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Waterpixels

Vaïa Machairas, Matthieu Faessel, David Cárdenas-Peña, Théodore Chabardes, Thomas Walter, and Etienne Decencière

Abstract-Many approaches for image segmentation rely on a first low-level segmentation step, where an image is partitioned 2 into homogeneous regions with enforced regularity and adherence 3 to object boundaries. Methods to generate these superpixels have 4 gained substantial interest in the last few years, but only a few 5 have made it into applications in practice, in particular because the requirements on the processing time are essential but are not met by most of them. Here, we propose waterpixels as a general 8 strategy for generating superpixels which relies on the marker controlled watershed transformation. We introduce a spatially 10 regularized gradient to achieve a tunable tradeoff between the 11 superpixel regularity and the adherence to object boundaries. 12 The complexity of the resulting methods is linear with respect 13 to the number of image pixels. We quantitatively evaluate our 14 approach on the Berkeley segmentation database and compare 15 it against the state-of-the-art. 16

Index Terms-Superpixels, watershed, segmentation. 17

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AO:3

I. INTRODUCTION

TUPERPIXELS (SP) are regions resulting from 19 a low-level segmentation of an image and are typically 20 used as primitives for further analysis such as detection, 21 segmentation, and classification of objects (see Figure 1 22 for an illustration). The underlying idea is that this first 23 low-level partition alleviates the computational complexity of 24 the following processing steps and improves their robustness, 25 as not single pixel values but pixel set features can be used. 26 27

- Superpixels should have the following properties:
- 1) homogeneity: pixels of a given SP should present 28 similar colors or gray levels; 29

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Fig. 1. Superpixels illustration. The original image comes from the Berkeley segmentation database. (a) Original image. (b) Waterpixels.

- 2) connected partition: each SP is made of a single connected component and the SPs constitute a partition of the image;
- 3) adherence to object boundaries: object boundaries should be included in SP boundaries;
- 4) regularity: SPs should form a regular pattern on the image. This property is often desirable as it makes the SP more convenient to use for subsequent analysis steps.

The requirements on regularity and boundary adherence are to a certain extent oppositional, and a good solution typically aims at finding a compromise between these two requirements.

In addition to these requirements on superpixel quality, computational efficiency is an absolutely essential aspect, as the partition into superpixels is typically only the first step of an often complex and potentially time consuming workflow. Methods of linear complexity are consequently of particular interest.

We therefore hypothesized that the Watershed transformation [1], [2] should be an interesting candidate for superpixel generation, as it has been shown to achieve state-of-the-art performance in many segmentation problems, it is non-parametric, and there exist linear-complexity algorithms to compute it, as well as efficient implementations [3], [4]. The only often cited drawback, oversegmentation, does not seem to be problematic for superpixel generation, as long as we can control the degree of oversegmentation (number of superpixels), and the regularity of the resulting partition.

Given these considerations, we propose a strategy for 58 applying the watershed transform to superpixel generation, 59 where we use a spatially regularized gradient to achieve a 60 tunable trade-off between superpixel regularity and adherence 61 to object boundaries. We quantitatively evaluate our method 62 on the Berkeley segmentation database and show that we 63 outperform the best linear-time state-of-the art method: Simple 64 Linear Iterative Clustering (SLIC) [5]. We call the resulting 65 superpixels "waterpixels." 66

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TABLE I RECAP CHART OF EXISTING METHODS TO COMPUTE REGULAR SUPERPIXELS (*n* IS THE NUMBER OF PIXELS IN THE IMAGE; *i* IS THE NUMBER OF ITERATIONS REQUIRED; N THE NUMBER OF SUPERPIXELS). "WP" CORRESPONDS TO OUR METHOD, CALLED "WATERPIXELS"

Method	[11]	[12]	[13]	[5]	WP
Generation type	1	2	1 (iterated)	2	1
(see section II-B)					
Seed type (see	A	C	C	C	B
section II-A)					
Control on num-	yes	yes	yes	no	yes
ber of SPs					
Control on regu-	no	yes	no	yes	yes
larity					
Post-processing	no	no	no	no	yes
free					
Complexity	O(n)	$O(in\sqrt{N})$	O(in)	O(n)	O(n)

