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Efficient controller synthesis of multi-energy systems for autonomous domestic water supply

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ABSTRACT. The continuous development of Information and Communication Technologies (ICT) facilitates the emergence and rapid proliferation of a wide variety of low-cost processors for the execution of programs in complex embedded applications. In this paper, the study explores the possibility to benefit from this wealth of computing capacity at a reasonable cost to solve concrete problems encountered in implementation of sustainable development processes, particularly in water and energy supply . . . In this work, we are focusing autonomous water supply in buildings of several floors using several tanks supplied by several sources of water and several pumping energy. The first problem to be solved is to propose pumping devices and a switching process between power sources, associated to an architectural structure guaranteeing significant reduction of pumping energy. The second problem is the system controller realization. It is question of achieving around a microprocessor, the central control body that ensures the coordination of the operation of discrete event system according to functional requirements of the system described by the user. For this, we have proposed a generic architecture justified by gains in potential energy. We also propose an automatic generation tool of control programs for different microprocessor targets taken from the functional design specification of the system given in a Grafcet form. To put them in evidence, the proposed case study is focused on a specific case of six floors building with several water resources, several energy sources, several pumping mechanisms and multilevel hierarchical priority access to water.

RÉSUMÉ. Le développement vertigineux des Technologies de l'Information et de la Communication (TIC) favorise l'émergence et la prolifération rapide d'une grande variété de processeurs à bas coût destinés à l'exécution de programmes embarqués dans des applications complexes. Dans ce papier, l'étude explore la possibilité de tirer profit de cette profusion de capacité de calcul à coût raisonnable pour résoudre des problèmes concrets que l'on rencontre dans la mise en place de processus de développement durable, notamment ceux qui concernent l'approvisionnement en eau et en énergie . . . Dans ce papier, nous visons l'étude d'approvisionnement en eau autonome dans des bâtiments à plusieurs étages en utilisant plusieurs citernes de stockage approvisionnées par plusieurs sources d'eau et d'énergie de pompage. Le premier problème à résoudre dans est de proposer des dispositifs de pompage et un processus de commutation entre les sources d'énergie, associé à une structure architecturale garantissant une réduction significative de l'énergie de pompage. Le second problème est la réalisation du contrôleur. Il s'agit de construire autour d'un microprocesseur l'organe central de

contrôle qui assure la coordination du fonctionnement d'un système à événements discrets suivant le cahier des charges spécifié par l'utilisateur. Pour cela, nous avons proposé une architecture générique justifiée par des gains d'énergie potentielle. Nous proposons aussi un outil de génération automatique de programmes de contrôle pour différentes cibles à microprocesseur à partir d'une spécification fonctionnelle sous la forme d'un Grafcet. Pour les mettre en évidence, le cas d'étude proposé est focalisé sur le cas spécifique d'un immeuble à six niveaux ayant plusieurs sources d'eau, plusieurs sources d'énergie, plusieurs mécanismes de pompage, ainsi que plusieurs niveaux hiérarchisés de priorité d'accès à l'eau.

KEYWORDS : ICT, sustainable development, water supplying, photovoltaic energy, Grafcet modeling, automatic synthesis, logic controller.

MOTS-CLÉS : TIC, développement durable, approvisionnement en eau, énergie photovoltaïque, modélisation Grafcet, synthèse automatique, contrôleur logique.

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1. Introduction

Information and Communication Technologies (ICT) have undergone enormous evolution in recent years. These changes have led to significant improvements in many application fields such as health care, education, commerce, . . . Automation is considered one of the most important sectors which has remarkably been developed thanks to the ICT revolution. For example, almost all digital devices, used to control automated electromechanical systems are nowadays based on sophisticated small microcontrollers instead of hard wired logic components (such as relays, cam timers, drum sequencers), that contribute explicitly to save time, energy, materials and money. Despite all these available advantages, sustainable development applications are slow to benefit from these to solve some implementation problems, such as energy and water distribution issues. For example, in 2013 Cameroon National Institute of Statistics (INS) declared that “almost 92% of households in Yaoundé suffer from intermittent water cuts.” Hence, “To reduce the shortages, households depend on the following sources: public water supply (55%), mineral water (10%), drilled wells (6%) and other undrinkable water sources (29%).” [6].

The use of multiple water supply sources is a feasible solution allowing to face the recurring interruptions of urban water supply services. There are, however, a number of problems: some sources (wells/drillings) require electrical energy to operate. This energy can itself even be available in several possibilities including classical urban energy distribution as well as local sustainable sources. However, whether water or energy sources, their costs differ from one another. A management strategy must therefore be implemented to select available sources that are least costly at each operating time.

The importance to invest on renewable energy sources (such as solar energy, wind energy, . . .) is highlighted to permanently improve the availability of water ([7, 10]). An optimization method is proposed in [11] to minimize energy consumption and to reduce leakage in a water distribution system (WDS) in a hydraulic context. However, the proposed algorithm cannot be applied in a context of household. A model of multi-criteria optimization for energy efficiency has been presented in [10]. But none of the existing methods presents the operational way of handling the issue of energy and water sources management.

The objective of this paper is to study energy control strategy for water supply problem in buildings having many floors. Precisely, it is to find solution that combines sustainable solutions and the advantages of ICT tools in order to realize a complete and autonomous system for water and power supply, with a particular emphasize on saving energy. This involves the establishment of appropriate pumping mechanisms and an efficient process of switching between energy sources. The smart system should guarantee the continuous providing of water to households, and automatically switch between several water and power resources according to the source availability and the service costs.

For ICT tools applied on the automation applications, International Electrotechnical Commission (IEC) has issued five standard programming languages defined in the IEC 6331-3 standard [9]. Among them, Grafset (or SFC) is a powerful graphical language useful for both specification and programming of industrial automation systems [5]. It is nowadays considered as one of the most used specification languages of IEC standard. Many research works have been carried out to promote and popularize this language, and many modeling and simulation tools as UniSim ([1, 8]), PLCopen XML [13], Isagraf,

... are based on Grafset standard. On the other hand, the Grafset language has actually been built and developed to be integrated in the design and implementation software for programmable logic controllers (PLC) devices ([1, 4, 12]).

PLC are digital devices basically used to control automated electro-mechanical systems. They are specially designed to survive in harsh industrial situations and could not be recommended for other simpler control applications. Hence, they are relatively expensive for developing countries and are not required to be operated in corresponding environments. Our investigations on Grafset synthesis have permitted to carry out a novel software tool that permits to automatically convert any Grafset specification code to a control program deployable on very economic microcontrollers. This tool is presented and can be exploited to generate the appropriate solution once the system is well specified in Grafset language.

The paper is organized as follows: Section 2 presents the problem to be solved with different configurations; the proposed model is explained in Section 3. Section 4 presents the study of the logic controller modelling using Grafset and a solution synthesis approach to obtain an automatic control system. Section 5 draws a case study with the corresponding Grafset model and conclusions are drawn in Section 6.

2. Problem statement

Consider a water providing system, associated to a building having m floors, n water supply sources, p energy sources used to pump water, and k tanks. Each floor of the building is supplied in water by a specific tank until the tank is empty. When the corresponding tank is empty, the connected floors are stocked by a global supply pipe connected to urban water distribution or to the highest tank of the plant.

2.1. Water storage of tanks

As shown in Figure 1, each tank is supplied with water by the descent of rainwater, by pumping water from the lower tank, or by opening water supplied by the urban network water distribution. Each tank supplies k floors of the building (for example $k = 3$). Each tank T_i is equipped with three water level sensors which indicate the empty tank (bT_i), the full tank (hT_i) and the average water level (mT_i). There are two ways of conveying water from sources to tanks: energy-free filling with rainwater and the pumping based filling. The urban water is also used to supply the floors when the first two sources are not supplied.

2.2. Energy-free filling

During the rains, the tanks are filled by rainwater harvested from the roofs.

