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Optical Extinction in a Single Layer of Nanorods

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We demonstrate that almost 100% of incident photons can interact with a monolayer of scatterers in a symmetrical environment. Nearly perfect optical extinction through free-standing transparent nanorod arrays has been measured. The sharp spectral opacity window, in the form of a characteristic Fano resonance, arises from the coherent multiple scattering in the array. In addition, we show that nanorods made of absorbing material exhibit a 25-fold absorption enhancement per unit volume compared to unstructured thin film. These results open new perspectives for light management in high-Q, low volume dielectric nanostructures, with potential applications in optical systems, spectroscopy, and optomechanics.

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Enhancing light-matter interactions at the nanometer scale is a key for many applications in the area of photonics, biophysics and material sciences [1,2]. Metallic particles are the archetype of nano-objects that can lead to strong interaction with light due to plasmonic resonances, with the drawback of intrinsic metal absorption [3]. Conversely, the weak scattering cross section of tiny dielectric nanoparticles originates from their nonresonant nature, making them inefficient for optical manipulation at the nanoscale. However, the extinction cross section can be increased by coherent multiple scattering in assemblies of nanoparticles, offering another degree of freedom to manipulate their optical response. It has been shown theoretically that it can lead to extremely sharp geometric resonances [4–9]. From the experimental point of view, arrays of resonant, metallic nanoparticles demonstrated the potential of the effect [10,11], making the localized surface plasmon resonance much narrower [12,13]. Arrays of nonresonant, dielectric nanorods should offer new possibilities for even higher quality-factor geometric resonances [14,15]. Indeed, sharp reflection resonances [7,8] and absorption enhancement [9] have been predicted for dielectric, sub-wavelength cylinder arrays.

It has to be emphasized that the scattering properties of nanoparticles are substantially modified, or even suppressed, in the proximity of a surface [6,7,16–19]. Here, we study a free-standing array of nanorods, with a filling fraction around 0.15. In contrast with the periodic nanostructures studied extensively in the past ten years (nanohole arrays in metal films [20,21], metal nanoparticle arrays [10–13], high-index-contrast gratings [22], guided-mode resonant structures [23,24]), resonant effects cannot be attributed to localized resonances neither to interactions between nanostructures mediated by electromagnetic

waves in matter (surface waves or guided modes in dielectric layers).

A free-standing monolayer of dielectric nanorods can be considered as a model structure for direct interactions in free space between nonresonant structures. In this Letter, geometric resonances are revealed by angle-resolved transmission and reflection measurements. We demonstrate nearly perfect optical extinction, and more than one order of magnitude absorption enhancement as compared to a same-volume thin film. The results can be fully explained by a multiple scattering effect and are in good agreement with an analytical model which includes the geometry and the material properties of the rods. It is also shown numerically that very large electric-field intensities can be obtained at the resonance wavelength, with field enhancements as large as 10⁵ for nanorod diameters of 50 nm.

Silicon nitride (SiN_x) deposited by plasma-enhanced chemical vapor deposition exhibits both transparent and absorbent optical behaviors for wavelengths between 1.5–5.5 μ m [25]. For this reason, it has been used to fabricate the studied free-standing membranes made of subwavelength rods. Membranes with 1D patterns were developed on Si substrates and drilled by dry etching [26,27] on large surface areas $(2.6 \times 2.6 \text{ mm}^2)$, having 500 nm square section bars and 3 μ m period. To increase the rigidity of the membrane, support bars were added in the fabrication design, as shown in Fig. 1(b). Their period was set to be large enough $(20 \ \mu\text{m})$ to ensure a negligible optical effect in the spectral range of interest.

Angle-resolved absolute transmission (T) and reflection (R) measurements were performed using a Fourier-transform infrared spectrometer with an InSb detector. The specular reflection measurements have been normalized with a gold mirror placed in the proximity of the membrane. The spectral resolution was set to 5 cm⁻¹

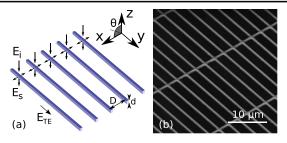


FIG. 1 (color online). Free-standing dielectric grating. (a) The schematic illustrates the geometrical parameters of the structure, measurement arrangement and the multiple scattering mechanism. (b) Scanning electron microscopy image of a 1D free-standing SiN_x membrane of 3 μ m period (D) made of square rods of 500 nm size (d).

