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### The VIMOS Public Extragalactic Redshift Survey (VIPERS)

Hierarchical scaling and biasing\*

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#### ABSTRACT

Aims. Building on the two-point correlation function analyses of the VIMOS Public Extragalactic Redshift Survey (VIPERS), we investigate the higher-order correlation properties of the same galaxy samples to test the hierarchical scaling hypothesis at  $z \sim 1$  and the dependence on galaxy luminosity, stellar mass, and redshift. With this work we also aim to assess possible deviations from the linearity of galaxy bias independently from a previously performed analysis of our survey.

*Methods.* We have measured the count probability distribution function in spherical cells of varying radii ( $3 \le R \le 10 h^{-1}$  Mpc), deriving  $\sigma_{8g}$ (the galaxy rms at 8  $h^{-1}$  Mpc), the volume-averaged two-, three-, and four-point correlation functions and the normalized skewness  $S_{3g}$  and kurtosis  $S_{4g}$  for different volume-limited subsamples, covering the following ranges:  $-19.5 \le M_B(z = 1.1) - 5\log(h) \le -21.0$  in absolute magnitude,  $9.0 \le \log(M_*/M_{\odot}h^{-2}) \le 11.0$  in stellar mass, and  $0.5 \le z < 1.1$  in redshift.

*Results.* We have performed the first measurement of high-order correlation functions at  $z \sim 1$  in a spectroscopic redshift survey. Our main results are the following. 1) The hierarchical scaling between the volume-averaged two- and three-point and two- and four-point correlation functions holds throughout the whole range of scale and redshift we could test. 2) We do not find a significant dependence of  $S_{3g}$  on luminosity (below z = 0.9the value of  $S_{3g}$  decreases with luminosity, but only at  $1\sigma$ -level). 3) We do not detect a significant dependence of  $S_{3g}$  and  $S_{4g}$  on scale, except beyond  $z \sim 0.9$ , where  $S_{3g}$  and  $S_{4g}$  have higher values on large scales ( $R \ge 10 h^{-1}$  Mpc): this increase is mainly due to one of the two CFHTLS Wide Fields observed by VIPERS and can be explained as a consequence of sample variance, consistently with our analysis of mock catalogs. 4) We do not detect a significant evolution of  $S_{3g}$  and  $S_{4g}$  with redshift (apart from the increase of their values with scale in the last redshift bin). 5)  $\sigma_{8g}$ increases with luminosity, but does not show significant evolution with redshift. As a consequence, the linear bias factor  $b = \sigma_{sg}/\sigma_{sm}$ , where  $\sigma_{sm}$ is the rms of matter at a scale of 8  $h^{-1}$  Mpc, increases with redshift, in agreement with the independent analysis of VIPERS and of other surveys such as the VIMOS-VLT Deep Survey (VVDS). We measure the lowest bias  $b = 1.47 \pm 0.18$  for galaxies with  $M_B(z = 1.1) - 5 \log(h) \le -19.5$  in the first redshift bin  $(0.5 \le z < 0.7)$  and the highest bias  $b = 2.12 \pm 0.28$  for galaxies with  $M_B(z = 1.1) - 5 \log(h) \le -21.0$  in the last redshift bin  $(0.9 \le z < 1.1)$ . 6) We quantify deviations from the linear bias by means of the Taylor expansion parameter  $b_2$ . We obtain  $b_2 = -0.20 \pm 0.49$  for  $0.5 \le z < 0.7$  and  $b_2 = -0.24 \pm 0.35$  for  $0.7 \le z < 0.9$ , while for the redshift range  $0.9 \le z < 1.1$  we find  $b_2 = +0.78 \pm 0.82$ . These results are compatible with a null non-linear bias term, but taking into account another analysis for VIPERS and the analysis of other surveys, we argue that there is evidence for a small but non-zero non-linear bias term.

Key words. large-scale structure of Universe - cosmology: observations - dark matter - galaxies: statistics

#### 1. Introduction

In the standard model of structure formation, the growth of density fluctuations from a primordial Gaussian density field is driven by gravity; it is possible to follow the evolution of these fluctuations through analytical and numerical approaches and predict the statistical properties for the dark matter field and dark matter haloes. Galaxies form in a complex process following the baryonic infall into dark matter halos: this means that the comparison between theory and observations is not straightforward, but it also implies that the spatial distribution of galaxies contains a wealth of information relevant for both cosmology and the physics of galaxy formation.

<sup>\*</sup> Based on observations collected at the European Southern Observatory, Cerro Paranal, Chile, using the Very Large Telescope under programs 182.A-0886 and partly 070.A-9007. Also based on observations obtained with MegaPrime/MegaCam, a joint project of CFHT and CEA/DAPNIA, at the Canada-France-Hawaii Telescope (CFHT), which is operated by the National Research Council (NRC) of Canada, the Institut National des Sciences de l'Univers of the Centre National de la Recherche Scientifique (CNRS) of France, and the University of Hawaii. This work is based in part on data products produced at TERAPIX and the Canadian Astronomy Data Centre as part of the Canada-France-Hawaii Telescope Legacy Survey, a collaborative project of NRC and CNRS. The VIPERS web site is http://www. vipers.inaf.it

Extracting and exploiting this information from the data requires a number of different and complementary statistical approaches. For example, while the two-point correlation function  $\xi_2(\mathbf{r})$  is the simplest and most widely used statistical indicator of galaxy clustering, a complete description of a distribution is only given by the full *J*-point correlation functions  $\xi_J$ , or equivalently, by the volume-averaged correlation functions  $\overline{\xi}_J$ , which are related to the *J*-order moments of the count probability distribution function (PDF)<sup>1</sup>. The count PDF gives the probability of counting *N* objects as a function of volume *V*. High-order correlations are particularly interesting because perturbation theory and numerical simulations can describe their behaviour for the gravitational evolution of matter density fluctuations.

The first estimates of the two- and three -point galaxy correlations functions on angular catalogues of galaxies were made by Groth & Peebles (1977), who found that these estimates were well described by the hierarchical relation  $\xi_3(r_{12}, r_{13}, r_{23}) =$  $Q[\xi_2(r_{12})\xi_2(r_{13}) + \xi_2(r_{13})\xi_2(r_{23}) + \xi_2(r_{12})\xi_2(r_{23})]$ . The three-point correlation function has subsequently become a standard statistical tool for the analysis of clustering and has been applied to simulations and recent surveys of galaxies (see e.g. Marín et al. 2008; Moresco et al. 2014), while its Fourier transform, the bispectrum, has also been applied to the analysis of the Ly<sub> $\alpha$ </sub> forest (Mandelbaum et al. 2003; Viel et al. 2004) and of the cosmic microwave background (CMB; Planck Collaboration XXIV 2014).

The scaling relation between the two- and three -point correlation functions was soon generalized to higher orders (Fry & Peebles 1978 up to J = 4; Sharp et al. 1984 up to J = 5) and was mathematically described by the so-called hierarchical models, where the *J*-point correlation functions are expressed as a function of products of the two-point correlation function. Different versions of these models were suggested, but Balian & Schaeffer (1989) showed that all of them belong to the general class of scale-invariant models, which are defined by the scaling property:

$$\xi_J(\lambda r_1, ..., \lambda r_J) = \lambda^{-(J-1)\gamma} \xi_J(r_1, ..., r_J).$$
(1)

From a physical point of view, the hierarchical scaling of the correlation functions is expected in the highly non-linear regime (the BBGKY hierarchy, see Davis & Peebles 1977; Fry 1984a; Hamilton 1988) and in the quasi-linear regime (from perturbation theory, see Peebles 1980; Fry 1984b; Bernardeau 1992; Bernardeau et al. 2002 and references therein).

Another prediction of the hierarchical models is that the normalized high-order reduced moments  $S_J \equiv \overline{\xi}_J/\overline{\xi}_2^{J-1}$  should be constant. In the present paper we focus on the normalized skewness  $S_3$  and kurtosis  $S_4$ . Peebles (1980) showed that in second-order perturbation theory, assuming Gaussian primordial density fluctuations and an Einstein-de Sitter model,  $S_{3m}$ , the normalized skewness of matter fluctuations assumes the value 34/7. Subsequent works have shown that the smoothed  $S_{3m}$  depends on the slope of the power spectrum and has a very weak dependence on the cosmological model (see Bernardeau et al. 2002).

While in standard models with Gaussian primordial fluctuations the skewness and higher-order moments assume non-zero values as a consequence of gravitational clustering, scenarios with non-Gaussian primordial perturbations also predict a primordial non-zero skewness, particularly at large scales ( $\geq 10 h^{-1}$  Mpc; Luo & Schramm 1993; Fry & Scherrer 1994; Gaztañaga & Maehoenen 1996; Gaztañaga & Fosalba 1998; Durrer et al. 2000); therefore these scenarios can in principle be constrained by measuring the high-order moments (Mao et al. 2014).

Moreover, it has been shown that the hierarchy of the *J*-point functions and the measurement of  $S_3$  and  $S_4$  can be used as a cosmological test to distinguish between the standard  $\Lambda$  cold dark matter ( $\Lambda$ CDM) and models including long-range scalar interaction between dark matter particles ("fifth force" dark matter models), as shown by Hellwing et al. (2010), who found the largest deviations in the redshift range 0.5 < z < 2.

However, the comparison between the theoretical predictions for the matter distribution and the observed galaxy distribution is not trivial, as a consequence of bias. One of the first results derived from the analysis of the first redshift surveys was that the amplitude of the two-point correlation function depends on galaxy luminosity and galaxy colour (see Marulli et al. 2013, and references therein); therefore, the galaxy distribution must generally differ from the underlying matter distribution. A common assumption is that the galaxy and matter density fields are related by a linear relation,  $\delta_g = b\delta_m$ , where  $\delta_g \equiv \Delta \rho_g / \rho_g$  and  $\delta_{\rm m} \equiv \Delta \rho_{\rm m} / \rho_{\rm m}$  are the galaxy and matter density contrast, respectively. This relation is a consequence of the scenario of biased galaxy formation, where galaxies form above a given threshold of the linear density field, in the limit of high threshold and low variance. Of course, this relation cannot have general validity: when b > 1 and  $\delta_m < 0$ , the linear relation gives an unphysical value  $\delta_g < -1$ .

