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Luminous blue variables: An imaging perspective on their binarity and near environment*

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ABSTRACT

Context. Luminous blue variables (LBVs) are rare massive stars with very high luminosity. They are characterized by strong photometric and spectroscopic variability related to transient eruptions. The mechanisms at the origin of these eruptions is not well known. In addition, their formation is still problematic and the presence of a companion could help to explain how they form.

Aims. This article presents a study of seven LBVs (about 20% of the known Galactic population), some Wolf-Rayet stars, and massive binaries. We probe the environments that surround these massive stars with near-, mid-, and far-infrared images, investigating potential nebula/shells and the companion stars.

Methods. To investigate large spatial scales, we used seeing-limited and near diffraction-limited adaptive optics images to obtain a differential diagnostic on the presence of circumstellar matter and to determine their extent. From those images, we also looked for the presence of binary companions on a wide orbit. Once a companion was detected, its gravitational binding to the central star was tested. Tests include the chance projection probability, the proper motion estimates with multi-epoch observations, flux ratio, and star separations.

Results. We find that two out of seven of LBVs may have a wide orbit companion. Most of the LBVs display a large circumstellar envelope or several shells. In particular, HD168625, known for its rings, possesses several shells with possibly a large cold shell at the edge of which the rings are formed. For the first time, we have directly imaged the companion of LBV stars.

Key words. Stars: variables: S Doradus – Stars: Wolf-Rayet – Stars: imaging – binaries: general – Stars: winds, outflows

1. Introduction

Luminous blue variables (LBVs) are rare massive stars that range in size from tens to more than 100 M_{\odot}. Their luminosity can reach or exceed the Humphreys-Davidson limit (Humphreys & Davidson 1979) with log(L/L_{\odot})=5 to 7. They are surrounded by massive envelopes created during major episodic eruptions with 0.1 to 20 M_\odot ejected and mass loss rates of 10^{-4} to $10^{-5}~M_\odot~yr^{-1}$ (Humphreys & Davidson 1994) suggesting super-Eddington winds (van Marle et al. 2008) in active phase. They have mass loss rates of 10^{-7} to $10^{-6}~M_\odot~yr^{-1}$ during quiescence.

Luminous blue variables show luminosity variations with different time-scales from days to decades (van Genderen 2001). LBVs that show S Dor phase are fast rotators with velocities reaching the critical regime in their minimum phase (Groh et al. 2009) and according to theoretical models, it is possible that they have strong polar winds (Maeder & Desjacques 2001; Owocki 2011). Their surrounding nebulae are often axisymmetric, such as the Homunculus nebula around η Car. However, Soker (2004)

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argues that a single-star model cannot reproduce these bipolar nebulae.

Interestingly, several massive stars exhibit nebular rings. One proposed way to form such rings is through the merger of a binary. The outer rings of SN 1987A in particular display a likeness with those around stars such as HD168625 and Sher 25 (Morris & Podsiadlowski 2009). This has led some to suggest that these stars may be good candidates for Galactic supernovae (Smith 2007, and references therein).

The cause of the major LBV eruptions is still debated. Different types of instabilities are proposed to explain them, among which radiation and turbulent pressure instabilities, vibrations, and dynamical instabilities (Humphreys & Davidson 1994). The constant dense slow wind of LBVs could play a role as well (Humphreys et al. 2014). Binarity with mass transfer (Kashi 2010; Kashi & Soker 2010) is also a promising explanation.

During their giant eruptive phase, extragalactic LBVs in the early eruption stages can be confused with normal supernovae (SNe). These events are sometimes called supernova impostors (Van Dyk & Matheson 2012). According to theory, LBVs should not explode as core-collapse SNe without passing through the Wolf-Rayet (WR) phase. However, recent SN radio lightcurve observations tend to demonstrate the opposite. They show the SN ejecta interacting with large amounts of circumstellar matter. It appears to be related to strong mass-loss episodes that occurred before the SN. LBVs during their S Dor phase with their giant outbursts would best explain them (Kotak & Vink 2006). Other observations support this scenario, spectroscopically in SN 2005gj (Trundle et al. 2008), and with direct identification of the progenitor in images in the cases of SN 2005gl (Gal-Yam & Leonard 2009) and SN 2010jl (Smith et al. 2011). Moreover, Groh et al. (2013) recently found that models can explain some SNe IIb by direct explosion of a relatively low-mass LBV star. This kind of LBV evolution could lead to the potential ultra-powerful pair-instability supernova (for the more massive of them with masses above 100 M_{\odot} , see Fryer et al. 2001).

Smith & Tombleson (2015) argue that because the LBVs are mostly isolated they probably result from binary evolution and can be considered massive evolved blue stragglers. This would imply that various types of massive stars could eventually become LBVs through binary mergers.

At the other end of stellar evolution, the formation is still not well understood, although models involving relatively distant low-mass companions (Krumholz 2012) may offer a decisive clue. Binarity may play a critical role in the formation of very massive objects with some protostellar collisions (Baumgardt & Klessen 2011; Tan et al. 2014). Moreover, it is expected that fragmentation could lead to the presence of lower mass companions with separations of hundreds or thousands of au (Krumholz et al. 2009; Krumholz 2012).

However, to date very few LBV stars are known with certainty to be binaries: in the Galaxy there is η Car (Damineli et al. 1997), MWC314 (Lobel et al. 2013), and HR Car (Rivinius et al. 2015). In addition, LBV1806-20 was found to be a double-lined binary by Figer et al. (2004), but it still lacks a spectroscopic follow-up to confirm its binary nature and to discard a contamination by another star in this crowded field. With VLTI-AMBER (Petrov et al. 2007) observations and with radial velocity variations, and the line shape modifications found in X-Shooter (Vernet et al. 2011) spectra, Martayan et al. (2012) indicate that the Pistol Star could also be binary. In other galaxies only HD5980 is known as a binary (Foellmi et al. 2008; Georgiev et al. 2011).

It is therefore important to investigate in a deeper and homogeneous way the presence of potential companions around LBV stars. So far, there has been no systematic search for companions of LBVs.

With very large telescopes, seeing-limited imaging probes scales $\sim 1''$, while with adaptive optics (AO) imaging the limit decreases to 60 mas (Sana & Le Bouquin 2010). In this article, we investigate the presence of potential companions in wide orbits with various imaging techniques mainly at IR wavelengths. Future investigations will focus on smaller spatial scales to find potential companions in closer orbits. Preliminary results can be found in Martayan et al. (2012). The presence of a companion provides constraints on models of star formation and evolution. Furthermore, it also gives clues to the shaping of the surrounding nebulae and possibly to the triggering of giant LBV eruptions.

In Section 2, we present our observational and archival data. Section 3 deals with the methods (chance projection probability, multi-epoch proper motion, etc.) used to determine whether the nearby objects are bound to the main stars, and discusses the results. The presence of the shells around the stars of the sample is reported in Section 4 with a detailed example from HD168625. Section 5 provides a summary. In Appendix A, the images of the stars of the sample are displayed and their remarkable environment structures are discussed. In Appendix B, small catalogues of stars in the NACO field of view of HD168625 and the Pistol Star are given.

Table 1. Stellar sample discussed in this paper, along with classification and coordinates from Simbad. Candidate LBV stars are identified with "cLBV". They are ordered following their classification and right ascension.

Star	Classification	Distance	RA(2000)	DEC(2000)
		kpc	h mn s	o / //
Pistol Star	cLBV	8 ¹	17 46 15.24	-28 50 03.58
WR102ka	LBV, WN10	8 ¹	17 46 18.12	-29 01 36.60
LBV1806-20	cLBV	11.8^{2}	18 08 40.31	-20 24 41.10
HD168625	cLBV, B6Ia	$2.2^3 (2.8^4)$	18 21 19.55	-16 22 26.06
HD168607	LBV, B9Ia	2.2^{3}	18 21 14.89	-16 22 31.76
MWC930	LBV, B5-B9e	3.5 ⁵	18 26 25.24	-07 13 17.80
MWC314	LBV, B3Ibe	3 ⁶	19 21 33.98	14 52 56.89
HD152234	O9.7Ia+O8V ^a	1.91 ⁷	16 54 01.84	-41 48 23.01
WR102e	WR, WC, "dustar" ^b	8 ¹	17 46 14.81	-28 50 00.60
HD164794	$O3.5Vf^++O5Vf^c$	1.1-1.8 ^{8,9,10}	18 03 52.45	-24 21 38.63

a: Classification from Sana et al. (2008).

b: Star is in the Pistol Star field, and is considered to be a WR-"dustar" by Marchenko & Moffat (2007).

c: Classification from Rauw et al. (2012).

1: Reid (1993), 2: Figer et al. (2004), 3: Chentsov & Gorda (2004), 4: Hutsemekers et al. (1994), Pasquali et al. (2002), 5: Miroshnichenko et al. (2005), 6: Miroshnichenko et al. (1998), 7: Ankay et al. (2001), 8: 1.58 kpc,Sung et al. (2000), 9: 1.79 kpc,(Blomme & Volpi 2014, and references therein), 10: 1.1 kpc,Bondar (2012).

2. Observations, archival data, and data reduction

The stars in our sample were selected for their properties to investigate the binary nature of LBVs and to study the envelope structure. On the one hand the Pistol Star, WR102ka, and LBV1806-20 are stars located near the Humphreys-Davidson limit (Humphreys & Davidson 1994), and on the other hand MWC314, MWC930, and WR102e are close to the limit where the rotational velocity reaches the critical velocity (Groh et al. 2009) for massive stars. HD168625 and HD168607 belong to the low-luminosity LBVs. The massive binary stars HD164794 and HD152234 were added for comparison purposes. The sample contains around 20% of the Galactic LBV/candidate LBV stars

Table 2. Summary of the NACO and VISIR observations. The service mode (SM) or visitor mode (VM) is indicated in col. 3. The length of the observations is given in hours or in nights in col. 4. Cols. 5 and 6 provide the weather condition: R-band image quality and sky transparency.

Date	Instrument	Mode	Length	Seeing	Transparency
17/06 + 01/08/2010	NACO	SM	$4 \times 1 h$	0.8"	clear
17-18/07/2011	NACO	VM	1 n	0.65''-0.8''	clear
18-19/07/2011 ¹	NACO	VM	0.5 n	$0.55^{\prime\prime}\text{-}0.65^{\prime\prime}$	clear-thin
20/07/2011 ²	VISIR	VM	0.5 n	1.0"-1.5"	thin-thick

1: a NACO technical problem prevented observation of the star WR102ka. 2: a significant fraction of the planned observations were not performed owing to the weather.

