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Superconductivity in doped semiconductors

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A historical survey of the main normal and superconducting state properties of several semiconductors doped into superconductivity is proposed. This class of materials includes selenides, tellurides, oxides and column-IV semiconductors. Most of the experimental data point to a weak coupling pairing mechanism, probably phonon-mediated in the case of diamond, but probably not in the case of strontium titanate, these being the most intensively studied materials over the last decade. Despite promising theoretical predictions based on a conventional mechanism, the occurrence of critical temperatures significantly higher than 10 K has not been yet verified. However, the class provides an enticing playground for testing theories and devices alike.

Introduction : half a century in a nutshell.

The notion that “doping” an insulating material by inserting or substituting atoms with a different valence state may bring about superconductivity (below an experimentally accessible critical temperature T_c) is not new. It has been successfully applied to various classes of solids, whereby the resulting free carrier density became a tunable variable, as illustrated in many contributions to this special issue. However, there was a time when the occurrence of superconductivity in materials with appreciably less than one carrier per atom was an open question. The main reason for this was that a lower carrier density was expected to reduce the efficiency of dielectric screening to the point where Coulomb repulsion could not be overcome by any pairing mechanism. In this context, the idea that semiconductors chemically doped beyond the critical value n_{MIT} for a metal-insulator transition to occur would eventually become superconductors was suggested and discussed quite early on for three-dimensional (3d) degenerate systems¹⁻⁴. It was experimentally applied in the 60’s to self-doped (with holes) narrow bandgap semiconductors, mostly tellurides such as GeTe^{5,6}, SnTe⁷⁻⁹, and the at that time more controversial PbTe^{10,11}. Electron doped systems were also investigated such as La_{3-x}Se₄^{12,13} and other lanthanum compounds, or the more popular reduced (or Nb-doped) SrTiO₃^{14,15}, a much wider bandgap semiconductor. In the case of GeTe, the “gap ratio” of the superconducting gap width 2Δ (Δ being the binding energy of the Cooper pair) to its critical thermal energy $k_B T_c$ was

measured¹⁶. The value of 4.3 was taken at the time as a confirmation of the conventional weak coupling mechanism usually referred to as¹⁷ BCS, which predicted a gap ratio of 3.5. Probably because increasing the carrier concentration n_e in these systems did not enhance the T_C values above 500 mK (the T_C vs n_e curve even followed a “dome” shape in one case¹⁵, or because the observations remained restricted to “ionic” semiconductors, this initial interest did not last^{16,17}.

One generation later, the observation of superconductivity ($T_C = 8$ K) in silicon clathrates where alkaline earth metals had been inserted in the cages for doping showed that sp^3 hybridization of column IV elements was compatible with superconductivity^{19,20}. Such experiments were inspired by studies of superconducting alkali-doped fullerenes (see the article by A. Ramirez in this issue). Their quantitative modelling²¹ by ab initio calculations and a conventional pairing mechanism illustrated the strength of the electron-phonon coupling in rigid sp^3 -bonded networks, and pointed to carbon-based clathrates as a route toward a higher T_C . Although quite telling in hindsight, these findings were not the origin of the discovery published the following year²² of type II superconductivity ($T_C=2.6$ K, onset at 4 K) in polycrystalline boron-doped diamond grown at high pressure and high temperature (HPHT). This seminal report, which included magnetotransport and magnetic susceptibility measurements, was quickly confirmed by other groups for boron-doped polycrystalline²³ and homoepitaxial²⁴ diamond films grown by Microwave Plasma-enhanced Chemical Vapor Deposition (MPCVD). As reviewed a few years ago^{25,26}, many groups have reproduced and extended these initial results, with transition onset temperatures soon reaching the 10 K mark in polycrystalline thick films. As for single crystal diamond, the maximum T_C reported so far was 8 K in C:B epilayers²⁷ grown along (111), written as $C_{(111)}:B$ in the following.

Such experimental evidence for superconductivity in boron-doped diamond motivated many theoretical quantitative studies. In order to estimate the maximum critical temperature that could be explained under the assumption of a phonon-assisted pairing mechanism, most of these resorted to numerical calculations involving the Virtual Crystal Approximation^{28,29} (VCA), periodic supercells^{30,31}, or both³². In some cases, the random incorporation of boron was taken into account³³⁻³⁵ by using the Coherent Potential Approximation (CPA). These studies generally used the calculated electronic and vibronic band structure to derive the electron-phonon coupling spectral distribution (the so-called Eliashberg function $\alpha^2F(\omega)$) and to compute the average coupling strength parameter λ by integrating the Ug_F product over the Fermi surface, g_F being the density of electronic states at the Fermi level E_F (defining a Fermi temperature T_F) and U the electron-phonon interaction potential. In diamond, because of the stiff 3d network resulting from sp^3 hybridization of the carbon atoms, U was found to be stronger than in the parent MgB_2 covalent superconductor³⁶, but g_F was much lower, leading to calculated λ values lying between 0.15 and 0.55 depending on the calculation method, for a doping level in the few at.% range. This was significantly lower than in MgB_2 , where λ is close to 1. These theoretical works then used the McMillan formula³⁷ to estimate T_C as a function of λ , of a logarithmic average phonon frequency represented here by the Debye energy $k_B\theta_D$, and of the screened and retarded Coulomb repulsion potential μ usually expressed as $\mu^*=\mu/[1+\mu \text{Log}(T_F/\theta_D)]$. With these parameters, this formula reads:

$$T_C = \theta_D/1.45 \exp[-(1.04(1+\lambda))/(\lambda -\mu^*(1+0.62 \lambda))] \quad \text{Eqn. 1}$$