Filling is done sequentially by going from the top tank to the lowest. In the case of low rainfall, the sequential of the tanks filling makes it possible to stock the water collected in priority in the tanks which have the highest potential energy. Especially, the filling of T_i is possible if the upper tank T_{i+1} is already full ($hT_{i+1} = 1$).

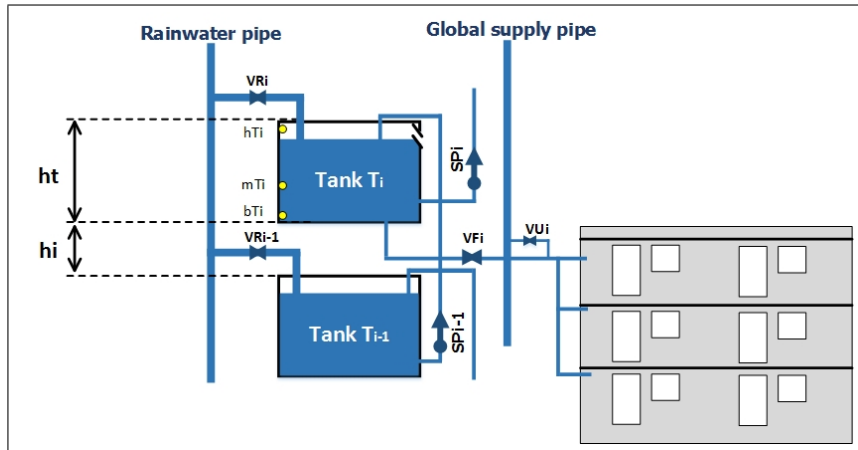


Figure 1. Schematic of an intermediary tank

The filling of the tank T_i consists in opening the valve VR_i when all the other valves VR_j ($j \neq i$) are closed. The filling ends when the tank T_i is filled ($hT_i = 1$), the valve VR_i is then closed and the filling of the tank T_{i-1} can begin.

2.3. Filling by pumping

In the absence of rain, the pumping allows to supply water to the tank T_i . It consists in activating the pump SP_{i-1} which transfers water from the tank T_{i-1} to the tank T_i . Depending on the form of energy used to supply the pump, we can distinguish 3 pumping modes :

– Pumping with the sun

In this pumping mode, water pumping from the tank T_{i-1} to the tank T_i is done without energy costs with solar water pumps that work with an electric motor whose power comes from photovoltaic cells located on solar panels that capture power from the sun's light.

In the presence of sufficient solar brightness ($srl = 1$), this zero energy cost pumping mode is systematically activated until the tank T_j is full ($hT_i = 1$) or the water level in tank T_{i-1} is under average level ($mT_{i-1} = 0$). This pumping mode is especially suited to rural environments in Africa. This is because sunlight is plentiful (with over six hours per day of maximum sunlight) and sufficient even for large quantity pumping, and the isolation of rural villages often makes it difficult to supply them with conventional energy supplies. Otherwise the need for water in rural village is generally low enough that it can be covered by solar pumping.

– Pumping with battery

During the night or when the solar radiation is insufficient, the pump SP_{i-1} is activated using batteries power supply when the level of water in the tank T_i is below the lower level ($bT_i = 0$). This pumping mode is activated until the tank T_i is full ($hT_i = 1$) or the water level in tank T_{i-1} is under average level ($mT_{i-1} = 0$).

Batteries accumulate excessive energy created by the photovoltaic (PV) panel system and store it to be used at night when there is no more solar energy input. Batteries can discharge rapidly and yield the current charging, ... For PV water pumping application, peep-cycle batteries are suitable to deliver few amperes required for pumping for hundreds of hours between charges. This type of battery is capable of many repeated deep cycles

and are best suited for PV power systems, compared to shallow-cycle batteries, as those used for starting a car that are designed to deliver several hundred amperes for a few seconds, then the alternator takes over and the battery is quickly recharged. These two types of batteries are designed for different applications and should not be interchanged. Ideally, a battery bank should be sized to be able to store power for 5 days of autonomy during cloudy weather. If the battery bank is smaller than 3 days pumping capacity, it is going to cycle deeply on a regular basis and the battery will have a shorter life. System size, individual needs and expectations will determine the best battery size for your system.

The energy cost of this pumping mode is almost zero because the cost is limited to the maintenance of the battery whose wear is induced by multiplicity of charge/discharge cycles.

– **Pumping with urban electricity**

During the nights when the batteries are faulty, power supply pumps is ensured by the urban electricity network. This method of pumping is costly since it is invoiced gradually and paid periodically to the urban electrification agency.

To reduce the energy cost, this mode of operation will be applied only if the corresponding tank is below the low level ($bT_i = 0$) and stops when the middle level is reached ($mT_i = 0$).

2.4. Purchasing to the urban distribution network

The urban network water distribution is realized by a public or private company. We assume that this network system guarantees to furnish sufficient pressure to propel water to the upper tank T_k without a need of any auxiliary pumping equipment. When a tank T_i is empty ($bT_i = 0$) and it is not possible to fill it with rainwater nor the water coming from the tank T_{i-1} , the floors of T_i are stocked by a global supply pipe connected to the urban water distribution or to the highest tank of the plant (as shown on Figure 3).

2.5. Input/Output configuration of an Intermediary tank

Considering the previous description, the input/output configuration of the controller of an intermediary tank T_i is described by the model presented in Figure 2.

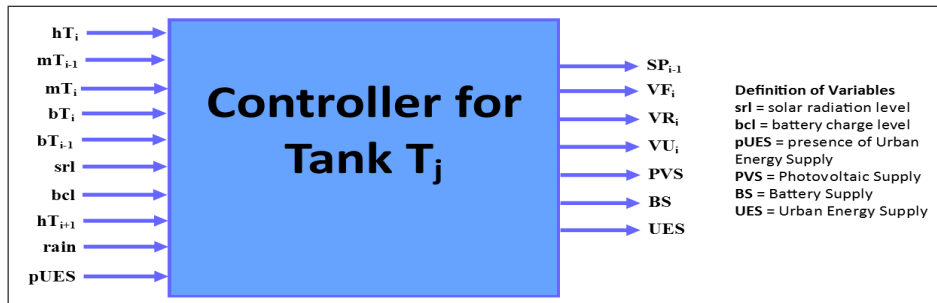


Figure 2. Input/output configuration of the controller of tank T_i

3. Proposed model

To solve that problem, there exists many possible architectural structures, presenting different gain of energy. They depend on many factors: the number of tanks k , the position of tanks with respect to floors, the pumping mechanisms, ... Whatever be the case, the final aim is to choose an architectural structure permitting to guarantee the supplying of every floor of the building with significant reduction of pumping energy.

3.1. Architectural structure

Generally, we may have any number k of tanks. In the case where there is only one tank ($k = 1$), that tank should supply water in all the floors of the building, which means that it would be situated above all the floors. It is then possible that the rainwater is not collected due to the position of that unique tank, which is relatively above the roof. However, if the rainwater is not used, this leads to the loss of a zero cost water source. The rainwater will be collected in a tank near the roof to allow the supply of any level of the building with zero energy.

When there are many tanks, every floor of the building could have its own tank. But if each of the m floors has its own tank, it necessitates m tanks. This is costly since the installation cost will be very huge unnecessarily. It is advantageous to group the floors in blocks to supply them with the same tank. Let η be the number of floors supplied by each tank (for example $\eta = 3$ on Figure 3). $k = \frac{m}{\eta}$ is the number of tanks to supply the m floors of the building. Hence, every tank T_i is preferably supplying the floors $\eta \times (i - 1)$, $\eta \times (i - 1) + 1$, $\eta \times (i - 1) + 2 \dots$, $\eta \times (i - 1) + \eta - 1 = \eta \times i - 1$. It avoids waste of energy, because the water present in that tank may be probably pumped since the tanks at the bottom.

It would be possible (when there is a need) to drive water from a tank to another. If the tank from which water is conveyed to the other one is above, none energy is necessary.

