

# Application of Monte Carlo techniques to LCO gas oil hydrotreating: Molecular reconstruction and kinetic modelling

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Maria Lopez Abelairas, Luis Pereira de Oliveira, Jan Verstraete. Application of Monte Carlo techniques to LCO gas oil hydrotreating: Molecular reconstruction and kinetic modelling. Catalysis Today, 2016, 271, pp.188-198. 10.1016/j.cattod.2016.02.041 . hal-01338408

# HAL Id: hal-01338408 https://hal.science/hal-01338408v1

Submitted on 28 Jul 2016

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- 1 Application of Monte Carlo techniques to LCO gas oil hydrotreating: molecular
- 2 reconstruction and kinetic modelling.
- 3
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- 4 5

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## 12 Abstract

The increasing pressure to satisfy the environmental criteria concerning oil products leads to 13 the need for developing accurate models to predict the performances of the refining processes. 14 In the current study, a stochastic two-step procedure using Monte Carlo techniques is applied 15 to and validated on the hydrotreating of Light Cycle Oil (LCO) gas oils. In the first step, a 16 mixture of molecules representative of the LCO gas oils is generated using a molecular 17 reconstruction method termed SR-REM. Subsequently, the Stochastic Simulation Algorithm 18 (SSA) is applied to simulate the evolution of the mixture composition during hydrotreating. 19 The results show that an accurate representation of eleven different LCO gas oils was 20 obtained by the application of the molecular reconstruction method. The hydrotreating 21 22 simulations of three LCO gas oils at different operating conditions showed a good agreement with the experimental data obtained at laboratory scale. The current stochastic procedure has 23 24 demonstrated to be a valid tool for the reconstruction of the composition of LCO gas oils and the simulation of the hydrotreating process. 25

26

## 27 Keywords

- 28 Composition modelling; molecular reconstruction; kinetic modelling; kinetic Monte Carlo;
- 29 stochastic simulation algorithm; LCO gas oil hydrotreating.

### 30 **1. Introduction**

31 The pressure on the quality and the maximum impurities content of refinery products has been

- 32 increased in the last decades due to the environmental concerns associated to their use. The
- 33 suitable performance of the processes aimed to remove these impurities is essential to satisfy
- 34 the specifications fixed for oil products. Among these processes, hydrotreating (HDT) is one

of the most mature technologies. The use of hydrogen at high temperature over a catalyst bed
allows to remove sulphur, nitrogen and other undesirable elements from the petroleum
distillates such as naphthas or gas oils.

The correctness in the prediction of HDT process performance directly depends on the 38 reliability of the used kinetic model. A lumping strategy, in which molecular components are 39 grouped according to their global properties, has usually been applied in the kinetics models 40 of complex hydrocarbons <sup>1-3</sup>. However, this approach is no longer manageable due to the 41 elevated number of generated groups and reaction pathways. The limited applicability of 42 lumped models has resulted in the development of molecular-based kinetic models <sup>2,4–9</sup>. In 43 this latter approach, reactant species and products are described by a selection of molecules or 44 small groups of them which react following networks formed by reactions at the molecular 45 46 level and distinguished by a global kinetic constant. The elemental steps are regrouped within the global reactions scheme, thereby reducing the number of reactive species and the size of 47 reaction network. Following this approach, Lopez Garcia et al.<sup>8</sup> have simulated the 48 hydrotreating of LCO gas oils and, more recently, Pereira *et al.*<sup>9–11</sup> have proposed a kinetic 49 methodology for its application on conversion of petroleum cuts based on the Stochastic 50 Simulation Algorithm (SSA) developed by Gillespie<sup>12</sup>. 51

52 These kinetics models required a molecular description of the feedstock. However, the high complexity of the petroleum cuts hinders their molecular characterisation even by using the 53 54 most advanced analytical techniques. To surpass this drawback, a molecular representation of the feedstock can be determined by the application of a molecular reconstruction algorithm. 55 56 This kind of algorithms provides a set of molecules from petroleum analyses and chemical knowledge. Several approaches have been performed in this sense, from the first model 57 proposed by Liguras and Allen<sup>13</sup> to the stochastic reconstruction (SR) developed by Neurock 58 et al.<sup>14</sup> in which a Monte Carlo method is used to sample the objective function. 59 Hudebine <sup>15,16</sup> has characterised different petroleum cuts by the application of a two-steps 60 algorithm based on SR algorithm and on reconstruction entropy maximisation (REM). The 61 combination of both methods (SR-REM) overcomes the drawbacks of its separated 62 application, such as noise of the objective function and computational effort. Posteriorly, 63 Pereira *et al.*<sup>17,18</sup> have modified Hudebine's method to introduce a genetic algorithm which 64 performs the minimisation of the objective function. 65

The current study is focused on the validation of the SR-SEM and SSA algorithms developed by Pereira *et al.* on the hydrotreating of Light Cycle Oil (LCO) gas oils. A brief description of the stochastic methodology applied to both molecular reconstruction and reaction simulation has been developed. Then, the molecular reconstruction of eleven LCO gas oil has been carried out and the hydrotreating of three of them has been simulated at different operational

71 conditions.

#### 72 2. Methodology

The stochastic methodology applied in the current work consists of two steps. In the first one, a molecular reconstruction algorithm is used to model the feedstock by means of a set of molecules which mixture properties are similar to those of the feedstock. This algorithm comprises two coupled methods: stochastic reconstruction (SR) and reconstruction by entropy maximization (REM). The application of the SR method enables to obtain a set of molecules typical for a given type of oil fraction. Then, the molar fraction of molecules is adjusted using the REM method in order to improve the predicted mixture properties.

