 \dot{\omega}_2 \omega_2$	Total power for the driven device	P_{TW}
$T_L^* \omega_2$	Power caused by contact observed by the driven device	P_L^*
$B_2 \omega_2^2$	Power caused by viscous damping B_2	P_{B2}

Taking into account Equations (6) and (7), power in contact P_c can be expressed as follows:

$$P_c = P_L - P_L^* = T_L \omega_1 - T_L^* \omega_2 \quad (8)$$

$$P_c = F_c (r_1 \omega_1 - r_2 \omega_2) = F_c \Delta_v$$

Using Equation (1) this takes the form:

$$P_c = \alpha (r_1 \omega_1 - r_2 \omega_2)^2 = \alpha \Delta_v^2 \quad (9)$$

We define the dynamic efficiency of the transmission $\eta_c(t)$ as:

$$\eta_c = P_L^* / P_L = (P_L - P_c) / P_L \quad (10)$$

which is equivalent to:

$$\eta_c = F_c r_2 \omega_2 / F_c r_1 \omega_1 = \frac{r_2 \omega_2}{r_1 \omega_1} = \frac{v_2}{v_1} \quad (11)$$

We assume that it is possible to measure the speeds v_1 and v_2 (or equivalently, ω_1 and ω_2) in this kind of mechanisms. Thus η can be computed dynamically.

The energy dissipated in the contact E_c between the surfaces in roller-on-tire system can be obtained from (9). Thus E_c depends on the speed between the surfaces as follows:

$$E_c = \int_{t_1}^{t_2} P_c dt = \int_{t_1}^{t_2} \alpha \Delta_v^2 dt \quad (12)$$

The dissipated energy could be considered as an image of the heat and material losses produced at the contact level during traction, as considered Similar conclusion were found by (Meyer & Sextro 2014). Thus, if heat losses are neglected, deterioration of surfaces D_c can be considered as proportional to the dissipated energy in the contact:

$$D = c E_c = c \int_{t_1}^{t_2} P_c dt = c \int_{t_1}^{t_2} \alpha \Delta_v^2 dt \quad (13)$$

where c is a proportionality factor that relates deteriorated material because of friction with the energy dissipated. That is, here the deterioration is considered as an image of the dissipated energy at the contact level during power transmission.

Equation (13) shows that the dynamics of the system and the contact surfaces deterioration are linked through α . From Equation (13) and since $\alpha = f(D)$, a nonlinear variation of the deterioration with respect to time according can be obtained:

$$\dot{D} = c \alpha \Delta_v^2 = H_{nonlinear}(\omega_1, \omega_2, D) \quad (14)$$

At the same time, α varies depending on the deterioration of materials. It is assumed that the bigger D , the lower α and that D is monotonically increasing and bounded until D_{max} . We define the maximum value of deterioration D_{max} , as the value of D in which the system is considered completely failed. In this paper, it is considered that the evolution of α depends on the evolution of the deterioration D as depicted in Figure 3. Consequently, a first order linear variation of α , with respect to D with slope $m > 0$, $m \in \mathbb{R}^+$ and initial value $b > 0$, $b \in \mathbb{R}^+$, is defined as:

$$\alpha = -mD + b \quad (15)$$

From Equations (14) and (15), we get:

$$\dot{D} = (-cmD + cb)(r_1 \omega_1 - r_2 \omega_2)^2 \quad (16)$$

$$\dot{D} = -m \underbrace{c \Delta_v^2}_{d(t)} D + b \underbrace{c \Delta_v^2}_{d(t)} \quad (17)$$