In diamond, $\theta_D = 2000$ K, quite a high value. As for μ^* , most of the authors assumed that the values typical for metals ($\mu^*=0.15$) still applied, despite the fact that the Fermi energy E_F and the average

phonon energy described by $k_B\theta_D$ were comparable in superconducting diamond (see table 1). Such an approach reproduced most of the trends of the experimental results, such as the magnitude of T_C or the negative sign of the pressure coefficient³⁸, and provided some insight as to which phonons contributed most significantly to the coupling³⁰⁻³². However, the simulations failed to reproduce the values of T_C when the free hole concentration n_h was reduced down to n_{MIT} , as well as the curvature of the experimental T_C vs n_h variations^{34,35,39,40}. Rescaling the coupling and screening parameters λ and μ^* according to power laws close to the critical concentration has been proposed for diamond⁴⁰ and silicon⁴¹ but remains specific and unsatisfactory. More general descriptions^{42,43} of the effect of approaching the MIT in disordered metals yield T_C enhancements which have not been detected in the materials under study here. Unfortunately, the powerful parameter-free approach where the Coulomb pseudo-potential μ does not need to be adjusted⁴⁴ has not been applied to any of the superconducting semiconductors so far. This situation prompted alternative theoretical approaches either based on the resonating valence bond model which assumes transport within an impurity band⁴⁵, at the crossover between the host band and the impurity band⁴⁶, or which relied on attractive spin-spin interactions between weakly localized holes near the Fermi level^{47,48}. Meanwhile, under the assumption of optical phonon-mediated pairing, the maximum achievable T_C in diamond has been tentatively estimated^{49,50}. In a similar manner, it was predicted^{51,52} that the rhombohedral $B_{13}C_2$ and cubic BC_5 compounds would yield a T_C value close to that observed in MgB_2 .

The calculated transition temperatures of a few K as detailed above for hole-doped diamond were also considered by some authors^{28,53} to be in sufficient agreement with experiment to warrant predictions of p-type superconductivity in other column IV semiconducting materials, namely Si and Ge. Despite the notorious incapacity of BCS theory to predict new superconductors⁵⁴, experimental evidence for superconductivity was gathered over the next few years, first in silicon⁵⁵, then in silicon carbide⁵⁶, both upon boron doping in the few at. % range, with T_C soon⁵⁷ reaching 1.5 K in 3C-SiC:B and 6H-SiC:B (cubic 3C and hexagonal 6H are two of the many polytypes of silicon carbide), and more recently⁴¹ 0.7 K in Si:B. Ab initio calculations in the spirit detailed above were performed about superconductive Si:B, resulting in λ values which remained^{41,55} below 0.45 even for 10 at.% B. Other dopants of silicon have also been investigated⁵⁸, the calculations pointing out the detrimental influence on the electron-phonon coupling strength of the lattice contraction brought about by atomic substitution by impurities with a smaller covalent radius, so that substitutional doping (n-type) of silicon with aluminum was seen theoretically as a favorable (but notoriously unpractical) option. Similar calculations have been proposed^{59,60} also in the case of SiC:B, where less energetic acoustic phonons were shown to come into play, in good agreement with specific heat measurements⁶¹. Further experimental studies showed that (p-type) doping 3C-SiC with aluminum^{62,63} yielded a similar T_C of 1.45 K.

The next column IV indirect bandgap semiconductor to be doped into superconductivity (see ref. 64 for a review) was germanium⁶⁵, with a maximum T_C of 0.5 K in Ge:Ga, again in rough agreement with ab initio calculations⁶⁶. Further optimization⁶⁷ of the flash annealing conditions led to an increase of T_C from about 0.2 to 0.5K as the Hall carrier density n_H was varied from 2 to $5 \times 10^{20} \text{ cm}^{-3}$. Other annealing strategies yielded less systematic variations, among which a few higher T_C values, at 1.2 K for⁶⁸ $n_H = 11 \times 10^{20} \text{ cm}^{-3}$, and 1K for⁶⁹ $n_H = 6 \times 10^{20} \text{ cm}^{-3}$. In parallel, a similar experimental process was applied by the same group on silicon, and SiO_2 :Ga/Si:Ga composites were shown to be superconducting⁷⁰. However, Aluminum and Gallium being superconducting elementary metals with respective T_C of 1.2K and 1.1 K, the authors have considered the possibility that the

superconductivity originated from Al or Ga clusters. They have so far concluded that Ga-rich amorphous nano-inclusions are present only in the case⁷¹ of Si:Ga. As explained in a recent summarizing overview⁷², such caveats apply to any compound containing one element (for instance Pb, In or Ga) which may form a superconducting island. This is the reason why except for the specific case of PbTe⁷³, the numerous reports about PbSe, InN and In₂O₃, or GaAs and GaN, despite their quality, will not be mentioned in this review. We shall also discard from the present survey the numerous and in general disordered metallic compounds containing Si or Ge, either binary (for example Au:Si, Mo:Si, W:Si, CoSi₂, Cu:Ge) or ternary, despite their interesting low temperature transport properties, including superconductivity. Doped cubic silicon clathrates and non-cubic high pressure superconducting phases of silicon will also be ignored, as well as the numerous superconducting carbon allotropes (such as metal-intercalated graphites and fullerenes), most of which are described elsewhere in this special issue.

As a matter of fact, a high pressure phase of solid boron is also superconducting, but its presence has been consistently ruled out in the boron-doped semiconductors under consideration here. The aggregation of boron has been the object of some attention in the case of diamond, where boron pairing has been found energetically favorable⁷⁴ in heavily-doped crystals. Aggregation in boron-rich regions has been observed in grain boundaries^{75,76}, without any clear correlation with superconductivity⁷⁷. On the contrary, in cases where the grain boundaries became atomically thin, the boron-rich triple points (most probably B₄C) were found to remain in the normal state⁷⁸ at low temperatures. The formation of B₄C crystalline particles on the (111) surface of diamond single crystals doped during their HPHT growth by the temperature gradient method has also been reported recently⁷⁹. Anyway, the quest for the boron-rich superconducting phases predicted theoretically^{51,52,80} has not been successful so far⁸¹. Although the spatial distribution of boron atoms has been recognized as a source of short range disorder, and of grain-to-grain heterogeneity in polycrystalline diamond^{77,82}, no such clustering has yet been reported to take place in single crystal C:B, nor in Si:B epilayers⁸³. Actually, from a material synthesis point of view, it must be stressed that most of the advances just described result from the recently available possibility of circumventing the solubility limit of the dopant impurities in the host material by using out-of equilibrium processing techniques such as Gas Laser Immersion laser doping⁸⁴ or shallow implantation/flash annealing sequences^{85,86}.

