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Characterization of Random Fields From NDT Measurements: a Two Stages Procedure

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ABSTRACT

Characterization of randomness and spatial variability of material properties, loading or deterioration processes of structures, from inspection, is a very challenging task that concentrates the improvement of Non Destructive Testing (NDT) tools on more efficient and higher structural coverage. In case of characterization of random loading or material properties, this challenge is arduous because of the limited number of measures and the quasi-infinite potential positions of local failures. This paper presents a two stages procedure for the stochastic characterization of random fields from NDT measurements. According to the stationarity property, the optimal quantity of NDT measurements and their position can be assessed once a quality requirement is included. The proposed procedure allows: (i) to quantify the properties of the ergodic stationary field, and (ii) to assess the second order parameters of the studied random variables. The paper ends illustrating the methodology with an application that considers the inspection of a concrete beam with a capacitive technique. The results indicate that the proposed methodology is useful to identify the parameters of a random field by reducing the number of NDT measures under given quality requirements.

Keywords: non-destructive testing, spatial variability, characterization, optimization, inspection, random field

1. INTRODUCTION

1.1. Background

Many countries worldwide are increasing expenditures for maintaining existing infrastructure. Within the framework of Bridge Management Systems (BMS), methods based on visual inspection have been firstly developed with a real potential and several applications [1] and new methods and techniques based on measuring and monitoring are still under development [2–5]. The extension of these methodologies and the development of new methods for optimizing the management of other assets different than bridges are still under consideration: sewer or railway networks [6,7], dams [8] and wharfs [9–12]. The common challenge is to optimize the allocation of resources for inspection, maintenance and repair from a risk analysis by ensuring an allowable risk [13–16]. Reliability

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methods offer the theoretical background and tools for safety assessment and Risk Based Inspection (RBI) methods account for uncertainty on measurements.

Optimal asset management requires quantifying the condition of the structure from on-site measured data. In the probabilistic thinking, this question has been addressed by random variable modeling and updating methods that have been widely developed during the three last decades. Random variable updating is very useful for condition assessment and reliability updating when a priori distribution is known and data coming from inspections or monitored systems is collected [5,9,17]. Basically, the Bayes theorem and its derivative tools (Bayesian Networks) offer the theoretical framework to deal with this issue. The so-called RBI generalizes these approaches in the case of non-perfect inspections by linking inspection and decisions [4,18–20]. RBI methods are powerful once there is no important spatial or temporal variability involved into the problem. This implies that the location of the most critical defect, from a reliability point-of-view, is known. In these cases, it can be assumed that the spatial distribution of defects in the neighboring zone does not affect the reliability assessment (robustness). Nevertheless, actual progresses in the development and implementation of new NDT techniques or embedded sensors for new and existing structures need to improve these methodologies within three directions:

- *Consideration of spatial variability*: it has been shown that spatial variability of real infrastructure cannot be described by random variables. Then, spatial randomness should be considered in several problems. For instance, previous studies [16,20] have found that inspections should also account for the spatial variability of the measured parameters.
- *Robust updating*: establishing a prior distribution for a whole set of material properties or model parameters for existing structures conditions the result of posterior distributions obtained after probabilistic updating [21]. The selection of prior distributions is a very difficult task because it is mainly based on the knowledge of experts and then probabilistic updating must be applied with care. Therefore, further research is required to develop new methods or to improve the existing ones to obtain posterior distributions based on robust updating which is less depending on the uncertainties of prior distributions [22].
- *Exploitation of data measured from NDT tools*: NDT tools offer new possibilities to collect a huge quantity of data by an operator or a new generation of remotely operating vehicles and robots – e.g. [23]. These data could be useful for randomness or spatial variability quantification. However, there are many uncertainties and errors inherent to the measure itself and the assessment of a material property or model parameter from a physical measure (speed wave, resistivity, etc.). New research efforts should be addressed to improve the understanding, controlling, and quantifying these sources of uncertainty and error.

1.2. Aims and Scope

Recent studies have focused on random field characterization based on NDT measurements. Nguyen et al [24,25] combined several NDT techniques, kriging and variograms to assess the spatial variability of concrete at different scales (point, local and global). Gomez-Cardenas et al [26] proposed an two-step approach to optimize the number and position of ultrasound measures required to localize critical zones. The main objective of this paper is to propose a methodology to find an optimal inspection configuration (number and localization of NDT measures) that minimizes the error of identification of probability distributions for a given quantity of interest (resistance, porosity, water content, etc.) with spatial dependency. This study does not focus on the detection of damage and/or critical zones. The paper focuses on second order random variables and it has been developed on the

basis of some basic but realistic assumptions about the inspection characteristics and the random field nature. The proposed flowchart considers a unique stochastic field that can be parameterized by the same parameters (for the distribution and the spatial variability) for several components built with the same material and subjected to the same degradation processes (same environment). For the sake of simplicity of the writing and the illustration, we will consider a one-dimensional spatially distributed field. However, this methodology could be extended to characterize a n -dimensional random field. This methodology is mainly based on a two stages procedure (Figure 1):

- The first stage aims to characterize the spatial correlation of the studied stochastic field – i.e. the parameter of a correlation function.
- The second stage is devoted to get “weakly correlated” data on structural components in view to build a sample of events assumed as independent.

The first part of the paper presents the adopted method for representing spatial variability – i.e., the Karhunen-Loève decomposition (Section 2). Section 3 details the proposed two-stages inspection strategy. The optimization of the number and position of NDT measures is based on a quality criterion that is also presented in Section 3. The paper ends with applications to a numerical and a real study cases to illustrate the potential of the methodology (Sections 4 and 5, respectively).

2. RANDOM FIELD MODELING OF INSPECTIONS

2.1. Usual Approaches for Spatial Variability Modeling

Random field theory is useful for modeling spatial variability of a given quantity (material property, deterioration process, load, etc.). Random fields could take several forms more or less complicated depending on the intrinsic characteristics of the structure (material randomness, construction process, etc.) and/or the interactions with external actions (environmental actions, deterioration processes, etc.). A stationary stochastic process can be used to represent spatial variability when the random field can be considered as homogeneous – i.e. the values of the statistical characteristics of this field do not change with the space). For instance, stationary stochastic processes have been used to model the spatial variability of surface chloride concentration [27], concrete properties [28–30] or soil properties [31–35]. In some cases, when a structure is affected by several phenomena that vary with time (e.g. deterioration) and/or with space (concrete casting in several layers), it is modeled as piecewise stationary stochastic process. This type of stochastic field can represent, for example, the vertical spatial variability of the increase of soil strength with depth or the vertical corrosion of structures located in coastal environments [10]. Figure 2 plots the mean loss of steel thickness due to corrosion with depth for sheet-piles in marine environment where the corrosion process is governed by several phenomena that depend on the exposure zone E at 10, 25 and 50 years (t_{10} , t_{25} and t_{50}). It can be observed that there is a characteristic for each considered zone –i.e., $E \in [E_A, E_T, E_L, E_I, E_M, E_S]$, limited by horizontal dashed lines: from the top to the bottom, Aerial (A), Tide (T), Low level of tide (L), Immersion (I), Mud (M) and Soil (S). In this case, a piecewise stationary stochastic field could be used to have a good representation of the spatial variability of the loss of thickness.

2.2. Usual Approaches for Inspection Modeling

During inspection, there are many factors that influence the quality of measurements – e.g, environmental conditions, error in the protocol, error due to material variability, and error induced by the operator [36]. These factors could lead, for a given inspection, to under or overestimations of the measured parameter. If the parameter is underestimated, the owner could decide “do nothing” when

repair is required. On the contrary, an overestimation generates a “wrong decision” where early repair generates overcharges [4,14,19]. In this paper we will consider inspection as perfect. It means that (i) there is no bias and (ii) the error is negligible or repetitively tests allow to obtain a good estimate of the real value computed as the average of measurements at a given point and therefore to assume error as negligible.

2.3. Main Assumptions for Stochastic Modeling

In order to simplify the presentation of the proposed methodology, we consider the following main assumptions about the nature of both the random field and inspection:

- The stochastic field is considered as second order stationary, statistically homogeneous and the type of marginal distribution is known (e.g., Normal). Then, we focus on the characterization of the second order parameters of the marginal distribution – i.e., mean and standard deviation. In the following applications we will consider a Gaussian random field.
- A larger number of measurements (more than 100) can be performed. It implies that the structure should have important dimensions or constituted by many components. That is allowed by the future generation of inspection with drones or robots.
- Inspections are regularly spaced for simplicity of the campaign planning. However, different spatial configurations of inspections could also be considered in the optimization problem.
- Inspections are considered as perfect as defined in Section 2.2 and in the literature [20].