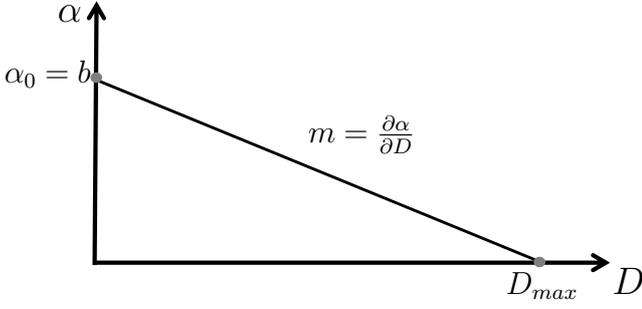


Figure 3: α as a function of D

Taking into account the term $d(t) = c(r_1\omega_1 - r_2\omega_2)^2$, Equation (17) can be rewritten as follows:

$$\dot{D} = -md(t)D + bd(t) \quad (18)$$

We can compute the maximum value of the deterioration with respect to time D_{max} as:

$$D_{max} \triangleq \lim_{t \rightarrow +\infty} D(t) \quad (19)$$

This can be calculated using Equation (18) with $\dot{D} = 0$, thus:

$$-mD_{max} + b = 0 \quad (20)$$

$$D_{max} = b/m = \alpha(0)/m \quad (21)$$

In a complementary way, we define the normalized deterioration as:

$$\bar{D} \triangleq D(t)/D_{max} = (m/\alpha(0))D(t) \quad (22)$$

From Equation (15), we get the special form:

$$D(\alpha) = (b - \alpha)/m = (\alpha(0) - \alpha)/m \quad (23)$$

Since $\Delta_v = v_1 - v_2 = r_1\omega_1 - r_2\omega_2$ and using (4) and (5):

$$\begin{aligned} \dot{\Delta}_v = & (r_1/J_1)(K_m I - \alpha r_1 \Delta_v - B_1 \omega_1) \\ & - (r_2/J_2)(\alpha r_2 \Delta_v - B_2 \omega_2) \end{aligned} \quad (24)$$

Equation (24) shows that it is possible to estimate the value of α from the measured speeds (recall that measuring the speeds is considered feasible in this kind of mechanisms), and assuming the other parameters of the systems as constant. Let denote this estimated value as $\hat{\alpha}$. Therefore using Equation (23), the deterioration \hat{D} can be estimated by:

$$\hat{D} = (\alpha(0) - \hat{\alpha})/m \quad (25)$$

Consequently, using equations (21), (22) and (25) it is obtained the normalized estimation of deterioration $\hat{\bar{D}}$:

$$\hat{\bar{D}} = \hat{D}/D_{max} = (\alpha(0) - \hat{\alpha})/\alpha(0) \quad (26)$$

Deriving Equation (23) with respect to time, and using Equation (14), we get:

$$\dot{D} = -(1/m)\dot{\alpha} \quad (27)$$

$$\dot{\alpha} = -mc\dot{D} = -mc\alpha\Delta_v^2 \quad (28)$$

Equation (28) can be rewritten taking into account Equation (9):

$$\alpha = -mc \int_{t_1}^{t_2} P_c dt \quad (29)$$

Therefore:

$$\alpha = -mcE_c + \alpha(0) \quad (30)$$

Summarizing, assuming a monotonically increasing of deterioration, the proposed model shows that roller-on-tire system reaches a maximum value of deterioration D_{max} , above which the transmission is consider failed, which depends on the initial value of the contact quality coefficient $\alpha(0)$ and the slope m , which represents the variation of $\alpha(0)$ with respect to deterioration of material D . At the same time the normalized estimation of deterioration $\hat{\bar{D}}$ can be obtained from $\alpha(0)$ and its estimation $\hat{\alpha}$. The estimated coefficient $\hat{\alpha}$ can measure the loss of material or the modification of the surface properties at the contact level, i.e. the material that allows the contact (or the existence of mechanical transmission). At the same time $\hat{\alpha}$ establishes a relation between material of contact and energy of contact.

