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1 On the variation of interaural time differences with frequency

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Abstract

Interaural time difference (ITD) is a major cue to sound localization in humans and animals. For a given subject and position in space, ITD depends on frequency. This variation is analyzed here using an HRTF database collected from the literature and comprising human HRTFs from 130 subjects and animal HRTFs from six specimens of different species. For humans, the ITD is found to vary with frequency, in a way that shows consistent differences with respect to a spherical head model. Maximal ITD values were found to be about 800 μ s in low frequencies and 600 μ s in high frequencies. The ITD variation with frequency (up to 200 μ s for some positions) occurs within the frequency range where ITD is used to judge the lateral position of a sound source. In addition, ITD varies substantially within the bandwidth of a single auditory filter, leading to systematic differences between envelope and fine-structure ITDs. Because the frequency-dependent pattern of ITD does not display spherical symmetries, it potentially provides cues to elevation and resolves front/back confusion. The fact that the relation between position and ITDs strongly depends on the sound's spectrum in turn suggests that humans and animals make use of this relationship for the localization of sounds.

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20 I. INTRODUCTION

21 In humans and many animals, a major cue to localize sounds in the horizontal plane is 22 the difference in time between the peaks and valleys of the acoustical wave at the two ears, i.e. 23 the interaural time difference (ITD). Remarkably, humans can distinguish ITD differences 24 as low as 20 μ s for a wide array of sound spectra and envelope characteristics below about 1.5 kHz (Mills, 1958; Brughera et al., 2013). Furthermore, ITD has been shown to have a 25 stronger influence than interaural level differences (ILD) on the perceived lateral location of 26 sounds with energy in low frequencies (below 2.5kHz, (Wightman and Kistler, 1992)). In 27 28 animals as well, ITD is used as a cue to sound location: cats, gerbils, birds, reptiles and 29 others have dedicated neural structures in the auditory brainstem to process ITD (Grothe 30 et al., 2010). Understanding the neural processing of ITDs requires a precise knowledge of 31 the nature of the temporal disparities imposed by the head, body and environment. 32 The relationship between source position and ITD is constrained by morphological pa-33 rameters including the interaural distance, head, ear position, shape, torso, and (even) hair (Duda et al., 1999; Algazi et al., 2001b). Measuring ITDs for tones using a manikin, 34 35 Kuhn (1997) found that the ITD also varies systematically with the frequency of the tone, as reproduced in Fig. 1a. The ITD for a 2000 Hz tone presented at 45° is 400 μ s (Fig. 1a, 36 dashed line), while the ITD for a 500 Hz tone at the same position is 600 μs — about 37 50\% larger. Conversely, sounds presented at different positions can produce the same ITD, 38 39 provided they have different frequency contents. It follows then that spatial position cannot 40 be estimated from ITD independently of sound frequency. This physical phenomenon is 41 known, and has been observed in models where the head is a rigid sphere (Kuhn, 1977), or an ellipsoid (Cai et al., 2015). As an illustration we computed ITDs from the spherical 42 head model (details below) using a head radius of 9.3 cm (as reported in (Kuhn, 1977)), and 43 44 plotted it on Fig. 1b. 45 Despite these early insights, the dependence of ITD on frequency in humans and animals

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has not, to our knowledge, been quantitatively examined. We propose here to bridge that

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gap by a careful and in-depth assessment of the frequency-dependence of ITD in human and animal acoustical data. Furthermore, we provide a new interpretation of this dependence, showing that it results in different ITDs in the envelope and fine-structure of auditory filters' outputs.

After a review of the physics of the frequency-dependence of ITD using previous reports of the spherical model (section II), we provide a quantitative analysis of this phenomenon in acoustical recordings of 130 subjects from four databases (section III). Further, we show that ITDs between the envelopes and fine-structures of binaural signals are different (section IV). Finally, we analyze the frequency-dependence of ITDs in the HRTFs of six different animal species (section V), and show that the highly non-spherical nature of many animals' heads makes it hard to predict the range of ITD from head size.

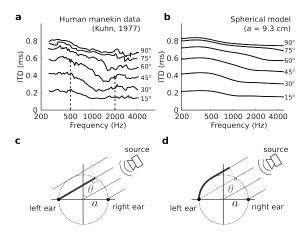


Figure 1: Frequency-dependence of ITD. (a) ITD measured with pure tones of varying frequency for different source positions on a human manikin (replotted from Kuhn (1977)).
(b) ITD computed for a spherical head model with head radius 9.3 cm. (c) Propagation of a planar sound wave with an acoustically transparent head. The additional pathlength to the contralateral ear (thick line) is a sine function of the azimuth angle θ. (d) Propagation of a high frequence planar sound wave diffracted by a sphere. The additional path to the contralateral ear is the thick line.

58 II. SCATTERING AND FREQUENCY-DEPENDENT ITDS

59 A. Phase ITD

The complete acoustical transformation occurring between a point source and the ears of a subject can be modeled as a pair of filters (H_L, H_R) usually termed Head Related Transfer Functions (HRTFs). The *phase ITD* (ITD_p, as reported in the original (Kuhn, 1977) study), is the ITD of the fine-structure of the binaural signal, defined at any frequency f using the phase response of the HRTFs:

$$ITD_{p}(f,\theta,\phi) = \frac{1}{2\pi f} \angle \left[\frac{H_{L}(f,\theta,\phi)}{H_{R}(f,\theta,\phi)} \right]$$
(1)

- 60 where θ is azimuth measured in radians, ϕ is elevation (in standard vertical-polar coordinates:
- 61 azimuth between -180° and 180°, and elevation between -90° (down) and 90° (up)). The
- 62 bracket operator \angle is the *unwrapped phase* operator that yields a continuous phase spectrum
- 63 (not constrained to $[-\pi,\pi]$). By convention, positive azimuth values indicate that the source
- 64 is to the right of the subject, where ITD_p is positive.

65 B. ITD in the spherical head model

- 66 In a first, simplified geometrical model of ITD, we can consider a planar acoustical
- 67 wave incident on an acoustically transparent head (Figure 1c). In this case, the ITD is
- 68 the difference in path lengths to the two ears (thick line) divided by the speed of sound:
- 69 ITD(θ) = $2\frac{a}{c}\sin(\theta)$, where θ is the azimuth of the sound source, c the speed of sound in air
- 70 and a the head radius. In this description, ITD does not depend on frequency: ITD does
- 71 show frequency dependence because the head is not acoustically transparent.
- A more plausible acoustical model of the situation is to assume that the head is a rigid
- 73 sphere, with ears lying on a diameter. The first observation that ITD is frequency-dependent
- 74 in this context is attributed to Lord Rayleigh's spherical head model (Rayleigh and Lodge,
- 75 1904). Many studies have then used this model to analyze binaural cues (Duda and Martens,
- 76 1998; Kuhn, 1977). In particular, the phase ITD, i.e. ITD_p as defined in Eq. 1, can be

numerically calculated at all frequencies for the spherical head model, as shown on Fig. 1b (for sources at infinite distance from the head, following Bruneau (2010)). In this model, ITD_p for any given source position generally decreases with increasing frequency (Fig. 1b), which is broadly consistent with the human manikin data reported by Kuhn (1977) and shown in Fig. 1a.

