

Directional results and absolute archaeointensity determination by the classical Thellier and the multi-specimen DSC protocols for two kilns excavated at Osterietta, Italy

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 was not successful. The obtained full geomagnetic field vector (declination, inclination and intensity) has been used for the archaeomagnetic dating of the two structures suggesting that the OSA kiln was for last time used between 1761-1841 AD and the OSB kiln between 1752-1831 AD, at 95 % of probability. This study shows that intensity determinations do not restrict the dating results when referring to the last few centuries, as this period is characterized by very small intensity variations.

 Keywords: Secular variation; geomagnetic field vector; archaeomagnetic dating; Italy

1. Introduction

 Baked clay archaeological materials often contain small quantities of ferromagnetic minerals that under certain conditions can register the direction and intensity of the Earth's magnetic field in the past. When heated at high temperatures, baked clay archaeological materials, such as kilns, hearths, bricks and pottery lose their magnetization and while cooling, they acquire a thermoremanent magnetization (TRM) that has the characteristics (direction and intensity) of the ambient magnetic field that is usually the Earth's magnetic field. Unless the material gets subsequently reheated or chemically altered, the TRM acquired remains stored in the archaeological artefacts and can be nowadays experimentally recovered offering important information about the past variations of the Earth's magnetic field.

 In the case that the age of the studied archaeological artefacts is well known based on the stratigraphy, archaeological findings and/or independent absolute dating methods such as radiocarbon, thermoluminescence, or dendrochronology, the obtained archaeomagnetic data can be used as reference points to draw regional secular variation (SV) curves and to improve the global geomagnetic field models. When no precise dating is available, the archaeomagnetic direction and intensity obtained experimentally can be used for dating the last firing of the studied material after comparison with reference SV curves.

 During the last decade, several archaeomagnetic studies (e.g. Schnepp and Lanos, 2006; Gómez-Paccard and Beamud, 2008; Tema and Lanza, 2008; Tema, 2013; Tema et al., 2014) have shown that archaeomagnetism can be a valuable dating tool for archaeology, particularly for the areas where a detailed SV curve is available and where no organic material for radiocarbon dating has been found. However, most of the up to now available studies are based on the determination of the direction of the Earth's magnetic field and only few of them include also archaeointensity analysis (Jordanova et al., 2004; Casas et al., 2007; Herries et al., 2008; De Marco et al., 2008; Tema et al., 2013), most probably because of its more complicated experimental determination.

 In this paper, we present a detailed rock-magnetic and archaeomagnetic study of two rescue excavation kilns discovered at the location of Osterietta, in Northern Italy. The full geomagnetic field vector has been determined and the archaeointensity for each kiln has been obtained with both the classical Thellier (Thellier and Thellier, 1959) and the multi-specimen protocols (Biggin and Poidras, 2006; Dekkers and Bӧhnel, 2006; Fabian and Leonhardt, 2010). A Matlab code for anisotropy correction during the Thellier experiment is provided and the archaeointensity results obtained from the Thellier and multi-specimen methods are compared and discussed. The full geomagnetic field vector has been used for archaeomagnetic dating of the two kilns after comparison with the reference curves produced by the SCHA.DIF.3K European geomagnetic field model (Pavón-Carrasco et al., 2009).

2. Archaeological site and sampling

 The two studied kilns were discovered in 2010, during the works for the 80 expansion of the Alessandria's ring road, at the location of Osterietta $(44.9\textdegree N, 8.6\textdegree E)$, in Northern Italy (Fig. 1). During two excavation campaigns that took place in 2010 and 2011, a production workshop has been identified and three kilns (in the areas 3, 4 and 6) have been excavated (Venturino et al., 2013). For the present archaeomagnetic study, samples have been collected from two of the kilns, namely OSA (area 3) and OSB (area 6), situated around 1 km away from the fortification walls of the old Alessandria city, known as *Cittadella of Alessandria* (Fig. 2a).

 OSA is a big kiln, oriented N-S, and consists of 6 *praefurnia* tunnels constructed by bricks (Fig. 2b). It has been only partly excavated as the combustion chamber is probably extended towards the northern part of the kiln, situated nowadays under the nearby highway. Each *preafurnia* tunnel is invested by series of bricks, horizontally situated. The combustion chamber, even though not excavated, was probably rectangular, as big as the excavated front of the kiln. The baking floor was constructed by bricks, pieces of which have been found in the refilling material.

 OSB kiln is situated around 100 m west of the OSA kiln and is oriented W-E. It is heavily damaged because of the intensive later agriculture activities in the area. It is not well conserved and most of the bricks that covered the *preafurnia* and the combustion chamber are lost. However, it has characteristics similar to those of OSA kiln, even though with smaller dimensions. There are still clearly visible two *preafurnia* tunnels of dimensions 2.5x0.9 m (however the total number of the tunnels is not known) and the rests of two support and baking floors (Fig. 2c).

 No ceramics or other characteristic artefacts have been found in the filling of the structures. The lack of such objects that could offer dating information and the kilns' common architecture style makes it hard for archaeologists to constrain the time of the use and the abandonment of this large production workshop. The only available dating information is based on a preliminary thermoluminescence (TL) analysis made on two bricks from kiln OSA, that suggests an age not older than XVI-XVII centuries AD (Venturino et al., 2013). However, the very limited amount of material sampled at the initial phase of the excavation (July 2010) for TL analysis has not allowed a complete and detailed TL investigation (Raimondo Prosperi, ARKAIA, personal communication). Furthermore, the proposed TL date has been calculated only from the total absorbed TL dose without including measurements of the environmental and annual dose, and the corresponding corrections. The available TL date can thus be used only as a general reference and does not offer a precise dating.

 For archaeomagnetic analysis, a total of 15 brick hand samples from OSA kiln have been collected (Fig. 2b), coming from the three first tunnels (numbered 1 to 6 from East to West). From OSB kiln, 8 brick hand samples have been collected from the *preafurnia* tunnels (Fig. 2c). All collected samples were oriented *in situ* with a magnetic compass and an inclinometer, signing the orientation arrow directly on the bricks' surface. No consolidation at the laboratory was needed as the bricks were very compact and well conserved. Bad weather conditions prevented the use of a sun compass. From each independently oriented brick, at least four cylindrical specimens of standard dimensions (diameter = 25.4 mm, height = 22 mm) were drilled in the laboratory. The prepared specimens were used for magnetic mineralogy experiments and for the determination of the archaeomagnetic direction and intensity.

3. Magnetic mineralogy

 The magnetic properties of the collected bricks have been investigated to identify the nature of the magnetic carriers, their domain state behaviour and their thermal stability with the objective to check their suitability for archaeomagnetic determinations. Isothermal remanent magnetization (IRM) acquisition curves, thermal demagnetization of three-axes IRM components (Lowrie, 1990), hysteresis loops and low-field thermomagnetic curves were measured for pilot samples.

