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# Multiscale investigation of stress-corrosion crack propagation mechanisms in oxide glasses

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## **Abstract**

Fracture propagation involves the coupling of many length scales ranging from the sample loading geometry to the molecular level. In brittle materials, the length scales of the damage process zone are reduced to a submicrometric scale and the coupling with the macroscopic scale is expected to be the domain of linear elastic fracture mechanics (LEFM). However, although 2D elastic analyses are generally adequate to describe the sample deformation at macroscopic scales, local investigations of failure mechanisms at the sample free surface require the use of 3D mechanical tools due to the crack front local curvature and to the corner point singularities at the intersection between the crack front and the external surfaces of the sample. We present here a thorough multiscale investigation of

the slow crack growth of a sharp crack in oxide glasses in the stress-corrosion regime, combining experimental and numerical analyses of the displacement fields from the millimeter scale to the nanoscale range. The principal aim of the study is identifying the length and time scales of the mechanisms of damage and interaction between water and glass, which have been the subject of an extensive debate in the last decades.

## **Keywords**

Multiscale mechanical analysis, Stress-corrosion, Atomic Force Microscopy, Digital Image Correlation, Glass Plasticity

## **1. Introduction**

Glass is a very widespread material due to its excellent transparency and corrosion resistance. It also has indeed excellent mechanical properties, because it is actually very stiff and can be brought to very high strength when it is produced into very thin fibers or layers, by reducing the number and size of defects and taking a particular care of the external surfaces. The main limitation remains the elevated brittleness of glass, i.e. its tendency to initiate and propagate fractures with very low energy dissipation. This can manifest itself in two very different ways. The first one is the well known catastrophic (critical) fracture, occurring upon overcoming some critical static or dynamic (shock) loading, and resulting in propagation velocities close to the sound speed in glass, i.e. several km/s. The second more subtle manifestation is the slow sub-critical propagation of pre-existing flaws under moderate stresses, which can involve very low velocities ranging from mm/s to pm/s and below (although this becomes hardly measurable) and which plays an outstanding role in the life duration of many loaded structures (the so called “*static fatigue*”). For oxide glasses, subcritical crack growth mainly originates from stress-corrosion mechanisms, which are related to different

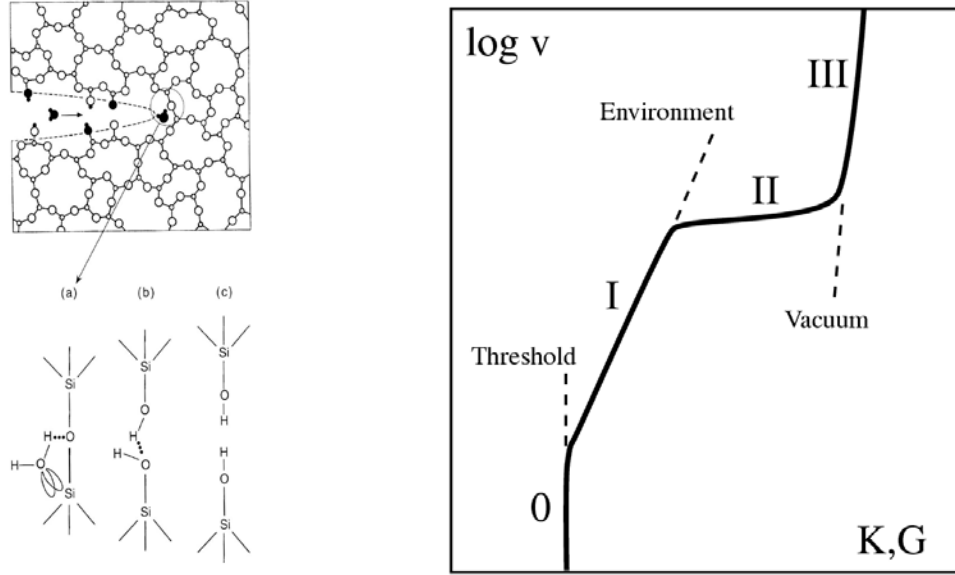
kinds of stress and temperature enhanced interactions of glass with the local environment at the crack tip, mainly with water molecules in wet or moist environment (cf. recent reviews from Ciccotti 2009, Freiman *et al.* 2009, and Wiederhorn *et al.* 2013).

The understanding of the mechanisms of glass strength reduction by Griffith cracks (Griffith 1920) and the role of stress-corrosion in the static fatigue of glass has lead to important applications concerning reinforcement fibers and telecom optical fibers which approach the theoretical strength of 10 GPa (Brambilla and Payne, 2009). When combining high quality surface finish with thermal of chemical tempering to induce compressive stresses on the glass surfaces, very strong flat glasses can also be produced, which allowed the development of very thin and light smartphone displays and a progressive increase of the use of glass as structural material such as in the transparent crosswalk over the Grand Canyon.

Stress-corrosion is a hydrolysis chemical reaction happening at the crack tip, which would normally be very slow on glass at ambient temperature, but is significantly accelerated due to stress concentration. Most ordinary oxide glasses are silicate glasses, where about 80 wt.% is constituted by a densely crosslinked network of silica tetrahedra,  $\text{SiO}_4$ , bonded by a common oxygen atom, thus creating Si-O-Si (siloxane) bridges that locally form some rings of radii down to 0.5 nm. The basic corrosion reaction is a three step reaction involving water adsorption on the Si-O bonds, then the hydrolysis reaction itself (exchange of electron and proton), and finally the separation of the bond in two separate silanol groups (Si-OH), which correspond to one step advance of the fracture in the main silicate network of the glass.

The vision of stress corrosion as a sequence of individual bond breakings by stress (and temperature) enhanced hydrolysis was established in the seventies (Wiederhorn 1967, Wiederhorn and Bolz 1970, Michalske and Bunker 1984). The kinetics of stress corrosion crack propagation can be represented by a three region scheme on a graph describing the logarithm of crack velocity  $v$

(spanning from cm/s to pm/s) against the stress intensity factor (SIF)  $K$ , when  $K$  is smaller than the toughness  $K_c$  that is of the order of  $1 \text{ MPa.m}^{1/2}$  for most glasses.



*Figure 1. Left: basic mechanisms of the stress-corrosion reactions (from Michalske and Freiman, 1983). Right: Schematic  $v(K)$  diagram for subcritical crack propagation in oxide glasses.*

Region I is the proper stress-corrosion regime, where the stress enhances exponentially crack propagation according to accelerated hydrolysis reactions. Region II is a plateau where crack velocity is limited by the migration of water molecules towards the very confined crack tip. Region III is a very steep region where the SIF is so high that crack can propagate without any contribution from water hydrolysis. In some glasses such as alkali-silicate glasses, an additional region 0 corresponds to a threshold for crack propagation.

The phenomenology of the stress-corrosion regime (region I), consists of an exponential dependence of the crack velocity on the stress intensity factor, an almost proportional dependence on humidity and an increase of crack velocity with temperature. This was experimentally established by Sheldon Wiederhorn (1967, 1970) who also proposed the following model equation:

$$v = v_0 \exp(\beta K) = A \left( \frac{p_{H_2O}}{p_0} \right)^m \exp \left( - \frac{\Delta E_a - bK}{RT} \right) \quad (1)$$

which is based on the chemical reaction rate theory for the hydrolysis of siloxane bonds by water molecules. The dependency on humidity  $\frac{p_{H_2O}}{p_0}$ , the main reactant, is a multiplicative power law with an exponent  $m$  close to 1, which is the order of the reaction. The dependency on both temperature  $T$  and  $K$  appears through an Arrhenius term, where  $R$  is the gas constant and the activation barrier  $\Delta E_a$  can be reduced by the presence of local tensile stress  $\sigma_{tip}$  at the crack tip of radius  $\rho$  (we can write  $\sigma_{tip} V_a = bK$ , where  $V_a$  is an activation volume of molecular dimensions).

Phenomenological equations such as Wiederhorn's (eq. 1) can describe the dependence of crack velocity on stress and on environmental parameters for most typical glasses and are compatible with a thorough consistent modeling based on the sharp-crack atomic-bonding paradigm (Lawn 1993). Yet the detailed nature of the stress-corrosion mechanisms that occur at the crack tip have been debated for decades (Marsh 1964b; Maugis 1985; Gehrke *et al.* 1991; Tomozawa 1996), and a general disagreement can be found on the relevance of several accessory phenomena that may participate in the stress-corrosion mechanisms at different stages of the process. Stress-corrosion can involve a complex interplay between the diffusion of reactive molecules (mainly water) into the crack cavity and into the glass network, the corrosion (or dissolution) of the network itself, and the migration of weakly bonded alkali ions under chemical or stress gradient (Gehrke *et al.* 1991; Bunker 1994). We note that in pure silica glass the absence of ion migration can lead to significantly different local corrosion mechanisms. All three phenomena are typically very slow under ambient conditions in the unstressed material, but they can significantly accelerate in the highly stressed neighborhood of the crack tip, depending especially on the nature of the environment and of its confinement in the crack tip cavity.