For high frequencies, when the wavelength is small compared to the head radius, the ITD tends to the difference between the shortest path lengths to the two ears divided by the speed of sound (thick line in Figure 1c), which is expressed in Woodworth's formula:

$$ITD_{HF}(\theta) = \frac{a}{c}(\sin(\theta) + \theta) \tag{2}$$

The low-frequency limit of ITD can be calculated by considering the first terms in the spherical-harmonic development of the acoustical field solution (Kuhn, 1977):

$$ITD_{LF}(\theta) \approx 3 \frac{a}{c} \sin(\theta)$$
 (3)

The ratio between low and high frequency ITD is then: $\frac{3\sin(\theta)}{\theta+\sin\theta}$, which is always greater than one. Thus the the low-frequency ITD is always greater than the high frequency ITD. For azimuths θ between 0 and $\pi/2$ radians (90°), this ratio is a monotonically decreasing function of θ . For sources near 0°, the ITD is 50% larger at high frequency relative to low frequency, but for those positions (close to the midline) ITD values are close to zero. Conversely, when the ITD is maximal for azimuths near 90°, the low frequency ITD is only about 16% larger than the high frequency ITD. Readers should note that this is hard to see on 1b.

89 C. Visualization of the scattering phenomenon

At low frequency, the head is small compared the wavelength of the sound, and one might infer that the ITD should be close to the situation when the head is acoustically transparent (Fig. 1c). This would predict a smaller ITD than in high frequency, yet the opposite occurs. The reason for this counter-intuitive phenomenon is that the sphere is not an obstacle between the source and the ears, but rather the ears are on the sphere and diffraction phenomena are at play (Kuhn, 1977).

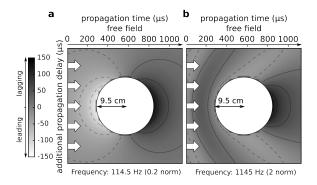


Figure 2: Propagation time of a planar sound wave in the presence of a sphere, relative to the propagation time in free field, for tone frequencies 114.5 Hz (a) and 1145 Hz (b). Propagation time in free field (no head) is shown on top. Negative values (lighter shades) indicate regions where phase is leading, and positive values (darker shades) indicate regions where the sound phase is lagging.

96 To get a better grasp of the situation, we calculated and represented the acoustical field 97 in the vicinity of the head, using the formula in Bruneau (2010, paragraph 5.2.3). In Fig. 2, 98 we show the steady-state propagation time of a monochromatic planar wave emanating from an infinite-distance source to the left ($\theta = 90^{\circ}$), relative to the propagation time for 99 100 an acoustically transparent head (free field). For head radius of 9.5 cm, the free field ITD 101 is about 550 μ s. For a low frequency tone (about 115 Hz, Fig. 2a), a phase lead appears on the ipsilateral side of the head (the acoustical wave is "compressed" against the head), and 102 103 a phase lag appears on the contralateral side (the wave must turn around the head). As a 104 result, the ITD is $550 + 150 + 150 = 850\mu$ s. For a high-frequency tone (1145 Hz, Fig. 2b), 105 the propagation time to the ipsilateral ear (left) is not affected by the head but there is 106 still a phase lag at the contralateral ear, corresponding to the additional path length. As a 107 result, the ITD is $550 + 150 = 700\mu s$, which is smaller than at low frequency.

The physical phenomenon is entirely specified by the wavelength $(\lambda = c/f)$ of the acoustical wave relative to the size of the sphere. To account for the effect of the size of the head, it is thus convenient to introduce a normalized frequency scale, where unit normalized

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- 111 frequency $(f_{norm} = 1)$ corresponds to the physical frequency of a wave with wavelength
- 112 equal to one sphere circumference: $f=c/2\pi a$. Scaling head size also scales ITD (it is
- 113 inversely related), and therefore ITD can also be normalized, so that a scaled ITD of unity
- 114 $(ITD_n = 1)$ corresponds to a physical ITD of a/c, the time for sound to propagate one
- 115 radius of the spherical head. Assuming a head radius of a = 9.5 cm, the low-frequency
- 116 condition of Fig. 2 corresponds to a normalized frequency of 0.2, and the high-frequency
- 117 condition to a normalized frequency of 2.0.
- 118 From this description, in terms of normalized time and frequency, the effect of changing
- 119 the head size on $ITD_p(f)$ is easier to grasp. It is two-fold: for a given normalized frequency,
- 120 the ITD depends linearly on head size; and the frequency scale on which ITD varies depends
- 121 linearly on the inverse of head size. In particular, the transition between the low and high
- 122 frequency regimes occurs at lower frequencies for bigger head sizes.

123 III. FREQUENCY-DEPENDENCE OF ITD IN HUMAN HRTFS

- Human head morphology is more complex than a sphere, and other parts of the human
- 125 body also influence the ITD (Kuhn, 1977). Furthermore, comparing the human-manikin
- 126 ITDs to the spherical-head ITDs in Fig. 1a-b reveals that ITDs exhibit a more complex
- 127 frequency-dependence in humans than in the spherical head model. Therefore it is necessary
- 128 to analyze the frequency-dependence of ITD from HRTF measured in real human subjects.

129 A. HRTF databases

- HRTF data were obtained from three publicly available databases (ARI (ARI, 2010),
- 131 CIPIC (Algazi et al., 2001a) and LISTEN-V1 (Warusfel, 2002)). Another set of data was
- 132 specifically recorded for this project (LISTEN-V2), following the protocol of the LISTEN-V1
- 133 database, and has not been made public yet. All data are available from the corresponding
- 134 author on request. Overall, this combined dataset includes 130 subjects (Table I). Because
- these databases were obtained in slightly different conditions (in particular spatial measure-

ment grids and number of samples), ITDs were evaluated separately in each database, and then all statistics were interpolated on a common space-frequency grid (that of LISTEN-V2) using a natural neighbor interpolation. Results are therefore always presented with a spatial resolution of 5° in azimuth and about 15° elevation.

As discussed above, the subject's head size affects ITD across positions and frequencies

140 B. Frequency dependence of human ITDs

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1. Acoustical head radius estimation and normalization

143 in a way that is completely predicted by the acoustics of sound propagation. We are not, 144 however, interested in the variability of ITD cues across the population of subjects that is explained by head size. Rather, we are interested in how this variability reflects the 145 146 variability in head morphologies. Furthermore, increasing headsize systematically shrinks 147 the frequency axis, thus averaging different subjects' ITD at each frequency will spuriously 148 smooth out ITD variations. Therefore, in order to account for the effect of head size across 149 the population of subjects, we normalize the time and frequency axes of each subject's 150 ITD data using a measure of the head of the subject derived from its HRTFs (usually 151 termed acoustical head radius, e.g. in (Algazi et al., 2001b)). Similar normalization methods 152 have been proposed in the context of reducing variability in spectral notches position and 153 amplitude (Middlebrooks, 1999). 154 We define the "acoustical head radius" for each subject as the radius of the spherical 155 model which best matches the subject's high-frequency ITD. More precisely, for each subject 156 we compute the high frequency ITD at all positions as the average phase ITD between 3kHz and 5kHz. We compute the spherical-model high-frequency ITDs in the exact same way 157 and for the same positions. The radius of the sphere is then adjusted so as to minimize the 158 159 squared differences between the subject's ITDs and the sphere's. This regression is performed using a standard gradient-descent algorithm. The best-fitting sphere radius resulting from 160 161 this procedure is the acoustical head radius of the subject. We validated this method by simulating HRTFs using the spherical head model, and recovering the radius of the simulated spherical head. As expected, we found that this method estimated accurately the radius of the sphere within 0.01 mm (over a range of sphere radii from 5cm to 15 cm).

