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Heat source estimation in anisotropic materials

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ABSTRACT

The present paper is devoted to the determination of heat source dissipation from infrared thermographic measurements. Such procedure is mainly based on the heat diffusion equation provided by thermodynamics principles. Especially, this requires time and spatial derivation of temperature fields and the knowledge of the material thermal conductivity. This work intends to extend such classical procedure for isotropic materials to the anisotropic context. At first, we propose a comparative study of several filtering methods required for the data processing of noisy and discrete thermal acquisitions. In a second part, a transversely isotropic effective thermal conductivity tensor is estimated by means of a homogenization-based method. From these both results, a heat source application is presented in order to analyze damage phenomena in transversely isotropic CFRP submitted to tensile tests.

Keywords: Heat source Thermal analysis Thermomechanics Anisotropic conduction

1. Introduction

For experimental investigations, optical techniques offer a major advantage for studying deterioration mechanisms without disturbances associated to the measure itself. Real time recording and high sensitivity are also of great interest (see general discussions of [1,2]). Among these methods, InfraRed Thermography (IRT) allows promising prospects for the monitoring of dissipative processes [3]. This technique provides 2D measurement of the thermal radiation induced by deformation mechanisms inside the material and emitted at its surface.

Several works have shown that thermograms acquired by IRT during mechanical loading tests can be used to highlight and characterize in some way the damage evolution in composite materials ([4–7] for instance). Nevertheless, the temperature should not be considered as an intrinsic indicator since it can be influenced by heat exchanges with the surrounding and/or by heat diffusion inside the material itself. In that case, heat sources associated to thermoelastic coupling and dissipations appear as much more relevant demonstrations of internal processes. Generally, these sources are deduced from the thermodynamical background, and especially from the heat diffusion equation. This involves spatial and time derivation of experimental thermal fields and consequently data processing with filtering operations. Many existing studies based on such approach have been performed, mostly for

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fatigue loading, and above all for isotropic materials [8–13]. The latter condition clearly simplifies mathematical developments and reduces computational times.

The present study aims at examining these calorimetric effects with account of anisotropic conduction. Using the same theoretical framework as previous studies, we intend here to introduce the material symmetry inside the heat source determination. For composites reinforced by long carbon fibers, the reinforcement architecture and also the preferential conduction directions of the reinforcements themselves need to be taken into account to properly identify the heat source fields. It is indeed essential to include these orientational effects to be able to enhance the overall understanding of the thermomechanical behavior of anisotropic materials. The application case considered in this work is the damage behavior of an unidirectional carbon-epoxy laminated material under uniaxial quasi-static tension tests. Temperature fields are monitored during axis and off-axis tests by means of an infrared camera. In view of the lack of experimental characterization of conduction properties of such material, homogenization techniques are employed to establish the conductivity tensor from its microstructural features (constituents properties and composite morphology).

2. Theoretical framework

2.1. Global heat source identification

The background of thermodynamics of irreversible processes is used to interpret time and space dependent temperature data in

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terms of heat sources [14]. Quasi-static processes and small perturbations are assumed. The formulation of the problem derives from the combination of the first (energy conservation) and second (admissible evolutions) principles of thermodynamics with the local state axiom. The latter allows to describe the thermodynamic state of a system by a set of state variables, including observable variables (for instance the absolute temperature *T*, the strain tensor ε) and internal variables V_i accounting for irreversible phenomena. According to the generalized standard materials theory, the behavior of the system can thus be entirely described by a thermodynamic potential ψ function of state variables that provides state laws at fixed V_i (equilibrium state) and by a pseudo-potential of dissipation φ function of flow variables $(\dot{\boldsymbol{\varepsilon}}, q, \dot{V}_i)$ ($\dot{\boldsymbol{x}}$ the rate of \boldsymbol{x} and q the heat flux) that gives evolution laws of irreversible processes. Considering a strain-based formulation with Helmholtz free energy $\psi(\mathbf{\epsilon}, T, V_i)$ as the thermodynamic potential, the mechanical stress tensor $\boldsymbol{\sigma} = \boldsymbol{\sigma}^e + \boldsymbol{\sigma}^{an}$ is decomposed in an *elastic* part $\sigma^e = \rho \frac{\partial \psi}{\partial z}$ (ρ the material density) and in an *anelastic* part $\sigma^{an} = \frac{\partial \varphi}{\partial z}$ that accounts for irreversibilities. Combining such framework with the heat conduction law of Fourier ($q = -\mathbf{k} \cdot grad T, \mathbf{k}$ the secondorder thermal conductivity tensor), one can thus obtain the classical expression of the local heat equation [10]:

$$\rho C\dot{T} + div(-\mathbf{k} \cdot gradT) = \underbrace{d_1 + s_{the} + s_{int}}_{s_t} + r_{ext}$$
 (1)