A major objection to the sharp-crack atomic-bonding paradigm comes from the hypothesis of a significant contribution of plastic deformation at the crack tip in the slow crack propagation mechanisms. Since the early works of Dugdale (1960) on metals, and the observations of plastic behavior of glass under compression in indentation and scratch marks (Taylor 1949), several investigations have been carried out to track the evidence of plastic behavior in the strong tensile stress field at crack tips in glasses.

The fracture energies measured by Wiederhorn (1969) for six glasses in inert environment range between 7 and 10 J/m<sup>2</sup>, a figure which is tenfold higher than twice the typical values of the surface tension of glasses  $\gamma = 0.5 \text{ J/m}^2$  (Griffith 1920) which suggests a significant contribution of irreversible processes in crack propagation. By considering a typical yield stress of 10 GPa for glass, the size of the crack tip plastic region associated to such fracture energies by the Dugdale model would be limited to a few nanometers. In the subcritical stress-corrosion regime, the fracture energies and the estimated sizes of the plastic regions are lower. However, the extent of the penetration of reactive molecules from the environment into the glass network has been much debated (Marsh 1964, Tomozawa 1984) and this can enhance damage and plasticity on larger regions around the crack tip (cf. Ciccotti 2009).

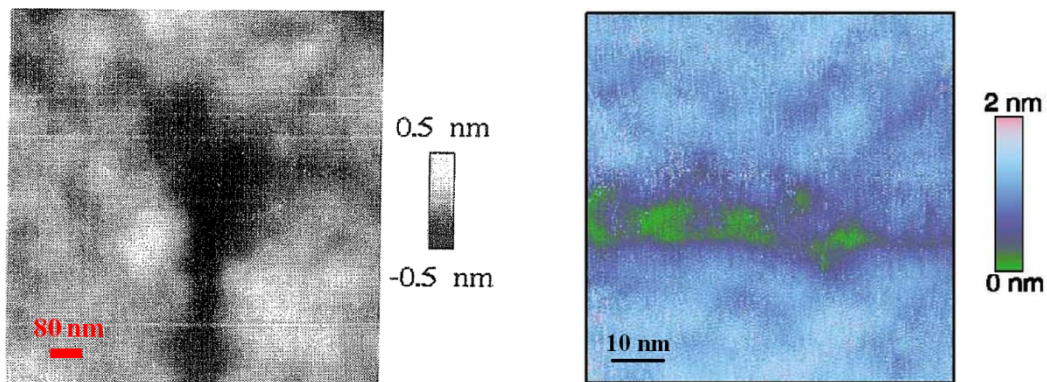


Figure 2 : in-situ AFM height observations of the neighborhood of a crack tip in glass. Left : observation from Guilloteau et al. (1996) of a local depression at the crack tip propagating from

*bottom to top. Right: observation from Célarié et al. (2003) of apparent nanoscale cavities ahead of a crack tip propagating from left to right.*

Since the early development of Atomic Force Microscopy (AFM) techniques it has been possible to probe *in-situ* crack propagation or the *post-mortem* crack surface morphologies to explore these mechanisms at their relevant nanometric scale leading to remarkable observations. In 1996 Guilloteau *et al.* made the first in-situ AFM measurements of the external glass surface during crack propagation following an indentation test in borosilicate glass. They observed the presence of a surface depression ahead of the crack tip. This was interpreted as a plastic deformation affecting a region of 50 nm size. The analysis leading to such a conclusion will be discussed below in details. Similar results were obtained by Célarié *et al.* (2003) on lithium-alumino-silicate glasses and by Prades *et al.* (2005) on silica glass, by in-situ AFM observation of slow fracture propagation in Double Cleavage Drilled Compression (DCDC) samples under pure mode I loading. The process zone size was observed to grow in size from 20 to 100 nm when the propagation velocity decreased from  $10^{-10}$  to  $10^{-12}$  m/s by lowering the SIF  $K$ . Moreover, these AFM measurements suggested that crack propagation in the process zone proceeds by the nucleation, growth and coalescence of nanometric cavities, in a similar way to what happens in the ductile fracture of metals at the (sub-)micrometer to millimeter scale. A complementary investigation by Bonamy *et al.* (2006) was based on the observation of a cutoff length close to 50 nm in the statistical correlation functions of the crack surface morphology measured post-mortem by AFM. This cutoff length was also attributed to the size of the process zone. On the other hand, Guin and Wiederhorn (2004) have observed that the *post-mortem* recombination of the AFM measurements of the morphology of opposing crack surfaces in silica and soda-lime showed no evidence for the expected traces of the nanocavities in



the bulk of the specimen. All these very resolved but seemingly contradictory AFM observations reopened the debate on crack tip plasticity.

The aim of this paper is to show that a coherent interpretation of these AFM nanoscale investigations, which are limited to the external surface of the sample in the close neighborhood of the crack tip, can be achieved by a thorough multiscale analysis of the mechanics of fracture from the macroscopic scale where the loading is applied to the sample, to the submicrometric scale where the crack tip singularity lives.

In most fracture mechanics test samples, the macroscopic aspects are tackled by establishing the expression of the stress intensity factor  $K$  as a function of the applied force  $F$ , the crack length  $a$  and the geometric parameters of the sample through a 2D finite element analysis. This approach conveniently describes the overall energetic balance during crack propagation as well as the in-plane elastic displacement fields of the sample at macroscopic scale. However, when considering the local fields close to the crack tip the actual shape of the crack front will play dominant role. Like in most test samples, the crack front shape of the DCDC sample (described in Fig. 3a) used in most of these AFM investigations is bowed into a parabolic shape as shown in figure 3. Since the AFM observations are intrinsically limited to the external surface of the sample, the fact that the crack front is not normal to the external surface breaks the 2D symmetry of the local stress and displacement fields. This prevents one from taking advantage of the classical plane stress or plane strain 2D solutions, especially for what concerns the out of plane displacement field, which is the main observable of AFM measurements.

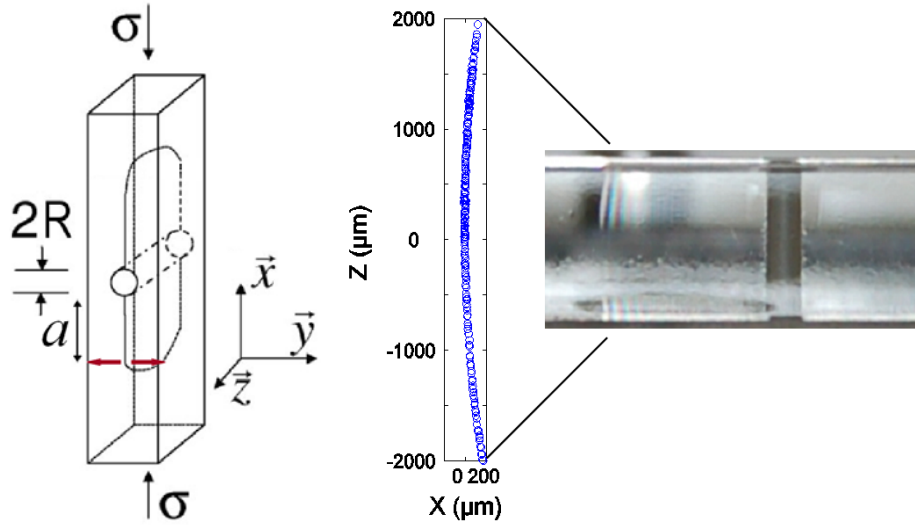


Figure 3. Left: Sketch of the DCDC geometry. Right: Side view of the DCDC sample, putting into evidence the parabolic shape of the crack front, which is measured in-situ during steady state crack propagation.