This paper is an extended version of [6]. It proposes a 67 more general approach (elaborating a whole family of water-68 pixels generation methods), with a more thorough validation 69 and improved results with regard to the trade-off between 70 boundary adherence and regularity, as well as computation 71 time. Moreover, we have developed and made available a fast 72 implementation of waterpixels. 73

II. RELATED WORK

Low-level segmentations have been used for a long time as 75 first step towards segmentation [7], [8]. The term superpixel 76 was coined much later [9], albeit in a more constrained frame-77 work. This approach has raised increasing interest since then. 78 Various methods exist to compute SPs, most of them based on 79 graphs [10], geometrical flows [11] or k-means [5]. We will 80 focus on linear complexity methods generating regular SPs. 81

Methods for SP generation are all based on two steps: 82 an initialization step where either seeds or a starting par-83 tition are defined and a (potentially iterative) assignment 84 step, where each pixel is assigned to one superpixel, starting 85 from the initialization. In the next section, we are going to 86 review previously published approaches for SP generation with 87 respect to these aspects and compare them regarding various 88 performance criteria. We limit the presentation of existing 89 methods to those with linear complexity. 90

A. Choosing the Seeds 91

In the first step, a set of seeds is chosen, which are typically 92 spaced regularly over the image plane and which can be either 93 regions or single pixels: 94

- Type A seeds are independent of the image content. These 95 are typically the cells or the centers of a regular grid. 96
- Type B seeds depend on the content of the image 97 (compromise between a regular cover of the image plane 98 and an adaption to the contour). 90
- Type C seeds are initially image independent, then they 100 are iteratively refined to take into account the image 101 contents. 102

If the seed does not depend on the image, an iterative 103 refinement is usually preferable, and therefore more time 104

is spent on the computation of the SP. Type B methods 105 may spend more time on finding appropriate seeds, but can 106 therefore afford not to iterate the SP generation. 107

B. Building Superpixels From Seeds

In the second step, the partition into superpixels is built 109 from the seeds. Among the methods with linear complexity, 110 there are two main strategies for this:

Shortest Path Methods (Type 1) [11], [13]: these methods 112 are based on region growing: they start from a set of seeds 113 (points or regions) and successively extend them by incorporating pixels in their neighborhood according to a usually image dependent cost function until every pixel of the image plane has been assigned to exactly one superpixel. This process 117 may or may not be iterated. 118

Shortest Distance Methods (Type 2) [5], [12]: these are 119 iterative procedures inspired by the field of unsupervised 120 learning, where at each iteration step, seeds (such as centroids) 121 are calculated from the previous partition and pixels are then 122 re-assigned to the closest seed (like for example the k-means 123 approach). 124

Even though methods inspired by general clustering meth-125 ods (type 2) seem appealing at first sight, in particular when 126 they globally optimize a cost function, this class of methods 127 does not guarantee connectivity of the superpixels for arbi-128 trary choices of the pixel-seed distance (see [5], [12]). For 129 instance, the distance metric proposed in [5] (a combination 130 of Euclidean and grey level distance), leads to non-connected 131 superpixels, which is undesirable. To solve this issue, a post-132 processing step is necessary, consisting either in relabeling the 133 image so that every connected component has its own label 134 (see [12]), leading to a more irregular distribution of SP sizes 135 and shapes, or in reassigning isolated regions to the closest and 136 large enough Superpixel, as in [5], leading to non-optimality 137 of the solution and an unpredictable number of superpixels. 138 In addition, such postprocessing increases the computational 139 cost and can turn out to be the most time-consuming step when 140 the image contains numerous small objects/details compared 141 to the size of the Superpixel. 142

On the contrary, methods based on region growing (type 1) 143 inherently implement a "path-type" distance, where the dis-144 tance between two pixels does not only depend on value 145 and position of the pixels themselves, but on values and 146 positions along the path connecting them. Type 1 methods 147 imply connected superpixel regions, for which the number of 148 superpixels is exactly the number of seeds.