(cLBVs) as defined by Clark et al. (2005) and Nazé et al. (2012). The sample is presented in Table 1 with information from Simbad. Unfortunately, the parallax and proper motion values based on the Hipparcos or Tycho missions are not reliable for these very distant stars.

To study the binarity and the environment of the objects in Table 1, two cameras with good spatial resolution were used. The first one is NACO with its adaptive optics facility (Lenzen et al. 2003; Rousset et al. 2003) and the second is VISIR (Lagage et al. 2004). Both cameras allow near- to mid-IR observations. Our observations are summarized in Table 2.

The NACO observations were reduced with the ESO NACO pipeline version 4.3.3¹ under EsoRex using the shift-and-add algorithm with dark and flat-field corrections. The VISIR observations were reduced using a new prototype pipeline version 4.0.0 under Reflex during beta-testing of the new interface (Freudling et al. 2013). The images were also combined with a shift-andadd algorithm using the object detection in each image. If the object was not detected, offset values written in the fits header of the raw data files were used to make the image. In some cases, the covered field was not large enough to include the entire surrounding nebula (the Pistol Star or HD168625). For the Pistol Star our data did not have enough signal to properly reconstruct the image (all observations of this target were stopped owing to windy observing conditions). Additional data were retrieved from ESO and other archives. In particular, we used SINFONI (Eisenhauer et al. 2003; Bonnet et al. 2004) data for WR102ka. We reduced the data using the Reflex interface and the pipeline version 2.5.2.1. Moreover, we also used the GATOR database images from Spitzer (Werner et al. 2004) and its instruments IRAC (Fazio et al. 2004) and MIPS (Rieke et al. 2004), and from WISE (Wright et al. 2010). Images from the MAST database, HST NICMOS (Thompson 1994), and WFC (Rajan 2010) and also from other missions or instruments were obtained for various stars in order to perform multi-imaging techniques, multiwavelength and multi-epoch measurements. The data from Herschel (Pilbratt et al. 2010), IUE (Boggess et al. 1978), SWIFT/UVOT (Roming et al. 2005), and EMMI (Dekker et al. 1986) lack spatial resolution for detecting object proper motion. The summary of the images is available in Table 3 (incl. pixel sizes), while in Table 4 the central wavelength of the filters used is mentioned.

The images of HD168625 are shown in Figs. 1 and 2, while for the remaining objects of Table 1 the images are presented in the Appendix in Figs. A.1 to A.8. They reveal the presence of nebular shell(s) around the main star. Close neighbour(s) are visible in the cases of the Pistol Star, HD168625, LBV1806-20,

Table 3. List of instruments used. The pixel size in angular units (mas or arcsec) of the cameras is indicated. The filters and NACO cameras (S13, S27, L27, L54) are mentioned. The central wavelength of each filter is provided in Table 4.

Star	NACO	VISIR	Spitzer archive	
	13,27,54 mas	75 mas	(irac 0.6", MIPS 1.2")	
Pistol Star	K-S13/S27, Lp-L27	PAH2*, SiC*, NeII*	irac1,2,3,4	
WR102ka	problem		irac1,2,3,4	
WR102ka			MIPS24	
LBV1806-20	K-S27, Lp-L27		irac1,2,3,4	
LBV1806-20			MIPS24	
HD168625	3.74/4.05/Lp-L54	PAH1, PAH2	irac1,2,3,4	
HD168625	K-S27, Lp-L27	SiC, NeII	MIPS24	
HD168607	K-S27, Lp-L27		irac1,2,3,4	
HD168607	*		MIPS24	
MWC930	K-S27, Lp-L27*			
MWC314	K-S27, Lp-L27		irac1,2,3,4	
HD152234	*	PAH1, SiC, NeII		
WR102e	K-S13/S27, Lp-L27		irac1,2,3,4	
HD164794	K-S27, Lp-L27		irac1,2,3,4	
HD164794	*		MIPS24	
Star	WISE-archive	HST-archive	other	
	(1.38")	25,50,100 mas	archive	
Pistol Star	1,2,3*,4*	yes	2MASS**	
WR102ka	1,2,3,4	no	SINFONI***	
LBV1806-20	1,2,3,4	yes	N/A	
HD168625	1,2,3*,4	yes	N/A	
HD168607	1,2,3,4	yes	N/A	
MWC930	1,2,3,4	yes	N/A	
MWC314	1,2,3,4	no	swift*, EMMI*	
HD152234	1,2,3,4	no	N/A	
WR102e	1,2,3*,4*	yes	N/A	
HD164794	1,2,3,4	yes*	VISIR*	

*: too faint, saturated, not used (insufficient resolution or not deep enough).
**: Skrutskie et al. (2006).

***: SINFONI, scale 250 mas × 150 mas, data presented in Oskinova et al. (2013).

Table 4. Central wavelength in μ m of filters used in this article.

Filter	λ	Filter	λ	Filter	λ	Filter	λ
2MASS-Ks	2.15	NACO-K	2.19	WISE1	3.4	NACO-Lp	3.45
irac1	3.6	irac2	4.5	WISE2	4.6	irac3	5.8
irac4	8.0	VISIR-PAH1	8.59	VISIR-PAH2	11.25	VISIR-SiC	11.85
WISE3	12	VISIR-Ne2	12.81	WISE4	22	MIPS	24

MWC314, and HD152234. Basic PSF fitting was performed to obtain their coordinates. The detection cut-off was set at a minimum of $3-\sigma$ over the background. The limiting magnitude depends on the instrument setup and exposure times and it reached 19-20 in K band and 13-15 in Lp. More than a limiting magnitude, the difference in magnitude (or the contrast at a given separation) could be more suited to characterizing the detection of a close companion. They are reported in Table 5.

3. Binarity

The binarity in massive stars is important because it might have an impact on

- the way they form. Recent models of massive star formation (Krumholz et al. 2009; Krumholz 2012, 2015) indicate that the star is created in multiple systems with companions in different orbital scales (including wide ones of hundreds to tens of thousands of au);
- the way they evolve (mergers, matter exchange, close orbital scale, Baumgardt & Klessen 2011; Tan et al. 2014; Krumholz 2015);

¹ ftp://ftp.eso.org/pub/dfs/pipelines/naco/naco-pipeline-manual-1.1.pdf



Fig. 1. Star HD168625, NACO images: a) $28'' \times 21''$ Lp image with labels of the surrounding stars; b): $6'' \times 4''$ zoom in K on the pair HD168625a,b. The SW companion is at 1.15'' from the main star. c) $6'' \times 4''$ zoom in Lp of HD168625a,b.

- the triggering of eruptions (intermediate to nearby scale, Kashi 2010; Kashi & Soker 2010);
- the shaping of the circumstellar environment (all orbital scales).

In this first article, we focus on wide-orbit companions that could provide some constraints on the star formation models and could help with constraints on the massive star formation process and on the shaping of the surrounding nebulae.

The first step in determining whether a star is in a potential binary system is detecting a potential companion. To this aim, one needs to probe different spatial scales. The largest scale is checked with the imaging techniques, assisted or not with an adaptive optics facility. NACO observations were mostly used because this is the instrument with the best spatial resolution with pixels of 13, 27, and 50 mas. Some HST images were used as well. The closest neighbours found to the main stars are listed in Table 5.

To determine the likelihood that a potential companion is bound to the main star, we used a combination of different techniques and criteria that are presented in the following sections.

Table 5. Separation, magnitude difference (left), chance projection probability (middle) depending on the sample and method used, and proper motion comment and binding status of potential companion to the main object (right). Blue values are larger than the defined limit (see text). Details of the columns are indicated at the bottom of the Table.

Star	Proj. sep.	prob. sep.	prob. sep.1	Max proj.	Δmag	P(field) ²	P(field) ²	P'(field)	P'cut-off	P,P',P''(field) ³	Comments	Status
	//	"	au	sep. " for	δ mag<8.5 ^m	NACO	trilegal%	trilegal		2MASS	Motion	
				10,000 au		%	all, $\pm 2^m$, $\pm 1^m$	%	%	%		
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
Pistol Star_4	0.75	1.21	9698	0.77	3.1 - 2.3	11	100, 9, 5	46	42	5,4,5	А	borderline
Pistol Star_3	1	1.61	12931	0.77	4.1 - 3.7	20	100, 40, 15	66	42	9,9,9	В	field
Pistol Star_1	1.39	2.24	17974	0.77	5 - 4.9	39	100, 100, 71	88	42	16,15,16	С	field
Pistol Star_2	1.44	2.32	18620	0.77	5 - 5	42	100, 100, 77	90	42	17,15,15	С	field
WR102ka_b	1.35	1.49	11920	0.77	~5	90	25, 0, 0	22	42	13,12,13	D	field
WR102ka_c	1.98	2.19	17520	0.77	3.5	100	52 , 0, 0	41	42	29,25,25	D	field
LBV1806-20b	0.76	1.23	14495	0.52	6.6	20	5, 5, 4	18	62	3,3,3		field
LBV1806-20c	0.9	1.45	17166	0.52	6.6	28	8, 8, 5	24	62	4,4,4		field
LBV1806-20d	1.3	2.1	24795	0.52	6.6	59	15, 15, 13	44	62	9,9,9		field
HD168625b	1.15	1.86	4089*	2.81	4.6 - 4.4	5	2, 1, 1	<1	12	3,3,3	E	bound
HD168625b real ⁴	1.15	1.33	2927**	3.94	4.6 - 4.4	5	2, 1, 1	<1	12	3,3,3	Е	bound
HD168607b	2.02	3.26	7183	2.81	10.1	100	8, 7, 7	65	12	7,6,7		field
HD168607c	4.19	6.76	14899	2.81	9.1	100	31, 31, 16	99	12	29,25,25		field
HD168607d	5.19	8.37	18455	2.81	10.1	100	45, 45, 35	100	12	45,36,36		field
MWC930b	2.88	4.65	16293	1.77	7.2	100	2, 2, 2	79	18	14,13,13		field
MWC930c	1.31	2.11	7411	1.77	>8	46	1, 1, 0	27	18	3,3,3	В	field
MWC314b		<1 mas	1.22	2.06				<1	16	<1,<1,<1	F	bound
MWC314c	1.18	1.9	5722	2.06	3.3 - 4.2	29	2, 1, 1	8	16	4,4,4		bound
HD152234b	0.51	0.83	1590	3.24		14	7, 7, 0	12	10	1,1,1	G	borderline
WR102e_b	0.71	1.15	9181	0.77	2.6 - 2.6	10	100, 94, 51	43	42	4,4,4	В	field
HD164794b		2-8 mas	14	4.48				<1	8	<1,<1,<1	Н	bound
HD164794c	2.4	3.87	6129	3.92	7.7	86	100, 100, 100	57	8	16,15,15		field
HD164794d	3.5	5.65	8938	3.92	8.5	100	100, 100, 100	83	8	35,29,30		field
HD164794e	4.6	7.42	11748	3.92	8.7	100	100, 100, 96	96	8	61,45,45		field

Column details:

col. 1: star ID, col. 2: projected separation as measured in the image, cols. 3 and 4: probable deprojected separation in arcsec or in au, col. 5: maximum projected separation in arcsec corresponding to 10,000 au, col. 6: magnitude difference, col. 7^1 : chance projection probability P(field) in NACO images, col. 8: P(field) using the trilegal model results and with counting from no restriction to $\pm 1^m$ difference with the main star, col. 9: chance projection probability P'(field) following the formula of Correia et al. (2006) with trilegal data, col. 10: cut-off probability limit for P' (see text), col. 11^2 : chance projection probability comparison P(field), P'(field) following the formula of Ciardullo et al. (1999) and using 2MASS data. Col. 12: Proper motion comment, col. 13: status of the potential companion: "bound", "borderline", "field".