Fett *et al.* (2008) showed the inadequacy of the 2D plane-stress solution used by Guilloteau *et al.* (1996) and then by Célarié *et al.* (2003) to represent the elastic out of plane surface displacement near the crack tip with a  $1/r^{1/2}$  dependence (figure 4 left). They pointed out that the mechanical solutions to describe the corner singularity of a 3D surface striking crack were provided by Benthem (1977) and Bažant and Essentoro (1979), and imply the use of a  $r^\lambda$  dependence (with  $\lambda \sim 1/2$ ) to describe the local displacement field. Fett *et al.* (2008) showed that using an alternative fit of the data of Célarié *et al.* (2003) based on a 3D elastic numerical simulation, the deviation of the displacement profiles measured by AFM from the elastic numerical solution is much less obvious (figure 4 right). However, the quality of the fit on the vertical topography profiles is insufficient to drive accurate conclusions, due to the fact that the vertical extent of the out of plane displacement

field on AFM images is of the same order of magnitude as the residual roughness (a few angstroms) even after excellent polishing.

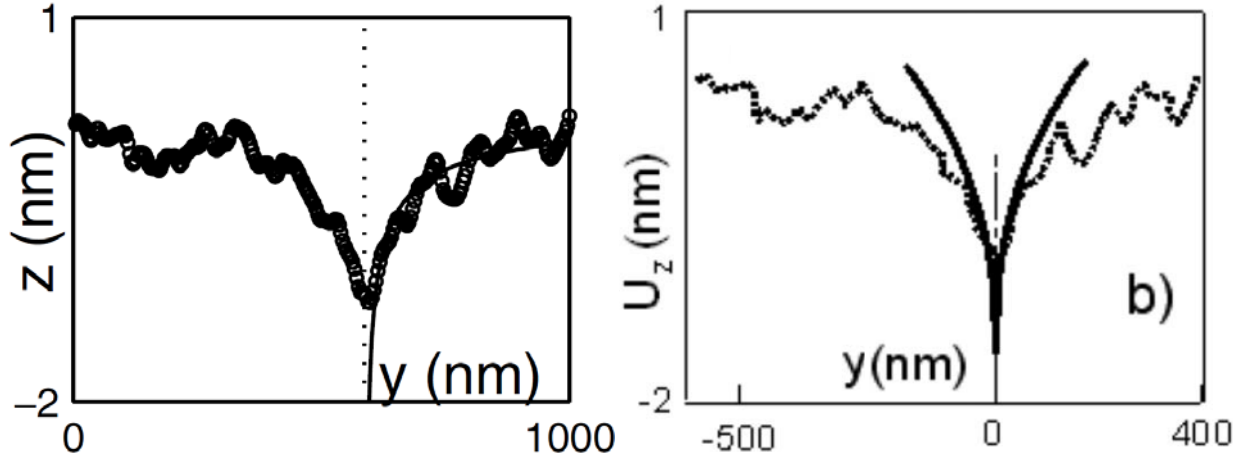


Figure 4. Left: AFM measurement of the out of plane displacement field in a section crossing the crack tip from Célarié *et al.* (2003), along with the  $1/r^{1/2}$  fit used therein. Right: a different fit of the same dataset as proposed by Fett *et al.* (2008) according to a 3D elastic numerical analysis.

In order to overcome this problem, we developed an extension of the Digital Image Correlation (DIC) Technique to AFM topographical images of in-situ crack propagation in order to separate properly the 3D surface displacement field from the nanoscale surface roughness (Han *et al.* 2010). We show here that only when insuring the steady state crack propagation we can interpret in a fully consistent way the nanoscale resolved displacement fields measured by AFM-DIC with the large scale surface displacement measured by optical profilometry (figure 5). The optical profilometry allows for appreciating the millimetric lateral extent of the crack tip surface depression, which is well separated from surface roughness and clearly attributable to an elastic effect at that scale. The different scales of these experimental observations are bridged by a 3D finite element modeling of

the whole DCDC sample involving the accurate crack front shape geometry. The overall multiscale strategy is presented in figure 5.

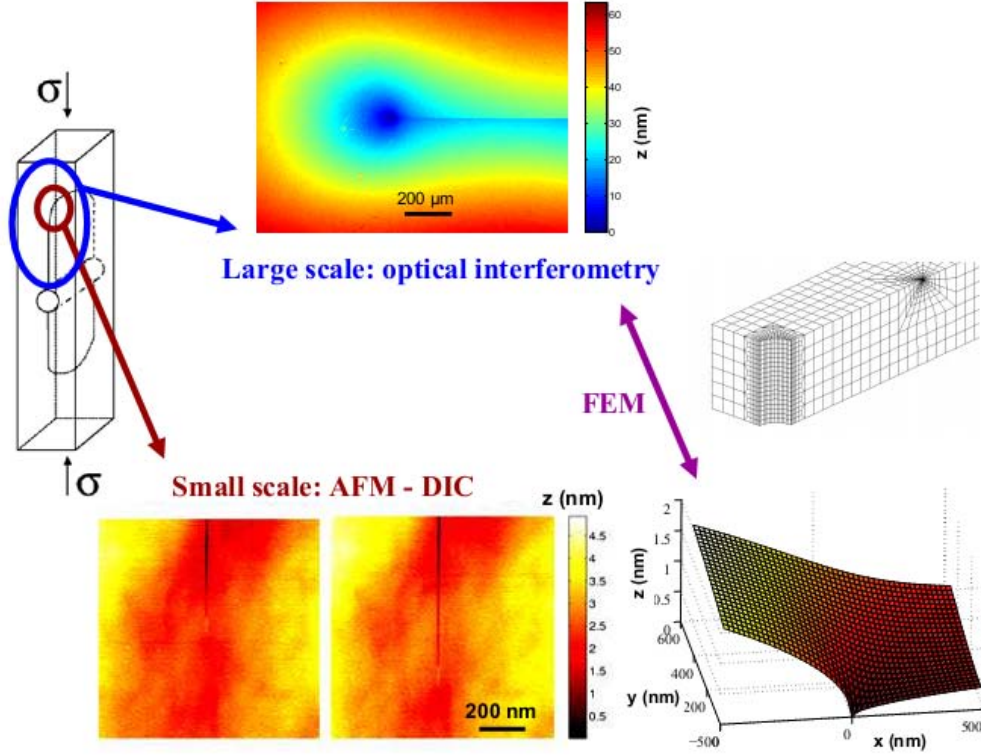


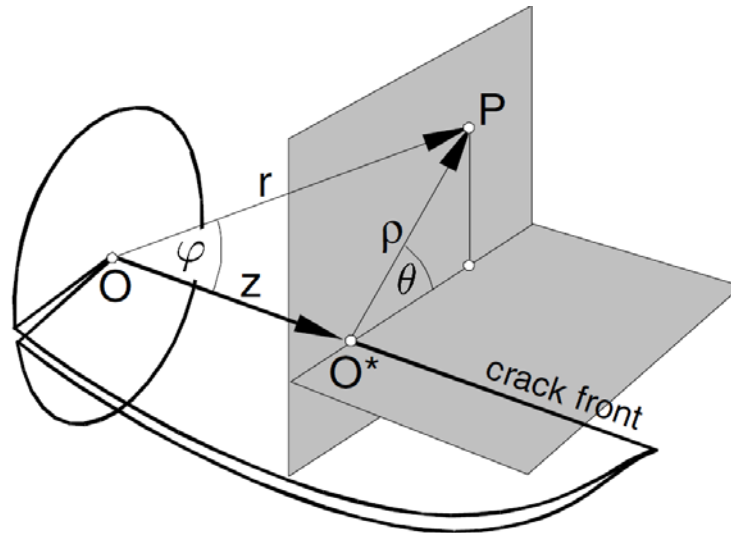
Figure 5. The DCDC test sample is represented on the left along with the regions corresponding to the two scales of observation. The large scale measurements by optical interferometry are illustrated on the top. The two small scale AFM images in the bottom represent two successive steps of steady state crack propagation that lead to the estimation of the local out of plane displacement field represented on their right. The finite element mesh on the right is used to bridge the two scales.

The results of this multiscale analysis provide strong evidence that accurate elastic solutions can describe faithfully the mechanics of the DCDC sample from the macroscopic scale where the load is applied down to the resolution limit of the AFM measurements, represented by the 10 nm size of

the probe. This is proved both from the consistency of the measured out of plane displacement throughout all the scales and from the identity (within 5% uncertainty) of the stress intensity factor independently obtained by either the macroscopic mechanical analysis of the structural response of the DCDC sample or by the submicroscale measurement of the crack tip asymptotic displacement fields.

## 2. Corner point singularity

We dedicate this second section to some theoretical notions on the corner point singularity, i.e. on the 3D nature of the asymptotic crack tip fields surrounding the region where a crack front intersects the external surface of the sample as in figure 6 (where a perpendicular intersection is chosen for simplifying the first description of the double coordinate system). Intensive theoretical and numerical studies, often disregarded, have been devoted to this problem by Benthem (1977), Bažant and Essentoro (1979), Dimitrov *et al.* (2006), and applied to the DCDC sample by Fett *et al.* (2008).