2.3 State-space model for the roller-on-tire system

In accordance with the above, roller-on-tire system is an uncertain system which depends on time-varying unknown-but-bounded uncertain parameters. Taking into account the states:

$$x = \begin{pmatrix} \omega_1 \\ \omega_2 \\ D \end{pmatrix}, \quad (31)$$

the control input $u = I$ and the output y , the representation of the system can be expressed as:

$$\begin{cases} \dot{x} = f(x) + Bu \\ y = Cx \end{cases} \quad (32)$$

B is an input matrix and C the output matrix. In an explicit form, the representation of the system is:

$$f(x) = \begin{pmatrix} -\frac{1}{J_1}(B_1 + \alpha r_1^2)\omega_1 + \frac{1}{J_1}\alpha r_1 r_2 \omega_2 \\ \frac{1}{J_2}\alpha r_2 r_1 \omega_1 - \frac{1}{J_2}(B_2 + \alpha r_2^2)\omega_2 \\ c\alpha(r_1\omega_1 - r_2\omega_2)^2 \end{pmatrix} \quad (33)$$

$$B = \begin{bmatrix} \frac{K_m}{J_1} \\ 0 \\ 0 \end{bmatrix}; C = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}; u = I$$

Remark that in this case the non-linearity of the system is due to the introduction of the state D .

2.4 Introducing randomness in the model

Randomness in the model can be introduced in two complementary modes: a) internal, to model the uncertainty on the parameters m and b (which are used to relate a with D) for a given system, and the system-to-system variability and b) external, to model the variability of the operating conditions and the usage system, in this case taking into account the input u .

2.4.1 Uncertain/random parameters

In Equation (15) $b \geq 0$ and $m \geq 0$ are considered as unknown parameters, but which belong to a given known interval taking into account real applications. Thus a normal distribution is introduced to represent them:

$$m \sim \mathcal{N}(m_m, \sigma_m^2), m_m > 0 \quad (34)$$

$$b \sim \mathcal{N}(b_m, \sigma_b^2), b_m > 0$$

where m_m and σ_m are the mean value and the standard deviation of the slope m respectively, and b_m and σ_b are the mean value and the standard deviation of b respectively.

As depicted in the shaded area in Figure 4 and according to Equations (15) and (35), the behavior of α with respect to D constitutes a bi-dimensional space of variation. The solid line inside the shaded area is an example of probable behavior.

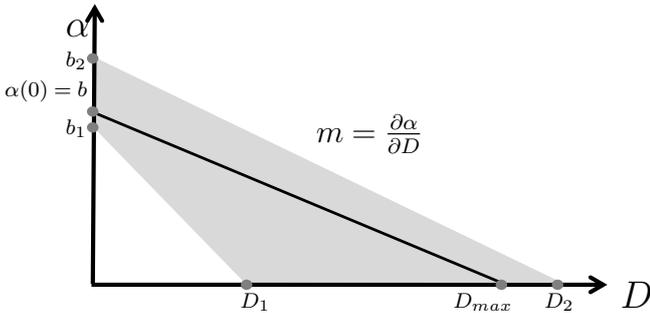


Figure 4: α as a function of D

2.4.2 Variable operating conditions and usage

The developed model is single input $u = I$. In this case, the variability of the operating conditions and the usage system is represented as the variation of I .

Consider an input I as a square signal. The times t_h , in which I is in high and t_l , in which I is in low can vary randomly. Thus an exponential distribution is introduced to represent it:

$$t_l \sim \text{Exp}(1/\mu_{tl}), 0 < \mu_{tl} \quad (35)$$

$$t_h \sim \text{Exp}(1/\mu_{th}), 0 < \mu_{tl} < \mu_{th}$$

where μ_{tl} and μ_{th} are the mean values of t_l and t_h respectively.

The deterministic operational mode, the internal mode of randomness and the external mode of randomness are used in a case study analysis in Section 3.

3 CASE STUDY ANALYSIS

To choose the parameters for simulations in order to validate the usefulness of the model, the contributions of (Huang & Nagurka 2003) and (Rodriguez 2014) were analyzed. In the first article, a similar workbench has a built-in bike wheel to model viscous and dry friction at the wheel bearing. The second contribution is a master-thesis developed in GIPSA-Lab (CNRS-France, Grenoble-INP, University Grenoble Alpes), which analyses the implementation of a real friction drive in an electrical bicycle. Table 3 shows the chosen parameters.