165 We then estimated the acoustical head radius of each subject in the population. We 166 found the average head radius over all subjects to be 9.5 cm (N=130, \pm 0.48 cm standard deviation, 8.3 to 10.8 cm range). For each subject, we computed the mean squared error 167 168 between ITDs derived from the optimal spherical model and acoustically measured ITDs. 169 The mean squared error was on average 67 $\mu s \pm 22 \mu s$ STD across the population, indicative 170 of a consistently good fit. The average head radius value we found is slightly higher than 171 the one reported in the (Algazi et al., 2001b) study, which was obtained using another ITD estimation method (onset-time differences), and only on positions on the horizontal plane. 172 The same estimation and fitting method on our data yields a radius of 8.43 cm (\pm 1.14 cm), 173 174 consistent with the value reported by (Algazi et al., 2001b).

The goal of this normalization procedure was to account for the systematic effect of head size on the variability of the ITD measures across the population. We computed the standard deviation of ITD at each frequency and position across the population of subjects before and after normalization. The average standard deviation before normalization was 54 μ s and reduced by about 20% with normalization (42 μ s STD, using the average head size of 9.5 cm to convert to physical units). This reduction was quantitatively different across databases, and more pronounced in databases with more subjects (45% in LISTEN-V2).

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182 Most ITDs and derived statistics are reported in the rest of the manuscript on normalized 183 frequency and ITD scales with a single pair of normalization factors (frequency and ITD) for the population. For ease of reading, when representing human ITD data, ITDs and 184 185 frequencies are represented both in normalized and direct physical units, with a conversion factor assuming a head radius equal to the average over the population (a = 9.5 cm). For 186 this value of the head radius, a normalized frequency of 1 corresponds to a frequency of 573 187 Hz, and a normalized ITD of 1 corresponds to an ITD of 278 μ s. Therefore, to convert from 188 189 normalized to physical ITD in μ s, multiply the normalized value by 278 μ s. To convert from 190 normalized to physical frequency, multiply the normalized value by $573~\mathrm{Hz}$.

191 2. Asymptotic ITD in the horizontal plane

- We estimated the asymptotic low and high frequency values of the ITD to compare them
- 193 with theoretical predictions from the spherical model (Figure 3).
- The high-frequency ITD, ITD_{HF}(θ) is estimated as the mean ITD between $f_{norm} = 7$
- 195 (4010 Hz) and $f_{norm} = 8$ (4600 Hz). As per construction, the Woodworth formula (Figure
- 196 3a, black) fits the data (shaded area: mean $ITD_{HF}(\theta)$ over subjects $\pm 1/2$ s.d.), except when
- 197 the azimuth is in the $70 110^{\circ}$ range, which has been previously documented (Aaronson
- 198 and Hartmann, 2014). Figure 3B shows the low frequency prediction with Kuhn's formula
- 199 (Eq. 3) alongside mean ITD estimated from HRTFs between $f_{norm}=0.5~(290~{\rm Hz})$ and
- 200 $f_{norm} = 0.6$ (350 Hz), termed low frequency $ITD_{LF}(\theta)$. Consistent with previous reports,
- 201 the approximation of the low-frequency ITD is reliable.
- On Figure 3c, the values of ITD across frequency are reported for seven positions on the
- 203 horizontal plane (0, 30, 60, 90° and the symmetrical positions). Curves represent the average
- 204 normalized ITD across subjects, and shaded areas are ± 1 s.d.. The standard deviation of
- 205 the normalized ITDs at each frequency and position was on average 46 μ s (0.16 normalized).
- 206 This variability is relatively small: it is about 6% of the maximal ITD value observed, and
- 207 is about a factor of two larger than a human just-noticeable difference (JND) in ITD (the
- 208 smallest ITD difference perceptible by human subjects (Mills, 1958)).
- In addition, the plots on Figure 3c reveal some fine variations of ITD with frequency
- 210 that are not accounted for by the spherical model (e.g. the low frequency bump for azimuth
- 211 $\pm 30^{\circ}$). This reveals that deviations of the human head morphology from a sphere contribute
- 212 systematically to the ITD versus frequency relationship.

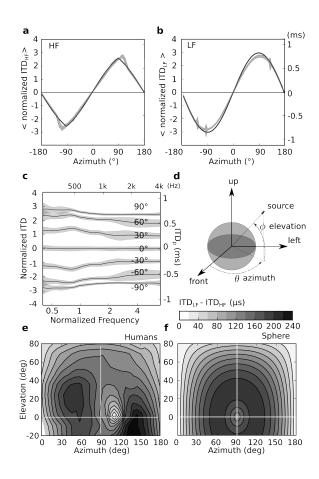


Figure 3: Frequency dependence of ITD in human subjects. (a) Inter-individual average normalized ITD in high frequency as a function of azimuth ±1/2 s.d. (shaded area). Black line indicates the theoretical value from the Woodworth model (Eq. 2). Corresponding ITD values for a head radius of 9.5 cm are shown on the right of panel b. (b) Average normalized ITD in low frequency ±1/2 s.d. (shaded area), black line indicates the theoretical value from Kuhn's formula (Eq. 3). (c) Average normalized ITD (black lines) as a function of frequency for seven source positions (shaded area: ±1/2 s.d.). (d) Azimuth θ and elevation φ are defined in a standard vertical-polar coordinate system (see text). (e) Difference between high- and low-frequency normalized ITD as a function of elevation and azimuth. Physical ITD is calculated for a head radius of 9.5 cm. (f) Same as (e) for the spherical model. Normalized units correspond to a head radius of 9.5cm.

