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# A CHR-Based Solver for Weak Memory Behaviors\*

Allan Blanchard<sup>1,2</sup>, Nikolai Kosmatov<sup>1</sup>, and Frédéric Loulergue<sup>2</sup>

<sup>1</sup> CEA, LIST, Software Reliability Laboratory, PC 174, 91191 Gif-sur-Yvette France  
firstname.lastname@cea.fr

<sup>2</sup> Univ Orléans, INSA Centre Val de Loire, LIFO EA 4022, Orléans, France

## Abstract

With the wide expansion of multiprocessor architectures, the analysis and reasoning for programs under weak memory models has become an important concern. This work presents an original constraint solver for detecting program behaviors respecting a particular memory model. It is implemented in Prolog using CHR (Constraint Handling Rules). The CHR formalism provides a convenient generic solution for specifying memory models, that benefits from the existing optimized implementations of CHR and can be easily extended to new models. We briefly present the solver design, illustrate the encoding of memory model constraints in CHR and discuss the benefits and limitations of the proposal.

## 1 Introduction

Concurrent programs are hard to design and implement, especially when running on multiprocessor architectures. Multiprocessors implement weak memory models [2] that allow, for example, instruction reordering or store buffering. Thus multiprocessors exhibit more behaviors than Lamport’s *Sequential Consistency* (SC) [9], a theoretical model where the execution of a program corresponds to an interleaving of the different threads.

Recent years have seen many works on formalization of weak memory models, both on hardware and software sides [12, 4, 10, 5, 6, 3, 1]. These formal models give us a way to compute, given a program and a memory model, the set of concrete executions allowed by the model. We can determine for example whether all executions of a program under a certain model are admitted under SC, and therefore, whether we can reason about this program using an interleaving semantics.

We propose a constraint solving based technique that allows to determine all admissible executions of a program under a memory model. This technique relies on Prolog and CHR (Constraint Handling Rules) [8]. A CHR program is a list of rules that act on a store of constraints, by adding or removing constraints in this store. The rules are activated if a combination of constraints in the store match the head of the rule (and satisfy an optional Prolog predicate called the *guard*). In our case, constraints are relations between instructions that are basically related to their order of execution. Rules are used to propagate information and to

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$p_0$ :	Thread 0 $(i_{00}) \mathbf{x} = 1;$ $(i_{01}) \mathbf{r}_0 = \mathbf{y};$		Thread 1 $(i_{10}) \mathbf{y} = 1;$ $(i_{11}) \mathbf{r}_1 = \mathbf{x};$	<pre> 1 :- include(sc). % :-include(tso).% for SC or TSO 2 3 program_p0(Vars, [Thread0,Thread1]) :- 4   Vars = [ x , y ], 5   Thread0 = [ (st,x,1), (ld,y,R0) ], 6   Thread1 = [ (st,y,1), (ld,x,R1) ]. 7 program_p1(Vars, [Thread0,Thread1]) :- 8   Vars = [ x , y ], 9   Thread0 = [ (st,x,1), f(any,any), (ld,y,R0) ], 10  Thread1 = [ (st,y,1), f(any,any), (ld,x,R1) ]. 11 12 ?- program_p0(Vars, P), apply_model(Vars, P). </pre>
$p_1$ :	Thread 0 $(i'_{00}) \mathbf{x} = 1;$ $(i'_{01}) \mathbf{fence};$ $(i'_{02}) \mathbf{r}_0 = \mathbf{y};$		Thread 1 $(i'_{10}) \mathbf{y} = 1;$ $(i'_{11}) \mathbf{fence};$ $(i'_{12}) \mathbf{r}_1 = \mathbf{x};$	

Figure 1: (a) Two programs  $p_0$  and  $p_1$ , and (b) their implementations with a solving request.

produce, from a given set of relations, more relations (characterizing the instruction ordering) that were previously unknown in the execution.

**The contributions** of this paper include a novel CHR-based technique for detection of admissible behaviors under memory models and a constraint solver prototype<sup>1</sup> implementing this technique for SC, TSO and PSO models. We discuss the benefits and limitations of this approach, and show how the use of CHR allows us to define our model in a concise and intuitive way, taking advantage of a well-established specification and solving mechanism.