with $C = \frac{\partial^2 \psi}{\partial T^2}$ the specific heat (assumed constant). This means that the rate of heat absorption $\rho C \dot{T}$ and the heat conduction divq are related to the overall heat source s_t produced by the material and to the external heat supply r_{ext} . Global heat source s_t involves the mechanical (intrinsic) dissipation d_1 and the thermoelastic coupling between the temperature and the strain s_{the} :

$$d_1 = (\boldsymbol{\sigma} - \boldsymbol{\sigma}^e) : \dot{\boldsymbol{\varepsilon}} - \rho \frac{\partial \psi}{\partial V_i} \dot{V}_i, \quad s_{the} = \rho T \frac{\partial^2 \psi}{\partial T \partial \boldsymbol{\varepsilon}} : \dot{\boldsymbol{\varepsilon}}$$
 (2)

Last term $s_{int} = \rho T \frac{\partial^2 \psi}{\partial T \partial V_i} \dot{V}_i$ corresponds to other thermomechanical coupling between the temperature and internal variables.

The heat source assessment is based upon the following classical assumptions [10,13]:

- Material thermo-physical parameters remain constant during the test.
- 2. External heat sources r_{ext} are time independent; denoting T_0 the equilibrated temperature field at the beginning of the test (reference point for which the specimen does not produce any heat source s_t), this implies that the reference equilibrium temperature field is such that $-div(\mathbf{k} \cdot grad T_0) = r_{ext}$.
- 3. The temperature variation has no influence on the microstructure state; weak thermal variations observed during the tests tend to corroborate this hypothesis; accordingly, internal coupling sources between T and V_i are not considered in the present study.

For quasi-static processes, convective terms of the total time derivative of the temperature are negligible. As detailed thereafter, studied specimen are thin composite laminates (2 mm thickness). An experimental analysis of thermal fields on the lateral part of the specimen showed that the surface temperature is representative of the temperature in the thickness. One can thus assimilate in what follows the temperature field measured at the surface of specimens to the mean temperature in the thickness and reduce the general problem to the two-dimensional framework. According to all these points, Eq. (1) can be simplified as follows:

$$\rho C\left(\dot{\theta} + \frac{\theta}{\tau}\right) + div(-\mathbf{k} \cdot grad\,\theta) = s_t = d_1 + s_{the} \tag{3}$$

where $\theta = T - T_0$ denotes the mean temperature variation (mean value in the specimen thickness) and τ is a time decrement characterizing heat exchanges between the specimen and the surrounding in the direction perpendicular to the plane of the specimen (see [13] for its experimental determination).

2.2. Thermoelastic source identification

According to Eq. (3), the determination of the intrinsic dissipation d_1 associated to damage phenomena requires the knowledge of the thermoelastic coupling s_{the} . In this way, we consider in this part the case of a thermo-elastic behavior (reversible process). In that case, the Helmholtz free energy around an initial equilibrium state ($\varepsilon_0 = \mathbf{0}, T_0$) is given by:

$$\rho\psi(\boldsymbol{\varepsilon},T) = \frac{1}{2}\,\boldsymbol{\varepsilon}:\mathbb{C}:\boldsymbol{\varepsilon} - \theta\,\boldsymbol{\alpha}:\mathbb{C}:\boldsymbol{\varepsilon} - \frac{1}{2}\,\frac{\rho C}{T_0}\left(T - T_0\right)^2 + \rho\psi_0 \tag{4}$$

with $\mathbb C$ the fourth-order stiffness tensor, α the second-order thermal expansion tensor and $\psi_0(\varepsilon_0, T_0)$ the free energy in the initial state. Since $d_1=0$, one has from (2) and (4):

$$\boldsymbol{\sigma} = \boldsymbol{\sigma}^e = \mathbb{C} : \boldsymbol{\varepsilon} - \theta \boldsymbol{\alpha} : \mathbb{C}$$
 (5)

and

$$S_{the} = -T\boldsymbol{\alpha} : \mathbb{C} : \dot{\boldsymbol{\varepsilon}} = -T\boldsymbol{\alpha} : \dot{\boldsymbol{\sigma}} - T\theta\boldsymbol{\alpha} : \mathbb{C} : \boldsymbol{\alpha}$$
(6)

3. Experimental part

3.1. Specimen

The material of interest is a fiber-reinforced composite laminate made of 14 unidirectional plies of prepreg Hexply® M10R/38%/UD150/CHS (global thickness of 2 mm). A ply is composed of high strength TORAYCA® T700S carbon fibers and M10 epoxy resin matrix. Some physical and thermal properties of the constituents and of the composite itself are given on Table 1. According to Standard NF EN ISO 527-5 for tensile tests on composites, rectangular samples have been cut from laminated plates for loading directions, namely 0° and 90°. Dimensions of samples are 250 mm in length, 20 mm (0°) and 25 mm (90°) in width and pasted glassepoxy heels are of 50 mm length. These samples are representative of a transversely isotropic composite around unit axis x_1 corresponding to the fiber direction.