213 3. Frequency variation of ITD as a function of azimuth and elevation

214 Consistent with previous reports, our data show that ITD is frequency-dependent in human HRTF, with similar differences between low and high frequency values as in the 215 spherical models in the horizontal plane. We now quantify this difference as a function 216 217 of both azimuth θ and elevation ϕ . Recall that we used a vertical-polar coordinate system (Fig. 3d). Fig. 3e shows the average difference ITD_{LF}-ITD_{HF} across subjects for all positions 218 219 on the spatial grid, converted to physical ITD values assuming head radius of 9.5 cm. For 220 comparison, the same quantity is shown for the sphere on Fig. 3f. 221 The difference between high and low frequency ITD exceeds 50 μ s for most of the 222 positions on the sphere, and can reach more than 200 μ s. As a comparison, human subjects can discriminate ITDs differing by a JND of only 20 μ s (Mills, 1958). Therefore, the variation 223 224 of ITD with frequency should be perceptually significant for most source positions away from 225 the midline. 226 For large enough source distances, the pressure at any point on the surface of a sphere 227 depends only on the angle between the ray from the center of the sphere to the source, 228 and the ray to the measurement point on the surface of the sphere (Duda and Martens, 229 1998). Because of this symmetry property, binaural cues are constant for sources lying on 230 so-called cones of confusion, centered on the interaural axis. In other words, acoustical cues in a spherical head model only depend on the angle of the source acoustical wave and the 231 232 medial-sagittal plane: the incidence angle $\beta = \arcsin(\cos(\phi)\sin(\theta))$. Cones of confusion are 233 then the set of points of equal incidence angle β . This aspect makes it hard to differentiate 234 sound sources positioned symmetric to the interaural axis, which includes front and back 235 positions. 236 Consistent with previous reports in humans, our data show that cones of confusion are 237 centered around source positions directly facing the ears (that is, at the same azimuth and 238 elevation as the ears, Aaronson and Hartmann, 2014). Furthermore, they appear distorted 239 (around $(\theta, \phi) = (110^{\circ}, 5^{\circ})$, Fig. 3e). In particular, the variation of ITD with frequency 240 quantitatively differs between front and back (and up and down) positions.

241 C. Maximal ITD

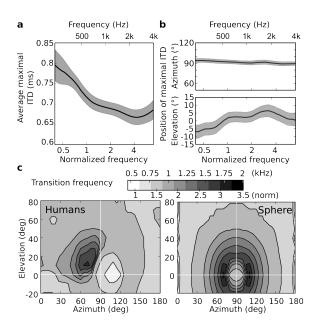


Figure 4: Maximal ITD and transition frequency in human subjects. (a) Maximal ITD across subjects as a function of frequency. (b) Azimuth (top) and elevation (bottom) where ITD is maximal as a function of frequency Shaded areas of (a) and (b) are the mean $\pm 1/2$ s.d. (c) Transition frequency (see text) as a function of azimuth and elevation in humans (left) and in the spherical model (right). Normalized units converted assuming a head radius of 9.5cm.

We estimated, from the unnormalized data, the maximal ITD over positions for each frequency and subject (reported here on a normalized frequency scale). By nature, ITD estimation can be unstable in high frequency because of the ambiguity inherent when unwrapping a phase response, and in low frequency because of the low frequency resolution. This is especially prominent when automatically processing a large number of recordings (several hundred positions, and subjects), and creates many outlier datapoints, which positively biases the estimation of a maximal ITD.

The 95% percentile (see, e.g., Papadatos, 1995) is a more robust estimator of sample maximum, which we define here as the maximal ITD. Consistent with the theory and previous reports, we found that the maximal low-frequency ITD value is 813 μ s \pm 70 μ s (s.d., see Fig. 4a). The maximal broadband ITD – computed as the peak lag of the cross-correlated impulse responses, was found to be 612 μ s \pm 34 μ s (s.d.). This value is very close to the value of the maximal high frequency ITD, 688 μ s \pm 47 μ s (s.d., see Fig. 3b).

The maximal ITD occurs for azimuth around 95° (Fig. 4b), for which the source is 255 256 directly facing one of the two ears, which is consistent with previous reports (Aaronson and 257 Hartmann, 2014). There are systematic variations of the position of maximal ITD with 258 frequency, but it remains near eccentric azimuths $(\pm 90^{\circ})$ and close to the horizontal plane (-10° to 10°). In the spherical model computations, the maximal ITD is reached at $\theta = 90^{\circ}$ 259 260 (Eq. 3), in humans it occurs for positions slightly more to the back (Fig. 4b), and for 261 sources originating from below or above the horizontal plane, depending on the frequency 262 of the signal (Fig. 4b).

263 D. Transition between ITD regimes

264 It could be argued that even though the ITD varies across frequency, this variation does not occur in the range where ITD is used as a cue to azimuth (i.e. the ITD is constant 265 266 below 1.8 kHz). To assess this, we examined the shape of the ITD versus frequency curves, 267 specifically trying to get at the frequency at which ITD effectively transitions between its low 268 and high frequency regimes. We define the transition frequency as the frequency at which the ITD equals the average between its high frequency (ITD_{LF} (θ, ϕ)) and low-frequency 269 270 $(ITD_{HF}(\theta,\phi))$ values for a given position. Because in general ITD is a decreasing function of frequency with a relatively narrow transition, this transition frequency allows us to separate 271 272 frequency regions of high and low ITD values for any position.

Figure 4C shows the transition frequency in humans and in the spherical head model 274 (for an infinitely distance source), as a function of azimuth and elevation. The transition

- frequency increases as the source is moving away from the median sagittal plane, up to an azimuth angle $\simeq 70^{\circ}$ where a maximum value $f_{\rm tran} \simeq 2.8$ (3.2 in the spherical model) is reached. It then decreases until a minimum is reached at $\theta \simeq 110^{\circ}$ and $\phi \simeq 0^{\circ}$ ($\theta = 90^{\circ}$ and $\phi = 0^{\circ}$ in the spherical model).
- In conclusion, for all positions, transition frequencies are between 1 and 3 (normalized scale), which corresponds to physical frequencies between approximately 600 and 1700 Hz.

 The ITD thus varies substantially at frequencies within the range where ITD is the dominant cue for sound laterality in the horizontal plane (Wightman and Kistler, 1992). The magnitude of transition frequencies in humans is overall similar to the predictions of the spherical model, yet as previously mentioned symmetries seen in the spherical model do not appear in the human HRTF data.

286 IV. ENVELOPE AND FINE-STRUCTURE ITD

287 When a sound wave excites the cochleae, different points on the basillar membranes are 288 preferentially excited by energy in different frequency bands. Many neurons in the auditory 289 system, in particular neurons in the midbrain that are sensitive to ITD, are also tuned 290 to different frequencies and are tonotopically organized. We have shown that ITD varies 291 substantially across different frequency bands, that is, between distant auditory filters (Fig. 292 5a). An interesting question is whether ITD also varies substantially within a single auditory 293 filter (Fig. 5b), as it would then have direct physiological relevance. We relate this question 294 to the difference between envelope and fine-structure ITD.