A simple prediction of linear biasing is that the two-point correlation function is amplified by a factor  $b^2$ , while  $S_3$  is inversely proportional to b. The analysis of the first redshift surveys revealed instead that different classes of galaxies selected in the optical and infrared bands, while differing in the amplitude of the two-point correlation function, have similar values of  $S_3$  (Gaztañaga 1992; Bouchet et al. 1993; Benoist et al. 1999); the same also holds for galaxy clusters (Cappi & Maurogordato 1995). In particular, Benoist et al. (1999) analysed volumelimited samples of the Southern Sky Redshift Survey 2 (SSRS2, da Costa et al. 1994) and found that, while the two-point correlation amplitude increases significantly with galaxy luminosity when  $L > L_*$  (Benoist et al. 1996), the value of  $S_3$  does not scale with the inverse of the bias parameter b and is independent of luminosity and scale within the errors: this implies that the bias is non-linear. Similar results were obtained in the Durham/UKST and Stromlo-APM redshift surveys (Hoyle et al. 2000) and in the larger and deeper 2dF Galaxy Redshift Survey (2dFGRS, Baugh et al. 2004; Croton et al. 2004a), which enabled a more detailed analysis: for example, Croton et al. (2004b) found evidence for a weak dependence of  $S_3$  on luminosity, while according to Croton et al. (2007) the  $S_J$  of red galaxies depends on luminosity, while blue galaxies do not show any dependence. In an analysis of the Sloan Digital Sky Survey (SDSS) Ross et al. (2006) found that the values of  $S_J$  are lower for late-type than for early-types galaxies.

In more recent years, deeper surveys enabled exploring the effects of the evolution of gravitational clustering and bias, thus placing stronger constraints on models of galaxy formation and evolution.

Wolk et al. (2013) measured the hierarchical clustering of the CFHTLS-Wide from photometric redshifts. They found an indication that at small scales the hierarchical moments increase with redshift, while at large scales their results are still consistent

<sup>&</sup>lt;sup>1</sup> However, there is the important exception of the lognormal distribution, see Coles & Jones (1991) and Carron (2011).

with perturbation theory for  $\Lambda$ CDM cosmology with a linear bias, but suggest the presence of a small non-linear term.

From the analysis of the VIMOS-VLT Deep Survey, based on spectroscopic redshifts, Marinoni et al. (2005; see also Marinoni et al. 2008) found that the value of  $S_3$  for luminous  $(M_B < -21)$  galaxies is consistent with the local value at z < 1while decreasing beyond  $z \sim 1$ , and that the bias is non-linear.

In this paper we analyse the high-order correlations and moments of the first release of the VIMOS Public Extragalactic Redshift Survey (VIPERS<sup>2</sup>) in the redshift range  $0.5 < z \le 1.1$ as a function of luminosity and stellar mass. We also derive an estimate of the non-linear bias. Our analysis extends those presented in a number of recent works that have investigated various aspects of galaxy clustering in the VIPERS sample. Some works have focused on two-point statistics, like the standard galaxygalaxy two-point correlation function to estimate redshift space distortions (de la Torre et al. 2013) and its evolution and dependence on galaxy properties (Marulli et al. 2013). A different type of two-point statistics, the clustering ratio, has been introduced by Bel & Marinoni (2014) and applied to VIPERS galaxies (Bel et al. 2014) to estimate the mass density parameter  $\Omega_{\rm M}$ . Micheletti et al. (2014) have searched the VIPERS survey for galaxy voids and characterized their properties by means of the galaxy-void cross-correlation. Bel et al. (in prep.) have proposed a method to infer the one-point galaxy probability function from counts in cells that Di Porto et al. (2014) have exploited to search for and detect deviations from linear bias; a result that we directly compare our results with. Finally, Cucciati et al. (2014) studied different methods for accounting for gaps in the VIPERS survey and assessing their impact on galaxy counts.

As cosmological parameters we have adopted  $H_0 =$  70 km s<sup>-1</sup> Mpc<sup>-1</sup>,  $\Omega_M = 0.25$ ,  $\Omega_{\Lambda} = 0.75$ , but all cosmologydependent quantities are given in  $H_0 = 100$  km s<sup>-1</sup> Mpc<sup>-1</sup> units associated with the corresponding power of  $h = H_0/100$ .

#### 2. High-order statistics

In this section we resume the formalism and define the statistical quantities measured in our work.

The volume-averaged *J*-point correlation functions are given by

$$\overline{\xi}_J(V) = \frac{1}{V^J} \int_V \xi_J \mathrm{d}V_1 ... \mathrm{d}V_J,\tag{2}$$

where for spherical cells (used in this work)  $\overline{\xi}_J$  is a function of the cell radius *R* and  $V = 4\pi R^3/3$ .

The volume-averaged two-point correlation function gives the variance of the density contrast:

$$\sigma^2(R) = \xi_2(R). \tag{3}$$

The volume-averaged *J*-point correlation functions can be easily derived from the moments of the count PDF P(N, R), that is, the probability of counting *N* objects in a randomly chosen spherical volume of radius *R* (see Peebles 1980). For simplicity, in the following we omit the dependence on *R*. At a fixed scale *R*, the centred moments of order *J* are

$$\mu_J = \sum_N P(N) \left( \frac{N - \overline{N}}{\overline{N}} \right)^J, \tag{4}$$

where  $\overline{N} = nV = \sum NP(N)$  is the mean number of objects in a cell of radius *R*.

<sup>2</sup> http://vipers.inaf.it

The volume-averaged correlation functions correspond to the reduced moments and up to the fourth order are given by the following relations:

$$\overline{\xi}_{2} = \mu_{2} - \frac{1}{\overline{N}}$$

$$\overline{\xi}_{3} = \mu_{3} - 3\frac{\mu_{2}}{\overline{N}} + \frac{2}{\overline{N}^{2}}$$

$$\overline{\xi}_{4} = \mu_{4} - 6\frac{\mu_{3}}{\overline{N}} + 11\frac{\mu_{2}}{\overline{N}^{2}} - 3\mu_{2}^{2} - \frac{6}{\overline{N}^{3}}$$
(5)

An alternative way to estimate the high-order correlations is through the factorial moments  $m_k$ :

$$m_k = \sum_N P(N)N^{\underline{k}},\tag{6}$$

where

$$N^{\underline{k}} \equiv N(N-1)...(N-k+1)$$
<sup>(7)</sup>

is the falling factorial power of order k (see e.g. Graham et al. 1994).

In fact, for a local Poisson process the moments about the origin of a stochastic field are given by the factorial moments of N; as our variable is the number density contrast  $(N - \overline{N})/\overline{N}$ , we have to convert the factorial moments  $m_k$  into the moments about the mean (central moments)  $\mu'_k$  through the standard relations

$$\mu'_{2} = m_{2} - m_{1}^{2}$$
  

$$\mu'_{3} = m_{3} - 3m_{1}m_{2} + 2m_{1}^{3}$$
  

$$\mu'_{4} = m_{4} - 4m_{1}m_{3} + 6m_{1}^{2}m_{2} - 3m_{1}^{4}.$$
(8)

We can finally derive the volume-averaged *J*-point correlation functions

$$\overline{\xi_J} = \frac{\mu'_J}{\overline{N}^J} \tag{9}$$

and the normalized moments  $S_J$ 

$$S_J = \frac{\overline{\xi}_J}{\overline{\xi}_2^{J-1}}.$$
(10)

The normalized moments can also be obtained through a recursive formula (Szapudi & Szalay 1993; Colombi et al. 2000):

$$S_J = \frac{\overline{\xi}_2 N^J}{N_c^J} - \frac{1}{J} \sum_{k=1}^{J-1} \frac{J!}{(J-k)!k!} \frac{(J-k)S_{J-k}m_k}{N_c^k},$$
(11)

where

$$N_c \equiv \overline{N\xi_2}.$$
 (12)

The values given in this paper were calculated using factorial moments.

At a fixed scale *R*, the deterministic bias parameter *b* can be directly measured through the square root of the ratio of the galaxy variance  $\sigma_g^2$  to the matter variance  $\sigma_m^2$ :

$$b(z) = \frac{\sigma_{\rm g}(z)}{\sigma_{\rm m}(z)}.$$
(13)

In the case of linear biasing, the galaxy density contrast  $\delta_g$  is proportional to the matter density contrast  $\delta_m$  by a constant factor b,  $\delta_g = b\delta_m$ : there is no dependence on scale, and b is the

only parameter that completely defines the relation between the galaxy and matter distribution.

As we have noted in the introduction, the linear biasing cannot have a general validity. It is more general and realistic to assume a local, deterministic non-linear bias  $b(z, \delta_m, R)$ , which can be written as a Taylor expansion (Fry & Gaztanaga 1993):

$$\delta_{\rm g} = \sum_{k=0}^{k} \frac{b_k}{k!} \delta^k,\tag{14}$$

where  $b_1 \equiv b$ . Fry & Gaztanaga (1993) have shown that such a local bias transformation preserves the hierarchical properties of the underlying matter distribution in the limit of small fluctuations (large scales).

In the case of linear bias,  $b_k = 0$  for k > 1, and the galaxy and matter normalized moments are then related by the following equation:

$$S_{Jg} = \frac{S_{Jm}}{b^{J-2}}$$
 (15)

In general, the deviation from linear biasing is measured by taking the second order of the expansion. In this case, the galaxy normalized skewness is given by the following relation:

$$S_{3g} = \frac{1}{b} \left( S_{3m} + 3\frac{b_2}{b} \right).$$
(16)

#### 3. VIPERS survey

The VIMOS Public Extragalactic Redshift Survey (VIPERS) is an ongoing ESO Large Programme aimed at determining redshifts for  $\sim 10^5$  galaxies in the redshift range 0.5 < z < 1.2, to accurately and robustly measure clustering, the growth of structure (through redshift-space distortions) and galaxy properties at an epoch when the Universe was about half its current age (Guzzo & The Vipers Team 2013; Guzzo et al. 2014). The survey is divided into two separate areas and will cover  $\sim 24 \text{ deg}^2$  when completed. The two areas are the so-called W1 and W4 fields of the Canada-France-Hawaii Telescope Legacy Survey Wide (CFHTLS-Wide); the CFHTLS optical photometric catalogues<sup>3</sup> constitute the parent catalogue from which VIPERS spectroscopic targets were selected. The VIPERS survey strategy is optimized to achieve a good completeness in the largest possible area (Scodeggio et al. 2009). Galaxies are selected to a limit of  $i_{AB} < 22.5$ , further applying a simple and robust gri colour pre-selection to effectively remove galaxies at z < 0.5. In this way, only one pass per field is required, allowing us to double the galaxy sampling rate in the redshift range of interest with respect to a pure magnitude-limited sample (~40%). The final volume of the survey will be  $5 \times 10^7 h^{-3}$  Mpc<sup>3</sup>, comparable to that of the 2dFGRS at  $z \sim 0.1$ .

