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Brazilian Congress structural balance analysis

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Abstract

In this work, we study the behavior of Brazilian politicians and political parties with the help of clustering algorithms for signed social networks. For this purpose, we extract and analyze a collection of signed networks representing voting sessions of the lower house of Brazilian National Congress. We process all available voting data for the period between 2011 and 2016, by considering voting similarities between members of the Congress to define weighted signed links. The solutions obtained by solving Correlation Clustering (CC) problems are the basis for investigating deputies voting networks as well as questions about loyalty, leadership, coalitions, political crisis, and social phenomena such as mediation and polarization.

Keywords

social network; signed graph; structural balance; Correlation Clustering; metaheuristic; politics

I INTRODUCTION

Structural balance theory is based on the notion of cognitive consistency between friendship and hostility. For example, an enemy of a friend is probably my enemy as well, while a friend of a friend is probably my friend or can become one (Heider, 1946). In simple terms, the interaction of individuals follows the tendency to create stable (albeit not certainly conflict-free) social groups. This can be specially interesting to study similarity and correlation networks, like those originated from common voting patterns, or alliances and disputes among parties or nations (Traag and Bruggeman, 2009; Macon et al., 2012; Doreian and Mrvar, 2015).

One appropriate criterion to measure the degree of balance in signed social networks is by solving the Correlation Clustering (CC) problem (Bansal et al., 2002; Demaine et al., 2006), which consists of partitioning a set of elements into clusters by analyzing the level of similarity between them. It aims to maximize the affinity inside each cluster (i.e. positive relationships) while, at the same time, minimizing the similarities between elements of different clusters (i.e. maximizing negative relationships).

The CC problem, which has been proved to be NP-hard (Bansal et al., 2002), can be applied in several areas, such as efficient document classification (Bansal et al., 2002), natural language processing (Elsner and Schudy, 2009), image segmentation (Kim et al., 2014) and, of course, signed social network analysis (Doreian and Mrvar, 1996; Brusco et al., 2011; Figueiredo and Moura, 2013; Levorato et al., 2015). With this objective, the level of balance in a social group can be used by social network researchers to study how (and if) a group evolves to a possible balanced state.

A relaxed version of the CC problem called Symmetric Relaxed Correlation Clustering (SRCC)

problem (Brusco et al., 2011; Figueiredo and Moura, 2013) can also be used to evaluate balance in signed social networks. This variant, although computationally harder to solve, allows the identification of special types of social relationship, such as polarization, mediation and differential popularity (Doreian and Mrvar, 2009), originally viewed as violations of structural balance.

We implemented an algorithm known as *ILS-CC* (Levorato et al., 2015), which can efficiently solve the aforementioned problems, providing useful information for social network analysis. Using the House of Cunha website (Andrade, 2016) and the work of Mendonça et al. (2015) as inspiration, we provide a novel analysis of Brazilian politics inside the Chamber of Deputies (CD). In Brazil, the Chamber of Deputies (*Câmara dos Deputados*) is the lower house of the National Congress, comprised of 513 federal deputies (from 25 political parties), elected by a proportional representation of votes to serve a four-year term. Based on the CD voting records, we generate several instances of signed social networks, according to certain grouping criteria. The clustering results obtained when invoking the *ILS-CC* procedure over these instances is the starting point of our study.

The analysis presented in this work can be applied to any network originated from voting patterns, where alliances and interest groups have strong influence.

This paper is organized as follows. Section II presents a literature review regarding Correlation Clustering problems and signed social network analysis. Section III describes the method applied to extract signed networks from the Chamber of Deputies voting data. Section IV presents an analysis of structural balance on the Chamber of Deputies voting networks, based on the solutions obtained by using our methodology. Finally, we show our conclusions in Section V.

II RELATED WORKS

Heider (1946) was the first to state Structural Balance (SB) theory in order to define sentiment relations among people belonging to the same social group (such as like/dislike, love/hate and cooperation/competitiveness). Signed graphs were later applied by Cartwright and Harary (1956), formalizing SB theory which affirmed that a stabilized social group could be divided into two mutually hostile subgroups (or clusters), each having internal solidarity. Davis (1967) then proposed the more general notion of "weak balance" or clusterable signed graph, when a balanced social group can be divided into two or more mutually antagonistic subgroups, each having internal solidarity.

When solving a clustering problem, one wants to find the most balanced partition¹ of a signed graph. Using structural balance as a measure, the clustering problem is equivalent to solving the optimization problem called Correlation Clustering (CC). To our knowledge, this problem was first addressed by Doreian and Mrvar (1996) (although not under this name), who provided a heuristic solution method for analyzing structural balance on real-world social networks. Their method was implemented in software Pajek (Batagelj and Mrvar, 2008). Having a document clustering problem in mind, Bansal et al. (2002) formalized the unweighted version of the CC problem and also discussed its NP-completeness proof. Later, Demaine et al. (2006) addressed the weighted version of the problem. Integer linear programming (ILP) can be used to solve the CC problem optimally (Figueiredo and Moura, 2013), but only if the number of elements is small. Since it consists of a NP-hard minimization problem, the only available solutions for larger instances are either heuristic or approximate. The solution of the CC problem and of

¹A partition is here defined as the division of the set of vertices V into non-overlapping and non-empty subsets.

some of its variants has already been applied in several areas, such as portfolio analysis in risk management (Harary et al., 2003; Huffner et al., 2010), biological systems (DasGupta et al., 2007; Huffner et al., 2010), grouping of genes (Bhattacharya and De, 2008), efficient document classification (Bansal et al., 2002), image segmentation (Kim et al., 2014) and community structure (Traag and Bruggeman, 2009).

In Yang et al. (2007), the CC problem is known as *community mining* and an agent-based heuristic called FEC is proposed to obtain its solution. Genetic algorithms have also been applied to document clustering, using the CC problem as objective function (Zhang et al., 2008). Lately, Drummond et al. (2013) presented a Greedy Randomized Adaptive Search Procedure (GRASP) (Feo and Resende, 1995) implementation that provides an efficient solution to the CC problem in networks of up to 8000 vertices. Then, based on this method, Levorato et al. (2015) introduced sequential and parallel ILS (Iterated Local Search) (Lourenço et al., 2003) procedures for the CC problem (known as *ILS – CC*), which outperformed other solution methods from the literature on three huge real-world signed social networks. Similarly to Mendonça et al. (2015), in this work, we will use the *ILS – CC* algorithm to evaluate the imbalance of voting networks.

Apart from the CC problem, alternative measures to structural balance and the associated clustering problems have also been discussed in the literature. In Doreian and Mrvar (2009), the definition of a k -balanced signed graph was informally extended in order to include relevant processes (polarization, mediation, differential popularity and subgroup internal hostility) that were originally viewed as violations of structural balance. For example, the existence of a group of individuals who share only positive relationships with everyone in the network counts as imbalance in the CC Problem. Nonetheless, the individuals in this group could be identified as mediators (i.e. their relations probably won't change over time) and, as pointed in Doreian and Mrvar (2009), their relations should not be considered as a contribution to the imbalance of the network.

Using this new definition, structural balance was generalized to a version labeled as *relaxed structural balance* (Doreian and Mrvar, 2009). Similarly to the CC problem, measuring the relaxed structural balance can be accomplished through the solution to the Relaxed Correlation Clustering (RCC) problem. It is originally defined on asymmetric relations between clusters (Figueiredo and Moura, 2013); however, a redefinition of relaxed imbalance of a partition P that takes into account only symmetric relationships is also available. This gives rise to a new graph clustering problem, the Symmetric Relaxed Correlation Clustering (SRCC) Problem (Figueiredo and Moura, 2013), which will be used in this work. The SRCC problem allows us to analyze mediation processes (positive and negative). That is not the case of the RCC problem, where mediation and differential popularity cannot be pointed out.

It is worth noting that the SRCC problem is closely related with the CC problem but it is not a particular case nor is a generalization. Actually, each feasible solution (a graph partition) of the SRCC problem is also feasible in the CC problem but the problems have different cost functions, i.e., there are different ways of evaluating the imbalance of a partition. The SRCC problem is intuitively as difficult as the CC problem and is indeed a NP-hard problem (Figueiredo and Moura, 2013).