295 A. Variation of ITD within a auditory filter

We first analyzed the variation of ITD within single channels for each position and subject (same HRTF database as in Section III). The variation of ITD is defined as the difference between the maximum and minimum ITD_p in a frequency band with constant Q = 4.3 (one-third octave) or with equivalent-rectangular bandwidths (ERB) (Glasberg

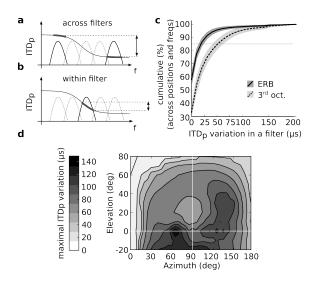


Figure 5: Variation of ITD within single auditory filters. (a) Schematics of the global variation of ITD across different auditory filters. (b) Schematics of the variation of ITD within a single auditory filter. (c) Proportion of positions and center frequencies where ITD variation within a single channel is smaller than a specified value. Lines are averages across population, \pm s.d.. Channel width is either 1 ERB or 1/3 octave. (d) Maximal ITD variation within single channels, as a function of azimuth and elevation, with ERB-wide channels.

and Moore, 1990) (Fig. 5b). In the ERB scale, the Q factor value varies between 5 and 9, indicative of the relatively narrow band filtering imposed by the auditory periphery. We computed the variation of ITD for center frequencies between 350 and 3000 Hz and for positions close to the horizontal plane ($|\phi| \leq 20^{\circ}$). We report the cumulative distributions of ITD variation on Fig. 5c: curves display the percentage of positions and center frequencies for which the ITD variation is lower than a given amount. In both conditions, for more than 15 % of the channels and positions the magnitude of the ITD variation is larger than 25 μ s (Fig. 5c). In Fig. 5d, we show the maximal variation of ITD in single channels as a function of azimuth and elevation (assuming ERB-wide channels). That is, for every position, we report the variation of ITD in the channel where it varies the most. At specific source positions, very large variations of ITD can occur within channels (up to 150 μ s): the

311 variation of ITD within a single channel is therefore quite substantial.

The fact that ITD varies within a frequency band means the signal undergoes more than a simple delay when passed through the HRTF. Mathematically, the phase responses of the monaural filters are nonlinear functions of frequency. We can approximate the IPD by an affine (i.e. linear with a non-zero intercept) function of frequency around the center frequency f_0 of a cochlear filter (Fig. 6a):

$$IPD(f) \stackrel{def}{=} ITD_p(f)f$$

$$\approx ITD_g(f_0)(f - f_0) + IDI(f_0)[1]$$

where phases are expressed in cycle. The slope of this fit is the *group* ITD, which is the ITD of the envelope (Marple Jr, 1999).

314 The intercept IDI is an additional shift in the phase of the fine-structure of the signal 315 (Fig. 6b). This shift only occurs when the phase ITD varies with frequency, i.e., when 316 propagation does not result in a pure delay. For this reason, we termed this binaural cue the Interaural Diffraction Index (IDI, see Rebillat et al. (2014)). The IDI can be seen as a 317 318 measure of the difference between group and phase ITDs at any frequency, converted into a phase value: $IDI = (ITD_p - ITD_g)f$. If IDI = 0 cycles, phase and group ITD are equal, and 319 320 locally frequency-independent. When the IDI is positive, by convention the phase ITD has a higher absolute value than the group ITD, and vice versa when IDI is negative. 321

322 B. Estimating ITD in the envelope and fine-structure of binaural signals

The group ITD is classically defined as the derivative of the unwrapped IPD curve with respect to frequency as represented in Fig. 6a. Because of occasional errors of the phase unwrapping operation, estimating the derivative from large sets of unwrapped IPD curve is unreliable. Instead we use an equivalent approach wherein we perform circular-linear fits on the wrapped IPD. The estimation can be formulated as a non linear least square problem, where IDIand ITD_gare chosen to minimize the fit error $\sum_f \|\text{IPD}(f) - (\text{IDI} + \text{ITD}_g f)\|^2$ over a given frequency band, where the norm $\|.\|$ is a norm on phases. Because wrapped phase

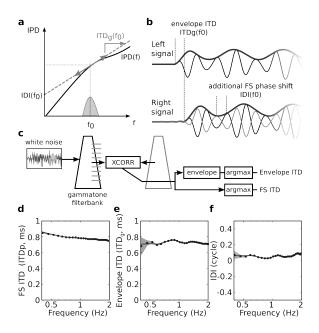


Figure 6: Envelope and fine-structure ITD. (a) The IPD for one position is unwrapped and an affine fit is taken locally around f_0 . The intercept of the fit is the IDI and the slope the group ITD. (b) When the IDI is zero, the delay is frequency-independent and both envelope and fine-structure are delayed by the ITDg (bottom, black signal). When IDI is non zero, the fine-structure undergoes an additional phase shift equal to the IDI (bottom, grey signal). (c) Simulation: white noise is passed through HRTF filters for one position (spherical head model, azimuth = 70°). The resulting signals are then fed into gammatone filterbanks. The responses in the two banks are then cross-correlated, and the result is separated in envelope and fine-structure components. The time lag of the maximum of the cross-correlation is the phase ITD, and that of the maximum of the envelope of the cross-correlation is the envelope ITD (see text). (d) Results of estimating phase ITD, ITD_p, from the IPD (plain line), and from simulations (mean: dots, shaded area: 95% confidence interval). (e) Same as (d) for ITD_g. (f) Same as (d) for IDI.

values are a circular quantity, so is the norm we use in the fit. It can be expressed as a cosine function of its argument: $||x||^2 = 1 - \cos(2\pi x)$. The precise algorithm used is described in more details in the Methods section of Luling *et al.* (2011).

333 To show in practice that group ITD and IDI can be extracted from the envelope and 334 fine-structure of band-limited binaural signals, we simulated a simple model of the auditory 335 periphery. We then computed the envelope and fine-structure ITD in different frequency 336 bands of our auditory model (Fig. 6c) using a standard cross correlation approach. The 337 auditory periphery model consisted of two gammatone filter banks receiving 100-ms-duration 338 white-noise inputs convolved with the spherical HRTFs. Each filter's response was then cross-correlated with the opposite frequency band. This operation is a good approximation 339 340 of the response of binaural neurons in the medial superior olive of mammals (Yin and Chan, 341 1990). The fine-structure ITD is obtained by computing the position of the maximum of 342 the cross correlation function. Then, the envelope of the cross-correlation is extracted using a Hilbert transform, and the maximum computed. This procedure yields an estimate of 343 344 the delay in the envelopes (i.e. it is equivalent to computing the maximum of the crosscorrelation of the envelopes Marple Jr (1999)). The results of this simulation are plotted 345 on Fig. 6d-f. Dotted points (with 95% confidence intervals over repeated trials) represent 346 347 the ITDs estimated using the simplified auditory model. The theoretical predictions (plain lines) were obtained by taking circular-linear fits of the IPD of the HRTF pair used. The 348 349 match between theory and simulation is excellent, which shows that the group ITD indeed 350 corresponds to the envelope ITD, which appears in the cross-correlation of the monaural 351 signals, and the IDI indeed corresponds to the additional shift of the fine-structure seen in 352 the cross-correlation function.

353 C. Analysis of envelope and fine-structure ITDs in human HRTFs

We computed ITDs in the envelope and fine-structure of the human data presented in Section III, according to the methods presented above. On Figure 7 we present the average ITD_p, ITD_g and IDI over the whole population. We observe that ITD_p and ITD_g can be dramatically different in some frequency bands (typically around 1kHz). As a result the IDI is non-zero in that range (Figure 7e), which corresponds to the frequency range just above

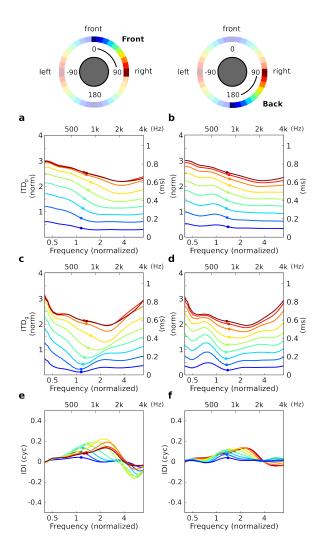


Figure 7: Averages over the whole population of normalized ITD_p (a,b), ITD_g (c,d), and IDI (e,f) for horizontal plane positions as a function of frequency. Top part of the figure depicts the lines color codes (positive azimuths, separated by 10°). Blue lines are more medial positions, and red more eccentric. Left column (a,c,e) displays data from the front positions, right column (b,d,f) from the back positions. Dots overlaid on the line plot represent the position of the transition frequency.

the "transition frequency" introduced above (data not shown).