Finally, the generated set of molecules is introduced as input in the second step concerning the molecule-based kinetic modelling of the conversion process. A kinetic Monte Carlo (kMC) method is applied to model the chemical reaction system at a molecular level. This approach is an alternative to traditional deterministic kinetic methods in which a serial of differential equations (ODE) are involved to obtain a temporal evolution of the species in the system.

#### 86 2.1. Molecular reconstruction

The SR method, from which a representative set of molecules is generated, uses probability 87 88 distributions functions (PDF's) of structural attributes, such as number of rings or number of side chains, to characterise the oil fraction to be reconstructed <sup>14,19</sup>. Feedstock analyses, which 89 90 provide information about atomic abundance (elemental analysis) or structural classes (GC-MS), and the previous knowledge about petroleum cuts should be taken into account to select 91 92 the proper structural attributes. The selected PDF's are sampled N times using a Monte Carlo 93 method in order to generate an initial set of N molecules (Figure 1). To carry out the transition 94 from PDF's to the set of molecules, the application of a building diagram and a serial of chemical rules is required to avoid the creation of impossible and unlikely molecules. The 95 96 building diagram is a decision tree that defines the sequence in which PDF's should be sampled to proceed to the posterior assembly of the different attributes, which provides the 97

structure of the molecule. During the assembly process, the application of chemical rules
discards the molecules which do not satisfy the thermodynamic or likelihood criteria.

The application of the Monte Carlo sampling procedure led to the creation of a mixture of N 100 molecules, each one with a molar fraction equal to 1/N. The average properties of this mixture 101 are calculated and compared with the experimental data by means of an objective function. 102 An optimisation method is used to minimise this objective function though the modification 103 of PDF's parameters. The simulated annealing  $^{15,19-21}$  and the genetic algorithms  $^{22-24}$  are both 104 usual methods applied to the optimisation of the objective function in the field of the 105 stochastic reconstruction. However, Schnongs<sup>24</sup> has demonstrated that the genetic algorithms 106 are more adapted to the stochastic reconstruction than the simulated annealing since the 107 genetic algorithms are less sensitive to the initial value of the distribution parameters and it 108 109 has also showed a lower oscillation of the value of the objective function.

110 Once the initial set of molecules is obtained, the second step based on the reconstruction by 111 entropy maximisation (REM) is applied. During this step, the molar fraction of the molecules 112 in the mixture is modified to obtain a mixture with properties closer to those experimentally 113 determined <sup>15</sup>. To carry out the adjustment of the parameters, the REM method, based on 114 Shannon's information theory <sup>25</sup>, uses the maximisation of an information entropy criterion 115  $(E(x_i))$  given by the Eq. (1):

(1)

116 
$$E(x_i) = -\sum_{i=1}^N x_i \cdot \ln(x_i)$$

117 with

118 
$$\sum_{i=1}^{N} x_i = 1$$
 (2)

where  $x_i$  corresponds to the molar fraction of molecule *i* and *N* is the number of molecules 119 present in the initial mixture determined by applying the SR method. This criterion guaranties 120 that, without constrains or available information, a given molecule cannot be preferred to 121 122 others, so that the distribution of the predefined set of molecules remains uniform. The introduction of a matrix of constrains from analytical data, mixing rules and the initial set of 123 124 molecules distorts this uniformity in order to match this information. These constrains are introduced in the entropy maximisation criterion by means of the Lagrange multiplier method. 125 126 In the case of linear constrains were used, the problem is reduced to an optimisation of Jparameters of a no-linear equation that can be performed by the conjugate gradient method. 127

128 Once the Lagrange parameters are determined, the molar fraction of the molecules is 129 calculated in order to obtain the representative mixture of molecules.

#### 130 2.2. Reaction modelling

The goal of the kMC method is to describe the chemical reaction system at the molecular 131 132 level by following the transformations of a discrete population of molecules. Contrary to deterministic methods, the temporal evolution of the system is not described by a set of 133 differential equations, but by a single probabilistic function termed the chemical master 134 equation (CME)<sup>26,27</sup>. This equation determines the different status of the system in a 135 sequence of discrete-time steps. The evolution of the system is a result from chemical 136 reactions, those have associated a probability function, which depends on the reactant 137 molecule and the rate constant. 138

However, CME cannot usually be solved by analytical or numerical methods due to its high
complexity. In this case, a Monte Carlo procedure developed by Gillespie <sup>12</sup> and termed
Stochastic Simulated Algorithm (SSA) is used to solve CME. This method is based on an
event-space approach, i.e., the evolution of the system is followed event by event, resulting in
disparate time intervals between two consecutive events or, in this particular case, reactions.
The scheme followed in the application of the kMC method has been illustrated in Figure 2.