3.2. Experimental setup

The experimental setup is shown in Fig. 1. Tensile tests are performed with a 100 kN electromechanical testing machine

Table 1Properties of the carbon/epoxy laminated composite and of its constituents (CES: data software Granta CES® selector).

Properties		Units	Values	References
Compos. density Compos. fiber vol fraction Compos. specific heat Compos. time decrement	$ ho \ f_f \ C$	[kg m ⁻³] - [J/kg/K]	1449 0.60 1000 4.7	Measured Hexcel CES Measured
Compos. thermal expansion	τ $\alpha_L \text{ (long)}$ $\alpha_T \text{ (trans)}$	[s] (×10 ⁻⁵) [K ⁻¹]	-0.12 3.40	CES
Fiber thermal conductivity	k_f^L (long k_f^T (trans)	[W/m/K]	9.4 1.6	Toray
Matrix thermal conductivity	k_m	[W/m/K]	0.4	CES

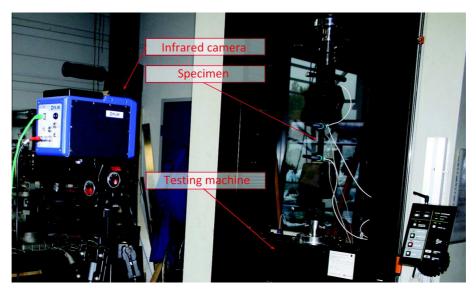


Fig. 1. Experimental setup.

INSTRON® 5500R. These tests are performed at ambient temperature with loading speed conventionally equal to 2 mm per min (0°) and 1 mm per min (90°) . To check the reproducibility of the response, three specimens are considered for each loading direction.

During the tests, a thermal acquisition is carried out on one face of the sample with a FLIR® Titanium SC7000 retrofitted camera (InSb sensors, focal plane array of 320 × 256 pixels, thermal resolution of around 25 mK). Numerous acquisition parameters are selected up, the main ones being: the emissivity of the sample (0.98 for carbon fiber laminate), the sampling frequency $(f_s = 150 \,\mathrm{Hz})$ and the distance between the lens and the specimen that leads to a spatial resolution smaller than 0.7 mm. Automatic calibration, control of the camera and data recording are done by Altair® software which is associated to the camera. Thermal images recorded by the infrared camera during the tensile tests thus capture the temporal and spatial dependency of the digitized temperature T. Altair® software allows to study a specific area of the sample. The size of studied area is of 218×36 pixels (respectively 154×33 pixels) with a pixel size of around 0.43 mm (resp. 0.68 mm) for 0° (resp. 90°) tests. In agreement with assumptions considered in Section 2.1, the analysis is done on temperature variation θ obtained by subtracting to each measured thermal data Tthe average of the ten first frames corresponding to the reference temperature field T_0 .

4. Identification of a filtering process

Eq. (3) provides an estimation of the heat source fields from time and spatial derivatives of the thermal field. Since thermal measurements are discrete and strongly affected by noise perturbations resulting for instance from environmental disturbances, measurement devices and/or quantization, a data processing is necessary to obtain a relevant interpretation of measurements.

4.1. Methodology

The aim of the data processing is to reduce time and spatial noises amplitude while keeping useful information. As derivative process may be seen as a first order high pass filter, low pass filtering methods at least of first order in time domain and second order in spatial domain should be considered to clear undesired effects of

derivatives. Several filtering methods studied in the literature [11,13] have been investigated: linear filters of kind unweighted average (time and spatial moving average), linear filters of kind weighted average (Finite Impulse Response and Infinite Impulse Response), polynomial smoothing obtained using least-squares polynomial approximation, nonlinear filter (spatial-median filter with median value taken on a 3×3 pixels square).

Each term of the left-hand side of Eq. (3) has been analyzed separately. First, thermal variation θ along time and its derivative $\dot{\theta}$ have been studied. The determination of the temporal term $\dot{\theta}$ has been performed with the numerical left derivation to keep high dynamic of useful signal observed in our case and to ensure causality of processing. For the analysis of second-order partial derivatives according to space variables entering the spatial conduction laplacian term $div(-\mathbf{k} \cdot grad \theta)$, central derivation commonly used in signal processing has been applied. The characterization of the data processing has been addressed regarding two issues of the filtering efficiency. First, temporal efficiency has been studied through variations of the temperature on two pixels, the first one subjected to a strong damage during the test and the second one subjected to a low one. Then, we have investigated the spatial efficiency through variations of the temperature along a pixel line and along a pixel column at two instants (two frames), the first one subjected to a strong damage and the second one subjected to environmental noise (frame close to the beginning of the test). Such a work has been carried out with Matlab® software.