 IRM acquisition curves of representative samples were obtained at the ALP Palaeomagnetic laboratory (Peveragno, Italy) with an ASC pulse magnetizer to impart the IRM, applying stepwise increasing magnetic fields up to 1.6 T, and a JR6 spinner magnetometer (Agico) to measure the remanent magnetization. The obtained curves for both OSA and OSB kilns are very similar, with a saturation of the magnetization reached at low fields varying from 0.2 to 0.4 T (Fig. 3). This observation is consistent with the presence of a low-coercivity mineral such as magnetite. Such interpretation is further supported by the thermal demagnetization experiments of a three component IRM (Lowrie, 1990). A composite orthogonally induced IRM was imparted to representative samples: first a maximum field (1.6 T) was applied along the cylinder – axis (Z), then an intermediate field (0.5 T) along the Y-axis and finally a minimum field (0.1 T) along the X-axis. Stepwise thermal demagnetization results of the three- axes IRM (Fig. 4) show the dominance of the magnetically soft fraction (< 0.1 T); however, in some samples mainly from OSB kiln (Fig. 4 c,d) the medium coercivity component is also important while the high coercivity component is in all cases negligible.

 Hysteresis measurements were performed with a Lake Shore 7400 Vibrating Sample Magnetometer (VSM) equipped with a chamber for low temperature (liquid

 nitrogen) measurement at INRIM (Torino, Italy). Five samples from the OSA kiln have been analysed. The hysteresis curves obtained at room temperature for representative samples (OSA-3, OSA-16 and OSA-19) show the coexistence of different magnetic contributions (Fig. 5a). The analysed powders exhibit, in fact, a ferrimagnetic behaviour, as appreciable from the hysteresis loops appearing at low 156 field values (coercive field H_c value ~ 10 mT) along with paramagnetic contributions. For further investigation of the ferrimagnetic carriers, hysteresis loops have been corrected for the paramagnetic contribution (Fig. 5 a, b, c). The shape of the loops and the low value of the coercive field suggest the presence of a soft magnetic phase, such as magnetite. Figs. 5b and 5c show the changes with temperature of the magnetization cycles exhibited by samples OSA-4 and OSA-7, respectively, in the temperature 162 range from - 196 °C to 25 °C. From the graphs, a significant content of ferromagnetic pseudo-single domain particles can be appreciated, which is related to the hysteretic behaviour and maintained at all the applied temperatures. The change of the shape of the hysteresis curves with temperature observed in figures 5b and 5c is expected to depend on the presence of smaller particles that progressively unblock their magnetization contribution moving from the soft ferrimagnetic to the superparamagnetic state as temperature decreases (see Figs 5b and 5c). Although variable, the superparamagnetic contribution of OSA samples is relevant: in the case of OSA-7 (Fig. 5c) there is a gain of magnetization higher than 50 % in the passage 171 from 25 °C to - 196 °C.

 Weak-field magnetic susceptibility measurements as a function of temperature (K–T curves) were carried out at the Palaeomagnetic laboratory of Géosciences Montpellier (France). Pieces of archaeological material from representative samples were first crushed and sieved to collect the 0.4-0.8 mm size fraction. Then K–T

 curves were acquired by heating the material from the liquid nitrogen temperature (- 177 196 °C) obtained with a cryostat apparatus (CS-L) to a high-temperature (around 620 °C) obtained with a CS-3 furnace coupled to the KLY-3 Kappabridge instrument (Agico, Czech Republic) and then cooled down to room temperature. K-T experiments indicate negligible magnetochemical changes for all samples (Fig. 6) as attested by the reversible shape of the heating and the cooling branches. The Curie temperatures, generally spreading between 550 and 580 °C, are indicative of the presence of magnetite or Ti-magnetite, in agreement with the results obtained from IRM and hysteresis experiments. We interpret the progressive increase in the susceptibility below the Curie temperature observed for all samples from OSB as a Hopkinson peak. This effect could be caused by the rotation of magnetic moments of single-domain grains. At low temperatures, a weak Vervey transition superposed on increasing curves is also observed for samples from OSB. This observation confirms that the magnetic carrier is magnetite and could also suggest the presence of a small fraction of larger grain behaving as multi-domain. Hopkinson peaks are not clearly observed in samples from OSA. This suggests a larger size for the ferrimagnetic grains, in the PSD-like behaviour in accordance with the hysteresis results. To sum up, the K-T curves provide decisive arguments, quite encouraging for palaeointensity determinations, identifying the main remanence carrier as thermally stable SD-PSD magnetite. Note that very few samples from OSA yield a paramagnetic-like behavior (sample OSA-3b in Fig. 6). We interpret these results as a heterogeneous distribution of the scarce ferrimagnetic minerals in the baked clays.

4. Archaeomagnetic field vector determination

4.1 Archaeomagnetic direction

 One specimen per sample from the OSA and OSB kilns has been selected for 202 the determination of the archaeomagnetic direction of each kiln. First the NRM of 15 specimens from OSA and 8 specimens from OSB was measured at the ALP Palaeomagnetic laboratory with a JR-6 spinner magnetometer. Following, all specimens have been stepwise thermally demagnetized from room temperature up to 580 °C with a Schonstedt TSD-2 furnace. The demagnetization results are illustrated as orthogonal vector projections of the remanent magnetization (Zijderveld, 1967) (Fig. 7). Zijderveld diagrams show that the magnetic remanence is very stable and it consists of one well defined Characteristic Remanent Magnetization (ChRM) direction.

 The directions of the ChRM for each specimen were evaluated from principal component analysis (Kirschvink, 1980). Directions calculated at specimen level are 213 well defined with maximum angular deviation (MAD) generally lower than 2° . Four specimens from OSA kiln were rejected as they didn't pass through the origin of the Zijderveld diagrams. Results from both OSA and OSB kilns at specimen level are reported in Table 1, together with the mean direction for each kiln. The statistical parameters are calculated assuming a Fisherian distribution (Fisher, 1953). Equal-area projections of the ChRM directions (Fig. 8) show a very good concentration around 219 the mean values. The calculated mean direction for kiln OSA is: D=341.8°, I= 66.2 °, $k= 389$, $\alpha_{95}= 2.3^{\circ}$ and for kiln OSB is: D= 339.6°, I= 67.5°, k= 504, $\alpha_{95}= 2.5^{\circ}$.