2.4. Karhunen-Loève Expansion

Given a probability space (Ω, \mathcal{F}, P) , a stochastic field or process with space or time Z is a collection of Z -valued random variables indexed respectively by a set s “space” or t “time”. Let us denote $Z(x, \theta)$ the one-dimensional stochastic field where θ represents the randomness and x the spatial coordinate. $Z(x, \theta_i)$ is called the i^{th} trajectory of this field and corresponds to a given realization θ_i of the field for whatever location x . $Z(x_l, \theta)$ is a random variable that is generated by θ at a given location $x = x_l$ that is characterized by its marginal distribution. Since we consider here only homogeneous stochastic fields, the marginal distribution of $Z(x_l, \theta)$ is independent on the location. For example, if $Z(x, \theta)$ represents the one-dimensional random field of the material strength for various beams built with the same isotropic and heterogeneous material, the proposed procedure aims to characterize the marginal distribution of strength from a series of spaced correlated NDT measurements on each component. In this case a trajectory represents one series of one-dimensional measurements on a given beam. A stochastic field is second order stationary if it follows three main properties:

- the expected value $E[Z(x, \theta)]$ does not depend on the location x – i.e., $E[Z(x, \theta)] = \mu_Z$;
- the variance $V[Z(x, \theta)]$ does not depend on the location x – i.e., $V[Z(x, \theta)] = \sigma_Z^2$; and
- the spatial covariance $COV[Z(x, \theta), Z(x', \theta)]$ depends only on the distance $(x-x')$.

Thus, the second order stationary is a property restricted to the two first probabilistic moments. It can be shown that various random fields such as geometries of welds for ships [37] or the spatial distribution of chloride concentration in reinforced concrete (RC) structures can be represented by stationary stochastic fields [38]. Note that if $E[Z(x, \theta)]$ is not constant with space, the time-dependent trend of the signal can be subtracted and the stationarity properties could be proved for the field $(Z(x, \theta) - E[Z(x, \theta)])$.

Several approaches can be used to represent a stochastic field $Z(x, \theta)$: Karhunen-Loève expansion, approximation by Fourier series, approximation EOLE, variograms, etc. [39]. In this paper, we select a Karhunen-Loève expansion to represent the stochastic field of the quantity of interest $Z(x, \theta)$ (resistance, porosity, water content, etc.). Karhunen-Loève expansion was selected by taking into account its simplicity of implementation and computational time. This expansion represents a stochastic field as a combination of orthogonal functions on a bounded interval $[-a, a]$:

$$Z(x, \theta) = \mu_Z + \sigma_Z \sum_{i=1}^{n_{kl}} \sqrt{\lambda_i} \xi_i(\theta) f_i(x) \quad (1)$$

where, μ_Z is the mean of the field Z , σ_Z is the standard deviation of the statistically homogeneous field Z , n_{kl} is number of terms in the truncated expansion, $\xi_i(\theta)$ is a set of independent centered Gaussian random variables, and λ_i and $f_i(x)$ are, respectively, the eigenvalues and eigenfunctions that depend on the type of autocorrelation function (ACF) $\rho(\Delta x)$. It is possible to analytically determine the eigenvalues λ_i and eigenfunctions $f_i(x)$ for some autocorrelation functions [40]. For example, if we assume that the field is second order stationary and we consider an exponential ACF:

$$\rho(\Delta x = x_1 - x_2) = \exp\left(-\frac{|\Delta x|}{b}\right); 0 < b \quad (2)$$

where b is the an autocorrelation parameter and $\Delta x \in [-a, a]$. The following transcendental equations can be obtained for the exponential ACF:

$$\begin{cases} \frac{1}{b} - \omega \tan(\omega a) = 0 \\ \omega - \frac{1}{b} \tan(\omega a) = 0 \end{cases} \quad (3)$$

where ω is obtained by solving eq. (3). If the solution of the second transcendental equation is noted ω^* , the eigenfunctions are:

$$f_i(x) = \begin{cases} \frac{\cos(\omega_i x)}{\sqrt{a + \sin(2\omega_i a) / 2\omega_i}} & \text{for even } i \\ \frac{\sin(\omega_i^* x)}{\sqrt{a - \sin(2\omega_i^* a) / 2\omega_i^*}} & \text{for odd } i \end{cases} \quad (4)$$

and the corresponding eigenvalues become:

$$\lambda_i = \begin{cases} \frac{2}{b(1/b^2 + \omega_i^2)} & \text{for even } i \\ \frac{2}{b(1/b^2 + \omega_i^{*2})} & \text{for odd } i \end{cases} \quad (5)$$

The spatial variability of various material properties or model parameters could be represented by an exponential autocorrelation. For instance, Figure 3 presents an autocorrelation function computed from cone penetration tests measurements in Australia [35]. It is noted that an exponential ACF as the described by eq. (2) could be used to represent the spatial autocorrelation of the measurements. The exponential ACF is adopted herein because we found that the experimental autocorrelation of the

spatial measures presented in section 5 follows this trend. However, other ACFs could be more appropriate to describe the spatial variability of other parameters.

3. DESCRIPTION OF THE PROPOSED METHODOLOGY

3.1. Proposed procedure

This methodology focuses on optimizing identically spaced inspections on structural components of similar characteristics – i.e., built with the same material and exposed to similar conditions. For instance, a set of 1D components (beams), or a large 1D-component subdivided artificially or physically (expansion joint or construction joints as pipe joints in a water network) in a set of short components, or belonging to a wall type structure (steel sheet pile or concrete wall). For illustrating the methodology, we consider a set of large 1D-components (beams). Section 4.4 discusses the case of small components for which characterization of spatial variability is difficult.

By using the results of inspections and random field modeling, we propose a two stages inspection method that provides: (i) the parameters of the spatial autocorrelation function and (ii) weakly correlated measurements that are gathered to build a sample used to characterize the statistics and the marginal distribution of Z . Figure 1 presents the flowchart of the proposed methodology.

The first stage encompasses three starts with an exhaustive inspection with $N_{s,l}$ inspections closely separated at distance L_b on a single component. This exhaustive inspection aims at obtaining correlated measurements used to estimate the autocorrelation parameter b (eq. (2)). By assuming that the random field is ergodic, one trajectory is sufficient to characterize the whole joint distribution of the stochastic process. L_b is mainly defined by expert knowledge. If there is no information about L_b , a small distance could be used. It could be reduced if there is no correlated information between two consecutive measures. This stage also requires the definition of the expected precision and confidence of the estimates to characterize. The following two steps are carried out when this information is available:

Step 1.1 – Assessment of the autocorrelation parameter and first estimates of Z : the experimental autocorrelation computed by the procedure described in Section 3.2. Once b is estimated, it is possible to use eq. (2) to determine an inspection distance, L_c , which provides weakly correlated events for Z during the inspection of the components. L_b and L_c can be related by the generic term IDT for Inspection Distance Threshold. Thus, L_b and L_c should satisfy: $L_b \in]0, \text{IDT}[$ and $L_c \in]\text{IDT}, L[$ where L is the length of the component. The IDT is defined by assuming that after a given distance, the events measured from an inspection can be considered as weakly correlated. A Spatial Correlation Threshold (SCT) of the spatial autocorrelation is used to determine IDT. Thus from eq. (2), the relationship between IDT and SCT is:

$$\text{IDT} = -b \ln(\text{SCT}) \quad (6)$$

For instance, for $b = 20\text{cm}$ and $\text{SCT}=0.2$, $\text{IDT}=32.2 \text{ cm}$. The selection of a given SCT value will influence the parameter estimate precision. Such an aspect is illustrated in detail in section 4.2. Besides determining b , the data obtained from the inspection on the first component (weakly correlated measures) is considered to determine first estimates of the mean μ_Z and σ_Z and the standard deviation of Z .

Step 1.2 – Optimization of the number of measures by using Monte Carlo simulations: the parameters b , μ_Z and σ_Z are used for modeling inspection trajectories by combining eq. (1) and

Monte-Carlo simulations. Each simulation simulates an inspection over a new component. Various components (whole structure) are simulated. The distance between two consecutive simulated measures for each trajectory is L_c . These simulations are devoted to determine an optimal number of inspections in terms of the precision and confidence on the estimates that are required by the asset owner (Section 3.3). Consequently, depending on the structural constraints (e.g., number and length of components) the outputs of this stage are the minimum: (i) number of components N_t , and (ii) number of inspections per component N_s separated by a distance L_c .

Once Stage 1 provides an optimal configuration for new NDT inspections, Stage 2 focuses on the statistical characterization of μ_Z and σ_Z as indicated in the following step (Figure 1):

Step 2.1 – Assessment of μ_Z and σ_Z : New NDT measurements are carried out by considering the configuration provided by stage 1 (N_t , N_s and L_c). Data estimated from these weakly correlated NDT measurements is finally used to assess the statistical parameters of Z .

3.2. Assessment of the Autocorrelation Parameter from Discrete Inspections

We assume that the stationary stochastic field can be characterized by an exponential ACF that depends on a parameter b (eq. (2)) and that a trajectory is sufficient to characterize the whole joint distribution. However, the methodology can be applied to other ACF for different applications [39,41]. Let us focus on the assessment of this ACF from experimental data Z (obtained from sensors or NDT tests). Then, the autocorrelation between two observations z_0 and z_k , ρ_k is given by [34]:

$$\rho_k = \frac{\sum_{i=1}^{n_b-k} (z_i - \mu_Z)(z_{i+k} - \mu_Z)}{\sum_{i=1}^{n_b} (z_i - \mu_Z)^2} \quad \text{with} \quad 0 \leq k < n_b \quad (7)$$

where z_i is the value of Z at location i , μ_Z is the mean value of Z and n_b is the number of observations of Z . Two major procedures have been reported in the literature for the estimation of b for a spatially variable property from a database. The first procedure searches b that maximizes the Maximum Likelihood Estimate (MLE) [42]. The second procedure, proposed by Vanmarcke [43] and applied in [44], estimates the model parameter that provides the best fit to the sample autocorrelation. This last method can lead to a biased estimation when data is lacking. Consequently, we use the MLE for the estimation of b . Thus, the likelihood function writes:

$$L_h = \prod_{i=1}^k \left(\frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\nu_i^2}{2}\right) \right) = \left(\frac{1}{\sqrt{2\pi}} \right)^k \exp\left(-\frac{\sum_{i=1}^k \nu_i^2}{2}\right) \quad (8)$$

where ν_i is the i^{th} component of the vector of independent standard values obtained from:

$$\nu = \mathbf{C}^{-1} \left(\frac{\hat{\mathbf{Z}} - \mu_{\hat{\mathbf{Z}}}}{\sigma_{\hat{\mathbf{Z}}}} \right) \quad (9)$$

where $\hat{\mathbf{Z}}$ is the vector of measurements after inspection of the random variable Z and \mathbf{C} a lower triangular matrix such that $\mathbf{C}\mathbf{C}^T = \boldsymbol{\rho}$ and $\boldsymbol{\rho}$ the autocorrelation matrix.