**Outline.** Section 2 presents weak memory models vs. SC model. Section 3 presents the solver, explains its functionality and optimizations, and points out some soundness and performance aspects. Section 4 discusses its benefits and limitations, and gives future work.

## 2 Weak Memory Models

A *memory model* describes how a program can interact with memory during its execution. Technical manuals of processors are often vague, and sometimes erroneous. Formal descriptions are necessary, but must be as abstract as possible to ease reasoning about them.

In a parallel context, Lamport [9] proposed *sequential consistency* (SC) where the semantics of the parallel composition of two programs is given by the interleaving of the executions of each program. For example, if we consider that two memory locations  $x$  and  $y$  initially contain 0 and that  $r_i$  are processor registers, the program  $p_0$  in Fig. 1a can only give one of the three possible final results: either  $r_0 = 0$  and  $r_1 = 1$ , or  $r_0 = 1$  and  $r_1 = 1$ , or  $r_0 = 1$  and  $r_1 = 0$ . The last result is obtained by the interleaving  $(i_{10})(i_{11})(i_{00})(i_{01})$ .

However, for the sake of performance, no current multiprocessor provides a sequentially consistent memory model. Models are *relaxed* or *weak* with respect to SC. In most processors, it is also possible to obtain the result  $r_0 = 0$  and  $r_1 = 0$ , not justifiable by an interleaving. To avoid this behavior, one can use *memory barriers* or *fences* that forbid reorderings through them (see program  $p_1$  of Fig. 1a).

There exist operational models for some weak memory models, for example [6]. However this kind of approaches is not really appropriate to capture the various existing memory models of processors and programming languages. Most approaches are based on constraints expressed as partial orders on events. In the case of memory models, the events of interest are related to memory: *read* (*load*) from, and *write* (*store*) to a memory location, as well as memory barriers.

Constraint-based approach have already been used to model memory models, see for example [11]. In this work, we propose a different approach using the particular case of CHR. Following [3], we use several relations to formalize memory models. The PO relation, for

<sup>1</sup>Available at <http://frederic.loulergue.eu/CHR/wmm.tar.gz>.

“program-order”, simply expresses that an instruction appears before another one in the list of instructions defining a thread. The CO relation, for “coherency-order”, is a per location total order of the write actions. The RF relation, for “read-from”, determines which write operation assigned the value at a location before this value is read from this location: it associates a unique write to each load. The FR relation, for “from-read”, relates each load operation with each of the write operations (if any) that overwrite the value after it was read by the load.

## 3 The Solver

### 3.1 Overview

A (candidate) execution can be determined by a total ordering (permutation) of memory stores to each location (CO), and an association of a unique store to each load (RF). (They can conflict PO, i.e. the initial order of instructions in threads.) Relations between instructions are modelled by CHR constraints. To compute admissible executions of a program under a given model, we generate all candidate executions (represented by the aforementioned relations), and filter them on-the-fly using CHR rules defined for the model. The set of candidate executions is easily generated (in our case, by a Prolog program using backtrack) by enumerating all possibilities of these relations. Without additional constraints, this set contains the executions authorized by a very weak generic model [3] allowing lots of intuitively incoherent behaviors (e.g. where, within the same thread, an old value that has been overwritten can still be read from the location after the overwriting operation).

To keep only executions allowed by the target memory model, we define CHR rules to filter out cases where the relations between instructions of a given execution are inadmissible. The principle is to compute the transitive closure of certain ordering relations (depending on the model) that the execution must satisfy according to the model. If the computed transitive closure exhibits a cycle, then, according to the model, some program instruction has to be executed strictly before itself, which is incoherent: the execution is not allowed. If this closure has no cycles, the ordering relations are admissible and the execution is allowed by the model. To efficiently use CHRs, we declare all CHR rules needed by the model before the Prolog program, so that they detect incoherent executions as early as possible during their generation.