*Figure 6. Representation of a crack front perpendicularly intersecting the external surface of a sample, along with the two spherical and cylindrical coordinate sets used to describe the corner singularity (after Dimitrov et al. 2006).*

The local symmetry of the crack problem around this singular point is rather spherical than cylindrical (as it is the case for a current point along the crack front away from the edge where classical 2D approaches hold). The asymptotic displacement field  $\mathbf{u}$  should thus be expressed as:

$$\mathbf{u}(r, \theta, \varphi) = K_{CP} r^\lambda \hat{\mathbf{U}}(\theta, \varphi) + \mathbf{U}_{rem} \quad (2)$$

where  $K_{CP}$  denotes the corner stress intensity factor (CSIF),  $(r, \theta, \varphi)$  are the spherical coordinates around the corner point as in figure 6. The radial dependency (where  $r$  is the distance from the corner point) is a power law with a complex exponent  $\lambda$  called corner singularity,  $\hat{\mathbf{U}}(\theta, \varphi)$  represents a universal angular function (depending on the exponent  $\lambda$ , on the Poisson's ratio and in general on the angle of incidence of the crack front on the free surface) and  $\mathbf{U}_{rem}$  is a non singular reminder. We can express this solution in the more classical cylindrical coordinate system  $(\rho, \theta, z)$  aligned with the crack front (where  $\rho$  is the distance from the crack front, cf. figure 6):

$$\mathbf{u}(\rho, \theta, z) = K(z) \rho^{1/2} \hat{\mathbf{u}}(\theta) + \mathbf{u}_{rem} \quad (3)$$

where  $K(z)$  represent the evolution of the classical stress intensity factor along the crack front as a function of the distance  $z$  from the corner point at the sample surface:

$$K(z) \sim K_{CP} z^{\lambda-1/2} \quad (4)$$

The classical value  $\lambda = 1/2$ , typical of 2D solutions, marks a break even point with respect to the limit of  $K(z)$  for  $z \rightarrow 0$ , i.e. in the neighborhood of the corner point. According to Dimitrov *et al.* (2006), if the real part of the corner singularity  $\lambda$  is smaller than  $1/2$ , then the SIF  $K(z)$  will tend to infinity for  $z \rightarrow 0$ . This case is denoted as a “strong-singularity” and it gives rise to enhanced

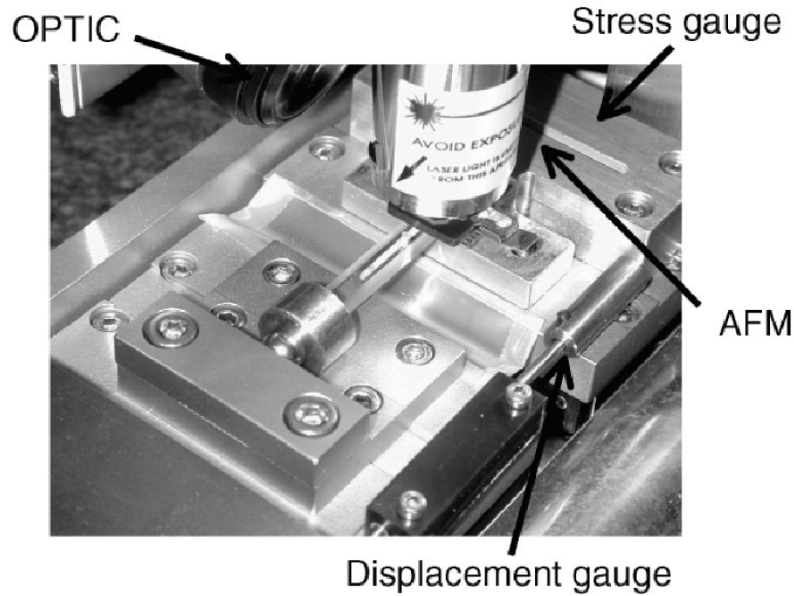
crack propagation near the surfaces even for a very small load. On the other hand, if the real part of the corner singularity  $\lambda$  is larger than  $1/2$ , then the SIF  $K(z)$  will tend to zero for  $z \rightarrow 0$ . This case is denoted as a “weak-singularity” and it gives rise to a vanishing propagation velocity of the crack corner point even when the crack propagates (away from the specimen surface). For the sake of simplicity we will refer here to  $\lambda$  as the real part only, which determines the main radial scaling of the asymptotic solutions, and we limit our description to a crack plane that is perpendicular to the external surface of the sample and to macroscopic mode I loading. Benthem (1977) and Bažant and Essentoro (1979) have shown that for a crack front merging perpendicularly to the free surface, the singularity is weak, resulting in a vanishing SIF at the corner point. In the general case, if the crack front strikes the external surface with an angle  $\alpha$  (measured from the normal to the external surface, like in figure 3), the corner singularity  $\lambda$  can be expressed as a universal decreasing function of the angle  $\alpha$  and an increasing function of the Poisson’s ratio  $\nu$  of the material.

Bažant and Essentoro (1979) and subsequently Dimitrov et al. (2006) have proposed an important interpretation of the consequences of this corner point singularity on the evolution of the crack front shape during the ensuing crack propagation. Notably, in the case of a strong singularity ( $\lambda < 1/2$ ) the crack will advance faster at the surface than in the bulk, thus inducing a reduction of the crack front angle  $\alpha$ , and hence an increase of  $\lambda$ . On the other hand, in the case of a weak singularity ( $\lambda > 1/2$ ) the crack corner point will be arrested and the crack will advance faster in the bulk, thus inducing an increase of the crack front angle  $\alpha$ , and hence a decrease of  $\lambda$ . It is thus a reasonable conjecture that the crack will reach a steady state crack propagation only after the corner point singularity has converged to the classical exponent  $\lambda = 1/2$ , when the stress intensity factor  $K(z)$  becomes a constant along the crack front. The crack front angle will thus reach a fixed angle  $\alpha$  that only depends on the Poisson’s ratio. For these reasons the steady state propagation is a very

convenient situation to perform a multiscale analysis. We remark that despite the expected corner singularity for steady state propagation has the same exponent  $\lambda = 1/2$  as for the in plane displacement field in the classical 2D crack tip singularity, the out-of-plane displacement at a corner point should also present a  $r^{1/2}$  singularity, which is not predicted by 2D solutions neither in plane stress or plane strain. In order to test this conjecture we perform our investigations on two glasses with a different Poisson's ratio.

### 3. In-situ investigations of crack propagation

In the present experiments, fractures were initiated and propagated on a DCDC sample using a precision loading apparatus (based on a Microtest load cell produced by Deben, Woolpit, UK) (cf. figure 1). The DCDC test set-up is particularly convenient for these studies due to its excellent stability and compactness (Jannsen 1974).



*Figure 7. Experimental setup for in-situ AFM imaging of the slow crack propagation in a DCDC specimen.*



The parallelepipedic DCDC samples of dimensions  $2w \times 2t \times 2L$  ( $4 \times 4 \times 40 \text{ mm}^3 \pm 10 \text{ }\mu\text{m}$ ) were polished to a RMS roughness of 0.5 nm (for an area of  $1 \text{ mm}^2$ ) and a hole of radius  $R = (500 \pm 10) \text{ }\mu\text{m}$  was drilled at their center to trigger the initiation of the two symmetric fractures of length  $a$ .

Two kinds of oxide glasses were tested: pure fused silica glass (Suprasil 311, Heraeus, Germany, Young modulus  $E = (72 \pm 2) \text{ GPa}$ , Poisson's ratio  $\nu = (0.17 \pm 0.01)$ ) and lithium-aluminium-silicate glass (produced by Saint-Gobain and called LAS in the following, with  $E = (83 \pm 2) \text{ GPa}$  and  $\nu = (0.22 \pm 0.01)$ ), which is the same glass used by Célarié *et al.* (2003).