VIPERS spectra are obtained using the VLT Visible Multi-Object Spectrograph (VIMOS, Le Fèvre et al. 2002, 2003) at moderate resolution (R = 210), with the LR Red grism at R =210 and a wavelength coverage of 5500–9500 Å. The typical radial velocity error is  $140(1+z) \text{ km s}^{-1}$ . A discussion of the survey data reduction and the first management infrastructure were presented in Garilli et al. (2012) and the detailed description of the survey was given by Guzzo et al. (2014).

The data set used in this and the other published papers is the VIPERS Public data release 1 (PDR-1) catalogue, made

available to the public in 2013 (Garilli et al. 2014). It includes about 47 000 reliable spectroscopic redshifts of galaxies and active galactic nuclei (AGNs). We here only selected galaxies with reliable redshift, that is, with spectroscopic quality flags 2, 3, 4, or 9 (see Garilli et al. 2014 for the definition).

To avoid regions dominated by large gaps, we here selected a subset of the total area covered by VIPERS: our limits are  $02^{h}01^{m}00^{s} \le RA \le 02^{h}34^{m}50^{s}$ ,  $-5.08^{\circ} \le Dec \le -4.17^{\circ}$ (7.67 square degrees) in W1 and  $22^{h}01^{m}12^{s} \le RA \le 22^{h}18^{m}00^{s}$ ,  $0.865^{\circ} \le Dec \le 2.20^{\circ}$  (5.60 square degrees) in W4.

We defined volume-limited subsamples with different absolute magnitude and stellar mass limits, following the same criteria as in Marulli et al. (2013). The choice of these particular samples is discussed in detail in that paper; here we recall their main properties.

The rest-frame *B*-band absolute magnitude and the stellar mass were estimated through the HYPERZMASS program (Bolzonella et al. 2000, 2010), which applies a spectral energy distribution (SED) fitting technique. To take into account luminosity evolution, we fixed as a reference limit the luminosity at our maximum redshift (z = 1.1) and assumed an evolution M(z) = M(0) - z (see Meneux et al. 2009 and also Ilbert et al. 2005; Zucca et al. 2009).

We did not correct the mass limit of the stellar-mass-limited subsamples; this limit was therefore kept fixed within each redshift bin because the evolution of  $M_*$  is negligible in our redshift range (Pozzetti et al. 2007, 2010; Davidzon et al. 2013).

The respective numbers of galaxies for the different subsamples are given in Table 1. We note that these numbers are slightly different from those in Marulli et al. (2013) because we applied more stringent angular limits to avoid regions nearby prominent gaps that might affect the counts in spherical cells (while the direct estimate of the two-point correlation function through counts of galaxy pairs can be easily corrected for by using a random catalogue with the same survey geometry).

#### 4. Analysis of mock catalogues

We used mock catalogues derived from cosmological simulations to estimate not only the statistical errors and the uncertainty related to cosmic variance, but also the systematic errors that are due to the inhomogeneous spectroscopic completeness and the specific geometry of the two fields. A detailed description of the way these mocks were built was given by de la Torre et al. (2013).

We analysed a set of 26 independent mock catalogues based on the dark matter halo catalogue of the MultiDark simulation (Prada et al. 2012), which assumes a flat ACDM cosmology with  $(\Omega_{\rm M}, \Omega_{\Lambda}, \Omega_{\rm b}, h, n, \sigma_{\rm 8m}) = (0.27, 0.73, 0.0469, 0.7, 0.95,$ 0.82). This catalogue was populated with galaxies using halo occupation distribution prescriptions, as described in de la Torre et al. (2013). In particular, the original halo catalogue was repopulated with halos below the resolution limit with the new technique of de la Torre & Peacock (2013), which enables reproducing the range in stellar mass and luminosity probed by VIPERS data. For luminosity-limited subsamples, galaxy luminosities were calibrated using VIPERS data, while for stellar mass-limited subsamples masses were assigned to galaxies using the stellar-to-halo mass relation (SHMR) of Moster et al. (2013). From the parent mock catalogues, a set of spectroscopic catalogues was derived by applying the same angular, photometric, and spectroscopic selection functions as were applied to the real data. For a more detailed and complete description of the mock catalogues see de la Torre et al. (2013).

<sup>&</sup>lt;sup>3</sup> Mellier et al. (2008), http://terapix.iap.fr/cplt/oldSite/ Descart/CFHTLS-T0005-Release.pdf

Table 1. Definition of the samples.

Limiting magnitude $M_B(z = 1.1) - 5 \log(h)$	Ng	$\sigma_{8 m g}$	S <sub>3g</sub>	$S_{ m 4g}$
$M_B(z=1.1) - 5\log(h)$				
	W1 + W4		$R = 8 h^{-1} \text{ Mpc}$	$R = 8 h^{-1} \text{ Mpc}$
<-19.5	8670 + 6863	$0.95 \pm 0.06$	$1.81 \pm 0.20$	$8.13 \pm 2.03$
<-20.0	6101 + 4963	$1.00\pm0.06$	$1.82 \pm 0.22$	$8.12 \pm 2.05$
<-20.5	3671 + 3025	$1.07 \pm 0.07$	$1.83 \pm 0.27$	$7.93 \pm 2.54$
<-21.0	1787 + 1478	$1.16\pm0.15$	$1.78\pm0.30$	$6.29 \pm 2.96$
<-20.0	7455 + 5384	$1.01 \pm 0.05$	$1.74 \pm 0.14$	$7.19 \pm 1.34$
<-20.5	4979 + 3475	$1.05\pm0.04$	$1.66 \pm 0.16$	$6.02 \pm 1.38$
<-21.0	2457 + 1664	$1.10\pm0.06$	$1.59 \pm 0.22$	$5.50 \pm 1.76$
<-20.5	2751 + 1805	$1.12 \pm 0.07$	$2.50 \pm 0.28$	$14.11 \pm 3.10$
<-21.0	1752 + 1067	$1.16\pm0.08$	$2.54\pm0.38$	$12.70\pm3.81$
Limiting stellar mass	$N_{ m g}$	$\sigma_{ m 8g}$	S <sub>3g</sub>	$S_{ m 4g}$
$\log(M/M_{\odot}h^{-2})$	W1 + W4		$R = 8 h^{-1} \text{ Mpc}$	$R = 8 h^{-1} \text{ Mpc}$
>9.0	8745 + 6544	$0.97 \pm 0.10$	$1.88 \pm 0.15$	$8.51 \pm 1.45$
>9.5	6091 + 4318	$1.03 \pm 0.10$	$1.94 \pm 0.15$	$8.66 \pm 1.43$
>10.0	3654 + 2581	$1.16 \pm 0.11$	$2.02 \pm 0.16$	$8.61 \pm 1.45$
>10.5	1292 + 713	$1.34\pm0.11$	$1.90\pm0.18$	$6.62 \pm 1.39$
>9.5	6159 + 4009	$1.09 \pm 0.08$	$1.88 \pm 0.14$	$7.59 \pm 1.37$
>10.0	3746 + 2428	$1.18 \pm 0.08$	$1.87 \pm 0.14$	$7.29 \pm 1.36$
>10.5	1467 + 819	$1.41 \pm 0.09$	$2.04\pm0.20$	$7.81 \pm 1.80$
>10.0	1644 + 964	$1.23 \pm 0.08$	$2.70 \pm 0.21$	$13.28 \pm 2.43$
>10.5	738 + 456	$1.43\pm0.09$	$3.19\pm0.29$	$16.18 \pm 3.88$
	$\begin{array}{r} <-20.5 \\ <-21.0 \\ <-20.0 \\ <-20.5 \\ <-21.0 \\ \hline \\ <-20.5 \\ <-21.0 \\ \hline \\ \hline \\ \\ \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{c ccccc} < -20.5 & 3671 + 3025 & 1.07 \pm 0.07 \\ < -21.0 & 1787 + 1478 & 1.16 \pm 0.15 \\ \hline \\ < -20.0 & 7455 + 5384 & 1.01 \pm 0.05 \\ < -20.5 & 4979 + 3475 & 1.05 \pm 0.04 \\ < -21.0 & 2457 + 1664 & 1.10 \pm 0.06 \\ \hline \\ < -20.5 & 2751 + 1805 & 1.12 \pm 0.07 \\ < -21.0 & 1752 + 1067 & 1.16 \pm 0.08 \\ \hline \\ \\ \\ \hline \\ \\ \\ \\ \hline \\ \\ \\ \\ \\ \\ \hline \\$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

From the mock spectroscopic catalogues we derived volumelimited subsamples with cuts in blue absolute magnitude and stellar mass corresponding to the observed ones. First of all, these mocks were used to test the effect of the gaps in the survey. As VIMOS is made of four quadrants  $7 \times 8$  separated by 2 arcmin, characteristic cross-shaped gaps are left in the survey; a further gap is present between the rows of pointings at different declination; finally, there are a few missing quadrants due to failed pointings. Cells whose projection on the sky includes a gap can potentially miss some galaxies, which affects final counts.

These gaps might be avoided by conservatively only counting galaxies in the cells that are completely included in one single quadrant, but in this way, only small scales would be sampled (the exact value obviously depends on the cell distance but it is generally lower than  $R \sim 5 h^{-1}$  Mpc). Alternatively, the counts in each cell might be associated with the effective volume of the cell, subtracting the volume falling into the gaps; but this less drastic choice, which would slightly alter the shape of the cells, would still limit the range of the sampled scales.

Another option would be filling the gaps. Cucciati et al. (2014) applied two algorithms that use the photometric redshift information and assign redshifts to galaxies based upon the spectroscopic redshifts of the nearest neighbours. In this way, it is also possible to take into account the varying completeness from field to field. Tests on mocks have shown that these algorithms are successful in reconstructing the lowest and highest density environments at a scale of 5  $h^{-1}$  Mpc, but not in recovering the count PDF and its moments due to systematic biases.

We therefore here adopted another solution. The tests on mocks have shown that when cells are not allowed to cross the gaps by more than 40% of their volume, the non-observed regions and the varying sampling rate can be approximated by a random Poisson sampling, and the original count PDF can be recovered with good precision (Bel et al., in prep.). This means that to obtain good estimates of the quantities we discuss here (*J*-point correlations and normalized moments), which depend

on the density contrast  $\Delta \rho / \rho$ , it is sufficient to implement the restriction on the volume of the cells falling into the gaps.

In our analysis, we conservatively only considered spherical cells for which no more than 30% of the volume falls in a gap. Moreover, to improve the statistics, we combined the counts of the W1 and W4 fields.