C. Other Properties

It is generally accepted that a good superpixel-generation 151 method should provide to the user total control over the num-152 ber of resulting Superpixels. While this property is achieved 153 by [11]-[14], some only reach approximatively this num-154 ber because of post-processing (either by splitting too big 155 superpixels, or removing small isolated superpixels as in [5]). 156 Another parameter is the control on superpixels regularity in 157 the trade-off between regularity and adherence to contours. 158 Only [5] and [12] enable the user to weight the importance 159

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of regularity compared to boundary adherence, so it can beadapted to the application.

As far as performance is concerned, one of the main 162 criteria is undoubtedly the complexity that the method 163 requires. Indeed, for Superpixels to be used as primitives for 164 further analysis such as classification, their computation should 165 neither take too long nor too much memory. This is the reason 166 why we focus on linear complexity methods. Among them, 167 SLIC appears to offer the best performance with regards to the 168 trade-off between adherence to boundaries and regularity [5]. 169 Moreover, since its recent inception, this method has become 170 very popular in the computer vision community. We will 171 therefore use it as reference for the quantitative evaluation of 172 our method. 173

174 D. Superpixels and Watershed

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In principle, the watershed transformation (see [15] for a review) is well suited for SP generation:

- 177 1) It gives a good adherence to object boundaries when
 178 computed on the image gradient.
- 179
 2) It allows to control the number and spatial arrangement
 180
 of the resulting regions through the choice of markers.
 - 3) The connectivity of resulting regions is guaranteed and no postprocessing is required.
- 4) It offers linear complexity with the number of pixels inthe image.

Indeed, it has been used to produce low-level segmentations
in several applications, including computation intensive
3D applications [16], [17], in particular when shape regularity
of the elementary regions was not required.

Previous publications claimed that the watershed transformation does not allow for the generation of spatially regular SP [5], [11]. Recently, we and others [6], [18] have shown that in principle the watershed transformation can be applied to SP generation.

Here, we introduce waterpixels, a family of methods based
 on the watershed transformation to compute superpixels.

III. WATERPIXELS

As most watershed-based segmentation methods, waterpixels are based on two steps: the definition of markers, from which the flooding starts, and the definition of a gradient (the image to be flooded). We propose to design these steps in such a way that regularity is encouraged.

A waterpixel-generation method is characterized by the following steps:

- 1) Computation of the gradient of the image;
- 205 2) Definition of regular cells on the image, centered on the vertices of a regular grid;
- 3) Selection of one marker per cell;
- 4) Spatial regularization of the gradient with the help of a distance function;
- 5) Application of the watershed transformation on the
 regularized gradient defined in step 4 from the markers
 defined in step 2.

These steps are illustrated in figure 2 and developed in the next paragraphs.

A. Gradient and Cells Definition

Let $f: D \to V$ be an image, where D is a rectangular subset of Z^2 , and V a set of values, typically $\{0, \ldots, 255\}$ 217 when f is a grey level image, or $\{0, \ldots, 255\}^3$ for color images. 219

The first step consists in computing the gradient image g 220 of the image f. The choice of the gradient operator depends 221 on the image type, *e.g.* for grey level images we might 222 choose a morphological gradient. This gradient will be used 223 to choose the seeds (section III-B) and to build the regularised 224 gradient (III-C). 225

For the definition of cells, we first choose a set of *N* points $\{o_i\}_{1 \le i \le N}$ in *D*, called *cell centers*, so that they are placed on the vertices of a regular grid (a square or hexagonal one for example). Given a distance *d* on *D*, we denote by σ the grid step, *i.e.* the distance between closest grid points. 230

A Voronoi tesselation allows to associate to each o_i a 231 Voronoi cell . For each such cell, a homothety centered on o_i 232 with factor ρ (0 < $\rho \le 1$) leads to the computation of the 233 final cell C_i . This last step allows for the creation of a margin 234 between neighbouring cells, in order to avoid the selection of 235 markers too close from each other. 236

B. Selection of the Markers

As each cell is meant to correspond to the generation of a unique waterpixel, our method, through the choice of one marker per cell, offers total control over the number of SP, with a strong impact on their size and shape if desired. 238

First, we compute the minima of the gradient *g*. Each minimum is a connected component, composed of one or more pixels. These minima are truncated along the grid, i.e. pixels which fall on the margins between cells are removed. 242

Second, every cell of the grid serves to define a region of interest in the gradient image. The content of g in this very region is then analyzed to select a unique marker, as explained in the next paragraph.

