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Constraints on modified gravity from Planck 2015: when the health of your theory makes the difference.

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We use the effective field theory of dark energy (EFT of DE) formalism to constrain dark energy models belonging to the *Horndeski* class with the recent Planck 2015 CMB data. The space of theories is spanned by a certain number of parameters determining the linear cosmological perturbations, while the expansion history is set to that of a standard Λ CDM model. We always demand that the theories be free of fatal instabilities. Additionally, we consider two optional conditions, namely that scalar and tensor perturbations propagate with subluminal speed. Such criteria severely restrict the allowed parameter space and are thus very effective in shaping the posteriors. As a result, we confirm that no theory performs better than Λ CDM when CMB data alone are analysed. Indeed, the healthy dark energy models considered here are not able to reproduce those phenomenological behaviours of the effective Newton constant and gravitational slip parameters that, according to previous studies, best fit the data.

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I. INTRODUCTION

Understanding the origin of the present acceleration of the universe is a key challenge for cosmology. Recent progress in the analysis of the Cosmic Microwave Background [1] has significantly strengthened the case for the so called Λ CDM model, in which the Einstein field equations are supplemented by a cosmological constant, and the dominant matter specie is cold dark matter. Beside fixing with high precision the parameters of the standard model, in some cases to sub-percentage level, CMB data impose stringent constraints also on new non-standard physics. A large class of dark energy scenarios, in which cosmic acceleration results from a time varying dark energy fluid or modifications in the action of the gravitational field, are now shown to be in conflict with observational evidences [2, 3].

Beside its theoretical simplicity, a most compelling virtue of Λ CDM is its ability to reproduce the observed cosmic expansion history. However, well beyond the behaviour of the homogeneous Universe as a whole, there are specific aspects of the evolution of the structures it contains, such as the way density fluctuations grow and deflect photons via the lensing mechanisms, which still escape full understanding. Indeed the six-parameters Λ CDM “calibrated” by Planck at high redshift seems to predict that structures grow faster in time and are more abundant in space than actually measured by galaxy surveys at $z \lesssim 1$. This is illustrated by the fact that the *rms* density fluctuations on the scale of $8h^{-1}$ Mpc—extrapolated from CMB data under the assumption of a Λ CDM universe governed by general relativity—is larger than the value effectively measured by means of a variety of galaxy observables, such as cluster counts [4–6], lensing [1, 7–9] and redshift space distortions [10–15].

In this perspective, it is certainly interesting the indication of [16], confirmed by the following analysis of [17], of a tension between the Λ CDM model scenario for structure formation and the available data that could be explained in terms of modified gravity. As far as linear cosmological perturbations are concerned, it is possible to boil down the effects of most modified gravity models to two dimensionless functions [18, 19]: the ratio between the gravitational coupling (as it appears in the Poisson equation) and the Newton constant, $\mu_{\text{MG}} = G_{\text{eff}}/G_N$, and the ratio between the two Newtonian potentials $\gamma_{\text{MG}} = \Psi/\Phi$. Since we can neglect anisotropic stress at late times, both quantities reduce to unity in the standard model. Anomalous values of these quantities are effectively reported in [16], who found 3σ evidence against the Λ CDM model when low-redshift probes are combined with CMB.

It is certainly premature to interpret these results as indication that the standard model of cosmology is missing some fundamental degree of freedom. Indeed, a strong statistical discrepancy arises only when galaxy weak lensing or redshift space distortions data are included—but the latter probes still lack the understanding of systematics of CMB experiments (*e.g.* [20–22]). Nonetheless, there is much hope that statistical and systematic errors will be minimized and brought under control in the next generation of redshift galaxy surveys such as Euclid [23], DESI [24] or eBOSS [25]. While waiting for future observational confirmation or disproof, it is worth investigating which, among the many theoretical models, is best suited for making sense of the observed discrepancies.

Instead of using phenomenological parameterizations, we propose here to describe deviations from the standard scenario directly in terms of “constitutive parameters” of alternative gravitational theories. This is made possible by a formalism that allows to describe disparate theoretical models of DE in a unified language. The *effective field theory of dark energy* (EFT of DE), at least in its minimal version, allows to explore all dark energy and modified gravity models that contain one additional scalar degree of freedom [26–33] (see [34–36] for a numerical implementation of

this formalism). Adding another scalar [37] or a non-minimal coupling dark energy-dark matter [38] is also relatively natural in this framework.

In this work we use EFT of DE to explore which modified gravity models are compatible with CMB temperature, polarisation and lensing power spectra. For definiteness, we will limit our analysis to those models that give perturbation equations containing up to two derivatives (*Horndeski* models [39], that can be seen as generalizations [40, 41] of *galileon* models [42]). Our goal is twofold. On the one hand, we want to single out specific MG models, in the Horndeski class, that are compatible with data and ultimately assess, via a Bayesian analysis of their evidence, whether these models are more likely than the standard picture. By doing this we aim at reproducing and extending preliminary analyses and results already presented in [16, 35, 43]. On the other hand, the novelty of the paper is that we disentangle in our analyses the constraining power of data from that of the theory, *i.e.* we highlight which portion of the parameter space spanned by non-standard theory is excluded not because of tension with observations, but because no healthy physical model is allowed there. We clearly show that the theory constraining power greatly helps in reducing the volume of the multidimensional parameter space that is statistically explored, as [44, 45] suggested.

The paper is organised as follows. In Section II we recall the main elements of the EFT formalism and we describe the parametrization we adopt. In Section III the method of analysis and the datasets are explained. In Section IV we present the results in the space of parameters. In Section V we show some results directly in the space of observables. In Section VI we draw our conclusions.

II. EFT FORMALISM AND PARAMETRIZATION

The effective field theory of dark energy allows to describe a vast range of dark energy models by using a limited number of time dependent couplings [26–31]. In particular, here we focus on the large class of theories containing up to one scalar degree of freedom in addition to the metric field, and up to two derivatives in the equations of motion—commonly defined as Horndeski theories. Upon use of the Friedmann equations, the relevant couplings can be reduced to a minimal set of truly independent functions and the split between background expansion history and perturbation quantities becomes complete [44–48]. While there is now a consensus on the power and the advantages of this formalism, there is no universal agreement on the conventions for the coupling functions yet. Here we use those of [44, 45], that maintain a more direct link with the underlying theories, with respect to those of Ref. [46, 47]. For a dictionary between the two notations we refer the reader to App. B of Ref. [48].

A. Background expansion history

One of the main advantages of the EFT formalism is the possibility of treating cosmological perturbations independently of the expansion history. As far as the latter is concerned, we fix the geometry of the Universe to that of a spatially flat Λ CDM model. This is fully consistent with the present observational status of the equation of state parameter [1, 2, 49]. The Hubble rate $H(z)$ as a function of the redshift is thus given, at late times, by

$$H^2(z) = H_0^2 [\Omega_m^0(1+z)^3 + 1 - \Omega_m^0] . \quad (1)$$

The only free parameter here is Ω_m^0 : today’s fractional matter density as inferred by geometrical probes of the background expansion history (e.g. by fitting the luminosity distance-redshift relation of supernovae data).¹

B. Non-minimal couplings: perturbation sector

In order to completely specify the perturbation sector we need three functions of the time, corresponding to the three non-minimal couplings: $\mu(t)$, $\mu_3(t)$ and $\epsilon_4(t)$. Along the $\mu(t)$ direction in the coupling space we find Brans-Dicke (*BD*)-type theories, while μ_3 , appears in cubic galileon- and Horndeski-3 theories. They are both parameters with mass dimensions, typically of order Hubble. On the other hand, ϵ_4 is a dimensionless order-one function of the time