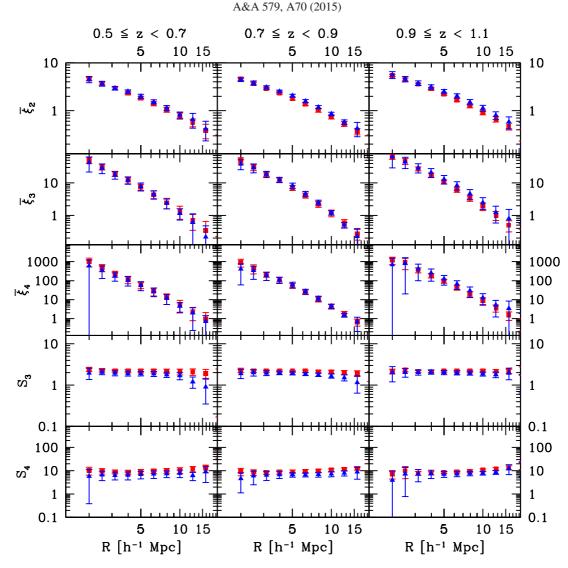
In Fig. 1 we show the results obtained from the analysis of mock subsamples limited at  $M_B(z = 1.1) - 5 \log(h) \le -20.5$  in the three redshift bins [0.5, 0.7], [0.7, 0.9], [0.9, 1.1]. We compare the ideal case with 100% completeness and no gaps to the more realistic case with gaps and the same spectroscopic incompleteness as in our observed catalogue, that is, including the effects of the target sampling rate, TSR(Q), and the spectroscopic sampling rate, SSR(Q), where Q indicates the quadrant dependence.

Two other selection effects were not taken into account: the colour sampling rate, CSR(z), and the small-scale bias due to the constraints in the spectroscopic target selection (slits cannot overlap). The first effect depends on redshift but it is weak in our redshift range (see Fig. 5 of Guzzo et al. 2014), while the second effect is negligible because the angular radii of our cells are generally larger than the size of one quadrant.

We note that other sources of systematic errors, as discussed by Hui & Gaztañaga (1999), are the integral constraint bias, affecting the *J*-point correlation functions, and the ratio bias, affecting the estimate of  $S_J$ . Given the large size of our volumes, such systematic effects are weaker than the other errors, however, and can be neglected.

Figure 1 shows that the original values are recovered with good precision (within  $1\sigma$  error), particularly in the scale range between 4 and  $10 h^{-1}$  Mpc.

A more detailed analysis of the differences is possible with Fig. 2, which gives the fractional difference for  $\overline{\xi_2}$ ,  $\overline{\xi_3}$ ,  $\overline{\xi_4}$ ,  $S_3$ , and  $S_4$  as a function of scale for the same mock subsamples as in Fig. 1: it shows that in most cases we can retrieve the *J*-point correlation functions and  $S_J$  with only a small systematic difference. In the first redshift bin  $(0.5 \le z < 0.7)$  at a radius  $R = 8 h^{-1}$  Mpc,  $\overline{\xi_2}$  is overestimated by 8%, while  $\overline{\xi_3}$  is



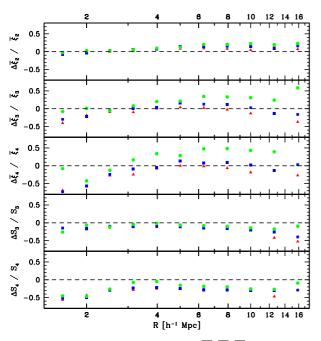
**Fig. 1.** Comparison between mock catalogues with a sampling rate of 100% and without gaps (red triangles), and with a sampling rate and gaps as in VIPERS (blue triangles). The subsamples are limited at  $M_B(z = 1.1) - 5 \log(h) \le -20.5$ . From top to bottom: volume-averaged two-, three-, and four-point correlation functions, normalized skewness  $S_3$  and kurtosis  $S_4$  in redshift space. First column:  $0.5 \le z < 0.7$ ; second column:  $0.7 \le z < 0.9$ ; third column:  $0.9 \le z < 1.1$ .

underestimated by 3% and  $\overline{\xi_4}$  by 6%: this translates into an underestimate of  $S_3$  by 16% and of  $S_4$  by 26%. We have similar values in the second redshift bin (0.7  $\leq z <$  0.9). In the last redshift bin (0.9  $\leq z <$  1.1) the *J*-point correlation functions show the largest difference, increasing with order *J*: but these deviations at different orders are correlated, so that finally the value of  $S_3$  at 8  $h^{-1}$  Mpc is underestimated by only 10% and of  $S_4$  by 20%, which is comparable to what is found for the other two redshift bins. The cause of the larger deviations in the last redshift bin is the lower density of the subsample; we take these systematics into account in the discussion of our results.

It is interesting to point out that we find values between 1.8 and 2.1 for  $S_3$  and between 8 and 10 for  $S_4$  for mocks; as an example, the analysis of the mock subsamples limited at  $M_B(z = 1.1) - 5 \log(h) \le -20.5$  in the redshift bin [0.7, 0.9] gives  $S_3 \sim 2.13 \pm 0.16$  and  $S_4 \sim 9.8 \pm 1.6$  at  $R = 8 h^{-1}$  Mpc.  $S_3$ and  $S_4$  show no significant redshift evolution, and their values are also comparable within the errors to the value measured in local redshift surveys for galaxies in a similar luminosity range.

Because we know both the cosmological and the "observed" redshift for galaxies in the mock samples, including the peculiar velocity and measurement error, we can estimate the conversion factor from redshift to real space from the mock samples. We need this factor to compare our results with secondorder perturbation theory predictions. Figure 3 shows the difference between the estimates in real and redshift space for the subsamples limited at  $M_B(z = 1.1) - 5\log(h) \le -20.5$  in the three redshift ranges. The redshift space correlation functions show the expected loss of power at small scales and the reverse trend at large scales. The estimate of the volume-averaged twopoint correlation function in redshift space is flatter than the corresponding estimate in real space; the difference becomes significant on scales smaller than  $\sim 4 h^{-1}$  Mpc. While the real space values of  $S_3$  and  $S_4$  increase at smaller scales, the increase is suppressed in redshift space; the difference becomes small beyond  $\sim 4 h^{-1}$  Mpc. However, at small scales we have large errors due to the small number of objects in the cells. For these reasons we focus our analysis on the 4–10  $h^{-1}$  Mpc range, and particularly at  $8 h^{-1}$  Mpc, where we expect to be in the quasi-linear regime and predictions of second-order perturbation theory should hold.

We recall here another bias affecting mass-selected galaxy samples, which has been discussed and tested with mock catalogues by Marulli et al. (2013). The lowest stellar mass



**Fig. 2.** Fractional difference of the average  $\overline{\xi_2}$ ,  $\overline{\xi_3}$ ,  $\overline{\xi_3}$ ,  $S_3$  and  $S_4$  (from top to bottom) for the same set of mock catalogues as defined in Fig. 1, i.e. with 100% sampling rate and without gaps, and with sampling rate and gaps as in VIPERS. The subsamples are limited at  $M_B(z = 1.1) - 5 \log(h) \le -20.5$ . Red triangles:  $0.5 \le z < 0.7$ ; blue squares:  $0.7 \le z < 0.9$ ; green hexagons:  $0.9 \le z < 1.1$ .

subsamples suffer from incompleteness because VIPERS is magnitude limited ( $i_{AB} < 22.5$ ); as a consequence, we can miss high mass-to-light ratio galaxies. From the analysis of mocks, Marulli et al. (2013) found that these galaxies are faint and red and that the clustering amplitude can be suppressed up to 50% on scales below 1  $h^{-1}$  Mpc. However, as discussed by Marulli et al. (2013), the abundance of red and faint galaxies is overpredicted by the semi-analytic model used for the tests, and the clustering of red galaxies appears to be overestimated with respect to real data (de la Torre et al. 2011; Cucciati et al. 2012), so that the amplitude of the effect might be overestimated. As we have previously noted, we did not analyse small scales and did not correct for stellar mass incompleteness.

#### 5. Results

#### 5.1. Volume-averaged correlation functions

In this section we present the results of our statistical analysis on the combined *W*1 and *W*4 samples.

Figure 4 shows the volume-averaged two-point correlation function obtained from counts in cells for luminosity- and stellar mass-limited subsamples in the three different redshift bins.

In the same figure, as a reference for comparing the results in the different redshift bins, we plot the expected real space power-law  $\overline{\xi_2}$  in the redshift bin [0.5, 0.7] for the  $M_B(z = 1.1) - 5 \log(h) \le -20.5$  subsamples (top panels) and  $M_* \ge 10.0 M_{\odot}$  (bottom panels), derived from the  $\xi_2$  estimate of Marulli et al. (2013); we converted their two-point correlation function to the volume-averaged correlation function through the formula (Peebles & Groth 1976):

$$\overline{\xi}_2 = \frac{72}{2^{\gamma}(3-\gamma)(4-\gamma)(6-\gamma)}\xi_2.$$
(17)

The line shows the effects of redshift space distortions, which lower the value of  $\overline{\xi}_2$  on small scales and increase it on large scales.

It is clear that the amplitude of  $\overline{\xi}_2$  increases with both luminosity and stellar mass at all redshifts.  $\overline{\xi}_2$  appears to have a stronger dependence on stellar mass than on luminosity, in agreement with the results of Marulli et al. (2013): see their Fig. 3 for the redshift space two-point correlation functions.

There are some fluctuations: for example, the dependence on luminosity appears to be slightly weaker in the intermediate and distant redshift bins. However, these variations are consistent when taking into account statistical errors and sample variance, which are included in error bars. We conclude that the dependence of the two-point correlation function on luminosity and stellar mass does not evolve significantly up to  $z \sim 1$ .

In Figs. 5 and 6 we show the volume-averaged three- and four-point correlation functions. Their behaviour reflects the two-point correlation functions, showing a stronger dependence of the correlation amplitude on stellar mass than on luminosity.

The specific signature of the hierarchical scaling is the power-law relation between high-order correlation functions (Eq. (10)). In Figs. 7 and 8 we show the three- and four-point volume-averaged correlation functions as a function of the two-point volume-averaged correlation functions. The data clearly follow the hierarchical scaling relations  $\overline{\xi}_3 \propto \overline{\xi}_2^2$  and  $\overline{\xi}_4 \propto \overline{\xi}_2^3$ . These relations appear to hold at all luminosities and masses in the the first two redshift bins, but some systematic differences appear in the last redshift bin, particularly for the stellar-mass limited subsamples, where points are systematically higher than the reference scaling law, but in this case the values are also consistent with the same scaling relation observed at lower redshifts.