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- *4.2 Archaeomagnetic intensity*
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4.2.1 Experimental procedure

 Absolute intensity determinations were carried out with both the Thellier and Thellier (1959) in its classical form and the multispecimen protocols (Biggin and Poidras, 2006; Dekkers and Bӧhnel, 2006; Fabian and Leonhardt, 2010). This double approach was possible as material was available in sufficient quantity. The main motivation of a double approach was to provide an additional reliability check with a multi-method consistency. All archaeointensity measurements were carried out at the Palaeomagnetic laboratory of Géosciences Montpellier.

 The classical Thellier protocol was applied on 56 samples; 32 from OSA kiln and 24 from OSB. On the basis of the rock magnetic investigations carried before the palaeointensity measurements, no *a priori* sample selection was performed. The ChRMs are clearly of thermoremanent origin, not disturbed by significant secondary components, and the magnetic properties seem to be reasonably stable during the laboratory heating. The measurement protocol is as follows. The samples are heated and cooled twice at each temperature step in presence of a 50 µT induction field during cooling. The field is oriented along the cylinder axis of the core (z-axis) for the first cycle and in the opposite direction for the second one. Samples were heated in 11 steps between 120 °C and 560 °C: steps of 60 °C were applied between 120 and 300 241 °C, 50°C between 300 and 400 °C, 40°C between 400 and 480 °C and finally 30 °C 242 between 480 and 540 $^{\circ}$ C. After every two-temperature steps, a pTRM check was performed to detect any alteration in the thermoremanent magnetization acquisition capacity. All heating–cooling cycles were performed in air. In our palaeointensity furnace, the temperature reproducibility between heating treatments at the same step 246 is within 1 °C , and the intensity of laboratory field is maintained with a precision 247 better than $0.1 \mu T$ (Camps et al., 2011). After each heating–cooling cycle, the remanent magnetization was measured with a 2G cryogenic magnetometer.

 The Thellier archaeointensity measurements were corrected for magnetic anisotropy effect by means of the anisotropy of TRM (ATRM) according to a standard procedure adopted in the Montpellier laboratory (see Fanjat et al., 2013). The ATRM tensors were determined during the Thellier experiment, at a temperature step for which at least 20% of the initial NRM is involved for the majority of samples. In 254 this study, a temperature of 440 °C has been chosen. The samples were remagnetized 255 at this temperature after the Thellier step (that yields $+Z$ and $-Z$ steps) in $+X$, $-X$, $+Y$, and -Y directions. All archaeointensity values were corrected for the ATRM according to Veitch et al. (1984) method. Our Matlab© code estimating this correction is provided and illustrated with a data example as supplementary material 259 (see Appendix). Just after the ATRM tensor determination at 440 $^{\circ}$ C, the effect on the cooling rate on the acquisition of the TRM was estimated by repeating the last pTRM- check with a 4-times slower cooling rate (12 h) than the one used in the Thellier protocol (3 h). The low cooling rate is simply achieved by switching off the fans of the cooling system of our furnace during the pTRM acquisition.

 The multispecimen (MSP) experiments were performed with a prototype of a very fast-heating infrared furnace developed in Montpellier (FURéMAG, patent #1256194). Two key points determine its characteristics. The first is to heat uniformly a single rock sample of a 10-cc-standard volume very fast. The second is to apply to the sample during the heating (and the cooling) a precise magnetic induction field, perfectly controlled in 3D with a measured precision better than 1° (Camps et al, in preparation). The MSP-DSC protocol (Fabian and Leonhardt 2010) was applied to both OSA and OSB kilns. As in this protocol the pTRM is imparted along the NRM direction, anisotropy correction is not necessary. During the test and the calibration of this furnace, Fanjat (2012) showed that it is also not necessary to apply cooling rate correction with the MSP protocol. The heating temperature Th is chosen freely, sufficiently high to work on a sufficient fraction of the TRM (at least 20 %) but sufficiently low to avoid chemical alteration. From the thermal demagnetizations performed in the directional analysis, we chose for all the samples a single 278 temperature of 400 $^{\circ}$ C to impart the laboratory pTRM.

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4.2.2 Archaeointensity results

 The Thellier archaeointensity data were interpreted with the Thellier-tool software provided by Leonhardt et al. (2004). We adopted a standard set of criteria derived from those proposed by Fanjat et al. (2013) and based on the statistical parameters introduced by Coe et al. (1978) and modified by Prévot et al. (1985) to interpret each individual archaeointensity data and filter out those of poor technical quality. Archaeointensity values at specimen level are accepted when the linear 288 segment in the Arai plots is defined by more than four points $(n > 4)$ and spans over 50% of the total extrapolated ChRM. We quantified the difference between two pTRM acquisitions at the same temperature by the Difference Ratio (DRAT) parameter (Selkin and Tauxe, 2000). DRAT is expressed in percent and corresponds to the maximum difference measured between repeated pTRM acquisition normalized by the length of the selected NRM-TRM segment. A maximum acceptable threshold is fixed arbitrarily at 10 % even though for most of our accepted results is lower than 5 %/. Jointly, we checked on the directional plots computed from the archaeointensity experiments that the NRM fraction used to calculate the archaeointensity corresponds effectively to the ChRM direction of the core. For instance, the low-temperature part of the NRM may contain natural secondary magnetizations, and a spurious remanent magnetization acquired during the laboratory heating may superpose to the NRM if chemical changes in the magnetic minerals occurred. In total, 34 out of the 56

 analyzed samples satisfied the quality criteria mentioned above and yielded acceptable archaeointensity determinations. The selected values at specimen level are listed in Table 2, few of them are illustrated on Figure 9. Among the 22 excluded samples, 14 are rejected because of curvature in the Arai plots in spite of a good linearity in the Zijderveld plots, 5 are rejected because of a multi-component behavior observed in the Zijderveld plot, and 3 are rejected because of a too small NRM 307 fraction destroyed ($f \le 0.5$) before irreversible magneto-chemical changes arise. Note that when two slopes are present in the Arai's diagrams (see for example sample OSA_7c on Figure 9), we chose the temperature interval yielding a paleointensity close to the other determinations.

 Averaging the 23 acceptable results from kiln OSA, we found an 312 archaeointensity value of $50.6 \pm 2.2 \mu T$. The individual values are fairly coherent as attested by the small value of the standard deviation (less than 5% of the average). A different case arises for kiln OSB for which a large scatter in the individual values is 315 observed. Kiln OSB yields an archaeointensity value of $47.1 \pm 6.9 \mu$ T, based on 11 acceptable results (Table 2). The large standard deviation, which is about 13% of the average, casts doubt on the reliability of this determination and it should be therefore cautiously used for archaeomagnetic dating.