¹ Indeed, by exploiting the *dark degeneracy* discussed *e.g.* in [44, 45, 51, 52], one could also consider an interesting mismatch between the actual, physical amount of dark matter (Ω_m^0) and the one inferred *geometrically* from the expansion history (x_0) by the Friedmann equations. In [44, 45], such mismatch was encoded in a parameter κ different than unity. Here we simply set $\Omega_m^0 = x_0$ and we leave testing this possibility for future work.

present in galileon/Horndeski 4 and 5 Lagrangians.² The reader familiar with the formalism will notice that we do not consider the function $\mu_2(t)$, which only affects the sound speed of the scalar fluctuations and that we thus set to zero. In summary, the background and perturbation sectors are characterized by one parameter and three functions of the time:

$$\{\Omega_m^0, \mu(t), \mu_3(t), \epsilon_4(t)\}. \quad (2)$$

In order to specify the time dependence of the couplings, it is convenient to promote the fractional matter density of the background to a time variable for the late Universe

$$x \equiv \frac{\Omega_m^0}{\Omega_m^0 + (1 - \Omega_m^0)(1 + z)^{-3}}. \quad (3)$$

In fact, x detaching from 1 triggers the rising of the recent dark energy dominated phase. It seems thus natural to parametrize the time behaviour of the coupling functions in (2) with the following expansion:

$$\mu(x) = (1 - x) \left[p_1 + p_1^{(1)} (x - \Omega_m^0) \right] H(x), \quad (4)$$

$$\mu_3(x) = (1 - x) \left[p_3 + p_3^{(1)} (x - \Omega_m^0) \right] H(x), \quad (5)$$

$$\epsilon_4(x) = (1 - x) \left[p_4 + p_4^{(1)} (x - \Omega_m^0) \right], \quad (6)$$

where the p_i are order-one coefficients that we want to constrain with our analysis. The above ansatz guarantees that the coupling functions go to zero at early times, and that all modified gravity effects are linked to the latest, dark energy dominated phase.

However, even with the non-minimal couplings switched off, dark energy could be persistent at very early times directly, in the energy budget of the universe. Since we are fixing the expansion history to Λ CDM, the only way for this to be the case is that its equation of state asymptotes to zero, thereby mimicking dark matter at the level of the background. In order to avoid this possibility, as explained in [45], we impose a constraint between the p_i parameters,

$$p_1^{(1)} = \frac{p_1 \log(\Omega_m^0) - 6 \log(1 + (1 - \Omega_m^0)p_4)}{1 - \Omega_m^0 + \Omega_m^0 \log(\Omega_m^0)}. \quad (7)$$

C. Viability conditions

The theory that we are describing contains one scalar and two tensor degrees of freedom. The viability conditions that we demand at any time is that such degrees of freedom are not affected by ghosts or gradient instabilities. A gradient term appearing in the quadratic Lagrangian for the fluctuations with the wrong sign would imply exponential growth of Fourier modes of any comoving momentum k . The wrong sign in the *time* kinetic term, on the other hand, would lead to “*ghost-like*” classical and quantum instabilities that are at least as serious [50]. As we will show, these conditions alone significantly restrict the parameter space that we are exploring. On top of these basic requirements that are always enforced, we consider in our analysis other two optional conditions, namely that the speed of propagation of scalar modes and tensor modes be not superluminal. Apart from the known causality problems related with the possibility of sending a signal faster than light, superluminal propagation has been argued to be incompatible with a consistent Lorentz invariant UV completion [54]. In summary, in this paper we will consider three main viability conditions:

$$\text{stable :} \quad \text{absence of ghosts and gradient instabilities (always enforced),} \quad (8)$$

$$\text{stable \& } c_s < 1 : \quad \text{scalar propagation speed not superluminal,} \quad (9)$$

$$\text{stable \& } c_s < 1 \ \& \ c_T < 1 : \quad \text{the above \textit{and} tensor propagation speed not superluminal.} \quad (10)$$

² This parameter is responsible for the anomalous gravitational wave speed $c_T \neq 1$ in theories of modified gravity, *i.e.* $c_T^2 = 1/(1 + \epsilon_4)$. In the paper [53], by using binary pulsar data, its present value, $\epsilon_4(t_0)$, has been constrained to more than 10^{-2} level.

D. MGCAMB with the EFT of DE parameters.

In our analysis, instead of solving the full set of linear perturbation equations for the couplings defined in (4)-(6), we encode the modifications of gravity in two functions of the time, μ_{MG} and γ_{MG} , following the approach implemented in the MGCAMB code [18, 55] and properly updating and modifying the public package³. This method has the remarkable advantage of allowing a simpler numerical implementation while keeping a clear mapping between the μ_{MG} - γ_{MG} functions and the underlying EFT theory.

Although MGCAMB works in synchronous gauge, the form of the equations and the definition of the relevant quantities look more transparent in Newtonian-gauge, defined by the perturbed metric taking the form

$$ds^2 = -(1 + 2\Phi)dt^2 + a^2(t)(1 - 2\Psi)\delta_{ij}dx^i dx^j. \quad (11)$$

The package MGCAMB evolves the standard conservation and Euler equations for the matter fields, implemented with other two equations, namely,

$$-\frac{k^2}{a^2}\Phi = \mu_{MG}(t, k) \frac{3H^2}{2} \left[\Delta + 3 \left(1 + \frac{p}{\rho} \right) \sigma \right], \quad (12)$$

$$\frac{k^2}{a^2} [\Psi - \gamma_{MG}(t, k)\Phi] = \mu_{MG}(t, k) \frac{9H^2}{2} \left(1 + \frac{p}{\rho} \right) \sigma. \quad (13)$$

In the above, $\Delta = \delta - 3H(\rho + p)v$ is the comoving density perturbation, σ the anisotropic stress, negligible at late times, and μ_{MG} and γ_{MG} are generally functions of both the time t and the comoving scale k . Note that in the differential equations integrated by MGCAMB the scalar degree of freedom is absent, so its effects must be encoded in these two functions. In the high- k limit, that is natural to consider as we are interested in models that produces the cosmic acceleration at late-time, these functions maintain only their dependence on t . In the EFT of DE formalism, they have been derived and discussed, *e.g.*, in [29, 44–47],⁴ In our analysis, we have fed MGCAMB with the EFT expressions of μ_{MG} and γ_{MG} quoted in the Appendix in eqs. (A4) and (A5). One can verify that, with our parameterization (4)-(6), (7), μ_{MG} and γ_{MG} go to one at early times.

It is natural to ask which is the level of accuracy on the CMB spectrum of this approximate approach with respect to the integration of the full set of linear equations. In Ref. [35] it is shown a comparison between MGCAMB and EFTCAMB in the particular case of $f(R)$ theories. Not surprisingly, the error increases at low multipoles l and for higher deviations from general relativity. By extrapolating to the present case we estimate an error of at most 10% at $l = 2$. Considering also that our posteriors are mainly driven by the viability conditions (see Secs. IV and V below), we conclude that our results can only be mildly affected by this approximation.

The effects of the different EFT parameters on temperature and lensing CMB power spectra are depicted in Fig. 1.