Two solution methods were initially presented in the literature for RCC problems: a greedy heuristic approach (Doreian and Mrvar, 2009) and a branch-and-bound procedure (Brusco et al., 2011). Computational experiments with both procedures were reported over literature instances with up to 29 vertices and for random instances with up to 40 vertices (Doreian and Mrvar, 2009;

Brusco et al., 2011). We extended the ILS procedure to solve the SRCC problem, by applying additional data structures and a new objective function to evaluate the partition (Figueiredo et al., 2016). As far as we know, the *ILS – CC* algorithm is the only metaheuristic approach that has been used to solve RCC problems.

Previous works have employed signed graph clustering methods to analyze networks of international alliances and disputes (Traag and Bruggeman, 2009; Macon et al., 2012; Doreian and Mrvar, 2015). In Levorato et al. (2015), by using the *ILS – CC* algorithm, we presented a historical and geopolitical analysis of the results obtained from the voting on resolutions in the United Nations General Assembly (UNGA). Mendonça et al. (2015) have then applied a parallel version of the *ILS – CC* algorithm to analyze a collection of signed networks representing voting sessions of the European Parliament. The obtained results were compared to a selection of community detection algorithms designed to process only positive links.

Several authors studied the voting behavior of politicians. As far the European Parliament (EP) is concerned, Hix and Noury (2009) compared voting behavior of Members of the European Parliament (MEPs) in different periods, analyzing issues such as party cohesion and coalition formation. On their turn, Hix (2002) evaluated different questions regarding voting behavior in the EP, including personal policy preferences, national party and European party disciplines.

In particular, regarding Brazil, Ames (1995) developed a model of legislative voting based on the operation of Brazil’s political institutions. Mainwaring and Liñán (1997) analyzed party discipline in the Brazilian constitutional congress of 1987–88. Figueiredo and Limongi (2000) analyzed how Brazilian presidents have succeeded by relying on the support of disciplined parties in order to get their agendas approved in the Congress. Calvão et al. (2015) performed an extensive analysis of data sets available for Brazilian proportional elections of legislators and city councilors throughout the period 1970–2014, plus a comparative analysis of elections for legislative positions, in different states and years.

III NETWORK EXTRACTION

In this section, we explain the retrieval of raw voting data, and how we extracted signed networks from it.

3.1 Brazilian Chamber of Deputies

The Chamber of Deputies (CD) provides web services² which supply information about each of its members, including the vote cast by a specific deputy for each proposition evaluated at the CD. A deputy is described by its name, state (one of 27 Brazilian Federative Units) and political party.

For a given proposition, a deputy can express his vote in either of four ways (Câmara, 2016): *Sim* (For: the deputy wants the proposition to be accepted), *Não* (Against: s/he wants the proposition to be rejected), *Abstenção* (Abstain: s/he refuses to take part in the election and does not vote; equivalent to a white vote) and *Obstrução* (Filibuster: a form of obstruction, where debate over a proposition is extended, in order to delay or entirely prevent a vote on the proposal).

Besides the previous votes, a deputy may not vote at all, which leads to a fifth vote type: *Ausência* (Absent: the deputy was not present during the voting session).

²Please visit <http://www2.camara.leg.br/transparencia/dados-abertos/dados-abertos-legislativo/webservices>

The Chamber of Deputies' web services provide raw voting data, which describe the behavior of deputies apart from the others. Nonetheless, since a network is naturally relational (relationships between individuals are the product of their opinion about topics of interest), voting data has to be processed to generate the networks we wish to analyze.

3.2 Extraction algorithm

The extraction method here explained is based on the work of Mendonça et al. (2015). However, this procedure is being applied to Brazilian voting networks for the first time, which demanded an extension to the original algorithm, for filibuster treatment. It starts with a comparison between all pairs of deputies, analyzing the similarity of their voting choices. The obtained measures make up what is known as the agreement matrix M . Each element m_{uv} of this matrix indicates the average agreement between two deputies u and v , in other words, their level of accordance taking into consideration all propositions voted during a given time period.

While filtering the results is a relatively simple task, processing agreement scores may seriously alter the resulting network, depending on the methodology applied. Given a certain pair of deputies u and v and a proposition p_i , the proposition-wise agreement score $m_{uv}(p_i)$ is determined by comparing the votes of both deputies. It ranges from -1 if they fully disagree (one voted FOR and the other AGAINST), to +1 if they entirely agree (they share the same vote: FOR or AGAINST).

As previously stated, a voting record may contain, besides FOR and AGAINST, other values which should be equally taken into account. The first case refers to absence of one deputy or both of them (it is worth remembering that the analysis is based on pairs of deputies). The general approach is to leave out all propositions p_i that fall into this case (Porter et al., 2005; Dal Maso et al., 2014). Since certain deputies have low attendance rates, this might lead to distorted agreement or disagreement average scores, due to the small number of common voting sessions. To prevent this, we assume a neutral score of zero if at least one deputy is absent when voting a given proposition.

The abstention process is more complicated to understand. For example, if the political party supports a completely different view from the deputy, such pressure may be enough to lead him/her to take a step towards abstention, despite the fact that s/he is FOR or AGAINST the proposition under analysis. Similarly, abstention may simply represent the deputy's neutral position when a specific topic is proposed (i.e. the deputy does not care whether or not the subject is approved). Literature provides different views to deal with ABSTAIN-FOR, ABSTAIN-AGAINST and ABSTAIN-ABSTAIN situations (Macon et al., 2012; Porter et al., 2005; Dal Maso et al., 2014). In this work, we make use of two different ways of calculating the scores. The first one (Table 1) treats abstention as half an agreement whenever it is paired with FOR, AGAINST or other abstention, yielding a value of +0.5. In the second one (Table 2), whenever two deputies abstain at the same time, this is viewed as a full agreement (+1 value). As opposed to that, if only one abstains, a zero score is assigned, since there is not sufficient information to assert they are in agreement or disagreement. So to make things more clear, absence was not included in the tables.

The last case is filibuster (or obstruction), a vote choice specific to the Brazilian Congress, which does not occur in the European Parliament and was, therefore, not studied by Mendonça et al. (2015). Such practice is used to create difficulties or hindrances in a systematic way to delay or impede the approval of a bill in parliament. It is normally used by minority groups

which do not have the necessary number of representatives to effectively hold back a decision taken by the majority. Therefore, any vote marked as obstruction is here regarded as AGAINST.

| | FOR | ABSTAIN | AGAINST |
|---------|------|---------|---------|
| FOR | +1 | +0.5 | -1 |
| ABSTAIN | +0.5 | +0.5 | +0.5 |
| AGAINST | -1 | +0.5 | +1 |

Table 1: Vote weights representing abstention as half an agreement Mendonça et al. (2015).

| | FOR | ABSTAIN | AGAINST |
|---------|-----|---------|---------|
| FOR | +1 | 0 | -1 |
| ABSTAIN | 0 | +1 | 0 |
| AGAINST | -1 | 0 | +1 |

Table 2: Vote weights representing abstention as absence of opinion Mendonça et al. (2015).

The proposition-wise agreement score is fully specified by choosing one of the previous processing strategies. By averaging this score over all considered propositions, the average agreement can be calculated (Mendonça et al., 2015). In a formal way, consider two users u and v , as well as the propositions resulting from the filtering stage: p_1, \dots, p_ℓ , for which both u and v voted. The average agreement m_{uv} between these two deputies is:

$$m_{uv} = \frac{1}{\ell} \sum_{i=1}^{\ell} m_{uv}(p_i) \quad (1)$$

Similarly to the work of Mendonça et al. (2015), we generated one signed graph for each year (from 2011 until June 2016), taking into account all the voting sessions in that year. Graph edges with weight smaller than 0.001 were removed from the graph. The set of vertices in each signed graph represents the list of deputies who voted at least one time in the corresponding year.

IV STRUCTURAL BALANCE ANALYSIS

In this section, based on the clustering results obtained with the ILS-CC algorithm on the graphs extracted according to Section 3.2, we investigate some aspects of Brazilian politics in the Chamber of Deputies, including loyalty, leadership, coalition, crisis, as well as social phenomena such as mediation and polarization.

As explained in the previous section, we followed two approaches when generating voting networks for each year in the period between January 2011 and June 2016. We will refer to each network as either v1 or v2, depending on the strategy while dealing with abstentions:

- v1** : abstention is worth half an agreement (+0.5), whenever it is paired with any kind of vote (FOR, AGAINST or other abstention);
- v2** : abstention is viewed as full agreement (+1 value) only if both deputies abstain. Otherwise, if only one abstains, a zero score is assigned.

In order to improve the readability of some charts, not all party labels have been displayed. For full information, all charts and tables used in this analysis are available on-line³.