 The MSP archaeointensity results are processed in two steps. First, we selected "*a posteriori*" the samples for which the ratio between the fraction of NRM overprinted by the laboratory pTRM and the total NRM is between 0.2 and 0.8. This selection ensures that, if present, the multidomain pTRM-tail effect (see e.g. Dunlop and Ozdemir, 2000) will be correctly measured. In addition, only samples for which the angle between the NRM and the NRM remaining after the laboratory pTRM overprint is lower than a threshold angle here arbitrarily chosen to be 10° , have been selected. This selection ensures that the NRM is the ChRM. Second, the MSP archaeointensities were determined by fitting the data with robust linear regression that is anchored to the point $(0, -1)$ for the fraction and domain state corrected values (see Fabian and Leonhardt, 2010, for a detailed explanation on this protocol and its treatment). The robust regression is used to minimize the influence of outliers by iteratively weighting the data by their distance to the fitting line (Holland and Welsh, 1977). We anchored the linear regression to the point (0, -1) since it represents a theoretical reference: when a sample is cooled in zero field there is no pTRM acquisition. We estimated the effect of the value of alpha parameter for the domain state correction (Fabian and Leonhardt, 2010) by comparing the archaeointensities computed for a value of 0.5 with the two archaeointensities calculated by means of the two extreme values of 0.2 and 0.8.

 MSP results are reported on Table 3 and illustrated on Figure 10. For kiln OSA, on 10 samples measured, only 2 were rejected from the analysis because of a low NRM fraction for the first one and significant change in direction after pTRM acquisition for the second one. The eight samples selected yield a very similar palaeointensity value whatever the protocol used (DB, FC, or DSC) and whatever the value of alpha parameter (Table 3). As recommended by Fabian and Leonhardt (2010), if not significantly different from the others, the value obtained with the MSP-345 DSC (alpha = 0.5) has to be chosen, that is 54.5 ± 3.5 for kiln OSA. The uncertainty is calculated from the regression analysis with the 95% confidence interval on the slope parameter estimate. This value is in good agreement and within the error bar with the value obtained with the conventional Thellier protocol.

 For kiln OSB, it has not been possible to calculate a MSP archaeointensity value. Seven out of the ten samples measured are rejected due to a too low NRM 351 fraction. Obviously, the set temperature of 400° C to impart a significant pTRM was a priori underestimated for a majority of samples. One can explain this mistake by a large heterogeneity in the magnetic properties of samples from kiln OSB. The remaining 3 accepted points are statistically poor: a best fitting line based on only 3 points would not be trustful.

5. Archaeomagnetic dating

 The full geomagnetic field vector obtained for both OSA and OSB kilns has been used for archaeomagnetic dating after comparison with the reference SV curves calculated from the SCHA.DIF.3K regional geomagnetic field model (Pavón- Carrasco et al., 2009) at the site coordinates. Archaeointensity data obtained from the classical Thellier experiment, available for the two kilns have been used, even though the mean archaeointensity for OSB kiln is characterized by an important uncertainty (6.9 μT).

 Possible ages at 95% confidence level have been calculated using the Matlab *archaeo_dating* tool (Pavón-Carrasco et al., 2011). The final dating for each kiln is obtained after the combination of the separate density functions for declination, inclination and intensity. For OSA, archaeomagnetic dating suggests that the kiln has been for last time used in the time interval 1761-1841 AD (Fig. 11a). If we repeat the 370 dating using the archaeointensity value obtained by the MSP technique $(54.5 \pm 3.5$ 371 uT) instead of that obtained by the Thellier experiment (50.6 \pm 2.2 uT), the dating result remains practically the same (1760-1841 AD). For OSB kiln, archaeomagnetic dating based on the full geomagnetic field vector suggests that it has been abandoned between 1752 and 1831 AD (Fig. 11b). Exactly the same age is obtained if dating of the OSB kiln is repeated based only on directional results. These results clearly show

 that dating in the last few centuries AD is evidently controlled by the directions while archaeointensity results have almost no influence. The very small intensity variations of the Earth's magnetic field in Europe during the last five centuries (Pavón-Carrasco et al., 2009) result in the calculation of an associated too wide probability density (see intensity probability diagrams in Fig. 11) that makes dating resolution based on archaeointensity very low and therefore does not contribute to further restrict the dating results.

 The dating results obtained here show that the two kilns were in use and abandoned almost contemporaneously, suggesting that they were constructed in order to satisfy the need of a large production of bricks. This dating is in good agreement with the archaeological findings of the site that suggest the presence of a big workshop at the area, with three big kilns already excavated. The hypothesis of the archaeologists that the bricks produced in the studied kilns could have been used for the construction of the fortification walls of the old city of Alessandria (Cittadella of Alessandria) is supported by our results. The Cittadella was designed by the Italian military architect Ignazio Bertola and was built between 1732 and 1808 AD, with some last parts added as late as 1833 (e.g. Magazzino del Genio) (Marotta, 1991). Its construction undoubtedly needed a large quantity of bricks and the vicinity of the kilns to the fortified walls strongly supports such connection. However, other hypothesis suggesting that the produced bricks were used for the construction of the long bridge made by stones and bricks connecting to the Cittadella, and/or for the construction between 1749 and 1831 AD of several multi-storey buildings arranged along the axis of the ancient quarter of Bergoglio, are also in good agreement with our results and cannot be excluded.

6. Conclusions

 Two big brick kilns excavated at Osterietta provided abundant material for a detailed rock-magnetic and archaeomagnetic study. Magnetic mineralogy analysis suggested the suitability of the material for both direction and intensity determinations, indicating the presence of thermally stable, SD-PSD magnetite as the main magnetic carrier. These results encouraged the use of both classical Thellier and the multi-specimen procedures for archaeointensity determination. The main results of our study can be summarized as follows:

409 1. Brick samples coming from the internal part of the kilns have been heated at high temperatures and have successfully registered the direction of the Earth's magnetic field at the time of their last cooling.

 2. Both classical Thellier and MSP techniques have been successfully applied to OSA kiln, giving very similar results (statistically undistinguishable).

 3. For kiln OSB, even though rock-magnetic analysis showed the presence of SD-PSD thermally stable magnetite grains, both Thellier and MSP methods have not given successful results. The archaeointensity determined by the classical Thellier method shows large standard deviation, about 13% of the average, probably due to important inhomogeneities between single bricks that result in discrepancies on the archaeointensity values determined at sample level. Using the MSP protocol, it was not possible to calculate a mean archaeointensity due to the very low NRM fraction involved, probably caused by a not adequate temperature choice.

 4. Archaeomagnetic dating suggests that OSA kiln was last used between 1761-1841 AD and OSB kiln between 1752-1831 AD, at 95 % of probability. In the case of both kilns, dating based on the full geomagnetic field vector gave exactly the same results with dating based only on directions. This suggests, that even when archaeointensities are well defined with small standard deviation (as in the case of kiln OSA), intensity results do not improve the precision of archaeomagnetic dating when referring to the last few centuries. That is because of the slight variations of the intensity of the Earth's magnetic field during the last five centuries.