Table 3: Chosen parameters

Parameter	Value	Unit
B_1	6.36×10^{-3}	$[Kgm^2/s]$
B_2	1.76×10^{-3}	$[Kgm^2/s]$
J_1	3.47×10^{-4}	$[Kgm^2]$
J_2	0.2	$[Kgm^2]$
r_1	0.0315	m
r_2	0.35	m
K_m	0.0477465	$[Vs/rad]$

3.1 Deterministic operational mode

3.1.1 Sharp stage of motion

The system model is simulated with an input step signal I with amplitude = 20A. Figure 5 shows the behavior of the power in the system.

Here, P_L the transferred power to the load, and P_L^* , the power seen by the driven device have a high value only at the beginning, and such as it was supposed $P_L > P_L^*$. The difference between P_L and P_L^* reflects the loss in contact, primarily at the beginning of motion, i.e. the sharp stage.

Remark that P_L and P_L^* reach a peak in the sharp stage, and after they drop; while P_{motor} , the electrical power of the motor, and P_{B1} , the power that appears as a result of the viscous damping parameter B_1 reach high and near values. P_L^* and P_{B2} are much lower because they depend on ω_2 which is lower than ω_1 . Here, it is possible to see that there is a considerable influence of the viscous damping parameter B_1 in the consumption of energy, i.e. the motor must provide more power to drive its own viscous damping parameter B_1 .

Figure 6 shows the behavior of the difference of power for given values of α with respect to time. Experimentally, it was found a maximum peak of this difference, i.e. the minimum efficiency η when α is

equal to 5.25. It means that the increasing of α tends to give lower losses but it do not necessarily produces the highest peak of losses. These dynamic changes reflect the importance to estimate and possibly to control the value of α .

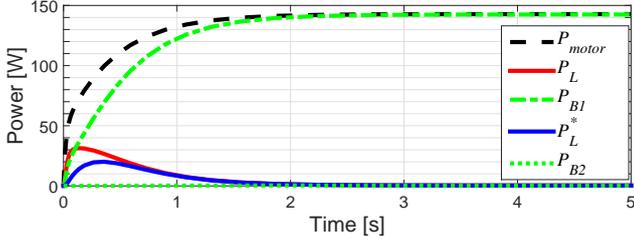


Figure 5: Behavior of power in roller-on-tire system

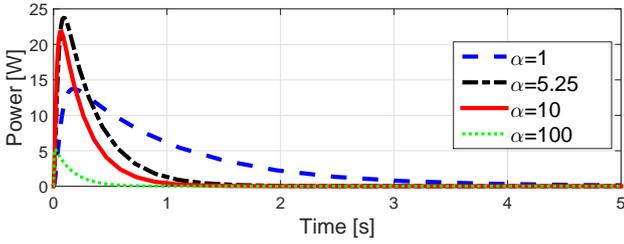


Figure 6: Loss between P_L and P_L^* for given values of α

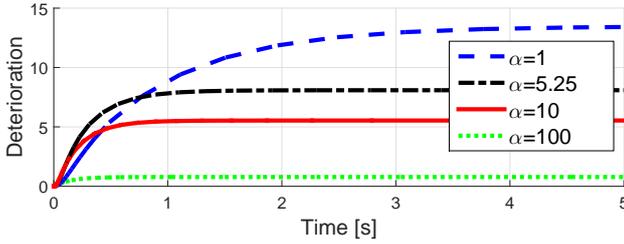


Figure 7: Deterioration for given values of α for *sharp stage* of motion. The higher the Δ_v , the higher the deterioration of material.

Figure 7 shows the behavior of the instantaneous D for a given parameter $c = 1$ for the same given values of α than the figure 6. It is evident that D is always increasing and that the highest values are related with power losses. It is also remarkable that the highest consumption of contact energy (material of contact) happen in the first seconds for every value of α , i.e. the sharp stage of motion when also Δ_v is higher.

3.1.2 Smooth stage of motion

Given values $c=1$, $m=0.01$ and $b=10$ are determined arbitrarily in the framework of possible implementation and taking into account previous simulations in order to introduce the variation of α according to Equation (15). Figure 8 shows the behavior of states v_1 , v_2 and D . Here is possible to see the behavior of deterioration at the smooth stage of motion, i.e. when Δ_v is lower, until the total failure. Deterioration reaches the D_{max} value at 300 hours of use for the given scenario.