4.2. Evaluation and results

Since there is no theoretical signal that could be used as a reference, several features of processed signals have been compared:

- Graphical plots of the original and filtered signals and their derivatives to give a first overview of the filtering efficiency.
- Graphical plots of the Fourier Transform modulus of the original and filtered signals and their derivatives to provide informations about the original signal amplitude attenuations along frequency.
- Pearson product-moment correlation coefficient to indicate the correlation degree between the original and filtered variables; this coefficient is between -1 (anticorrelation) and +1 (exact correlation), 0 corresponding to independent variables [15].

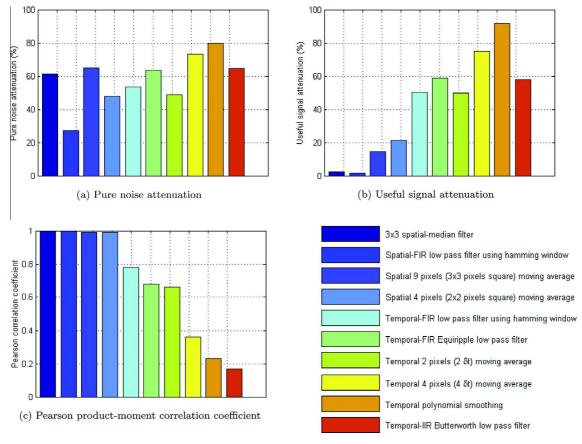


Fig. 2. Comparison of the efficiency of filtering methods for estimating the temporal term $\dot{\theta}$.

- Standard deviation of the original and filtered signals on a noisy area in order to evaluate pure noise attenuation.
- Standard deviation between specific points of the original and filtered curves to evaluate the preservation of the useful signal.

As an illustration, a comparison of the efficiency of filtering methods is done on the estimation of the temporal derivative $\hat{\theta}_f$ of the filtered temperature variation θ_f : Fig. 2a (respectively Fig. 2b) provides the relative variation of original and filtered signals standard deviations for the analysis of pure noise (resp. useful signal) attenuation and Fig. 2c the value of the Pearson product-moment coefficient for each method. Therefore the best compromise corresponds to a high value in Fig. 2a and c associated with a low value in Fig. 2b. In Fig. 3 is also depicted the influence on the spatial and temporal evolution of the temperature.

It appears that the 3×3 pixels spatial-median filter provides in our case the best results: it decreases the amplitude of noise (Figs. 2a and 3a), keeps the significant features of the signal (Figs. 2b and 3b) and leads to an optimal correlation according to the Pearson product-moment correlation coefficient (Fig. 2c). The FIR low pass filter using Hamming window and the spatial 9 pixels $(3\times3\ pixels\ square)$ moving average also give interesting results. Yet, the former induces important delays and is not as effective on noise reduction (see Fig. 2a) and the latter tends to reduce the amplitude of the useful signal (see Fig. 2b). It has been noticed also that no temporal filtering is needed when using 3×3 pixels median-filter on spatial temperature variation. Indeed, temporal dynamics of temperature is relatively slow regarding time sampling frequency ($f_s = 150 \, \text{Hz}$), so an efficient spatial filter naturally induces temporal filtering. It was also found that filtering on the derived terms is needless due to the satisfactory reduction of noise on the thermal fields with the spatial-median filter.

5. Estimation of the effective conductivity tensor by homogenization

As underlined in the Introduction, existing works often deal with isotropic materials for which the conductivity tensor is such that $\mathbf{k} = k\mathbf{I}$ with k a scalar value and \mathbf{I} the second-order identity tensor. In our case, a transversely isotropic thermal conductivity tensor \mathbf{k} needs to be considered to account for the oriented thermal conduction of studied composites. In view of the lack of experimental data, this section intends to determine such intrinsic data of the material by means of a homogenization scheme. Considering adequate conditions for the problem, such a method makes it possible to establish the effective properties of heterogeneous materials from their microstructural features [16]. Precisely, following developments are based on the strong analogy between well-known elasticity problems and conduction ones [17,18].

Let denote Ω the volume of the Representative Volume Element (RVE) of the heterogeneous material, $\partial\Omega$ its outer boundary and n the outward unit normal to $\partial\Omega$. The macroscopic temperature gradient G can be defined as the mean temperature on the boundary $\partial\Omega$. From the divergence theorem, one can demonstrate that the macroscopic temperature gradient G corresponds to the average value of its microscopic corresponding quantity g:

$$G = \frac{1}{\Omega} \int_{\partial \Omega} T(z) \, n(z) \, dS = \frac{1}{\Omega} \int_{\Omega} g(z) \, dV = \langle g \rangle \tag{7}$$

where T(z) and g(z)=gradT(z) denote respectively the local temperature and the local temperature gradient for any point z of Ω . On the other hand, the macroscopic heat flux Q can be defined as the mean value of the external heat density on the boundary $\partial\Omega$. Under stationary conditions (equivalent to usual equilibrium conditions of elasticity problems), one has divq=0 and the divergence