All measurements are done after an extensive stabilization consisting of several hours of steady state propagation, so that crack propagation conditions can be considered as stable. We also insure stable environmental conditions of temperature ( $\pm 1^\circ\text{C}$ ) and relative humidity ( $\pm 1\%$ ). The propagation velocity is accurately measured in the range between  $10^{-5}$  and  $10^{-12} \text{ nm/s}$ . The details of the setup and techniques can be found in Célarié (2004) and Grimaldi et al (2008). The macroscopic value of the stress intensity factor  $K$  was computed according to one of the most recent 2D finite element analyses by Pallares et al. (2009):

$$\frac{\sigma\sqrt{\pi R}}{K} = \left[ c_0 + c_1 \frac{w}{R} + c_2 \left( \frac{w}{R} \right)^2 \right] + \left[ c_3 + c_4 \frac{w}{R} + c_5 \left( \frac{w}{R} \right)^2 \right] \frac{a}{R} \quad (5)$$

where  $\sigma$  is the external load,  $a$  is the crack length, and the set of parameters is:  $c_0=0.3156$ ,  $c_1=0.7350$ ,  $c_2=0.0346$ ,  $c_3=-0.4093$ ,  $c_4=0.3794$ , and  $c_5=-0.0257$  for  $2.5 \leq w/R \leq 5$  and the range of applicability is  $w < a < L - 2w$ .

## 4. 3D macroscopic analyses of the DCDC specimen

### 4.1 Crack front shape

The crack front shape is measured in-situ by means of a CCD camera at different stages of crack propagation. Several high resolution images are stitched to obtain the whole crack front spanning the 4 mm thickness of the sample (cf. figure 8). The crack front can be fitted very accurately by a parabolic shape, providing the value of the terminal angle,  $\alpha$ . This angle is found to be independent on the conditions of loading and environment, and it assumes two clearly different values for the two glasses. The average value for silica glass is  $\alpha = (8.5 \pm 1)^\circ$ , while for the LAS glass it is  $\alpha = (15 \pm 1)^\circ$ . The dominant increasing dependency of  $\alpha$  on the Poisson's ratio is qualitatively consistent with the predictions of Bažant and Essentoro (1979), although the theoretical values are somehow lower (respectively  $\alpha = 5.1^\circ$  for silica glass and  $7.3^\circ$  for LAS glass, for  $\lambda = 1/2$ ).

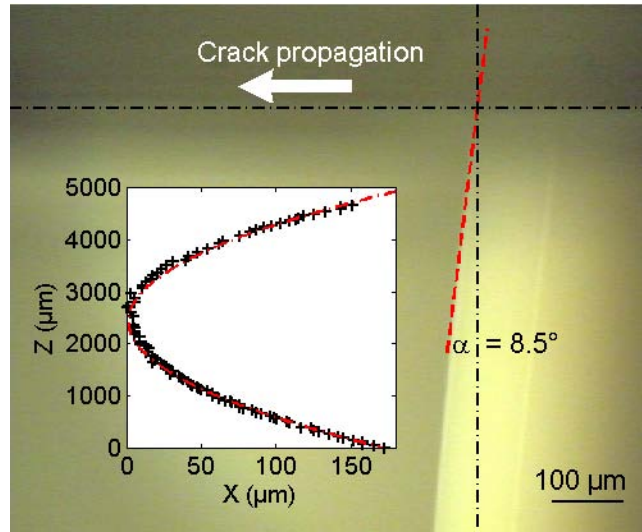


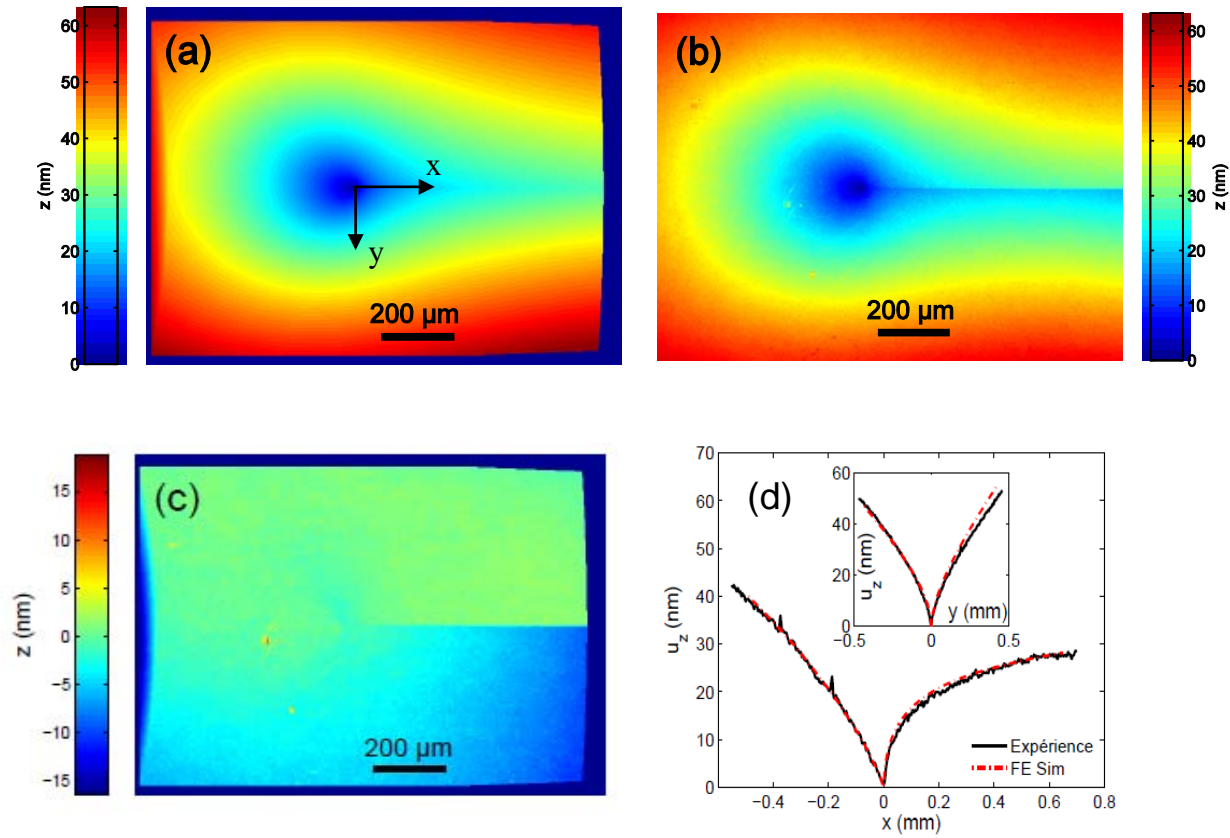
Figure 8. Experimental in-situ image of the crack front at the free surface ( $z=0$ ) in a DCDC fused-silica glass sample. Inset: parabolic fit over the whole crack front.

## 4.2 Out-of-plane displacement

The measurements of the out-of-plane displacement on the DCDC samples was performed by an optical profilometer (Wyko NT9100, Bruker, California), placed in a metrological room with temperature  $T = (20.0 \pm 0.1)^\circ\text{C}$  and relative humidity  $RH = (50 \pm 1)\%$ . By using Phase-Shifting

Interferometry the instrument can reach subnanometric vertical resolution, the lateral resolution being limited by the  $\times 5$  lens quality ( $\pm 500$  nm on  $1.27 \times 0.95$  mm<sup>2</sup> images).

A typical image on silica glass is shown in figure 9(b). The measured out-of-plane displacement field  $u_z$  describes a funnel centered at the crack tip, which vertically spans 50 nm over the mm scale of the image, and is thus not affected by the nanometric surface roughness. Considering the large lateral scale of observation, this displacement field can be clearly attributed to an elastic effect related to the transverse Poisson contraction caused by the in plane tensile stress fields around the crack tip.



*Figure 9. Comparison between (a) finite element simulation and (b) optical profilometry measurements of the out-of-plane displacement field of a crack in silica glass. The weak residual is shown in (c). Two orthogonal cross-sections intersecting at the crack tip are shown in (d).*

These results were compared to the out-of-plane displacement field predicted by the 3D finite element simulation (described in detail in section 6), which accounts for the experimentally measured shape of the crack front. An excellent agreement was reached on the whole range of scales spanned by the optical images as illustrated in figure 9 for silica glass. The residual error is less than 10% of the image vertical dynamics and can be attributed to a weak additional mode III loading present in the experiment but not included in the simulation.

## **5. Nanoscale analysis of the asymptotic fields**

AFM observations are done in tapping mode on a D3100 from Veeco Metrology Inc., Santa Barbara, California. After an extensive stabilization consisting of several hours of steady state crack propagation and imaging, each AFM image series is acquired within a few hours, so that crack propagation conditions can be considered as stable and AFM drifts are minimized. This provides optimal conditions of the application of Digital Image Correlation techniques. A detailed description of techniques can be found in Han *et al.* (2010), but we recall here the most relevant information for interpreting the results.