The initial step of the procedure consists in the "molecular discretisation" of the set of 145 molecules generated by applying the SR-REM method. During this step, the replication of the 146 molecules in the mixture is performed according to their molar fraction and it is based on the 147 same principle as the procedure developed by Hudebine and Verstraete<sup>21</sup> for the creation of a 148 representative set of molecules for gasoline fractions. A replication factor  $(F_{rep})$ , defined as 149 the maximum number of molecules in the discrete mixture, is multiplied by the mole fraction 150 of each molecule in order to calculate the number of replications.  $F_{rep}$  also defines the lowest 151 mole fraction to be retained since the molecules with a mole fraction lower than  $0.5/F_{rep}$  are 152 discarded. The factor 0.5 arises from the rounding off to the closest integer. 153

In the next step of the kMC procedure, all potential reaction events should be identified and listed taking into account a set of reaction rules that generates the reactions by inspecting the structure of the molecules. Once all potential reaction events are identified, the normalised probability for each reaction event is calculated as the ratio of its stochastic rate ( $R_v$ ) to the sum of the rates of all reaction events (M), as shown in Eq. (3):

159 
$$P_{\nu} = \frac{R_{\nu}}{\sum_{i}^{M} R_{i}} \qquad (3)$$

160 with

161 
$$R_v = h_v \cdot c_v \qquad (4)$$

162 where  $h_v$  is the number of distinguishable combinations of the reactant molecule and  $c_v$  is the 163 stochastic rate parameter. For monomolecular reactions, the number of distinguishable 164 combinations of the reactant molecules  $h_v$  equals 1, while for bimolecular reactions, it is equal 165 to the number of available molecules of the second reactant. The stochastic rate parameter  $c_v$ 166 is closely linked to the deterministic rate parameter  $(k_v)$  of each reaction. In the case of 167 monomolecular reactions,  $k_v$  and  $c_v$  are equal, while for bimolecular reactions,  $c_v$  is equal to 168 the ratio of  $k_v$  by reaction volume V.<sup>12</sup>

169 The effect of the reaction temperature on the stochastic rate is taking into account by means of170 the Arrhenius expression reflected in Eq. (5):

171 
$$c_{v} = c_{v}(T_{ref}) \cdot \exp(-\frac{E_{a}}{R} \cdot (\frac{1}{T} - \frac{1}{T_{ref}}))$$
(5)

where  $c_v(T_{ref})$  is the stochastic rate constant of the reaction type *v* at the reference temperature  $T_{ref}$ ,  $E_a$  is the activation energy, *R* is the ideal gas constant, *T* is the system temperature and  $T_{ref}$  is the reference temperature.

The subsequent step of the algorithm is aimed to the determination of the cumulative reaction probability distribution  $(D_R)$ , which grouped all *M* reactions that can take place in the mixture at a given time *t*.

178 A first random number  $(RN_I)$  is obtained to determine the reaction time step  $(\Delta t)$  according to 179 the Eq. (6), as proposed Gillespie <sup>12</sup>:

180 
$$\Delta t = -\frac{\ln(RN_1)}{\sum_i^M R_i} \tag{6}$$

181 The distribution  $D_R$  is randomly sampled in order to select the next reaction ( $\mu$ ) to be

executed in the next reaction time step. For this purpose, a second random number between 0

and 1 is drawn ( $RN_2$ ) and used to select the next reaction from the cumulative distribution  $D_R$ , as shown in Eq. (7):

185 
$$D_R(\mu - 1) < RN_2 \le D_R(\mu)$$
 (7)

- 186 Once the reaction and the time step have been defined, the system is updated by the execution
- 187 of the selected reaction, which implies the replace of the reactant(s) by the product(s) and the
- increase of simulation time in  $\Delta t$ . The simulation continues reaction by reaction until the final
- simulation time is reached and a set of product molecules is obtained.
- 190 Due to its stochastic nature, the algorithm should be executed several times in order to
- 191 provide several sets of molecules which average can be a proper representation of the
- 192 molecules in the reaction system.

#### 193 3. Application to the molecular reconstruction of LCO gas oils

- 194 LCO gas oils are gas oil fractions obtained from the catalytic cracking process and composed
- 195 by a mixture of saturates (paraffins and naphthenes), olefins and aromatic hydrocarbons $^{8}$ .
- 196 These mixtures also show a marginal presence of nitrogen but an important content in
- 197 sulphur, which is present in heterocyclic structures, such as thiophenes and
- 198 benzothiophenes<sup>28</sup>. Their boiling point is in the range of  $120^{\circ}$ C to  $450^{\circ}$ C, which corresponds
- to the molecules with a number of carbons between  $C_8$  and  $C_{30}^{29}$ . According to this data and
- the mass spectrum, LCO gas oils are formed by molecules with none or one poly-aromatic
- structure with a number of rings which usually ranges from 0 to  $4^{30-32}$ .

202 In the current work, it has been performed the molecular reconstruction of eleven LCO gas oils using the SR and REM algorithms. The PDF's of molecular attributes in Table 1 is used 203 to generated the set of molecules that would represent the LCO gas oils. Two kind of PDF's 204 (histograms and gamma functions) were used to defined molecular attributes. The use of 205 histograms is limited to the attributes with a narrow range of possible values (less than three) 206 while the gamma functions describe the attributes with a higher number of possible values. 207 These PDF's have been defined taking into account the previous knowledge about LCO gas 208 209 oils composition. Firstly, it is considered that the molecules in mixture are only constituted by carbon, hydrogen and sulphur due to the negligible presence of nitrogen species. Then, 210 211 nitrogen content is fully assigned to carbon fraction, the most abundant element in mixture. 212 Another hypothesis is that paraffins, which would also include the marginal olefins fraction, are formed by alkyl chains with at least 8 carbons. It is also considered that, according to 213 experimental data, each molecule is formed by a maximum of 4 cycles, in which linear alkyl 214 chains can be the unique substituents, and that the sulphur containing compounds present in 215 the mixture only belong to the thiophenes family and its derivatives. 216