Table notes:

1: Probable separation should be $\leq 10,000$ au.

2: P(field) ≤10%.

3: Probabilities should be $\leq 5\%$.

4: "real" stands for companion in the disk plane with an inclination angle of 60° (O'Hara et al. 2003; Smith 2007) corresponding to a deprojection of 30°.

*: the separation goes up to 5205 au if the largest distance is considered. **: the separation goes up to 3725 au.

A: no motion estimates, B: large motion indicating a foreground object, C: small motion, D: only SINFONI "image", E: small motion, low projected speed, F: see Lobel et al. (2013), G: only VISIR image, H: see Rauw et al. (2012).

The error in the chance projection probability estimates is usually lower than 1% (see text).

3.1. Method of chance projection probability

With a single epoch image, one can obtain an indication of whether a companion is bound to the main star by using the chance projection probability as previously performed by Oudmaijer & Parr (2010) with NACO for B and Be stars.

As inputs for this determination, it is necessary to know

- 1. the projected distance of the potential companion to the main star in arcsec. It gives the projected area *s*. The probability of having an apparent stellar association is related to the possibility that a star randomly falling in the area s can obtain the same image of the main star with a companion;
- 2. the projected size of the field of view that provides the total projected area *S* of the field of view. The ratio between *S* and *s* gives the number of area components *N* of the system;
- 3. the magnitudes of the stars in the field of view or their flux ratio to the main star;
- 4. the Galactic coordinates of the main star;
- 5. the extinction coefficient A_v of the main star;
- 6. the number of stars *n* in the field of view.

There are two ways to determine *n*. The first is a simple counting in the NACO (or another instrument) images. The second is to use a model of the Galactic star population, here we used the "trilegal" model (Girardi et al. 2005). With the trilegal code, it is necessary to know point number 3 to provide a cut-off in magnitude, point 4 for the location in the Galaxy, point 5 to provide the corresponding extinction, and point 2 for the size of the field to consider. The magnitude cut-off (20-21) in the K or Lp band is provided by the faintest star detected in NACO (aperture magnitude obtained with Sextractor). We used different A_{ν} values in order to determine a range of solutions.

When K and Lp NACO images are available the results with the trilegal model with the K or Lp cut-off were compared and found to be identical. However, we also found that this model is not perfectly able to reproduce the star population in a few cases by comparing with the counting in the NACO images. For instance in the field of the Pistol Star, the trilegal model appears to be too optimistic with excessive numbers of stars. Changing the value of A_{ν} does not help to diminish the number of stars. In the case of MWC314 and MWC930, the results appear too pessimistic with insufficient stars with respect to the NACO images. Indeed, changing the values of A_v or the magnitude cut-off did not improve our comparison.

We consider the possibility of randomly finding a star in the area determined in point 1. This defines the probability of chance projection that the potential companion is a field object and is not bound to the main star. This probability P(event=k) with the previously defined parameters uses the combinatorics and the hypergeometric distribution (Brandt 2014) of the available stars once projected in the field

$$P(e=k) = \frac{C1 \times C2}{C3} \tag{1}$$

with $C1=C_m^k$, $C2=C_{N-m}^{n-k}$, and $C3=C_N^n$. The variables are m= number of companions visible in the image, k=number of events for being a binary (corresponding to the number of stars to be added in the multiple system), N= number of area components, and n= number of objects to distribute in N. The combinatorics function C corresponds to

$$C_a^b = {a \choose b} = \frac{a!}{b!(a-b)!}$$
(2)

The chance projection probability with the different input sets is provided in Table 5 in columns 7 and 8. An estimate of the errors was performed considering a 5% uncertainty on the counting of the number of stars in the field and/or in the area. It usually results in an uncertainty of less than 1% in the chance projection probability. However, this error follows the separation as it increases, but this does not affect the interpretation of the probability results.

We list the projected separation of the main star to the potential companion in arcsec. The NACO image is a projection and the potential companion stars can be above or below the plane of projection. Thus, we account for the deprojected distance by correcting the projected distance with the most probable angle for the random distribution of the orbital plane inclination angle (arcsin($\pi/4$)). In the case of HD168625 the inclination angle is known and we present both estimates using the known angle (real) and the most probable angle. We adopt a significance level of 10% for the probability of random association to consider that a companion is physically bound to its central star. This threshold of 10% corresponds to a slightly significant result (1.7 σ), while 5% would be considered more significant (2 σ).

In addition to the formula we used, the probability P'(field)that a star is a field object can be computed following Correia et al. (2006). For PMS objects they consider that a probability of 1% is not negligible and the nearby star should be considered as a field star (the association only results by a chance alignment). However, the distance to Earth of the objects is not taken into account by their formula. The objects in their article are at a distance below 190 pc. Therefore, by scaling this formula, and the cut-off for being bound or not to the distance of the star to Earth, we compute a cut-off probability ranging from 8% at 1,580 pc to 62% at 11,800 pc. In Table 5 in columns 9 and 10, we also report the probability of a chance projection following the method of Correia et al. (2006) and the scaled cut-off probability. We also note that our formula is usually more pessimistic (70% of the time), i.e. providing a higher probability value than the formula by Correia et al. (2006) using the same type of counting with the trilegal data.

To obtain another estimate, we used the probability P''(field) defined by Ciardullo et al. (1999), which is given in col. 11 in

Table 5. We compare the results of this method with the probabilities obtained with our formula and with the method of Correia et al. (2006) using the same 2MASS raw data. The result is also provided in col. 11 following the order: our formula, the Correia et al. (2006) formula, and the Ciardullo et al. (1999) formula. The results are comparable even though, as already noted, their probability of chance projection is often a bit lower than the one determined with our method. Ciardullo et al. (1999) consider two objects bound if the probability of a chance superposition is less than 5%. However, as illustrated with the Pistol Star in Fig. A.1 for very far objects, non-AO (2MASS-K) images result in a lower number of visible stars than with AO-assisted images (NACO-K). As a consequence, chance projection probability determination should be performed with high angular resolution images or adequate catalogues for those distant stars.

3.2. Multi-epoch observations and proper motions

Multi-epoch images can be used to determine potential proper motions of the objects and eventually an orbit, or to detect whether the star is a background or foreground star. If the motion of the "neighbour" star is larger than the motion of the main object then it is considered to be a foreground field object. If the motion is of the same order of value or smaller than the main star, then the neighbour is considered to be at the same distance of the main star or to be a background object. However, the proper motion of the main star is usually not known or is uncertain. The difference in right ascension and declination, but also in separation between the main star and the potential companion, is considered in order to detect any proper motion. We mainly considered the separation difference because in most of the cases the sampling or the signal-to-noise ratio is not high enough to safely estimate a position to within a fraction of pixel. We only consider valid a proper motion larger than the size of the biggest pixel in the sample for each star. The absolute-coordinate comparison was discarded to avoid systematics and shifts between the World Coordinate System (WCS) calibration of images originating from different cameras. Considering the large distance to the stars, providing an orbit goes beyond the possibility of the data.

To perform a multi-epoch analysis, we require good spatial resolution and a pixel size that is as small as possible. For instance, considering a displacement of 10 mas at the speed of 10 km s⁻¹ at 2 kpc, both epochs should be separated by an interval of 10 yrs. With a displacement of 50 mas at the speed of 100 km s⁻¹ at 8 kpc, the two epochs should be separated by an interval of 19 yrs. Both examples consider the best possible case with a motion parallel to the projection plane.

Using the Kepler and Newton laws for different mass ranges of a circular orbit with different star separations (up to 10,000 au), we obtain a range of possible orbital velocities and periods. From the simulations, the orbital velocities should be less than 10 km s^{-1} with periods of thousands or tens of thousands of years. It is believed that higher velocities indicate field objects.

To obtain larger time intervals, we searched in the ESO and MAST archives. The best archival images in terms of spatial resolution and pixel size are those from the HST-NICMOS and WFC for the objects of our sample. HST images were retrieved for the Pistol Star, WR102e, HD168625, HD168607, MWC930, LBV1806-20, and HD164794. In the last case, the images are not used because they are underexposed for our purpose. The proper motion of objects found in the field of LBV1806-20 and HD168607 are not discussed here because they are too distant (>10,000 au) or too faint (δ mag=10^m) to be bound. Unfortu-

nately, there is no HST data for MWC314 and the EMMI images do not show the nearby star at 1.18". For the stars HD168625, the Pistol Star, WR102e, and MWC930, the characteristics of their multi-epoch observations are provided in Table 6. Table 7 compiles the proper motion information and the implied binary status for stars HD168625, the Pistol Star, WR102e, and MWC930.

Table 6. Summary of the characteristics of the multi-epoch observations for several stars in our sample. The epochs in MJD and the civil date are provided at the bottom of the table.

Star	Epoch	Instrument	Time int.	Pixel size	Limiting
					displacement,
			yr	mas	velocity
Pistol Star	1a*-2a	NICMOS-NACO	12.76	13-50	50 mas
and	2a-3a	NACO-NACO	1.08		150 km s ⁻¹
WR102e	1a-3a	NICMOS-NACO	13.84		
HD168625	1b-2b	HST/WF-WF	0.19	27-50	50 mas
	2b-3b	WF-NICMOS	1.07		40 km s ⁻¹
	3b-4b	NICMOS-NACO	12.88		at 2.2 kpc
	1b-4b	WF-NACO	14.14		*
MWC930	1c-2c	HST/ACS**-NACO	5.15	25-27	27 mas, 80 km s ⁻

*: Epoch 1a from Figer et al. (1998), **: Ubeda (2014)

Epochs "a": 1a=50705.41-14/09/1997, 2a=55364.23-17/06/2010,

3a=55760.05-18/07/2011.