3.3. Definition of a reliability oriented measure of quality of inspection

When focusing on a practical application, we aim at optimizing the total number of weakly correlated inspections $N = N_p \times N_s \times N_t$ where N_p is the number of repetitive tests for reducing the error of inspection, N_s is the number of inspected sections and N_t the number of trajectories (Figure 4). Here,

the error of inspection is not considered (Section 2.3) and by neglecting the N_{sI} inspections of the first stage, the total number weakly correlated inspections simply becomes $N=N_s \times N_t$.

We use simulated data to find the minimum number of inspections that ensure a given quality of the estimates. In this case the quality will be evaluated with respect to the ‘theoretical’ expectation and standard deviation of the stochastic field Z (μ_Z and σ_Z). $\mu_{\hat{Z}}$ and $\sigma_{\hat{Z}}$ are respectively the mean and standard deviation of the stochastic field Z estimated from N simulated measurements after inspection and computed by:

$$\mu_{\hat{Z}} = \frac{1}{N} \sum_{i=1}^N \hat{z}_i \quad \text{and} \quad \sigma_{\hat{Z}} = \sqrt{\frac{1}{N} \sum_{i=1}^N (\hat{z}_i - \mu_{\hat{Z}})^2} \quad (10)$$

The quality of a result of inspection can be expressed by several concepts. If we consider the error of measurement, risk oriented measures have been developed: PoD, PFA [14], PoI [17], PGA and PWA [3,4]. Otherwise, and in case of a finite number of measurements and a finite size of the structure (spatial field effect), other measures can be defined based on distribution tails or a confidence interval of the probability of failure [44]. We select in this paper a confidence interval of both the mean μ and the standard deviation σ expressed as a percentage ε (precision) of μ and σ , respectively. We combine random field modeling and Monte-Carlo simulations to estimate the bounds of the confidence interval numerically for target probabilities $P_{ii,\mu}$ and $P_{ii,\sigma}$ for both the mean and the standard deviation, respectively. In a real case, these probabilities could be defined by the asset owner depending on the type of application (structural reassessment, reliability study, etc.). These target probabilities are compared with the following probabilities computed from inspection data:

$$P_{\hat{Z}}^{\mu} = P\left(\mu_{\hat{Z}} \in \left[(1 - \varepsilon_{\mu})\mu_Z; (1 + \varepsilon_{\mu})\mu_Z\right]\right) \quad (11)$$

$$P_{\hat{Z}}^{\sigma} = P\left(\sigma_{\hat{Z}} \in \left[(1 - \varepsilon_{\sigma})\sigma_Z; (1 + \varepsilon_{\sigma})\sigma_Z\right]\right) \quad (12)$$

Eqs (11) and (12) are very difficult to estimate. Hence, they are numerically estimated herein by considering data generated from random field modeling. If only a statistical error is considered (measures are independent), confidence intervals theory gives analytical estimates of the precision (ε_{μ}^{th} and $\varepsilon_{\sigma}^{th}$) as a function of the number of measurements N :

$$\varepsilon_{\mu}^{th} = u_{1-\alpha/2} \frac{\sigma_Z}{\mu_Z \sqrt{N}} \quad (13)$$

$$\varepsilon_{\sigma}^{th} = u_{1-\alpha/2} \frac{1}{\sqrt{2N}} \quad (14)$$

where $u_{1-\alpha/2} = 1.96$ for $P_{ii,\mu} = P_{ii,\sigma} = 0.95$. In the case of measurements on trajectories with a weak dependency between data, these values will increase. It is also important to note that both precision and confidence depend on the number of measurements and therefore could be limited by the structural configuration – e.g., the maximum N is limited by the structural size or the number of components.

Depending on the final use of the estimates, several precisions ε or confidence levels P_{ti} can be required for the mean and the standard deviation. The optimal number of inspections can differ between these two estimates. For instance, for optimizing the assessment of μ_Z :

$$N_{opt,\mu} = \underset{N}{\operatorname{argmin}} \left(P_{ti,\mu} \leq P_Z^\mu \right) \quad (15)$$

A different value $N_{opt,\sigma}$ could be obtained for optimizing the assessment of σ_Z . Then, the optimal number of measurements N_{opt} writes:

$$N_{opt} = \max \left(N_{opt,\mu}; N_{opt,\sigma} \right) \quad (16)$$

4. APPLICATION TO A NUMERICAL EXAMPLE

4.1. Problem Description

This example aims to illustrate: (i) the effect of considering correlated measures in the assessment of the mean and standard deviation of the marginal distribution, (ii) the possibilities for the selection of optimal inspection configurations for specific structures, and (iii) the special case of small size structures. We will therefore consider in the first part a structure with a larger size for which $L \gg b$ allowing to assess b from a theoretical point of view. The last part of this section highlights some issues about the size of the structures.

We suppose that the random field to inspect is Gaussian, stationary, ergodic, and characterized by: $b = 1\text{m}$, $\mu_Z = 100$ and $\sigma_Z = 20$ and that the length of the structure is $L=200\text{ m}$. This example does not focus on the assessment of the autocorrelation parameter b . Section 5 will present a complete application of the two-stages methodology for a study case including some considerations for the assessment of b . We aim to provide an inspection protocol that ensures: $P_{ti,\mu} = P_{ti,\sigma} = 0.95$.

4.2. Effect of SCT on the Precision of the Estimates

We first analyze the effect of the choice of SCT on the precision of the estimates quantified by ε_μ and ε_σ (Figure 5). For $N_s=20$ measurements on a large component ($N_i=1$) with length $L=200\text{m}$, the theoretical values computed from eqs. (13) and (14) are: $\varepsilon_\mu^{th} = 9.3\%$ and $\varepsilon_\sigma^{th} = 33\%$. These values correspond to the maximum precision estimated from $N=20$ independent measurements (statistical error only). It is observed that the precision obtained from consecutive measurements is close to the theoretical value when SCT is small. This effect is more pronounced when SCT is lower than 0.3 for both ε_μ and ε_σ . Therefore, it is noted that a threshold level of autocorrelation could be defined to provide the distance of inspection. In the following, we fix $\text{SCT}=0.3$ to compute IDT and define L_c from eq. (6).

4.3. Selection of Optimal Configurations for Inspection

As described in Section 3.3, for given precisions (for instance $\varepsilon_\mu = 5\%$ and $\varepsilon_\sigma = 20\%$) and a fixed L_c value, it is possible to estimate the required number of measurements N_s and N_i to ensure $P_{ti,\mu} = P_{ti,\sigma} = 0.95$ (eqs. (11) and (12)). By assuming that $\text{SCT}=0.3$, eq. (6) provides that $\text{IDT} = -b \ln(0.3) \approx 1.2\text{m}$. Since $L_c \in]\text{IDT}, L[$, we select $L_c = 1.2\text{m}$. Figure 6 presents the couple of minimum required values for N_s and N_i to guarantee these requirements. For both estimates, the number of measures per component

decreases when the number of components is larger. Based on a given structural configuration (e.g., limited number or length of components), Figure 6 illustrates how estimating the number of measures per component N_s spaced by $L_c = 1.2$ m on N_t components. The number of required measures is almost the same for these quality requirements. However, more measurements will be needed if we require a larger precision on the standard deviation.

The optimization can be also expressed in terms of total number of measurements N . Figure 7 gives the minimum total number of required measurements as a function of the number of available components N_t , for instance a given number of beams in a bridge. As indicated by eq. (10), there are different optimum values for the mean and the standard deviation. In this case, the optimal number of measures N_{opt} is driven by the assessment of μ_Z and computed from eq. (11). Here the optimal number is $N_{opt} = 40$ for $N_t = 4$ components and $N_s = 10$ measures per component separated by $L_c = 1.2$ m. This inspection configuration requires only a total inspection zone of 12m per component. Depending on structural accessibility, the decision maker could decide to perform more spaced measurements that should improve the quality of the estimates. Different conclusions could be drawn if costs of measurements are included in the analysis. For example, the cost of inspecting an additional component could be higher than the cost of increasing the number of measures per component.