³Please visit <https://public.tableau.com/profile/mario.levorato>

4.1 A brief introduction to Brazilian politics

From 1994 to 2002, Brazil was governed by president Fernando Henrique Cardoso, member of the PSDB (Brazilian Social Democracy Party). In 2002, PSDB was defeated in the presidential elections by PT (Brazilian Labor Party) and president Lula da Silva was elected for a four-year term, being reelected in 2006 for one more period of four years. Then, in 2010, president Dilma Rousseff (also a PT member and supported by president Lula da Silva) won the elections, becoming the next president and, like her predecessor, was also reelected in 2014 for an additional four-year term.

Since 2013, Brazil has been facing intense political and economical crisis, aggravated by successive scandals of corruption in the heart of the government (Connors, 2016; Robins-Early, 2016). In 2016, an impeachment process was started, on charges related to breaking budget laws, and president Dilma Rousseff was turned away from her post (Watts, 2016b; BBC, 2016). However, a more detailed research over international news articles reveals different views about the root causes of the political crisis and the impeachment itself (Alston, 2016; Bevins, 2016; Connors, 2016; Leahy, 2016; Rapoza, 2016; Shahshahani and Nation, 2016; Taub, 2016).

In order to help understanding the political groups and parties referenced in the analysis, we first provide a list of the three party alliances during the presidential elections held in 2010 (Table 3) and in 2014 (Table 4). In our analysis, we will refer to the first party alliance (candidate Dilma Rousseff, in both presidential elections) as the government coalition, while the second party alliance (candidates José Serra in 2010, and Aécio Neves in 2014) will be called opposition.

| Candidate | Coalition parties | # |
|----------------|---|----|
| Dilma Rousseff | PCDOB, PDT, PMDB, PR, PRB, PSB, PSC, PT , PTC, PTN | 10 |
| José Serra | DEM, PMN, PPS, PSDB , PTB, PTDOB | 6 |
| Marina Silva | PV* | 1 |

Table 3: Coalitions in the 2010 presidential elections, ordered by the number of parties (#) and quantity of votes. Six more candidates (from six remaining parties) ran for presidency in 2010. Like **PV**, their parties were not in a coalition.

| Candidate | Coalition parties | # |
|----------------|---|---|
| Dilma Rousseff | PCDOB, PDT, PMDB, PP, PR, PRB, PROS, PSD, PT | 9 |
| Aécio Neves | DEM, PEN, PMN, PSDB , PTB, PTC, PTDOB, PTN, SD | 9 |
| Marina Silva | PHS, PPL, PPS, PRP, PSB , PSL | 6 |

Table 4: Coalitions in the 2014 presidential elections, ordered by the number of parties (#) and quantity of votes. Eight more candidates (from eight remaining parties) ran for presidency in 2014. Their parties were not in a coalition.

Another useful piece of information is the list of parties according to their orientation (Table 5).

Although some parties classify their orientation as center-left or center-right, a great portion of them can be regarded as center parties. As of 2016, the block known as "super-center" includes PEN, PHS, PP, PR, PRB, PROS, PSC, PSD, PSL, PTB, PTN and SD.

As mentioned in the introduction, the Chamber of Deputies (*Câmara dos Deputados*) is the lower house of the National Congress, comprised of 513 federal deputies (from 25 political parties), elected by a proportional representation of votes to serve a four-year term. Table 6 displays the number of elected deputies from each party/coalition, for the 2010 (2011-2014 term) and 2014 elections (2015-2018 term).

| Orientation | Parties | # |
|--------------|---|-----------|
| Left | PCB, PCDOB, PCO, PSOL, PSTU, PT | 6 |
| Center-left | PDT, PMN, PPL, PPS, PROS, PSB, PSDB, REDE, SD | 9 |
| Center | DEM, PEN, PHS, PMB, PMDB, PRP, PSD, PSDC, PSL, PTB, PTC, PTDOB, PTN, PV | 14 |
| Center-right | NOVO, PR, PRB, PSC | 4 |
| Right | PP, PRTB | 2 |
| Total | - | 35 |

Table 5: List of Brazilian political parties according to their orientation (Vasconcellos, 2016a,b).

4.2 Methodology

We attempt to identify groups of deputies (and their respective parties) in the Chamber of Deputies signed networks, generated based on voting session records publicly made available by the open data initiative of the Brazilian Government ⁴.

To do so, we apply the *ILS – CC* (Levorato et al., 2015) procedure to solve the two problems introduced in Section II: the Correlation Clustering (CC) problem and the Symmetric Relaxed Correlation Clustering (SRCC) problem. The procedure changes the objective function that evaluates the clustering partition accordingly.

However, based on the obtained results, we chose to rely our analysis solely on SRCC clustering results ⁵. The reason is that all CC solutions presented only one or two clusters as output, which, to our knowledge, did not accurately represent the political groups in the Chamber of Deputies. One possible explanation is that, as stated in Section II, when compared to the SRCC problem, the CC problem tends to over-evaluate the imbalance of a network, for penalizing relationships associated, for instance, with mediation processes. As we shall see next, parliament mediation groups were indeed detected when solving the SRCC problem.

Next we present several clustering results that help answering interesting questions concerning political dynamics. Each question and its respective analysis is organized in a subsection.

4.3 Evaluation of the loyalty of parties from the same coalition

We have extracted a table which, for each year, coalition and party (columns *Year*, *Party Alliance* and *Party*, respectively), gives details about the percentage of deputies from each party in each cluster (columns *C1* to *C4*). This way it is possible to spot if the majority of the deputies of a specific party does not belong to the most populous coalition cluster, which constitutes a strong evidence that such party is unfaithful to its coalition. By using this data, one can verify that, for example, in 2011 (Table 7), only 41% of PDT, 38% of PR and 42% of PRB deputies were classified inside the largest ruling coalition cluster, formed by 206 deputies. In 2012 (Table 8), only 16% (3 in 19) of PSC deputies accompanied the biggest government group, comprised of 237 deputies. Finally, in 2014 (on both network versions), just half of PT and PDT deputies followed the government coalition (see column *C1* in Table 9).

⁴The data services of the Brazilian Chamber of Deputies website can be found at <http://www2.camara.leg.br/transparencia/dados-abertos>

⁵We solved the SRCC problem by fixing the number of clusters (k) in the solution to $k = 4$, so as to reflect the number of coalition groups: the three main coalitions in each four-year term, listed in Tables 3 and 4, plus an additional group to represent all the candidates / parties not in a coalition.

4.4 Evolution of the support of the government coalition

We start by analyzing two tables that provide, for each year and network version (columns *Year* and *Version*, respectively), the number of deputies according to their respective party alliance and the cluster to which they belong (columns *Party Alliance* and columns *C1* to *C4*, respectively). The first table (Table 10) refers to the period from 2011 to 2014 (54th legislature of the Chamber of Deputies), while the second one (Table 11) gives information about the years of 2015 and 2016 (55th legislature, corresponding to president Dilma Rousseff’s second presidential term).

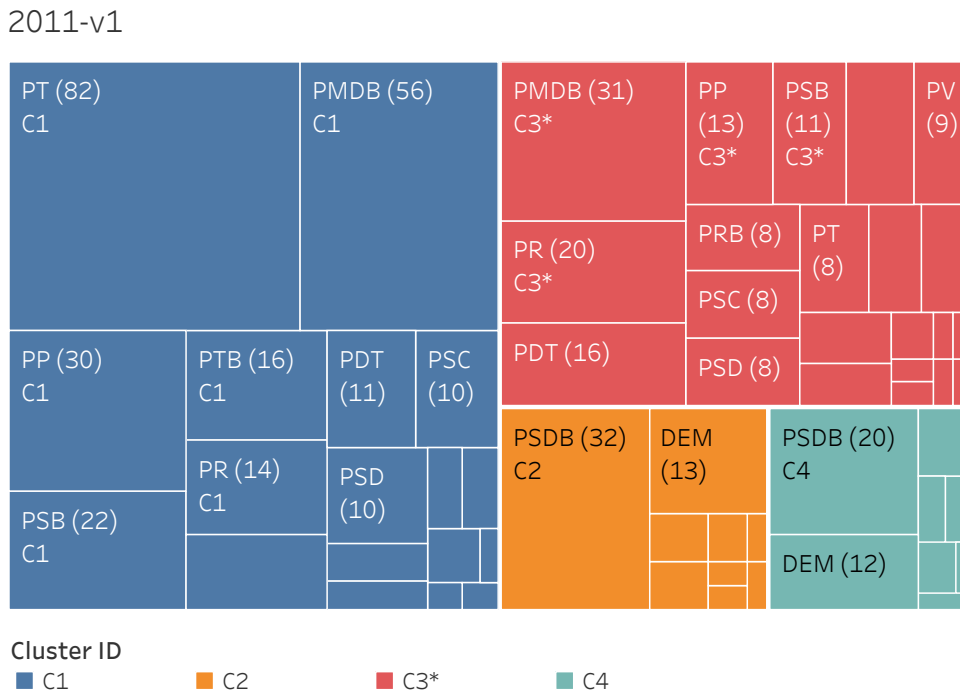


Figure 1: SRCC clustering results for the year of 2011, when solving version v1 of the voting network, by fixing the number of clusters in the solution to $k = 4$. Each cluster is marked with a different color and a cluster label (begins with letter C, below the party name). For each cluster, the treemap displays the sum of deputies (in parenthesis), grouped by their respective party. Cluster labels marked with an asterisk (*) consist of mediation groups.