In order to define the relationships between distributions and also identify the sampling steps, 217 a building diagram is needed for the reconstruction of the molecules in LCO gas oils (Figure 218 3). First, the type of molecule to be constructed (saturate or aromatic) is determined by 219 220 distribution 1. In the case of saturate molecules, distribution 3 allows to determine the number of cyclohexane rings (ranged from 0 to 4). When the number of rings present is null, the 221 molecule to be constructed is a paraffin, which chain length is determined by the application 222 of distribution 8. Contrary, in the case of a naphthenic units with between 1 and 4 223 cyclohexane rings, it is necessary to determine the number (distribution 6) and type 224 225 (distribution 7) of the side chains. In the case of aromatic molecules, the number of benzenes, 226 cyclohexanes and thiophenes is determined by distributions 2, 3 and 4, respectively. These 227 three distributions are sampled until the total number of rings is inferior or equal to 4. The number of benzenes is always 1 or higher to avoid the creation of naphthenic molecules in 228 229 this route. Besides, according to experimental data, most of the thiophene rings do not contain cyclohexane rings, so that distribution 3 is not sampled when thiophene rings are present. 230 231 Once the number and type of cycles is defined, the distributions 5 and 6 are used to find the number of side chains in naphthenic and aromatic rings, respectively, and the distribution 7 is 232 applied to determine the type of chain. 233

Elemental analysis (carbon, hydrogen, sulphur and nitrogen), average molecular weight, 234 specific gravity, simulated distillation, mass spectrometry (MS), <sup>1</sup>H NMR and <sup>13</sup>C NMR were 235 used to characterise the LCO gas oils analytically. Elemental analysis is used to remove the 236 molecules which are composed by an element with a null experimental value. For example, if 237 238 sulphur presence has not been detected, all sulphureted molecules (benzothiophenes and dibenzothiophenes) are eliminated. In a similar way, all molecules belonging to a 239 spectrometric family which has not been found in mass spectrometry analyses are suppressed. 240 Spectrometric families are determined according to the number of aromatic and thiophene 241 rings in compounds. Thus the following families can be distinguished: saturates (paraffins and 242 243 cycloparaffins), monoaromatics (alkylbenzenes, tetralins...), diaromatics (naphthalenes, diphenyls...), triaromatics and compounds with more than three aromatic rings (anthracenes, 244 phenanthrenes...), benzothiophenes and dibenzothiophenes. Meanwhile, simulated distillation 245 enables to discard the molecules with a boiling temperature 5°C under the initial or 5°C over 246 247 the final boiling point. This correction is introduced due to the bias between the real boiling point and the value obtained from simulated distillation curve <sup>33</sup>. The "experimental" 248

molecular weight was calculated using an API correlation based on specific gravity and
 simulated distillation <sup>34</sup>.

#### 251 *3.1. Sensitivity of the stochastic method*

The average properties of the simulated mixture of molecules are calculated by the application of a number of linear mixing rules. An objective function (*OF*) is used to perform the comparison between calculated and measured properties. This function is the sum of the relative deviations between calculated and experimental data and it is given by Eq. (8):

$$0F = \frac{1}{N_p} \cdot \sum_{i=1}^{N_p} \delta_i \tag{8}$$

where  $N_p$  is the number of properties present in objective function and  $\delta_i$  is the relative deviation between the calculated and experimental values of property *i* which is calculated following Eq. (9):

260 
$$\delta_{i} = \frac{1}{N_{M,i}} \cdot \sum_{j=1}^{N_{M,j}} \frac{|x_{j,i}^{exp} - x_{j,i}^{calc}|}{x_{j,i}^{exp}}$$
(9)

where  $N_{M,i}$  is the number of measurements of property *i* (for example, the number of points in the simulated distillation) and  $X_{j,i}^{exp}$  and  $X_{j,i}^{calc}$  are, respectively, the experimental and calculated values of measurement *j* of property *i*.

An elitist genetic algorithm developed by Pereira *et al.*<sup>18</sup> was applied in order to minimise 264 this objective function by the modification of the parameters of the PDF's for the structural 265 attributes. Genetic algorithms <sup>22–24</sup>, as well as simulated annealing <sup>15,19–21</sup> and particle swarm 266 optimization<sup>35</sup>, are robust global optimizers, a characteristic required for their application in 267 stochastic models. Besides, according to its elitist nature, the applied methodology allows to a 268 certain percentage of individuals to move to the following generation (in this case, a 269 percentage of 50% was considered), with which the best individuals (i.e. those with the lowest 270 271 OF values) remain in the next generation.

The number of molecules is an important parameter in molecular reconstruction since an excessively low number would lead to an inadequate representation of the attributes of the represented mixture. Otherwise, the use of a large number of molecules would imply a significant increase in calculation time. In order to determine the optimal value for this parameter, the sensibility of the stochastic method has been tested by the generation of 100 mixtures of *N* molecules from a set of parameter distributions determined for a LCO gas oil. 278 *N* value was varied in a range between 10 and 20000 molecules and the average, minimum,

- 279 maximum and standard deviation values were determined for the objective function in each
- point (Figure 4). In addition, the time necessary to perform the calculation was also
- 281 represented.