To summarize it, we present on Figure 3 a generic architecture having m floors supplied by k tanks with $k - 1$ surface pumps associated and one immersed pump. On that figure, there are $\forall i \in \{1, 2, 3, \dots, k\}$:

- VR_i is the valve opening rainwater from the rainwater pipe to the tank T_i .
- VF_i is the valve opening water from the tank T_i to the floors associated to it.
- VU_i is the valve opening water from the urban pipe to the floors associated to the tank T_i .
- SP_i is the surface pump pumping water from the tank T_i to the tank T_{i+1} ($i \leq k - 1$).

There is also the following valves:

- VR is the valve allowing to evacuate the surplus of rainwater when all the tanks are full.
- VU is the valve driving water from urban distribution network to the floors. It closes whenever the water level in all the k tanks is above the low level ($bT_i = 1$).

Some sensors are also used to read and send some information to the controller :

- The sensor *rain* indicates that it is raining. When it is raining, $r = 1$ and all pumping mechanisms stop, except for T_k .

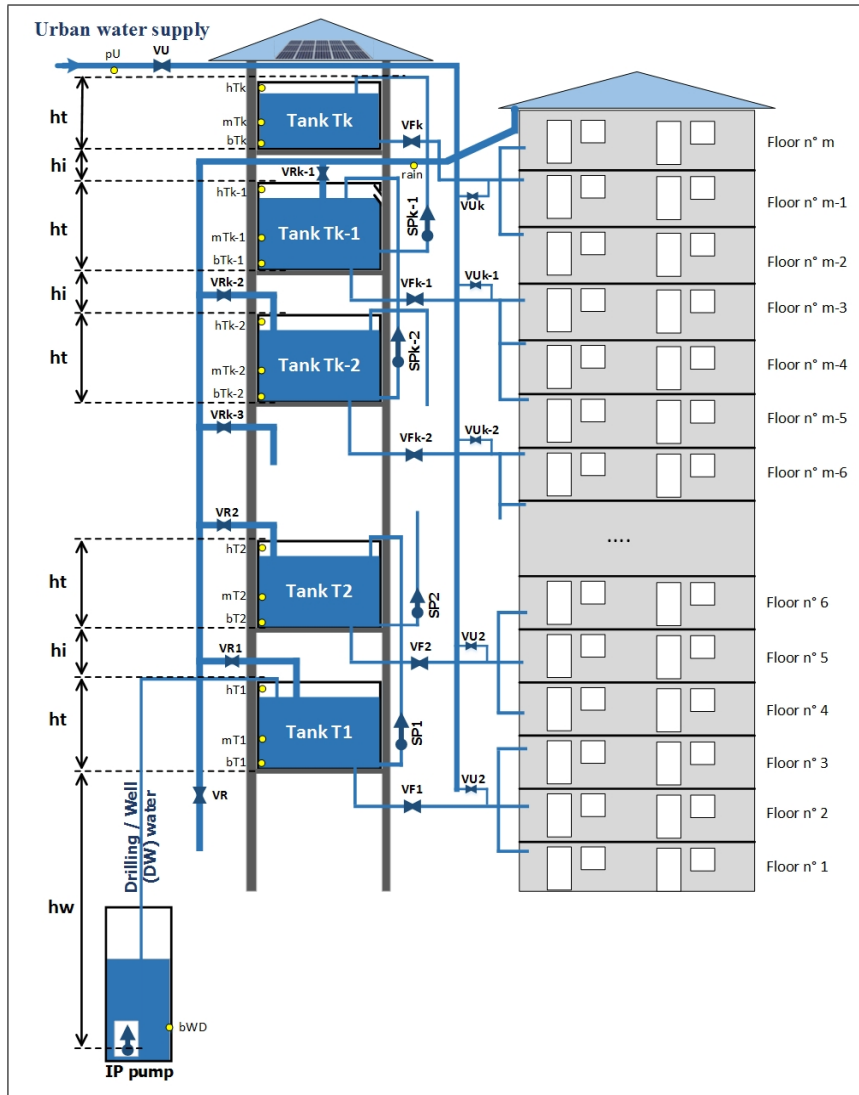


Figure 3. General physical architecture

– The sensor pU indicates that the urban water distribution network is supplied ($pU = 1$).

– The sensor bWD located inside the well/drilling tells the controller that there is water inside to be pumped by the immersed pump IP .

3.2. Tanks supplying and energy issues

Whether the pumping energy is zero cost or not, it is necessary and imperative to avoid any waste of energy. The tanks must then be placed and the pumps positioned in such a way that they can be operated by avoiding the losses of potential energy. Here, we evaluate this energy to justify the chosen pumping mechanisms.

Let $E_{i,j}$ be the amount of energy necessary to supply the tank T_j with the tank T_i , $i, j \in \{1, 2, \dots, k\}$ and $i \neq j$ with a water volume of $V(m^3)$. Considering that hi is the height between two successive tanks and ht is the height of each tank,

If $i > j$, water of volume V can be conveyed directly from the tank T_i to the tank T_j without been pumping. Then $E_{i,j} = 0$.

If $i < j$, to move the volume V of water from the tank T_i to the tank T_j directly, the height is $(j - i)(ht + hi) + ht$ and

$$E_{i,j}(1) = \rho g V [(j - i)(ht + hi) + ht] \Rightarrow \frac{E_{i,j}(1)}{\rho g V} = (j - i)(ht + hi) + ht$$

Where $\rho(Kg/m^3)$ is the density of water, and $g(N/Kg)$ is the gravity of Earth.

When $i < j$, if the same volume V of water is moved from T_i to T_j passing through the tanks $T_{i+1}, T_{i+2}, \dots, T_{j-1}$, then $E_{i,j}(2) = E_{i,i+1} + E_{i+1,i+2} + \dots + E_{j-1,j} = \sum_{l=i}^{j-1} E_{l,l+1}$. $E_{l,l+1} = \rho g V (2ht + hi)$, which is constant. Then

$$E_{i,j}(2) = \sum_{l=i}^{j-1} \rho g V (2ht + hi) = \rho g V (j - i)(2ht + hi) \Rightarrow \frac{E_{i,j}(2)}{\rho g V} = (j - i)(2ht + hi)$$

The $\rho g V (j - i)ht$ energy surplus is due to the fact that the water first enters the intermediate tanks being sent higher. The difference between those two amounts of energy is given by

$$E_{i,j}(2) - E_{i,j}(1) = \rho g V [(j - i)(2ht + hi) - (j - i)(ht + hi) - ht] = \rho g V (j - i - 1)ht$$

In summary, when $i < j$, since $\rho g V (j - i - 1)ht \geq 0$, $E_{i,j}(2) - E_{i,j}(1) \geq 0$. It is then better to move water directly from the tank T_i to the tank T_j without passing through the intermediate tanks. But this advantage is apparent because the realization of such an architecture is very difficult due to the following reasons:

– **Costly and cumbersome:** this requires an amount of $(j - i)$ different water lines equipped with pumps, from the tank T_i to the tanks $T_{i+1}, \dots, T_{j-1}, T_j$. For all the building, it requires a total of $1 + 2 + \dots + (k - 1) = \frac{(k-1)k}{2}$ lines. All this is cumbersome and too expensive.

– **Unknowning of the floor where the water will be used:** the volume V of water may be used elsewhere in building floors, except those supplied by the tank T_j .

Water should then be pumped steps by steps from tanks T_i to tanks T_{i+1} , $i = 1, 2, \dots$

3.3. Number of tanks and energy issues

If there is only one tank, it implies a too wasting of pumping energy, which may not be available. The main reason is that the rainwater may not used. In fact, it is difficult to place the highest tank in order to collect rainwater and supply the highest floors.

Let's show that it is better to use many tanks and pump water from tanks to tanks, from the drilling/wells to a specific floor, instead of pumping it up to the highest tank before redistributing it to floors.

We consider two cases: there are two tanks (Case 1) and there is only one tank (Case 2). The following is the calculation of the amount of energy required to pump a volume $V(m^3)$ of water from wells/drilling to the lower floors. We consider that $V = V_1 + V_2$,

where V_1 is the volume of water used to supply the lower floors and V_2 the volume used to supply the upper floors.