**Language.** An input program is modelled by the list of declared variables and the list of lists of instructions of its threads. The implementation of  $p_0$  and  $p_1$  in Prolog is shown in Fig. 1b, lines 4–6, 8–10. The considered instructions are either a memory operation (load or store) or a fence. A load (resp. a store) is a tuple  $(ld, loc, v)$  (resp.  $(st, loc, v)$ ) where  $loc$  is the read (resp. written) location and  $v$  its value. A fence, written  $f(OP1, OP2)$ , takes as parameters the types of instructions whose order we want to force. For example, by writing  $f(st, ld)$ , we state that any store preceding this fence is ordered strictly before any load following the fence. The notation  $any$  expresses “any type of operation”. For example,  $f(ld, any)$  states that all loads preceding the fence are ordered before any instruction that follows it.

### 3.2 The Generic Model

A first step is to take the list of instructions of each thread and to enrich them by the thread identifier and instruction index in the list. As we perform this operation, we also create CHR constraints  $i/5$ ,  $fence/4$  for memory operations and fences of the form  $i(n\_thread, n\_inst, op, loc, v)$  and  $fence(n\_thread, n\_inst, t\_op1, t\_op2)$ . In this model we consider PO, CO, RF, FR and barrier relations, defined by CHR constraints

```

1 :- chr_constraint rel/3, trace/3, cycle/2.
2 trace(R,Begin,End) \ trace(R,Begin,End) <=> true.
3 trace(R,Begin,End), rel(R,End,Begin) <=> cycle(R,Begin).
4 trace(R,Begin,End), rel(R,End,Next) ==> inf(Begin,Next) | trace(R,Begin,Next).
5 rel(R,Begin,End) ==> inf(Begin,End) | trace(R,Begin,End).

```

Figure 2: Cycle detection (file `cycle.pl`).

`po/2`, `co/2`, `rf/2`, `fr/2`, `barrier/2`. We extract `po` relation by reading the list of instructions of each thread and setting `po` for two consecutive memory operations in it. For example, the constraint `po(i(0,0,st,x,1),i(0,1,ld,y,R0))` will be generated to represent the program order of the two instructions  $i_{00}$  and  $i_{01}$  of thread 0 of  $p_0$  in Fig. 1a. We also define `ipo`, the transitive closure of `po`.

The relations `CO` and `RF` are generated by enumerating all possible solutions in a straightforward way. The `CO` relation is obtained after generating a permutation of all stores to each memory location (with an additional store at the beginning to write *undefined*), and setting the constraints `co(i1,i2)` for any two consecutive stores  $(\dots, i_1, i_2, \dots)$  in the permutation. The `RF` relation associates each load to a possible origin store. For the example of execution of Sec. 2, returning  $r_0 = 1$  and  $r_1 = 0$ , the constraints are `rf(i(1,0,st,y,1),i(0,1,ld,y,1))` and, as we add a store to *undefined* for initialization, `rf(i(-1,-1,st,x,undefined),i(1,1,ld,x,undefined))`. Notice that the read values (here, Prolog variables `R0,R1`) are unified with the written ones. The `-1` value of `n_thread`, `n_inst` indicates the initial definition of the program memory state.

The relation `FR` is computed by two rules: `rf(ST,LD), co(ST, ST2) ==> fr(LD,ST2)` and `fr(LD,ST), co(ST,ST2) ==> fr(LD,ST2)`. The first one means “if there is a `RF`-relation between `ST` and `LD`, and there is a `CO`-relation between `ST` and `ST2`, then add a `FR`-relation between `LD` and `ST2`”. The second adds the subsequent overwritings, if any.

Finally, we have some `CHR` rules that, taking the set of instruction constraints and the set of fence constraints, produce `barrier` constraints that force order on instructions. One example for  $p_1$  in Fig. 1a is `barrier(i(0,0,st,x,1),i(0,2,ld,y,R0))`.

### 3.3 Cycle Detection

Basically a memory model is defined by the relations between instructions that are allowed by the model. As these relations between two instructions express which one appears before the other, we can transitively produce all chains of dependencies. If a chain is a cycle, the execution exhibits an incoherence, since it means that an instruction happens before itself. The detection of a cycle is done by the `CHR` code of Fig. 2.

We use three `CHR` constraints. Constraint `rel(R,Begin,End)` states that instructions `Begin`, `End` are related by relation `R`. The transitive closure `trace(R,Begin,End)` means that `Begin`, `End` are transitively related by a trace, that is, a chain of relations `R`, while `cycle(R,Begin)` indicates that a cycle is found from `Begin` to itself.