It was observed that the increase of the size of the mixture leads to a drop of the objective function until attaining an asymptotic value at N = 5000 (Figure 4.a). The increase of the number of molecules also implies a rapprochement of the minimum and maximum values and a reduction in the standard deviation of the objective function. However, the drop of the standard deviation is very mild at N > 5000, while the calculation time continues to rise linearly with the size of the mixture (Figure 4.b). Then, a set of 5000 molecules was considered as optimal to perform the stochastic reconstruction of LCO gas oils.

### 289 3.2. Construction of the molecular representation of LCO gas oils

290 The analyses used in this case for the molecular reconstruction were the elemental analysis,

291 MS and simulated distillation. The elemental analysis provides information on the number of

thiophenes, while the information on the chemical structure is provided by MS and by

simulated distillation in the case of the average molecule size and size distribution. The

experimental and simulated properties were compared in Table 2 for a LCO gas oil.

295 Properties that were not used in reconstruction step (specific gravity, molecular weight, <sup>1</sup>H

NMR and  ${}^{13}$ C NMR) were calculated from the predicted molecular mixture and also

297 compared with the corresponding experimental values.

298 The properties of the mixture obtained after the application of the SR step are mostly in good

agreement with the analytical results. Some deviations are nevertheless observed in the

300 simulated distillation curve. These differences may be explained by the fact that the

301 distillation curve is calculated under the assumption that all molecules are perfectly separated

by the use of increasing boiling points. However, this is not strictly true (especially in the

region near the initial and final distillation points), since the chromatographic columns are not

304 completely apolar and separation is influenced by the polarity of the molecules <sup>29</sup>.

305 On the other hand, the coupled application of SR and SEM schemes led to a significant

306 improvement in the agreement between predicted and experimental data for most of the

307 properties (Table 2). The most meaningful effects were observed on more specific and

detailed analyses, such as NMR and MS, while only small improvements could be detected in

the more global measurements, such as in the case of elemental analysis.

On the following step, a total of eleven LCO gas oils have been reconstructed, and the 310 properties of the predicted mixtures have been compared with the corresponding experimental 311 data in order to perform the validation of the current methodology (Figure 5). It was found a 312 good agreement with the analytical results for most of the evaluated properties. However, a 313 deviation was detected for the predicted average molecular weight, which was mostly placed 314 below the value calculated from experimental data. This may be explained by the alterations 315 in the determination of the distillation curve, which imply a reduction in the boiling point of 316 the molecules with respect to their normal value. It leads to the prediction of molecules 317 318 smaller than their counterpart and, consequently, to reduce the average molecular weight of 319 the mixture.

- 320 These results show that the predicted set of molecules are proper molecular representations of
- 321 the corresponding LCO gas oils. Some of these simulated mixtures have been used as inputs
- 322 for the kinetic model of the hydrotreating of LCO gas oil.

#### 323 4. Application to the hydrotreating of LCO gas oils

- 324 Once the representative set of molecules has been generated for each LCO gas oil, the
- 325 hydrotreating reactions are simulated by applying the kMC method. The experimental data
- 326 used in this step has been collected from previous studies developed at IFP Energies nouvelles
- 327 about the hydrotreating of these oil fractions  $^{36}$ .
- 328 Three main type of reactions are involved in the hydrotreating process: hydrodesulphurisation
- 329 (HDS), hydrodenitrogenation (HDN) and hydrogenation of benzene and cyclohexane rings
- and of olefins. However, the reactions of hydrodenitrogenation and hydrogenation of olefins
- 331 will be neglected due to the lack of nitrogen and olefins in the mixture. Similarly, the HDS
- reactions are limited to heterocyclic structures since it has been considered that sulphur is
- only present in the mixture as thiophenes and their derivatives.
- Hydrogenation of aromatic rings (HDA), an exothermic and reversible reaction, is
- thermodynamically limited at typical hydrotreating conditions, so that the reverse reaction of
- dehydrogenation should also be considered. Korre *et al.*<sup>37</sup> have indicated that no partially
- 337 hydrogenated ring compounds, such as dihydronaphthalene and hexahydrophenanthrene, were
- found in the product stream, which shows that hydrogenation proceeds in a ring-by-ring
- manner. Besides it was detected that the higher number of aromatic rings, the higher reactivity
- of the molecule. This fact implies that polyaromatic species, such as pyrene, would be the
- 341 most reactive whereas that the HDA of monoaromatics, such as alkyl benzenes and tetralines,

would be the slowest. Other qualitative trend observed during the process was that, for the
molecules with more than two aromatic rings, the hydrogenation of the rings in the middle of
the molecule goes faster than in the case of the external rings <sup>38,39</sup>. To this, it should be added
the fact that the present of alkyl substituents and of cyclohexane rings increases the

346 hydrogenation rate  $^{37}$ .