(wavelength range: $1.5-5.5 \mu m$) and a homemade achromatic optical system allows a $\pm 0.5^{\circ}$ angular resolution [28]. An artifact observed around 4.25 μm is produced by the change of the CO₂ content in air during the experiments. The free-standing membrane is illuminated in the plane perpendicular to the rod axis with an incident wave vector $k = (k_x, k_z)$. The spectra have been recorded under an incidence angle θ ranging from 0° to 60° in 0.5° increments. The illumination area was set to 2.2 mm² to take into account a large number of rods (over 500).

In Fig. 2 is plotted the experimental dispersion diagram of the optical extinction 1- $T(\omega, k_x)$, where $T(\omega, k_x)$ is the specular transmission in transverse electric (TE) polarization (electric field parallel to the rod axis), $\omega = 2\pi c/\lambda$ is the frequency, λ is the wavelength, and $k_x = (\omega/c)\sin\theta$ is the x component of the incident wave vector. This diagram shows sharp-bright features. At normal incidence only one is visible, the corresponding transmission spectrum (inset, Fig. 2) reveals that nearly total optical extinction (94%) is

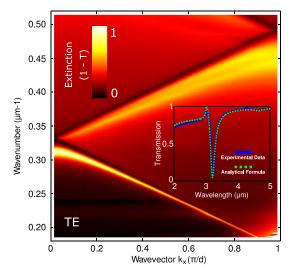


FIG. 2 (color online). Extinction coefficient in the (ω, k) plane. Close to Rayleigh frequencies, almost complete extinction is achieved due to geometric resonance. (Inset: Theoretical and experimental transmission spectra at normal incidence, TE).

achieved in spite of (i) the low fill factor (15%) of the grating and (ii) the perfect transparency of the material (no loss at 3.2 μ m). The optical response of the dielectric membrane changes in a very narrow spectral range from transparent to opaque behavior. From almost total transmission at 3 μ m, the signal drops sharply at 3.2 μ m to just 6%.

The dispersion diagram is characterized by two branches with bright-dark bands. The resonances occur close to the onset of a new propagating order, i.e., close to the Rayleigh frequency given by $\lambda_m = D/m(\pm 1 - \sin(\theta))$, where m is an integer ($m = \pm 1$ in Fig. 2). The optical transmission of this system can be considered as the sum of two components: direct transmission and light scattered by the rods, inducing constructive and destructive interferences with characteristic Fano line shape [29].

The physical mechanism of this geometric resonance is closely related to a multiple scattering mechanism. Each subwavelength rod behaves like an individual scatterer with a dipolar response. It can be modeled as an infinite circular cylinder with a polarizability $\alpha \approx \alpha_0[1-i\frac{k^2}{4}\alpha_0]^{-1}$, where $\alpha_0=\pi a^2(\epsilon-1)$ is the static polarizability, a the cylinder radius, and ϵ is the dielectric permittivity of the rods. When illuminated by a plane wave, each rod of the array re-radiates a field proportional to its dipole moment p_y . Conversely, the incident field on each rod is the sum of the incident plane wave (E_i) and the scattered fields (E_s) from the other rods, as sketched in Fig. 1(a). The dipolar moment can be written as

$$p_{y} = \hat{\alpha}E_{i}, \qquad \hat{\alpha} = \left(\frac{1}{\alpha} - G_{b}k^{2}\right)^{-1}, \tag{1}$$

where the effective polarizability $\hat{\alpha}$ accounts for the multiple scattering mechanism. G_b is the dynamic depolarization term which only depends on the geometrical parameters, i.e., the period D, the radius a, as well as the wavelength and the angle of incidence θ . The geometric resonance is defined by the pole of the effective polarizability. This description leads to an analytical model for the far-field response of the membrane [7].

To effectively compare the measured and calculated spectra of T and R, the parameters used in the model are the following: grating period $D = 3 \mu m$, radius of the rods $a = 0.3 \mu m$ to maintain the area equivalence of the rod section. In the spectral range of interest, the dielectric constant of SiN_x material is influenced by absorption bands due to the stretching of N-H and Si-H bonds at about 3 and 4.6 μ m, respectively. These bounds are related with the presence of hydrogen in the plasma-enhanced chemical vapor deposition process [25]. To account for these effects, the complex values of the dielectric constant have been retrieved by using the reflection and transmission measurements of an unstructured SiN_x membrane with similar thickness and fabrication method [27]. At last, the spectral shift of the resonance within the convergence angle of the incident beam is of the order of its linewidth. This effect has been taken into account by convoluting the calculated spectra with a 0.5° waist Gaussian profile [27].