The first rule (line 2) is a *simplagation* rule, written  $A \setminus B \Leftrightarrow C$ . The meaning is “if there exist two constraints `A` and `B`, add `C`, keep `A` and remove `B`”. So here, the goal is to remove duplicate traces with the same origin and end, as they will generate the same final traces.

The *simplification* rule at line 3 expresses that, if we have a trace from `Begin` to `End`, and we find a relation between `End` and `Begin`, we have to replace these two constraints by a new one that indicates the existence of a cycle starting from `Begin`.

```

1 :- include(generic_model).
2 :- include(cycle).
3 :- chr_constraint sc/2.
4
5 sc(I0,I1) ==> rel(sc, I0, I1).
6
7 sc(I0,I1), sc(I0,I1) <=> sc(I0,I1).
8 po(I0,I1) ==> sc(I0,I1).
9 co(I0,I1) ==> sc(I0,I1).
10 rf(I0,I1) ==> sc(I0,I1).
11 fr(I0,I1) ==> sc(I0,I1).

1 :- include(generic_model).
2 :- include(uniproc).
3 :- chr_constraint rfe/2 , ppo/2, tso/2.
4 % po-WR pairs are not preserved by TSO
5 ppo(i(_,_ ,st,_ ,_), i(_,_ ,ld,_ ,_)) <=> true.
6 ipo(I0,I1) ==> ppo(I0,I1).
7
8 ext(i(T0,_ ,_,_,_), i(T1,_ ,_,_,_)):- \+ T0 = T1.
9 rf(I0,I1) ==> ext(I0,I1) | rfe(I0, I1).
10
11 tso(I0,I1) ==> rel(tso, I0, I1).
12 barrier(I0,I1) ==> tso(I0,I1).
13 ppo(I0,I1) ==> tso(I0,I1).
14 rfe(I0,I1) ==> tso(I0,I1).
15 co(I0,I1) ==> tso(I0,I1).
16 fr(I0,I1) ==> tso(I0,I1).

```

Figure 3: Solver files for memory models (a) SC and (b) TSO

The third rule produces the transitive closure by adding longer traces whenever it finds a relation to continue an existing trace, unless it leads to a cycle since the cycle detection is fired by the previous rule. The order of rules is thus essential for performance. To optimize the search further and to limit the quantity of traces we work on, we consider an arbitrary total order `inf` on instructions, and we add an instruction to a growing trace only if it is strictly greater (w.r.t. `inf`) than the origin of the trace. Indeed, since we compute traces from every instruction at the same time, to detect any cycle it is sufficient to compute traces going only through instructions strictly greater than the trace origin (cf. Sec. 3.5). We ensure this behavior by the CHR syntax `R ==> Guard | N` which says “if we match `R`, add `N` only if `Guard` is true”.

The fourth rule selects every known relation between two instructions and adds it as a cycle candidate `trace` (using the same optimization by `inf` as above).

If we wish to keep only allowed executions, we can optimize the constraint filtering even further and add another rule `cycle(_ ,_) <=> false` that fails whenever a cycle is detected. Thus, inadmissible executions will be rejected as soon as detected.

### 3.4 Formalization of a Memory Model

To formalize a model we first identify the relations that it preserves and we create a new relation that we name according to the model acronym. Each occurrence of a preserved relation will create a new constraint with this name. The goal is then to produce the transitive closure and to launch the detection of cycles for this constraint.

For example, SC preserves the relations PO, CO, RF and FR and it does not care about barriers (since instructions are necessarily kept in order due to PO). We will name the new relation `sc`. Fig. 3a shows how we model it with CHR. Line 5 launches the computation of the transitive closure. Basically, every time we find a constraint `sc(A, B)` we add a new constraint `rel(sc, A, B)`. The cycle detection is provided by the inclusion of `cycle.pl`, line 2. Cycle rules and `rel` rule are added before any other rule about SC, to ensure the earliest detection of cycles. Lines 7–11 show how to state that `sc` preserves other relations. Every time such a relation is met, we add a new `sc`-relation.