Coming back to some of the superconducting semiconductors which were studied most intensively half a century ago, one cannot fail to mention that single crystal SnTe is nowadays considered as a crystalline topological insulator^{87,88} when it is low-doped and in the rocksalt structure (its low T phase). Moreover, In-doped SnTe is an intriguing superconductor in its own right^{11,89}, as are TI-doped^{73,90,91} PbTe and even more so In-doped PbTe, which features both ferroelectricity at low In content (rhombohedral phase) and⁹² “topological superconductivity” above a critical In content of a few at.%, at which a structural transition to a cubic rocksalt phase occurs. Such aspects are dealt with in S. Sasaki’s contribution in this volume. In the case of La_{3-y}Se₄, it is the thermoelectric properties that are drawing increasing interest⁹³. As for SrTiO₃, it is still the most dilute 3d superconductor by far⁹⁴, down to free electron density values around $5 \cdot 10^{17} \text{ cm}^{-3}$ which challenge any BCS-type of pairing mechanism⁹⁵. It has been the object of many studies spread over the last 50 years⁹⁶. Recently, it has been shown (see the contribution of Triscone & Gabay in this special issue) that the interface of SrTiO₃ with another oxide could give rise to a 2d metal with a superconducting ground state^{97,98}. Before describing in the next sections the normal and superconducting 3d states of some of the

materials mentioned in this introductory historical overview, we propose to summarize in fig. 1 their T_C dependence on the nominal free charge carrier density as estimated from Hall effect, (except in the case of silicon, where boron concentrations have been used) in the spirit of a previous and broader review⁹⁹. Beside the usual uncertainties on the critical temperature values arising from an author's dependent definition, it should be stressed that the direct derivation of the apparent normal state carrier density from Hall effect data suffers from shortcomings related either to macroscopic doping heterogeneities or to the Fermi surface shape-dependent value of the Hall factor, which may differ significantly from unity. As a matter of fact, such apparent densities have been found to be larger than the chemical concentration of the doping element by 50% in⁹ SnTe, and by up to an order of magnitude in diamond^{27,40}. A numerical application of equation 1 to the case of silicon ($\theta_D = 640$ K) using a boron concentration-dependent electron-phonon coupling parameter λ evaluated by ab initio supercell calculations⁴¹ is also given in fig. 1 to illustrate the shortcomings of such a simple approach when it comes to predicting T_C variations over a wide range of concentrations. Figure 1 also displays some scatter among the experimental data coming from different groups. In the particular case of silicon, T_C depends on thickness (hence the two sets of points in fig. 1) in such a way that it seems to be determined by the sheet boron density rather than by its volumic concentration⁴¹.

3d normal state properties

Many of the standard properties of the above-mentioned materials can be found in current handbooks and databases, albeit referring mostly to their undoped semiconducting state. Some low T but normal state parameters usually deemed¹¹ to be relevant for the discussion of the superconductivity are listed in table 1 for the three tin and germanium and lead tellurides^{91,100,101}, strontium titanate⁹⁴, as well as for the four group IV covalent superconductors: germanium⁶⁷, silicon⁴¹, silicon carbide^{57,62} and diamond²⁷. The cubic fcc structure of germanium telluride at high temperature becomes rhombohedrally distorted along the cube diagonal at room temperature and below. Strontium titanate has a cubic perovskite crystal structure at room temperature and undergoes a structural transition to tetragonal around 110 K or lower, depending on the self-doping level. All other materials have a cubic structure, except for the 6C-SiC polytype. The bandgap width E_G as well as the Debye temperature θ_D and the relative permittivity at low frequency ϵ_r are expected to vary upon heavy doping: for example, on the basis of specific heat measurements of superconducting samples, θ_D in 3C-SiC:B has been estimated⁶¹ at 590 K and that of heavily doped bulk diamond¹⁰² C:B at 1440 K, i.e. much lower than the nominal values given in table 1. It should be mentioned however that in other HPHT C:B samples, similar measurements indicated that θ_D remained unaffected¹⁰³. As for the Bohr radius of the acceptor or donor impurity, it is given by $r_{\text{Bohr}} = \epsilon_r \hbar^2 / m^*_{\text{Bohr}} e^2$ within the hydrogenoid approximation parametrized by a specific effective mass m^*_{Bohr} . This radius provides^{104,105} an estimate for the critical impurity concentration n_{MIT} at the metal-insulator transition (MIT) according to Mott's prediction $r_{\text{Bohr}} n_{\text{MIT}}^{1/3} = 0.26$. This critical concentration has not been determined experimentally in all systems considered here, but is known to vary over a wide range, from below 10^{16} cm⁻³ in SrTiO₃ (a material possibly deviating from Mott's prediction) to $4 \cdot 10^{17}$ in Ge and $4 \cdot 10^{18}$ in¹⁰⁶ Si:B and $3 \cdot 5 \cdot 10^{20}$ cm⁻³ in^{27,40} C₍₁₁₁₎:B and C₍₁₀₀₎:B. The critical exponents around this 3d MIT have been determined in the latter two materials^{40,106}. Superconductivity was experimentally observed in these materials above a concentration n_{cmin} which was equal to or greater than n_{MIT} . The corresponding range of Fermi energies was estimated in table 1 by the

minimum Fermi temperature T_{Fmin} calculated within a one band free electron picture ($m^* = 1$). Its ratio to the Debye temperature is larger than 10 in the tellurides, but decreases when increasing the bandgap from 4 in germanium to about one in diamond, where the applicability of the adiabatic approximation and of the usual μ^* value might be questioned. As for $SrTiO_3$, it yields a much smaller ratio, on the order of 0.1, comparable to the situation of heavy-fermion superconductors, making a phonon-mediated pairing mechanism very unlikely⁹⁴ and calling for alternative models¹⁰⁷.