III. METHOD OF ANALYSIS AND DATA

The aim of the analysis is to simultaneously evaluate the constrains on the set of standard cosmological parameters $\Omega_b h^2$, $\Omega_c h^2$, θ , τ , n_s , A_s , that define a flat universe with a Λ CDM background history, plus the p_i coefficients that encode the dark energy/modified gravity effects, as described in (4)-(6). In this respect, notice that $\Omega_b h^2$ is the baryon energy density, $\Omega_c h^2$ is the cold dark matter energy density, θ is the ratio of the sound horizon to the angular diameter distance at the decoupling time, τ is the optical depth to reionization, n_s is the scalar spectral index and A_s is the amplitude of the primordial scalar perturbation spectrum, at $k = 0.05 Mpc^{-1}$. Deviations from standard cosmology in the neutrino sector are not considered in the following analysis. Therefore, the relativistic number of degrees of freedom parameter is fixed to $N_{eff} = 3.046$ and the total neutrino mass to $\sum m_\nu = 0.06eV$. Notice that the Ω_m^0 parameter in (2) corresponds to $(\Omega_b h^2 + \Omega_c h^2)/h^2$.

In this analysis, we focus in this analysis on the most recent CMB data from the Planck experiment [58, 59]. In particular we include in our datasets the temperature high- l power spectra from the 100, 143, 143x217 and 217 GHz channels (PlikTT likelihood) and the temperature and polarization spectra at low- l described in [59], that includes Planck observations at low and high frequency channels, WMAP observations between 23 and 94 GHz [60] and

³ <http://www.sfu.ca/~aha25/MGCAMB.html>

⁴ When using the results of [45], one should keep in mind that, in that notation, $\mu_{MG} = \kappa G_{eff}/G_N$.

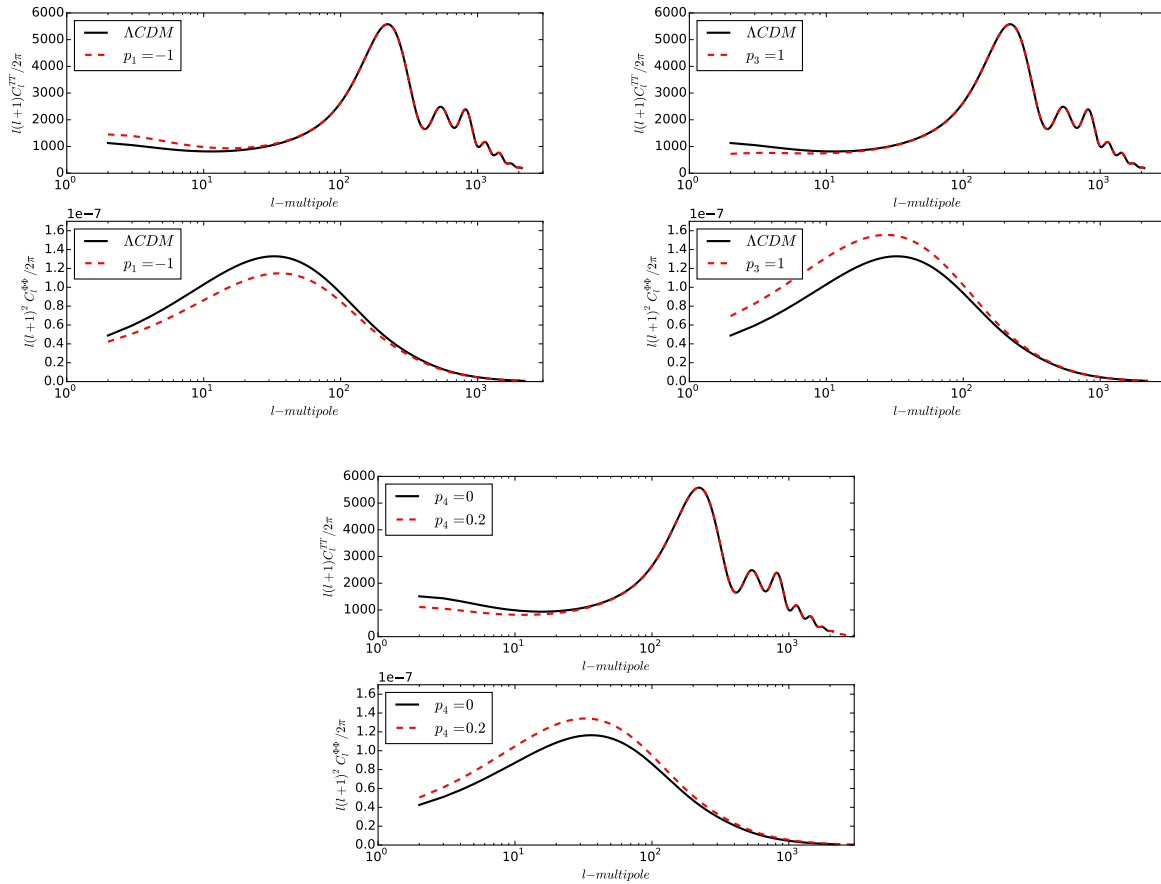


FIG. 1: Effects of the EFT couplings on the temperature and lensing CMB spectra. For the top figures we have switched on, in turn, the p_1 or p_3 parameter while keeping the others to zero. For the bottom figure, we have switched on the p_4 parameter, while keeping $p_3^{(1)}$, $p_4^{(1)}$ to zero and p_1 and p_3 fixed in a stable configuration. The signs have been chosen on the basis of stability. Note that a negative p_1 tends to be compensated by a positive p_3 , which explains the degeneracy of Fig. 4 below, second panel. On the other hand, the effects of p_3 show up only at very low l , which explains why the likelihood is not very sensitive to this parameter (see Fig. 3 and Panels 1 and 3 of Fig. 4).

measurements at 408MHz from [61]. We also include the information on CMB lensing from the trispectrum. We refer to this combination of datasets as PLANCK.⁵

As already explained in Sec. IID, we explore the constraints on this set of parameters by computing the CMB observables with a MGCAMB code properly modified to include the EFT parametrization.

The public available CosmoMC package [62, 63], version July2015, is used to explore the parameter space with the Monte Carlo Markov Chain method. The Gelman and Rubin method is used to set the converge of the chains, requiring $R - 1 < 0.03$.

We consider two different extensions of the standard model. The *3D*-Model, that corresponds to a minimal extension with one free parameter for every non-minimal coupling. And the *5D*-Model that, by adding a term in the Taylor expansion (4)-(6) of the coupling functions, gives more freedom to the functional space. In summary, the two models

⁵ Notice that the high- l polarization dataset is not included as it is insensitive to the EFT parameters and it does not improve the constraints.