The results are shown in Fig. 3(a) for eight different angles of incidence (5° to 40° degrees, alternated for clarity, TE polarization). A quantitative agreement is observed between the experimental and the theoretical results for both transmission and reflection. The small remaining discrepancies between simulated and experimental curves are attributed to fabrication imperfections (roughness, inhomogeneities) of the membrane. The line shape and the decrease of the linewidth with angle are well reproduced by the model, the modulations of $R_{\rm max}$ and $T_{\rm min}$ corresponding to the transparency and absorption bands of the material.

The resonance can lead to perfect optical extinction below the onset of the first diffraction order for a nonlossy material [7], with a huge enhancement of the field on the rods and between them [14]. For a material with an absorption band, strong absorption resonances were also predicted [9]. In this context, it is instructive to present the absorption spectra [see Fig. 3(b)]. We first consider the absorption spectrum for a given incidence angle. It is

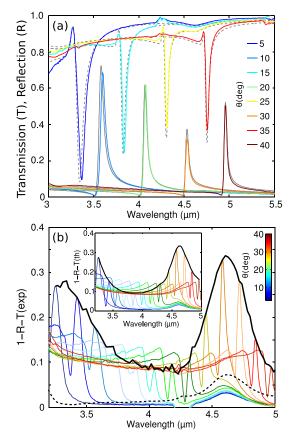


FIG. 3 (color online). Experimental and theoretical spectra for different incidence angles, from 5° to 40° (resonance shift from short to long wavelengths). (a) Transmission and reflection (simulated spectra: gray dotted lines). (b) Absorption spectra and the absorption of the unstructured membrane at $\theta=15^\circ$ (black dotted line) (inset: the corresponding simulated absorption spectra). The envelopes of the absorption maxima at resonance are depicted in black full lines.

computed as A=1-R-T, and includes light diffusion due to inhomogeneities and residual roughness, which is supposed to be negligible. Below the resonance wavelength, the curve is dominated by the contribution of the first-order diffraction wave (about 10%). Above the resonance wavelength, the absorption drops almost to zero. It is worth mentioning that off-resonance (e.g., blue curves at 4.6 μ m) a membrane with only 15% material is absorbing just 50% less than a full nonstructured membrane (3% and 7%, respectively).

At resonance, the absorption spectrum features a maximum. Remarkably, when the resonance is matching the Si-H band ($\lambda \simeq 4.6 \mu m$), the absorption efficiency of the membrane is enhanced by more than one order of magnitude as compared to nonresonant absorption at the same wavelength, reaching 33%. This value is comparable with the maximum value of 50%, predicted for the absorption of similar systems [9]. The absorption cross sections can be defined as: $\sigma_a = D(1 - T - R)$ [13], where σ_a is expressed in unit of length due to the translational symmetry in the y direction. The volume absorption coefficient $\alpha_v =$ σ_a/d^2 , defined as the cross section per unit particle volume [16], reaches a value of $\alpha_v = 4 \ \mu \text{m}^{-1}$. It can be compared to the absorption coefficient of the unstructured membrane, defined as $\exp(-\alpha d) = R + T$: $\alpha = 0.16 \ \mu \text{m}^{-1}$. These results show that for a fixed volume of material, the absorption enhancement factor in the nanorod array compared to the thin film case reaches 25. This behavior is completely reproduced by the model, as shown in the inset of Fig. 3(b).

These properties can be fully extended to 2D arrays of nanorods, much more suited to practical applications. Indeed, the square 2D arrays allow improved robustness and insensitivity to polarization at normal incidence. Freestanding membranes with square 2D patterns were fabricated with the same geometrical parameters as the 1D analogue (width of the rods 500 nm, grating period 3 μ m); see Fig. 4(a). Figure 4(b) shows the transmission spectra measured at normal incidence. We obtain 97% optical extinction for both polarizations [TE and transverse magnetic (TM)]. As previously, Fano resonances are observed, at slightly larger wavelengths (3.36 μ m) with even higher extinction efficiency than in 1D structures. Actually, at normal incidence, the structure behaves as a superposition of two orthogonal 1D nanorod arrays.

At oblique incidence, the optical response is modified as compared with the 1D case. The dispersion diagrams of the optical extinction are shown in Fig. 4(c) and 4(d). For the TE case, the two dispersion branches observed in the 1D grating are also present. It originates from multiple scattering involving the excitation of the dipole moment p_y of the y axis nanorods. An additional thin, flat band appears at 3.1 μ m. It follows the Rayleigh anomalies of the diffracted waves having the in-plane wave vectors $\mathbf{k} = (2\pi/\lambda)\sin\theta\mathbf{x} \pm (2\pi/D)\mathbf{y}$. The dipole moments p_x of the x axis nanorods are excited by the small x component of the