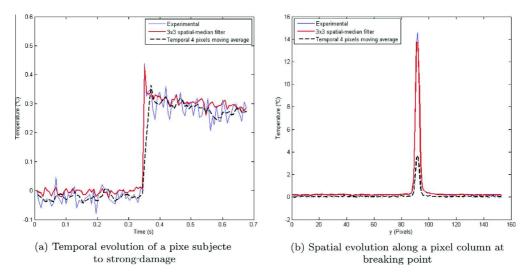


Fig. 3. Influence of two filtering methods on the temperature variation (0° sample).

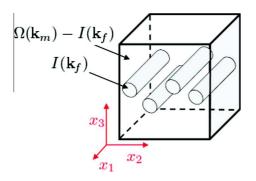


Fig. 4. Representative Volume Element of the transversely isotropic composite considered; (x_1,x_2,x_3) forms an orthonormal basis.

theorem shows again that the macroscopic heat flux Q corresponds to the mean value of the local heat flux q:

$$Q = \frac{1}{\Omega} \int_{\partial \Omega} q(z) \cdot n(z) z \, dS = \frac{1}{\Omega} \int_{\Omega} q(z) \, dV = \langle q \rangle \tag{8}$$

The RVE studied here is the laminated specimen itself including two phases (epoxy matrix and carbon fibers, Fig. 4), that can be considered as statistically homogeneous in regards to the fiber dimension. Spatial distribution of fibers is random, the matrix is continuous and interfaces are assumed to be perfect. Also, the material exhibits a 'matrix-inclusion' morphology since fibers have the same shape, orientation and thermal behavior. Precisely, homogeneous constituents locally follow the Fourier linear thermal law. If the matrix can be considered as isotropic, fibers exhibit a transversely isotropic behavior around their unit axis x_1 . The local conductivity tensor is thus such that:

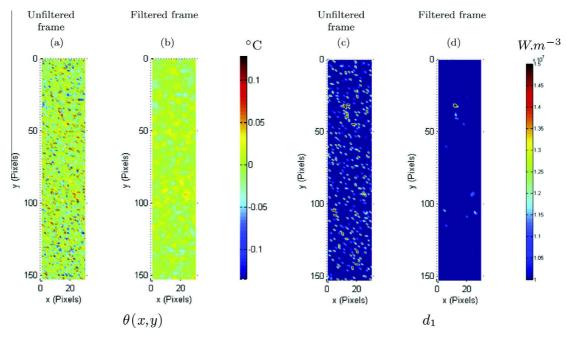


Fig. 5. Influence of the spatial-median filtering on the temperature variation field and on the associated mechanical dissipation field (90° sample, $t = t_{bt} - 4\delta t$ with t_{bt} the breaking time and $\delta t = 1/f_s = 6.6$ ms).

$$\mathbf{k}(z) = \begin{cases} \mathbf{k}_m = k_m \mathbf{I}, & \forall z \in \Omega_m \\ \mathbf{k}_f = k_f^L x_1 \otimes x_1 + k_f^T (\mathbf{I} - x_1 \otimes x_1), & \forall z \in \Omega_f \end{cases}$$
(9)

where k_m denotes the matrix conductivity, k_f^L (respectively k_f^T) the fiber conductivity in the longitudinal (resp. transversal) direction and Ω_m (resp. Ω_f) the matrix (resp. fiber) volume such that $\Omega_m \cup \Omega_f = \Omega$ and $\Omega_m \cap \Omega_f = \emptyset$.

A uniform homogeneous macroscopic thermal gradient G is imposed at the outer boundary $\partial\Omega$ of the RVE. Assuming an initial natural state, the superposition principle allows to relate local and macroscopic thermal gradients as follows:

$$g(z) = \mathbf{A}(z) \cdot \mathbf{G}, \quad \forall z \in \Omega$$
 (10)

Second-order tensor **A** is called the concentration tensor and satisfies $\langle \mathbf{A} \rangle = \mathbf{I}$ to ensure the consistency condition (7). For homogeneous constituents, the effective thermal conductivity of the composite \mathbf{k}_{hom} that links overall quantities $(Q = -\mathbf{k}_{hom} \cdot G)$ comes to the following simplified form [19,20]:

$$\mathbf{k}_{hom} = \sum_{r} f_r \mathbf{k}_r \cdot \langle \mathbf{A} \rangle_r \tag{11}$$

with $\{f_r = \frac{\Omega_r}{\Omega}\}_{r=\{mf\}}$ the volume fraction of each phase and $\langle . \rangle_r = \frac{1}{\Omega_r} \int_{\Omega_r} .dV$ the average value on the phase r. Average concen-

tration tensor $\langle \mathbf{A} \rangle_r$ provides then the average thermal gradient on the r phase ($\langle g \rangle_r = \langle \mathbf{A} \rangle_r \cdot G$). Introducing the condition (7), Eq. (11) comes to:

$$\mathbf{k}_{hom} = \mathbf{k}_m + f_f(\mathbf{k}_f - \mathbf{k}_m) \cdot \langle \mathbf{A} \rangle_f \tag{12}$$