4.4. Effect of the Size of the Structure

Previous subsections assume that the components are larger enough to find a set of “weakly correlated” measurements. Let us focus on small structures and the related shortcomings for optimal characterization. We consider the same stochastic field as described in Section 4.1 and we decrease the size of a structure from the original length of 200m until 10m. Figure 8 shows the effect of the size of the structure on the precision of the estimates μ_Z and σ_Z . These results correspond to $N=20$ measures on a single component. Therefore, the theoretical precisions agree with the values computed in Section 4.2. When $SCT > 0.8$, there is no a unique trend because in this case the measures are very close and only describe the local shape of the inspected trajectory. For components larger than 50m, 20 measurements can be realized whatever SCT. It is consequently observed that for $L > 50$ m both ε_μ and ε_σ converge similarly to the case where $L = 200$ m (Figure 5). It is also noted that for shorter components ($L = 10$ and 25m) the values of ε_μ and ε_σ cannot be computed because it is not possible to carry out 20 measures. Therefore, the convergence until the theoretical value cannot be reached for shorter components. For shorter components, the precision on the assessment of the estimates μ_Z and σ_Z could be improved by adding more measurements on additional components $N_t > 1$. However, if $L < b$, it could be very difficult to obtain a good characterization of the spatial variability.

5. APPLICATION TO A STUDY CASE

5.1. Description of the Structure and the NDT Tool

The objective of this example is to characterize the marginal distribution and spatial variability of the water content W , modeled as a second order random variable, for a reinforced concrete beam exposed to natural environmental conditions in Bouguenais (Pays de la Loire, France) by using NDT inspections (Capacitive technique). The inspection was performed on the first of March 2012 with high relative humidity of air ($H_{air} = 99\%$) and a low temperature ($T = 5^\circ\text{C}$). Figure 9 presents the configuration of the experiment. The proposed methodology is applied to inspections on two

horizontal trajectories called Line A and Line B. A vertical distance of 40 cm separates these lines. To neglect the error of the measurement, we performed $N_p=30$ repetitive tests on each point and we select the mean value to represent the reference measurement of water content at each point. Figure 9 also includes the histogram for these $N_p=30$ repetitive tests. Therefore, according to Section 2.2, we justify the assumption that these repetitive tests will provide a “perfect” measurement. The repetitive tests are carried out on $N_s=80$ horizontal points separated by 20 cm for each line.

Figure 10 presents the experimental devices. The principle of the Capacitive technique is based on the resonance frequency measurement of an oscillating circuit (around 30-35 MHz) between several electrodes lying on the upper face of the concrete slab (Figure 9) [45,46]. As the combination of medium and electrodes behave like a capacitor, a variation of the dielectric properties of the medium induces a shift of the resonant frequency. A calibration enables to obtain directly the concrete relative permittivity from the frequency measurements, which is mainly related to the water content and the mixing components [47–49]. The volume investigated depends on the geometry of the electrodes. In this study, we used larger electrodes to investigate a 6-8 cm depth of concrete, volume that is more coherent with ground penetrating radar measurements. For simplicity, we consider, for this concrete, a linear relationship between relative humidity and NDT outputs:

$$W = \frac{48.4981 - (F_c - F_{air})}{31.753} \quad (17)$$

where F_c and F_{air} are frequency values in RC beam and in the air at situ, respectively. Ongoing studies in several laboratories worldwide are searching for more accurate relationships by considering a multi-technique approach to account that each NDT tool is sensitive to humidity, porosity, size and type of aggregates.

5.2. Data and Modeling

Figure 11 presents the two trajectories obtained for lines A and B based on measures with a filter that remove the few outliers. The shape and the values are different for each line. Line A shows more variability but lower values in comparison to line B. It is expected to find lower water content in the line A because the drying process is faster in the upper zones – i.e., they are more exposed to wind and there is a diffusion of water through the lower zones. The variability could also be explained by other factors as the segregation of concrete. Taking into account this variability with height, we cannot merge the data of both lines to estimate the marginal distribution of W in this practical application. Therefore, in this case we will use the data from one trajectory to characterize the spatial variability and recommend an optimal number and spatial distribution of measures for the second trajectory. We verify first that the autocorrelation shape is similar.

Figure 12 presents the autocorrelation data for trajectories A and B. We obtained a classical shape where the autocorrelation decreases with distance including negative values [34]. After fitting the experimental data with eq. (2) according to the method presented in Section 3.2, we found that the exponential autocorrelation functions are very close for the two lines. We obtained: $b=0.45\text{m}$ and $b=0.51\text{m}$ for lines A and B, respectively. It means that the exponential function could be useful to represent the autocorrelation and therefore for modeling the horizontal spatial variability of the water content in RC beams at different depths. Data of line B seems to be more regular (Figure 11) and its experimental autocorrelation is more close to the exponential function. Therefore, in the following, we will use the data from line B to characterize the spatial variability and recommend an optimal number and spatial distribution of measures for the study of the data of line A. Figure 12 only presents

autocorrelation values for 8m to illustrate the decay of the values for the first 2 meters; but these values were estimated by considering the information of the whole beam (16m).

5.3. First Stage

According to Section 3, the first stage of the inspection methodology is devoted to the assessment of b on a single trajectory. There is an error on the assessment of b because this parameter is deduced from a limited number of measurements N_{sI} on a given trajectory. This error is mainly due to the number of measurements N_{sI} on a trajectory (statistical error) and the choice of L_b . Although b could be modeled as a random variable B , we decide to consider it as a deterministic value determined from sufficiently correlated measures. b for line B is $b=0.51\text{m}$. Thus, we validate that the inspection distance $L_b = 0.2\text{m}$ ensures higher correlation between measured data (Figure 12). By defining a $\text{SCT}=0.3$, we can determine $\text{IDT}=0.61\text{m}$ from eq. (6). Then the distance between two weakly correlated inspections is $L_c = 0.6\text{m}$ for determining the first estimates of μ_Z and σ_Z that will be used to model the random field. By using the experimental data obtained from this first stage, Figure 13a plots μ_B and σ_B as a function of the number of measures in the first trajectory N_{sI} for 1,000 simulated trajectories. The convergence of μ_B through the value of b determined from the 80 measurements is faster and the error is less than 0.05m for $N_{sI} \geq 45$ measures. σ_B decreases when N_{sI} is larger by reducing the uncertainty on the assessment of the parameter b .

Figure 13b presents the mean and the 95% confidence interval of μ_B for 1000 simulated trajectories as well as the values of b computed from experimental data, as a function of N_{sI} . The various experimental points for a given N_{sI} correspond to different sets of N_{sI} over the total number of measurements. It can be observed that the scatter is large when N_{sI} decreases and could even reach 0.9m for $N_{sI}=20$. It is also noted that b estimated from experimental data is close to μ_B when $N_{sI}>45$. These results therefore indicate that the assessment of b requires a minimum number of correlated measures N_{sI} .

Let us now fix the value $N_{sI}=45$ measures and optimize the number and spatial distribution of measurements. By considering the autocorrelation parameter identified during the first stage ($b=0.51\text{m}$) and selecting a $\text{SCT}=0.3$, the distance between two weakly correlated inspections is $L_c = 0.6\text{m}$. Due to the length of the beam, practically, the maximum number of measures is $\max(N_s)=26$. This information is used to estimate the theoretical mean and standard deviation from weakly correlated measures $\mu_{W,26}=10.12\%$ $\sigma_{W,26}=0.67\%$. Values of $\mu_{W,26}$, $\sigma_{W,26}$ and b will be used to optimize the number and spatial distribution of inspections.

Figure 14 describes the effect of the choice of a confidence level ($P_{ti}=95\%$ and 90%) on the precisions ε_μ and ε_σ . After performing Monte Carlo simulations, we plot the evolution of ε_μ and ε_σ as a function of the number of measures per trajectory N_s . The shape of the curves is consistent with the theoretical eqs. (13) and (14). Namely, ε_μ and ε_σ decrease for larger quantity of available data. For all cases, more inspections are required if the confidence level increases. For example, at a given precision level $\varepsilon_\mu = 10\%$, the needed number of inspections N_s increases from 9 to 12 if the confidence level increases from 90% to 95% . It is also noted that the maximum precisions are limited by the geometry of the structure in this case. For instance, for a confidence level of 90% , the maximum precisions are $\varepsilon_\mu = 5.2\%$ and $\varepsilon_\sigma = 20\%$ when $N_s = 26$ measures.

For the second stage, we fix the following precision levels ($\varepsilon_\mu = 10\%$ and $\varepsilon_\sigma = 30\%$) and the confidence interval ($P_{ti,\mu} = P_{ti,\sigma} = 95\%$). Consequently, by using the results presented in Figure 14, we obtain the optimum values: $N_{opt,\mu} = 12$ and $N_{opt,\sigma} = 20$ measures. Finally, by applying eq. (15), $N_{opt} = 20$ measures. This information will be used to characterize the marginal distribution of the water content on the line A, modeled as a second order variable.

5.4. Second Stage and Validation

By considering the output of the first stage ($L_c=0.6\text{m}$, and $N_{opt}=20$ measures), the estimates of the mean and standard deviation of W for the line A are: $\mu_{W,20}=9.46\%$ and $\sigma_{W,20}=0.86\%$. To verify if these values are within the confidence interval, we take as a reference the mean and the standard deviation for all the 26 weakly correlated measures: $\mu_{W,26}=9.37\%$ and $\sigma_{W,26}=0.85\%$. This information is also used to compute the bounds of the confidence interval. Thus, Figures 15 and 16 present respectively the evolution of μ_W and σ_W with N_s for virtual (simulation) and real inspections and the quality requirements defined in Section 5.3 ($\varepsilon_\mu=10\%$, $\varepsilon_\sigma=30\%$, and $P_{ii}=95\%$). For the assessment of the mean, these results confirm that after $N_{opt,\mu}=12$ measures (found for the line B) the estimates are inside the confidence interval. Similar behavior was found for the standard deviation by confirming the optimal value $N_{opt}=20$ measures for the assessment of both estimates. We observe similar results for the virtual and the real inspection by confirming that this type of simulation is adapted for representing the spatial variability of the water content.