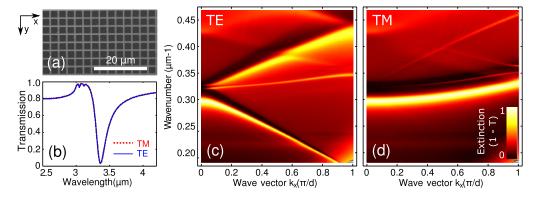


FIG. 4 (color online). Free-standing dielectric membranes with a 2D square design. (a) Scanning electron microscopy image of the structure (period $D=3~\mu m$ and rod size d=500~nm). (b) Transmission spectra acquired at normal incidence in both TE and TM polarizations and (c)–(d), Optical extinction dispersion relation for the two orthogonal polarizations.

electric field of these diffracted waves for $\theta \neq 0$ [30,31]. A similar, wider band is observed for TM polarization. It is related to the dipole moments p_x of the x axis nanorods.

In relation with the sharp extinction resonances, the nanorod array exhibits very high field enhancements. The map of the electric field intensity, and the evolution of the field enhancement with the rod diameter, have been calculated by rigourous coupled-wave analysis and are reported in Fig. 5, for 1D arrays [27,32]. It shows that the maximum of the electric field is located in the center of the nanorods. Importantly, as the nanorod diameter d decreases, the electric-field intensity increases as $(\lambda/d)^4$ [14]. Field enhancements as large as 10^5 are obtained for nanorod diameters of 50 nm. It opens the way to the conception of high-Q dielectric structures with very low volumes, despite the large surface area covered by the nanorod array. In view of applications, the influence of the finite size of the array on the mode volume and on the

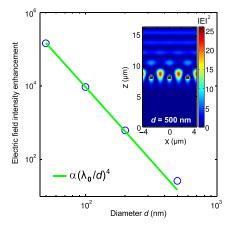


FIG. 5 (color online). Electric-field enhancement in 1D nanorod arrays as a function of the diameter d, at resonance ($\theta=0^{\circ}$). Circles: full electromagnetic calculation. Line: $(\lambda_0/d)^4$ law, where the resonance wavelength can be approximated by $\lambda_0 \simeq 3~\mu \mathrm{m}$ for small diameters. Inset: Map of the electric-field intensity for $d=500~\mathrm{nm}$, normalized to the incident field. The position of the rods is shown with black squares.

field-enhancement is an important issue that should be addressed. It is also important to note that the linewidth and the spectral position of the resonance can be easily tuned by varying the geometrical parameters of the nanorod array (period, diameter) or the external environment. The resonance is not restricted to the range of frequencies of plasmons, and can be shifted from the visible to the far-IR wavelength range.

In conclusion, we have described and measured the farfield response of free-standing, subwavelength dielectric nanorod arrays. Extremely sharp peaks together with nearly total extinction are experimentally demonstrated. When the rods are made of a lossy material, an absorption enhancement factor of 25 is found. These singular properties originate from two important features: (i) scatterers are nonresonant and much smaller than the wavelength, and (ii) free-space interactions between the scatterers. It is worth noticing the similarities between the coherent multiple scattering mechanism evidenced in nanorod arrays, and the well-known Bragg diffraction arising in the threedimensional arrangement of a crystal lattice. Both phenomena are based on low cross-section scatterers. However, the constructive interference of the Bragg diffraction mechanism involves a large number of lattice planes. Surprisingly, it is shown here that nearly 100% of incident photons interact with a single layer of sparse scatterers periodically arranged in a symmetrical environment. The optical response is quantitatively reproduced with an analytical model based on multiple light scattering in free-space. This is a fundamental difference with freestanding sub-wavelength gratings having higher filling fraction (photonic crystal slabs, guided-mode resonant structures, high-index contrast structures, ...), whose optical response is mainly driven by guided modes in the slab. We also emphasize the differences with free-standing transmission gratings acting as diffraction gratings in the short-wavelength range, or effective medium layers in the long-wavelength range [33].

The properties of free-standing nanorod arrays could have an important impact for applications in surface enhanced Raman scattering [34], fluorescence enhancement [35], nonlinear optics [36], and coherent light emission [37]. Beyond, a wide variety of stop-band filters and selective mirrors can be achieved with nanostructured membranes, with potential applications in multispectral imaging [38,39] and optomechanics [40–42]. As an illustration, an efficient optomechanical interaction has been achieved recently with unstructured membranes placed in a high-finesse cavity [41,42]. With increased reflectivity and drastic reduction of the mirror mass, free-standing nanorod arrays could offer strong improvement of the optomechanical coupling, and open new possibilities to probe the quantum regime of mechanical systems.

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