Works on the single-inhomogeneity problem, initiated by Eshelby in elasticity [21] and extended to thermoelasticity ([22–24] for example), provide solutions to derive estimations of $\langle \mathbf{A} \rangle_f$. In the present context of an unidirectional composite with high carbon fiber volume fraction, the scheme proposed by Mori and Tanaka [25] has been choosen as it generally provides a good adequation with experimental results and finite element simulations. Moreover, it accounts in some way for the interactions between constituents. Accordingly, the concentration tensor of fibers writes:

$$\langle \mathbf{A} \rangle_f = \mathbf{A}_m^f \cdot \left[(1 - f_f) \mathbf{I} + f_f \mathbf{A}_m^f \right]^{-1}$$
 (13)

where

$$\mathbf{A}_{m}^{f} = \left[\mathbf{I} + \mathbf{S}_{E}^{I} \cdot (\mathbf{k}_{m})^{-1} \cdot (\mathbf{k}_{f} - \mathbf{k}_{m}) \right]^{-1}$$
(14)

The second-order depolarization tensor S_E^l (the so-called Eshelby tensor of elastic problems) depends on the shape and orientation of inclusions [18]. Since carbon fibers are modeled as an infinite

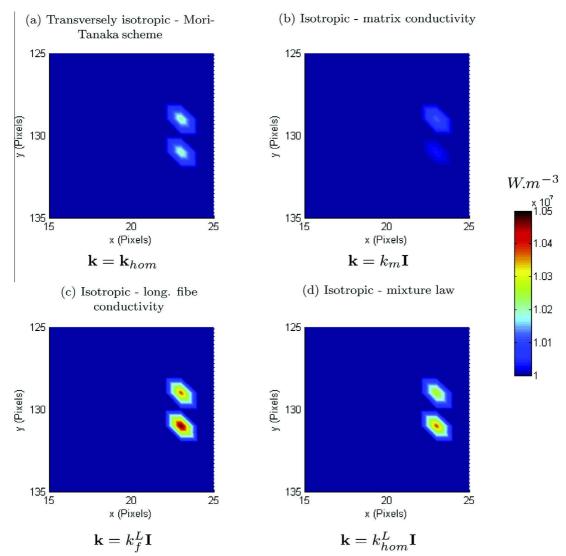


Fig. 6. Influence of the material symmetry of the conduction behavior on the estimation of the mechanical dissipation field d_1 (90° sample, $t = t_{bt} - 4\delta t$).

cylindrical inclusion of axis x_1 with circular section (Fig. 4), one has [23,26]:

$$\mathbf{S}_{E}^{I} = \frac{1}{2} \left(\mathbf{I} - \mathbf{x}_{1} \otimes \mathbf{x}_{1} \right) \tag{15}$$

Relevant calculations give rise to the final expression of the effective conductivity of the composite, namely:

$$\mathbf{k}_{hom} = k_{hom}^{L} \mathbf{x}_1 \otimes \mathbf{x}_1 + k_{hom}^{T} (\mathbf{I} - \mathbf{x}_1 \otimes \mathbf{x}_1)$$
(16)

with

$$k_{hom}^{L} = (1 - f_f) k_m + f_f k_f^{L}, \quad k_{hom}^{T} = k_m \frac{(1 - f_f) k_m + (1 + f_f) k_f^{T}}{(1 + f_f) k_m + (1 - f_f) k_f^{T}}$$
(17)

In agreement with the cylindrical geometry of fibers and their transversely isotropic behavior around the same axis, the composite exhibits also a transversely isotropic behavior around x_1 . Note also that the effective longitudinal conductivity k_{hom}^L corresponds to the classical law of mixtures and, more generally, that results are similar to those obtained with self-consistent formula [27,28]. Including data of Table 1, numerical application leads to $k_{hom}^L = 5,80 \, \text{W/m/K}$ and $k_{hom}^T = 0,85 \, \text{W/m/K}$, which confirms the preferential conduction of the composite along its longitudinal direction.