In addition, table 2 gathers some published examples^{11,39,41,55,62,67,73,91,94,95,101,108,109} of low temperature normal state transport parameters (Fermi vector k_F , low T conductivity, residual resistivity ratio RRR, mean free path L_{mfp} and Ioffe-Regel parameter) which depend on the doping level of these materials, in the relevant range of apparent free carrier concentrations n_H deduced from the Hall coefficient. The Fermi vector k_F was deduced from Shubnikov-de Haas oscillations (SnTe) or Nernst effect ($SrTiO_3$) measurements when available, and from free electron estimates for Ge, Si, SiC and diamond. Moreover, effective density of states relative masses m^*_{dos} of 2, 2.4 and 5 respectively in^{11,18} SnTe, in⁶ GeTe and in¹¹⁰ $SrTiO_3$ have been deduced from the Sommerfeld coefficient determined by specific heat measurements. More recently, similar studies yielded mass values of 1.2 and 1.7 in the cases of⁶¹ SiC:B and¹⁰² C:B. Angle-resolved photoemission spectroscopy (ARPES) measurements of superconducting diamond epilayers have shown that their electronic band structure could not be distinguished from that of epilayers doped below the critical concentration n_{cmin} , and that both were the same as that of the undoped crystal¹¹¹. They yielded a few 2d projections of the Fermi surface for epilayers grown along^{111,112} (111) and¹¹³ (100). As illustrated by fig. 2, in the latter case, under a polarized incident synchrotron beam, rotating the sample surface by 45° led to two partial projections on the Γ -X-K plane of the Brillouin zone corresponding respectively to the light and heavy hole subbands. Assuming that the boron concentration provides an estimate of the hole concentration n_h at the surface of this sample led to $k_F = 3.3 \text{ nm}^{-1}$, in rough agreement with the green contours shown in fig. 2, despite the fact that the heavy hole subbands do not lead to a spherical Fermi surface⁵³, a feature that might explain the Hall factor deviating from unity²⁷. Please note that in all experiments, the photoemission of unreconstructed heavily doped diamond surfaces could be analyzed as representative of the bulk of the crystal. Finally, since most free carrier concentrations given in tables 1 and 2 correspond to a plasmon frequency ω_p lying in the near or mid-infrared range, optical spectroscopies have also been applied to SnTe and¹⁰⁰ GeTe, as well as to heavily doped silicon¹¹⁴ and diamond¹¹⁵⁻¹¹⁷. A simple interpretation of the plasmon edge within the Drude model has been found sufficient in most cases to yield carrier concentrations and damping factors $\gamma = \tau^{-1}$ typical of overdamped dilute metals, with relaxation times τ in the 0.2 to 10 fs range fully compatible with the mean free path values given in table 2, generally lower than 1 nm in diamond, as confirmed by ARPES measurements¹¹¹.

In principle, a quantitative Kramers-Kronig analysis of the optical spectral response in the infrared energy range of lattice phonon or impurity-related vibrational modes should yield the Eliashberg function $\alpha^2F(\omega)$ describing the spectral variation of the electron-phonon coupling parameter. In practice, this challenge has been taken up in the case of diamond¹¹⁶, whereby the dominant contribution of optical phonons and the possible contribution of boron-related local modes predicted by ab initio numerical studies³⁰⁻³² were confirmed. The electron-phonon coupling was also illustrated by high resolution studies of photoemission phonon replicas of the Fermi edge in superconducting diamond¹¹⁸. Since the phonons involved in the coupling are expected to be softened, Raman studies

have been performed on superconducting silicon⁵⁵ and diamond¹¹⁹ and zone-center optical phonon frequencies have been extracted from first order Raman spectra, despite their polarization- and excitation energy- dependent Fano lineshape deformation¹²⁰. The resulting softening values, 3% at most^{55,119}, were significantly weaker than predicted by VCA calculations^{28,29}. Before being used for estimating the electron-phonon coupling strength for these particular phonons, they should moreover be corrected for doping-induced lattice strain¹¹⁹ which affects mostly the lattice parameter along the growth direction in the case of unrelaxed homepitaxial layers^{27,55,120,121}. More to the point, second order Raman¹²³ or inelastic X-ray^{124,125} scattering (IXS) allowed to detect lattice phonons away from the zone center and have confirmed that in the case of diamond the optical phonons were specifically affected in the region of the Brillouin zone occupied by free holes, as illustrated in fig. 2. However, even in that case, the softening (up to 5 %) was much weaker than predicted¹²⁴, while the broadening of the IXS phonon lines could not be explained without invoking additional disorder effects or even macroscopic heterogeneities in these very thick epilayers. Average coupling parameter λ values deduced from such measurements ranged from 0.2 to 0.4 depending on the derivation method³⁶, still too low for equation 1 to account for the T_c values measured on the same samples.

Another striking feature common to many of the materials listed in table 2 is the low value of the residual resistivity ratio $RRR = \sigma_{4K}/\sigma_{300K}$, around unity in GeTe, Ge, Si, and diamond. This stems from two opposite and slow variations of the normal state resistivity above and below a specific temperature at which the inelastic mean free path becomes of the order of the elastic scattering length, resulting in a broad and weak resistivity minimum. This temperature lies around 40 K in⁵⁵ Si:B, above²⁵ 150 K and up to^{22,39} 300 K in C:B. Below that temperature, the resistivity increases when the temperature decreases and goes through a peak before dropping sharply at the superconducting transition temperature T_c . In the range between T_c and about 40K, the conductivity extrapolates to a finite temperature according to the weak localization expression^{25,109,126}: $\sigma(T) = \sigma_0 + A_{ee}T^{1/2} + B_{ep}T$, where A_{ee} and B_{ep} refer respectively to interelectronic and electron-phonon interactions. As described below, the resistivity peak at low T is significantly enhanced in heavily doped nanocrystalline (nc-C:B) diamond films¹²⁷⁻¹²⁹ while the magnetoresistance changed sign^{128,130} with the field, as expected for a granular system. The weak localization observed in the granular disordered metal nc-C:B has been proposed to herald an unconventional superconductivity in that material through a spin-flip pairing mechanism^{127,131}. Although presenting also a dip at intermediate temperature⁹¹, the variations of the resistivity of PbTe:TI have been ascribed to a charge Kondo effect^{73,91}, i.e. a totally different effect which has important consequences for the interpretation of the superconductivity in this compound¹³². The last item listed in table 2 is the Ioffe-Regel parameter $k_F L_{mfp}$: below unity, localization sets in, and the quasi-classical approximation is no longer appropriate. From the data of table 2, this has been observed so far only in diamond doped slightly above n_{MIT} and grown^{39,40} along (100).

3d superconducting properties

As outlined in the historical survey opening this review, the bulk nature of the superconducting transition in these materials has been attested by measuring the heat capacity anomaly associated to carrier pairing below T_c in¹¹ SnTe, in⁶ GeTe and⁹¹ PbTe, as well as in¹⁰⁹ SrTiO₃, in⁶¹ SiC and¹⁰² diamond,

but not in germanium nor in silicon, while susceptibility data is lacking only in the case of germanium. However, the specific heat jump value was often significantly lower than expected from weak coupling BCS theory. In complement to the results mentioned in the introduction and to the $T_C(n_H)$ data plotted in fig. 1, we illustrate also in table 3 with a few examples the experimentally determined dependence on the nominal carrier concentration n_H of various additional parameters of the superconducting state of some semiconductors, such as the critical magnetic fields H_C or $H_{C2}(T=0)$ depending on the superconductor type, the coherence lengths ξ_{GL} and ξ_0 deduced from $H(T)$ phase diagrams through $\xi_{GL}^2 = \Phi_0/2\pi H_{C2}(0) = \xi_0 L_{mfp}$, the London penetration depth λ_L and the Ginzburg Landau parameter $\kappa_{GL} = \lambda_L/\xi_{GL}$. Whenever possible, the examples have been taken from the same references as those collected in table 2. According to these values, the only system clearly⁹⁴ in the clean limit was SrTiO₃, while the only apparent type I superconductors were 3C-SiC:B and 6H-SiC:B. The fact that most of the materials under consideration are type II superconductors in the dirty limit fulfills early predictions³ based on the long penetration depth and short mean free path expected for such systems.