Epochs "b": 1b=50597.59-29/05/1997, 2b=50666.80-06/08/1997,

3b=51056.06-31/08/1998, 4b=55761.17-19/07/2011.

Epochs "c": 1c=53880.35-25/05/2006, 2c=55761.06-19/07/2011.

Table 7. Summary of the proper motion estimates and inferences about possible membership in a binary system of potential companion as defined in Table 5.

Star	Neighbour	Displacement	Comments	Conclusion
		mas		
Pistol Star	P4, P2		not enough data	
	P3	250	too large	foreground
	P1	27	smaller than pixel	
	P8,P9,P10,P13	> 50	too large	foreground
	P14,P15,P16	> 50	too large	foreground
WR102e	b	> 50	too large	foreground
HD168625	b	< 27	approaching a	bound
	d, k, m	51 to 161	too large	foreground
	j, h	<50	small	background
	c	50	away from a	not bound
MWC930	c	> 80	too large	foreground

The motion found for HD168625b at 1.15'' (see Fig. 1) is smaller than the NACO pixel size. If true, it gives a projected velocity in the image of less than 10 km s⁻¹. Its motion could indicate that it is approaching HD168625a. This is one of the rare cases where we can actually obtain an estimate of a fraction of a pixel for the position of the star. However, this was not possible in some HST images. Recently, Aldoretta et al. (2015) confirmed by interferometric observations the presence of this companion.

Star c has a motion of the order of 50 mas going away from HD168625. The other stars are only visible in our "wide" NACO image.

3.3. Star separation and flux ratio tests

Because the separation is projected in the images, we de-project to derive the proper distance of the potential companion to the main star. For this purpose the deprojected distance is obtained using the most probable angle in the case of random distribution of the orbital inclination angle (corresponding to $\arcsin(\pi/4)$). If

the distance of the main object to Earth is known, the separation in au of the potential companion to the main star can be determined. For wide binaries it can range up to 20,000 au (Lépine & Bongiorno 2007; Longhitano & Binggeli 2010) or even larger (Shaya & Olling 2011), but we use a conservative distance of 10,000 au. It corresponds to about 90% of the binary star distribution shown in Lépine & Bongiorno (2007). Krumholz et al. (2009) and Krumholz (2012) also indicate that companions can be expected at a distance of 5,000 au or more. Sana et al. (2014) show that at a separation of 8", the cumulative multiplicity frequency reaches 91%. It would correspond to a distance of 16,000 -au at a typical distance of 2 kpc. For deprojected distances above 10,000 au the neighbour star is probably not bound to the main star (Sana et al. 2014, actually indicate that at large separation only the brightest companions are bound to the main star). The maximum projected separation in arcsec corresponding to the linear separation of 10,000 au in the image is also provided (see Table 5). The results are indicated in Table 5, cols 3 to 5. Stars P4; HD168625b; HD168607b; MWC314b,c; MWC930c; WR102e_{*b*}; HD152234b; and HD164794b,c,d are separated from the main component by less than 10,000 au. This test eliminates 50% of the potential companions visible in the images as bound in a binary system.

According to the study by Sana et al. (2014) among massive stars, it is not rare to find binaries with a magnitude difference in K or Lp of ~8-8.5^m. The limiting magnitude would ensure that almost all potential companions are caught. In addition, they also used NACO to find binaries in O stars, as this threshold would be adequate for LBV stars and corresponds to a late B-type star (using the models from Schaller et al. 1992). The results are provided in Table 5, col. 6, while we give the angular projected separation corresponding to 10,000 au as an indication in col. 5. This test allows us to discard 30% of the potential companions visible in the images as bound in a binary system. The results are discussed in Section 3.4.

3.4. Binarity assessment and discussion

To summarize, a companion is bound to the main star if it complies with the following criteria:

- The deprojected/probable separation must be smaller than 10,000 au. This value is given in Table 5, col. 4. The projected separation (from col. 2) is corrected with the most probable angle of projection to provide a more realistic angular separation (col. 3) converted to au in column 4.
- The difference in magnitudes must be δ mag<8.5^m (Table 5, col. 6).
- The chance projection probability P(field) must be smaller than 10%, P'(field) smaller than the cut-off probability, or P"(field) smaller than 5%. In column 7 we indicate the chance projection probability for the potential companion considering the stars counted in the NACO images (except for WR102ka for which SINFONI image is used). In column 8, we provide the chance projection probability for the potential companion considering the stars counted in the results of simulations with the trilegal code (Girardi et al. 2005). They differ by the magnitude ranges used: all trilegal stars, stars with a maximum difference of $\pm 2^m$ and $\pm 1^m$.

In column 9, the chance projection probability following the formula of Correia et al. (2006) is provided and the scaled cut-off probability is given in column 10. In column 11, the chance projection probabilities P(field), P'(field), and P''(field) respectively following our formula, the formula of

Correia et al. (2006), and the formula of Ciardullo et al. (1999) are provided using the same set of 2MASS data. The same 5% limit is applied to the result of P(field) and P'(field) in col. 11 for consistency with the result of P"(field). When they show contradictory results, we consider the majority of results as a better trend of the probability.

- The multi-epoch analysis must yield a small motion (Table 5, col. 12).

The conclusion about the status of the potential companion, bound, not bound, or borderline is given in the last column of Table 5.

- Therefore, HD168625 and MWC314 have a companion in a wide orbit. The latter is known to host a close companion at less than 1 mas (Lobel et al. 2013) that is beyond the capability of the imaging technique. MWC314 could be a triple hierarchical system like HD152234 (Sana et al. 2008). HD168625b being bound to HD168625a would imply that it is in the equatorial plane of the system inclined by 60° with respect to the observer. The role of this star is questionable for shaping the inner shell, which appears somewhat distorted. Could this companion help to clear the material ejected by the central star in the inner cavity?
- P4 is a borderline companion for the Pistol Star, similarly for HD152234b with HD152234a. HD152234b is probably bound to the main star because the separation is small, the magnitude ratio is 2.5 according to Mason et al. (2009), and the chance probability is low but at the limit. Based on the observations of Mason et al. (2009), Sana et al. (2008) also concluded that this companion is probably bound to the main star. Together with the central spectroscopic binary it composes a triple system.

In addition, some stars are known to host a close companion not resolved by the imaging techniques. This is the case for the Pistol Star (Martayan et al. 2012); MWC314, see above; and LBV1806-20, whose spectrum showed a double line signaling a close companion (Figer et al. 2004) estimated by Eikenberry et al. (2004) to orbit at less than 450 au (representing much less than 1 mas). However, there is currently no spectroscopic monitoring to confirm the binary nature. In addition, Rauw et al. (2012) found a close companion at ~10 mas of HD164794, while Sana et al. (2014) resolved the system with the VLTI-PIONIER (Le Bouquin et al. 2011) and found a separation of 5 mas. Aldoretta et al. (2015) estimated the separation to be ~19 mas. These companions are not ruled out by our criteria. Overall, about two out of seven of the LBV stars in our sample are found to host a companion in a wide orbit.

Because more than 75% of O stars are binaries according to Chini et al. (2012) and Sana et al. (2012, 2014), it is expected that LBVs are binaries as well, but very few LBVs are known to host a companion (Rivinius et al. 2015; Lobel et al. 2013; Damineli et al. 1997). Following Sana et al. (2014), about 30-35% of the binaries are found with a large projected separation (as in this paper). In this study, two (HD168625, MWC314) out of the seven LBVs (29%) in the sample with high angular resolution images are binaries with a companion in a wide orbit. Because of the huge luminosity of the LBVs, it is quite difficult to detect the surrounding companions. It implies that the multiplicity rate found is certainly a lower limit.

The Pistol Star, WR102ka, MWC930, HD168607, and LBV1806-20 do not seem to have a companion on a wide orbit, even if P4 is borderline for the Pistol Star. However, the statistical analysis was performed on a small number of stars and

should be extended to more LBV/cLBVs, although the sample we use already represents 20% of the stars of this type (considering the sample of 35 LBVs + cLBVs defined by Clark et al. 2005). Recently, Aldoretta et al. (2015) resolved or partially resolved a companion around three out of nine Galactic LBVs, producing a binary rate of 33% in their sample. Among the LBVs, only HD168625 is shared by both studies. Joining the two studies, the sample results in 4 binaries among 15 LBVs. It corresponds to a $27\pm17\%$ binary fraction with a confidence rate of 95%.

What could be the impact of a companion in a wide orbit on the evolution of the central star and its eruptions? With a separation of at least 1500 au, unless with a highly eccentric orbit, they appear too distant to trigger any eruption by mass transfer or to have any impact on the day-to-day stellar evolution of the main star. In such a case, their main role would be to allow the formation of the star and the nebula (see Krumholz 2012) in addition to the possible shaping of the nebula. However, according to Kaib & Raymond (2014), despite a large separation of thousands of au, collisions could occur between the components of a binary system on average every 1,000 to 7,500 yrs in our Galaxy. If this is true it could imply that despite a large separation, companions in a wide orbit could still trigger cataclysmic events or eruptions.

4. General circumstellar environment description

Table 8. Detected nebular shells, their semi-minor and semi-major dimensions in arcsec and in pc. In the case of a round shell, only one extent is provided. The extent size is defined using the convention of 10% of the peak surface brightness (Tylenda et al. 2003).

Star	shell radii	shell radii	λ	Figure	shell radii
	$\operatorname{arcsec} \times \operatorname{arcsec}$	$pc \times pc$	μm		$pc \times pc$
					Weis (2011)
Pistol Star	25.5×24	0.99×0.93	8	A.1	0.8×1.2
WR102ka	58×55	2.25×2.13	22	A.2	
LBV1806-20*	_	_	3.4-22	A.3	
HD168625 int ¹	19×14	0.20×0.15	22	1, 2	0.17×0.13
HD168625 imd1	46×41	0.49 imes 0.44	22	2	
HD168625 ext ¹	80 : ×70 :	0.85 imes 0.75	22	2	
HD168625 ring1	33×40	0.35×0.43	8	2	
HD168607	9.5	0.10	22	A.4	
MWC930	59×54	1.00×0.92	22	A.5	
MWC314	26	0.38	22	A.6	
HD152234	16-20	0.15-0.19	3.4-22	A.7	
HD164794	11	0.06-0.10	5.6	A.8	

The distance of the stars to the Earth is available in Table 1.