6. Results and discussion

In a first step, Fig. 5 intends to illustrate the influence of the spatial-median filter on the field data. The two first pictures show respectively the unfiltered (5a) and filtered (5b) temperature variation fields θ of the whole sample at a specific instant of the 90° test, namely at $t = t_{bt} - 4\delta t$ with t_{bt} the breaking time and $\delta t = 1/f_s = 6.6$ ms. This clearly demonstrates the interest of the filtering process in avoiding spatial noise disturbances and in localizing overheating (note that the reduction in time noise amplitude was previously illustrated in Fig. 2). To highlight the influence of the filtering process on the source estimation, the mechanical heat source field d_1 at the same instant has been established from unfiltered (Fig. 5c) and filtered (Fig. 5d) temperature acquisitions. Global heat source s_t has been obtained from the procedure detailed in Section 2 and by using the effective thermal conductivity tensor derived in Section 5. Material properties defined in Table 1 have provided expressions of the stiffness \mathbb{C} and thermal expansion α tensors (both transversely isotropic). The stress rate $\dot{\sigma}$ given by the loading machine provides finally the mechanical heat source d_1 from the theoretical source s_{the} (Eqs. (3) and (6)). Again, applying the spatial-median filter to the temperature data leads to a much more relevant interpretation of mechanical heat source that only reveals significant dissipative events. We can note also that overheating observed on temperature field (Fig. 5b) and most important source values (Fig. 5d) usually do not match. This reinforces the need to determine dissipation sources to get a more accurate indicator of damage.

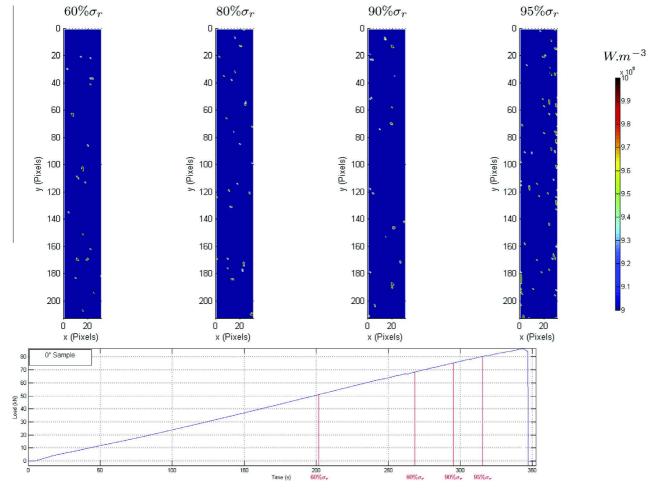


Fig. 7. Mechanical dissipation field d_1 for 0° sample at different load levels ($\sigma_r = 2166$ MPa).

In a second step, we intend to investigate the influence of the material symmetry on the estimation of the mechanical dissipation field. For greater clearness, let focus on a local area $(10 \times 10 \text{ pixels})$ of the sample previously studied $(90^{\circ}$ test, $t = t_{bt} - 4\delta t)$. Following the procedure of Section 2 and working with filtered temperature, our aim is to compare the dissipation fields d_1 obtained when using different expressions of the effective thermal conductivity tensor \mathbf{k} . Graphical maps of Fig. 6 were thus obtained under different assumptions regarding the thermal conduction behavior. Precisely, Fig. 6a corresponds to the transversely isotropic conduction case studied in Section 5 with conductivity tensor \mathbf{k} given by Eq. (16). Three others figures were obtained with simplified representations based on an isotropic conduction behavior $\mathbf{k} = k\mathbf{I}$:

- in Fig. 6b, one uses the matrix conductivity ($k = k_m$),
- in Fig. 6c, the longitudinal fiber conductivity is considered $(k = k_f^L)$,
- the last case shown in Fig. 6d deals with a law of mixture $(k = k_{hom}^L)$.

As shown by these pictures, the localization and intensity of the mechanical dissipation differ according to the considered material symmetry, and even differ between the three isotropic cases. Compared with the anisotropic case (Fig. 6a), using the matrix conductivity (Fig. 6b) globally underestimates the heat source d_1 while the longitudinal fiber value (Fig. 6c), and in a lesser extent the mixture law (Fig. 6d), overestimate it. These results are in agreement with

the order of magnitude of constituents conductivity properties (Table 1). Then, the two main sources obtained in the anisotropic case appear as quite equivalent in intensity (Fig. 6a), whereas isotropic conduction assumptions lead to distinct values. In the latter case, the source of the top of picture Fig. 6b is higher than the bottom one, while reverse result is achieved in Figs. 6c and d. It is also worth noting that the mixture law case uses the same longitudinal conductivity value of \mathbf{k} as the anisotropic case and differs only for its transverse component. Differences between Figs. 6a and d demonstrate that the anisotropic character of the thermal conduction clearly affects the mechanical dissipation sources. It is thus of main importance to introduce a physical representation of the thermal conduction behavior to get a relevant estimation of heat sources, and consequently to account for orientational effects involved in anisotropic materials. Such issue becomes even more crucial when the spatial conduction term $div(-\mathbf{k} \cdot grad \theta)$ represents the major part of the heat sources in the local heat equation. The homogenization approach used in this work to derive the effective thermal conductivity tensor offers then interesting perspectives to account for even more complex anisotropic situations.