Please note that in the case of diamond, a distinction was made between a bulk (and possibly polycrystalline) HPHT sample¹⁰², and single crystal epilayers grown by MPCVD along³⁹ (100) or along¹¹⁶ (111), respectively dubbed $C_{(100)}$:B and $C_{(111)}$:B. As illustrated both by fig. 1 and table 3, for a given apparent carrier density n_H , the T_C values are much higher in $C_{(111)}$:B than in $C_{(100)}$:B. This has been tentatively attributed to a better ordering of the substitutional boron impurities¹³³ when the diamond lattice grows along (111), to a higher substitutional to interstitial (or paired substitutional¹³⁴) incorporation ratio for (111)-oriented growth, and finally to a favorable tetragonal strain state²⁷ of the (111)-oriented epilayers when compared to the isotropic dislocation-rich¹³⁵ relaxed state²⁷ of the (100)-oriented epilayers grown in the same reactor. However, the opposite situation, where dislocations appear in (111)-oriented epilayers at a lower boron concentration than in layers grown along (100), has also been reported¹³⁶. Anyway, a positive (tensile) strain coming from substitution by a “larger” impurity is expected to enhance T_C in group IV superconducting semiconductors^{21,58}, in agreement with experimental^{22,137} and theoretical³⁸ results showing that in diamond the hydrostatic pressure coefficient of T_C is negative. It is also worth noting that for strained epilayers, the band splitting of the heavy and light hole bands at Γ induced by the tetragonal strain is expected to modify the shape of the Fermi surface, and thus to affect both the Hall factor and the critical temperature. This strain has opposite signs in Si:B and C:B.

Since the pioneering tunnel spectroscopy studies¹⁶ of GeTe, the superconducting gap of energy seen by the quasiparticles around the Fermi level has been investigated in^{96,138} SrTiO₃, in¹³⁹ $C_{(100)}$:B, in¹⁴⁰ C:B, in^{141,142} $C_{(111)}$:B and¹⁴³ Si:B. Thanks to the development of ultra-low T scanning tunnel microscopy (STM) and spectroscopy (STS), the latter studies have provided local maps of the local variations of the coherence peak intensity and of the superconducting gap^{139,142,143}. In the case of $C_{(100)}$:B surfaces, vortex images and some evidence for localized gap states were obtained, the latter remaining a puzzle^{63,139}. The temperature dependence of the local pair binding energy Δ deduced from the excitation gap has been also studied in diamond and silicon, and found in excellent agreement with a *s*-wave BCS superconductivity with a BCS ratio $\Delta/k_B T_C = 1.75$ both for a C:B plate¹⁴⁰ and $C_{(100)}$:B epilayers^{123,139}, while a 20% dispersion about the BCS value was observed¹⁴³ on Si:B. Two coupled gaps had been detected earlier in SrTiO₃, with a BCS ratio close to 1.76 for the larger one⁹⁶, as well as a possible signature of the soft phonon mode at 1.9 meV involved in the low temperature structural

transition¹³⁸. Moreover, optical methods have yielded superconducting gap values for $C_{(111)}:B$, infrared and THz spectroscopies¹¹⁶ appearing to be better suited than high resolution photoemission¹⁰⁹ for the purpose. The resulting Δ values were plotted in fig. 3 as a function of the critical temperature T_C , and found to be fully compatible with a conventional weak coupling BCS description. Finally, a crucial test of the nature of the pairing attractive interaction is of course the isotope atomic mass (M) effect on T_C , usually quantified by the exponent $\beta = -d\text{Log}T_C/d\text{Log}(M)$. $\beta = 0.5$ is considered the hallmark of a phonon-mediated BCS mechanism, although β may take lower values because of Coulomb repulsion effects. Specific heat measurements¹⁰³ of isotopically substituted HPHT C:B have yielded a much higher β exponent of 1.8, while similar studies of the resistive transition led to $\beta = 1.4 \pm 0.4$ for other HPHT C:B samples¹⁴⁴, and to isotope exponent values of 0.6, 1.1 and 1.8 in $C_{(100)}:B$ epilayers¹⁴⁵. If the isotopic mass effect seems thus to be established in the sole case of diamond, confirming the crucial role of electron-phonon coupling in this material, its magnitude remains to be explained. Frequent Cooper pair breaking¹⁴⁶, possibly triggered by the local nature of some of the coupling phonons¹⁴⁵, has been considered as a plausible origin for this phenomenon¹⁴⁴.

Applying the BCS model in the dirty limit within a one-band free electron picture, the slope at T_C of the $H(T)$ phase diagram (at the boundary between the vortex phase and the normal phase) may also be used to estimate the Ioffe-Regel parameter ($k_F L_{mfp}$). The values of -1 T/K for diamond, -0.2 T/K in silicon, and -0.02 to -0.1 T/K in GeTe lead to Ioffe-Regel parameter values in good agreement with those deduced from normal state transport measurements (table 2). Such a successful consistency check between superconducting and normal state properties brings further support to a weak coupling mechanism being at work in these three materials. No such agreement was found in the other materials, the mixed state estimate of $k_F L_{mfp}$ being significantly smaller than the normal state estimate the case of germanium, while the opposite was true for SnTe. Another point was the relevance of the proximity of a carrier concentration-induced MIT to understand the superconducting properties of diamond close to this transition. Comparison to the parent silicon system showed that, in the latter, superconductivity was not any simpler to understand in detail⁴¹, despite the absence of any MIT in the doping range of interest.