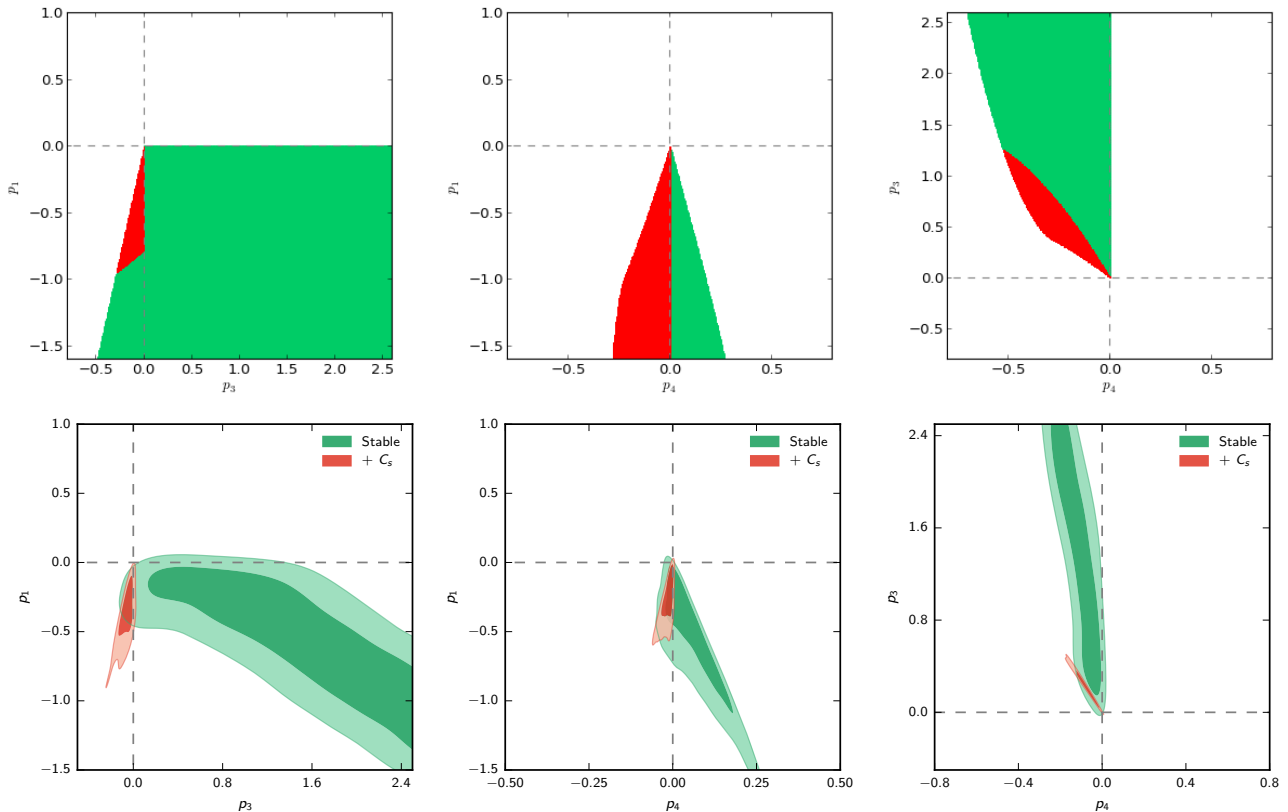


FIG. 2: We illustrate here the role of the viability conditions in shaping the EFT parameter constraints, for two possible scenarios: stable (green), stable & scalar subluminality (red). Top: from left to right, viability regions for $p_4 = 0$, $p_3 = 0$, $p_1 = 0$, and where we have fixed $\Omega_m^0 = 0.27$. Bottom: two-dimensional posteriors for the corresponding pairs of EFT parameters when considering the PLANCK dataset. We marginalize over the cosmological parameters. For visualisation clarity, the EFT parameters not shown in each plot are set, in turn, to zero. The viability regions are thus different from those of the 3D case presented below in Fig. 4. Viability conditions tightly reduce the width of the parameter space, data further reduce the allowed regions. Interestingly the Λ CDM case is always at the corner of the viable space.

are characterized by the following sets of EFT free parameters:

$$3D\text{-Model} : \quad \{p_1, p_3, p_4\} \quad (14)$$

$$5D\text{-Model} : \quad \{p_1, p_3, p_4, p_3^{(1)}, p_4^{(1)}\}. \quad (15)$$

In the first model $p_3^{(1)}$ and $p_4^{(1)}$ are set to zero.

IV. RESULTS: CONSTRAINTS ON EFT PARAMETERS

A. The role of viability conditions

To begin, let us emphasise one of our main results: the main role of the theoretical viability conditions in determining the parameter constraints. In Fig. 2 we plot the two-dimensional posterior PDF of the *model 3D* (bottom panels) and we compare it with the areas delimited purely by the viability requirements (top panels), *i.e.*, without data. To make the relation between regions of viability and posteriors clearer, here we do not marginalize over the third EFT parameter but only on the six Λ CDM ones, fixing in turn one of the three p_i parameters to zero. These plots show, on the one hand, the important role of viability conditions in shaping the posterior distributions. Another important feature highlighted here is that within the space of theories considered, and with the additional constraint of reproducing the same expansion history as Λ CDM, setting all couplings to zero lies at the edge, more precisely on

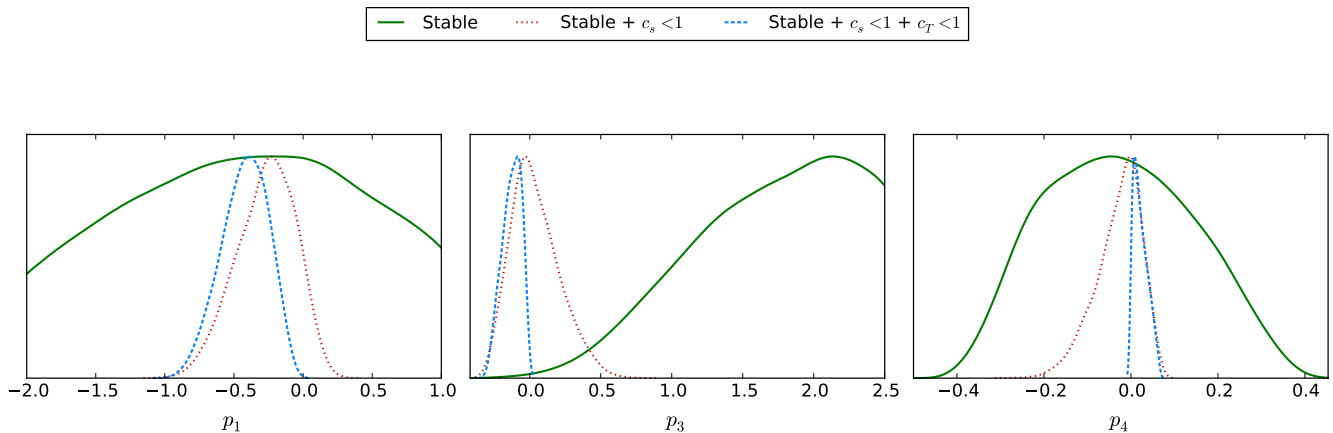


FIG. 3: Planck constraints on the $3D$ -model, the minimal EFT extension of the six-parameter Λ CDM model. The marginalised, posterior distribution for p_1 , p_3 and p_4 is shown. The likelihood analysis is carried out by also letting vary the six parameters of the standard Λ CDM model and the foreground parameters. The constraining power of theoretical priors is also shown: The solid line shows the posterior obtained after removing the portion of the parameter space in which unstable theories live. Likelihood intervals obtained by requiring that scalar perturbations, in stable theories, propagate at subluminal speed are shown by dotted lines. Dashed lines show results when also tensor perturbations are forced to propagate at subluminal speed.

a tight corner, of the allowed parameter space. (see also Figs 1 and 2 of Ref. [44] on this). In other words, Λ CDM is an extremal among all modified gravity models with the same equation of state $w = -1$. This implies that, when we sample the theory space by means of the Markov chain algorithm, the chance of hitting Λ CDM model is extremely small. In practice, the standard Λ CDM model is never reached by the chain. What typically happens is that the χ -squared minimisation tends to go, from a given stable point, towards the origin of the parameter space (Λ CDM). However, while approaching Λ CDM, the allowed region becomes a tight throat, and finding stable theories becomes more and more difficult. As a result, the posteriors are often decentered from Λ CDM, without necessarily implying a better fit of the data (*i.e.* see 3). In this theory landscape, Λ CDM is truly an extremal among all models with the same background expansion history.