The aim of the technique is to extract the displacement field between two AFM topographic images, the reference image  $f(\vec{x})$  and the deformed image  $g(\vec{x})$ , taken on the same surface at two different times, the crack length increasing during the time interval (cf. figures 10(a) and 10(b)). The generalization of the so-called “opticalflow conservation” which relates the two images can be written as:

$$f(\vec{x}) = g(\vec{x} + \vec{u}(\vec{x})) + v(\vec{x}) \quad (6)$$

where  $\vec{u}(\vec{x})$  (respectively,  $v(\vec{x})$ ) denotes the in-plane (respectively, out-of-plane) displacement field. In other words, the roughness of the two surfaces is used to obtain the in-plane displacement field and then the subtraction of the registered images allows obtaining the out-of-plane displacement field by eliminating the contribution of roughness. In order to develop a robust method, we resort to an “Integrated” DIC approach as introduced by Roux and Hild (2006). The displacement field  $(\vec{u}(\vec{x}), v(\vec{x}))$  is sought as a combination of a few expected fields  $\Phi_n(\vec{x})$ :

$$(\vec{u}(\vec{x}), v(\vec{x})) = \sum_{i=1}^{10} a_i \Phi_i(\vec{x}) \quad (7)$$

Six of the base fields represent regular transformations such as uniform extension or shear, which allows for the correction of AFM drifts. Additionally, four others represent the linear elastic fracture mechanics in-plane and out-of-plane singular fields on each image. The steady-state crack propagation condition can be used to enforce the identity of the crack tip fields on the two images after a translation along the crack path direction, thus reducing the number of unknowns.

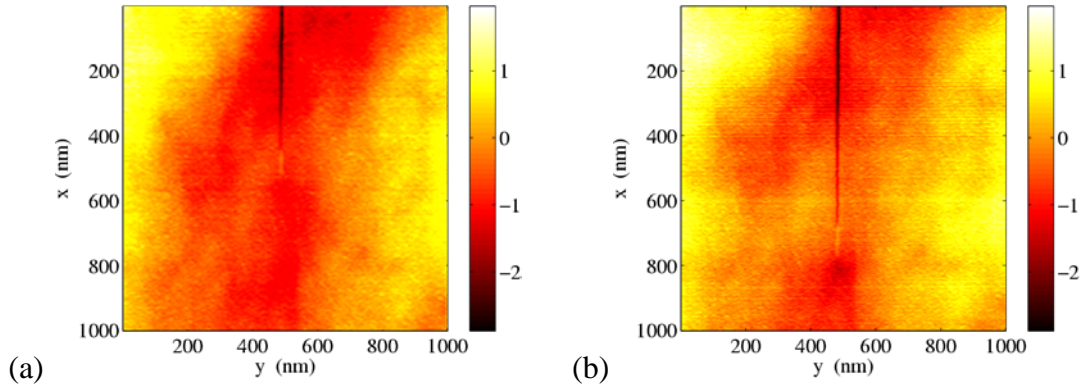
The in-plane component of the crack tip field can be well approximated by the 2D plane stress condition. On the other hand, the out-of-plane component  $\psi(\vec{x})$  of the singular displacement field is not known analytically. According to the conjecture of Dimitrov *et al.* (2006) discussed in section 2 the crack front geometry adjusts itself during steady-state propagation so that the singularity exponent  $\lambda$  becomes 1/2, as for the 2D in-plane components, yet the angular dependence remains unknown. We thus used the trial solution  $\psi_0(\vec{x}) = \sqrt{|\vec{x}|}$  to register both images, and then we adjusted the residual field by a simple algebraic expression proposed as a systematic Fourier expansion (truncated at very low order) respecting the mode I crack symmetries:

$$\psi(\vec{x}) = \rho_{DIC} \sqrt{|\vec{x}|} \cdot F_{DIC}(\theta) \quad (8)$$

$$\rho_{DIC} = K_I(1+\nu)/\sqrt{2\pi E} \quad (9)$$

$$F_{DIC}(\theta) = a_{DIC} + b_{DIC} \cos(\theta/2) + c_{DIC} \cos(\theta) \quad (10)$$

The analysis on a first image pairs on silica glass provided the coefficients:  $a_{DIC} = 0.28$ ,  $b_{DIC} = 0.67$  and  $c_{DIC} = -0.72$ . These values were found to be compatible with all ensuing analyses on silica glass, in agreement with what expected by the conjecture of Dimitrov *et al.* (2006), which let them depend only on the Poisson's ratio. We thus fixed their values in the IDIC code for silica glass, reducing the analysis to the determination of one single unknown physical parameter corresponding to the mode I stress intensity factor  $K$ . An example of application of the final technique to a silica glass sample can be found in figure 10. For this first investigation, the crack propagation velocity is  $v = (0.7 \pm 0.1)$  nm/s, the applied force  $F = (1844 \pm 4)$  N and the average crack length  $a = (6145 \pm 10)$   $\mu\text{m}$ . The stress intensity factor can be estimated to  $K_I^{vol} = (0.39 \pm 0.02)$   $\text{MPa} \cdot \text{m}^{1/2}$  according to eq. (5).



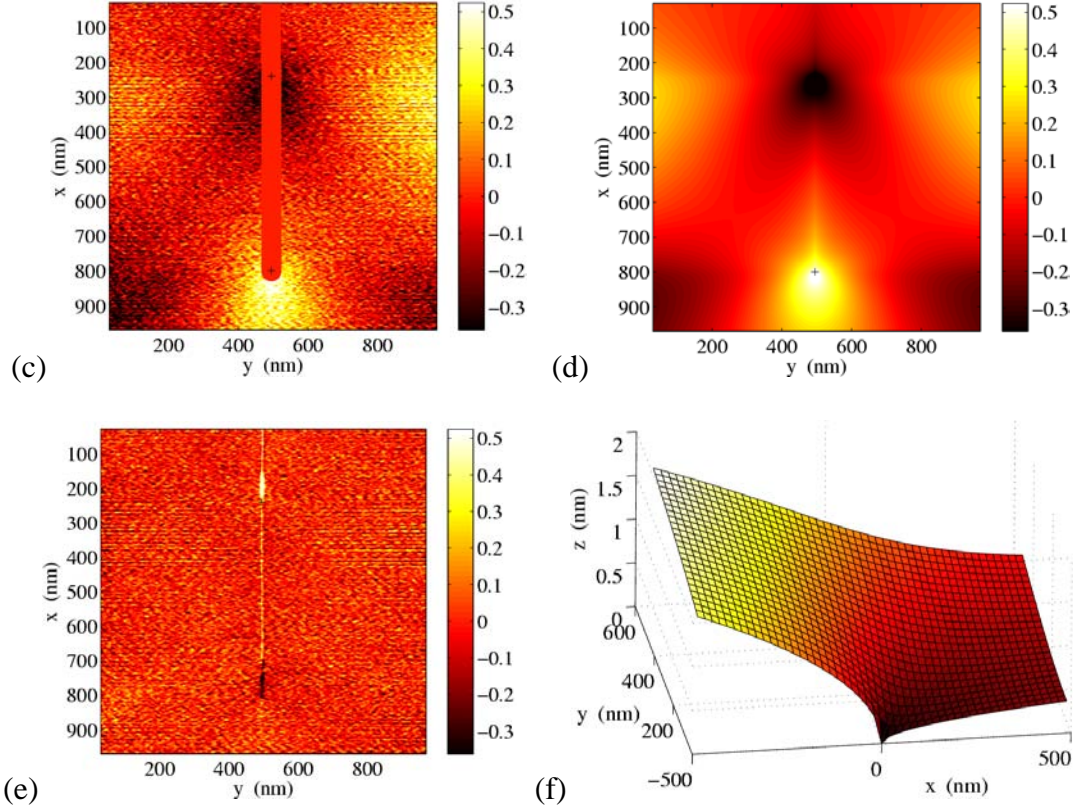


Figure 10. (a) and (b) are respectively the reference and deformed AFM height images for the IDIC analysis. (c): Raw residual field obtained after correction of in-plane displacement. Note that the crack path is masked for the IDIC analysis. (d): Fitted displacement field,  $\psi(\vec{x} - \vec{x}_0) - \psi(\vec{x} - \vec{x}_1)$ . (e): Remaining residual after fit subtraction. (f): Out-of-plane displacement  $\psi(\vec{x})$  associated with the crack opening. A cut through the symmetry plane  $y=0$  is shown, with the crack tip located at the origin (after Han et al., 2010).