We observe that, in the first year of president Dilma Rousseff’s government (2011), the government coalition is divided, roughly speaking, in two or three big groups, depending on the network version on which the analysis is based. According to version v1 (Figure 1), the largest cluster (C1) has 64% of the allied deputies. Also, the great majority of the president’s party (PT), 82 deputies, are to be found in this cluster.

From 2012 onwards, a clear basis consolidation can be observed, with 77% of the allied deputies in the same group (cluster C1 in Figure 2). This cluster also holds more than 80 deputies of president’s party (PT).

In 2013 (Figure 3), the percentage of allied deputies inside the largest cluster (C1) rises to 82% of the coalition (74 PT deputies). However, in 2014 (the last year of president Dilma Rousseff’s first term), a change of course comes about. This measure falls to 66% (Figure 4) and, even worse, only about half of PT’s deputies are inside the main coalition group (C3).

A close look at president Dilma Rousseff’s second presidential term is surprising. In 2015, the biggest group of what should be the government’s new coalition (cluster C1 in Figure 5) is

2012-v1

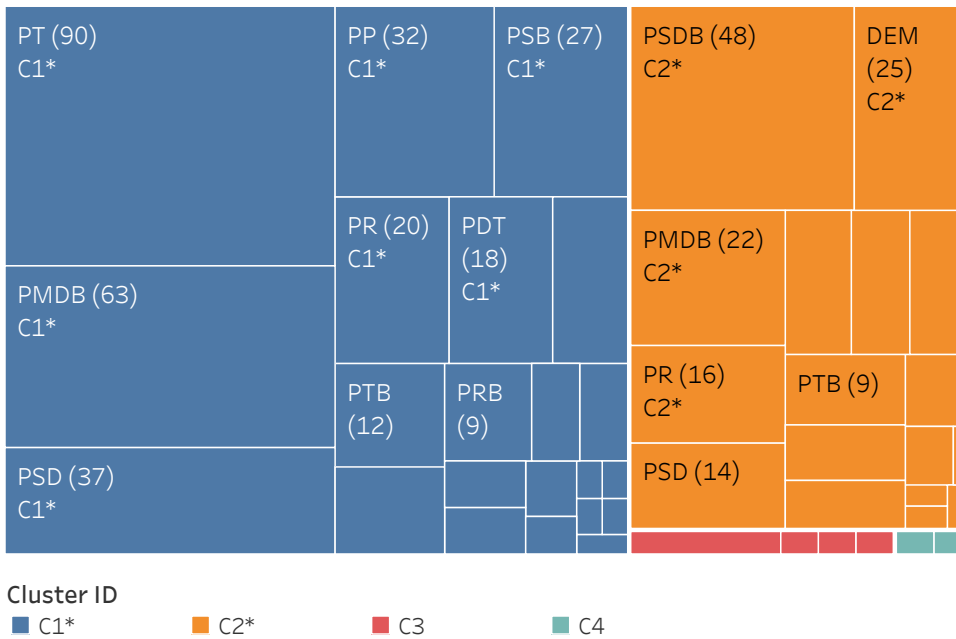


Figure 2: SRCC clustering results for the year of 2012, when using version v1 of the voting network, by fixing the number of clusters in the solution to $k = 4$. Each cluster is marked with a different color and a cluster label (begins with letter C, below the party name). For each cluster, the treemap displays the sum of deputies (in parenthesis), grouped by their respective party. Cluster labels marked with an asterisk (*) consist of mediation groups.

2013-v2

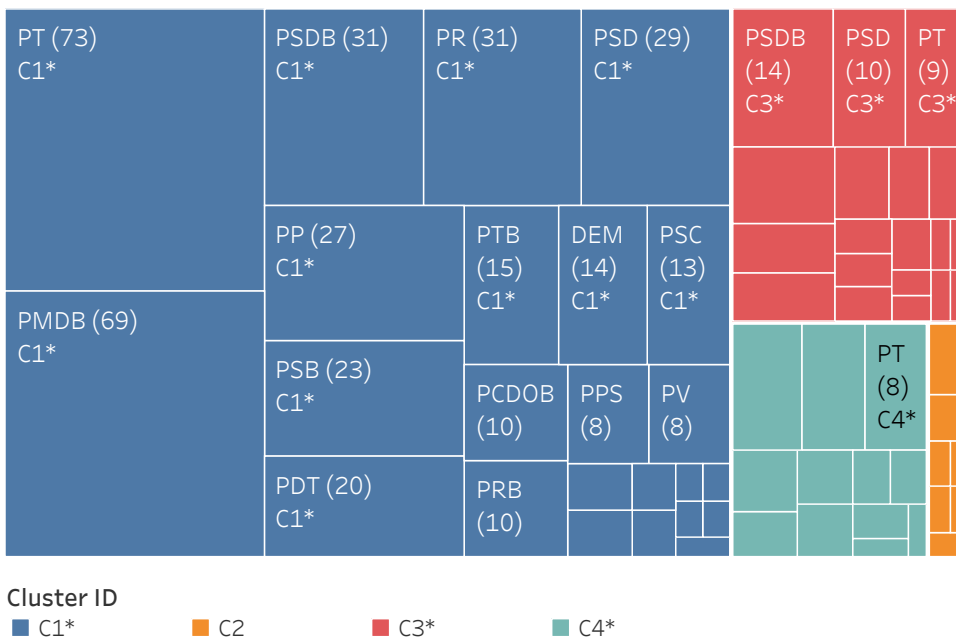


Figure 3: SRCC clustering results for the year of 2013, when using version v2 of the voting network, by fixing the number of clusters in the solution to $k = 4$. Each cluster is marked with a different color and a cluster label (begins with letter C, below the party name). For each cluster, the treemap displays the sum of deputies (in parenthesis), grouped by their respective party. Cluster labels marked with an asterisk (*) consist of mediation groups.

2014-v2

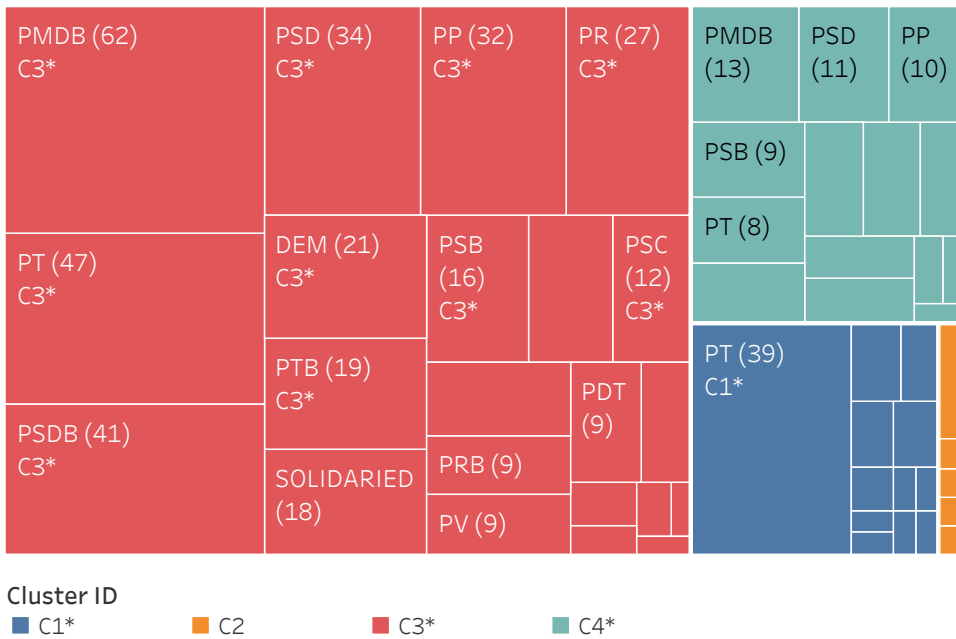


Figure 4: SRCC clustering results for the year of 2014, when using version v2 of the voting network, by fixing the number of clusters in the solution to $k = 4$. Each cluster is marked with a different color and a cluster label (begins with letter C, below the party name). For each cluster, the treemap displays the sum of deputies (in parenthesis), grouped by their respective party. Cluster labels marked with an asterisk (*) consist of mediation groups.

formed by 70% of the total number of deputies of the coalition as a whole. Notwithstanding, this group houses at most 10 deputies of the president's party (PT). Consider as well that the greatest part of PT deputies is in fact isolated in a smaller cluster, together with a few deputies from less influential parties. Note that both network versions show almost identical results⁶.