 5. The dating results obtained here support the hypothesis that the discovered kiln workshop was used for the production of bricks during the construction of the fortified walls of the *Cittadella* of Alessandria and/or the construction of secondary walls and buildings of the ancient quarter of Bergoglio that took place between 1749 and 1831 AD.

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Fig. 1. Map of Italy with the location of the Osterietta archaeological site.

- Fig. 2. a) General view of the position of the OSA and OSB kilns, situated near the
- the Alessandria city and its old *cittadella*. b-c) Photos and samples position of the kilns OSA and OSB, respectively.

 Fig. 3. Normalized IRM acquisition curves up to 0.4 T for representative samples from a) kiln OSA and b) kiln OSB. Insets show the same IRM curves up to 1.6 T.

 Fig. 4. Stepwise thermal demagnetization of three IRM components following Lowrie (1990) for representative samples from the a-b) OSA and c-d) OSB kilns. Symbols: dot= Soft- (0.1 T); diamond= Medium- (0.5 T); square= Hard- (1.6 T) coercivity component.

 Fig. 5. Hysteresis loops for representative samples from OSA kiln after subtraction of the paramagnetic contribution. a) Magnetic behaviour of three different samples (OSA- 3, OSA-16, and OSA-19) at room temperature; b- c) Comparison of the magnetic behavior of the same sample (sample OSA-4 and OSA-7 respectively) at different 597 temperatures in the range -196 to 25 \degree C. A slight increase of the coercive field with decreasing temperature can be noticed.

 Fig. 6. Dependence of weak-field susceptibility on temperature for representative samples from kilns OSA and OSB.

 Fig. 7. Stepwise thermal demagnetization results from representative samples from kilns OSA (upper part) and OSB (lower part) illustrated as Zijderveld plots. Symbols: 605 full dots $=$ declination; open dots $=$ apparent inclination.

Fig. 8. Equal area projection of the ChRM directions for kilns OSA and OSB.

 Fig. 9. Composite Arai's diagrams for 2 samples from kiln OSA and 2 samples from kiln OSB, respectively. Solid (open) circles are NRM-TRM points accepted (rejected) to calculate the least squares line used to estimate the archaeointensity. Triangles denote the pTRM checks. NRM and TRM are normalized by the NRM max and TRM max, respectively.

 Fig. 10. MSP archaeointensity determinations for kiln OSA (a,b) and kiln OSB (c,d), respectively. Closed (open) symbols represented data used (rejected) in the robust regression of the responses in Q parameters on the predictors in magnetic field (B). The MSP-DB and MSP-FC data and fitting lines (a,c) are represented with magenta and blue lines, respectively. For MSP-DSC plots (b,d), data and fitting lines are 620 calculated with alpha $= 0.5$. The dashed-black lines are the 95% confidence intervals on the best fitting lines.

 Fig. 11. Archaeomagnetic dating results for a) kiln OSA and b) kiln OSB. Up: declination (left), inclination (middle) and intensity (right) reference secular variation curves calculated from the SCHA.DIF.3K model (red curve with error band) and the kiln's measured direction and intensity (blue line with green error band); middle: calculated probability density functions for declination (left), inclination (middle) and intensity (right); down: combined probability density function for declination, inclination and intensity.

Tables caption

 Table 1. Archaeomagnetic directional results. Columns: Sample; Temperature interval used for the calculation of the direction of the ChRM at specimen level; Declination 637 (°); Inclination (°); MAD: Maximum Angular Deviation; Mean value: N= number of 638 independently oriented samples; D_m = mean declination; I_m= mean inclination; k= 639 precision parameter; $\alpha_{95} = 95\%$ semi-angle of confidence according to Fisher (1953).

Table 2. Thellier-Thellier archaeointensity results.

 Columns: n is the number of points in the interval of temperature Tmin–Tmax used to determine the archaeointensities; the fraction of NRM (f), the gap factor (g), and the quality factor (q) were calculated according to Coe et al. (1978); DRAT corresponds to the difference ratio between repeat pTRM steps normalized by the length of the selected NRM-pTRM segment; H is the uncorrected archaeointensity estimate for individual specimen and uncertainty; FaTRM and FCR are the scaling factors for TRM anisotropy and cooling rate corrections, respectively; unweighted averages for uncorrected archaeointensities H, ATRM corrected archaeointensities HaTRM, and ATRM plus cooling rate corrected archaeointensities HaTRM,CR.

Table 3. Multispecimen protocol results.

 Archaeointensity values are estimated by the zero-crossing point of the Robust linear regression on the Q parameters obtained with the MSP-DB protocol (Dekker and Bohnel, 2006), fraction correction (MSP-FC) or domain state correction protocols (Fabian and Leonhardt, 2010) as function of the laboratory field. The 95% confidence interval on the archaeointensity are calculated from the 95% confidence interval on the fitting line. R-squared is the coefficient of determination indicating how well data fit the model. RMSE is the root mean squared error for the fitting line.

673

Fig. 5

- 698
- 699

-
-
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(a)

- (b)
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-
- Fig. 11

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757 **Appendix**

758 **Matlab code estimating the factor (f) for ATRM correction** 759 **during Thellier-Thellier**

760 by Pierre CAMPS, CNRS and University of Montpellier, France. pcamps [at] univ-montp2 [dot] fr

761 v1.0 (01/01/2015)