B. The $3D$ -Model

In Fig. 3 and 4 we present constraints on the minimal EFT extension of the standard model of cosmology ($3D$ model). The most prominent feature visible in the one-dimensional posteriors of p_1 , p_3 and p_4 in Fig 3 is that the theoretical requirement of subluminality (for both scalar and tensor modes) significantly narrows the posterior interval of the EFT parameters. The theoretical viability conditions are thus powerful instruments that complement and increase the discriminatory power of data. Specifically, the main effect of the subluminality prior on p_1 and p_4 parameters is a reduction of the distribution width around the null value, while the net effect on p_3 is instead to shift it towards lower values, compatible with the absence of modified gravity signals.

The amplitude of the posterior intervals suggest that the best fitting EFT parameters are small, of order 1, thus confirming the reliability of the series expansions (4)-(6) in featuring the essential scaling of the coupling functions $\mu(t)$, $\mu_3(t)$ and $\epsilon_4(t)$. While the one dimensional PDF peaks at around zero for both p_3 and p_4 , a negative value of p_1 is preferred under any viability conditions. This would apparently imply that the C_l data are best fitted by non-standard gravity models predicting larger temperature fluctuations than Λ CDM at low l (see Fig 1). This fact seems thus at variance with observational lack of power at low l multipoles in the CMB TT spectrum. The paradox is easily solved by inspecting the 2-dimensional posteriors of the parameters. Indeed, Fig. 4 clearly shows that the EFT parameter p_1 is strongly degenerate with p_4 . The observed anti-correlation results from the fact that both excite the same range of multipoles of the temperature power spectrum (see Fig 1). In other terms, an increase in power generated by a negative p_1 is mostly compensated by the suppression mechanism activated by a positive value of p_4 .

As for the goodness of the fit and its implications for models selection, Table I shows that the observed decreasing in the χ^2 value associated to the best fitting EFT model is not significant, *i.e.* it is not enough for the best fitting *model 3D*, which has 3 more degrees of freedom than the standard model of cosmology, to be statistically preferred. Additionally, Table I shows that the best fitting value of the Λ CDM parameters are close, and statistically indistinguishable, from those of the reference Λ CDM model calibrated by Planck.

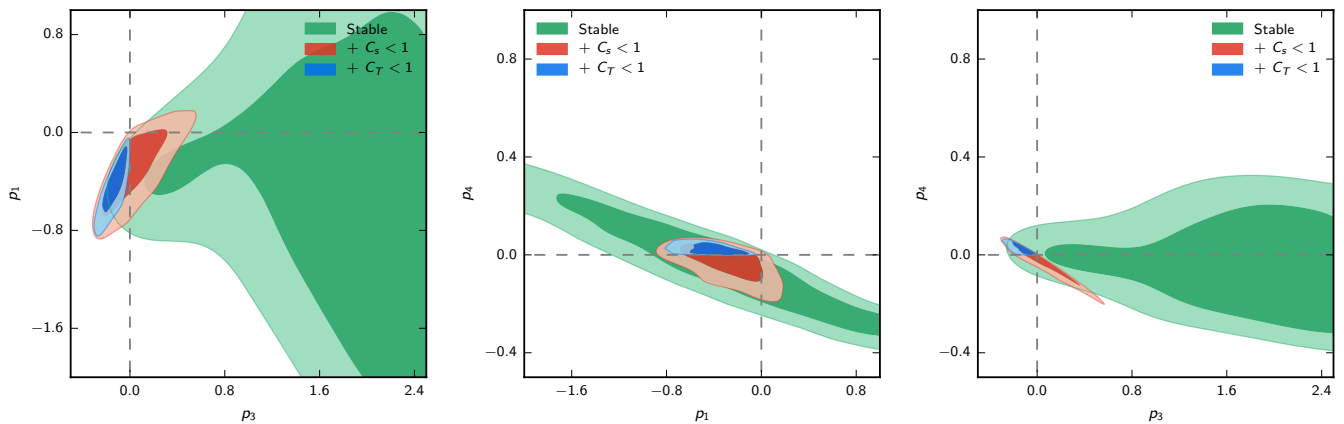


FIG. 4: Planck constraints on *model 3D*, the minimal EFT extension of the six-parameter Λ CDM model. The 2D, marginalised, posterior distributions for the zero-*th* order EFT parameters p_1 , p_3 and p_4 , are shown. Marginalisation is over the remaining EFT parameters and the six Λ CDM parameters shown in Table I. Contours display the 68% and 95% c.l.. Different colours corresponds to the three different viability scenarios explained in II C.

The bi-dimensional projected posterior PDF of the *model 3D* parameters is shown in Fig. 4 for the three combinations of parameters. Here, when displaying two EFT parameters, we are marginalizing over other parameters. This explains the differences between Fig 2 and Fig 4. This picture shows that asking for subluminal velocities considerably narrows the confidence regions. Interestingly, the viability priors not only impose tighter constraints as compared to those derived from cosmological measurements alone, but they also compensate both the statistical insensitivity and the parameter degeneracy.

We remark that among the three EFT parameters, p_3 is the least constrained. Linear perturbation equations which describe the growth of the matter distributions in the universe are weakly sensitive to this parameter that controls the emergence of galileon/Horndeski-3 type models in our modified gravity landscape. This result is the consequence of what we saw in Fig 1, that is, the amplitude of the linear power spectrum of temperature fluctuations are mostly sensitive to p_3 only on very large cosmic scales (low l), where CMB data are fewer and affected by large statistical and systematic noise.

C. EFT and the other (standard) parameters of Λ CDM

Fig. 5 shows that, contrary to naive expectations, adding extra dimensions to the dark energy parameter space does not shift nor enlarge significantly the confidence interval of the six Λ CDM parameters measured by Planck. This is due to the fact that the p_i parameters do not show appreciable degeneracy with the Λ CDM parameters. In other terms, CMB measurements of the 6-parameters of the Λ CDM model are robust against the inclusion of external couplings controlling the perturbation sector. Our formalism, which displays a clear separation between expansion rate and perturbation sectors, allows one to check this very clearly. The 6 parameters of the Λ CDM model are essentially insensitive to small variations in the EFT parameters, in the sense that the centers of the Planck error bars are not offset, nor the interval of confidence degraded (Tab. I). Interestingly, the insensitivity to small variations in the EFT parameters is not an harmful issue. Indeed, as Fig. 5 shows, physical priors on the viability of alternative gravity models help in beating down the lack of resolution on EFT parameters, thus reducing the uncertainty associated to their estimate.

D. The 5D model

The absence of any 3-parameters EFT model performing better than Λ CDM, together with the above remarks on the statistical power of the viability constraints, suggest to extend our parameter space by including two additional degrees of freedom, represented by the terms $p_3^{(1)}$ and $p_4^{(1)}$ in Eqs. (5) and (6). By this choice, the parameterization becomes more flexible and, in principle, able to capture subtler time behaviors of the EFT coupling functions. This, in turn, should allow one to explore the space of Horndeski theories in a finer way, and eventually single out models,