*: There is no indication for the star LBV1806-20 because it is deeply embedded in a complex with other WR stars and it is not possible to determine to which star the nebula belongs.

The last column provides the measurements performed by Weis (2011) in pc. 1: The outer radius measured along the axes ESE-WNW and NE-SW of the internal (int), the intermediate (imd), and the external (ext) shells are given for HD168625. As a reference, the dimensions of the NE ring are also indicated.

In the infrared images, all stars in the sample exhibit surrounding nebular shells. Their size was measured in the images using the convention of 10% of the peak surface brightness as defined in planetary nebula studies (Tylenda et al. 2003). Taking into account their distance to Earth, the shell size in parsec (pc) is listed in Table 8. The Pistol Star, HD168625, MWC930, and WR102ka all exhibit large shells with a diameter of at least 1 pc. MWC314 presents an intermediate-size shell of about 0.8 pc diameter, but we cannot detect in the infrared the large bipolar structure found by Marston & McCollum (2008) in H α . For reference, η Car's shell "radius" is about 0.5 pc. We do not provide

any measurement for LBV1806-20 because it is deeply embedded in a complex nebular environment with several WR stars. It is therefore not possible to safely assign shell membership to a given star. In some cases, the envelope is smaller than 0.2 pc and might result from another mechanism than matter ejected by giant LBV eruption. This is the case for the non LBVs HD152234, HD164794, and possibly for the LBV HD168607. In Section 4.1 the environment of HD168625 and its multiple shells is discussed as an example, while in Appendix A the main environmental structures of the remaining stars of the sample are presented along with their corresponding infrared images.

4.1. HD168625: shells and rings

In the infrared images (Figs. 1, 2), HD168625 clearly shows two different shells and possibly an additional fainter third component. Their sizes (in arcsec and in pc) are listed in Table 8. The internal shell is well known and we observed it with NACO (Fig. 1). Depending on the wavelength, different extents of the same shell can be observed (i.e. NACO versus WISE). The dynamical age of the internal shell ranges from 4,000 to 5,700 yr according to Nota et al. (1996), Pasquali et al. (2002), and O'Hara et al. (2003).

By doing a cut of the WISE4 image or using the flux gradient, a break in the latter can be seen with two different slopes. The steeper one corresponds to the known "intermediate" shell (Hutsemekers et al. 1994, their "outer shell"), while the other one in the outer part could correspond to a fainter redder external shell. Its inner part would be blended with the intermediate shell (see Fig. 2). A forthcoming study will present this external shell in detail; in particular, careful comparison with the WISE4 extended PSF² and features³ was performed to confirm the presence of this external shell. Interestingly, the famous rings discovered by Smith (2007) in the IRAC4 image coincide with the inner border of the external shell (see Fig. 2). He indicates that the internal equatorial ring and the intermediate shell are coeval with an age of a few thousand years. The intermediate and external shells probably result from previous eruptions or stellar phases with wind expansion.

Ghost patterns in the MIPS image prevent us from properly finding the extent of the external shell. The ratio of the semimajor to the semi-minor axis ranges from 1.1 to 1.2 for the external and intermediate shells, respectively, while it ranges from 1.4 to 1.5 for the internal shell.

If the external shell is confirmed, it could indicate that the rings of HD168625 are possibly formed by the collision of a fast wind with a slower and previously ejected material. This observation supports the scenario proposed by Chita et al. (2008). According to these authors, the formation of such rings could be the result of the collision of an anisotropic wind created during the blue supergiant phase of a fast rotating star with a shell created by the star in a previous red supergiant phase. Smith et al. (2007) proposed that the rings are formed in the blue supergiant phase. Smith et al. (2013) suggested that the collision with the fast wind of a blue supergiant is not needed to form the rings. An expanding equatorial ring may be ejected by a blue fast rotating supergiant star with a clearing of the caps. This scenario does not require the presence of another older shell.

Other objects like SN1987A or Sher 25 also reveal similar rings. Hendry et al. (2008) ruled out the presence of a binary companion and found that the rings of the blue supergiant Sher 25 were formed during the blue loop evolutionary phase. The rings of SN1987A have shown brightening episodes explained by the collision of matter with different velocities (Larsson et al. 2011).

Another alternative scenario is proposed by Morris & Podsiadlowski (2009) who invoked the merger model to explain the creation of the rings during the red supergiant phase. However, it only explains co-eval shells.

The exact nature of stellar fast and slow outflow is unknown. Do they originate from a normal stellar wind of a red or blue supergiant or from LBV eruption? HD168625 could become a template star that explains the other stars with similar rings such as Sher 25.

5. Conclusions

This study, based on multiwavelength imaging techniques, allowed the environment of LBVs and other massive stars to be probed on a scale of $\sim 0.1''$. Our conclusions are the following:

- 1. In our sample, two out of seven of the LBVs could have a companion in a wide orbit.
- 2. Several stars could be a triple hierarchical system with a close and a wide binary system (possibly MWC314 or HD152234).
- 3. For the first time LBV companions were directly imaged.
- 4. The presence of a companion in a wide orbit is an indicator of the way the star formed: as a group of stars. It also contributes to constraining models of massive star formation. However, the actual contribution of the wide orbit companion to the main day-to-day stellar evolution of the central star is questionable.
- 5. All stars are surrounded by circumstellar matter, ejected in outbursts, by a wind, or both.
- 6. The creation of the nebular rings of HD168625 is possibly due to the collision of fast material with a previous slower shell, which is presented here for the first time but needs to be confirmed.
- 7. The companions can act on the shaping of the surrounding nebula. HD168625b could be at the origin of the clearing of the internal cavity and of the asymmetric structure of the internal ring.

Other spatial scales must be probed with other techniques (interferometry and spectroscopy) to infer the presence of close companions and to analyse the circumstellar matter structure close to the star.

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tion. This research has made use of the NASA/ IPAC Infrared Science Archive,

² http://wise2.ipac.caltech.edu/docs/release/allsky/expsup/ sec4_4c.html#psf

³ http://wise2.ipac.caltech.edu/docs/release/allsky/expsup/sec2_4bii.html tional Aeronautics and Space Administration and the National Science Founda-#conspicuous_PSF_ring



Fig. 2. Star HD168625, Spitzer and WISE images: a) WISE 10' \times 10' tricolour image R=WISE4, G=WISE2, B=WISE1. The intermediate and external nebulae are visible. The star \approx 1' west of HD168625 is HD168607. b) 2.75' \times 2.75' Spitzer-irac4 image. The image shows the nebular rings reported by Smith (2007). c) WISE channel 4 image at 22 μ m of HD168625 with labels of the internal, intermediate, and external shells (shown by ellipses). The position of the NE ring reported by Smith (2007) is also indicated. It matches the outer border of the intermediate shell and the inner border of the external shell. In these images, it is just possible to see a local flux minimum between the intermediate and external shell. This flux minimum is used to define the limits of both shells.

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Appendix A: Description of the circumstellar environment

In the following sections, the infrared images of the stars with their main circumstellar environment structures are discussed.

Appendix A.1: Pistol Star

In Fig. A.1, we present infrared images of the Pistol Star and its surrounding environment including WR102e, among others. The comparison between 2MASS and NACO images illustrates the adaptive optics capability. The WISE and Spitzer-IRAC images show the large shell ejected by the Pistol Star. Our NACO images show the nearby stars of the Pistol Star (with a zoom) and WR102e. We also note in this image the resolved double star V4644 Sgr.

Appendix A.2: WR102ka

The infrared images in Fig. A.2 show that the star is embedded in a complex ambient nebula, but the WISE image also shows that the star is surrounded by an almost spherical shell. The bottom part of the figure is the reconstructed image (median) over the SINFONI cube in the K band. See the main text of the article for the discussion of the nearby stars.

Appendix A.3: LBV1806-20

The Spitzer and WISE images in Fig. A.3 show that the star LBV1806-20 lies in a complex region with massive stars and with filaments and nebulae. None of these structures is centred in LBV1806-20, but with the other two WR stars, it probably shapes this surrounding environment. The NACO image shows the nearby stars of LBV1806-20 discussed in the main text.

Appendix A.4: HD168607

In Fig. A.4, the surrounding environment of HD168607 appears bluer (warmer) than in the LBV neighbour HD168625. The shells of the latter reach the vicinity of HD168607.

Appendix A.5: MWC930

Fig. A.5 presents the large circular shell of MWC930 visible in the WISE images. The objects next to MWC930 seen in the NACO image are discussed in the main text.

Appendix A.6: MWC314

Fig. A.6 presents the infrared images of MWC314. The Spitzer and WISE images show the circumstellar nebula that appears less bright than in other LBVs. In the NACO-Lp image, the wide companion discussed in the main text can be seen.

Appendix A.7: HD152234

Sana et al. (2014) indicate that HD152234 is a complex system with a close binary system called Aa and Ab that they resolved with PIONIER (Le Bouquin et al. 2011). As shown in Fig. A.7-right, we resolved the B companion at 0.5" with VISIR data. The nebular envelope of the system is shown in Fig. A.7-left.

Appendix A.8: HD164794

Fig. A.8 shows the infrared images for HD164794. The IRAC and WISE images display the circumstellar shell, but it also looks as if a filament is crossing this star. Is it actually a foreground nebular filament or a jet of this binary system? With the data that we have it is not possible to safely infer the nature of this structure, but this structure appears too large to be a jet. The MIPS24 image is unfortunately saturated around this star, but it reveals the large complex ambient nebula. In the NACO-K image, the nearby stars previously discussed are visible.

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Fig. A.1. Multiband images of the Pistol Star. Top row: a) $28'' \times 25''$ 2MASS K-band image, the red crosses correspond to 2MASS known objects; b) $1.12' \times 1.12'$ Spitzer irac4 image treated to enhance the surrounding nebula of the Pistol Star; c) WISE $2' \times 2'$ "tricolour" image R=WISE2, G=WISE2, B=WISE1, the channels 4 and 3 are saturated and cannot be used. This image shows the large nebula surrounding Pistol Star. Bottom row: d) NACO $28'' \times 25''$ K image, the red circles correspond to 2MASS stars; several known stars are identified in the image. It illustrates the adaptive optics capability in the field; e) zoom ($7'' \times 5''$) of image d where the surrounding stars are numbered. The white circle has a 5.5'' diameter. The objects labelled "u" are possible artefacts. For all images, the orientation is north-top, east-left.