HDS is an exothermic and basically irreversible reaction at the hydrotreating conditions <sup>40</sup> 347 through which sulphur is removed from the petroleum cuts in form of hydrogen sulphide. The 348 removal of this element is one of the main aims of hydrotreating process due to its catalyst 349 poisoning and pollution potential<sup>11</sup>. The HDS reactivity of sulphureted species closely 350 depends on their structure. According with this, non-heterocyclic compounds present a very 351 higher reactivity at hydrotreating conditions than heterocyclic species, such as thiophenes 352 353 family and derivatives. Different reactivities are also found within this last compounds family, in which thiophenes (Ts) and benzothiophenes (BTs) show a higher reactivity than 354 dibenzothiophenes (DBTs)<sup>41</sup>. The hydrotreating rates of the heterocyclic species are also 355 influenced by the presence of substituent groups in the positions adjacent to the sulphur 356 atom <sup>9</sup>. The desulphurisation process in these species goes through two different pathways: 357 (1) the direct removal of the sulphur atom without ring hydrogenation (hydrogenolysis 358 pathway) or (2) the saturation of the thiophene and the fused benzene rings prior to the 359 removal of the sulphur atom from the thiophene ring (hydrogenation pathway). The HDS of 360 Ts, BTs and unsubstituted DBTs mostly follows the hydrogenolysis pathway whereas 361 hydrogenation becomes the preferred pathway for DBTs at the same time that the degree of 362 substitution increases <sup>40,41</sup>. 363

Taking into account the above information, the reaction types reflected in Table 3 has been considered during the stochastic modelling of LCO hydrotreating. A set of reaction rules is also established in order to identify the reaction events from the structure of the molecule. Hydrogenation of aromatic rings and dehydrogenation of saturated rings have been included in the current model as ring-by-ring reactions while it have been considered that sulphur is removed from thiophene rings as  $H_2S$ . Besides, the rate constants of the HDT reactions must be specified.

In the case of hydrogenation and dehydrogenation reactions, their reaction rates can becalculated from Eq. (10) and (11), respectively:

$$R_{Hydro} = c_{Hydro} \cdot p_{H_2} \quad (10)$$

374 
$$R_{Dehydro} = c_{Dehydro} = \frac{c_{Hydro}}{\kappa_{eq}}$$
(11)

375 where  $c_{Hydro}$  and  $c_{Dehydro}$  are the stochastic reaction constants for hydrogenation and

dehydrogenation (s<sup>-1</sup>),  $K_{eq}$  is the equilibrium constant (mol·(mol·atm)<sup>-1</sup>), and  $p_{H^2}$  is the partial pressure of hydrogen (atm).

The expressions for the calculation of hydrogenation rate constants and the equilibrium
constants have been developed in previous studies <sup>17</sup>, starting from the quantitative
structure/reactivity correlations (QS/RCs) proposed by Korre *et al.*<sup>37</sup>. They are given in Eq.
(12) and (13), respectively:

$$\ln(c_{Hydro}) = -4.65 - 7.06 \cdot n_{H}^{1.18} - 1.08 \cdot \left|\frac{\Delta H_{R}^{0}}{R}\right| +0.616 \cdot N_{AR} + 0.330 \cdot N_{SR} - 2.80 \cdot N_{TR} \quad (12) -\frac{E_{a}}{R} \cdot \left(\frac{1}{T} - \frac{1}{T_{Ref}}\right)$$

$$\ln(K_{eq}) = 2.952 - 13.215 \cdot n_{H} + 5.196 \cdot 10^{-3} \cdot \left|\frac{\Delta H_{R}^{0}}{R}\right| -0.784 \cdot N_{SR}$$

$$-\frac{\Delta H_{R}}{R} \cdot \left(\frac{1}{T} - \frac{1}{T_{Ref}}\right)$$
(13)

383

where  $n_H$  is the stoichiometric coefficient for molecular hydrogen,  $\Delta H_R^0$  is the heat of reaction at 25°C (J·mol<sup>-1</sup>),  $N_{AR}$  is the number of aromatic rings in the molecule,  $N_{SR}$  is the number of saturated rings,  $N_{TR}$  is the number of thiophenes fused to the aromatic ring,  $E_a$  is the activation energy (J·mol<sup>-1</sup>), R is the ideal gas constant (J·(K·mol)<sup>-1</sup>), T is the temperature of the system (K), and  $T_{ref}$  is the reference temperature (K).

The values of the coefficients in the  $K_{eq}$  expression proposed by Korre *et al.*<sup>37</sup> have been 389 modified in order to obtain a better agreement between predicted and experimental 390 391 equilibrium data. The experimental data of a set of 21 compounds, including anthracene, phenanthrene and benzene, have been used to determine the new constants. For the 392 hydrogenation rate constant  $c_{Hydro}$ , the  $N_{TR}$  term was added to reflect the effect of the presence 393 of thiophene rings on the hydrogenation of aromatic rings, as observed in 394 hydrodesulphurisation kinetics  $^{40}$ . An exponential coefficient was also added to the  $n_H$  term to 395 improve the prediction of the kinetics of benzoic compounds. The hydrogen exponential 396 coefficient, the coefficient for the thiophene correction and the independent term in the 397 expression for  $k_{SR}$  were determined by minimising the difference between the predicted and 398

experimental data for the gas oil LCO1 (Table 4) during its hydrotreating at 300 °C (Figure 6.a).

A very good agreement between experimental and predicted data was obtained for 401 402 monoaromatic compounds. Besides, the fast hydrogenation of the aromatic compounds with 403 more than two aromatic rings was also properly reflected but some differences could still be 404 observed for saturates and diaromatic compounds. Despite they followed the same tendency than the predicted data, the experimental data showed a larger removal of diaromatic 405 compounds and also a higher concentration of saturated compounds. The introduction of 406 hydrogen exponential coefficient may be the cause for this deviation since, although it 407 provides a better prediction of benzoic compounds kinetics, it worsens the results for other 408 409 molecules, such as naphthalenes.