Case 1 : In presence of two tanks, water is pumped from the well/drilling to the lower tank T_1 (supplying the lower floors with V_1) and from T_1 to the upper tank T_2 (supplying the upper floors with V_2):

$$E_1 = \rho g[(hw + ht)(V_1 + V_2) + (2ht + hi)V_2] \Rightarrow \frac{E_1}{\rho g} = (hw + ht)(V_1 + V_2) + (2ht + hi)V_2$$

Where hw is the height between the well/drilling and the tank T_1 .

Case 2: Water is pumped directly from the well/drilling to the upper tank T_2 , from which all the building is supplied:

$$E_2 = \rho g[(hw + 2ht + hi)(V_1 + V_2)] \Rightarrow \frac{E_2}{\rho g} = (hw + ht)(V_1 + V_2) + (ht + hi)(V_1 + V_2)$$

The difference of energy $E_2 - E_1$ is such that:

$$\frac{E_2 - E_1}{\rho g} = (hw + hi)V_1 - ht \times V_2 = hi \times V_1 + ht(V_1 - V_2)$$

In practice, ht is very less than hi . It may be possible to have $hi = 6 \times ht$.

$$\text{If } V_1 = V_2 = \frac{V}{2} \text{ then } \frac{E_2 - E_1}{\rho g} = hi \times \frac{V}{2}$$

This energy gain is obtained without considering the fact that rainwater is not collected and used. When rainwater is not used, it involves an enormous loss of energy.

Generalization with k tanks

The previous calculations takes into consideration only two tanks. Let's generalize it with k tanks. For this, we consider the general architecture of Figure 3, and $V = V_1 + \dots + V_k$, $V_i \geq 0, \forall i \in \{1, 2, \dots, k\}$. V_i is used by the tank T_i to supply the floors numbered $\eta \times i - j, j \in \{0, 1, \dots, \eta - 1\}$, where η is the number of floors supplied by every tank T_i .

E_1 is the amount of energy necessary to pump water from tanks to tanks, pumping only the necessary water volume ($V_{i+1} + \dots + V_k$) from T_i to T_{i+1} , steps by steps. Hence we have :

$$E_1 = \rho g \left(\sum_{i=1}^k V_i (hw + ht) + \rho g \left(\sum_{i=2}^k V_i (hi + 2ht) + \rho g \left(\sum_{i=3}^k V_i (hi + 2ht) + \dots + \rho g (V_{k-1} + V_k) (hi + 2ht) + \rho g V_k (hi + 2ht) \right) \right) \right)$$

$$\frac{E_1}{\rho g} = (hw + ht) \sum_{i=1}^k V_i + (hi + 2ht) \sum_{i=2}^k V_i + (hi + 2ht) \sum_{i=3}^k V_i + \dots + (hi + 2ht)(V_{k-1} + V_k) + (hi + 2ht)V_k \Rightarrow \frac{E_1}{\rho g} = (hw + ht) \sum_{i=1}^k V_i + (hi + 2ht)(0V_1 + 1V_2 + \dots + (k-1)V_k)$$

Then,

$$\frac{E_1}{\rho g} = (hw + ht) \sum_{i=1}^k V_i + (hi + 2ht) \sum_{i=1}^k (i-1)V_i$$

Concerning E_2 , water is pumped from the well/drilling to the tank T_k , before providing the other tanks (T_{k-1}, \dots, T_1). Hence,

$$E_2 = \rho g \sum_{i=1}^k V_i [hw + ht + (k-1)(hi + ht)] = \rho g (hw + ht) \sum_{i=1}^k V_i + \rho g [(k-1)(hi + ht)] \sum_{i=1}^k V_i$$

$$\frac{E_2}{\rho g} = (hw + ht) \sum_{i=1}^k V_i + (k-1)(hi + ht) \sum_{i=1}^k V_i$$

The difference of energy $E_2 - E_1$ is then given by:

$$\frac{E_2 - E_1}{\rho g} = (k-1)(hi + ht) \sum_{i=1}^k V_i - (hi + 2ht) \sum_{i=1}^k (i-1)V_i$$

By reorganizing it into factors of hi and ht , we have

$$\frac{E_2 - E_1}{\rho g} = hi \left[(k-1) \sum_{i=1}^k V_i - \sum_{i=1}^k (i-1)V_i \right] + ht \left[(k-1) \sum_{i=1}^k V_i - 2 \sum_{i=1}^k (i-1)V_i \right]$$

Hence,

$$\frac{E_2 - E_1}{\rho g} = hi \sum_{i=1}^k (k-i)V_i + ht \sum_{i=1}^k (k-2i+1)V_i$$

Sign of $E_2 - E_1$, considering that $k > 1$

$\sum_{i=1}^k (k-i)V_i > 0$ and $\sum_{i=1}^k (k-2i+1)V_i$ may be negative. But, because in reality $ht < hi$ (possibly $ht = \frac{hi}{6}$), $\left| \sum_{i=1}^k (k-i)V_i \right| > \left| \sum_{i=1}^k (k-2i+1)V_i \right|$ and then $E_2 - E_1 > 0$.

If $V_1 = V_2 = \dots = V_k = \frac{V}{k} = V_0$, we have

$$\frac{E_2 - E_1}{\rho g V_0} = hi \sum_{i=1}^k (k-i) + ht \sum_{i=1}^k (k-2i+1)$$

But, $\sum_{i=1}^k (k-i) = \frac{k(k-1)}{2}$ and $\sum_{i=1}^k (k-2i+1) = 0$, then $\frac{E_2 - E_1}{\rho g} = \frac{k(k-1)}{2} hi \times \frac{V}{k}$.

In other words, $E_2 - E_1 = \frac{k(k-1)}{2} \rho \times g \times hi \times V$.

In summary, the use of a single tank leads to neglect rainwater and a waste of pumping energy. It is necessary to use at least $k = 2$ tanks. To gain energy, water must be pumped from the well/drilling to the lowest tank T_1 using an immersed pump, from any tank T_i to T_{i+1} ($1 \leq i \leq k-1$) using surface pumps. Also, The rainwater must be collected first in T_k then in $T_{k-1}, T_{k-2} \dots$ to gain in potential energy. This water is not lowered before it is brought up again, by losing energy.

4. Logic Control using Grafcet

From the physical layout architectural water supply system (as shown in Figure 3), we can describe several functional requirements of systems considered in particular contexts. In addition to the case of the whole system, some interesting systems may be obtained considering the fact that there is the absence of one of the following functions: urban electricity supply, drilling/well, urban water supply or battery. In this section, our attention is focused on the whole system from which the solution to other systems cases can be obtained. Initially, let's look at an overview of the Grafcet modeling language. Next, we will propose pieces of grafcet to model the basic functionalities of this system and finish it with the presentation of the synthesis solution strategy.

4.1. The Grafcet modeling language

The Grafcet (Graphe Fonctionnel de Commandes et d'Étapes/Transition), a graphic language for modeling automated systems, is the most international formalism used for high-level description of complex sequential systems [5]. It is widely used in several domains such as home automation, automotive, power generation, manufacturing, etc. A grafcet specifies the behavior of a logic control system. This language has been standardized by the International Electrotechnical Commission IEC 60848 [3], and is understandable and readable compared to other specification languages as Petri net, Relay ladder, Instruction list, etc.

A grafcet (program written in Grafcet language) is a graph that consists of two types of nodes: steps and transitions. A step is represented by a square, while a transition is represented by a horizontal line. The initial steps have a double square. Directed edges are necessarily used to connect steps to transitions or transitions to steps. Each step may be associated with several actions which represent the outputs of a Grafcet graph. An action is symbolized by a rectangle which is connected to a step. The same action can be connected to many steps and it becomes true if at least one of those steps is active. Some elements are used to separate structurally steps and transitions: when there are many steps in the upstream of a transition, a "junction AND" represented with a double-line is put between those steps and this transition. A "distribution AND", represented with a double-line, is used to separate a transition with many steps when this transition has many steps in the downstream. When there are many transitions in the upstream of a step, a "junction OR" represented with a simple horizontal line is used. A "distribution OR" also represented with a simple horizontal line is used to separate a step to many transitions that are in the downstream of this step.