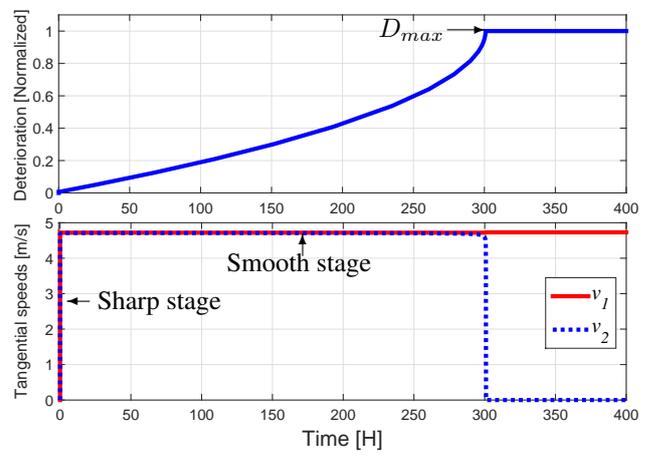


Figure 8: Deterioration D , tangential speed of motor v_1 and tangential speed of wheel v_2 for a step input. It shows the failure of system at 300h.

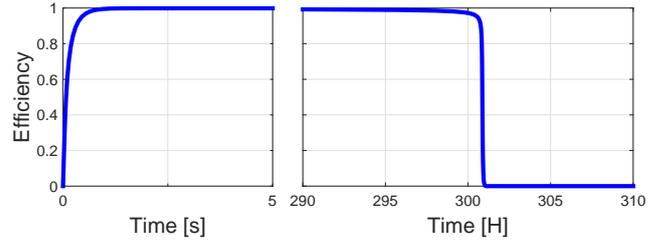


Figure 9: Behavior of efficiency η for sharp stage and failure stage. Step input.

Finally, the efficiency η of the mechanical power transmission is evaluated in the sharp stage and in the failure stage as depicted in Figure 9. Remark that in the sharp stage the variation of η is sharp also. On the other hand, η begins to variate before of the total failure and it has a slow variation.

3.1.3 Variable behavior of input

A square signal is introduced to represent several cycles of use. In this case t_h and t_l are the times in which the signal is in high and low respectively. One use cycle is the time in which the contact material deteriorate, i.e. when $\Delta_v > 0$.

Figure 10 shows the states v_1 , v_2 and D with an fixed input of $t_h = 10000s$ and $t_l = 10s$ chosen arbitrarily. As a result, v_1 continues responding to the input signal, but not v_2 . Here is shown that the roller-on-tire system reaches the D_{max} near to 96.7h. It means that with multiple cycles of activation, an earlier D_{max} is reached. Figure 11 shows the behavior of α for the same scenario.

3.2 Stochastic operational mode

3.2.1 Internal mode of randomness

According to Section 2.4 we can introduce randomness in the model. Firstly, a fixed step input is introduced to the system, which represents a cyclical behavior, where t_h and t_l are constant.

Figure 12 shows D for 100 simulations. Here m and b are chosen randomly using a normal distribution with mean values of $m_m = 0.01$ and $b_m = 10$ respectively and with standard deviations of $\sigma_m = 0.001$ and $\sigma_b = 1$ respectively. The different behaviors are

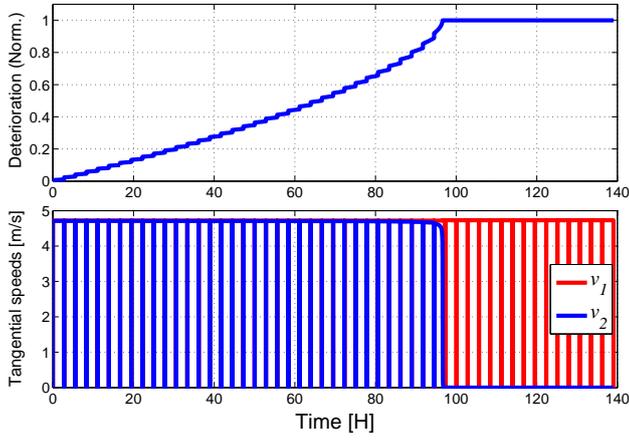


Figure 10: Deterioration D , tangential speed of motor v_1 and tangential speed of wheel v_2 for a square input with $t_h = 10000s$ and $t_l = 10s$. It shows the failure of system at 96.7h.