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For all positions, we find that the IDI is close to zero for lower frequencies. It then positively increases in low frequencies (below 2-3 kHz) and then drops to negative values for higher frequencies (above about 4kHz). Therefore, generally the fine-structure ITD is higher

than the envelope ITD for frequencies between 1 and 3 kHz, and smaller in high frequencies (around 4kHz). While both ITDs are monotonically increasing functions of eccentricity (Figure 7a-b, c-d), the relationship is more complex for IDI. In addition, as noted in the above statistical analyses, the frequency-dependence of ITD is different for front and back positions (Figure 7e,f), which is potentially a cue to disambiguate between them.

368 V. FREQUENCY-DEPENDENCE OF ITD IN ANIMALS

369 In many animal species, neurons tuned to ITD have been identified, e.g. in the Medial 370 Superior Olive (MSO) or Inferior Colliculus (IC) of mammals (Yin and Chan, 1990). A recent debate has emphasized the importance of the natural distribution of binaural cues in 371 372 our understanding of electrophysiological data (Grothe et al., 2010). In this context, and 373 more generally in neurophysiological studies of sound localization, binaural cues (ITD and 374 Interaural Intensity Differences, IID) have been measured for a number of animal species, 375 including mammals, but also birds and reptiles. 376 As seen in humans, a strong dependence on morphological features of the animals is found in many instances. For example, the owl's facial ruff (Campenhausen and Wagner, 377 2006), or the cat's pinnae (Tollin and Koka, 2009) increase the magnitude of ITD at a given 378

position. However, the variation of ITD with frequency has received little attention until

recently (Benichoux et al., 2015). We applied the same analysis as above to measured HRTFs

381 of different animal species.

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382 A. Animal HRTF recordings

We measured the HRTFs of six taxidermist animal models, using the same setup as for the human recordings (LISTEN-V2, see Table I): rat, rabbit, guinea pig, chinchilla, cat and macaque. All animals had their ear canals obstructed by the taxidermy, which means that recordings are taken in a blocked-meatus configuration. Animal models were chosen according to the well-preserved quality of their pinnae. We previously showed that 388 HRTFs measured on taxidermist models agree closely with acoustical simulations based on 389 3D models of the animal with rigid boundaries (Rebillat *et al.*, 2014).

390 In general, animal models were in a natural-looking position, in which the head of the animal is not aligned with the body. Therefore, the coordinate system is rotated so that 391 the head points in the 0° direction. This is achieved by computing the head angle relative 392 393 to the body: the azimuth that minimizes the magnitude of the low-frequency ITD value. Head angles were generally non-zero for all models (rat 10°, rabbit -10°, guinea pig 20°, 394 395 chinchilla -20°, cat -55°, macaque -30°). It should also be noted that the interaural distance 396 of the rabbit, guinea pig and macaque models in the present study are noticeably smaller 397 than those of animals of the same species whose recordings are reported in the literature 398 (see Table II).

399 B. Frequency-dependent ITD in animals

A difference between low- and high-frequency ITD in animals has been previously shown 400 401 in a number of animal species: in the rat (Koka et al., 2008), rabbit (Kim et al., 2010), guinea 402 pig (Greene et al., 2014), chinchilla (Lupo et al., 2011; Koka et al., 2011), cat (Roth et al., 403 1980; Tollin and Koka, 2009) and macaque monkey (Spezio et al., 2000). Yet, only very 404 few studies reported the frequency-dependent ITD curves for many azimuth positions. The 405 phase ITD for all animal models and frequencies between 350 and 3000 Hz is reported on 406 Fig. 8, for positions in the horizontal plane. Consistent with physical acoustics, and the 407 above results in humans, the phase ITD is frequency-dependent in all species.

Because humans are bipeds, no part of the body normally finds itself on the way between the source and the ears. In many quadrupeds, for example in the cat (Fig. 8e), sounds coming from the back can be reflected or scattered by the body before reaching the head and ears. This morphological asymmetry results in large differences between the frequency-dependent ITDs of sources in the front (solid curves) and in the back (dashed). Thus in principle, front and back positions can be distinguished on the basis of the ITD at different

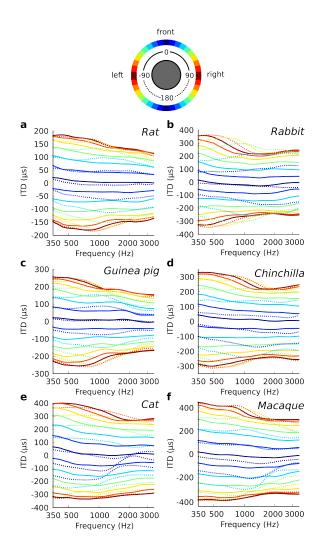


Figure 8: Animal ITDs in the horizontal plane, for 24 positions around the head (separated by 15°). Top: line color code; front positions, solid lines; back, dashed lines. (a) Rabbit, (b) Guinea pig, (c) Chinchilla, (d) Cat, (e) Rat, (f) Macaque.

frequencies. Similarly, it was shown using acoustical measures and simulations that the posture of the animal influences the frequency-dependent pattern of ITD (Rebillat *et al.*, 416–2014).

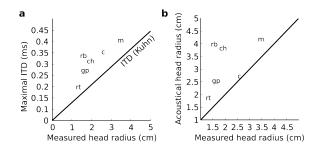


Figure 9: Comparison of measured ITD range with anatomy. (a) Maximal measured low-frequency ITD as a function of half the interaural distance measured on the taxidermist models. Predictions are shown for Kuhn's formula (solid). (b) Acoustical head radius estimated with Woodworth's formula (see Text) vs. half the interaural distance measured on the taxidermist models (dashed line: diagonal). Legend: rb: rabbit; ch: chinchilla; gp: guinea pig; m: macaque; rt: rat; c: cat.

417 C. Estimating animal ITD from head size

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418 For electrophysiological studies, a way to estimate the maximal ITD for a given animal species is to measure the interaural distance and then use one of Woodworth's (Eq. 2) or 419 Kuhn's formula (Eq. 3). The maximal ITD is thus obtained in low frequencies (via Eq. 3) 420 421 for the most eccentric position, that is $ITD_{max} = 3a/c$. However, in some species there is 422 evidence that this method yields an underestimation of the maximal ITD (see, e.g. (Tollin and Koka, 2009) in the cat). "In Fig. 9a, the maximal ITD measured in the horizontal 423 424 plane is reported as a function of the half interaural distance of the animal, measured as the 425 half distance between the entrances of the (occluded) ear canals. In all cases, the maximal 426 ITD is well correlated with the physical head size, but substantially larger than predicted 427 using the Kuhn formula. We further computed the acoustical head radius for each animal 428 model, as we did in humans (see Section III). Consistent with previous observations (e.g. 429 (Tollin and Koka, 2009)), the acoustical head radius of animals is substantially larger than 430 their physical "head radius" (the half interaural distance of the animal model, Fig. 9b).