6. CONCLUSIONS

This paper proposed an original two stages method for the optimal stochastic characterization of random fields from NDT measures in view to (i) assess the shape parameter of the correlation function, and (ii) deduce the parameters of the marginal distribution for a second order variable. One-dimensional stochastic fields with exponential autocorrelation are selected for illustration. The role of the distance between measurements for the stochastic characterization is highlighted and a probabilistic-oriented measure of quality is defined in terms of confidence intervals of the two first statistical moments. That underlines the key role of SCT, the spatial correlation threshold that allows us to rationally define a “weakly dependence” in terms of quality of assessment of the statistical moments. The methodology relies on (i) the assessment of the autocorrelation function on a first trajectory and the use of this information for the optimization of NTD measurements (stage 1), and (ii) the assessment of the parameters of the marginal distribution on a given set of components by knowing the distance between inspections, the number of measures per component, and the number of components (stage 2). The paper ends with practical applications and suggestions for optimizing the stochastic characterization of the water content in a concrete beam by using a capacitive NDT. We found that the optimized configuration ensures the quality requirements.

Further work in this area will be addressed to:

- the application to other NDT techniques,
- the consideration of other types of autocorrelation functions,
- the updating of the optimized configuration and the value of the autocorrelation parameter after inspection of new components, and
- the extension of the methodology for optimizing 2D inspection configurations.

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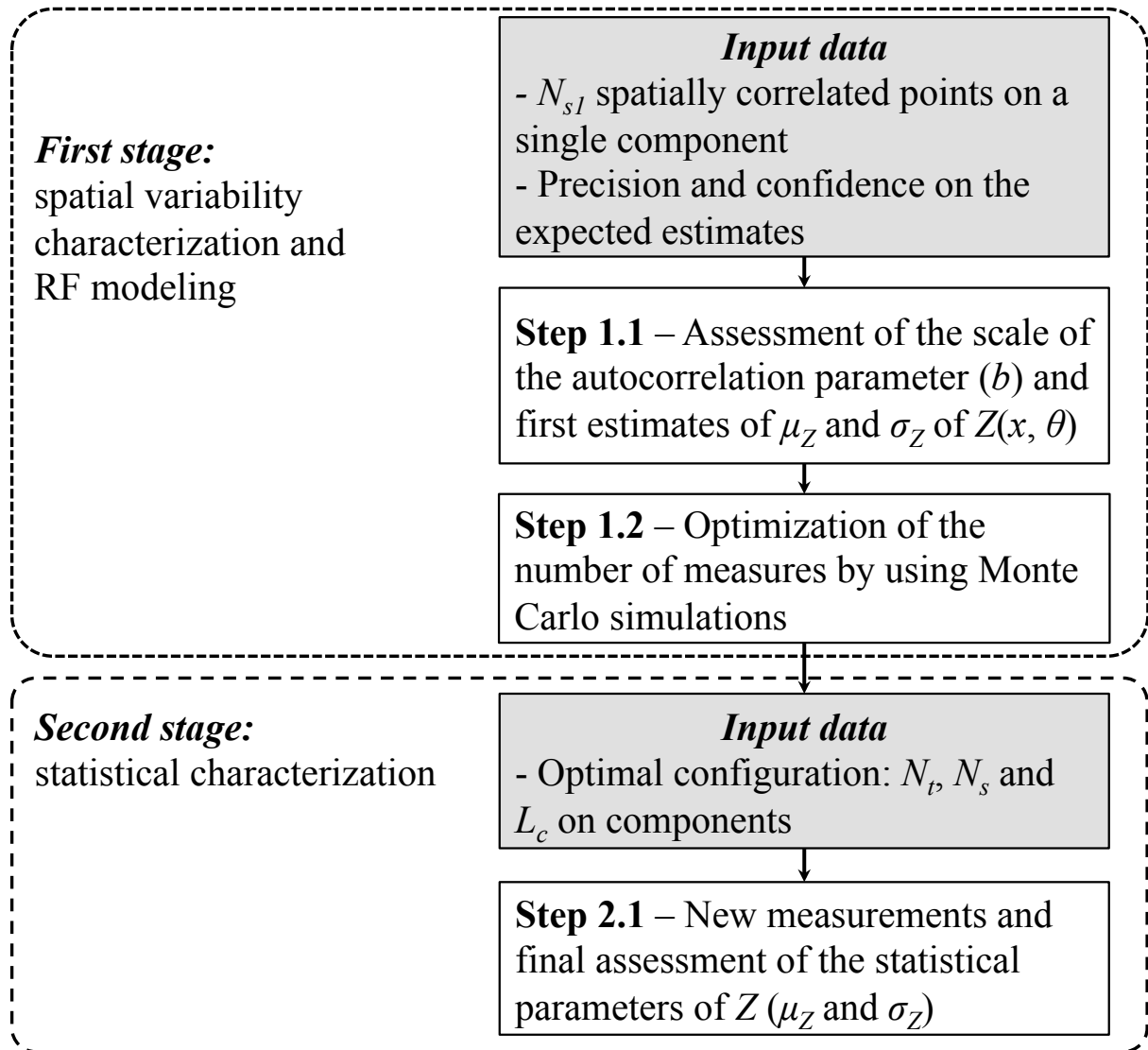


Figure 1. Flowchart of the proposed methodology.

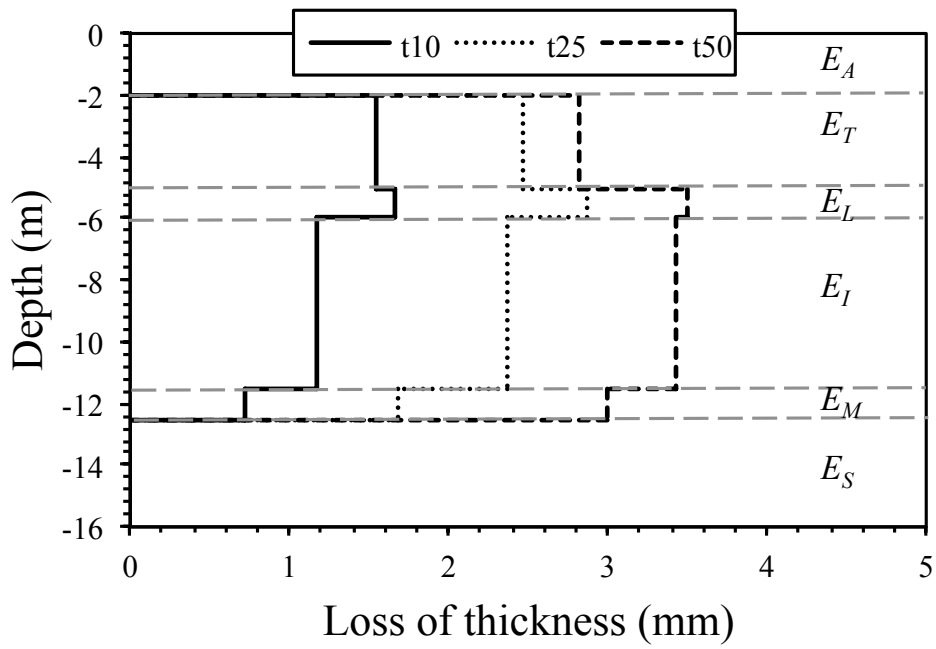


Figure 2. Mean value of steel thickness loss in each zone at times 10, 25 and 50 years (adapted from [10]).

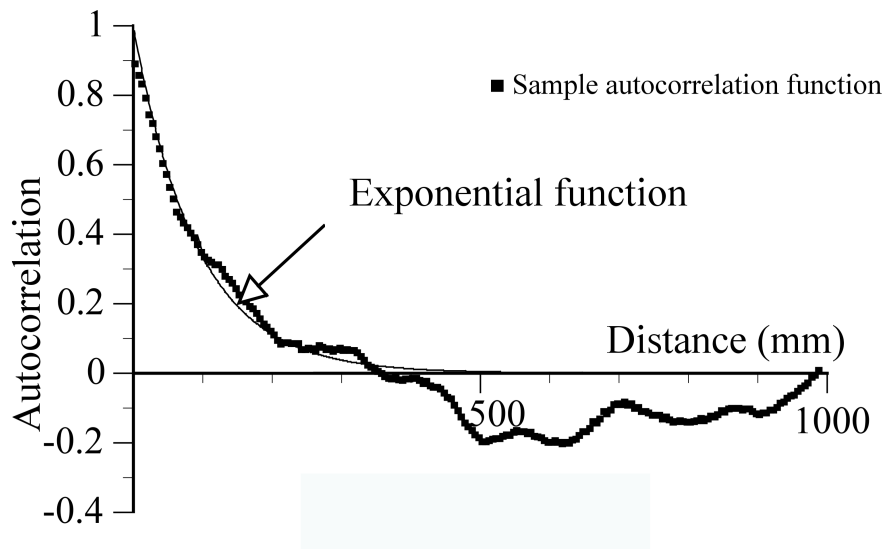


Figure 3. Spatial correlation of cone tip resistance in a clay (adapted from [35]).