Low dimensionality issues and devices

The fact that the critical doping level for the MIT and for the onset of superconductivity n_{cmin} coincide in diamond has also given some impetus to studies aiming at controlling and studying a superconductor to insulator transition (SIT) in this system. As emphasized by theoretical studies promoting either a “fermionic”¹⁴⁵ or a “bosonic”¹⁴⁸ model for this transition, the SIT may be investigated experimentally by changing not only the carrier concentration but also the disorder and the thickness of the epitaxial film. Thickness effects on T_C have been observed below about 200 nm and down to 5nm, but they appear similar for both epitaxial films doped far above¹³⁵ n_{MIT} or much closer¹⁴⁹ to the MIT, so that fundamental aspects of the SIT are ruled out from their interpretation. Once normalized to the T_C “bulk” value, the observed variations may be in both cases explained by a simple geometrical effect related to a weaker order parameter at the surface¹⁵⁰⁻¹, but yield a critical thickness value of 25 nm, much longer than the Thomas Fermi screening length supposed to be relevant in that case. This open question deserves further attention, at least as long as the coincidence of n_{cmin} with n_{MIT} is not disproved. More generally, controlled ways to change the effective disorder in these superconducting semiconductors should be sought.

Beside film thickness reduction or disorder variations, another way to induce effective dimensionality effects at a less intrinsic level is to introduce grains and to vary their size relative to the film thickness and to other physically relevant lengths. This has been performed in boron doped nanocrystalline diamond : for grain sizes smaller than the thickness and comparable to the coherence length¹⁵², or comparable to the thickness^{81,153}, the granularity of the system takes over and percolation effects are expected. The role of the grain boundaries and intragranular metallic transport parameters, quite obvious in the normal state^{130,154,155} takes another twist below T_C , with an influence of the intergranular Josephson coupling, as well as that of the heterogeneity of the local superconductivity among the grains and even within the same grain, which has been assessed by scanning tunnel microscopy^{77,78}. For micrometer-sized grains, the enhanced weak localization effects may be hidden at low temperatures by a sharp and pronounced “bosonic” resistivity peak occurring at a temperature close to the onset of superconductivity¹²⁹. Such granularity-induced and percolation effects do not seem to have triggered the same interest in the other superconducting semiconductors.

Patterning of micro- or nanocrystalline superconducting diamond films into wires less than 100 nm-wide preserved their superconducting properties¹⁵⁶ up to 1 K and 1T. Such e-beam patterned wires and loops, including a thinner region inducing a weak link, were used to make superconducting quantum interference devices (SQUID) working at magnetic fields reaching¹⁵⁷ 4T. Similar films grown on a sacrificial silicon oxide were also patterned into double clamped suspended beams. These micromechanical resonators were driven and read out in the superconducting state at MHz frequencies¹⁵⁸. Future combinations of smaller oscillators with the SQUID should soon establish the potential of superconducting nanocrystalline diamond for dissipation-free quantum opto-mechanics. Finally, in the case of diamond, the “natural” Josephson junctions occurring at grain boundaries and the “artificial” weak junctions resulting from thinning nanocrystalline wires have found¹⁵⁹ a single crystal counterpart in vertical SNS weak-link Josephson junctions grown epitaxially along (111). When the thickness of the normal state diamond of such structures was made much larger than the coherence length, a proximity effect could be observed. Moreover, Shapiro steps were detected under microwave irradiation¹⁶⁰. This result illustrated recent improvements in the sharpness of the doping transitions upon epitaxial MPCVD growth^{149,161} at the normal-superconductor interface, and opened the way for the fabrication of hybrid systems involving either optical color centers or mechanical oscillators, or both. Be it for the above mentioned quantum-limited sensing, or for quantum data processing using more elaborate devices such as Josephson field effect transistors, the ability to grow homoepitaxial Josephson junctions should improve significantly the transparency of the normal-superconductor interfaces. Similar strategies and more audacious qubits schemes have been proposed in the case of silicon^{64,162}, but they have not yet materialized.

As mentioned at the end of the introduction (and in the contribution by Triscone & Gabay), low dimensionality effects quite different from the above have been demonstrated for the interface of SrTiO₃ with another perovskite oxide where the 2d electron gas extending a few nm within SrTiO₃ from the interface was shown to have a superconducting ground state below⁹⁷ 0.2 K or⁹⁸ 0.3 K. A similar 2d gas was generated at the pristine SrTiO₃ single crystal surface by using the electrical double layer gate created in an organic electrolyte. When sheet carrier densities of the order of 10^{14} cm⁻² were obtained in this way¹⁶³, an electric-field-induced 2d superconducting state appeared below 0.4 K, a T_C value comparable to the values given in fig. 1 for Nb-doped SrTiO₃.

Finally, for the sake of completeness, it should be mentioned that very high T_c values (145 K) have been reported¹⁶⁴ for a specific type of low-dimensional silicon pyramidal sandwich nanostructures self-assembled on top of n-type (100)-oriented wafers, whereby ultra-narrow p-type silicon quantum wells were confined by heavily boron-doped superconducting delta “barriers”¹⁶⁵. These amazing results, which still await an independent confirmation, have been attributed to the transport of small hole bipolarons resulting from the presence of negative-U centers associated to the boron impurities¹⁶⁵⁻¹⁶⁷. More generally, it must be recognized that at this moment, and similarly to the cases of germanium and silicon carbide, superconductivity studies of boron doped silicon lack independent confirmations by other groups.

Summarizing remarks

In summary, most of the experimental data currently available about single crystal (or large grain polycrystalline) superconducting semiconductors hint at a conventional pairing mechanism, except in the case of PbTe and SrTiO₃, the latter being the only electron-doped system in the whole family. However, quantitative agreement with simple models was not yet demonstrated over a wide doping range for any of the “conventional” systems, while additional evidence is still required to assess the status and potential of germanium and silicon carbide. Except for one very recent and preliminary report¹⁶⁸, the occurrence of critical temperatures significantly higher than 10 K has not been verified, despite promising theoretical predictions for sp³ carbon clathrates²¹ and cubic boron-carbon compounds¹⁶⁹⁻¹⁷⁰.

Diamond clearly stands out as the most studied and archetypical group IV superconducting semiconductor⁶⁴. Ten years after its discovery, this material even shows some promise for superconducting quantum devices. In the near future, much older players with less conventional superconducting properties, PbTe and SrTiO₃, and a younger one with an impressive technological maturity, silicon, will certainly provide additional opportunities for testing new and old theories, as well as futuristic hybrid devices.