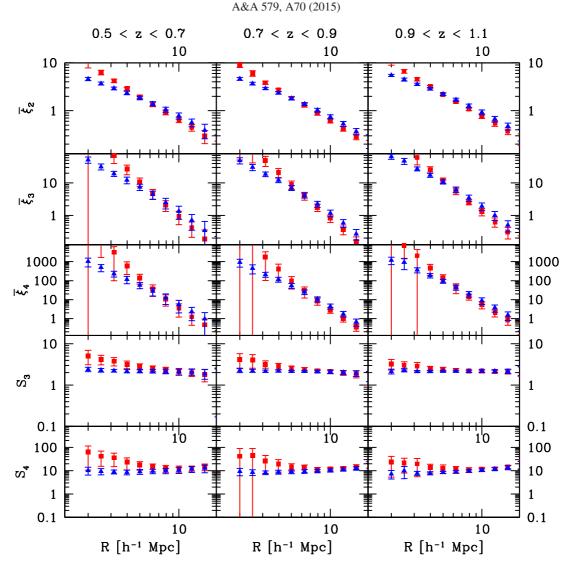
As we have previously discussed, the existence of these scaling relations has been verified in the local Universe: they are expected for the matter distribution in the quasi-linear regime, as a consequence of gravitational clustering. In this case, it is natural that they do not evolve with redshift: however, it is not an obvious result to observe the same hierarchical behaviour for the galaxy distribution at all redshifts, given the evolution of bias.

#### 5.2. Skewness and kurtosis

From the counts in cells we derived the rms  $\sigma$  (Eq. (3)), the normalized skewness  $S_3$  and kurtosis  $S_4$  (Eq. (11)) for the different VIPERS subsamples. Their values at  $R = 8 h^{-1}$  Mpc are given in Cols. 4–6 of Table 1. The  $R = 8 h^{-1}$  Mpc reference radius is nearly optimal because it is large enough to enter into the quasilinear regime, and at the same time it is in the scale range for which we have a good sampling.

In Figs. 9 and 10 we show  $S_3$  and  $S_4$  as a function of luminosity and stellar mass in the three redshift bins. We also show the predictions of second-order perturbation theory in real space for the matter distribution and the corresponding predictions for galaxies, derived from the matter value assuming the linear bias estimated from  $\overline{\xi_2}$ , and corrected for redshift space distortion using the factors obtained from mocks. This derivation is described in the next subsection. The theoretical curves for  $S_3$  and  $S_4$  are shown for radii larger than  $\sim 6 h^{-1}$  Mpc, as they are calculated in the quasi-linear regime.

In the first redshift bin, both for luminosity and stellar mass limited samples, the value of  $S_3$  is constant and around 2 at small and intermediate scales, but it starts decreasing beyond  $R \sim 8 h^{-1}$  Mpc. In principle, variations of  $S_3$  with scale can be due to changes in the slope of the power spectrum or to



**Fig. 3.** Comparison between mock catalogues with 100% sampling rate and without gaps in real space (red squares) and redshift space (blue triangles). The subsamples are limited at  $M_B(z = 1.1) - 5\log(h) \le -20.5$ . First column:  $0.5 \le z < 0.7$ ; second column:  $0.7 \le z < 0.9$ ; third column:  $0.9 \le z < 1.1$ .

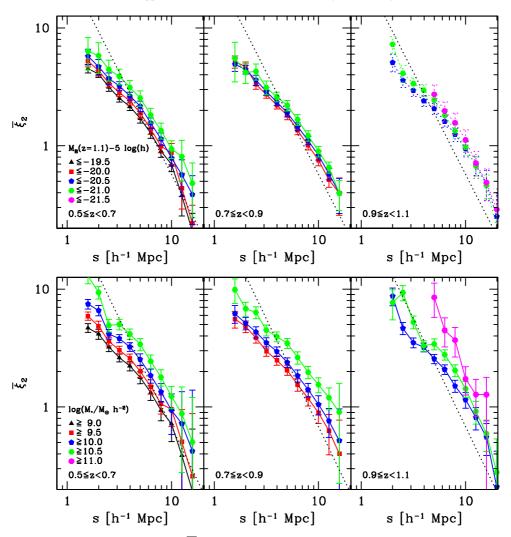
a scale-dependent bias. However, such a systematic effect can be ascribed to the small number of independent cells at large scales, as shown by mocks and reflected in the large error bars. In the same redshift bin,  $S_4$  shows a small decrease at large scales and is consistent with a constant value of ~7.3 between 4 and 10  $h^{-1}$  Mpc. In the range  $6-8 h^{-1}$  Mpc, the best scales to compare with perturbation theory (on larger scales the errors increase significantly), the theoretical predictions for  $S_3$  and  $S_4$ are slightly higher than the observed values corresponding to the  $M_B(z = 1.1) - 5 \log(h) \le -20.5$  subsample, but only at  $1\sigma$  level.

In the second redshift bin the value of  $S_3$  for luminositylimited subsamples is around 1.8, sligthly lower than in the first bin, but still consistent within the errors; moreover, it is consistent with a constant value in the whole range of scales. The value of  $S_3$  for mass-limited subsamples is also constant in the whole range of scales and is consistent with the value in the first redshift bin.  $S_4$  has an analogous behaviour: while showing a systematic decrease, particularly in luminositylimited subsamples, it is still consistent with a constant value in the range  $4-16 h^{-1}$  Mpc. As in the case of the first redshift bin, in the range  $6-8 h^{-1}$  Mpc the theoretical predictions for  $S_3$  and  $S_4$  are slightly higher than the corresponding observed values. In the third redshift bin the values of  $S_3$  and  $S_4$  for luminosity- and stellar-mass-limited subsamples increase systematically with scale. Moreover, in contrast with the two previous redshift bins, in the range 6–8  $h^{-1}$  Mpc, the theoretical predictions for  $S_3$  and  $S_4$  are lower than the observed values.

To better appreciate the significance of these deviations, we note that of 26 mocks, 3 show an increase of the values of  $S_3$  and  $S_4$  similar to what we find in the last redshift bin.

In fact, higher-order statistics are very sensitive to large-scale structure, and the correlated variations in the measured values of  $S_3$  and  $S_4$  probably indicate genuine fluctuations in the galaxy distribution (see e.g. the discussion in Croton et al. 2004b).

In our case, this interpretation is suggested by checking the W1 and W4 fields separately: we find that in the outermost redshift shell, both  $S_3$  and  $S_4$  are larger in W1 than in W4. For example, for the  $M_B(z = 1.1) - 5\log(h) \le -21.0$  subsample, at  $R = 8 h^{-1}$  Mpc, we find  $S_3 = 2.7 \pm 0.5$  in W1 and  $S_3 = 1.6 \pm 0.3$  in W4. Analogously, for the  $\log(M/M_{\odot}h^{-2}) \ge 10.5$  subsample at  $R = 8 h^{-1}$  Mpc, we find  $S_3 = 3.4 \pm 0.5$  in the W1 field and  $S_3 = 2.0 \pm 0.3$  in the W4 field. This difference might be regarded as the imprint of spatially coherent structures more prominent in W1.



**Fig. 4.** Volume-averaged two-point correlation functions  $\overline{\xi_2}$  as a function of the *B* absolute luminosity (*upper panels*) and stellar mass (*lower panels*). The limits of the subsamples in absolute magnitude and stellar mass are shown in the *left upper* and *lower panels*. Black triangles:  $M_B(z = 1.1) - 5 \log(h) \le -19.5 (\log(M_*/M_{\odot}h^{-2} \ge 9.0 M_{\odot})$ ; red squares:  $M_B(z = 1.1) - 5 \log(h) \le -20.0 (\log(M_*/M_{\odot}h^{-2} \ge 9.5 M_{\odot})$ ; blue pentagons:  $M_B(z = 1.1) - 5 \log(h) \le -21.0 (\log(M_*/M_{\odot}h^{-2} \ge 10.5 M_{\odot})$ ; magenta heptagons:  $M_B(z = 1.1) - 5 \log(h) \le -21.5 (\log(M_*/M_{\odot}h^{-2} \ge 10.5 M_{\odot})$ ; magenta heptagons:  $M_B(z = 1.1) - 5 \log(h) \le -21.5 \log(h) \le -21.5 \log(h) \le -20.5 (\log(M_*/M_{\odot}h^{-2} \ge 10.5 M_{\odot})$ ; predicted from the power-law fit of  $\xi_2$  in Marulli et al. (2013).

In conclusion, the values of  $S_3$  and  $S_4$  do not show any significant dependence on luminosity or on stellar mass: the points corresponding to different subsamples are consistent within the error bars (we discuss a possible weak dependence on luminosity in the next subsection). There is no evidence of evolution in redshift either, apart from the systematic increase of  $S_3$  and  $S_4$ with scale in the last redshift bin.

Taking into account the behaviour of mocks, the observed systematic variations in the values of high-order moments are consistent with the fluctuations expected for comparable volumes randomly extracted from a ACDM universe.

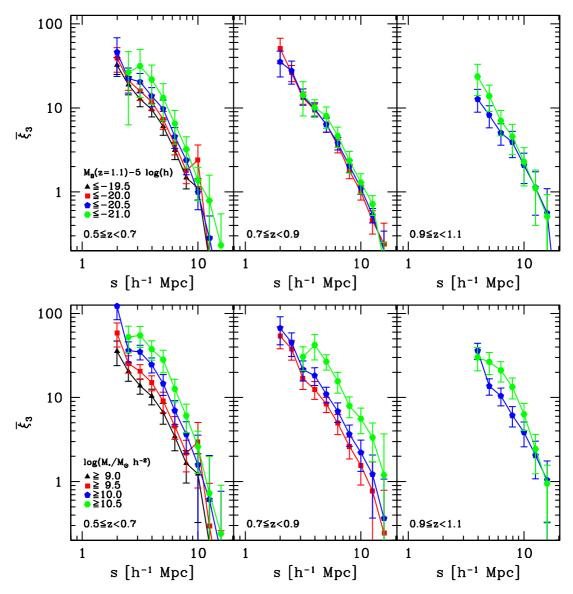
It is possible to compare our results on  $S_3$  and  $S_4$  with those obtained by Wolk et al. (2013) for the four CFHTLS-Wide fields. They have divided the galaxies in the photometric catalogue into four redshift bins through the estimated photometric redshifts; for galaxies with  $M_g < -20.7$ , they have estimated  $S_J$  as a function of angular scale and the corresponding 3D values through deprojection, which, as they discussed, rely on some approximations. Their work is therefore complementary to ours: they have a larger area and number of objects, but we can directly estimate the 3D (redshift space)  $S_J$ ; they can sample smaller, highly non-linear scales where we do not have enough statistics, but we can better sample the quasi-linear scales; finally, we can also test the dependence of  $S_3$  on luminosity and stellar mass.