⁷⁶² **Contents**

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- 764 [Set initial conditions.](https://mail-attachment.googleusercontent.com/attachment/u/0/?ui=2&ik=7ff5849c75&view=att&th=14afece0173a2532&attid=0.1.1&disp=inline&safe=1&zw&saduie=AG9B_P8cmhu-kLczE_iEiqvGWYcV&sadet=1422272200905&sads=M7I_z2xtR_KyT8qzpnHsq1GpIrc#0.1.1_2)
- 765 [Build the design matrix for 6-positions measurement scheme](https://mail-attachment.googleusercontent.com/attachment/u/0/?ui=2&ik=7ff5849c75&view=att&th=14afece0173a2532&attid=0.1.1&disp=inline&safe=1&zw&saduie=AG9B_P8cmhu-kLczE_iEiqvGWYcV&sadet=1422272200905&sads=M7I_z2xtR_KyT8qzpnHsq1GpIrc#0.1.1_5)
- 766 [Compute the pTRM acquired along +X,+Y+Z,-X,-Y,-Z](https://mail-attachment.googleusercontent.com/attachment/u/0/?ui=2&ik=7ff5849c75&view=att&th=14afece0173a2532&attid=0.1.1&disp=inline&safe=1&zw&saduie=AG9B_P8cmhu-kLczE_iEiqvGWYcV&sadet=1422272200905&sads=M7I_z2xtR_KyT8qzpnHsq1GpIrc#0.1.1_6)
- 767 [Quality tests](https://mail-attachment.googleusercontent.com/attachment/u/0/?ui=2&ik=7ff5849c75&view=att&th=14afece0173a2532&attid=0.1.1&disp=inline&safe=1&zw&saduie=AG9B_P8cmhu-kLczE_iEiqvGWYcV&sadet=1422272200905&sads=M7I_z2xtR_KyT8qzpnHsq1GpIrc#0.1.1_9)
- 768 [Calculate tensor and sigma value.](https://mail-attachment.googleusercontent.com/attachment/u/0/?ui=2&ik=7ff5849c75&view=att&th=14afece0173a2532&attid=0.1.1&disp=inline&safe=1&zw&saduie=AG9B_P8cmhu-kLczE_iEiqvGWYcV&sadet=1422272200905&sads=M7I_z2xtR_KyT8qzpnHsq1GpIrc#0.1.1_11)
- 769 [Correction Factor for TRM anisotroptry](https://mail-attachment.googleusercontent.com/attachment/u/0/?ui=2&ik=7ff5849c75&view=att&th=14afece0173a2532&attid=0.1.1&disp=inline&safe=1&zw&saduie=AG9B_P8cmhu-kLczE_iEiqvGWYcV&sadet=1422272200905&sads=M7I_z2xtR_KyT8qzpnHsq1GpIrc#0.1.1_16)
- 770 [Print the result](https://mail-attachment.googleusercontent.com/attachment/u/0/?ui=2&ik=7ff5849c75&view=att&th=14afece0173a2532&attid=0.1.1&disp=inline&safe=1&zw&saduie=AG9B_P8cmhu-kLczE_iEiqvGWYcV&sadet=1422272200905&sads=M7I_z2xtR_KyT8qzpnHsq1GpIrc#0.1.1_21)
- 771 [Example of INPUT file](https://mail-attachment.googleusercontent.com/attachment/u/0/?ui=2&ik=7ff5849c75&view=att&th=14afece0173a2532&attid=0.1.1&disp=inline&safe=1&zw&saduie=AG9B_P8cmhu-kLczE_iEiqvGWYcV&sadet=1422272200905&sads=M7I_z2xtR_KyT8qzpnHsq1GpIrc#0.1.1_22)

⁷⁷² **Preliminary comments**

- 773 First, we compute the A-TRM tensor by means of procedures adapted from L. Tauxe's algorithm
774 implemented by the fortran program aarm s ITauxe, 1998I that use the off-axis remanence terms implemented by the fortran program aarm s [Tauxe, 1998] that use the off-axis remanence terms.
- 775 Then, we calculate anisotropy factor correction following the method described by **Veitch et al., 1984** (Arch. Sc. Geneve, 37, 3 pp 359-373).
- 777 INPUT file : JRA format with 6 measurements in the following order $+Z$, $-Z$, $+X$, $-X$, $+Y$, $-Y$ (example -778 of an input file is provided at the end of this document) of an input file is provided at the end of this document)
- 779 OUTPUT : f_atrm factor and some others parameters...

780 **Cautionary notes** :

- 781 [1] In this program, the NRM direction in core coordinates is determined from the +Z and -Z steps at the temperature step selected for the anisotropy determination. If this direction is significantly differe 782 the temperature step selected for the anisotropy determination. If this direction is significantly different from the direction obtained by with PCA analysis processed within the temperature interval used for 783 from the direction obtained by with PCA analysis processed within the temperature interval used for paleointensity estimate, this later should be used. paleointensity estimate, this later should be used.
- 785 **[2]** This software is distributed on an "AS IS" basis, WITHOUT WARRANTY OF ANY KIND, either express or implied.
- 787 **[3]** Papers reporting results obtained with the present source code may cite in the references or bibliography the paper by Tema et al., Stud. Geophys. Geod., XX, (X), pp-pp, 2015.

⁷⁸⁹ **Set initial conditions.**

790 input_filename='OS1_3b.jra';
791 nb Pos = 6;

nb $Pos = 6;$

792 First, check the number of steps measured in the datafile (MUST be equal to 6)

```
793 infile = fopen(input_filename,'r');<br>794 allText = textscan(infile,'%s','de
794 allText = textscan(infile,'%s','delimiter','\n','CommentStyle','%');<br>795 numberOfLines = length(allText{1});
795 numberOfLines = length(allText{1});<br>796 frewind(infile);
         frewind(infile);
797<br>798
798 if numberOfLines ~= nb_Pos
799 disp('ERROR : input file in wrong format !!!')
800 disp('6 measurements +Z, -Z, +X, -X, +Y, -Y are required for 801 calculation')
801 calculation')<br>802 return:
              return;
803 end
804 Preallocating memory for arrays
```

```
805 sample_name = cell(1,numberOfLines);<br>806 xyz = zeros(nb Pos,3); % cartes
806 xyz = \overline{z}eros(nb_Pos,3); % cartesians coordinates<br>807 bline = zeros(3,3); % NRM remaining.
807 bline = zeros(\overline{3}, 3);<br>808 H6 = zeros(nb Pos, 3);
808 H6 = zeros(nb_Pos,3); % applied field directions<br>809 a6 = zeros(nb_Pos*3.nb Pos);
809 a6 = zeros(nb_Pos*3,nb_Pos);<br>810 w = zeros(1,nb Pos*3);
          w = zeros(1, nb Pos*3);
```
⁸¹¹ **Build the design matrix for 6-positions measurement**

⁸¹² **scheme**

```
813 dec6 = [0 \text{ pi}/2 \text{ 0 pi } 3 \text{*pi}/2 \text{ 0};814 inc6 = [0 \t0 \tpi/2 \t0 \t0 \t-\pi/2];815<br>816
816 for i=1:nb Pos<br>817 [H6(i,1), H6(
             [H6(i,1),H6(i,2),H6(i,3)]= sph2cart(dec6(i),inc6(i),1.0);
818 end
819<br>820
820 % Fill nonzero components of design matrix 821 for i=1:nb Pos
821 for i=1:nb_Pos<br>822 index = (i-1)822 index = (i-1)*3+1;<br>823 a6(index,1) = H6(
823 a6(index, 1) = H6(i, 1);<br>824 a6(index, 4) = H6(i, 2);
824 a6(intdex, 4) = H6(i, 2);<br>825 a6(intdex, 6) = H6(i, 3);825 a6(index, 6) = H6(i, 3);<br>826 index = (i-1)*3+2;
826 index = (i-1)*3+2;<br>827 a6(index, 4) = H6(
827 a6(index, 4) = H6(i, 1);<br>828 a6(index, 2) = H6(i, 2);
828 a6(index, 2) = H6(i, 2);<br>829 a6(index, 5) = H6(i, 3);829 a6(index, 5) = H6(i, 3);<br>830 index = (i-1)*3+3;
830 index = (i-1)*3+3;<br>831 a6(index, 6) = H6(
831 a6(index, 6) = H6(i, 1);<br>832 a6(index, 5) = H6(i, 2);832 a6(index,5) = H6(i,2);<br>833 a6(index,3) = H6(i,3);a6(intdex,3) = H6(i,3);834 end
835<br>836
         b6 = (a6' * a6) \a6'; % design matrix
```
⁸³⁷ **Compute the pTRM acquired along +X,+Y+Z,-X,-Y,-** ⁸³⁸ **Z**