Appendix B: Catalogues of stars surrounding HD168625 and the Pistol Star in NACO images

This section gives the catalogue of surrounding objects in the NACO Lp-band field of HD168625 in Table B.1 and in the NACO K-band field of the Pistol Star in Table B.2. They are provided for archive purposes and as an astrometric reference for any future proper-motion analysis. The magnitudes in the table are indicated without guarantee for the Pistol Star due to a possible zeropoint offset of 1 magnitude. This results from the lack of usable reference stars with the same instrumental setup as used for the Pistol Star. Other known stars in the observed field are variable as well, preventing an accurate photometric calibration.

Table B.1. Catalogue of objects surrounding HD168625 in a radius of 18" as shown in Fig. 1. The NACO Lp magnitude is provided as an indication.

Star ID	RA(2000)	DEC (2000)	Lp mag.
	h mn s	o / //	
HD168625a	18 21 19.49	-16 22 26.16	3.56 ± 0.00
HD168625b	18 21 19.46	-16 22 27.23	7.59 ± 0.00
starD	18 21 19.57	-16 22 19.23	8.91 ± 0.00
starL	18 21 18.58	-16 22 19.03	10.96 ± 0.03
starM	18 21 18.71	-16 22 17.32	11.10 ± 0.03
starC	18 21 19.22	-16 22 23.58	11.17 ± 0.03
starJ	18 21 20.55	-16 22 29.76	11.61 ± 0.05
starH	18 21 19.42	-16 22 13.35	12.04 ± 0.07
starK	18 21 18.71	-16 22 20.08	$>13 \pm N/A$



Fig. A.2. Multiband images of WR102ka. a) $2.75' \times 2.75'$ Spitzer tricolour image R=irac4, G=irac3, B=irac2; b) WISE $2' \times 2'$ tricolour image R=WISE3, G=WISE2, B=WISE1. c) Spitzer-19' × 19' MIPS-24 μ m image; d) reconstructed image from SINFONI in K (8" × 8"). The object labelled "d" is possibly an artefact.



Fig. A.3. Multiband images of LBV1806-20. a) $2.75' \times 2.75'$ Spitzer tricolour image R=irac4, G=irac2, B=irac1; b) WISE $2' \times 2'$ tricolour image R=WISE3, G=WISE2, B=WISE1; c) Spitzer-10' × 12' MIPS-24 μ m image. In this image the LBV1806-20 is on the left side of the central tri-structure; d) $28'' \times 21''$ NACO image in the K band.

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Fig. A.4. Multiband images of HD168607. a) $2.75' \times 2.75'$ Spitzer tricolour image R=irac4, G=irac2, B=irac1; b) WISE $2' \times 2'$ tricolour image R=WISE3, G=WISE2, B=WISE1; c) NACO $28'' \times 21''$ Lp image.



Fig. A.5. Multiband images of MWC930. Left: a) WISE $2' \times 2'$ tricolour image R=WISE4, G=WISE2, B=WISE1. It shows the nebula surrounding MWC930. Right: b) NACO $7'' \times 5''$ K-band image; there are several nearby objects.

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Fig. A.6. Multiband images of MWC314. a) Spitzer- $6' \times 2'$ MIPS-24 μ m image; b) 2.75' × 2.75' Spitzer tricolour image R=irac4, G=irac2, B=irac1, the blue and red spots close to the central object are artefacts due to the high flux levels of MWC314 in those channels; c) WISE 2' × 2' tricolour image R=WISE3, G=WISE2, B=WISE1. It shows the nebula surrounding MWC314; d) NACO 8" × 6" Lp image. The nearby star is at 1.18" NNW.



Fig. A.7. Multiband images of HD152234. Left: WISE $2' \times 2'$ tricolour image R=WISE4, G=WISE3, B=WISE1. Right: VISIR-SiC $4.2'' \times 2.9''$ image. There is a fainter star indicated by a red arrow at 73° NE and at 0.5'' from the main object.



Fig. A.8. Multiband images of HD164794. a) WISE $10' \times 8.5'$ tricolour image R=WISE4, G=WISE3, B=WISE1; b) $2.75' \times 2.75'$ Spitzer tricolour image R=irac4, G=irac3, B=irac2; c) NACO $6'' \times 4''$ image in K.

Table B.2. Catalogue of objects surrounding the Pistol Star within a box of $14'' \times 14''$ as defined in Fig. A.1-d. The NACO K magnitude is provided as an indication. An offset of the zeropoint may exist (magnitudes may have to be corrected by about +1 mag). Entries with K mag values of 99 indicate there are no reliable measurements. Stars with (+) are blended and their magnitude is not accurate (indicated with :).

The Pistol Star 17 46 15.10 -28 50 3.58 6.75 ± 0.00	
The fistor star $174015.10-28505.58 + 0.75 \pm 0.00$	
PI 17 46 15.09 -28 50 2.20 11.73 ± 0.02	L
P2 17 46 14.99 -28 50 3.40 11.68 ± 0.02	L
P3 17 46 15.03 -28 50 3.90 10.85 ± 0.0	l
P4 17 46 15.07 -28 50 4.22 9.86 \pm 0.00 P5(, P() 17 46 15.17 -28 50 2.45 12 44 \pm 0.00	~
P5(+P6) $1/46 15.1/-28 50 2.45 12.44: \pm 0.0$ P7 $17.46 15.24 - 28.50 2.51 - 13.53 \pm 0.0$	2
P8 17 46 15 25 -28 50 2.36 13 74 + 0.04	5
P10(+P9+P16) 17 46 15.01 -28 50 4.95 13.11: ± 0.0	3
P11 17 46 14.93 -28 50 4.94 14.17 ± 0.0	7
P12 17 46 15.18 -28 50 5.08 13.01 ± 0.03	3
P13 17 46 15.17 -28 50 5.96 13.65 \pm 0.04	ļ
P14 1/40 14.89 -28 50 3.00 13.96 \pm 0.00 P6 17.46 15 10 28 50 2.24 00.00 \pm 00.0))()
P9 $17461502-28504689900+990$	00
P15 $17.46\ 14.93\ -28\ 50\ 1.17\ 99.00\pm 99.0$	00
P16 17 46 14.99 -28 50 5.11 99.00 ± 99.0	00
WR102e 17 46 14.67 -28 50 0.63 9.71 ± 0.00	
$(WR102e)b 17 46 14.70 -28 50 0.03 12.26 \pm 0.02$	2
V4644Sgr 17 46 14.26 -28 50 2.61 8.46 ± 0.00	
$\begin{bmatrix} FMG99]4 & 174614.89 - 284955.01 & 10.49 \pm 0.0 \\ \begin{bmatrix} FMG99]6 & 174614.25 - 28495648 & 1041 + 0.00 \\ \end{bmatrix}$)
LHO5 $174615.82 - 284951.0913.68 \pm 0.03$	5
MLB_PS1 17 46 15.43 -28 50 17.62 13.08 ± 0.03	3
MLB_ $PS2$ 17 46 15.80 -28 49 50.39 13.93 ± 0.03	5
MLB_PS3 17 46 14.44 -28 49 50.17 12.99 ± 0.02	2
MLB_PS4 17 46 14.46 -28 49 50.31 12.77 ± 0.02	2
MLB_PS5 1/46 14.92 -28 49 50.48 14.23 \pm 0.0 MLP_PS6 17.46 15 11 28 40 50 53 13.82 \pm 0.0	/
MLB_PS7 17 46 13.11 -28 49 50.53 13.82 \pm 0.0. MLB_PS7 17 46 14 89 -28 49 50 62 14 50 \pm 0.00	,)
MLB $PS8$ 17 46 15.86 -28 49 50.70 17.27 ± 1.12	2
MLB_ <i>PS</i> 9 17 46 15.25 -28 49 50.84 12.05 ± 0.0	l
MLB_PS10 17 46 15.61 -28 49 50.91 12.27 ± 0.02	2
MLB_PS11 17 46 14.99 -28 49 50.94 11.76 ± 0.0	l
MLB_PS12 17 46 15.80 -28 49 51.02 14.83 \pm 0.12 MLD_PS12 17 46 15.50 -28 49 51.02 14.83 \pm 0.12	2
MLB_P515 174615.59 -284951.14 12.14 \pm 0.0 MLB_P514 17461456 -284951.67 1330 \pm 0.0	2
MLB_PS15 17 46 14.83 -28 49 52.04 11.37 + 0.0	,
MLB_PS16 17 46 14.69 -28 49 52.35 14.84 ± 0.12	2
MLB_PS17 17 46 14.64 -28 49 52.45 13.23 ± 0.02	3
MLB_PS18 17 46 15.58 -28 49 52.46 99.00 ± 99.0	00
MLB_PS19 17 46 14.35 -28 49 52.53 13.63 \pm 0.04 MLP_PS20 17 46 15 76 28 40 52 70 12 27 \pm 0.04	+ ,
MLB_ $PS21$ 17 46 15 23 -28 49 52 29 12 27 \pm 0.0	2
MLB $PS 22$ 17 46 15.92 -28 49 53.02 11.74 ± 0.0	
MLB_PS 23 17 46 15.49 -28 49 53.00 15.93 ± 0.33	3
MLB_PS 24 17 46 15.12 -28 49 53.14 14.59 ± 0.10)
MLB_PS 25 17 46 14.63 -28 49 53.30 13.46 \pm 0.04	ł
MLB_PS 20 17 46 15.69 -28 49 53.36 12.88 \pm 0.02 MLB_PS 27 17 46 14 67 28 40 53 42 13 82 \pm 0.02	2
MLB_ $PS28$ 17 46 15 40 -28 49 53 51 13 37 + 0.04	, 1
MLB_PS29 17 46 15.16 -28 49 53.54 13.53 \pm 0.04	1
MLB_PS 30 17 46 15.70 -28 49 53.56 13.11 ± 0.02	3
MLB_ <i>PS</i> 31 17 46 15.62 -28 49 53.69 12.20 ± 0.0	l
MLB_PS32 17 46 15.18 -28 49 53.83 13.43 ± 0.04	ł
MLB_PS35 1746 14.34 -28 49 53.84 14.90 \pm 0.14 MLB_PS34 1746 15.82 -28 49 53.88 14.09 \pm 0.04	t í
MLB $PS35$ 17 46 14.83 -28 49 54.12 13.84 + 0.02	5
MLB_PS 36 17 46 15.40 -28 49 54.37 11.59 ± 0.0	
MLB_PS 37 17 46 15.58 -28 49 54.31 17.13 ± 0.99)
MLB_PS 38 17 46 16.15 -28 49 54.43 13.74 ± 0.04	ł
MLB_PS 39 17 46 15.14 -28 49 54.54 14.75 \pm 0.12	ļ
MLB_ $PS40$ 1/4014.09 -284954.5814.06 ± 0.00 MLB_ $PS41$ 17.4614.87 28.4054.7611.60 ± 0.00	
MLB_PS42 17 46 14 62 $-284954.7011.09 \pm 0.01$	2
MLB_ $PS43$ 17 46 16.14 -28 49 54.91 14.10 \pm 0.00	5
MLB_PS44 17 46 15.38 -28 49 55.00 12.73 ± 0.02	2
MLB_PS45 17 46 16.10 -28 49 55.04 14.76 ± 0.1	l
MLB_PS46 17 46 14.82 -28 49 55.07 13.87 ± 0.03	5
MLB_ $PS4$ / 1/46 15.8/ -28 49 55.05 16.33 ± 0.4 MLB_ $PS4$ 8 17.46 14.05 28 40 55 18 13 10 ± 0.0	2
MLB $PS49$ 17.46 14.05 -26.49 55.18 15.19 \pm 0.0. MLB $PS49$ 17.46 15.42 -28.49 55.21 13.00 \pm 0.07	, 3
$MLB_PS50 17 46 15.81 -28 49 55.20 13.47 \pm 0.04$	ł