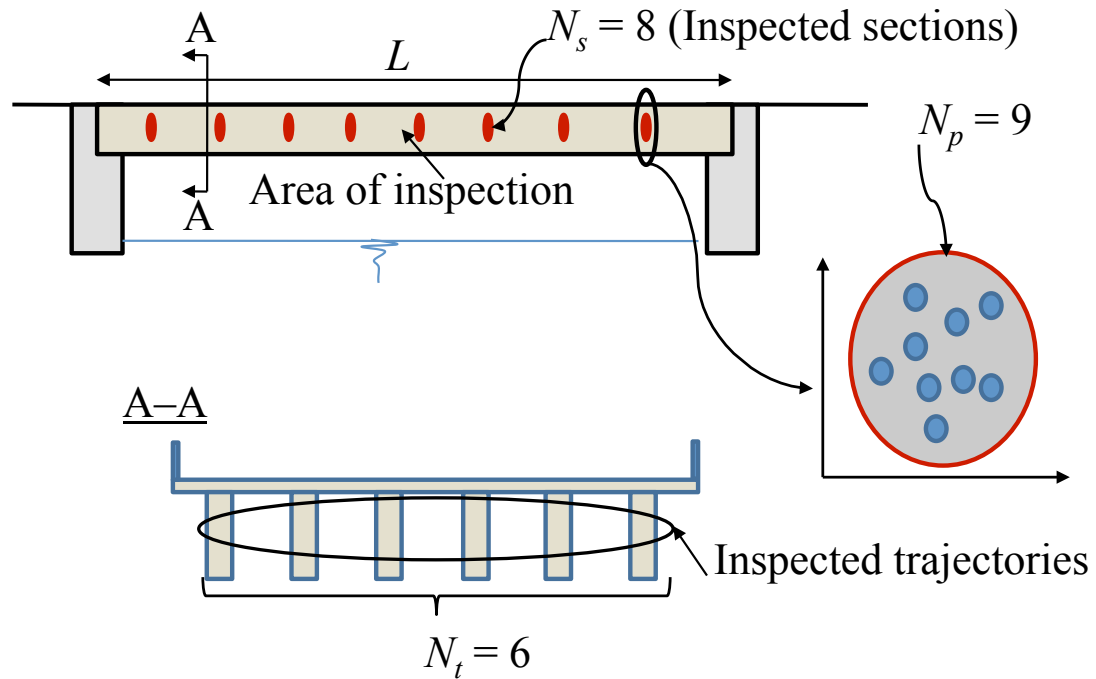


Figure 4. Definition of the number of inspections.

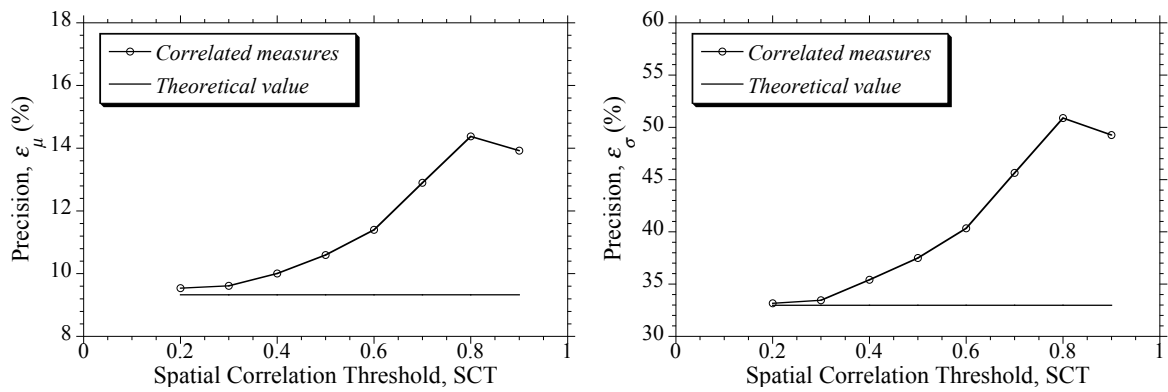


Figure 5. Effect of SCT on the precisions ε_μ and ε_σ .

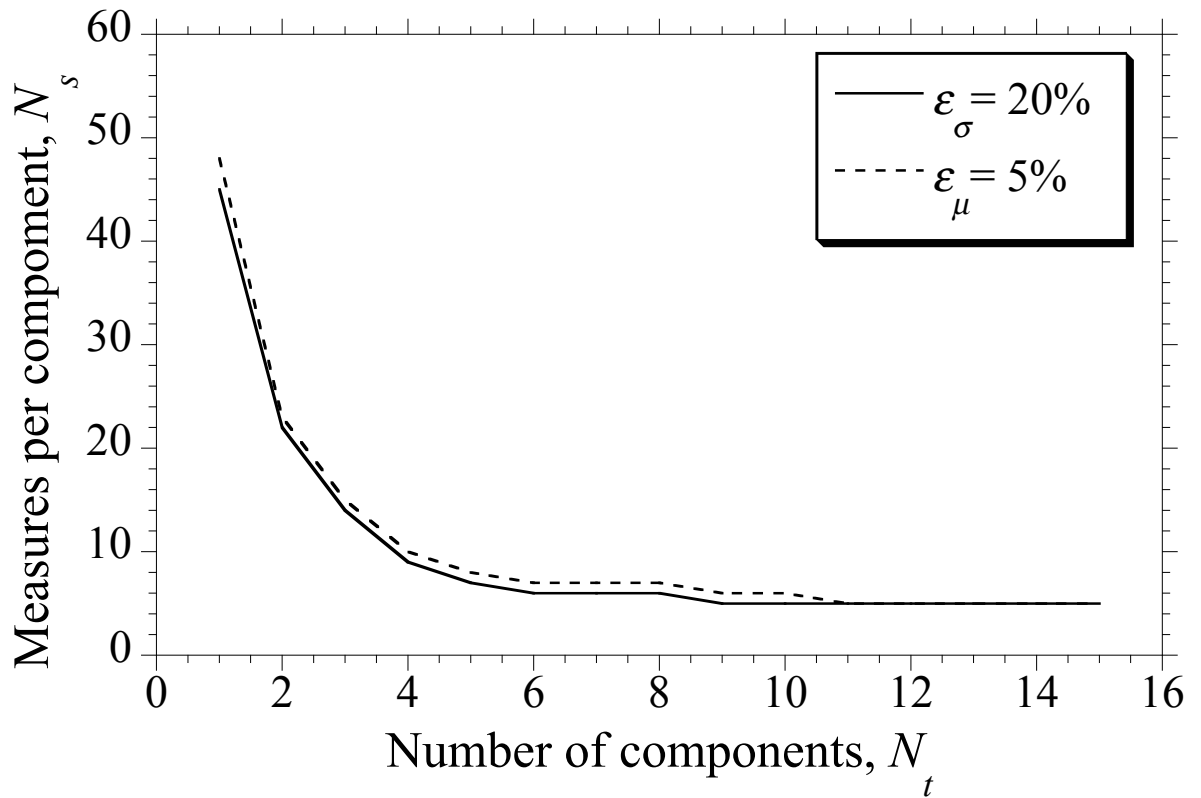


Figure 6. Number of required N_s and N_t to ensure $P_{i,\mu} = P_{i,\sigma} = 0.95$ ($L_c = 1.2$ m).