839 Read the data file

```
840 i=0;<br>841 whil
841 while ~feof(infile)<br>842 inline=faetl(inf
842 inline=fgetl(infile);<br>843 if ~isempty(inline) &
843 if ~isempty(inline) && ~strncmp(inline,'%',1)
844 \qquad \qquad \text{i=i+1;} \\ 845 \qquad \qquad \text{A=ssca}845 A=sscanf(inline,'%6c, %5c, %f, %f, %f, %f ');<br>846 sample name{i} = strcat(A(1:6));
846 sample_name{i} = strcat(A(1:6));<br>847 treatment{i} = strcat(A(7:11))
847 treatment{i} = strcat(A(7:11));<br>848 xyz(i,1) = A(12) * 10^A(15);
848 xyz(i,1) = A(12) \times 10^{A}(15);<br>849 xyz(i,2) = A(13) \times 10^{A}(15);849 xyz(i,2) = A(13) * 10^A(A(15);<br>850 xyz(i,3) = A(14) * 10^A(A(15);xyz(i,3) = A(14) * 10^A(A(15);851 end<br>852 end
```

```
852
```
853 Compute the baselines (NRM remaining)

```
854 for i = 1:3<br>855 bline(1,i)
          bline(1,i) = (xyz(3,i) + xyz(4,i))/2; % +X and -X
856 bline(2,i) = (xyz(5,i) + xyz(6,i))/2; % +Y and -Y<br>857 bline(3,i) = (xyz(1,i) + xyz(2,i))/2; % +Z and -Z
          bline(3,i) = (xyz(1,i) + xyz(2,i))/2; % +Z and -Z
858 end
```
859 Compute the pTRM acquired in the 6 positions

```
860 pTRM(1,:) = xyz(3,:) - bline(1,:); % +X<br>861 pTRM(2,:) = xyz(5,:) - bline(2,:); % +Y
861 pTRM(2,:) = xyz(5,:) - bline(2,:); % +Y<br>862 pTRM(3,:) = xyz(1,:) - bline(3,:); % +Z
862 pTRM(3,:) = xyz(1,:) - bline(3,:); % +Z<br>863 pTRM(4,:) = xyz(4,:) - bline(1,:); % -X
863 pTRM(4,:) = xyz(4,:) - bline(1,:); % -X<br>864 pTRM(5,:) = xyz(6,:) - bline(2,:); % -Y
864 pTRM(5,:) = xyz(6,:) - bline(2,:); % -Y<br>865 pTRM(6,:) = xyz(2,:) - bline(3,:); % -Z
          pTRM(6,:) = xyz(2,:) - bline(3,:); % -Z
```
⁸⁶⁶ **Quality tests**