A similar picture takes place in 2016 (Figure 6), when about two thirds of the supposedly allied deputies belong to the same group, which contains only 11 PT deputies. Similarly, 50 PT deputies can be found in another cluster.

Briefly speaking, results point out that in the years of 2015 and 2016, even though there are still large groups in which most deputies are from the so-called government coalition, such groups are no longer in accordance with the president's party, which is perfectly understandable because of the political crisis and the loss of parliamentary support, news widely broadcast (Dyer, 2015; Boadle, 2016; Watts, 2016a).

4.5 Strength of party leadership

This study was carried out as follows: for each year from 2011 to 2016 and for each party, we scanned data about the deputies and the clusters from which they make part. This information was then cross-referenced with the cluster where the leader of the respective party is found. This way it is possible to have a clear view of how strong the leadership of each party is: if a specific deputy belongs to different cluster than its party leader, on average, this deputy did not vote the way his party expected. The full results with the information about the deputies classified

⁶Please visit <https://public.tableau.com/profile/mario.levorato> for a full list of charts and tables.

2015-v1

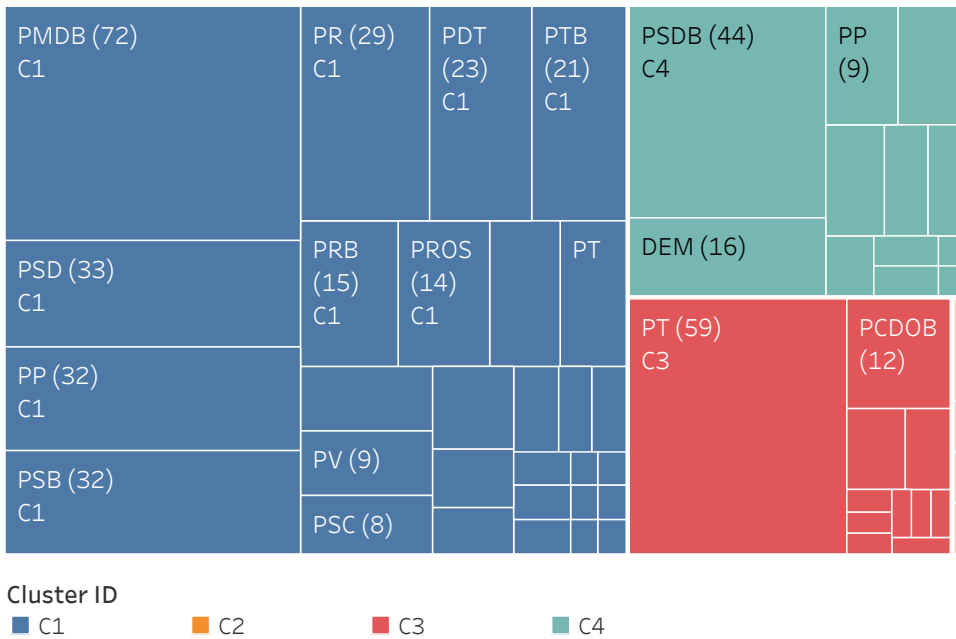


Figure 5: SRCC clustering results for the year of 2015, when using version v1 of the voting network, by fixing the number of clusters in the solution to $k = 4$. Each cluster is marked with a different color and a cluster label (begins with letter C, below the party name). For each cluster, the treemap displays the sum of deputies (in parenthesis), grouped by their respective party. Cluster labels marked with an asterisk (*) consist of mediation groups.

2016-v1

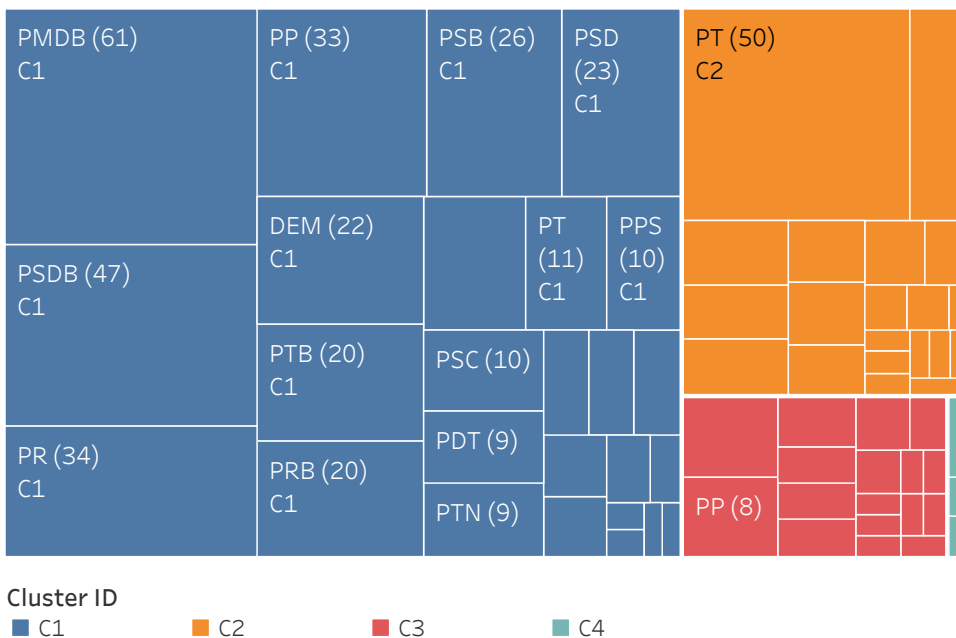


Figure 6: SRCC clustering results for the year of 2016, when using version v1 of the voting network, by fixing the number of clusters in the solution to $k = 4$. Each cluster is marked with a different color and a cluster label (begins with letter C, below the party name). For each cluster, the treemap displays the sum of deputies (in parenthesis), grouped by their respective party. Cluster labels marked with an asterisk (*) consist of mediation groups.

in the same cluster as their respective party leader (percentage) are available in Table 12 for 2011-2014 and in Table 13 for 2015-2016.

For each year, the following parties have been identified as having low percentage ($\rho < 50\%$) of deputies who vote after their party leaders, independently of the analyzed network version:

- 2011: PRB, PRP, PSC, PSD.
- 2012: PR, PSB, PSC, PSD, PTB, PV.
- 2013: PCDOB, PRP, PV.
- 2014: PCDOB, PDT.
- 2015: PSC.
- 2016: PCDOB, PMB, PSL, PTDOB.

Deep consideration into this list will reveal that, as we spot a considerably great number of deputies arranged in clusters where their party leaders are not present, there is strong evidence that, on average, voting recommendations from party leaders have not been followed by many deputies.

4.6 Detection of mediation groups in the chamber of deputies by the algorithm

When the ILS-CC algorithm analyzes the voting networks of the Chamber of Deputies, two versions for each year, it proves to be quite successful in identifying positive mediation groups, that means, clusters whose most internal and external relationships are positive. In the conducted study, a group was classified as showing mediation properties whenever its positive relationship percentage was above 90% and also its internal positive link ratio exceeded that same level.