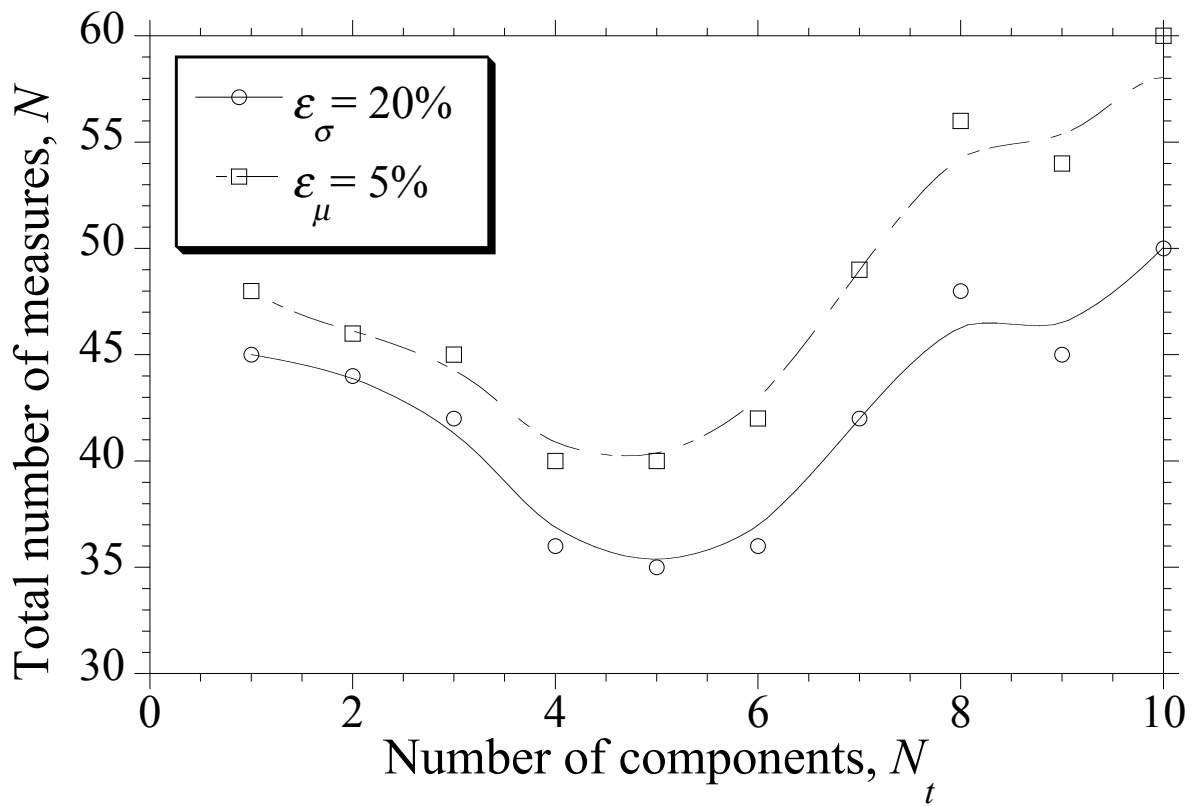


Figure 7. Total number of measures as a function of N_t to ensure $P_{i,\mu} = P_{i,\sigma} = 0.95$ ($L_c = 1.2$ m).

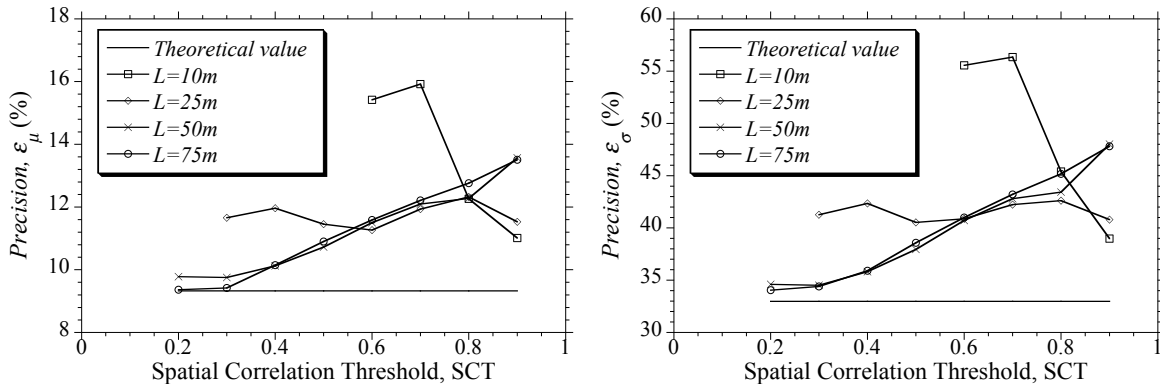


Figure 8. Effect of the size of the structure on the precisions ε_{μ} and ε_{σ} .

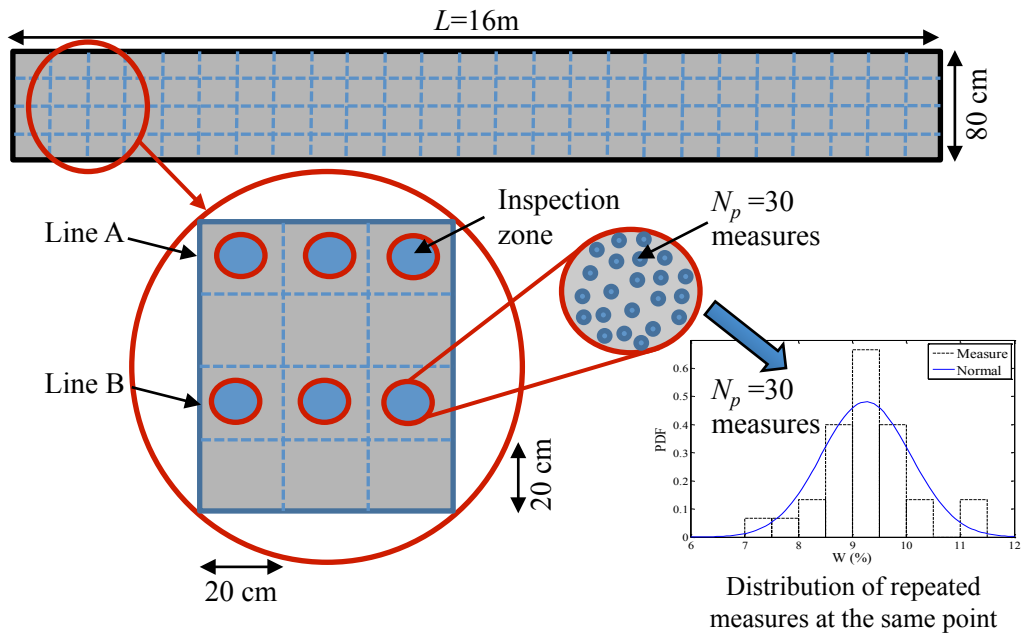


Figure 9. Configuration of the inspection at the RC beam.



Figure 10. Devices used for obtaining the NDT data.

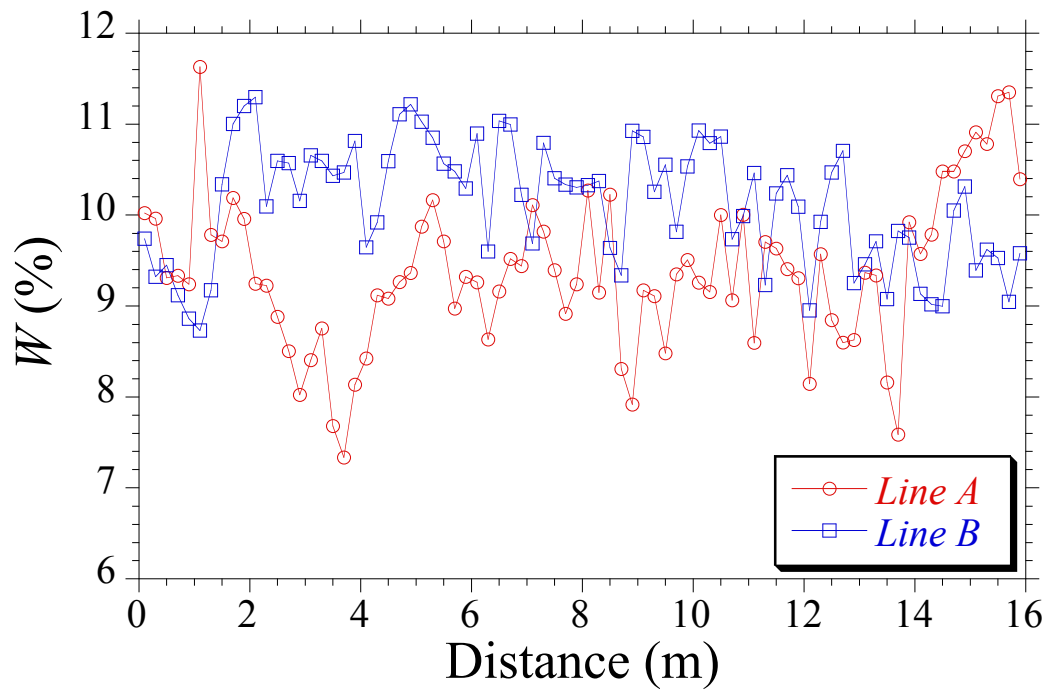


Figure 11. Experimental trajectories of W .