For each cell, the corresponding marker is chosen among the minima of g which are present in this very cell.

If several minima are present, then the one with the highest surface extinction value [19] is used. We have found surface extinction values to give the best performances compared with volume and dynamic extinction values (data not shown). 253 254 255 255 255 256

It may happen that there is no minimum in a cell. This 256 is an uncommon situation in natural images. In such cases, 257 we must add a marker for the cell which is not a minimum 258 of g, in order to keep regularity. One solution could be to 259 simply choose the center of the cell; however, if this point 260 falls on a local maximum of the gradient g, the resulting 261 SP may coincide with the maximum region and therefore be 262 small in size (leading to a larger variability in size of the SP). 263 We propose instead to take, as marker, the flat zone with 264 minimum value of the gradient inside this very cell. 265

In both cases (i.e. either there exists at least one minimum in the cell or there is not), the selected marker has to be composed of a unique connected component to ensure regularity and connectivity of the resulting superpixel. However, it might not be the case, respectively if more than one minimum 270

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Fig. 2. Illustration of waterpixels generation: (a): original image; (b) corresponding Lab gradient; (c): selected markers within the regular grid of hexagonal cells (step $\sigma = 40$ pixels); (d): distance function to markers; (g): distance function to cell centers; (e) and (h): spatially regularized gradient respectively with distance functions to selected markers (d) and to cell centers (g); (f) and (i): Resulting waterpixels obtained by respectively applying the watershed transformation to (e) and (h), with markers (c).

have the same highest extinction value, or if more than one
flat zone present the same lowest gradient value in the cell.
Therefore, an additional step enables to keep only one of
the connected components if there is more than one potential
"best" candidate.

The set of resulting markers is denoted $\{M_i\}_{1 \ge i \ge N}$, $M_i \subset D$. The result of the marker selection procedure is illustrated in Figure 2.c.

279 C. Spatial Regularization of the Gradient and Watershed

The selection of markers has enforced the pertinence of future superpixel-boundaries but also the regularity of their pattern (by imposing only one marker per cell). In this paragraph, we design a spatially regularized gradient in order to further compromise between boundary adherence and regularity.

Let $Q = \{q_i\}_{1 \le i \le N}$ be a set of N connected components of the image f. For all $p \in D$, we can define a distance function d_Q with respect to Q as follows:

$$\forall p \in D, \ d_Q(p) = \frac{2}{\sigma} \min_{i \in [1,N]} d(p,q_i) \tag{1}$$

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where σ is the grid step defined in the previous section. The normalization by σ is introduced to make the regularization independent from the chosen SP size.

We have studied two possible choices of the q_i . The first one is to choose them equal to the markers: $q_i = M_i$. Resulting waterpixels are called *m*-waterpixels. The second one consists in setting them at the cell centers: $q_i = o_i$, which leads to *c*-waterpixels. We have found that the first gives the best adherence to object boundaries, while the second produces more regular superpixels. 299

The spatially regularized gradient g_{reg} is defined as follows: 300

$$g_{reg} = g + kd_Q \tag{2}$$

where g is the gradient of the image f, d_Q is the distance function defined above and k is the spatial regularization parameter, which takes its values within \Re^+ . The choice of k is application dependent: when k equals zero, no regularization of the gradient is applied; when $k \to \infty$, we approach the Voronoi tessellation of the set $\{q_i\}_{1 \ge i \ge N}$ in the spatial domain.

In the final step, we apply the watershed transformation on the spatially regularized gradient g_{reg} , starting the flooding from the markers $\{M_i\}_{1 \le i \le N}$, so that an image partition $\{s_i\}_{1 \le i \le N}$ is obtained. The s_i are the resulting waterpixels.