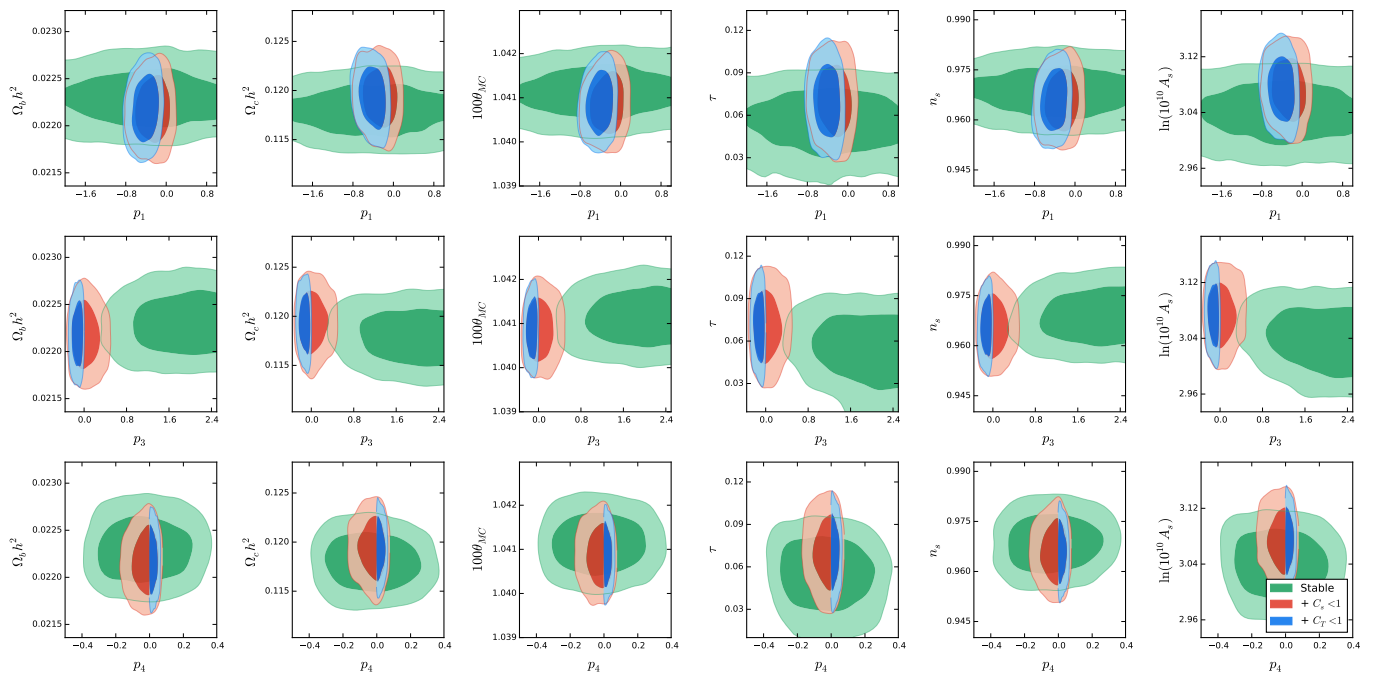


FIG. 5: The bidimensional, marginalised, posterior PDF projected onto various planes defined by the zero- th order EFT parameters p_1 , p_3 , p_4 , and the 6 parameters of the Standard Λ CDM model is shown.

if any, that outperform the standard one. Results of this likelihood analysis are displayed in Fig. 6 and in the last column of Table I.

As expected, EFT parameters are somewhat less constrained when the $5D$ model is considered, since we are dealing with more degrees of freedom. Nevertheless, the contours in the first row of Fig. 6 show that the degeneracies between the 0^{th} -order parameters are unaffected by the additional parameters. Also, no remarkable degeneracies are evident between the 0^{th} -order parameters p_3 , p_4 and the 1^{st} -order parameters $p_3^{(1)}$, $p_4^{(1)}$. This implies that the $3D$ model already catches the main features of the modifications of gravity. However, the enlargement of the constraints completely washes out the indication of a preferred negative p_1 . As a consequence, no signals of new physics emerge, also within this enlarged parameter space.

Finally, we note that in $5D$ the Markov chain could not find stable region to be explored when all viability conditions were imposed—this is the reason why no blue contour is displayed in Fig. 6. This further shows the difficulty of finding stable theories around Λ CDM. Since such a difficulty is a “volume effect” (*i.e.*, roughly, the smallness of the quantity *volume of stable theories/total volume*), it is not surprising that it can be made worse by going to higher dimensions in the theory space.

V. RESULTS: CONSTRAINTS ON COSMOLOGICAL OBSERVABLES

A complementary approach consists in constraining not the space of theories, as we did above, but quantities that are closer to direct cosmological observables. To this purpose, we consider the pair of functions $\mu_{\text{MG}}(t)$ (the effective Newton constant) and $\gamma_{\text{MG}}(t)$ (the gravitational slip), as defined in Eqs. (17) and (18). Indeed, these are the cosmological functions that are directly constrained by most observational probes. Any deviations from the unity of these functions, at any redshift, is notably considered a smoking gun for modified gravity.

Interestingly, the Planck Collaboration recently highlighted that the combination of CMB and redshift-space distortions (RSD) and/or galaxy weak-lensing data (WL) indicate a deviation from the standard value, at about 3 sigma, of both these functions at redshift $z = 0$ (see Fig. 14 of Ref. [16]). Namely, values of $\mu_{\text{MG}}(0)$ lower than 1 and values of $\gamma_{\text{MG}}(0)$ higher than 1 seem to be preferred by this combination of probes. This result is largely driven by the preference of these probes for a *rms* density fluctuations on the scale of $8h^{-1}$ Mpc lower than expected in standard gravity [7, 12–14]. Whether these are just unidentified systematics or real physical indications, it is worth trying to see if these results are compatible with any healthy theory of the Horndeski class.

The main methodological difference between our approach and that adopted in [16] is the way in which the time