This last part finally illustrates some opportunities provided by the present work, specially for the damage analysis. Using the full methodology, including spatial-median filter and transversely isotropic conductivity tensor, we present the evolution of the mechanical dissipation during mechanical tests. In Fig. 7 (respectively Fig. 8) are depicted several maps of the mechanical dissipation at different levels of the breaking stress σ_r for the 0° (resp. 90°)

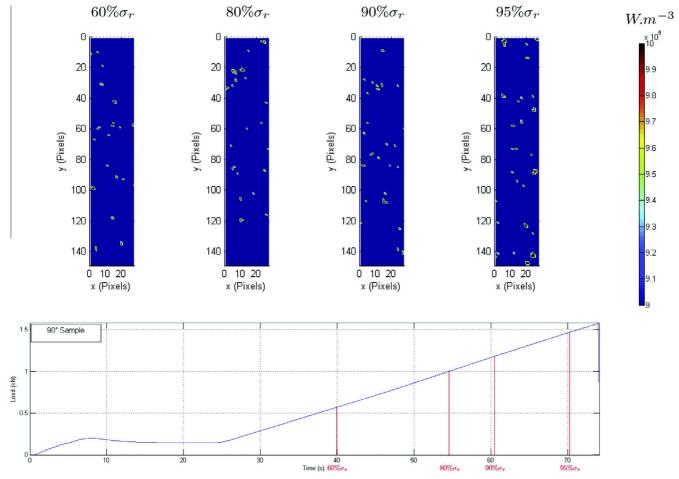


Fig. 8. Mechanical dissipation field d_1 for 90° sample at different load levels ($\sigma_r = 32$ MPa).

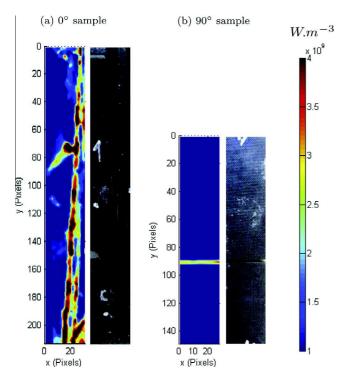


Fig. 9. Mechanical dissipation field d_1 and post-mortem observation for 0° and 90° samples at breaking time.

loading direction. For both tests, we observe local dissipative phenomena, corresponding to local high amplitude mechanical dissipations, that are randomly distributed on specimen surfaces. This stands in agreement with the random location distribution of damage put in evidenced by tomography in woven carbonepoxy laminates [4]. It is also worth noting that, for both axis and off-axis loads, mechanical dissipation d_1 at the beginning of the test is of the same amplitude (around 10⁷ W m⁻³) and that highest amplitude zones do not exhibit any preferential geometric shape or orientation. In contrast, dissipation behavior clearly differs close to failure according to the loading direction. At 95% of the 0° yield stress, it can be observed an increase in the number of local dissipation events, whereas evolution of sources is much more progressive for the 90° test. The mode of dissipated energy can be related to damage mechanisms features and kinetics associated to each loading configuration. 0° samples undergo fiber/ matrix debonding which suddenly accelerates at the end of the test leading to a macroscopic crack parallel to the axial direction. Mechanical dissipation field d_1 at breaking load has a very high amplitude (maximum value greater than $4 \times 10^9 \, \text{W m}^{-3}$) and post-mortem observation illustrates such behavior (Fig. 9a). On the other hand, 90° samples exhibit a diffuse matrix cracking all along the test and failure corresponds to the development of the weakest defect in the direction orthogonal to the load. Fig. 9b corroborates the less brittle character of such failure mode with a lower level of dissipated energy d_1 (maximum value of $2.8 \times 10^9 \text{ W m}^{-3}$).

7. Conclusions

In this study, an original approach for estimating heat sources in anisotropic materials is presented. Input data are obtained from infrared thermographic measurements during axis and off-axis tensile tests on carbon–epoxy laminates. In order to determine the mechanical dissipations produced by the material considered,

a filtering method based on the use of a spatial-median filter has been developed. At the same time, the Mori–Tanaka homogenization approach has provided the effective transversely isotropic conductivity tensor of the composite material.

This work intends to provide a better interpretation of thermal measurements in anisotropic environment, leading to a much more accurate localization and characterization of dissipation sources. For instance, the application of the present methodology has allowed to demonstrate some correlations between most important dissipation events and acoustic emissions of high energy for carbon composites under tensile tests [29]. Moreover, the micromechanical contribution allows full perspectives to heat sources studies through the account of several parameters which may affect results, such as orientational aspects, spatial interactions between the constituents or damage evolution. Based on this approach, further works should now be conducted on various anisotropic material submitted to different loading configurations (specially off-axis loads) to improve the understanding of dissipative phenomena and their modeling.

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