A series of 5 images of the same  $1 \times 1 \mu\text{m}^2$  zone swept by a crack is first analyzed. As an example, we report in figure 10 the steps of the IDIC analysis of the first two AFM height images of the series. The reference and deformed height images are represented in figure 10(a) and (b). The residual map without out-of-plane displacement is shown in figure 10(c) and the corresponding elastic solution is represented in figure 10(d). Figure 10(e) shows that no obvious long-range trend

is left in the final residual. The out-of-plane displacement due to the opening of a crack at the origin is shown in figure 10(f). The quality of the IDIC measurement is evaluated by measuring the normalized residual, i.e. the standard deviation of the remaining residual, normalized by the peak-to-valley roughness of the original topographic image. In the present cases, even though the kinematic field was adjusted with very few parameters, the normalized residual  $n$  is very stable at 1.6%, a remarkably low value which gives confidence in the convergence of the procedure. The measured stress intensity factor values (using the elastic moduli for silica glass: Young modulus of 72GPa and a Poisson's ratio of 0.17) is  $K^{DIC} = (0.39 \pm 0.04) \text{ MPa.m}^{1/2}$ , which is in excellent agreement with the macroscopic value of  $(0.39 \pm 0.02) \text{ MPa.m}^{1/2}$  estimated independently. Note the huge difference of length scale used in both estimates (millimeter vs nanometers). A second image series was tested in Han *et al.* (2010) after zooming to  $200 \times 200 \text{ nm}^2$  images around the crack tip. Although the residuals of 5% are slightly higher, they still do not show any trend out of a 10 nm distance from the crack tip, which represents the lateral resolution limit of the AFM related to the tip size. Moreover the locally estimated value of  $K^{DIC}$  of  $(0.41 \pm 0.05) \text{ MPa.m}^{1/2}$  is still in excellent agreement with the macroscopic measurement.

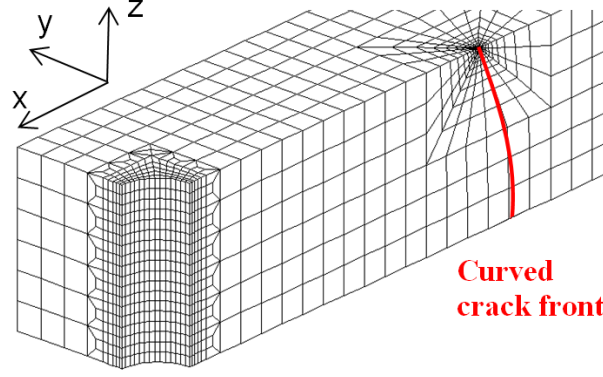
## 6. 3D elastic finite element simulation

The 3D finite element simulation used to represent the linear elastic stress and displacement fields of a realistic DCDC specimen with curved crack fronts is implemented by the finite element code CAST3M<sup>1</sup>. The mesh is constituted of linear elastic isotropic eight nodes elements. The details of the sample loading configuration and the mesh geometry are shown in figure 11.

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<sup>1</sup> CAST3M software is developed by CEA-Saclay, France. Reference web page: <http://www-cast3m.cea.fr/cast3m/index.jsp>





*Figure 11. 3D mesh for the finite element simulation of the DCDC sample. Due to symmetry, only  $1/8^{\text{th}}$  of the specimen is meshed. The crack front is curved to a parabolic front with terminal angle  $\alpha$  and the mesh is densified at the corner point singularity.*

The material's linear elastic response is defined by the Young's modulus  $E$  and the Poisson's ratio  $\nu$  of silica glass as defined in section 3. Thanks to the symmetry of the geometry, we can limit the simulation to one eighth of the specimen by imposing the boundary conditions  $u_x = 0$  along the symmetry plan normal to  $\vec{e}_x$  and  $u_y = 0$  along the symmetry plan normal to  $\vec{e}_y$  on the uncracked ligament. The compressive stress  $\sigma$  is applied on the two opposite faces, without imposing any displacement constraints. We thus neglect the effects of friction at the platen/sample surfaces, but they will be negligible if the crack front remains at a sufficiently large distance  $w$  away from the end of the sample. The crack has a length  $a$  measured from the edge of the hole to the corner point of the crack front. The crack front is curved with a parabolic shape terminating with an adjustable angle  $\alpha$ . The gap between the millimeter length scale of the external mechanical loading and the nanometer length scale of the asymptotic crack tip fields close to the corner point singularity requires an adapted mesh with an exponential densification of elements down to 0.01 nm close to the corner point singularity. The mesh is also refined close to the central hole.

To investigate the influence of the geometrical parameters on the corner singularity  $\lambda$ , a series of meshes was designed with twenty five values for the terminal angle  $\alpha$  ranging from  $6^\circ$  to  $17.5^\circ$ . The rest of the geometry is kept constant, the external size and hole are as in our test samples, the crack length and loading were the same as for the tests with optical profilometer, in order to reproduce at best the macroscopic behavior of the out-of-plane displacement field. On the other hand, the local asymptotic behavior at the corner point should be independent of the crack length.

We already presented in section 4 (figure 9) the good performance of the 3D simulation against the out-of-plane measurement of the optical profilometer on a 1 mm large image. We will focus here on the description of the corner point singularity in order for the 3D FE simulation to bridge the two scales of experimental observation.

In order to extract the corner point singularity  $\lambda$ , three different indicators are investigated: these consist of the power law fit of the two main components  $u_x$  and  $u_y$  of the mode I displacement field and of the 2D stress intensity factor profile  $K(z)$  when approaching the corner point. For both components of the displacement fields, the fit is done at the free surface along the crack lips ( $x > 0$ ,  $y = 0$ ) in the distance range  $1 \text{ nm} < x < 1 \text{ }\mu\text{m}$  from the tip, which according to Pallares *et al.* (2009) is well included in the region of  $K$ -dominance (i.e. dominance of the Irwin square root singularity in a 2D analysis) of the DCDC. The stress intensity factor  $K(z)$  is evaluated along the crack front using the  $J$  integral estimators included in the code and then fitting a power law exponent according to equation (4). The obtained values of the corner singularity exponent  $\lambda$  are shown in figure 12(left) as a function of the terminal angle  $\alpha$ . We observe an overall good agreement between the estimates obtained using  $u_x$ ,  $u_y$  and  $K(z)$ . By applying the conjecture of a corner singularity exponent  $\lambda = 1/2$  expected for a steady state crack propagation, the first three indicators would predict a terminal angle  $\alpha = 7 \pm 1^\circ$ , which is intermediate between the theoretical prediction of  $5.1^\circ$  according to

Bažant and Essentoro (1979) and our measured value of  $8.5 \pm 1^\circ$  (cf. section 4.1). The agreement is quite satisfactory. Some more precise results may be achieved by refining the mesh along the crack front within the material bulk, but the reach of such a precision is out of the scope of the present investigation aimed at understanding the appropriate bridging over length scales.

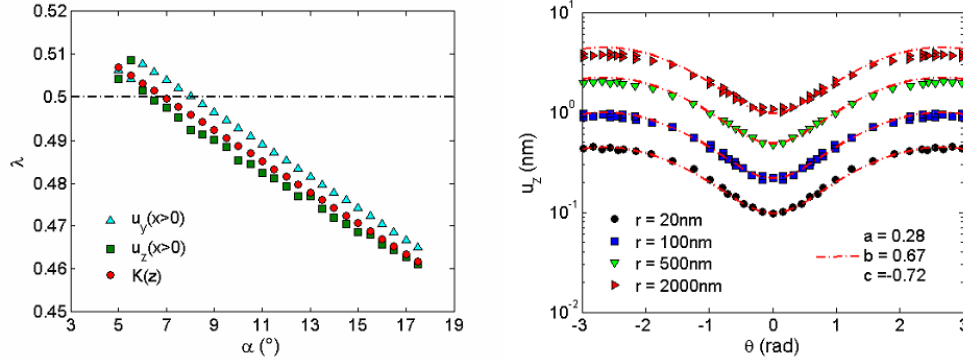


Figure 12. Finite element calculations: Left: Representation of the corner singularity exponent  $\lambda$  as a function of the terminal angle  $\alpha$  obtained for the Poisson's ratio  $\nu = 0.17$  of silica glass – Right: Representation of the out-of-plane displacement  $u_z(r, \theta)$  obtained by simulation ( $\lambda = 1/2$ ) as a function of  $\theta$  for different  $r$ . The red dashed lines correspond to the fit according to equation (10).