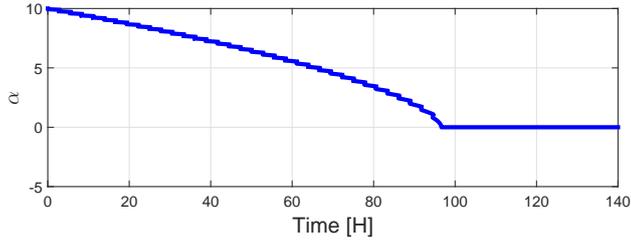


Figure 11: α for or a square input with $t_h = 10000s$ and $t_l = 10s$.

compared with an scenario with fixed values of $t_h = 10000s$ and $t_l = 10s$.

This simulation allows inferring that if it is possible to know the values of m and b since the beginning then is could be possible have a good estimation of time of failure.

3.2.2 External mode of randomness

Figure 13 shows D for 100 simulations. Here t_h and t_l are chosen randomly using an exponential distribution with mean values of $t_h = 10000s$ and $t_l = 10s$ respectively and parameters $b = 10$ and $m = 0.01$. The different behaviors are compared with an scenario with fixed values of $t_h = 10000s$ and $t_l = 10s$.

This kind of external mode of randomness is similar to real operation conditions, for which the t_h and

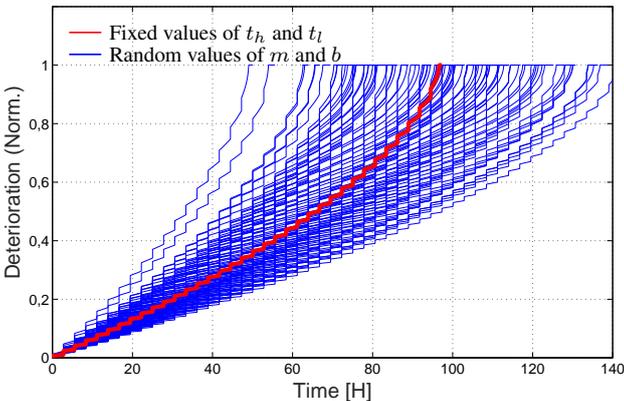


Figure 12: Internal mode of randomness. Blue lines: Deterioration D , for 100 random performances. m and b are chosen randomly using a normal distribution. Red line: simulation of performance for fixed values of $t_h = 10000s$ and $t_l = 10s$.

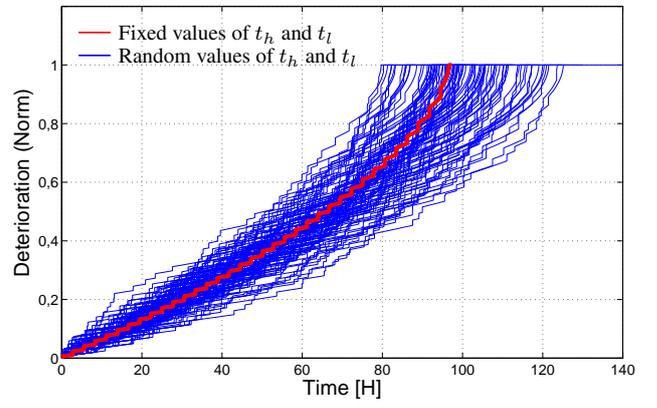


Figure 13: External mode of randomness. Blue lines: Deterioration D , for 100 random performances. t_h and t_l are chosen randomly using an exponential distribution with mean values of $t_h = 10000s$ $t_l = 10s$ respectively. Red line: simulation of performance for fixed values of $t_h = 10000s$ and $t_l = 10s$.

t_l are unknown. Results shows that despite of the randomness of t_h and t_l the deterioration behavior follows what seems a normal distribution. It could be useful, for example to estimate the failure time with an acceptable level of uncertainty.