The Grafcet evolution from the initial state is done by firing transitions according to the following five evolution rules [3]:

- **Rule 1:** At the initial time, all the initial steps are active; all the other steps are inactive.
- **Rule 2:** A transition is enabled when all the steps that immediately precede this transition are active. A transition is fireable when it is enabled and when the associated transition condition is true. A fireable transition must be immediately fired.
- **Rule 3:** Firing a transition provokes simultaneously the activation of all the immediately succeeding steps and the deactivation of all the immediately preceding steps.
- **Rule 4:** When several transitions are simultaneously fireable, they are simultaneously fired.
- **Rule 5:** When a step shall be both activated and deactivated, by applying the previous evolution rules, it is activated if it was inactive, or remains active if it was previously active.

These rules enable the calculation of the subsequent state and the corresponding output signals caused by an input event.

4.2. Grafcet specification model for the system

Here, we propose some general Grafcet models for the specification of processes under control of the logic controller whose the general architecture is presented in Figure 3. In

Figure 2, there is the I/O specification of intermediary tanks controller. This is a part of entire controller which should control the modeling of water providing of tanks & floors according to multilevel hierarchical priority access to water, and the switching process between water & energy sources.

4.2.1. Grafcet modeling water providing of tanks

According to the description of the tanks supplying given in subsections 2.2 & 2.3, there are three cases of tanks:

- The lower tank T_1 : water is pumped with the immersed pump IP .
- The highest tank T_k : water is pumped with a surface pump SP_{k-1} .
- The other T_i ($2 \leq i \leq k$) tanks: water is pumped with the same condition as T_k , and the filling of T_i with rainwater is conditioned by the fact that T_{i+1} is already full ($hT_{i+1} = 1$).

The water providing of tanks is well specified during the modeling of the switching process presented in 4.2.3. This process can be specified with the Grafcet model of Figure 4. Variables $ppM1$ and $ppM2$ indicate the presence of pumping energy. $ppM1 = srl + \overline{srl} * bcl$ concerns the first mode inherent to pumping with zero energy cost (with sun or with storage batteries) and the variable $ppM2 = \overline{srl} + bcl * pUES$ is related to pumping with energy cost, where $pUES$ informs on the presence of urban electricity.

Figure 4.b presents the providing of any tank T_i : When T_i lacks water ($mT_i = 0$) and if there is rainwater ($rain = 1$), the valve VR_{i+1} is opened and T_i is provided until it is full ($hT_i = 1$). If there is not rainwater ($rain = 0$), the second alternative is used when T_{i-1} is provided ($mT_{i-1} = 1$) and there is power to supply the surface pump SP_i . The action SP_{i-1} is put on to pump water from T_{i-1} to T_i .

It is the same with T_1 (Figure 4.a) except that water is pumped from IP pump. Also, bWD indicating the level of water in the drilling/wells. For T_k , when it is raining, the opening of VR_k is not subject to the conditions hT_{k+1} (the tank T_{k+1} does not exist), but only to the condition $rain * !mT_k$ (Figure 4.c).

To manage the fact that when it is raining, tanks are filled from the highest to the lowest, we consider that T_k is filled with rainwater with the condition $!mT_k * rain$ (receptivity of the transition going from the step 9 to the step 10); and $\forall T_i, i \in \{1, \dots, k-1\}$ the condition to fill T_i with rainwater is $!mT_i * mT_{i+1} * rain$ (receptivity of the transition from the step 5 to the step 6), so T_{i+1} must be fulfilled first ($hT_{i+1} = 1$).

In addition, the action VR allows the evacuation of the surplus of rainwater when all the tanks are full ($hT_1 * hT_2 * \dots * hT_k = 1$). It stops when there exists a tank T_j whose water level is below the medium level ($mT_j = 0$). In this case, the filling process of T_j starts automatically. To avoid damages between the time all tanks are full and when at least one tank has a water level below the medium, exhaust outlets may be put on each tank. The process of opening and closing VR is specified with the Grafcet model of Figure 5.

4.2.2. Grafcet modeling water providing of floors

Every floor is attached to a tank T_i from which it is provided.

The valve VF_i should remain opened while there is water inside T_i ($bT_i = 1$). VF_i is closed as soon as the tank is empty ($bT_i = 0$), in which case the urban distribution

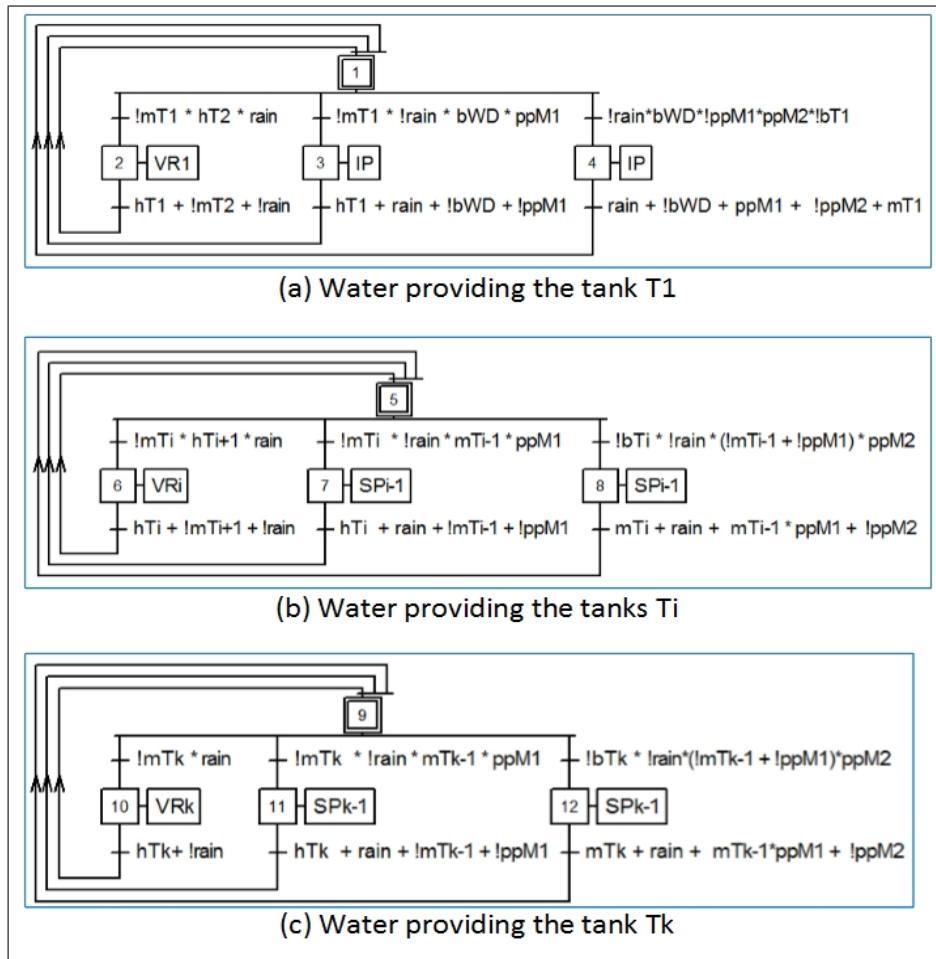


Figure 4. Grafcet specification of water providing tanks

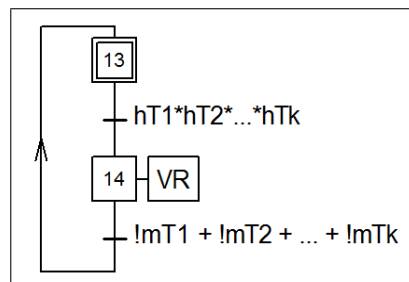


Figure 5. Grafcet specification of opening/closing the exhaust valve VR .