A comparison with their Fig. 12 shows that, as expected (see our Fig. 3), their deprojected values for  $S_3$  and  $S_4$  on small scales ( $R < 5 h^{-1}$  Mpc) are higher than our redshift space values. On larger scales, the redshift space effect on  $S_3$  and  $S_4$  becomes negligible, and their estimate is consistent with ours.

We note that Wolk et al. (2013) found significant deviations in the results for the W3 field, while we have found differences between W1 and W4 in our last redshift bin: this shows that sample variance is still significant for high-order statistics on the scale of CFHTLS Wide Fields.

#### 5.3. Implications for biasing

We now discuss the implications of our analysis for biasing. We concentrate on the reference scale  $R = 8 h^{-1}$  Mpc, where second-order perturbation theory predictions can be applied and results are still reliable (errors and systematic deviations increase on larger scales). Because we aim to compare our results with the



**Fig. 5.** Volume-averaged three-point correlation functions as a function of the *B* absolute luminosity (*upper panels*) and stellar mass (*lower panels*). The limits of the subsamples in absolute magnitude and stellar mass are shown in the *left upper and lower panels* (symbols and colours are the same as in Fig. 4).

matter density field, statistical quantities referring to galaxies are indicated with a subscript g and those relative to matter with a subscript m.

Figure 11 shows the values of  $\sigma_{8g}$  (top panel) and  $S_{3g}$  (bottom panel) at  $R = 8 h^{-1}$  Mpc for the VIPERS volume-limited subsamples with different limiting absolute magnitudes and in the different redshift bins. In the same figure we also show the corresponding VVDS estimates (Marinoni et al. 2005) and the 2dFGRS estimates for the local Universe (Croton et al. 2004b) for galaxies with a similar luminosity as ours.

At a given redshift, VIPERS subsamples with a brighter absolute magnitude limit have higher values of  $\sigma_{8g}$ , but there is no significant evolution of  $\sigma_{8g}$  with redshift. The same holds when combining our results with those of the 2dFGRS in the local Universe and those of the VVDS at higher redshift:  $\sigma_{8g}$  shows no significant evolution from z = 0 to z = 1.4 (VVDS points are systematically lower but at the  $1\sigma$  level). This implies (see e.g. the discussion in Marinoni et al. 2005) a strong evolution of the linear bias b with redshift because  $\sigma_{8m}$  increases with time (see Eq. (13)). There are various models that describe the evolution of b(z) and explain its decrease with time (see e.g. Blanton et al. 2000); from an empirical point of view, we note that the available data can be fitted by the simple relation  $b(z) \propto 1/\sigma_{8m}$ .

The skewness  $S_{3g}$  of the VIPERS subsamples measured at  $8 h^{-1}$  Mpc and plotted as a function of redshift has more fluctuations than  $\sigma_{8g}$ , with a minimum value in the redshift bin [0.7,0.9], but it does not show a significant dependence on luminosity and is still consistent with a constant value independent of redshift. The values of  $S_{3g}$  in the VVDS below z = 1.2 are lower than VIPERS values, but are consistent within the errors, while they start to decrease beyond  $z \sim 1.1$ .

The absence of a significant evolution of  $S_{3g}$  with redshift is not limited to our redshift range: the values of  $S_{3g}$  measured in VIPERS are similar to those measured in the 2dFGRS, that is,  $S_3 \sim 2.0 \pm 0.2$ , where depending on the subsample  $S_{3g}$  varies from 1.95 to 2.58 (while not shown in the figure, the values of  $S_4$  are also consistent with the 2dFGRS ones). Therefore, taking into account all data points, starting from the local value for the 2dFGRS up to z = 1.1 (VIPERS and VVDS data),  $S_{3g}$  is consistent with a constant value ~2: in VIPERS

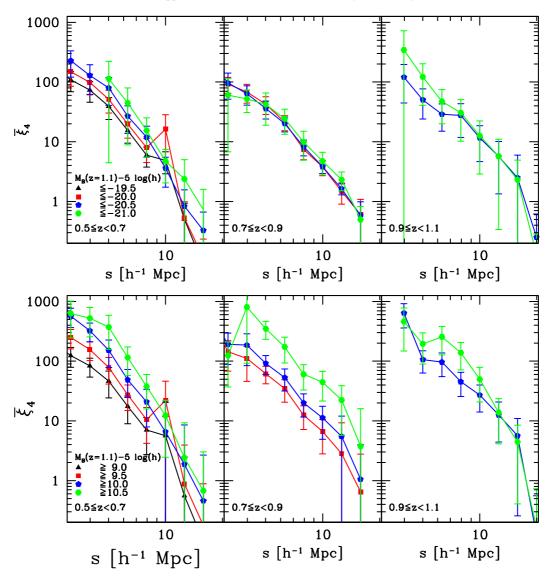


Fig. 6. Volume-averaged four-point correlation functions as a function of the *B* absolute luminosity (*upper panels*) and stellar mass (*lower panels*). The limits of the subsamples in absolute magnitude and stellar mass are shown in the *left upper* and *lower panels* (symbols and colours are the same as in Fig. 4).

the strongest but marginal deviations of the  $S_{3g}$  value are for  $M_B(z = 1.1) - 5\log(h) \le -20.0$  galaxies in the nearest redshift range [0.5, 0.7] and for  $M_B(z = 1.1) - 5\log(h) \le -21.0$  galaxies in the most distant redshift interval [0.9, 1.1], both giving a value of  $S_{3g}$  that is 15% higher.

Figure 12 shows  $\sigma_{8g}$  (top panel) and  $S_{3g}$  at 8  $h^{-1}$  Mpc (bottom panel) as a function of absolute magnitude for the three redshift bins.  $\sigma_{8g}$  shows a systematic increase with luminosity (reflecting the dependence of the correlation amplitude on luminosity), but at a given absolute luminosity its value is similar in the three redshift bins.

 $S_{3g}$  appears to be independent of absolute magnitude, with fluctuations from sample to sample. However, if we exclude the points relative to the last redshift bin, where  $S_{3g}$  has a higher value, the data might suggest a small decrease of  $S_{3g}$  with increasing luminosity, reminiscent of the results of Croton et al. (2004b) for the 2dFGRS.

A trend of  $S_{3g}$  with luminosity is interesting because in the hypothesis of linear biasing,  $S_{3g}$  is inversely proportional to the bias factor *b*: knowing from the two-point correlation function

of our samples that *b* increases with luminosity, we expect a corresponding decrease of  $S_{3g}$ .

To test whether our results are consistent with the linearity of bias, we therefore estimated the bias of galaxies with respect to the underlying matter density field at  $R = 8 h^{-1}$  Mpc, using the observed  $\sigma_{8g}$  and  $S_{3g}$  of the galaxy distribution and estimating  $\sigma_m$  and  $S_{3m}$  of the matter distribution through perturbation theory.

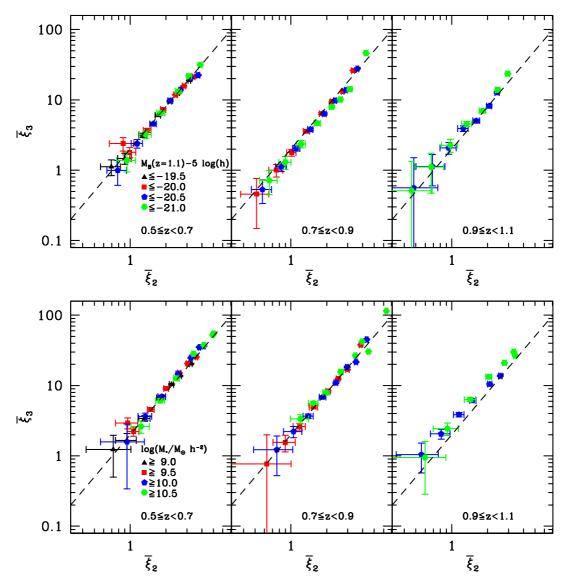
Juszkiewicz et al. (1993) and Bernardeau (1994a, 1994b; see also Bernardeau et al. 2002, and references therein) have shown that for a smoothed density field with primordial Gaussian fluctuations, Peebles' unsmoothed value of  $S_{3m} = 34/7$  (Peebles 1980) has to be corrected according to the expression

$$S_{3m} = 34/7 + d\ln \sigma_m^2 / d\ln R,$$
 (18)

where  $d\ln \sigma_m^2/d\ln R$  is the logarithmic slope of the linear variance of the matter density field smoothed with a spherical tophat function of radius *R*,

$$\sigma_{\rm m}^2(R) = \frac{1}{2\pi^2} \int_0^\infty {\rm d}k k^2 P(k) W^2(kR).$$
(19)

A70, page 11 of 18



**Fig. 7.** Scaling relation of the volume-averaged two- and three-point correlations as a function of the *B* absolute luminosity (*upper panels*) and stellar mass (*lower panels*). The limits of the subsamples in absolute magnitude and stellar mass are shown in the *left upper and lower panels* (symbols and colours are the same as in Fig. 4). The dashed line represents the scaling relation  $\log_{10}(\overline{\xi}_3) = 2\log_{10}(\overline{\xi}_2) + \log_{10}(2)$ .

For a power-law spectrum  $P(k) \propto k^n$ , Eq. (18) becomes  $S_{3m} = 34/7 - (n+3)$ .

Similar relations hold for higher orders, involving higherorder derivatives.

The values obtained from perturbation theory have been tested with numerical simulations, and it has been shown that in the range we are studying, that is, at  $R = 8 h^{-1}$  Mpc and for  $\sigma_{8m} \sim 1$ , they are very accurate: for example, the difference in the  $S_3$  values is smaller than a few percent (Baugh et al. 1995; Fosalba & Gaztanaga 1998; Bernardeau et al. 2002).

Applying Eqs. (18) and (19) and using the software CAMB (Lewis & Bridle 2002), we have computed the values of  $\sigma_{8m}$  and  $S_{3m}$  for a power spectrum with the new cosmological parameters derived from the *Planck* mission (Planck Collaboration XVI 2014) and with the old Millennium parameters (first year WMAP data and 2dFGRS, with  $\Omega_{M} = 0, 25, \Omega_{\Lambda} = 075, n = 1$  and  $\sigma_{8m} = 0.9$ ).