867 Check possible changes in NRM directions during pTRM acquisitions

```
868 fprintf('NRM directions after acquisition along X, Y, and Z \n');<br>869 for i = 1:3
       for i = 1:3870<br>871
871 angle=atan2(norm(cross(bline(3,:),bline(i,:))),dot(bline(3,:),bline(i<br>872 .:)));
872 ,:)));<br>873 [nrm
          [nrmbECL,nrmINC,nrmF] = cart2sph(bline(i,1),bline(i,2),bline(i,3));874
875 formatSpec = 'Decl: 6.1f Inc : 6.1f Angle : 6.1f \n\pi;<br>876 fprintf(formatSpec, rad2deq(nrmDECL), rad2deq(nrmINC),
876 fprintf(formatSpec, rad2deg(nrmDECL), rad2deg(nrmINC), 877 rad2deg(angle)):
       rad2deg(angle));
878 end<br>879 NRM
       NRM directions after acquisition along X, Y, and Z880 Decl: 85.4 Inc : 65.0 Angle : 0.8 
881 Decl: 82.3 Inc : 66.1 Angle :<br>882 Decl: 85.3 Inc : 65.8 Angle :
       Decl: 85.3 Inc : 65.8 Angle : 0.0
```
883 Compare the remanence direction to the direction of applied field

```
884 angle_threshold = 15;<br>885 for i = 1:nb Pos
```

```
885 for i = 1:nb Pos<br>886 angle=atan2(no.
```

```
886 angle=atan2(norm(cross(H6(i,:),pTRM(i,:))),dot(H6(i,:),pTRM(i,:)));<br>887 if rad2deg(angle) > angle threshold
          if rad2deg(angle) > angle threshold
```

```
888 formatSpec = 'WARNING, angle between pTRM and applied field :<br>889 % 4.1f for position : % d \n\cdot :
889 %4.1f for position: %d \n';<br>890 forintf(formatSpec. ra
890 fprintf(formatSpec, rad2deg(angle), i);<br>891 else
891 else<br>892
892 formatSpec = 'OK, angle between pTRM and applied field : %4.1f 893 for position : %8f \n';
893 for position : %d \n';<br>894 fprintf(formatSp
                   fprintf(formatSpec, rad2deg(angle), i);
895 end
896 end<br>897 OK.
897 OK, angle between pTRM and applied field : 1.6 for position : 1<br>898 OK, angle between pTRM and applied field : 0.3 for position : 2
898 OK, angle between pTRM and applied field : 0.3 for position : 2<br>899 OK, angle between pTRM and applied field : 1.7 for position : 3
899 OK, angle between pTRM and applied field : 1.7 for position : 3<br>900 OK, angle between pTRM and applied field : 1.6 for position : 4
900 OK, angle between pTRM and applied field : 1.6 for position : 4<br>901 OK, angle between pTRM and applied field : 0.3 for position : 5
901 OK, angle between pTRM and applied field : 0.3 for position : 5<br>902 OK, angle between pTRM and applied field : 1.7 for position : 6
         OK, angle between pTRM and applied field : 1.7 for position : 6
```
⁹⁰³ **Calculate tensor and sigma value.**

```
904 Tensor before normalization
```

```
905 for i=1:nb Pos<br>906 for i=1:3906 for j=1:\overline{3}<br>907 index =
907 index = (i-1)*3+j;<br>908 w(index) = pTRM(i,
               w(index) = pTRM(i,j);909 end
910 end
\frac{911}{912}912 x = b6 * w';<br>913 a = diag([x])913 a = diag([x(1) x(2) x(3)]);<br>914 a(1.2) = x(4);
914 a(1,2) = x(4);<br>915 a(1,3) = x(6);
915 a(1,3) = x(6);<br>916 a(2,3) = x(5);
916 a(2,3) = x(5);<br>917 a(2,1) = a(1,2)917 a(2,1) = a(1,2);<br>918 a(3,2) = a(2,3);918 a(3,2) = a(2,3);<br>919 a(3,1) = a(1,3);a(3,1) = a(1,3);920 Tensor normalized by trace
921 t=sum(diag(a));<br>922 a=a/t:922 a=a/t;<br>923 w=w/t;w=w/t;
924 Compute sigma value
925 comp = horzcat(reshape(a, 1, 9), reshape(-a, 1, 9));<br>926 s = sum((w - comp).^2);
         S = sum((w - comp).^2);927<br>928
928 free = 12; \frac{1}{3} npos*3-6<br>929 if(S > 0)
929 if(S > 0)<br>930 s
                     sigma=sqrt(S/free);
931 else
                     sigma=0.;
933 end
934 Calculate eigenvalues and right eigenvectors of the A-TRM tensor
```

```
935 [eigenVectors, eigenValues] = eig(a, 'vector');<br>936 for i=1:3
       for i=1:3
```

```
937<br>938
938 [decl\_ev, incl\_ev, F\_ev] = cart2sph(eigenVectors(1,i), eigenvectors(2,i), e)<br>939 i denVectors(3,i));
          igenVectors(3, i));
940<br>941
941 decl_ev=rad2deg(decl_ev);<br>942 incl_ev=rad2deg(incl_ev);
942 incl_ev=rad2deg(incl_ev);<br>943 if incl ev < 0
943 if \overline{1}ncl ev < 0<br>944 incl ev=
944 incl_ev=-incl_ev;<br>945 declev=declev-1
                       \text{decl} ev=decl ev-180;
946 end<br>947 if
947 if decl_ev < 0<br>948 decl ev=
                       decl ev=decl ev+360;
949 end
950<br>951
951 formatSpec = 'Sample %s eing_v %4.6f Decl : %3.1f Incl : 952 %3.1f \n';
952 \frac{3.1f}{n};<br>953 fprintf(
953 fprintf(formatSpec, sample_name{1},<br>954 eigenValues(i).decl ev.incl ev):
          eigenValues(i), decl ev, incl ev);
955 end<br>956 Sami
956 Sample OS1_3b eing_v 0.311277 Decl : 351.1 Incl : 72.3<br>957 Sample OS1_3b eing_v 0.342807 Decl : 219.9 Incl : 11.9<br>958 Sample OS1 3b eing v 0.345916 Decl : 127.1 Incl : 12.9
957 Sample OS1 3b eing v 0.342807 Decl : 219.9 Incl : 11.9<br>958 Sample OS1 3b eing v 0.345916 Decl : 127.1 Incl : 12.9
                                 eing \overline{v} 0.345916
```
⁹⁵⁹ **Correction Factor for TRM anisotroptry**

960 Please note that NRM direction is obtained from the +Z and -Z steps. This direction **must** be taken 961 from the Arai plot if it's significantly different.

```
962 m = bline(3,:)'; % NRM direction
963<br>964
      u=[0;0;1]; % u is the unit vector along z-axis
```
965 Calculate the unit vector (h) in direction of ancient field

```
966 h anc=a\m/norm(a\m);
967<br>968
968 [</math>rDec_c,rInc_c,r]=cart2sph(h_anc(1),h_anc(2),h_anc(3));<br>969 Dec c=radtodeg(rDec c);969 Dec<sub>_C</sub>=radtodeg(rDec_c);<br>970 if Dec c < 0
970 if \overline{Dec\_c} < 0<br>971 Dec c
                   Dec c = 360.0 + Dec c;
972 end<br>973 Inc
         Inc_c=radtodeg(rInc_c);
974<br>975
975 angle_r=atan2(norm(cross(m, h_anc)),dot(m, h_anc));<br>976 angle=rad2deg(angle r);
         angle=rad2deg(angler);
```

```
977 Calculate the correction factor f
```

```
978 f=norm(a*u)/norm(a*h_anc);
```

```
979 Calculate the degree of Anisotropie (Nagata, T., 1961. Rock Magnetism, 2nd edition. Maruzen, Tokyo)
```

```
980 P = max(diag(a))/min(diag(a));
```
981 Calculate the shape parameter (Jelinek, V., 1981. Tectonophysics 79, T63?T67.)

```
982 shape_T = (2 * log(a(2,2)) - log(a(1,1)) - log(a(3,3))) / 983 (log(max(diaq(a))) - log(min(diaq(a))));
          (\log(\max(\text{diag}(a))) - \log(\min(\text{diag}(a))));
```
⁹⁸⁴ **Print the result**

985 fprintf('Sample f P T Dec Inc Dec_c
986 Inc c Angle \n'); 986 Inc_c Angle \n');
987 fprintf('------------987 fprintf('-- $---------\ (n')$; 989
990 990 formatSpec = ' %s %7.4f %6.3f %6.3f %7.1f %7.1f %7.1f %7.1f
991 %7.1f\n'; 991 $\frac{87.1f}{n}$;
992 fprintf(f) 992 fprintf(formatSpec, sample_name{1}, f, P, shape_T, rad2deg(nrmDECL), 993 rad2deg(nrmINC), Dec c, Inc c, angle); 993 rad2deg(nrmINC), Dec_{_C}, Inc_c, angle);
994 Sample f P T Dec 994 Sample $f = \overline{P} = T$ Dec Inc Dec_c Inc_c 995 Angle 995 Angle
996 ------996 --- 997
998 998 OS1_3b 0.9851 1.096 1.114 85.3 65.8 81.1 67.8 2.6

¹⁰⁰⁰ **Example of INPUT file**

 type OS1_3b.jra
 1002 % Name, treat, 1002 % Name, treat, Xc, Yc, Zc, power OS1_3b, Z+440, 0.05, 2.34, 9.97, -1 OS1_3b, Z-440, 0.33, 2.26, 0.31, -1 OS1_3b, X+440, 5.43, 2.33, 4.89, -1 OS1_3b, X-440, -5.05, 2.36, 5.19, -1 OS1_3b, Y+440, 0.28, 7.49, 5.02, -1 OS1_3b, Y-440, 0.31, -3.10, 4.98, -1

1009
1010

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