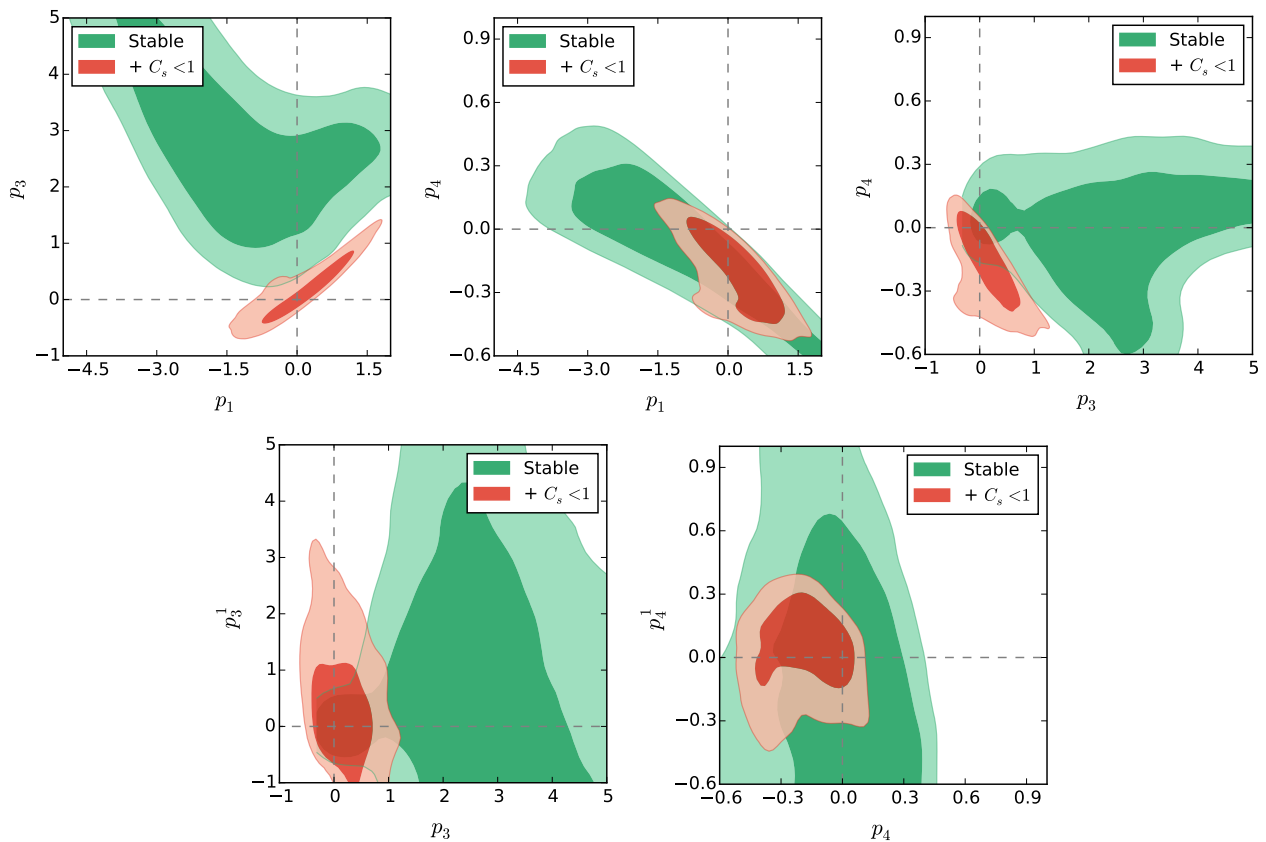


FIG. 6: Planck constraints on the $5D$ model, the maximal EFT extension of the six-parameter Λ CDM model explored in this paper. The 2D, marginalised, posterior PDF for all the free fitting parameters in Eqs. (4)-(6) is shown. Marginalization is over the remaining EFT parameters of model $5D$ and also over the six Λ CDM parameters shown in Tab. I. The likelihood contours display the 68% and 95% c.l.. In these plots the blue contours are not displayed because the Markov chain was virtually unable to find theories satisfying *all* viability conditions.

scaling of the function μ_{MG} and γ_{MG} is parameterised. There, two phenomenological behaviors are chosen for these functions: one in which the time variation is proportional to the dark energy density (dark-energy related parameterisation) and the other in which the variation is proportional to $1 - a$ (time-related parameterisation). In both cases, μ_{MG} and γ_{MG} evolve independently of one another. Here, the expressions of μ_{MG} and γ_{MG} are theoretically determined within the context of the EFT theory and they can be tracked back to underlying physical healthy theories. Remarkably, such functions do not have a generic behaviour but, rather, they present definite features and specific correlations, especially when all viability conditions are used to select models [44, 45].

The results of our analysis are presented in Fig. 7 and show the importance of not neglecting viability conditions in phenomenological constraints. First we note that there is no stable EFT model that lives in the portion of the space of observables characterised by a negative value of $\mu_{\text{MG}} - 1$ today. Therefore a large part of the region allowed by phenomenological models in [16] is *a-priori* excluded as unphysical. More importantly, the best-fitting region arising by combining CMB and RSD and/or WL lays in the unstable region. That means that, even if confirmed by following experiments, that signal do not corresponds to the effects of any viable Horndeski theory.

Even more stringent conclusions emerge if subluminal propagation speed of scalar and tensor perturbations is required. In this case we find an additional tight constrain on the present value of γ_{MG} that is strictly lower than 1 in viable theories.

The healthy EFT models that satisfy to the most stringent set of our conditions (no ghosts and gradient instabilities, subluminal propagation speed for scalar and for tensor perturbations) are indeed characterized by a positive value of $\mu_{\text{MG}} - 1$ and a negative value of $\gamma_{\text{MG}} - 1$. As a result, the favoured values of those parameters are pulled back towards the Λ CDM region, without no compelling evidence for any better description of data than that offered by the Λ CDM model.

The fact that Λ CDM seems to live on the border of the 2σ confidence level of the most constrained posterior likelihood (blue region in Fig. 7) is just an artefact due to the sampling behaviour when the parameter space is cut by

Parameters	Λ CDM	3D			5D
		Stable	Stable & $c_s < 1$	Stable & $c_s < 1$ & $c_T < 1$	Stable & $c_s < 1$
$\Omega_b h^2$	0.02224 ± 0.00023	0.02231 ± 0.00024	0.02217 ± 0.00022	0.02219 ± 0.00023	0.02215 ± 0.00023
$\Omega_c h^2$	0.1186 ± 0.0020	0.1180 ± 0.0021	0.1194 ± 0.0019	0.1194 ± 0.0019	0.1198 ± 0.0020
100θ	1.04101 ± 0.00047	1.04113 ± 0.00049	1.04087 ± 0.00044	1.04089 ± 0.00047	1.04084 ± 0.00047
τ	0.066 ± 0.017	0.060 ± 0.020	0.075 ± 0.015	0.073 ± 0.016	0.073 ± 0.016
n_s	0.9675 ± 0.0060	0.9687 ± 0.0061	0.9656 ± 0.0058	0.9657 ± 0.0059	0.9650 ± 0.0059
$\log(10^{10} A_s)$	3.062 ± 0.030	3.050 ± 0.039	3.082 ± 0.027	3.078 ± 0.029	3.080 ± 0.029
p_1	—	$-0.43^{+0.95}_{-0.21}$	$-0.28^{+0.17}_{-0.20}$	$-0.42^{+0.21}_{-0.17}$	$0.10^{+0.58}_{-0.37}$
p_3	—	> 0.13 (95% c.l.)	0.04 ± 0.17	$-0.12^{+0.08}_{-0.06}$	$0.13^{+0.28}_{-0.40}$
p_4	—	$-0.03^{+0.16}_{-0.19}$	$-0.030^{+0.068}_{-0.035}$	$0.023^{+0.009}_{-0.023}$	$-0.18^{+0.28}_{-0.13}$
p_3^1	—	—	—	—	$0.41^{+0.39}_{-0.91}$
p_4^1	—	—	—	—	$0.03^{+0.18}_{-0.11}$
χ^2	11276.97	11276.22	11278.46	11278.62	11277.52

TABLE I: Constraints on the parameters for the 3D and 5D models, together with the six standard Λ CDM parameters (the notation for the latter is the standard one, see *e.g.* [1]).

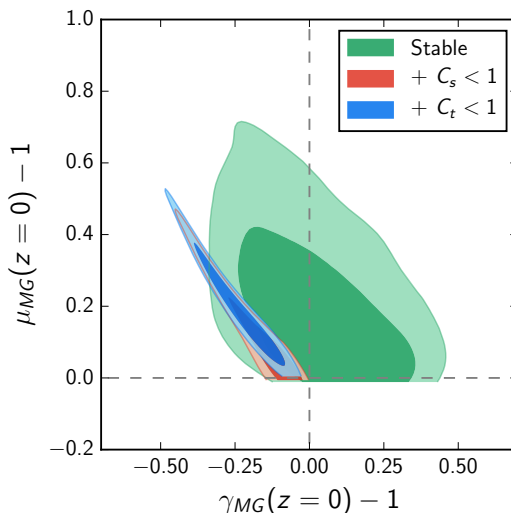


FIG. 7: 68 % and 95 % contour plots for the two parameters (μ_{MG} , γ_{MG}) obtained by evaluating Eqs. (A4) and (A5) at the present time using the minimal parameterisation of the 3D model.

viability conditions. As a matter of fact the stability regions for these models is a sharp corner of which the Λ CDM models occupies the vertex. This regions is thus virtually inaccessible by the Markov Chain.

The one-dimensional posteriors of μ_{MG} and γ_{MG} from PLANCK, when healthy conditions on the theories are imposed, are depicted in Fig 7.

Despite the larger contours, the same behaviour (value of $\mu_{MG} - 1$ close to positive and negative value of $\gamma_{MG} - 1$) is confirmed by the 5D-model.