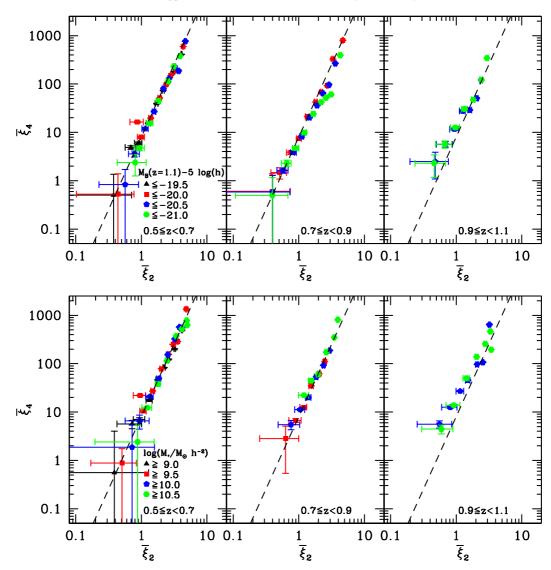
We here assumed that the standard  $\Lambda$ CDM model is correct. With other assumptions, such as a dark energy component with

an evolving equation of state or modified gravity, the clustering and bias evolution would be affected (see e.g. Munshi et al. 2004), as would the redshift distortions (Hellwing et al. 2013). This dependence on cosmology will be studied in a future work.

We also converted the observed  $\sigma_{8g}$  and  $S_{3g}$  to real space values by applying correction factors directly derived from the mocks.

For the subsample limited at  $M_B(z = 1.1) - 5 \log(h) \le -20.50$ , we give in Table 2 the redshift range (Col. 1), the values of  $\sigma_{8g}$  (Col. 2),  $\sigma_{8m}$  (Col. 3),  $b = \sigma_{8g}/\sigma_{8M}$  (Col. 4),  $S_{3g}$  (Col. 5),  $S_{3m}$  (Col. 6), all measured at a scale of  $R = 8 h^{-1}$  Mpc.

In Fig. 13 we plot our estimates for the linear bias term b as a function of redshift, with the correponding estimates for VIPERS of Marulli et al. (2013) and Di Porto et al. (2014). As expected, the estimates are fully consistent, with b increasing with luminosity and redshift. As discussed by Di Porto et al. (2014), there is only a difference in the last redshift bin where the estimate of Marulli et al. is lower than that of Di Porto et al. (2014). The difference is probably due to the way b is estimated



**Fig. 8.** Scaling relation of the volume-averaged two and four-point correlations as a function of the *B* absolute luminosity (*upper panels*) and stellar mass (*lower panels*). The limits of the subsamples in absolute magnitude and stellar mass are shown in the *left upper and lower panels* (symbols and colours are the same as in Fig. 4). The dashed line represents the scaling relation  $\log_{10}(\overline{\xi}_3) = 3 \log_{10}(\overline{\xi}_2) + \log_{10}(8)$ .

(counts in cells in our case and in Di Porto et al. 2014, pair counts in Marulli et al. 2013). Our estimate is consistent with both the other two estimates at the  $1\sigma$  level, however.

In Fig. 14 we compare the linear bias directly measured from the ratio of the galaxy and matter rms,  $b = \sigma_{8g}/\sigma_{8m}$ , with the ratio of the galaxy and matter skewness,  $S_{3m}/S_{3g}$ . Under the hypothesis of linear biasing, the two ratios should have the same value. For the first two redshift bins we find slightly different values: the skewness ratio is systematically higher than the bias directly computed from the variance. The third redshift bin shows the largest discrepancy, but with the opposite behaviour, that is, the skewness ratio is lower than the bias directly computed from the variance. This different behaviour is a consequence of the fact that the value of  $S_{3g}$  in the last redshift bin increases with scale and becomes higher than at lower redshifts.

We can quantify the degree of non-linearity by directly estimating the second-order term  $b_2$  from Eq. (16):

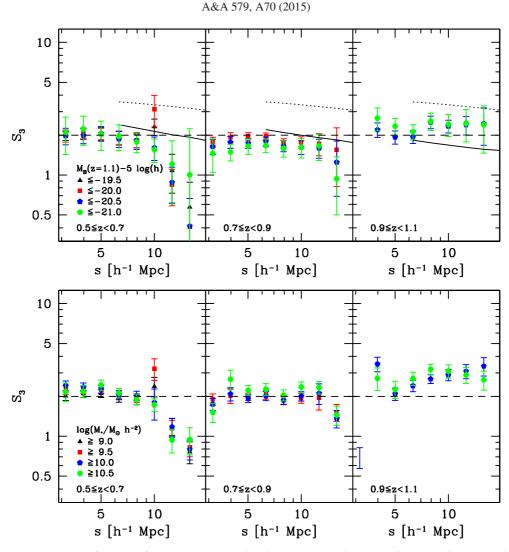
$$b_2 = b(bS_{3g} - S_{3m})/3, \tag{20}$$

where we used the real space values  $S_{3g}$  and *b* obtained from the redshift space values by using the conversion factor calculated

from the mocks. We note that this correction is small (a few percent) at our scale of  $R = 8 h^{-1}$  Mpc, because this scale is at the transition from the regime of small-scale velocity dispersion (where redshift space correlation functions are lower than real space ones) to the regime of infall where redshift space correlations are higher than real space ones (see Fig. 3).

In this formalism, if b > 0,  $b_2$  is negative when  $\sigma_{8g}/\sigma_{8m} < S_{3m}/S_{3g}$ . This is what happens in the first two redshift bins, where at nearly all magnitudes  $b_2$  is negative: for example, for the subsample limited at  $M \le -20.5(z = 1.1) - 5\log(h)$ , we find  $b_2 = -0.20 \pm 0.49$  in the first redshift bin and  $b_2 = -0.24 \pm 0.35$ , in the second redshift bin. In contrast, we find a positive  $b_2$  in the third bin, with  $b_2 = +0.78 \pm 0.82$ .

As we have noted above when discussing the results of our tests on mocks, the assumption that masked regions and inhomogeneities can be described as a Poissonian random sampling gives a small bias with an overestimate of *b* of a few percent and an underestimate of  $S_3$  around 10–15%. Using the correction factors derived from the average of the mocks, we find for the subsample limited at  $M \le -20.5(z = 1.1) - 5 \log(h)$  $b_2 = -0.03 \pm 0.49$  in the first redshift,  $b_2 = -0.25 \pm 0.35$  in the



**Fig. 9.** Normalized skewness  $S_3$  as a function of the *B* absolute luminosity (*upper panels*) and stellar mass (*lower panels*). The limits of the subsamples in absolute magnitude and stellar mass are shown in the *left upper* and *lower panels* (symbols and colours are the same as in Fig. 4). We note that black points corresponding to galaxies with M < -19.50 or  $M_* \ge 9.0 M_{\odot}$  are only plotted for the first redshift bin ([0.5, 0.7]), but most of them are not visible as they lie below the points of the other samples. The dashed line corresponds to  $S_3 = 2$ . In the *top panels*, the dotted line is the prediction from second-order perturbation theory for the matter distribution in real space; the solid line is the prediction of  $S_3$  for galaxies with  $M_B(z = 1.1) - 5\log(h) \le -20.5$  (to be compared to blue pentagons): it was obtained from the matter values, converted to redshift space and divided by the corresponding linear bias factor.

second redshift bin, and  $b_2 = +0.72 \pm 0.82$  in the third bin. The differences are well within  $1\sigma$  error.

It would be tempting to interpret these results as suggesting a possible evolution of the non-linear bias  $b_2$  with redshift, with a similar trend, for example, as for the model of Sefusatti & Komatsu (2007). Unfortunately, the problem is the extreme sensitivity of  $b_2$  to the errors on b and  $S_{3g}$ , amplified by a factor  $b^2$ , and we have seen that subsamples in the last redshift bin are affected by larger errors and systematic trends.

With these caveats, we can check the consistency of our results with other works in the same redshift and luminosity ranges. In this comparison, one has to take into account the sensitivity of  $b_2$  to the different methods and, as pointed out by Kovač et al. (2011), to sample variance. In fact, even local measurements of the non-linear term have given different values (see e.g. Verde et al. 2002 and Pan & Szapudi 2005, and the discussion in Gaztañaga et al. 2005 and Marinoni et al. 2008).

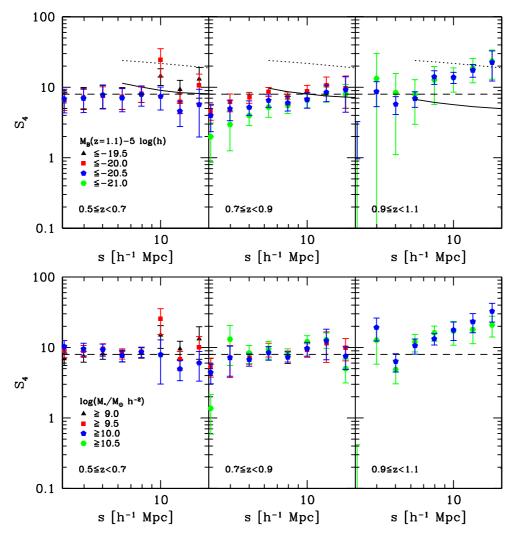
First of all, Di Porto et al. (2014) have analysed the VIPERS data reconstructing the bias relation from the estimate of the

probability distribution function: they found a small (<3%) but significant deviation from linear bias.

In their analysis of the four CFHTLS Wide fields, Wolk et al. (2013) have found that perturbation theory predictions agree well with their measurements when taking into account the linear bias, but note that there is still a small discrepancy that can be explained by the presence of a non-linear bias term. This is also consistent with what we found.

Marinoni et al. (2005) have analysed VVDS volume-limited samples limited at  $M_B < -20 + 5 \log(h)$  (this limit was fixed and did not take into account luminosity evolution) in the redshift bins 0.7 < z < 0.9 and 0.9 < z < 1.1, finding  $b_2 = -0.20 \pm 0.08$  and  $b_2 = -0.12 \pm 0.08$  (here the errors do not include sample variance): these values are consistent with ours below z = 1.

Kovač et al. (2011) analysed the *z*COSMOS galaxy overdensity field and estimated the mean biasing function between the galaxy and matter density fields and its second moment, finding a small non-linearity, with the non-linearity parameter  $\tilde{b}/\hat{b}$ (defined in the formalism of Dekel & Lahav 1999) at most 2% with an uncertainty of the same order.



**Fig. 10.** Normalized skewness  $S_4$  as a function of the *B* absolute luminosity (*upper panels*) and stellar mass (*lower panels*). The limits of the subsamples in absolute magnitude and stellar mass are shown in the *left upper* and *lower panels* (symbols and colours are the same as in Fig. 4). We note that black points corresponding to galaxies with M < -19.50 or  $M_* \ge 9.0 M_{\odot}$  are only plotted for the first redshift bin ([0.5, 0.7]), but most of them are not visible as they lie below the points of the other samples. The dashed line corresponds to  $S_4 = 8$ . In the *top panels*, the dotted line is the prediction from second-order perturbation theory for the matter distribution in real space; the solid line is the prediction of  $S_4$  for galaxies with  $M_B(z = 1.1) - 5 \log(h) \le -20.5$  (to be compared to blue pentagons): it was obtained from the matter values, converted to redshift space and divided by the corresponding linear bias factor.