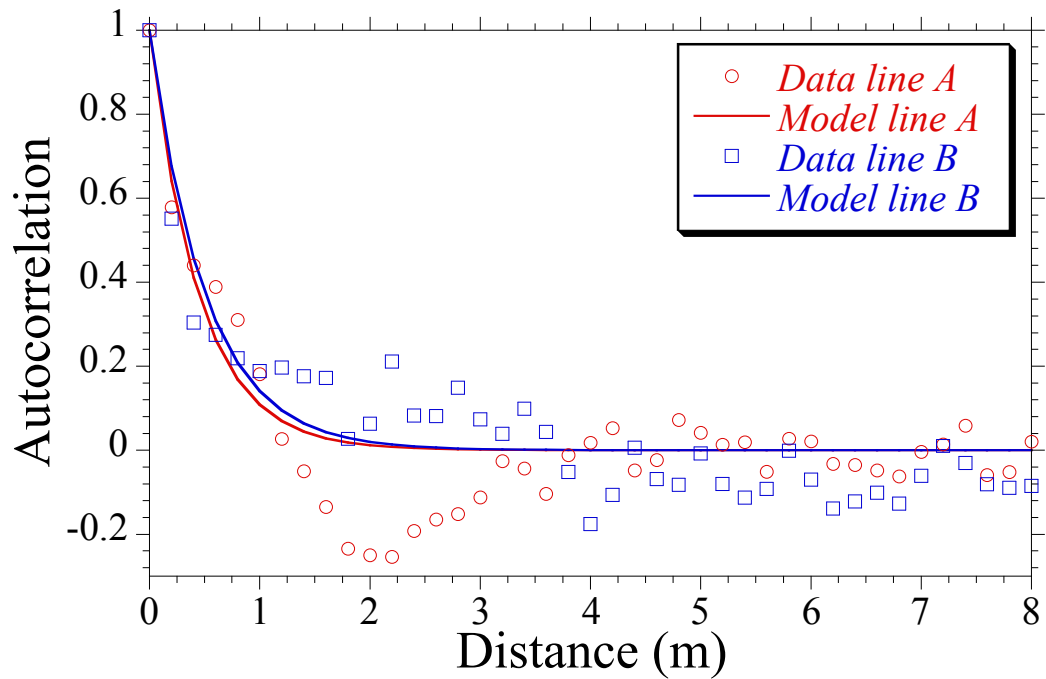


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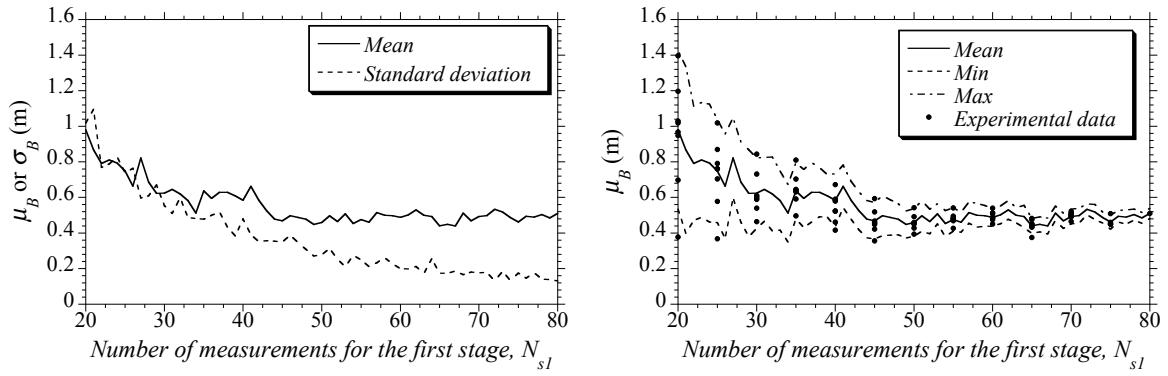


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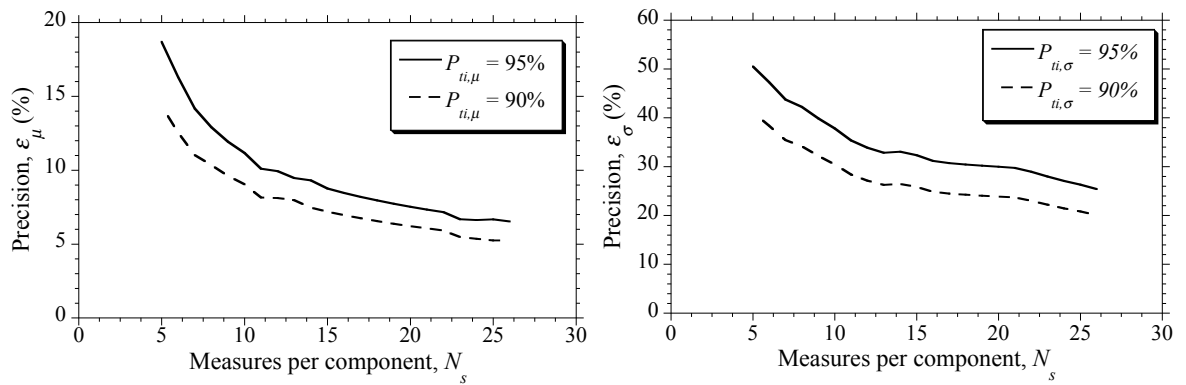


Figure 14. Influence of N_s on the precisions ϵ_μ and ϵ_σ .

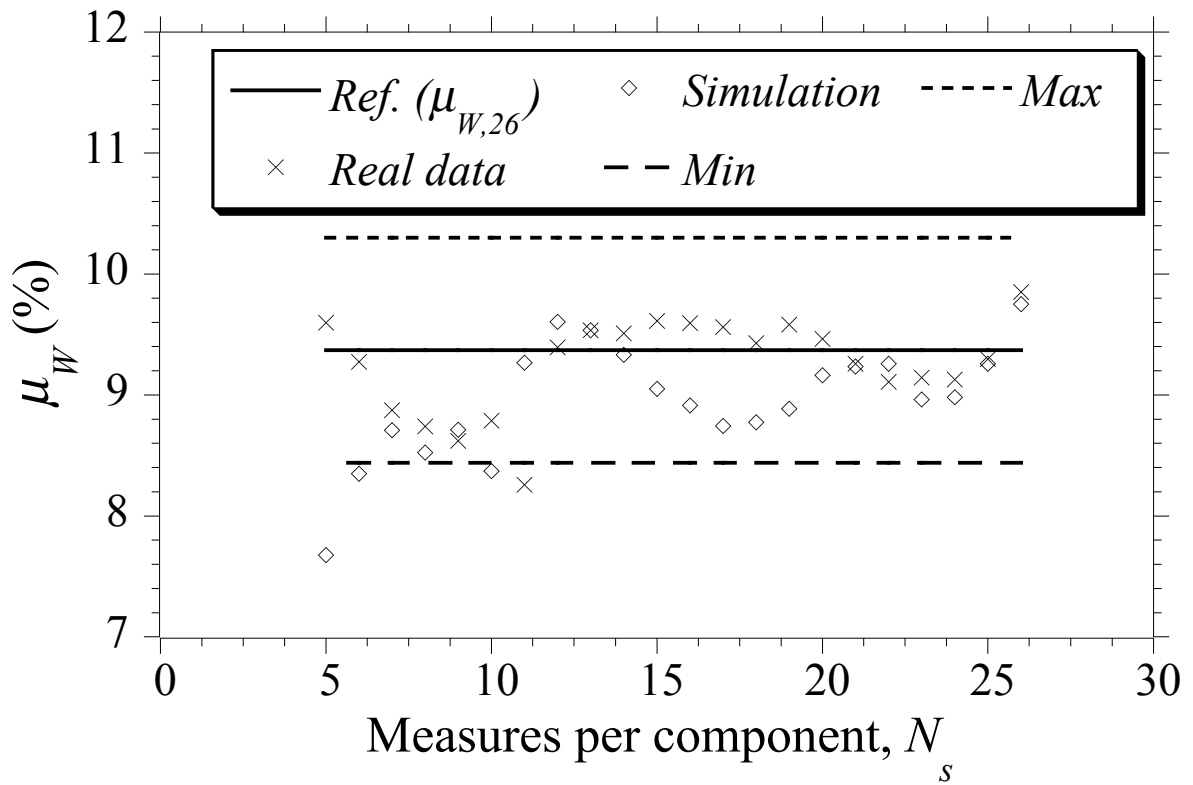


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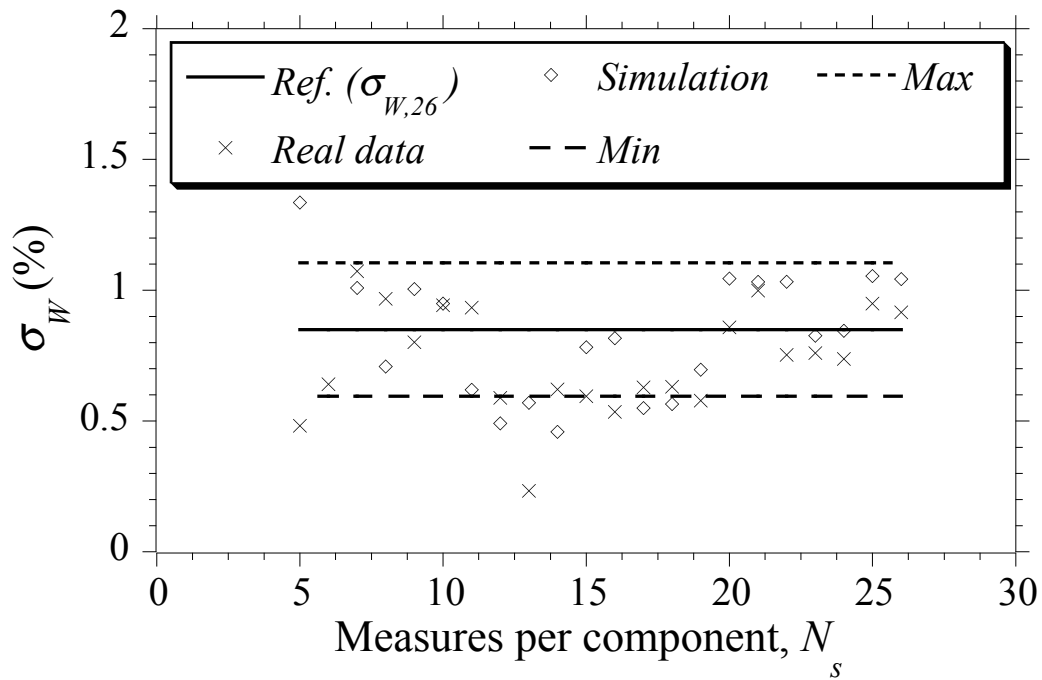


Figure 16. Comparison between modeling and real results in the case of $\varepsilon_\sigma=30\%$ and $P_{i,\sigma}=95\%$.