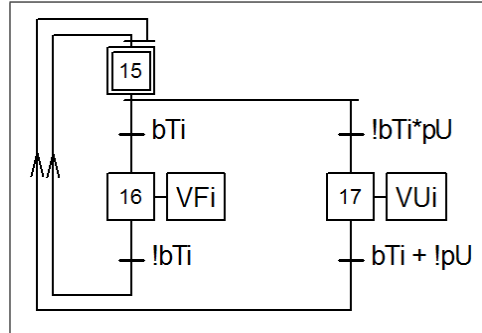


Figure 6. Gafcet specification of water providing floors network takes over with the valve VU_i when it is supplied ($pU = 1$). VU_i is also closed as soon as T_i becomes supplied again ($bT_i = 1$) or the urban network becomes unavailable ($pU = 0$).

The conditions bT_i , $!bT_i$, $!bT_i * pU$ and $bT_i + !pU$ present in the Grafcet specification model of Figure 6 are then justified.

4.2.3. Grafcet modeling switching process between energy sources

When modeling water providing of tanks (4.2.1) and water providing floors (4.2.2), the switching process between water sources is handled by activating/deactivating the gates control. Because every pump can function with many energy sources, the switching process between energy sources issue should also be solved. For that, it is necessary to use another electronic component electrically controllable, as multiplexers for example.

With p sources of energy, we rank them from the cheapest to the most expensive: E_1, E_2, \dots, E_p . We associate a variable pE_j (presence of energy to the source E_j) to every power source E_j . $pE_j = 1$ when the source E_j has energy ($j = 1, 2, \dots, p$).

A mechanism implemented by a multiplexer is then putted in place. It permits to select between the available sources of the p sources a particular source E_j having the lowest cost, to be connected on the multiplexer output E_{out} .

Let $\lambda = \lceil \log_2 p \rceil$, such that $p < 2^\lambda$ (there should be one empty energy in input). We define the variables $MX_1, \dots, MX_{\lambda-1}$ used in input of a multiplexer MX for the selection between the sources E_1, E_2, \dots, E_p , as presented on Figure 7.

To select a particular source E_j (i.e. to connect E_j to E_{out}), $\forall j \in \{1, 2, \dots, p\}$ we can have $j = (j_\lambda, j_{\lambda-1}, \dots, j_1) = (MX_\lambda, \dots, MX_1)$, where $(j_\lambda, j_{\lambda-1}, \dots, j_1)$ is the binary representation of j . We then define the actions MX_{j_z} ($z \in \{1, 2, \dots, \lambda\}$), which are activated when $j_z = 1$ in that representation of j . Table 1 presents the truth table of that mechanism.

Addresses: $j = j_\lambda j_{\lambda-1} \dots j_2 j_1$					$E_{out} = E_j$
MX_λ	$MX_{\lambda-1}$...	MX_2	MX_1	Output
0	0	...	0	0	None
0	0	...	0	1	E_1
...
1	1	...	1	1	E_p

Table 1. Truth table of MX_1 and MX_2 multiplexers

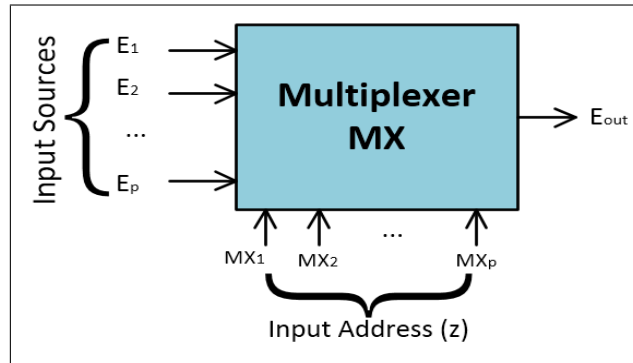


Figure 7. Multiplexer MX for power sources switching

As long as there is at least one available source, E_{out} remains supplied until none source has power. Also, when E_{out} is not supplied, it becomes supplied as soon as one source of energy becomes available. The energy is provided independently of the fact that E_{out} is used by a pump or not. It can be specified by the grafcet of Figure 8.

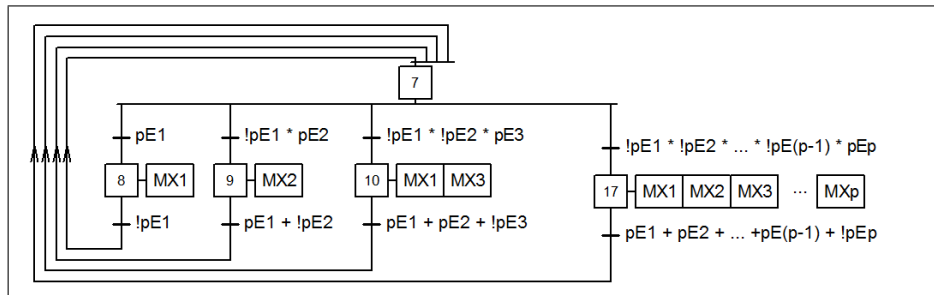


Figure 8. Grafcet specification of the switching process between power sources providing a pump

In the specific context of water providing of households, the sensors pE_j correspond to the signals $srl, bcl, pUES, \dots$ whereas the sources E_j are PVS, BS, UES, \dots with $j \in \{1, 2, \dots, p\}$. Here, we consider that all the pumps (surface & immersed) are supplied with the same sources of energy. In contrary, it is possible to have many types of pumping sources (24vols, 220vols, \dots). Sources can then be reorganized in groups and this switching mechanism can easily be applied to each group.

4.3. Synthesis solution strategy

Given the technical design specifications of the water supply system, the grafcet specification model is derived from. We present in this subsection the synthesis process for logical control systems specified in Grafcet. A grafcet model can be realized on programmable controllers (such as microcontrollers or PLCs). However, they do not allow a direct implementation on control targets like microcontrollers, which cost comparatively less than PLCs. For this, we have conducted research on the automatic and robust synthesis of logic controllers specified in Grafcet language and realized on microcontroller targets.

A program synthesis tool is then designed for microcontrollers, according to the Grafcet algebraic equations approach broadly presented in sub-section 4.4.

Referring to Figure 9, the synthesis process can be split into multiple steps which are broadly described as follows:

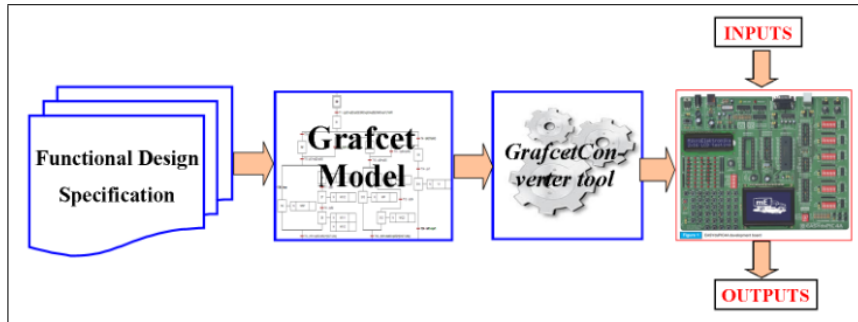


Figure 9. Synthetic approach solution

– **Step 1. Functional Design Specification (FDS) of the system :**

The design and development of any system starts with the description of requirements. An FDS is the most important step in the design of any control system. It provides details of the proposed solution to be implemented, to meet user requirements. Thus, FDS is the documentation that defines what the system should do and what functions and facilities should be provided by this system in order to satisfy the requirements. After the FDS specifying all the functions (e.g. pumping, switching, measuring ...), the objects (sensors, pumps, switches ...) and sequential interactions which are associated with the system, the controller is broadly specified with an *Inputs/Outputs* system presenting all the signals in input and all actions in output.