**Table 2.** Real space values of  $\sigma_8$  and  $S_3$  of galaxies with  $M_B(z = 1.1) - 5\log(h) \le -20.50$  vs. those expected from second-order perturbation theory (with Millennium and *Planck* cosmological parameters).

Redshift range	$\sigma_{8g}$	$\sigma_{8m}$	b	$S_{3g} (R = 8 h^{-1} \text{ Mpc})$	$S_{3m} \left( R = 8 h^{-1} \text{ Mpc} \right)$
	(real space)	(WMAP/Planck)	(linear bias)	(real space)	(WMAP/Planck)
$0.5 \le z < 0.7$	$1.00 \pm 0.12$	0.61/0.63	$1.65 \pm 0.20$	$1.91 \pm 0.29$	3.52/3.48
$0.7 \le z < 0.9$	$0.98 \pm 0.08$	0.55/0.57	$1.77 \pm 0.14$	$1.76 \pm 0.18$	3.52/3.48
$0.9 \le z < 1.1$	$1.04\pm0.13$	0.51/0.52	$2.04 \pm 0.27$	$2.28\pm0.25$	3.52/3.48

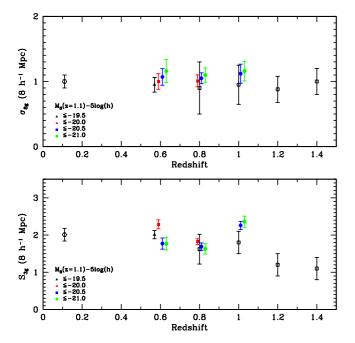
Gaztañaga et al. (2005) have found  $b = 0.93^{+0.10}_{-0.08}$  and  $c_2 = b_2/b = -0.34^{+0.11}_{-0.08}$  from the measurement of the  $Q_3$  parameter in the three-point correlation function of the 2dFGRS for the local Universe.

The non-linear term we have measured in the redshift interval between z = 0.5 and z = 0.9 is therefore similar to what has been measured in the above surveys. We conclude that there is general evidence for a small but non-zero non-linear  $b_2$  term. It is also clear that no evolution of  $b_2$  with redshift can be detected in the available data, in contrast to the linear bias term.

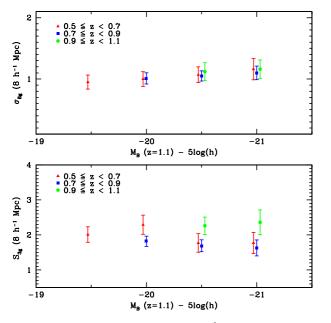
#### 6. Conclusions

We have analysed the high-order clustering of galaxies in the first release of VIPERS, using counts in cells to derive the volume-averaged correlation functions and normalized skewness  $S_{3g}$  and kurtosis  $S_{4g}$ . We have analysed volume-limited subsamples with different cuts in absolute magnitude and stellar mass in three redshift bins; these subsamples are the same as in Marulli et al. (2013).

Errors were estimated through a set of mock catalogues, derived from dark matter halo catalogues repopulated with the

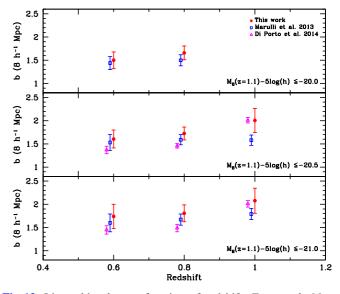


**Fig. 11.**  $\sigma_{8g}$ (*upper panel*) and  $S_{3g}$  (*lower panel*) as a function of redshift. Colours represent the different absolute magnitude limits as in previous figures. The open hexagon represents the corresponding value for 2dFGRS galaxies in the absolute magnitude  $M_{b_I}$  range [-21, -20] (Croton et al. 2004b). Black open squares are the values for VVDS galaxies brighter than  $M_B = -21$  (Marinoni et al. 2005). For better visibility, points corresponding to different redshifts are slightly shifted in magnitude.

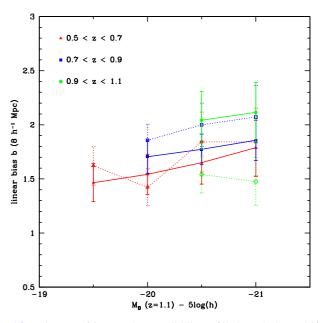


**Fig. 12.**  $\sigma_{8g}$  (*upper panel*) and  $S_{3g}$  at  $R = 8 h^{-1}$  Mpc (*lower panel*) as a function of galaxy luminosity for the three redshift bins. Red triangles:  $0.5 \le z < 0.7$ ; blue squares:  $0.7 \le z < 0.9$ ; green hexagons:  $0.9 \le z < 1.1$ . For better visibility, points corresponding to different redshifts are slightly shifted in magnitude.

method of de la Torre & Peacock (2013). The mocks were built to reproduce the properties of VIPERS, including masks and selection effects. Our analysis has shown that the high-order statistical properties of these mocks are consistent with observations.



**Fig. 13.** Linear bias *b* as a function of redshift. *Top panel*:  $M_B \leq -20.0(z = 1.1) + 5 \log(h)$ ; *middle panel*:  $M_B \leq -20.5(z = 1.1) + 5 \log(h)$ ; *bottom panel*:  $M_B \leq -21.0(z = 1.1) + 5 \log(h)$ . Red hexagons: our estimates of  $b = \sigma_{8g}/\sigma_{8m}$ . Blue squares: estimates of Marulli et al. (2013). Magenta triangles: Di Porto et al. (2014).



**Fig. 14.** Estimates of  $b = \sigma_{8g}/\sigma_{8m}$  (solid lines, filled symbols) and  $b' \equiv S_{3m}/S_{3g}$  (dotted lines, open symbols); b' = b under the assumption of linear bias. Red lines with triangles:  $0.5 \le z < 0.7$ ; blue lines with squares:  $0.7 \le z < 0.9$ ; green lines with hexagons:  $0.9 \le z < 1.1$ .

We also studied the dependence of the second- and thirdorder statistics of galaxy counts on the bias, deriving the linear bias term b and the first non-linear term  $b_2$ , and comparing our results with predictions from perturbation theory and with other works in the literature.

Here are our main conclusions.

- We showed that the hierarchical scaling relations  $\overline{\xi}_3 \propto \overline{\xi}_2^2$ and  $\overline{\xi}_4 \propto \overline{\xi}_2^3$  hold in the range of scales and redshifts we could sample, that is,  $3 \le R \le 10 h^{-1}$  Mpc and  $0.5 \le z < 1.1$ . These relations are consistent with predictions from gravitational clustering and with the scaling observed in local surveys.

- $S_{3g}$  and  $S_{4g}$  appear to be independent of luminosity; however, if we do not not take the last redshift bin into account, there is a slight decrease of  $S_{3g}$  with increasing luminosity, an effect previously detected locally in the 2dFGRS by Croton et al. (2004b).
- The values of  $S_{3g}$  and  $S_{4g}$  are scale-independent within the errors and do not evolve significantly at least up to z = 0.9. We detected a systematic increase with scale in the last redshift bin (beyond ~10  $h^{-1}$  Mpc), mainly due to one of the two CFHTLS fields (*W*1); this deviation is consistent with what can be expected from the sample variance shown by mock catalogues.
- The observed values of  $S_{3g} \sim 2 \pm 0.2$  and  $S_{4g} \sim 8 \pm 0.4$  are similar to those measured in local surveys for galaxies in the same luminosity range. This confirms the substantial absence of evolution of  $S_{3g}$  in the redshift range 0 < z < 1 at the level of ~10%. This result is expected for  $S_{3m}$ , but is not trivial for  $S_{3g}$ , given the evolution of bias.
- At second order, galaxies with higher luminosity or stellar mass have a larger amplitude (greater linear bias parameter) of the volume-averaged two-point correlation function, consistently with the direct analysis of the two-point correlation function by Marulli et al. (2013). We showed that our estimate of the linear bias parameter  $b = \sigma_{8g}/\sigma_{8m}$  is consistent within  $1\sigma$  with those of Marulli et al. (2013) and Di Porto et al. (2014). The linear bias increases both with luminosity and with redshift: in our redshift range, we measured the lowest bias  $b = 1.47 \pm 0.18$  for galaxies with  $M_B(z = 1.1) - 5\log(h) \le -19.5$  in the redshift bin  $0.5 \le z < 0.7$  and the largest bias  $b = 2.12 \pm 0.28$  for galaxies with  $M_B(z = 1.1) - 5\log(h) \le -21.0$  in the redshift bin  $0.9 \le z < 1.1$ .
- For a given luminosity class,  $\sigma_{8g}$  does not evolve with redshift. For example, comparing our values for  $M_B(z = 1.1) - 5 \log(h) \le -20.5$  to the corresponding value measured in the 2dFGRS, we found that  $\sigma_{8g}$  is consistent with a constant value 1.0 (our  $1\sigma$  error is 10%), from z = 0to  $z \sim 1$ . Given that  $\sigma_{8m}$  increases with time, we have the empirical relation  $b(z) \propto 1/\sigma_{8m}(z)$ .
- The value of the non-linear bias parameter  $b_2$  measured below  $z \sim 1$  at the scale  $R = 8 h^{-1}$  Mpc, that is, in the quasilinear regime, is negative but not statistically different from zero when taking into account the error; however, taking into account the ensemble of results coming from this and other surveys in the redshift range  $0.5 \le z < 1$  (Marinoni et al. 2005; Kovač et al. 2011; Wolk et al. 2013; Di Porto et al. 2014), there is evidence for a small but non-zero non-linear term. Including the results from local surveys as well, no evolution of  $b_2$  with redshift can be detected in the available data.
- The comparison with the properties of mocks and with the predictions of perturbation theory shows that our results are consistent with the general scenario of biased galaxy formation and gravitational clustering evolution in a standard ACDM cosmology.

In conclusion, we have provided an independent check on the second-order statistical studies of the galaxy distribution through our analysis; we explored the galaxy bias with an independent technique; finally, we determined the higher-order statistical properties of the galaxy distribution in the redshift range between 0.5 and 1.1, thanks to the combination of volume and

density of galaxies in the VIPERS survey. When VIPERS is complete, it will be possible to perform a more general analysis, which will allow us not only to decrease error bars, but also to include the dependence of high-order statistics on galaxy colour, to apply other high-order statistical tools such as the void probability function, and to give better constraints on the non-linear bias.

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A70, page 18 of 18

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