HDS reactions have been classified in five families according to the structure of the reacting
molecule and a rate parameter was assigned to each one (Table 4). The reaction rates are the
component directly given by the corresponding rate constant following Eq. (15):

$$R_{HDS} = c_{HDS} \qquad (15)$$

The rate constants  $c_{HDS}$  were obtained from the fit to the experimental data of the LCO gas oil which was previously used to determine the coefficients in Eq. (15) (Figure 6.b). In this case, the predicted curves perfectly fit to experimental data of both BT and DBT compounds.

In order to validate the current modelling methodology, the hydrotreating of the three LCO 417 gas oils in Table 4 has been simulated at different conditions of temperature and partial H<sub>2</sub> 418 pressure. These LCO gas oils present different composition profiles. LCO1 and LCO2 both 419 420 present a significant content in sulphur aromatics (mainly DBT in LCO1 and BT in LCO2) 421 while, in the case of LCO3, the content in these compounds is very lower (less than 1.5% wt) and the addition of sulphides such as dimethyl disulphide (DMDS) is required in order to 422 reach an adequate partial pressure of H<sub>2</sub>S over the process. Besides, LCO3 is mainly 423 composed by saturated compounds (almost 60% wt) unlike the other two gas oils, in which 424 425 diaromatics are the most abundant compounds.

The predicted results after 1 h of operation have been compared with analytical data in the parity plots depicted in Figure 7. A good agreement with experimental data was found for saturated and monoaromatic compounds with an average relative error lower than 14%. The prediction of the species with three or more aromatic rings was accurate in most of the

experimental points and a very good fit was also found for sulphur aromatic compounds. 430 Performance variations due to modifications in operational conditions, i.e. temperature and 431 hydrogen partial pressure, were contemplated and well-reflected on the current model. On the 432 other hand, as in the case of LCO1, some differences were also detected for diaromatic 433 compounds in LCO3. High complexity of mixtures, which leads to the use of correlations to 434 determine the reactivity of each molecule in hydrogenation/dehydrogenation processes, 435 implies a greater difficulty to accurately predict the content in all aromatic species, although a 436 good global agreement between predicted and experimental data was reached. 437

#### 438 **5.** Conclusions

A stochastic two-steps procedure has been described and validated on the hydrotreating of 439 440 three LCO gas oils at different operational conditions. In the first step, a molecular 441 reconstruction algorithm is used to represent the feedstock by means of a set of molecules which mixture properties are similar to those of feedstock. This algorithm is formed by the 442 443 combination of two methods: stochastic reconstruction (SR) and reconstruction by entropy maximization (REM). The SR method leads to obtain a set of molecules typical of a given 444 445 feedstock while the molar fraction of molecules is adjusted using the REM method in order to improve the predicted mixture properties. Then, the generated set of molecules is used as 446 input in the second step concerning the molecule-based kinetic modelling of the hydrotreating 447 process and in which a kinetic Monte Carlo (kMC) method is applied. The expressions for the 448 449 calculation of adsorption, equilibrium and hydrogenation/dehydrogenation rate constants have been obtained by applying the quantitative structure/reactivity correlations (QS/RCs). 450

451 The current stochastic methodology has demonstrated to be a valid tool for the reconstruction 452 of LCO gas oils by combining their available analytical data. This procedure can be used not 453 only to get the molecular information that is not provided by analytical data but also to obtain 454 an accurate molecular representation which can be used as input in kinetic models. Monte Carlo techniques have also given good results in their application on the kinetic simulation of 455 the hydrotreating of LCO gas oils. Moreover, the simulation of the reactions does not require 456 a pre-defined kinetic network due to it is generated as the reactions proceed. Besides, the use 457 of the corrected QS/RCs led to a good prediction of molecular reactivities in complex 458 mixtures of hydrocarbons such as LCO gas oils. 459

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#### 564 Figure captions

565 **Figure 1.** Flowchart of the SR-REM algorithm

566 Figure 2. Flowchart of the kMC method

- 567 **Figure 3.** Building diagram for LCO gas oils
- 568 Figure 4. Evolution as a function of the number of molecules in the predicted mixture of (a)
- the average value of the objective function (white diamonds) and the maximum (black
- triangles) and minimum (black squares) values (b) the CPU time required (white diamonds)
- and the standard deviation of the objective function (black crosses)
- **Figure 5.** Parity plots for the predicted properties of eleven gas oils after SR-REM
- application: (a) density  $(g/cm^3)$ , (b) molecular weight (g/mol), (c) <sup>13</sup>C NMR signatures (%
- mole): primary saturated  $CH_3$  (black diamonds), secondary saturated  $CH_2$  (white squares),
- tertiary saturated CH (white rounds), aromatic CH (black crosses), condensed aromatic C
- 576 (white triangles) and substituted aromatic C (black rounds), and (d) <sup>1</sup>H NMR signatures (%
- 577 mole): diaromatic H (black diamonds), monoaromatic H (white squares), H alpha (white
- rounds), H beta (black crosses) and H gamma (white triangles)
- Figure 6. Comparison between experimental (points) and predicted values (lines) for LCO1:
  (a) for aromatic families: saturates (black diamonds and black continuous line),
- 581 monoaromatics (black squares and black discontinuous line), diaromatics (white squares and
- 582 grey discontinuous line) and compounds with more than two aromatic rings (white diamonds
- and grey continuous line); and (b) for sulphur families: benzothiophenes (black squares and
- 584 continuous line) and dibenzothiophenes (white squares and discontinuous line). All data are
- 585 expressed as weight fraction (%)
- **Figure 7.** Parity plots for the compounds concentration predicted by means of kMC method after 1 h of hydrotreating: (a) saturates, (b) monoaromatics, (c) diaromatics, (d) compounds
- 588 with more than two aromatic rings and (e) sulphur compounds: benzothiophenes (black
- diamonds) and dibenzothiophenes (white rounds). In the case of benzothiophenes all points
- 590 overlap each other due to their similar values close to point (0.0, 0.0)
- 591