Because of the large number of political parties in the Brazilian CD (over 23 parties), we chose to rely our analysis on individual deputies instead of parties associated with mediation. We have cross-referenced the list of deputies inside each mediation cluster with the list of party leaders of the CD⁷ plus the list of deputies that preside permanent committees of the CD⁸, for a total of 60 deputies who act as potential mediators. Table 14 lists the mediation clusters, for each year and voting network version, as well as how many of its deputies belong either to party leadership or to permanent committees. Remark that in the years of 2015 and 2016 no mediation groups were detected, probably due to the unstable political environment. The obtained results suggest that the mediation groups detected by the SRCC algorithm are in accordance with the corresponding political scenario.

Additionally, in every figure that contains a treemap (see Figure 4) showing what is inside each cluster (parties and number of deputies), the information about which groups have mediation properties is also present in the cluster labels marked with an asterisk (*).

4.7 The split of the government ruling party when the Brazilian political crisis began

The clustering results for 2014 strongly suggest that president Dilma Rousseff's party (PT) split, with 47 deputies in the first cluster, 39 in the second and 8 in the third. As seen on Figure 4, the treemap shows the fragmentation of PT in the last year of the president's first term.

⁷The list of CD party leaders is available at <http://www2.camara.leg.br/deputados/liderancas-e-bancadas>.

⁸The list of permanent committees of the CD is available at <http://www2.camara.leg.br/atividade-legislativa/comissoes/comissoes-permanentes/>.

4.8 Government coalition's loss of support after president Dilma Rousseff's reelection

According to the results obtained by the ILS-CC algorithm, in 2015, after president Dilma Rousseff's reelection, three clusters cover 99% of the deputies (Figure 5). The parties inside each cluster reveal the main political groups at that time:

- the largest group includes mainly center parties, such as the majority of PMDB, PSD, PP and PR;
- the second biggest group is formed by opposition parties like PSDB and DEM;
- the last one represents the government core parties, such as PT (59 deputies) and PCDOB (12 members).

A comparison between 2015 and previous years (see Figures 1, 2 and 5) reveals that the government coalition has gone through a substantial loss of support, mostly from center parties. These results anticipate a movement which became clear only the following year, when PMDB and other center-parties voted to leave the governing coalition (Boadle, 2016; Watts, 2016a; Barchfield and Savarese, 2016).

4.9 Center parties moved towards opposition when the government coalition lost power

Looking at the data for the years of 2015 (Figure 5) and 2016 (Figure 6), one can observe that the majority of center party and opposition deputies started sharing the same group. There was a strong approximation between PMDB (center), PSDB and DEM (opposition), which have previously been in separate clusters. According to the charts, one can notice that center parties have moved towards opposition.

In 2015, there was a large movement of parties from the government coalition, which went to a "super-centered" group. These parties include: PROS (12), PRB (12), PDT (22), PR (25), PP (28), PSD (33) and PMDB (71).

In 2016, the following coalition parties have effectively migrated to what can be interpreted as a huge opposition cluster: PDT(17), PRB (20), PSD (21), PP (30), PR (33) and PMDB (56).

News broadcast confirm this movement: first, the approximation between Brazil's biggest party (PMDB) and PSDB was reported (Gonçalves, 2016; Sambo and Godoy, 2016). Shortly after, PMDB voted to leave the governing alliance (Boadle, 2016; Watts, 2016a), followed by three other parties (PDT, PRB and PP) (Barchfield and Savarese, 2016).

4.10 Polarization between political groups

In 2012 (on both network versions), the chamber of deputies is polarized in two large groups (see Figure 2). The first one with 238 members, led by the majority of PT and PMDB deputies (government base). The other cluster is mainly characterized by opposition parties, such as PSDB and DEM, but it also includes dissidents from center parties like PMDB and PSD.

4.11 Relative imbalance of the analyzed signed social networks

Several authors have mentioned that real-world signed social networks are more balanced than expected (Kunegis et al., 2009; Leskovec et al., 2010; Kunegis et al., 2010; Facchetti et al., 2011). As seen on Table 15, the signed social networks generated from the Brazilian CD voting data are in fact highly balanced, which supports existing research about that topic.

V CONCLUDING REMARKS

In this article, we have investigated some of the aspects inherent to signed voting networks and political relationships, by using data from the Brazilian Chamber of Deputies (CD). We have first extracted a collection of networks based on voting patterns of the CD members. We have also applied a clustering algorithm specifically designed for signed networks, called *ILS – CC*, which aims to reduce structural balance.

The analysis of the identified clusters has shown that mediation groups do exist in the Chamber of Deputies. Detected in different years, these groups include several deputies who might act as potential mediators, such as party leaders and presidents of permanent committees of the CD. The applied algorithm has also allowed us to gather evidence that certain parties are indeed unfaithful to their coalition. Besides, the obtained data perfectly confirms the news broadcast about the Brazilian political situation, such as the loss of support that government coalition experienced.

Equally, the algorithm has proved to be a useful tool to spot parties under weak leadership and the existence of polarization between two large political groups. Our analysis also confirmed that the signed social networks we generated from the Brazilian CD voting data are indeed extremely balanced, hence supporting previous related works.

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2010

| Coalition | Party | |
|--------------------------------|---------------|------------|
| Dilma Rousseff (Government) | PDT | 28 |
| | PMDB | 79 |
| | PR | 41 |
| | PRB | 8 |
| | PSB | 34 |
| | PSC | 17 |
| | PT | 88 |
| | Total | 295 |
| Jose Serra (Opposition) | DEM | 43 |
| | PPS | 12 |
| | PSDB | 54 |
| | PTB | 21 |
| | Total | 130 |
| Marina Silva | PV | 15 |
| | Total | 15 |
| Not in a coalition | PCdoB | 15 |
| | PHS | 2 |
| | PP | 41 |
| | PSOL | 3 |
| | PTdoB | 4 |
| | Other parties | 8 |
| | Total | 73 |
| Total | | 513 |

2014

| Coalition. | Party | |
|--------------------------------|---------------|------------|
| Dilma Rousseff (Government) | PCdoB | 10 |
| | PDT | 19 |
| | PMDB | 66 |
| | PP | 37 |
| | PR | 34 |
| | PRB | 21 |
| | PROS | 11 |
| | PSD | 36 |
| | PT | 70 |
| | Total | 304 |
| Aecio Neves (Opposition) | DEM | 22 |
| | PSDB | 54 |
| | PTB | 25 |
| | PTdoB | 1 |
| | SD | 15 |
| | Total | 117 |
| Marina Silva | PHS | 5 |
| | PPS | 10 |
| | PSB | 34 |
| | Total | 49 |
| Not in a coalition | PSC | 13 |
| | PSOL | 5 |
| | PV | 8 |
| | Other parties | 17 |
| | Total | 43 |
| Total | | 513 |

Table 6: Number of elected deputies from each party and coalition, for the 2010 elections (2011-2014 term, on the left) and for the 2014 elections (2015-2018 term, on the right).

| Year | Version | Party Alliance | Party | Cluster ID | | | | Total |
|------|---------|----------------|---------------|---------------|---------------|---------------|------------|---------|
| | | | | C1 | C2 | C3 | C4 | |
| 2011 | v2 | Government | PDT | 41.38% | 6.90% | 27.59% | 24.14% | 100.00% |
| | | | | 12 | 2 | 8 | 7 | 29 |
| | | | PMDB | 67.42% | 2.25% | 12.36% | 17.98% | 100.00% |
| | | | | 60 | 2 | 11 | 16 | 89 |
| | | | PR | 37.84% | 8.11% | 18.92% | 35.14% | 100.00% |
| | | | | 14 | 3 | 7 | 13 | 37 |
| | | | PRB | 41.67% | | 33.33% | 25.00% | 100.00% |
| | | | | 5 | | 4 | 3 | 12 |
| | | | PSB | 64.71% | 2.94% | 14.71% | 17.65% | 100.00% |
| | | | 22 | 1 | 5 | 6 | 34 | |
| | | PSC | 61.11% | | 22.22% | 16.67% | 100.00% | |
| | | | 11 | | 4 | 3 | 18 | |
| | | PT | 91.11% | | 5.56% | 3.33% | 100.00% | |
| | | | 82 | | 5 | 3 | 90 | |
| | | PTC | | | | 100.00% | 100.00% | |
| | | | | | | 1 | 1 | |
| | | Total | 66.45% | 2.58% | 14.19% | 16.77% | 100.00% | |
| | | | 206 | 8 | 44 | 52 | 310 | |
| | | | Opposition | DEM | 7.89% | 68.42% | 7.89% | 15.79% |
| | | 3 | | 26 | 3 | 6 | 38 | |
| | PMN | 75.00% | | | 25.00% | | 100.00% | |
| | | 3 | | | 1 | | 4 | |
| | PPS | | | 58.33% | 25.00% | 16.67% | 100.00% | |
| | | | | 7 | 3 | 2 | 12 | |
| | PSDB | 1.72% | 91.38% | 3.45% | 3.45% | 100.00% | | |
| | | 1 | 53 | 2 | 2 | 58 | | |
| | PTB | 72.73% | | 13.64% | 13.64% | 100.00% | | |
| | | 16 | | 3 | 3 | 22 | | |
| | Total | 17.16% | 64.18% | 8.96% | 9.70% | 100.00% | | |
| | | 23 | 86 | 12 | 13 | 134 | | |
| | Total | 51.58% | 21.17% | 12.61% | 14.64% | 100.00% | | |
| | | 229 | 94 | 56 | 65 | 444 | | |