We can also use the FE simulation to test the angular functions determined by DIC for the corner point singularity. We represent in figure 12(right) the out-of-plane displacement  $u_z(r, \theta)$  obtained by the simulation as a function of the angle  $\theta$  for different distances  $r$  from the crack tip in the domain  $20 < r < 2000$  nm. The expressions (8,9,10) used to adjust the DIC results were also plotted in the same figure by using the same set of coefficients ( $a_{DIC} = 0.28$ ,  $b_{DIC} = 0.67$  and  $c_{DIC} = -0.72$ ). The residuals become larger than 10% only when  $r > 2000$  nm. This remarkable agreement is a further validation of the sound multi-scale reconstruction of the 3D mechanics of the DCDC specimen from the macroscopic scale down to the asymptotic corner singularity field that dominates the in-situ AFM images.

## 7. Discussion and conclusion

The present multi-scale investigation offers a consistent mechanical view of the steady state subcritical fracture propagation in a DCDC specimen. The 3D analysis of the crack tip field is shown to be an unavoidable step to link the macroscopic features of the loading and the nanoscale asymptotic crack tip field as measured at the accessible free surface of the sample. The macroscopic loading is transferred to the crack front singular fields through the structural response of the DCDC sample which is essentially captured by a 2D analysis at large to intermediate scales. When approaching the crack front at distances comparable to the sample thickness  $w$ , the details of its non straight geometry become dominant, yet locally we can still approximate the neighborhood of the crack front by a 2D fracture field. However, when approaching the incidence of the crack front onto the free surface, the 2D symmetry is essentially broken and a different self-similar corner point singularity emerges with an intrinsic 3D structure. This allows a range of possible local corner singularities, yet it was argued that only the exponent  $\lambda = 1/2$  is compatible with a steady state propagation of the crack front, inducing a prediction of the terminal angle  $\alpha$  as only related to the Poisson's ratio, together with a prescription of  $r^{1/2}$  fields also for the out-of-plane components of displacement (a result that is strongly different from the 2D predictions in either plane stress or plane strain conditions). Our multiscale experimental and numerical analysis provides a consistent validation of this global picture, and the ultimate proof is that the local stress intensity factor obtained through the DIC analysis of submicrometric sized AFM images close to the crack tip corner point provides a robust and consistent estimation of the macroscopically measured stress intensity factor under different propagation conditions. The key of this success is the quality of the steady state crack propagation. By enforcing several hours of equilibrated slow crack growth in a very stable sample such as DCDC, the crack front progressively finds a shape that remains invariant

throughout the entire propagation, equilibrated through all scales and under a very pure mode I loading (thanks to the principle of local symmetry). This allows both to relate the macroscopic and microscopic loading very accurately, and to insure that the crack tip displacement field in a series of subsequent AFM images is substantially identical. This mechanical information is the key to separate this nanometric out-of-plane displacement field from the nanometric surface roughness which has the same order of magnitude, and which generally prevents quantitative evaluation of small displacement fields on AFM images. We underline that although AFM nanoscale measurements have generally a poor metrological content due to the interplay of drifts, tip/sample interactions and imaging feedback details, the use of DIC to extract displacement fields from very similar images can provide very accurate and metrological results, especially when the singular nature of the crack tip fields under study allows a clear separation from the more regular AFM drifts. A second key of this success is the incredible mechanical properties of silicate glasses, which were proved to allow the use of continuum mechanics and linear elasticity down to 10 nm scales from the crack tip, which is by itself an amazing result. Full 3D elastic solutions were used here as a first reasonable guess to establish a connection from the macroscopic scale down to the nanometric neighborhood of the corner point singularity. However, the extremely low values of the residual fields measured by DIC, and especially the absence of any observable trend in the residual fields out of a 10 nm region from the crack tip become a striking evidence of the appropriateness of these elastic solutions to describe the crack tip fields down to the extreme lateral resolution of AFM imaging. This set of measurements constitutes a clear and sound solution to the long debate on the length scales of the inelastic processes acting at the crack tip of glasses during stress-corrosion slow crack propagation (Wiederhorn *et al.* 2013).

What about the reported AFM observations suggesting crack tip plasticity at 100 nm scales? As above discussed the crack tip topography as studied by Guilloteau *et al.* (1996) and Célarié *et al.*

(2003) call for proper 3D corner point solutions to be quantitatively interpreted, and these early experimental results should be revisited within such a framework. Lopez-Cepero *et al.* (2008) showed that the apparent nanoscale cavities observed by Celarié *et al.* (2003) (cf. figure 2 left) could originate from the superposition of the out-of-plane crack tip elastic depression and of the surface roughness which has the same order of magnitude. In a previous investigation (Lechenault *et al.* 2010) we also showed that the 20-100 nm cutoff length observed in the correlation functions of the nanoscale roughness of the fracture surfaces can be generated by a subtle non-linear filtering induced by the geometrical interaction of the nanoscale sized AFM tip (subject to wear) and the self-affine nanoscale roughness. These subtle artifacts should be used as an important lesson concerning the danger of misinterpreting very resolved nanoscale investigations. The multi-scale mechanical consistency of the reported study is a precious safeguard against this risk.

Is this the end of the story concerning the active debate on plasticity and damage around the crack tip in glasses? We believe that the question is settled concerning the 100 nm scale, but our present analysis cannot resolve features below the 10 nm scale which is the limit of lateral resolution of AFM in-situ investigations (and even in post-mortem fractographic investigations when looking for a cutoff in the lateral lengths). And indeed when considering the separation of two atoms, non-linearities of interactions are evidently involved, resulting at least in non-linear elasticity, and most probably in plasticity with irreversible reorganization of the amorphous atomic arrangement. Moreover, when examining more closely the literature on the evidences of water penetration at the crack tip, we find several experimental evidences of water penetration in regions of a few nanometers (yet no more than 10 nm). These are generally post-mortem investigations of the water concentration depth profile on crack surfaces in silicate glasses performed by resonant nuclear reaction (Lanford *et al.* 1979), optical reflectivity (Stavrinidis and Holloway, 1983) and more recently by small angle neutron reflectivity (Lechenault *et al.* 2010). These evidences are very

strong, but as in all post-mortem investigations, they do not provide details on the moment where water really penetrated and on the mechanisms of coupling with the stress-corrosion crack propagation. A more recent AFM post-mortem investigation by Wiederhorn *et al.* (2011) has shown that a possible mechanical coupling between water penetration in the crack tip region and crack propagation in silica glass could come from the induced local swelling of the glass and the consequent build up of local compressive stresses, which can have an effect of shielding crack tip stresses. This mechanism is analogous to the well studied coupling between ion exchange leaching in alkali-silicate glasses and the crack tip stresses (Fett *et al.* 2005), which results in the presence of the stress-corrosion threshold of propagation described in figure 1 (right). It is noteworthy that, even in the more highly corrosive context of leachable glasses, the volume affected by leaching and compressive stresses is limited to a region of size well below 10 nm from the crack tip (Wiederhorn *et al.* 2013, Célarié *et al.* 2007).

In order to discuss the final implications of the present analysis on the understanding of the stress-corrosion mechanisms we recall some recently performed complementary observations thanks to our in-situ AFM investigation technique. By using a complementary AFM imaging technique, called phase imaging, we showed that the crack tip cavity is so sharp that it is filled with a spontaneous water condensation from the ambient moist atmosphere in a submicrometric neighborhood of the crack tip (Grimaldi *et al.* 2008). While this condensate was shown to be close to pure water at condensation equilibrium in pure silica glass (Pallares *et al.*, 2011), complementary observations on alkali-silicate-glasses (Célarié *et al.* 2007) have shown that the chemical composition of this condensate keeps evolving in time due to the leaching of sodium out from the glass. These observations are of the greatest importance to the understanding of the stress-corrosion kinetics under ordinary moist atmosphere since this condensate constitutes the effective local environmental condition at the crack tip region where the stress-corrosion occurs.

We can conclude our discussion by stating that the combination of the investigations of crack tip stresses along with the understanding of the local environmental condition is likely to offer an undisputable key to a thorough understanding of the role of glass composition on the measured phenomenological parameters of the stress-corrosion curves (Wiederhorn *et al.* 2013). Another major perspective comes from the recent outstanding developments in the performances of molecular dynamics towards the simulation of stress-corrosion reactions on space and time scales that could soon approach from below the limits of the measurable range accessible by our in-situ AFM experimental investigations (Mischler *et al.* 2005; Du and Cormack 2005, Kermode *et al.* 2008) thereby opening a formidable opportunity for a novel experimental/modeling dialog.

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