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Tables

	Low T crystal phase	E_G (eV)	θ_D (K)	ϵ_r ($/\epsilon_0$)	Dop.	r_{Bohr} (nm)	n_{cmin} (nm^{-3})	m^*T_{Fmin} (K)
SnTe	rocksalt	0.19-0.3	140	1200	V_{Sn}	230	0.25 ⁽⁹⁸⁾	1680
GeTe	fcr distorted	0.1-0.2	170	36	V_{Ge}	2	0.9 ⁽⁹⁸⁾	3950
PbTe	rocksalt	0.35	140	1000	Tl, In	250	0.05	570
SrTiO ₃ n-type	Tetragonal (Perovskite)	3.1	450	20000	V_O Nb	600	0.0005 ⁽⁹³⁾	24 ⁽⁹³⁾
Ge	diamond	0.66	360	16	Ga	5	0.2 ⁽⁶⁷⁾	1450
Si	diamond	1.1	640	12	B	2	0.3 ⁽⁴¹⁾	1890
3C-SiC	Zincblende	2.4	1270	9.7	B, Al	1	0.4 ⁽⁶²⁾	2300
6H-SiC	hexagonal	3	1200	9.6-10	B	1	0.25 ⁽⁵⁷⁾	1680
C	diamond	5.5	2000	5.7	B	0.4	0.4 ⁽²⁷⁾	2300

Table 1: Normal state general properties of some superconducting semiconductors. The bandgap width E_G , the Debye temperature θ_D and the relative permittivity at low frequency ϵ_r are those of the undoped material. The minimum carrier concentration for which superconductivity has been reported (n_{cmin}) has been measured by Hall effect, except for silicon (*italics*).

	Dopant	n_H (nm^{-3})	k_F (nm^{-1})	σ_{4K} (Ωcm) ⁻¹	RRR	L_{mfp} (nm)	$k_F L_{mfp}$	reference
SnTe	V_{Sn}	1	0.63	2.5×10^4	-	39	25	Ref. 11
SnTe	V_{Sn}	2	0.78	2×10^4	-	17	13	Ref. 11
GeTe	V_{Ge}	0.86	2.9	2×10^4	-	30	87	Ref. 11
GeTe	V_{Ge}	0.18	1.7	1.3×10^4	1.3	40	68	Ref. 100
PbTe	Tl	0.05	1.1	3×10^3		14	15	Refs 73 & 91
PbTe	Tl	0.09	1.4	10^3		3.2	4.5	Refs 73 & 91
SrTiO ₃	V_O	5.5×10^{-4}	0.24	10^3	2700	140	33	Refs 94 & 107
SrTiO ₃	V_O	4×10^{-3}	0.37	4×10^3	480	140	52	Refs 94 & 107
SrTiO ₃	V_O	0.027	0.51	1.5×10^4	490	120	61	Refs 94 & 107
SrTiO ₃	Nb	0.16	0.56	10^5	120	37	21	Refs 94 & 107
Ge	Ga	0.53	2.5	5×10^3	1	7	18	Ref. 67
Si	B	5	5.3	8×10^3	1.25	1.3	6.9	Ref. 55
Si	B	<i>0.55</i>	2.5	8×10^3	1.2	3.2	8.1	Ref. 41
Si	B	<i>1.4</i>	3.5	1.6×10^4	1.2	3.4	12	Ref. 41
Si	B	<i>2.8</i>	4.4	1.4×10^4	1.3	2	8.7	Ref. 41
3C-SiC	B	1.9	3.8	1.6×10^4	11	14	53	Ref. 62
3C-SiC	Al	0.7	2.8	1.3×10^3	5.3	2.2	6.2	Ref. 62
6H-SiC	B	0.25	2.3	8×10^2	4.7	3	6.9	Ref. 62
C	B	1.8	3.8	4×10^2	0.9	0.34	1.3	Ref. 101
C ₍₁₀₀₎	B	0.56	2.6	70	2	0.23	0.5	Ref. 39
C ₍₁₀₀₎	B	1.3	3.3	4×10^2	1.2	0.5	1.8	Ref. 39
C ₍₁₁₁₎	B	2.1	4	5×10^2	-	0.6	2.4	Ref. 108
C ₍₁₁₁₎	B	13	7.3	1.4×10^3	0.9	0.5	3.8	Ref. 108

Table 2: Normal state properties of some superconducting semiconductors for various doping-induced free carrier concentrations n_H deduced from the Hall coefficient, except in the case of silicon where boron concentrations (in italics) have been used. The residual resistivity ratio RRR was defined as $\rho_{300K}/\rho_{4K} = \sigma_{4K}/\sigma_{300K}$. The mean free path L_{mfp} was generally deduced from Hall mobility values within the free electron picture, and yielded the Ioffe-Regel parameter $k_F L_{mfp}$.

	n_H (nm^{-3})	T_C (K)	$H_{C2}(0)$ or H_C (Tesla)	ξ_0 (nm)	ξ_{GL} (nm)	λ_L (nm)	κ_{GL} (nm)	type
$\text{Sn}_{1-\delta}\text{Te}$	1	0.065	5×10^{-4}	6200	490	55	1.4	II, dirty ¹¹
$\text{Sn}_{1-\delta}\text{Te}$	2	0.21	8.5×10^{-4}	2400	230	63	3.7	II, dirty ¹¹
$\text{Ge}_{1-\delta}\text{Te}$	0.86	0.08	1.6×10^{-3}	3900	340	75	2.5	II, dirty ¹¹
$\text{Ge}_{1-\delta}\text{Te}$	1.5	0.31	0.038	1200	140	110	6.8	II, dirty ¹¹
PbTe:TI	0.09	1.15	0.39	260	29	160	5	II, dirty ⁷³
PbTe:TI	0.11	1.4	0.6	300	24	150	8	II, dirty ⁷³
$\text{SrTiO}_{3-\delta}$	5.5×10^{-4}	0.09	0.05		100	5800		II, clean ⁹⁴
$\text{SrTiO}_{3-\delta}$	4×10^{-3}	0.18	0.11		56	2200		II, clean ⁹⁴
$\text{SrTiO}_{3-\delta}$	0.032	0.34	0.15		44	760		II, clean ⁹⁴
$\text{SrTiO}_3:\text{Nb}$	0.16	0.43	0.22		37	340		II, clean ⁹⁴
Ge:Ga	0.53	0.5	0.5	100	26	>100	>14	II, dirty ⁶⁷
Si:B	4	0.58	0.11	1000	50	60	20	II, dirty ¹¹⁸
3C-SiC:B	1.9	1.5	0.013	360	70	130	0.32	I, dirty ⁶²
3C-SiC:Al	0.7	1.5	0.037	150	18	210	1.8	II, dirty ⁶²
6H-SiC:B	0.25	1.4	0.012	200	24	360	0.31	I, dirty ⁶²
C:B	1.8	4.5	4.2	240	9	160	18	II, dirty ⁹⁹
$\text{C}_{(100)}:\text{B}$	1.3	0.38	0.37	-	30	225	7.6	II, dirty ³⁹
$\text{C}_{(100)}:\text{B}$	2.1	2.5	2.44	120	12	154	13	II, dirty ³⁹
$\text{C}_{(111)}:\text{B}$	6	8	7	95	6.9	72	10	II, dirty ¹¹³