VI. CONCLUSIONS

Exploring beyond the standard model of gravity in the quest for some yet missing physical mechanism that could explain cosmic acceleration relies on two premises: high quality astronomical data and flexible parametric scheme that can detect anomalous signals and, at the same time, can interpret them in terms of fundamental physics. A specific framework that achieves the latter goal is the effective field theory of dark energy. In this paper we constrain the EFT of DE operators by means of the Planck 2015 data. A key feature of this formalism is that it allows one to analyze the expansion history of the cosmic metric independently of the perturbation sector. We have exploited this possibility to set the EFT background to that of a Λ CDM geometry: as a matter of fact, most geometrical probes of

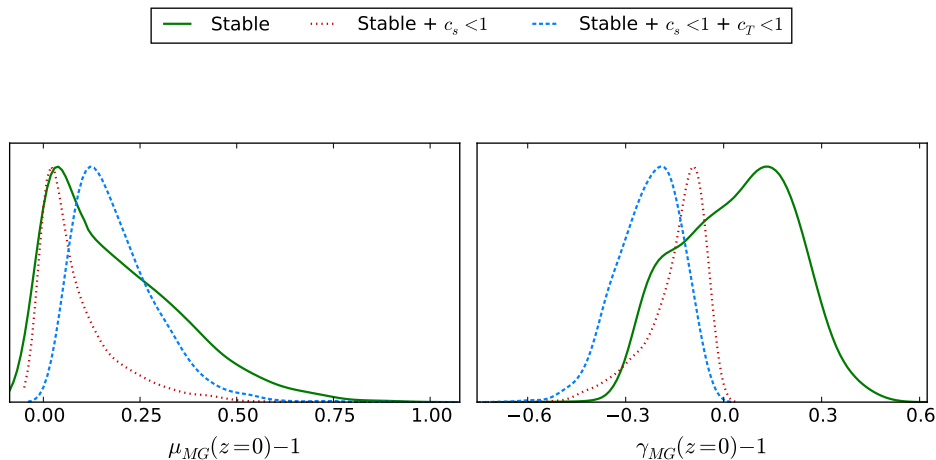


FIG. 8: Case 3D. Posterior distributions for the μ_{MG} and γ_{MG} parameters

cosmology are compatible with the standard Λ CDM expansion history.

The simple requirement that modified gravity theories do not violate fundamental physical principles such as causality and stability results in stringent constraints on the accessible regions of the EFT parameter space. Taken together, the ‘no-go’ regions excluded on theoretical grounds and the regions statistically excluded by CMB data, convincingly suggests that no scalar-field based extension of GR is more likely than the standard gravitational scenario. This result confirms and strengthens what already found by [16] on the basis of various purely phenomenological, and thus physically less justified, models.

A complementary line of attack, that gives further angle on the issue, consists of analyzing the “observables” μ_{MG} and γ_{MG} . When their redshift evolution is modelled in a purely phenomenological way, then the ensemble of our cosmological data constrain the local ($z \simeq 0$) value of these quantities to be $\mu_{MG} < 1$ and $\gamma_{MG} > 1$ (see *e.g.* [16]). Physically sound theories, however, never end up producing such values of μ_{MG} and γ_{MG} *today*. Fig. 8 shows that the value of G_{eff} for modified gravity theories not rejected by data, is, at present epoch never smaller than the Newton constant. Additionally, $\gamma_{MG}(t_0) - 1$ becomes negative as soon as the condition for subluminal propagation of perturbations is enforced.

Although we conclude that the models of dark energy/modified gravity considered here do not seem to be able to outperform predictions of the Λ CDM model, this does not mean that dark energy altogether cannot improve the fit to CMB data. For instance, we could consider scalar field models *beyond* Horndeski [48, 64], or models with more and/or different degrees of freedom than a scalar field. Also, some of our assumptions could be weakened, such as that of imposing no dark energy at early times, which leads to the constraint (7) among our parameters. The alternative would be that dark energy density does not become subdominant at early epochs. But since we are imposing the Λ CDM expansion history, this means that its equation of state must mimic non-relativistic matter at early times. Also, along the same “dark degeneracy” lined by [51, 52], we could consider models where the physical amount of dark matter today, Ω_m^0 , and the geometrical parameter entering the expression of the Hubble rate $H(z)$ as a function of the redshift are two distinct quantities. In the notations of [44, 45] this corresponds to considering $\kappa \neq 1$.

In an upcoming paper, while exploring along some of these directions, we will show results obtained by including in the analysis also observables extracted from low-redshift galaxy datasets.

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Appendix A: More formulas of the EFT formalism

Our couplings are implicitly defined by the following action written in unitary gauge [].

$$\begin{aligned}
S = S_m[g_{\mu\nu}, \Psi_i] + \int d^4x \sqrt{-g} \frac{M^2(t)}{2} \\
\left[R - 2\lambda(t) - 2\mathcal{C}(t)g^{00} + \mu_2^2(t)(\delta g^{00})^2 - \mu_3(t)\delta K\delta g^{00} + \right. \\
\left. \epsilon_4(t) \left(\delta K^\mu{}_\nu \delta K^\nu{}_\mu - \delta K^2 + \frac{{}^{(3)}R\delta g^{00}}{2} \right) \right]
\end{aligned} \tag{A1}$$

The above describes the background and the first order perturbation equations of the entire set of Horndeski theories. Beside the coupling functions, in the action there appears derived quantities, \mathcal{C} and λ , that can be identified roughly with the kinetic and potential energy density of dark energy. They can be calculated by applying the background Einstein equations [27]:

$$\mathcal{C} = \frac{1}{2}(H\mu - \dot{\mu} - \mu^2) - \dot{H} - \frac{\rho_m}{2M^2}, \tag{A2}$$

$$\lambda = \frac{1}{2}(5H\mu + \dot{\mu} + \mu^2) + 3H^2 + \dot{H} - \frac{\rho_m}{2M^2}. \tag{A3}$$

$$\mu_{\text{MG}}(t) = \frac{M^2(t_0)[1 + \epsilon_4(t_0)]^2}{M^2(1 + \epsilon_4)^2} \frac{2\mathcal{C} + \dot{\mu}_3 - 2\dot{H}\epsilon_4 + 2H\dot{\epsilon}_4 + 2(\mu + \dot{\epsilon}_4)^2}{2\mathcal{C} + \dot{\mu}_3 - 2\dot{H}\epsilon_4 + 2H\dot{\epsilon}_4 + 2\frac{(\mu + \dot{\epsilon}_4)(\mu - \mu_3)}{1 + \epsilon_4} - \frac{(\mu - \mu_3)^2}{2(1 + \epsilon_4)^2}}, \tag{A4}$$

$$\gamma_{\text{MG}}(t) = 1 - \frac{(\mu + \dot{\epsilon}_4)(\mu + \mu_3 + 2\dot{\epsilon}_4) - \epsilon_4(2\mathcal{C} + \dot{\mu}_3 - 2\dot{H}\epsilon_4 + 2H\dot{\epsilon}_4)}{2\mathcal{C} + \dot{\mu}_3 - 2\dot{H}\epsilon_4 + 2H\dot{\epsilon}_4 + 2(\mu + \dot{\epsilon}_4)^2}, \tag{A5}$$

where to simplify the notation we have defined with a circle some ‘‘generalized time derivatives’’,

$$\dot{\mu}_3 \equiv \dot{\mu}_3 + \mu\mu_3 + H\mu_3, \tag{A6}$$

$$\dot{\epsilon}_4 \equiv \dot{\epsilon}_4 + \mu\epsilon_4 + H\epsilon_4. \tag{A7}$$

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