– **Step 2. Grafcet model :**

The next step is to represent the technical specification of the system by Grafcet model. We propose UniSim software tool in order to edit Grafcet chart [8]. It is a graphical user interface (GUI) that offers gallery of specific graphical objects (shapes) for all Grafcet elements (such as steps, transitions, transition-conditions and actions). The user can easily select these graphical objects, place them onto a drawing page and attach them together in order to create specific grafcet charts. Furthermore, UniSim tool permits to reformat or serialize Grafcet data into XML format [13], this option ensures that this information can be easily processed by another software application (interoperability property), especially the one that we have realized.

– **Step 3. GrafcetConverter tool :**

We have built this software tool in order to directly read and extract the Grafcet data from XML format file and generate the appropriate program according to the Grafcet algebraic equations approach presented in subsection 4.4. This program in C language is ready to be compile by the appropriate compiler to build the corresponding binary program. Furthermore, *GrafcetConverter* tool provides a simulation engine with which we can simulate the Grafcet program and verify whether it meets the requirements or not before generating the C-program for the selected microcontroller. This tool can generate code for microcontrollers, especially the EASYdsPIC4 of the Microship dsPIC family [14].

– **Step 4. Integrated Circuit :**

We are using the EASYdsPIC4A microcontroller, a full-feature and very powerful development system for PIC microcontrollers from Microchip [14] that holds a dsPIC30F4013 microprocessor. In C language, we have implemented the Grafcet interpretation algorithm [5] using the MPLAB IDE. The board is programmed by generating and transferring a binary program to the EEPROM board through USB cable or RS-232 COM port. When the code is uploaded in the board and the board reinitialized, the board runs and serves as the sit control of the system.

4.4. Grafcet implementation with algebraic equations

In the program outputted by the synthesis tool, to make sure that the evolution of the Grafcet situation is done according to the Grafcet evolution rules, we automatically generate Grafcet algebraic equations as stated by J. Machado et al in [2]. They use algebraic equations as a common model for simulation and formal verification to obtain a safe controller specification that will be implemented on PLC.

This control program runs according to a scan-based perception which is an effect of the PLC cyclic mode of operation. Figure 10 presents the scan-based cycle processed in every step of the microcontroller (μC) during its sequential execution.

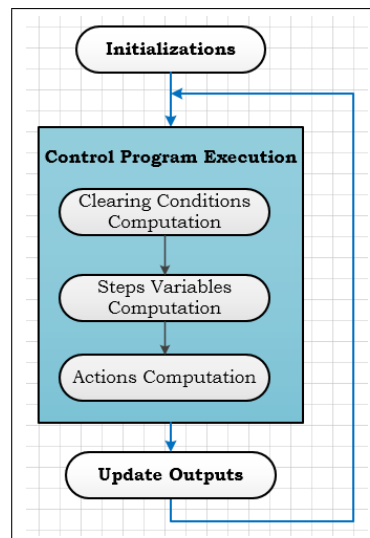


Figure 10. $\mu C/PLC$ Scan cycle

The Grafcet algebraic equations generated when producing a control program are defined as follows:

Let $CC(tr)$ (Clearing Condition) be a Boolean variable associated to every transition tr of a Grafcet. A transition tr can be cleared if it is enabled and if its associated transition condition $TC(tr)$ is true. $CC(tr)$ is formulated as follows:

$$CC(tr) = \left(\prod_{j=1}^m X_j^{tr} \right) \times TC(tr)$$

where :

- X_j^{tr} is the step activity Boolean variable associated to step j and directly preceding transition tr ,
- $TC(tr)$ is the transition condition associated to transition tr and
- m is the number of steps immediately preceding the transition tr .

Any Boolean step activity associated to each Grafset step is computed as follows:

$$X_i(0) = \begin{cases} 1 & \text{if } X_i \text{ is an initial step} \\ 0 & \text{else} \end{cases}$$

$$X_i(t+1) = \sum_{j=1}^p CC(tr_j^{i-}) + X_i(t) \times \prod_{j=1}^q \overline{CC(tr_j^{i+})}$$

where :

- $X_i(t)$ is the step activity variable of step i in the t^{th} scan cycle,
- $X_i(t+1)$ is the step activity variable of step i in the $(t+1)^{th}$ scan cycle,
- p is the number of transitions directly preceding the step i ,
- q is the number of transitions directly succeeding the step i ,
- $CC(tr_j^{i-})$ is the clearing condition of transition j , directly preceding the step i and
- $CC(tr_j^{i+})$ is the clearing condition of transition j , directly succeeding the step i .

For actions computation, a Boolean variable A is associated to each action \mathcal{A} . An action \mathcal{A} may be associated to several steps and its value $A(t)$ is obtained by computing the $OR(+)$ operation of the step activity variables $X_i^{\mathcal{A}}$, $i = 1, 2, \dots, h$ of h steps to which this action is associated. Hence,

$$A(t) = \sum_{i=1}^h X_i^{\mathcal{A}}(t)$$

Where $X_i^{\mathcal{A}}(t)$ is the activity variable of a step to which the action \mathcal{A} is associated.

5. Case study

In this section, we present a case study, describing the physical layout architecture of a water & energy supply system and its synthetic scheme.

5.1. System Features

Figure 11 illustrates the water distribution system for a six-floor building, consisting of: several water sources ($n = 3$), several sources of pumping energy ($p = 5$), several

water access valves with different priority levels, control system, in addition to two ($k = 2$) water tanks (T_1 and T_2).

As described in the general case (sub-section 3.1), we consider:

Three water sources:

- Urban network water distribution,
- Well/Drilling Water and
- Reserve of rainwater.

Five sources of pumping energy:

- Source E_1 or PVS : is 24 volts solar panel. Its presence is indicated by the electrical power sensor srl .
- Source E_2 or BS : is 24 volts battery, can be charged with solar power. The electrical power sensor bcl indicates its presence.
- Source E_3 : is 220 volts AC to 24 volts DC transformer, from Source **E5**. The electrical power sensor $pUES$ indicates its presence.
- Source E_4 : is inverter generator, provides 220 volts. Its presence is known thanks to the electrical power sensor bcl .
- Source E_5 or UES : is public electricity network, provides 220 volts. Its presence is known thanks to the electrical power sensor $pUES$.

Pumping mechanisms

– **The surface pump** SP is setup for 24 volts DC; the power supply is provided either by direct solar panels **E1**, or by solar charged battery **E2** or by transformer **E3**. SP permits to pump the water from T_1 up to T_2 .

– **Immersed pump** IP is setup for 220 volts; the power supply is provided either by the inverter **E4** or by the urban network **E5**. IP permits to pump the well water up to T_2 .

Water access valves: $VU, VR, VR_1, VF_1, VF_2, VU_1$ and VT_2 .

This architecture of this case study works according to the detailed description presented in Section 2 where there are water storage of tanks (2.1), the ways of conveying water from sources to tanks: energy-free filling with rainwater (2.2), the pumping based filling (2.3) and pumping purchased to the urban distribution network (2.4). The switching process between power sources and valves is then presented.

Multiplexers are used as presented in 4.2.3 for the switching process between sources of pumping energy. The **surface pump** SP is supplied either by $E1, E2$ or $E3$. The selection of the desired source among them can then occur by means of a multiplexer switch MX_1 . The **immersed pump** IP is supplied either by $E4$ or $E5$. Hence, the selection of the desired source can occur by means of a multiplexer switch MX_2 .

5.2. The logic control system

The water distribution system is completely controlled by a smart control system (controller). It has its proper power supply that makes it autonomous.