Overall, our animal results suggest that the maximal ITD should not be estimated from

432 a crude measure of the morphology of the animal (here interaural distance), because this 433 leads to a systematic underestimation of the magnitude of ITD for all species.

434 VI. SUMMARY AND DISCUSSION

435 A. Summary

436 In this paper, we have quantified the variation of ITD with frequency in humans and 437 animals, measured in anechoic space. First, we confirmed that ITD does vary significantly 438 with frequency, as predicted by a spherical head model (Kuhn, 1977) and mentioned in 439 previous studies (Wightman and Kistler, 1989). Specifically, maximal ITD values were found to be about 800 μ s in low frequencies and 600 μ s in high frequencies. Therefore, the 440 441 low frequency ITD can be larger than the high frequency ITD by as much as 200 μ s, which is an order of magnitude larger than human JNDs in ITD discrimination tasks (of the order 442 443 of 20 μ s), even for pure tones (Brughera et al., 2013) (10-40 μ s for frequencies below 1250 444 Hz). The transition between low- and high-frequency ITDs occurs at frequencies between 445 600 and 1800 Hz, within the range where ITD is a dominant cue for localization in the 446 horizontal plane (Wightman and Kistler, 1992). 447 Additionally, we observe that the frequency-dependence of ITD does not exhibit sim-448 ple spherical symmetries. In particular, symmetrical front and back (and up and down) 449 positions, both in humans and animals, have different frequency-dependent ITDs. The fre-450 quency dependence of ITD provides, in addition to azimuth, a cue to elevation including information about front versus back. 451 452 We also show that for multiple of source positions, ITD varies not only globally across the spectrum, but also locally within the bandwidth of a single auditory filter. This causes 453 454 different ITDs for envelope and fine-structure, which can provide additional information 455 about the position of the sound source. Furthermore, those cues can be estimated from 456 binaural signal using cross-correlation. The difference in group and fine-structure ITD is 457 quantified by the interaural diffraction index (IDI).

458 B. Relation with psychoacoustical experiments

459 A few studies have examined the sensitivity of human subjects to the frequency-460 dependence of ITD. Kistler and Wightman (1992) showed that localization errors for bursts of white noise are similar with individual HRTFs compared to HRTFs in which the monaural 461 phase information was degraded. However, these manipulated HRTFs — minimum-phase 462 filters, do in fact preserve the frequency-dependence ITDs, in a way known to be close to 463 those of measured HRTFs (Kulkarni et al., 1999). 464 465 In a study on the cues for externalization of sounds, Hartmann and Wittenberg (1996) showed that human subjects are unable to detect the substitution of the phase information 466 467 of HRTFs by a properly adjusted frequency-independent ITD. The test was done for a source location at 37° on the horizontal plane, in an anechoic room. According to our analysis, at 468 469 that location the ITD varies by about 130 μ s across frequency and the transition frequency is 900 Hz (about 1.6 in normalized frequency). Kulkarni et al. (1999) also found that human 470 subjects were unable to discriminate individual HRTFs from linear phase HRTFs, as long as 471 472 the average low-frequency ITD was correct. Constan and Hartmann (2003) also showed that 473 subjects cannot determinate whether binaural sounds have frequency-independent ITDs or frequency-dependent ITDs as in the spherical model — however, neither of these two cases 474 475 is entirely realistic. 476 The fact that human subjects cannot perceive the difference is puzzling, because they can detect ITD changes of 10-40 μ s in pure tones below 1250 Hz (Brughera et al., 2013). 477 Furthermore, in a two-dimensional absolute localization task the mean error is about 5° in 478 479 the frontal hemifield (for broadband noise bursts, Makous and Middlebrooks (1990)), which corresponds to about 50 µs ITD. As the ITD variation across the spectrum can reach 200 480 μ s for some positions, systematic frequency-dependent errors should be observed if the ITD 481 482 variation were discarded.

tones when they are presented in isolation, but they cannot detect them when they are

Together, these studies suggest that human subjects can detect small ITD changes in

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485 embedded in a complex sound, as long the average ITD is unchanged. This is consistent 486 with the notion that source location is inferred from the pattern of ITD, but that only that inferred location, rather than the acoustical cues, is available to conscious perception and 487 488 behavior, and in particular is used in discrimination tasks. Thus, two sounds with different 489 patterns of frequency-dependent ITD are indistinguishable if they yield the same estimated 490 location. This is consistent with other aspects of binaural hearing. In particular, it has been shown that the sensitivity to interaural intensity differences (IID) is substantially degraded 491 492 when the use of intracranial position as a cue is eliminated by roving the the ITD of the 493 stimuli (Bernstein, 2004).

494 A possible experiment to determine whether ITD information is discarded in estimating 495 the location of the source is to include judgements of the position of sounds with different 496 frequency contents. For example, localization performance could be tested as in measured 497 HRTFs with linear phase HRTFs, but with band-pass filtered noises in different frequency regions. If the frequency-dependence of ITD is discarded, then results should be identical 498 499 in the two conditions (provided the ITD of linear phase HRTFs is adjusted). On the other 500 hand, if the variation of ITD is indeed taken into account to estimate source position, we should observe systematic errors depending on frequency and position. 501

502 C. Binaural coherence

503 Binaural coherence is defined as the maximal value of the cross-correlation of monaural signals (Gabriel and Colburn, 1981). Humans are very sensitive to small changes in bin-504 505 aural coherence, usually modeled by adding a small amount of independent noise at each ear (usually below 3-4\% for noise (Gabriel and Colburn, 1981)). In HRTF recordings, bin-506 507 aural coherence is found to be mainly affected by the amount reverberation in the room: 508 binaural coherence is very high in anechoic environments, and dramatically goes down as the environment gets more reverberant (Hartmann et al., 2005). It can be argued that the 509 510 effect of the variation of ITD within an auditory filter is a decreased coherence (Constan and Hartmann, 2003). Yet, in anechoic conditions this effect remains marginal, especially for the narrow bands of noise resulting from filtering by the auditory periphery (less than 0.1% (Constan and Hartmann, 2003)).

514 We argue here for a different interpretation of the frequency-dependence of ITD. De-515 coherence due to reverberation is intrinsically non-deterministic: different wavefronts reach the listener at different times depending on the unknown geometry of the room. On the 516 517 other hand, we have shown above that the frequency-dependence of ITD has a fully deter-518 ministic effect: envelope and fine-structure ITD cues are affected in a way that is predicted 519 by the morphology of the subject. Decoherence, insofar as it is non-deterministic, objec-520 tively makes the task of recovering the ITD from the cross-correlation function harder. It is unclear, however, why imposing different ITDs in the envelope and fine structure of the 522 monaural signals would make the recovering of ITDs harder, because it is fully deterministic. 523 Therefore, we argue that the variation of ITD in small frequency bands is best thought of as 524 imposing different ITDs in the envelope and fine-structure of monaural inputs, rather than 525 as causing binaural decoherence, as imposed by adding independent white noise to monaural 526 inputs.