Another interesting case is when the target model is more relaxed, that is, when the model preserves only some relations of the generic model. For example the TSO model will relax two kinds of relations: program order when the instructions are a store followed by a load, and read-from when the two instructions are in the same thread. The reordering propagates

transitively: multiple stores can be reordered after consecutive loads. If the developer wants to restore these relations, they will have to add fences. This model is illustrated in Fig. 3b.

We add a relation named `ppo` (“preserved-program-order”). Every relation `ipo` will generate a relation `ppo` except the ones mentioned before. So we add the rule on line 5, that replaces every constraint `ppo(store, load)` by “true”, which means that we just remove it, and a rule (line 6) that will generate `ppo` from `ipo`. We add another relation named `rfe` (“read-from-external”). The associated rule (lines 8-9) builds `rfe`-relations from `rf` by only adding those that concern instructions in different threads. Finally, we create the `tso` relations as for SC. Again, the order of rules here is essential for both soundness and performance (cf. Sec. 3.5).

Most weak memory models respect a coherency between communications (CO, RF, FR) and PO per location. In essence, it restores the uni-processor coherency (e.g. it forbids to read an old value from an overwritten location, that is allowed by the generic model, as mentioned in Sec. 3.1). It is formalized in the included `uniproc` file (not detailed here), which includes and relies on `cycle`, so we do not have to include it again.

The implementation of the PSO model is quite straightforward once TSO is implemented. It consists in weakening the preserved-program-order a bit more by removing all `ipo`-pairs starting with a store instead of only removing store-load pairs. Concretely, we replace the rule line 5 in the TSO model by the following one: `ppo(i(_,_,st,_,_),_) <=> true`.

**Applying the solver to programs.** The application of the solver for a given model to a program is performed automatically as illustrated in Fig 1b for program  $p_0$  described in Sec. 2. We include the target model, that already includes the generic model with all other necessary definitions. The program is loaded using two variables (variables involved in the program and lists of instructions of threads). Applying the target model solver to the program (line 13) will generate all candidate executions, and the CHR rules of the model will determine if each execution is allowed by the model or not.

In this case the SC model detects 3 admissible executions for both programs  $p_0$  and  $p_1$ . The TSO model allows 4 admissible executions for  $p_0$ , while for  $p_1$ , as we have fences, some relations will be restored and TSO will allow only 3 executions (exactly as SC). TSO allows more executions than SC on  $p_0$  since ST/LD pairs of instructions can be reordered (that can lead to the result  $r_0 = 0$  and  $r_1 = 0$ ). In  $p_1$ , we restore the sequentially consistent behavior of  $p_0$  by adding fences, preventing reordering even in the TSO model.

### 3.5 Discussion on Soundness and Performance

While using CHR, the order of rules can be essential for both soundness and performance. We emphasize two particular points regarding the order of rules in the proposed solver: cycle detection and computation of preserved-program-order relation `ppo`.

In cycle detection (cf. Fig. 2), we want to ensure that the solver does not miss any traces and avoids to consider equivalent traces when possible. First, as mentioned in Sec. 3.3, the rule at line 2 in Fig. 2 removes equivalent traces that have exactly the same origin and end points. As it is the first rule, we will not waste time by using the following rules for two equivalent traces since we will keep only one of them. Second, trace generation starts simultaneously from all known relations `rel(R, Begin, End)` where instruction `Begin` is less than `End`, while other instructions are added at the end of a trace only if they are greater than its origin (lines 4-5). So, every cycle has a minimal instruction from which we can find this cycle as a trace from an origin through greater instructions followed by a return to the origin, cf. line 3. (Notice that we still need to consider subtraces of the same cycle when they start from other nodes.) Third, the addition of an instruction to a trace (line 4) is done by adding a new constraint, without



removing the “old” ones that can still be necessary to generate other grown traces, so we do not miss paths.

When defining a relation such as preserved-program-order  $\text{ppo}$  (cf. Sec. 3.4), there are two ways to proceed: to define preserved relations or to define removed relations. The first way is always sound (as we only add information), while the second one requires more care. In particular, it is important to place the rule which removes relaxed relations before the rules that generate the constraints for cycle detection (see e.g. lines 5–6, 11, 13 in Fig. 3b). Otherwise, these rules would generate constraints for cycle detection before the relaxed relation is actually removed from the store and could thus forbid allowed executions.