Table B.2. continued

MLB_PS51	17 46 14.68	-28 49 55.81	12.65 ± 0.02
MLB_PS 52	17 46 14.48	-28 49 55.84	14.09 ± 0.06
MLB_PS 53	17 46 14.04	-28 49 55.86	14.56 ± 0.07
MLB_PS54	17 46 14.37	-28 49 55.86	13.78 ± 0.05
MLB_PS 55	17 46 15.67	-28 49 56.11	12.65 ± 0.02
MLB_PS 56	17 46 14.94	-28 49 56.18	13.42 ± 0.04
MLB_PS 57	17 46 15.42	-28 49 56.22	14.28 ± 0.08
MLB_PS 58	17 46 14.34	-28 49 56.42	13.63 ± 0.04
MLB PS 59	17 46 14.94	-28 49 56.46	13.54 ± 0.04
MLB_PS60	17 46 15.95	-28 49 56.71	14.70 ± 0.11
MLB_PS61	17 46 15 16	-28 49 56 84	13.74 ± 0.05
MLB_PS62	17 46 14 90	-28 49 57 38	1340 ± 0.04
MLB_PS63	17 46 14 54	-28 49 57 41	14.33 ± 0.01
MLB_PS64	17 46 14 90	-28 49 57 40	14.55 ± 0.00 99.00 ± 99.00
MLB PS65	17 46 16 00	-28 49 57 47	14.81 ± 0.12
MLD_1505	17 46 14 00	-28 49 57.47	14.01 ± 0.12 12.97 ± 0.05
MLD_FS00	17 40 14.90	-26 49 57.50	13.67 ± 0.03
MLD_PS0/	17 40 13.33	-28 49 57.01	16.11 ± 2.42
MLD_PS08	17 40 14.00	-20 49 57.02	10.35 ± 0.47
MLB_PS 09	17 40 14.78	-28 49 57.85	16.22 ± 0.43
MLB_PS 70	17 46 16.13	-28 49 57.86	15.45 ± 0.20
MLB_PS71	17 46 14.04	-28 49 58.22	10.89 ± 0.01
MLB_PS72	17 46 16.10	-28 49 58.33	14.07 ± 0.06
MLB_PS73	17 46 15.03	-28 49 58.42	99.00 ± 99.00
MLB_PS74	17 46 14.44	-28 49 58.48	13.33 ± 0.03
MLB_PS75	17 46 15.78	-28 49 58.54	13.35 ± 0.03
MLB_PS76	17 46 14.11	-28 49 59.20	13.94 ± 0.06
MLB_PS77	17 46 15.38	-28 49 59.21	13.76 ± 0.05
MLB_PS78	17 46 15.51	-28 49 59.22	13.63 ± 0.04
MLB_PS79	17 46 14.74	-28 49 59.24	13.46 ± 0.04
MLB_PS80	17 46 14.89	-28 49 59.33	13.60 ± 0.04
MLB PS 81	17 46 15.87	-28 49 59.48	14.03 ± 0.06
MLB PS 82	17 46 14.06	-28 49 59.63	13.14 ± 0.03
MLB_PS83	17 46 14.95	-28 49 59.66	14.54 ± 0.10
MLB_PS84	17 46 15 09	-28 49 59 78	1345 ± 0.04
MLB_PS85	17 46 15 82	-28 49 59 81	14.29 ± 0.08
MLB_PS86	17 46 14 16	-28 /0 59 96	11.27 ± 0.00 11.27 ± 0.01
MLD_1500 MLB_DS87	17 46 14 37	28 40 50 00	11.27 ± 0.01 14.35 ± 0.08
MIB PS88	17 46 15 77	28 50 0 01	14.33 ± 0.00 14.47 ± 0.00
MLD_FS00	17 46 15.77	-28 50 0.01	14.47 ± 0.09 14.22 ± 0.07
MLD_PS 69	17 40 15.01	-28 50 0.09	14.25 ± 0.07
MLB_PS90	17 40 15.40	-28 50 0.12	14.54 ± 0.09
MLB_PS91	17 46 16.06	-28 50 0.84	12.56 ± 0.02
MLB_PS92	17 46 15.15	-28 50 0.94	13.99 ± 0.06
MLB_PS93	17 46 15.62	-28 50 0.94	11.40 ± 0.01
MLB_PS94	17 46 15.63	-28 50 1.07	10.57 ± 0.01
MLB_PS95	17 46 15.64	-28 50 1.22	11.26 ± 0.01
MLB_PS96	17 46 14.14	-28 50 1.07	13.77 ± 0.05
MLB_PS97	17 46 14.39	-28 50 1.05	14.15 ± 0.07
MLB_PS98	17 46 15.35	-28 50 1.10	13.97 ± 0.06
MLB_PS99	17 46 16.00	-28 50 1.35	13.28 ± 0.03
MLB_PS 100	17 46 15.48	-28 50 1.39	10.93 ± 0.01
MLB_PS 101	17 46 14.28	-28 50 1.44	12.88 ± 0.02
MLB_PS 102	17 46 15.56	-28 50 1.44	12.82 ± 0.02
MLB_PS103	17 46 16.08	-28 50 1.75	13.85 ± 0.05
MLB PS 104	17 46 15.60	-28 50 1.84	11.33 ± 0.01
MLB PS 105	17 46 14.11	-28 50 1.84	12.57 ± 0.02
MLB PS 106	17 46 14.15	-28 50 1.94	11.57 ± 0.01
MLB PS 107	17 46 15.93	-28 50 2.64	12.66 ± 0.02
MLB PS 108	17 46 14.72	-28 50 2.78	14.84 ± 0.12
MLB_PS109	17 46 15.63	-28 50 2.88	14.55 ± 0.10
MLB $PS110$	17 46 14 26	-28 50 2.99	947 ± 0.00
MLB $PS111$	17 46 15 97	-28 50 3 26	15.71 ± 0.27
MLB_PS112	17 46 15 04	-28 50 3 60	9.89 ± 0.00
MLB_PS112	17 46 14 20	-28 50 3 69	12.66 ± 0.02
MLB PS114	17 46 14 00	28 50 3 72	12.00 ± 0.02 13.22 ± 0.03
MLD_DS114	17 46 14.09	-28 50 3.72	13.22 ± 0.03 14.48 ± 0.00
MLD_FS115	17 46 10.03	-28 50 3.84	14.46 ± 0.09
MLD PC117	17 40 14.1/	-20 30 3.90	11.01 ± 0.01
WILD_PS117	17 40 15.80	-28 50 4.05	13.78 ± 0.03
MLB_PS118	17 40 15.50	-28 50 4.24	14.00 ± 0.10 12.05 ± 0.00
MLB_PS119	1/40 14.78	-28 50 4.44	13.95 ± 0.06
MLB_PS120	1/46 15.54	-28 50 4.57	14.30 ± 0.08
MLB_ <i>PS</i> 121	1/46 14.69	-28 50 4.77	14.79 ± 0.12
MLB_ <i>PS</i> 122	17 46 14.11	-28 50 4.99	14.50 ± 0.09
MLB_PS123	17 46 14.80	-28 50 5.25	13.96 ± 0.06
MLB_PS124	17 46 15.48	-28 50 5.25	99.00 ± 99.00
MLB_PS125	17 46 15.37	-28 50 5.39	14.89 ± 0.13
MLB_PS126	17 46 14.47	-28 50 5.74	13.08 ± 0.03
MLB_PS127	17 46 14.26	-28 50 5.76	18.40 ± 3.17
MLB_PS128	17 46 14.71	-28 50 5.79	13.31 ± 0.03
MLB_PS 129	17 46 16.00	-28 50 5.78	14.51 ± 0.09
MIB_{PS130}	17 46 15 62	-28 50 5 94	13.93 ± 0.06