Table 7: Party coalition and clustering details for the year of 2011, when solving version v2 of the voting network, by fixing the number of clusters in the solution to $k = 4$. For each coalition (column Party Alliance) and for each party (column Party), each cell shows the percentage of deputies of that party inside each cluster (columns C1 to C4).

| Year | Version | Party Alliance | Party | Cluster ID | | | | Total |
|------|------------|----------------|---------|------------|--------|---------|---------|---------|
| | | | | C1 | C2 | C3 | C4 | |
| 2012 | v2 | Government | PDT | 60.71% | 3.57% | 10.71% | 25.00% | 100.00% |
| | | | | 17 | 1 | 3 | 7 | 28 |
| | | | PMDB | 80.23% | | 10.47% | 9.30% | 100.00% |
| | | | | 69 | | 9 | 8 | 86 |
| | | | PR | 61.11% | | 19.44% | 19.44% | 100.00% |
| | | | | 22 | | 7 | 7 | 36 |
| | | | PRB | 90.00% | | 10.00% | | 100.00% |
| | | | | 9 | | 1 | | 10 |
| | | | PSB | 81.08% | | 13.51% | 5.41% | 100.00% |
| | | | 30 | | 5 | 2 | 37 | |
| | | PSC | 15.79% | | 36.84% | 47.37% | 100.00% | |
| | | | 3 | | 7 | 9 | 19 | |
| | | PT | 92.47% | 1.08% | 4.30% | 2.15% | 100.00% | |
| | | | 86 | 1 | 4 | 2 | 93 | |
| | | PTC | 100.00% | | | | 100.00% | |
| | | | 1 | | | | 1 | |
| | | | Total | | 76.45% | 0.65% | 11.61% | 11.29% |
| | | | 237 | 2 | 36 | 35 | 310 | |
| | Opposition | DEM | 16.67% | | 43.33% | 40.00% | 100.00% | |
| | | | 5 | | 13 | 12 | 30 | |
| | | PMN | 100.00% | | | | 100.00% | |
| | | | 2 | | | | 2 | |
| | | PPS | 18.18% | | 63.64% | 18.18% | 100.00% | |
| | | | 2 | | 7 | 2 | 11 | |
| | | PSDB | 5.36% | 7.14% | 48.21% | 39.29% | 100.00% | |
| | | 3 | 4 | 27 | 22 | 56 | | |
| | PTB | 57.14% | | 14.29% | 28.57% | 100.00% | | |
| | | 12 | | 3 | 6 | 21 | | |
| | Total | | 20.00% | 3.33% | 41.67% | 35.00% | 100.00% | |
| | | | 24 | 4 | 50 | 42 | 120 | |
| | Total | | 60.70% | 1.40% | 20.00% | 17.91% | 100.00% | |
| | | | 261 | 6 | 86 | 77 | 430 | |

Table 8: Party coalition and clustering details for the year of 2012, when solving version v2 of the voting network, by fixing the number of clusters in the solution to $k = 4$. For each coalition (column Party Alliance) and for each party (column Party), each cell shows the percentage of deputies of that party inside each cluster (columns C1 to C4).

| Year | Version | Party Alliance | Party | Cluster ID | | | | Total |
|-------|---------|----------------|--------|------------|---------|---------|---------|---------|
| | | | | C1 | C2 | C3 | C4 | |
| 2014 | v2 | Government | PDT | 10.53% | 5.26% | 47.37% | 36.84% | 100.00% |
| | | | | 2 | 1 | 9 | 7 | 19 |
| | | | PMDB | 1.25% | 5.00% | 77.50% | 16.25% | 100.00% |
| | | | | 1 | 4 | 62 | 13 | 80 |
| | | | PR | | | 81.82% | 18.18% | 100.00% |
| | | | | | | 27 | 6 | 33 |
| | | | PRB | 10.00% | | 90.00% | | 100.00% |
| | | | | 1 | | 9 | | 10 |
| | | PSB | 3.85% | | 61.54% | 34.62% | 100.00% | |
| | | | 1 | | 16 | 9 | 26 | |
| | | PSC | | 6.67% | 80.00% | 13.33% | 100.00% | |
| | | | | 1 | 12 | 2 | 15 | |
| | | PT | 41.49% | | 50.00% | 8.51% | 100.00% | |
| | | | 39 | | 47 | 8 | 94 | |
| | | Total | 15.88% | 2.17% | 65.70% | 16.25% | 100.00% | |
| | | | 44 | 6 | 182 | 45 | 277 | |
| | | Opposition | DEM | | | 75.00% | 25.00% | 100.00% |
| | | | | | | 21 | 7 | 28 |
| | | | PMN | | | 66.67% | 33.33% | 100.00% |
| | | | | 2 | 1 | 3 | | |
| PPS | 11.11% | | | 66.67% | 22.22% | 100.00% | | |
| | 1 | | | 6 | 2 | 9 | | |
| PSDB | 2.04% | | 83.67% | 14.29% | 100.00% | | | |
| | 1 | | 41 | 7 | 49 | | | |
| PTB | | 5.00% | 95.00% | | 100.00% | | | |
| | | 1 | 19 | | 20 | | | |
| Total | 1.83% | 0.92% | 81.65% | 15.60% | 100.00% | | | |
| | 2 | 1 | 89 | 17 | 109 | | | |
| Total | 11.92% | 1.81% | 70.21% | 16.06% | 100.00% | | | |
| | 46 | 7 | 271 | 62 | 386 | | | |

Table 9: Party coalition and clustering details for the year of 2014, when solving version v2 of the voting network, by fixing the number of clusters in the solution to $k = 4$. For each coalition (column Party Alliance) and for each party (column Party), each cell shows the percentage of deputies of that party inside each cluster (columns C1 to C4).

Coalition Loyalty 2011-2014

| Year | Version | Party Alliance | Cluster ID | | | | Total |
|------|---------|----------------|---------------|--------------|---------------|--------------|----------------|
| | | | C1 | C2 | C3 | C4 | |
| 2011 | v1 | Government | 199 64.19% | 4 1.29% | 103 33.23% | 4 1.29% | 310 100.00% |
| | | Opposition | 22 16.42% | 48 35.82% | 28 20.90% | 36 26.87% | 134 100.00% |
| | v2 | Government | 206 66.45% | 8 2.58% | 44 14.19% | 52 16.77% | 310 100.00% |
| | | Opposition | 23 17.16% | 86 64.18% | 12 8.96% | 13 9.70% | 134 100.00% |
| 2012 | v1 | Government | 238 76.77% | 68 21.94% | 2 0.65% | 2 0.65% | 310 100.00% |
| | | Opposition | 27 22.50% | 89 74.17% | 4 3.33% | | 120 100.00% |
| | v2 | Government | 237 76.45% | 2 0.65% | 36 11.61% | 35 11.29% | 310 100.00% |
| | | Opposition | 24 20.00% | 4 3.33% | 50 41.67% | 42 35.00% | 120 100.00% |
| 2013 | v1 | Government | 132 44.59% | 2 0.68% | 158 53.38% | 4 1.35% | 296 100.00% |
| | | Opposition | 64 57.66% | | 46 41.44% | 1 0.90% | 111 100.00% |
| | v2 | Government | 239 82.13% | 6 2.06% | 28 9.62% | 18 6.19% | 291 100.00% |
| | | Opposition | 70 65.42% | 1 0.93% | 22 20.56% | 14 13.08% | 107 100.00% |
| 2014 | v1 | Government | 196 70.76% | 6 2.17% | 41 14.80% | 34 12.27% | 277 100.00% |
| | | Opposition | 98 89.91% | 1 0.92% | 2 1.83% | 8 7.34% | 109 100.00% |
| | v2 | Government | 44 15.88% | 6 2.17% | 182 65.70% | 45 16.25% | 277 100.00% |
| | | Opposition | 2 1.83% | 1 0.92% | 89 81.65% | 17 15.60% | 109 100.00% |

Table 10: Party coalition during the 2010 presidential elections, for the 2011-2014 term. For each year (column *Year*) and network version (column *Version*), the table shows the number of deputies in each party alliance (column *Party Alliance*) found in each cluster (columns *C1* to *C4*). Results obtained when fixing the number of clusters in the solution to $k = 4$.