**Experiments.** We tested our solver for different models against 18 examples<sup>2</sup> provided for the implementation of a dedicated tool Herd [3]. On these small (but representative) examples, our solver returns the same allowed executions as those found by Herd.

Execution time on these examples being too fast, we also compare performances of our solver with Herd on some examples involving a series of (possibly wrong) message passing. Experiments have been performed on an Intel Core i7-4800MQ, 4 cores, 2.7Ghz, 16Go RAM. For example, the following code involves three message passing:

```

1 mp3 (V, [T0, T1, T2]) :-
2   V = [ x, m ] ,
3   T0 = [ (st, x, 1), (st, m, 1), (ld, m, M0), (ld, x, X0) ],
4   T1 = [ (ld, m, M1), (ld, x, X1), (st, x, 2), (st, m, 2) ],
5   T2 = [ (ld, m, M2), (ld, x, X2), (st, x, 3), (st, m, 3) ].

```

In such an example, the typical question is: if we get  $M0 = 3$ ,  $M1 = 1$  and  $M2 = 2$ , do we get  $X0 = 3$ ,  $X1 = 1$  and  $X2 = 2$ ?

As it is composed of multiple writes and reads to the same locations, the combinatorial explosion is very fast. For each model, we indicate the number of allowed executions and the time needed to compute them with our CHR-based solver and with Herd. The timeout is fixed to 1 hour. The number of executions indicated for the generic model corresponds to the number of candidate executions. We present here the results for 3 and 4 message passings (denoted 3MP and 4MP).

In this benchmark, our solver is configured to immediately reject forbidden executions as soon as they are detected, while Herd does not perform such early rejections. When combinatorial explosion becomes really big, our solver computes allowed executions faster than Herd thanks to an early pruning of the search tree.

Model	Data	3MP	4MP
SC	#exec	678	81 882
	CHR	3.3s	747s
	Herd	5.5s	> 1h
TSO	#exec	800	96 498
	CHR	3.2s	752s
	Herd	4.1s	> 1h
PSO	#exec	2 258	516 030
	CHR	6.4s	2796s
	Herd	3.8s	> 1h
Generic	#exec	147 436	255 000 000
	CHR	3.3s	> 1h
	Herd	1.2s	1405s

## 4 Conclusion and Future Work

We have presented an original CHR-based solver for detection of admissible executions of a given program w.r.t. a given memory model, and illustrated it for SC, TSO and PSO models.

<sup>2</sup>Examples available at <http://virginia.cs.ucl.ac.uk/herd/> (record “armed cats”).



It is suitable for a rigorous exhaustive analysis of program executions of small programs that becomes intractable for bigger ones due to the combinatorial explosion of their number.

We think that seeing memory models as constraints over executions is well adapted. The design of such a solver is convenient and pragmatic. The generation of basic executions and cycle detection relies on a few optimizations in order to be more efficient and to ensure on-the-fly filtering of constraints. The proposed approach makes the definition of specific models from the generic one very practical and relatively straightforward. In particular, it is not very hard when the model becomes more complicated, as for models like ARM for example. CHR provides an easy way to express constraints about execution of programs, they have also been used for detection of incorrect behaviors in imperative program analysis in [7].

Moreover, the use of a well established mechanism of constraint specification and solving, here Prolog and CHR, brings the benefit of years of optimization and debugging to handle our problem without having to re-develop constraint resolution. We do not claim that our implementation of this problem is most efficient. Dedicated tools like [3] could be faster since they are specialized for this precise problem and can implement a solving engine without being as generic as CHR. But such dedicated tools are harder to develop as they potentially require a new optimized code that has to be carefully developed and debugged.

In future work, we plan to extend the solver to other models, like ARM. It would be interesting to support other kinds of instructions (e.g. binary operations) to handle all kinds of data or address dependencies often used for synchronization in ARM. Another direction would be to experiment on different programs of various sizes to produce precise benchmarks, in order to compare the solver to dedicated tools, as well as to further optimize it.

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