Table B.2. continued

MLB_PS131 17 46 15.38 -28 50 6.04 13.27 ± 0.03
MLB PS132 174614.50 -28506.14 10.89 ± 0.01
MLP $DS 122 17.4614.70 28.50.612 12.84 \pm 0.02$
$\text{WLD}_{PS} \text{ 155 } 1740 14.70 - 2850 0.15 12.84 \pm 0.02$
MLB_ <i>PS</i> 134 17 46 14.39 -28 50 6.15 11.90 ± 0.01
MLB PS135 174615.51 -2850619 1390+005
MI B PS136 17 /6 1/ 00 28 50 6 26 1/ 27 + 0.09
$MLD_F 5 150 1740 14.90 - 26 50 0.20 14.27 \pm 0.08$
MLB_ <i>PS</i> 137 17 46 15.46 -28 50 6.33 13.12 ± 0.03
MLB PS138 17461549-2850644 1299+003
$MLD DC 120 17 46 15 41 20 50 6 50 14 24 \pm 0.07$
$\text{MLD}_{PS} 159 \ 1740 \ 15.41 \ -28 \ 50 \ 0.50 \ 14.24 \pm 0.07$
MLB_PS140 17 46 14.04 -28 50 6.68 12.13 ± 0.01
MLB PS141 174615.28-28506.66 13.95 ± 0.06
MLP $PS142$ 17.46.15.50 28.50.6.74 12.40 + 0.02
$\text{WLD}_{FS} 142 \ 1740 \ 15.59 \ -2650 \ 0.74 \ 12.40 \pm 0.02$
MLB_PS 143 17 46 15.81 -28 50 6.95 12.18 ± 0.01
MLB PS144 17461461 -2850696 1445+009
MLB $PS145$ 1746 1524 2850 700 1208 ± 0.03
$MLD_F 5 145 1740 15.24 -26 50 7.00 12.96 \pm 0.05$
MLB_PS146 17 46 15.56 -28 50 6.97 12.00 ± 0.01
MLB $PS147$ 17 46 15 36 -28 50 7 12 16 08 + 0 38
$MED_{15} = 147 + 17 + 0.15.50 + 20.50 + 7.12 + 10.00 \pm 0.50$
MLB_PS 148 17 46 15.67 -28 50 7.19 12.50 ± 0.02
MLB PS149 17461543 -28507.26 14.43 ± 0.09
MLP $PS150 17.4615.54 28.507.26 10.02 \pm 0.01$
$\text{WILD}_{PS} 150 \ 1740 \ 15.54 \ -28 \ 50 \ 7.50 \ 10.95 \pm 0.01$
MLB_PS 151 17 46 16.10 -28 50 7.41 11.75 ± 0.01
MLB $PS152 17.461556 -2850760 10.33 \pm 0.00$
$MED_{10} 152 17 40 15.50 20 50 7.00 10.55 \pm 0.00$
NILD_P3133 1/4014.93 -28 30 /.60 15.73 ± 0.27
MLB_PS154 17 46 15.09 -28 50 7.65 13.63 ± 0.04
MIR PS155 1746 15 47 -28 50 7 71 12 10 - 0.01
$MID D015(17.4(15.72 - 20.50.7.0) + 12.17 \pm 0.01)$
MLB_PS156 17 46 15.72 -28 50 7.89 13.89 ± 0.05
MLB PS157 174615.64 -28508.04 13.96 ± 0.06
MIR DS158 17 46 16 06 20 50 0 17 14 50 + 0.00
$w_{LD} = r_{5,1,50} + 1740 + 10.00 + 26.50 + 8.17 + 14.50 \pm 0.09$
MLB_ <i>PS</i> 159 17 46 15.07 -28 50 8.26 14.35 ± 0.08
MLB PS160 17461584 -2850846 1438 + 0.08
$\mathbf{MID} \ \mathbf{DC161} \ 17.461554 \ 20500.50 \ 50.050 \ 12.50 \ 0.004$
$w_{LD} = F_{5} = 101 = 1740 = 13.34 - 26.50 = 8.52 = 13.52 \pm 0.04$
MLB_PS162 17 46 14.91 -28 50 8.79 99.00 ± 99.00
MLB PS163 174614.50 -2850902 1421 + 007
MI P DS 164 17 46 14 22 20 50 0.22 16 00 + 0.00
$w_{LD} = r_{5104} + 1740 + 14.55 - 26.50 + 9.25 + 10.98 \pm 0.80$
MLB_ <i>PS</i> 165 17 46 15.45 -28 50 9.35 14.10 ± 0.06
MLB PS166 17461552 -2850934 1408 + 0.06
$\mathbf{MID} \mathbf{DC167} 17.461611 20.500.56 14.00 0.10$
$NILD_{P3} 107 1740 10.11 - 28 50 9.56 14.92 \pm 0.13$
MLB_PS168 17 46 15.80 -28 50 9.71 14.78 ± 0.12
MI B PS169 17 46 15 20 28 50 10 10 14 44 + 0.00
$MLD_{I} = 107 + 1740 + 15.20 + 26 - 50 + 10.10 + 14.44 \pm 0.09$
MLB_ <i>PS</i> 170 17 46 14.39 -28 50 10.13 14.65 ± 0.10
MLB PS171 17461531 -285010261310+003
MED_10171 17 10 10:01 20 50 10:20 10:10 ± 0:05
$NILD_{PS} 1/2 1/40 10.0/ -28 50 10.6/ 14.18 \pm 0.0/$
MLB_PS173 17 46 15.37 -28 50 10.70 13.89 ± 0.05
MLB PS174 17461557 -28501076 1440 \pm 0.00
$MED_{15174} = 174015.57 = 205010.70 = 14.49 \pm 0.09$
MLB_PS175 1746 14.52 -28 50 10.78 14.31 ± 0.08
MLB_PS176 17 46 14.35 -28 50 10.92 14.52 ± 0.09
MI B PS177 17 46 15 07 28 50 11 00 12 01 + 0.04
$MLD_F 5 177 1740 15.07 - 26 50 11.00 15.91 \pm 0.06$
MLB_ <i>PS</i> 178 17 46 15.74 -28 50 11.19 12.18 ± 0.01
MLB PS179 17461550 -285011291431 + 0.08
$\mathbf{M} = \mathbf{D} = $
MLB_PS180 17 46 14.63 -28 50 11.38 10.64 ± 0.01
MLB PS181 17 46 14.70 -28 50 11.46 13.31 ± 0.03
MI D DC102 17 46 15 02 20 50 11 05 11 02 - 0.01
$\text{WILD}_{FS} 162 \ 1740 \ 15.03 \ -28 \ 50 \ 11.95 \ 11.92 \ \pm 0.01$
MLB_PS183 17 46 15.00 -28 50 12.05 11.34 ± 0.01
MIR PS184 17 46 14 78 -28 50 12 02 15 00 - 0 16
$\frac{1000}{100} = 1000 \pm 1000 \pm 10000000000000000000000$
MLB_PS185 17 46 15.50 -28 50 12.17 14.53 ± 0.09
MLB PS186 17 46 15.79 -28 50 12.25 14.53 ± 0.09
MI B DS 187 17 46 15 21 20 50 12 20 1 100 ± 0.05
$MLD_F 5 107 1740 13.21 - 20 30 12.29 13.88 \pm 0.05$
MLB_ <i>PS</i> 188 17 46 16.14 -28 50 12.59 10.72 ± 0.01
MLB PS189 17 46 14.38 -28 50 12 82 11 19 + 0.01
MI B DS 100 17 46 15 24 20 50 12 70 12 05 0 005
$\text{WLD}_{F5} \text{ 190 } 1740 \text{ 15.54 } -2850 \text{ 12.79 } 13.85 \pm 0.05$
MLB_ <i>PS</i> 191 17 46 15.33 -28 50 12.84 13.92 ± 0.06
MLB PS192 17461564 -28501298 1286 + 0.02
$\mathbf{MID} \mathbf{DC102} 17.4615.02 20.5012.10 \mathbf{12.00 \pm 0.02} \mathbf{MID} \mathbf{DC102} 17.4615.02 20.5012.10 15.00 20.5012.10 15.00 20.5012.10 15.00 20.5012.10 15.00 15$
$\text{WILD}_{F5195} = 1740 = 15.02 - 2850 = 13.18 = 15.80 \pm 0.29$
MLB_PS194 17 46 14.68 -28 50 13.71 14.32 ± 0.08
MI B PS195 17461552 -28501203 1305 - 0.02
$10.03 \pm 0.03 \pm$
MLB_ <i>PS</i> 196 17 46 15.94 -28 50 14.07 12.43 ± 0.02
MLB PS197 174615.47 -285014151063+001
$\mathbf{MID} \ \mathbf{DC100} \ 17.4615.22 \ 20.5014.04 \ 12.06 + 0.05$
$NILD_{P3} 198 1740 15.33 - 2850 14.24 13.86 \pm 0.05$
MLB_ <i>PS</i> 199 17 46 15.62 -28 50 14.27 12.51 ± 0.02
MLB $PS200$ 17 46 15 36 -28 50 14 30 13 46 \pm 0.04
$\frac{1}{100} = 15200 + 1740 + 15.30 + 2650 + 14.59 + 15.40 \pm 0.04$
MLB_PS 201 17 46 15.44 -28 50 14.40 11.45 ± 0.01
MLB PS202 17461460 -285014421421 + 0.07
$MLD D D D D D 17 4(14.00 -20.50 14.42 14.21 \pm 0.07)$
MLB_ $PS203$ 17 46 14.69 -28 50 14.52 14.01 ± 0.06
MLB PS204 17461542 -28501458 1263 + 0.02
MID DC005 17.461512 205014.77 14.17 0.07
$\text{IVIL}\mathbf{D}_{F5205174015.15-285014.7714.17\pm0.07}$
MLB_PS 206 17 46 15.31 -28 50 15.20 14.15 ± 0.07
MIR PS207 17 46 15 67 20 50 15 40 12 74 + 0.02
$MLD_F 5 207 1740 13.07 - 26 50 15.40 12.74 \pm 0.02$
MLB_PS 208 17 46 15.95 -28 50 15.68 13.87 ± 0.05
MLB $PS209$ 17 46 15 60 -28 50 15 85 12 85 \pm 0.02
$MLD_{-1} = 5207 + 17 + 0.15.00 + 20.50 + 15.05 + 12.05 \pm 0.02$
MLB_ <i>PS</i> 210 17 46 15.56 -28 50 16.53 13.37 ± 0.04
MLB PS211 17 46 15 66 -28 50 16 50 14 85 + 0 12
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MLP DC212 17 46 14 00 20 50 16 02 12 06 0 000
$MLB_{PS212} 17 46 14.90 -28 50 16.82 13.96 \pm 0.06$
MLB_ <i>PS</i> 212 17 46 14.90 -28 50 16.82 13.96 ± 0.06 MLB_ <i>PS</i> 213 17 46 14.86 -28 50 16.96 15.04 ± 0.15
MLB_ <i>PS</i> 212 17 46 14.90 -28 50 16.82 13.96 ± 0.06 MLB_ <i>PS</i> 213 17 46 14.86 -28 50 16.96 15.04 ± 0.15 MLB_ <i>PS</i> 214 17 46 15.84 -28 50 17.05 13.47 ± 0.04
$ \begin{array}{c} \text{MLB_}PS212 & 174614.90 & -285016.82 & 13.96\pm0.06 \\ \text{MLB_}PS213 & 174614.86-285016.96 & 15.04\pm0.15 \\ \text{MLB_}PS214 & 174615.84-285017.05 & 13.47\pm0.04 \\ \text{MLB_}PS215 & 174614.86-285017.05 & 13.47\pm0.04 \\ \text{MLB_}PS215 & 174614.86-285017.0513.47\pm0.04 \\ \text{MLB_}PS215 & 174614.2614285017.0513.47\pm0.04 \\ \text{MLB_}PS215 & 174614.2614285017.0513.47\pm0.04 \\ \text{MLB_}PS215 & 174614.2614285017.0513.47\pm10.46141414141414141414$