Table 3 : Carrier density-dependent superconductivity parameters for various degenerate semiconductors: critical temperatures T_C and magnetic fields H_C (clean limit) or $H_{C2}(T=0)$, coherence lengths ξ_0 and ξ_{GL} , London penetration length λ_L and Ginzburg-Landau coefficient κ_{GL} , as well the type of superconductivity.

Figure captions :

Figure 1 : Nominal free carrier dependence of the critical temperature T_c for the superconductive transition of various heavily doped degenerate semiconductors : B-doped diamond grown along^{27,39} (100) or²⁷ (111), B-doped silicon for two different epitaxial film thicknesses⁴¹, Ga-doped germanium⁶⁷⁻⁶⁹, B-doped⁶² or Al-doped⁵⁷ silicon carbide, self-doped or Nb-doped strontium titanate^{15,94}, Tl-doped lead telluride⁷³, self-doped selenium^{8,9} and germanium⁵ tellurides. The lines correspond to T_c estimates for three μ^ values, as deduced from equation 1 for $\theta_D = 640$ K, λ being evaluated by ab-initio supercell calculations⁴¹.*

Figure 2 : Color-coded intensity (bottom) and spectral shift (top) maps onto the X-T-K principal plane of the Brillouin zone of a boron doped diamond homoepitaxial layer(C:B), deduced respectively from (bottom) polarized Angle Resolved Photoemission Spectroscopy¹¹³(ARPES) and from (top) Inelastic X-ray Spectroscopy¹²⁵ (IXS) measurements performed at SOLEIL (ARPES) and ESRF (IXS) synchrotron facilities. Different ARPES configurations allow to distinguish the contributions of the heavy hole (hh) and light hole (lh) subbands. The spectral shift measured by IXS is that of the optical phonons of C:B with respect to those of the undoped crystal.

Figure 3 : Experimentally determined critical temperatures T_c (either local or macroscopic) as a function of the pair binding energy(half-gap) Δ measured by tunnel spectroscopy at very low temperatures for diamond¹³⁹⁻¹⁴¹, silicon¹⁴³, germanium telluride¹⁶ and strontium titanate^{97,138}. The straight line corresponds to the weak coupling BCS ratio.

Figure 1

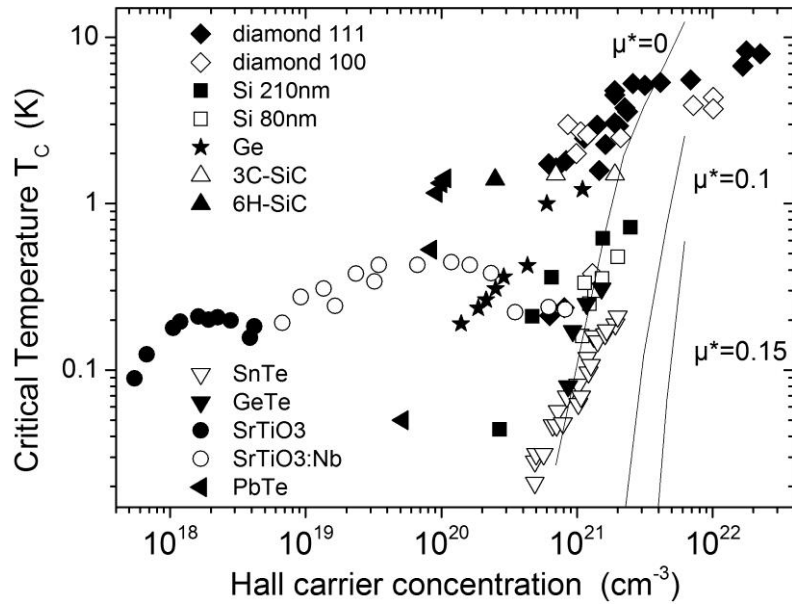


Figure 2

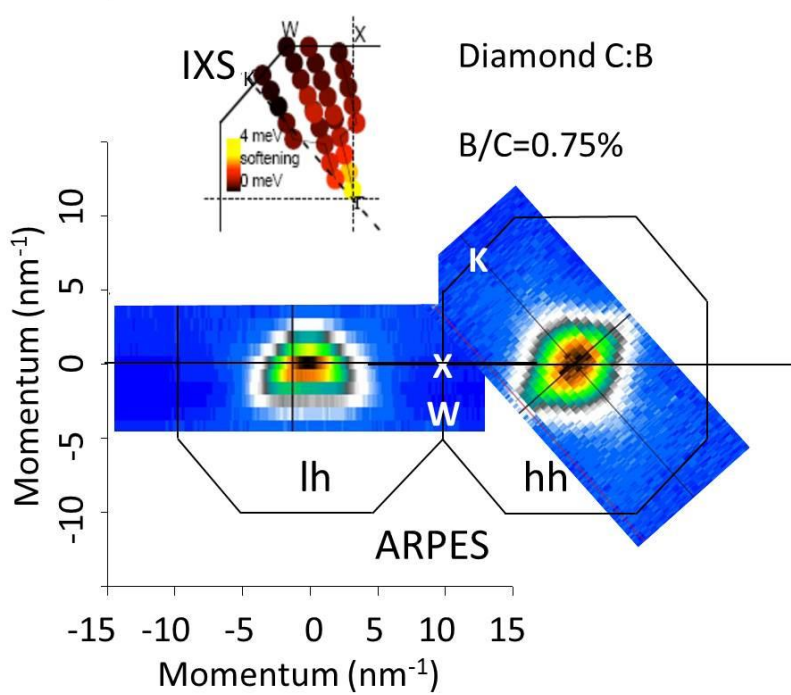


Figure 3