 Table 1. Structural attributes of LCO gas oil molecules

	Structural attribute	Values	Distribution	Parameter names
1	Type of molecule	0 or 1	Histogram	0
2	Number of benzene rings per core	1,, 4	Gamma	1 and 2
3	Number of naphthenic rings per core	0,, 4	Gamma	3 and 4
4	Number of thiophenes per core	0 or 1	Histogram	5
5	Acceptance probability for aromatic carbon CH	0 or 1	Histogram	6
6	Acceptance probability for naphthenic carbon CH <sub>2</sub>	0 or 1	Histogram	7
7	Type of the side chains	0, 1 or 2	Histogram	8 and 9
8	Length of the paraffinic chains	>0	Gamma	10 and 11

**Table 2.** Comparison between experimental and calculated properties after the SR and REM

 steps

		Experimental	Simulated (after SR)	Simulated (after SR- REM)
	Carbon	80.05	80.85	80.00
Elamental analysis (9/t)	Ludrogen	09.93	09.03	09.99
Elemental analysis (%WI)	Rydrogen System	9.21	9.55	9.13
	Sulphur	0.84	0.82	0.86
	Initial boiling point	143	143	143
	5%	214	175	211
	10%	231	211	232
	20%	250	250	250
	30%	259	268	267
	40%	273	288	270
Simulated distillation	50%	284	314	284
(°C)	60%	299	334	299
	70%	314	351	315
	80%	330	369	334
	90%	340	385	355
	90%	363	303	383
	Final hailing point	202	402	505 402
	Final boiling point	398	405	405
	Saturates	11.00	10.49	11.12
	Monoaromatics	12.90	17.07	12.98
	Diaromatics	58.40	49.25	58.36
Mass spectrometry (%wt)	Triaromatics	8.50	16.40	8.48
	Tetraaromatics	3.00	1.53	2.97
	Benzothiophenes	4.00	1.39	3.96
	Dibenzothiophenes	2.20	3.86	2.13
	Aromatic CH	39.10	34.23	36.62
	Fused aromatic C	8.00	12.17	12.03
	Substituted aromatic C	15 30	14 69	14.95
C NMR (%wt)	Saturated CH <sub>2</sub>	15.30	15.62	14.96
	Saturated CH <sub>2</sub>	19.20	19.02	18.19
	Saturated CH	2 70	3 03	3 25
	Saturated CII	2.70	5.95	5.25
	Diaromatic H	25.70	24.26	27.64
	Monoaromatic H	2.30	3.40	2.59
H NMR (%wt)	Saturated alpha H	33.90	27.39	27.61
	Saturated beta H	27.30	29.33	27.80
	Saturated gamma H	10.80	15.61	14.37
Others	Molecular weight (g/mol)	192	194	184
	Density 20°C (g/cm <sup>3</sup> )	0.9701	0.9710	0.9729

Type of reaction	Reaction	$c (s^{-1})$
Hydrogenation	$\downarrow$ + 2H <sub>2</sub> $\rightarrow$	Eq. (10)
Dehydrogenation	→ ↓ 2H <sub>2</sub>	Eq. (11)
	Hydrogenolysis of thiophene and their derivatives	
	$\begin{array}{c} & & \\$	138.90
	Hydrogenolysis of BT and their derivatives	
	$\begin{array}{c} & & \\$	55.60
	Hydrogenolysis of DBT and their derivatives	
Hydrodesulphurisation	$\begin{array}{c} & & \\$	19.40
j i i i i i i i i i i i i i i i i i i i	Hydrogenolysis of 4-alkyl-DBT and their derivatives	
	$ \begin{array}{c} & & \\ & & $	0.56
	Hydrogenolysis of 4,6-dialkyl-DBT and their	
	derivatives $+ 2H_2 \rightarrow + H_2S$	0.06

## **Table 3.** Reaction types and their parameters (c)

	LCO1	LCO2	LCO3
Hydrotreating conditions			
$pH_2(atm)$	69.1	95.1	46.1
$T(^{\circ}C)$	300/330	300/330	300/310/320
Composition			
$\hat{C}(\%wt)$	88.01	88.57	87.23
H(%wt)	10.51	9.74	12.57
S(%wt)	1.48	1.69	1.45
Saturates (%wt)	28.58	19.85	59.84
Monoaromatics (%wt)	16.14	22.23	9.55
Diaromatics (%wt)	34.24	38.96	26.20
Triaromatics and more (%wt)	11.49	8.95	3.19
BT (%wt)	2.70	6.39	0.67
DBT (%wt)	6.86	3.61	0.56

**Table 4.** Hydrotreating conditions (partial  $H_2$  pressure and temperature) and properties fromSR-REM algorithm for the three LCO gas oils used as input in the kMC method

Figure 1.



## Figure 2.



Figure 3.



Figure 4.







Figure 6.



Figure 7.