The input points of the controller are connected to sensors, which permit to report events and transmit this information as signals to the controller. The 13 digital input sensors used in our system are summarized as follows:

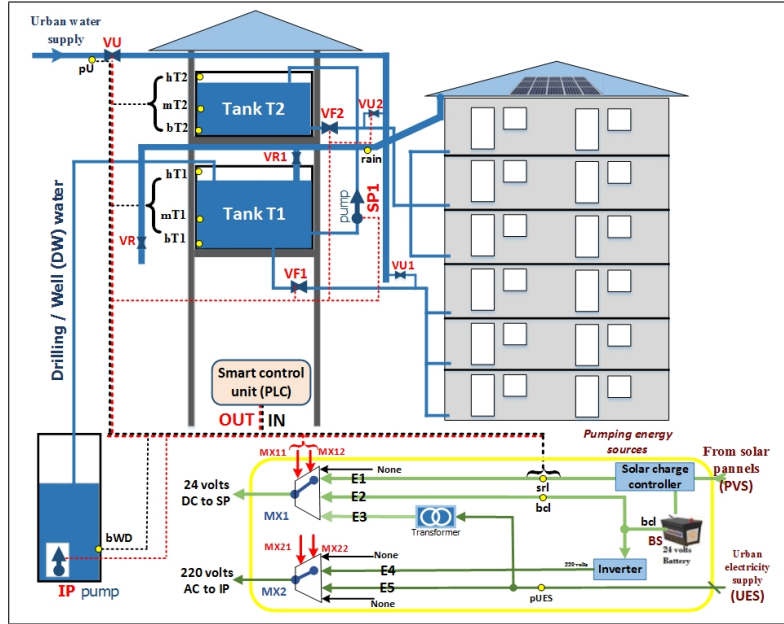


Figure 11. Synthetic diagram of the system

- Water level sensors : $bT_1, mT_1, hT_1, bT_2, mT_2, hT_2, bWD$.
- Pressure sensors : $pU, rain$.
- Electrical power sensors: srl, bcl and $pUES$ ($pE_1 = srl, pE_2 = bcl, pE_4 = bcl, pE_5 = pUES$).

The controller will then read, analyze the input signals and activate actions to be activated, according to the $\mu C/PLC$ scan-base cycle of Figure 10. These generated actions are interpreted as output signals transmitted to output devices (such as actuators and relays) to control the water circulation system. The 13 digital output devices used in our system are :

- Inductors : IP, SP .
- Relays : $VR, VR_1, VF_1, VF_2, VU, VU_1, VU_2$.

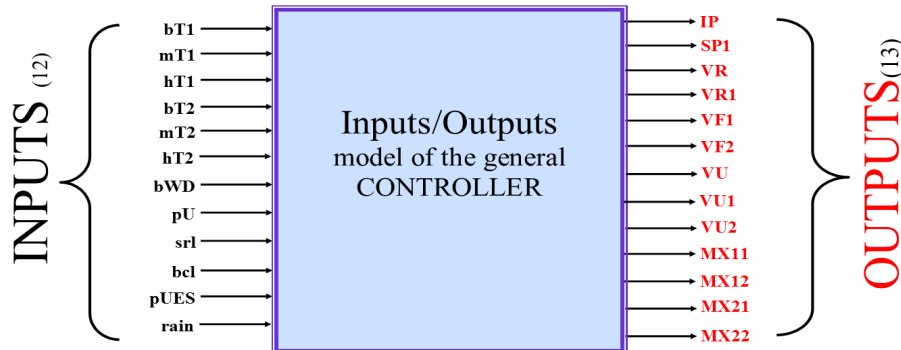


Figure 12. Input/Output model of the case study logic control system

– **Inputs of multiplexer switches** : MX_{11} and MX_{12} (for MX_1 multiplexer to select either E_1 , E_2 or E_3 pumping energy sources), MX_{21} and MX_{22} (for MX_2 multiplexer to select either E_4 or E_5 pumping energy sources).

The Input/Output model of that logic control system is presented on Figure 12. In that model, power sources are replaced by MX_{11} , MX_{12} , MX_{21} and MX_{22} which permit to command the selection of one of the power sources.

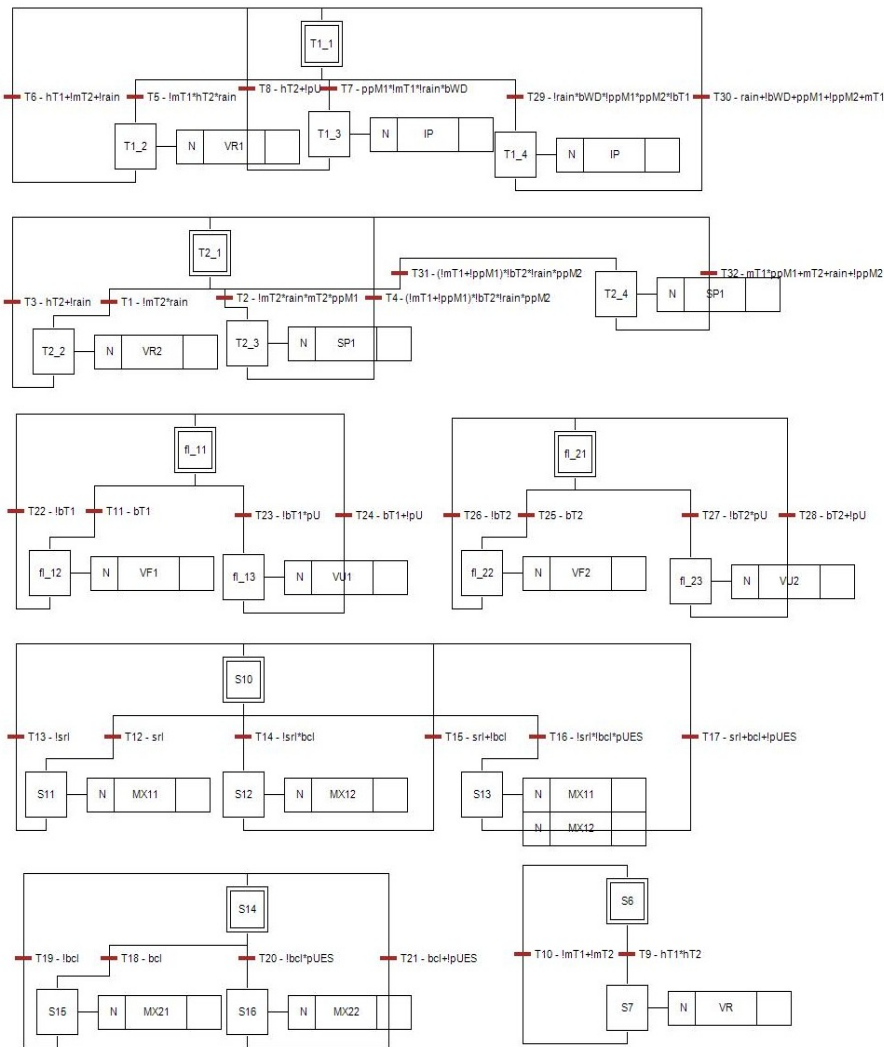


Figure 13. Grafcet specification of the case study controller

5.3. Grafcet specification model for the system

From functional specifications of the water supply system described in the previous subsection, we derive the corresponding Grafcet specification model, according to the

general method described in subsection 4.2. The Grafcet specification of the functioning of this logic control system is shown on Figure 13.

As described in the synthesis process in 4.3, when a binary program associated to the Grafcet specification model of the water supply system is sent to the EASYdsPIC4A board, this board serves as the core of the smart control unit. Thus, it receives input signals from the sensors (presence of water, pressure, and electric power), analyzes them and generates output signals in form of commands or actions to perform specific acts (open/close valves, turn on/off the pumps or choose a power source).

6. Conclusion and Perspectives

In this paper, we have presented the ability to exploit ICT advantages in order to resolve critical issues ongoing in developing countries, particularly households water supplying with electrical energy issue. We have then designed a generic and sophisticated control system that permits the analysis and the study on the availability of several energy & water sources having different costs; and automatically take a decision on the best source to be selected for ensuring continuous water service in the whole building without any interruption and with the lowest cost. The pumping mechanisms and the switching process between power sources is based on energy calculations which guarantee a considerable reduction in pumping energy.

Furthermore, the designed architecture of the water distribution system presents a generic concept of water supply that may be integrated in a building project as well as in an already existing building, having several floors and supplied through several tanks. The controller of such events-driven systems can be realized thanks to the synthesis tool, *GrafcetConverter*, that reads the Grafcet model of the system under study and produces a C-program which, after compilation and loading in the board, runs at each step by reading inputs and performing the necessary actions

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