Coalition Loyalty 2015-2016

| Year | Version | Party Alliance | Cluster ID | | | | | Total |
|------|---------|----------------|---------------|--------------|---------------|--------------|------------|----------------|
| | | | C1 | C2 | C3 | C4 | C5 | |
| 2015 | v1 | Government | 229 69.60% | 3 0.91% | 82 24.92% | 15 4.56% | | 329 100.00% |
| | | Opposition | 49 41.88% | | 3 2.56% | 65 55.56% | | 117 100.00% |
| | v2 | Government | 210 63.83% | 3 0.91% | 95 28.88% | 21 6.38% | | 329 100.00% |
| | | Opposition | 28 23.93% | | 7 5.98% | 82 70.09% | | 117 100.00% |
| 2016 | v1 | Government | 201 63.41% | 89 28.08% | 23 7.26% | 4 1.26% | | 317 100.00% |
| | | Opposition | 104 86.67% | 7 5.83% | 9 7.50% | | | 120 100.00% |
| | v2 | Government | 23 7.26% | 92 29.02% | 186 58.68% | 14 4.42% | 2 0.63% | 317 100.00% |
| | | Opposition | 11 9.17% | 8 6.67% | 88 73.33% | 11 9.17% | 2 1.67% | 120 100.00% |

Table 11: Party coalition during the 2014 presidential elections, for the 2015-2018 term. For each year (column *Year*) and network version (column *Version*), the table shows the number of deputies in each party alliance (column *Party Alliance*) found in each cluster (columns *C1* to *C4*). Results obtained when fixing the number of clusters in the solution to $k = 4$.

Party Leadership (2011-2014)

| Party | Year / Version | | | | | | | |
|-------|----------------|-----|------|------|------|------|------|------|
| | 2011 | | 2012 | | 2013 | | 2014 | |
| | v1 | v2 | v1 | v2 | v1 | v2 | v1 | v2 |
| DEM | 34% | 68% | 83% | 40% | 69% | 32% | 89% | 75% |
| PCDOB | 73% | 80% | 100% | 100% | 23% | 23% | 27% | 27% |
| PDT | 55% | 28% | 64% | 25% | 44% | 80% | 21% | 47% |
| PMDB | 63% | 67% | 73% | 80% | 42% | 82% | 81% | 78% |
| PMN | | | | | 67% | 67% | 100% | 33% |
| PP | 67% | 67% | 82% | 90% | 31% | 75% | 91% | 74% |
| PPS | 33% | 58% | 64% | 18% | 55% | 73% | 89% | 22% |
| PR | 54% | 35% | 44% | 19% | 62% | 84% | 88% | 82% |
| PRB | 33% | 42% | 90% | 90% | 90% | 100% | 10% | 90% |
| PROS | | | | | 100% | 100% | 67% | 62% |
| PRP | 50% | 50% | | | 50% | 50% | 100% | 100% |
| PSB | | | 27% | 14% | 70% | 85% | 88% | 62% |
| PSC | 44% | 17% | 47% | 47% | 53% | 11% | 73% | 80% |
| PSD | 35% | 17% | 27% | 18% | 35% | 59% | 79% | 71% |
| PSDB | 34% | 91% | 86% | 48% | 65% | 6% | 92% | 84% |
| PSOL | 33% | 67% | 100% | 100% | 67% | 67% | 100% | 100% |
| PT | 91% | 91% | 97% | 92% | 62% | 81% | 51% | 50% |
| PTB | 73% | 73% | 43% | 29% | 68% | 88% | 85% | 95% |
| PTDOB | 75% | 75% | 100% | 67% | 67% | 100% | 100% | 100% |
| PV | 75% | 33% | 50% | 40% | 50% | 20% | 89% | 100% |

Table 12: For each party (column *Party*), displays the percentage of its deputies who vote after their party leader (i.e. deputies classified in the same group of their party leader), for each year between 2011 and 2014 (columns *2011* to *2014*) and for each network version (columns *v1* and *v2*). On certain periods, the numbers associated with a party may not have been shown. Either because the party still did not exist at that time or did not have any representation in parliament at all.

Party Leadership (2015-2016)

| Party | Year / Version | | | |
|-------|----------------|------|------|------|
| | 2015 | | 2016 | |
| | v1 | v2 | v1 | v2 |
| DEM | 30% | 96% | 85% | 77% |
| PCDOB | 92% | 92% | 50% | 50% |
| PDT | 100% | 96% | 59% | 64% |
| PEN | 100% | 100% | 75% | 75% |
| PHS | 100% | 100% | 100% | 100% |
| PMB | | | 14% | 14% |
| PMDB | 96% | 95% | 11% | 77% |
| PP | 78% | 68% | 69% | 4% |
| PPS | 58% | 75% | 100% | 100% |
| PR | 83% | 71% | 83% | 80% |
| PRB | 75% | 40% | 100% | 100% |
| PROS | 100% | 86% | 71% | 71% |
| PRP | | | 100% | 100% |
| PSB | 94% | 68% | 79% | 61% |
| PSC | 46% | 43% | 71% | 71% |
| PSD | 89% | 89% | 70% | 64% |
| PSDB | 80% | 96% | 87% | 2% |
| PSL | | | 25% | 25% |
| PSOL | 100% | 100% | 100% | 100% |
| PT | 83% | 89% | 82% | 82% |
| PTB | 81% | 69% | 95% | 81% |
| PTDOB | 100% | 50% | 50% | 50% |
| PTN | 75% | 25% | 82% | 18% |
| PV | 90% | 20% | 67% | 67% |
| REDE | 100% | 100% | 80% | 80% |

Table 13: For each party (column *Party*), displays the percentage of its deputies who vote after their party leader (i.e. deputies classified in the same group of their party leader), for the years of 2015 and 2016 (columns *2015* and *2016*; until June 2016) and for each network version (columns *v1* and *v2*). On certain periods, the numbers associated with a party may not have been shown. Either because the party still did not exist at that time or did not have any representation in parliament at all.

| Year | Cluster ID | Version | | Number of Records |
|------|------------|---------|----|-------------------|
| | | v1 | v2 | |
| 2011 | C3 | 18 | 10 | |
| | C4 | | 8 | |
| | Total | 18 | 18 | |
| 2012 | C1 | 29 | 26 | |
| | C2 | 19 | | |
| | C3 | | 11 | |
| | C4 | | 11 | |
| | Total | 48 | 48 | |
| 2013 | C1 | 27 | 35 | |
| | C3 | 21 | 6 | |
| | C4 | | 6 | |
| | Total | 48 | 47 | |
| 2014 | C1 | 37 | 4 | |
| | C2 | 0 | | |
| | C3 | 4 | 39 | |
| | C4 | 9 | 7 | |
| | Total | 50 | 50 | |

Table 14: For each year, network version (v1, v2) and mediation cluster detected by the algorithm, displays the quantity of deputies which belong either to party leadership or to permanent committees of the parliament. A blank cell means that mediation properties do not apply to the corresponding cluster for a specific year / network version.

| Year | 2010 | | 2011 | | 2012 | | 2013 | |
|------------|-------|-------|-------|-------|-------|-------|-------|-------|
| Version | v1 | v2 | v1 | v2 | v1 | v2 | v1 | v2 |
| $\%SRI(P)$ | 0.25% | 0.26% | 0.38% | 0.43% | 0.34% | 0.33% | 0.31% | 0.35% |
| Year | 2014 | | 2015 | | 2016 | | | |
| Version | v1 | v2 | v1 | v2 | v1 | v2 | | |
| $\%SRI(P)$ | 0.07% | 0.07% | 0.39% | 0.40% | 1.92% | 2.32% | | |

Table 15: Symmetric Relaxed Imbalance ($\%SRI(P)$) measure obtained with the solution of the SRCC problem over the CD signed graphs, according to year and network version.