4 FROM DETERIORATION MODELING TO THE DEVELOPMENT OF A RELIABILITY ADAPTIVE SYSTEM

Analytical physics-based models of degradation are useful to develop new techniques under the framework of Prognostic Health Management (PHM), which can be defined as the field of activities that links studies of failures in mechanisms to a system life-cycle management. Recently, type 5 of PHM so-called Reliability-Adaptive Systems or RAS has been introduced to its classification for (Rakowsky & Bertsche 2015).

In some systems, for example in the friction-based ones, the failure is imminent because of deterioration of materials in contact, and the main goal is trying to optimize the use of functioning resources until the failure. In other words, planned actions which tend to initiate changes of behavior of the component, rather than reacting to failures are needed. To achieve that, to lower work load or wear by selecting appropriate optimal system configurations of components is required according to (Meyer & Sextro 2014). Systems which possess this capability are called Reliability-Adaptive Systems or RAS by (Rakowsky 2006). In other words a reliability control can allow to manage the deterioration of components like in the self-optimizing mechatronic systems, which are, according to (Gausemeier, Rammig, Schäfer, & Sextro 2014), a class of intelligent technical systems able to autonomously adapt their behavior if user requirements or operating conditions change.

In the framework of PHM modern approaches the proactive actions are focused in system-level and component-level. Then, combination of experienced-

based, data-driven and model-based approaches (Byington, Watson, Roemer, Galie, McGroarty, & Savage 2003), seems to be an appropriate way to improve the efficiency of management proactive actions according to (Muller, Suhner, & Iung 2008). In this context, common goals for the proactive actions are a) the reduction of the probability of unexpected component failures in a reliable way and/or b) the feasible implementation on-line.

In this sense, component-level proactive strategies continue being explored (See for example (Nguyen, Dieulle, & Grall 2014)). Physics-based models can explain the phenomena of deterioration in a deterministic way, which can be useful to manage the useful lifetime of a component in control loop to get systems type RAS with feasible implementation. This is specially useful in embedded systems due the computational restrictions.

In this paper, we developed a deterioration model linking the system control input and the deterioration behavior, which can be seen as a first step towards the development of a comprehensive reliability adaptive system. The next step is using the information and the features of the model to estimate on-line the deterioration and the model parameters, to synthesize a reliability adaptive control law in order to manage the RAS taking into account jointly the different point of views of reliability, performance and energy efficiency.

5 CONCLUSIONS

The proposed model allows analytically to predict an interval of useful lifetime before the total-failure-time of actuator, including stochastic perturbations. The model takes into account the variation of the contact quality coefficient with respect to the deterioration of the contact-surface material, and this deterioration with respect to the difference of the tangential speeds. Results show that the model represents properly and dynamically the deterioration of surfaces depending of the difference of tangential speeds, i.e. the more the difference (sharp motion stage), the more deterioration. In the smooth motion stage, the estimation of deterioration depends on the initial estimation of the contact quality coefficient.

The estimation of contact quality coefficient is supported on the assumptions that the relative speed is known at every time-instant. Results show that if it is possible to know the value of contact quality coefficient at every time-instant, then it could be possible to have a good estimation of the failure time. It could be useful, for example to estimate the failure time with an acceptable level of uncertainty. Additionally, despite of the unknown input conditions, the deterioration behavior follows central tendency. The precision only depends on the size of the uncertainties on the system parameters and future system usages. Therefore, it could be feasible, for example to esti-

mate the failure time with an acceptable level of uncertainty.

This model can be probed in close loop scenarios, with the advantage of probing and simulating control techniques on reliability and fault tolerant control areas for a basic mechanical system. This is particularly useful in learning and researching about RAS systems. Indeed, since such a model would link the control and the reliability of the system, it opens the door to develop a control system which allows the device to adapt autonomously its behavior if user requirements or operating conditions change.

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