527 D. Signal processing of binaural sounds

Our results are relevant to two classes of signal processing applications: reproduction of binaural sounds and sound localization algorithms. The large variation of ITD with frequency suggests that it is important for proper reproduction of binaural sounds. However, it could be that humans can adapt to non-natural ITD patterns, as they do to spectral cues (Wanrooij and Opstal, 2005). In either case, we note that replacing frequency-dependent ITDs with fixed ITDs removes some potential cues to elevation.

State-of-the-art sound localization algorithms using HRTF-filtered inputs do use the frequency-dependence of ITD to estimate source location. In the algorithm described by May et al. (2011), sounds are divided into frequency bands, and position is estimated with a

537 maximum likelihood approach from the overall ITDs in these bands. Because ITD likelihood 538 for each position is measured with KEMAR HRTFs, this algorithm uses the variation of ITD 539 across channels. However, it does not use the variation of ITD within channels.

540 Other algorithms use HRTF data with the within-channel ITD variations preserved, 541 (Durkovic et al., 2011; Macdonald, 2008) and were shown to perform well in realistic condi-542 tions. In each frequency band, monaural signals are convolved with the contralateral HRTF 543 of a candidate source position (i.e., left signal with right HRTF), and the position giving the 544 highest cross-correlation is picked. A spiking neural model relying on similar ideas was also 545 previously presented (Goodman and Brette, 2010): it used cross-correlation, biophysically 546 modeled with coincidence detection between spike trains, and performed better when the variation of ITD within channel was taken into account. 547

${f E.~Electrophysiology}$

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549 The firing rates of neurons in several auditory brainstem nuclei, in particular the me-550 dial superior olive (MSO) and inferior colliculus (IC) of mammals, is sensitive to the ITD 551 of binaural sounds (Grothe et al., 2010). Similar to humans, we have shown that ITD is 552 frequency-dependent in animals, in the frequency range where it is used for sound localiza-553 tion (Fig. 8). Furthermore, we showed that asymmetries in this frequency-dependence exist 554 between front and back positions, presumably due to reflections on the back of the animals 555 (Fig. 8). Finally, we have noted that the maximal ITD is generally larger than when esti-556 mated from simple morphological considerations (Fig. 9). All these observations should be 557 taken into account when interpreting electrophysiological measurements.

In the physiological literature, two types of frequency-dependent properties have been discussed (Grothe et al., 2010; Day and Semple, 2011; Benichoux et al., 2015). The preferred ITD of binaural neurons, i.e., the ITD that elicits the largest firing rate, depends on their preferred frequency: at the level of the population those quantities are inversely correlated.

This observation has been seen as a challenge to the mainstream theory, according to which

- 563 neurons are tuned to the ITD of particular source locations, which should cover all possible
- 564 locations independently of the frequency band (Grothe et al., 2010). In our animal mea-
- 565 surements, ITD is also larger in lower frequencies than in high frequencies although to a
- 566 smaller extent than in electrophysiological recordings. An additional contribution to large
- 567 low-frequency ITDs in animals is early reflections on the ground, which produce arbitrarily
- 568 large ITDs in low frequencies (Gourevitch and Brette, 2012).
- Many binaural neurons also display a second type of frequency-dependence: for a given
- 570 neuron, the preferred ITD depends on the frequency of the sound (Day and Semple, 2011).
- 571 We have shown that ITD varies also with frequency within an auditory filter, which provides
- 572 a potential ecological explanation of this variation (Benichoux et al., 2015). The present
- 573 analysis suggests that cells with frequency-dependent best delays should be differentially
- 574 sensitive to envelope and fine-structure delays.

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Database	N_s	$\Delta\theta$	$\Delta \phi$	N_{sub}	Room type
LISTEN-V1	8192	15 °	\simeq 15 $^{\circ}$	49	Anechoic
LISTEN-V2	8192	$5\degree$	\simeq 15 $^{\circ}$	35	Anechoic
CIPIC	200	$\simeq 10~^\circ$	$5.6\degree$	36	Anechoic
ARI	2400	$5\degree$	$10~^{\circ}$	10	Semi-anechoic

Table I: Overview of the different human HRTF databases used in this study. For each database, the sampling frequency is 44.1 kHz. N_s : length of the head-related impulse responses in samples. $\Delta\theta$, $\Delta\phi$: approximate spatial resolution in azimuth and elevation. N_{sub} : number of subjects from each database included in the present study. The LISTEN database consists of the 49 subjects freely available on the IRCAM website (LISTEN-V1) and of 35 subjects measured later with an increased spatial resolution in azimuth (LISTEN-V2). Measurements for the ARI database have been performed under semi-anechoic conditions and because of measurement artifacts, only 10 subjects have been retained and the spatial resolution in elevation has been decreased to 10 °.

	Max	ITD	Interaural distance			
Animal	LF	HF	Tax. models	Reported	Acoustical	
Rat	$165~\mu \mathrm{s}$	134 μs	2.7 cm	$2.96~\mathrm{cm^1}$	$3.78~\mathrm{cm}$	
Rabbit	$319~\mu \mathrm{s}$	$246~\mu \mathrm{s}$	$3.2~\mathrm{cm}$	$5.6~\mathrm{cm^2}$	$8.02~\mathrm{cm}$	
Guinea pig	$242~\mu \mathrm{s}$	$184~\mu \mathrm{s}$	$3.35~\mathrm{cm}$	$4.94~\mathrm{cm}^3$	$5.02~\mathrm{cm}$	
Chinchilla	$293~\mu \mathrm{s}$	$240~\mu \mathrm{s}$	$3.9~\mathrm{cm}$	$3.6~\mathrm{cm^4}$	$7.68~\mathrm{cm}$	
Cat	$335~\mu \mathrm{s}$	$276~\mu \mathrm{s}$	$5.2~\mathrm{cm}$	$5.6~\mathrm{cm}^5$	$5.44~\mathrm{cm}$	
Macaque	$393~\mu \mathrm{s}$	$310~\mu \mathrm{s}$	$7.0~\mathrm{cm}$	$10.4~\mathrm{cm}^6$	$8.36~\mathrm{cm}$	

Table II: Overview of the animal ITD data. Maximal ITDs measured in low and high frequencies for the animal HRTFs. Interaural distances are the distances measured between the ear canal entrances of the taxidermized models (Tax. models), or the value as reported in previous studies (Reported), or twice the acoustical head radius (Acoustical, estimated from ITDs). References: ¹(Koka et al., 2008), ²(Kim et al., 2010), ³(Greene et al., 2014), ⁴(Lupo et al., 2011), ⁵(Roth et al., 1980), ⁶(Spezio et al., 2000).

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762 Figure 8 Animal ITDs in the horizontal plane, for 24 positions around the head (sepa-763 rated by 15°). Top: line color code; front positions, solid lines; back, dashed 764 lines. (a) Rabbit, (b) Guinea pig, (c) Chinchilla, (d) Cat, (e) Rat, (f) Macaque. 24

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