IV. EXPERIMENTS

In order to evaluate waterpixels, the proposed method has 313 been applied on the Berkeley segmentation database [20] 314 and benchmarked against the state-of-the-art. This database is 315 divided into three subsets, "train", "test" and "val", containing 316 respectively 200, 200 and 100 images of sizes 321×481 or 317 481×321 pixels. Approximately 6 human-annotated 318 ground-truth segmentations are given for each image. These 319 ground-truth images correspond to manually drawn contours. 320

A. Implementation 321

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We have found that it is beneficial to pre-process the images 322 from the database using an area opening followed by an area 323 closing, both of size $\sigma^2/16$ (where σ is the chosen step size 324 of the regular grid). This operation efficiently removes details 325 which are clearly smaller than the expected waterpixel area and 326 which should therefore not give rise to a superpixel contour. 327

The Lab-gradient is adopted here in order to best reflect our 328 visual perception of color differences and hence the pertinence 329 of detected objects. The margin parameter ρ , described 330 in III-A, is set to $\frac{2}{3}$. 331

The cell centers correspond to the vertices of a square or an 332 hexagonal grid of step σ . The grid is computed in one pass 333 over the image, by first calculating analytically the coordinates 334 of the set of pixels belonging to each cell and then assigning 335 to them the label of their corresponding cell. We will display 336 the results for the hexagonal grid, as hexagons are more 337 isotropic than squares. Interestingly, they also lead to a better 338 quantitative performance, which was intuitively expected. 339

The implementation of the waterpixels was done using the 340 Simple Morphological Image Library (SMIL) [21]. SMIL is a 341 Mathematical Morphology library that aims to be fast, light-342 weight and portable. It brings most classical morphological 343 operators re-designed in order to take advantage of recent 344 computer features (SIMD, parallel processing, ...) to allow 345 handling of very large images and real time processing. 346

B. Qualitative Analysis 347

Figure 3 shows various images from the Berkeley 348 segmentation database and their corresponding waterpixels 349 (*m*-waterpixels and *c*-waterpixels, hexagonal and square grids, 350 different steps). Figures 3.b and 3.c (zooms of original image 351 presented in 3.a for *m*-waterpixels and *c*-waterpixels respec-352 tively) show the influence of the regularization parameter k353 (0, 4, 8, 16) for an homogeneous (blue sky) and a 354 textured (orange rock) regions. As expected, when $k \to \infty$, 355 *m*-waterpixels tend towards the Voronoi tessellation of the 356 markers, while *c*-waterpixels approach the regular grid of 357 hexagonal cells. Both show good adherence to object bound-358 aries, as shown in Figures 3.d, 3.e, 3.f. Of course, enforcing 359 regularity decreases the adherence to object boundaries (see 360 the zoom in Figure 3.f for k = 16). One advantage of 361 waterpixels is that the user can choose the shape (and size) of 362 resulting superpixels depending on the application requisites. 363 Figure 3.d, for example, presents waterpixels for hexagonal 364 (second and third columns) and square (fourth column) grids. 365 As a gradient-based approach, the quality of the watershed 366

is dependant on the borders contrast. If we look at the contours 367

of objects missed by waterpixels, we see that it is due to the 368 weakness of the gradient, as illustrated in Figure 4. 369

C. Evaluation Criteria

SP methods produce an image partition $\{s_i\}_{1 \le i \le N}$. In order 371 to compute the SP borders, we use a morphological gradient 372 with a 4 neighborhood. Note that the resulting contours are 373 two pixels wide. To this set S_c , we add the one pixel wide 374 image borders S_b . The final set is denoted C. The ground 375 truth image corresponding to the contours of the objects to be 376 segmented, provided in the Berkeley segmentation database, 377 is called GT. 378

In superpixel generation, we look for an image decomposi-379 tion into regular regions that adhere well to object boundaries. 380 We propose to use three measures to evaluate this trade-381 off, namely boundary-recall, contour density and average 382 mismatch factor, as well as computation time.

There are two levels of regularity: (1) the number of pixels 384 required to describe the SP contours, which can be seen as a 385 measure of complexity of individual SP, and (2) the similarity 386 in size and shape between SP.

The first property is evaluated by the Contour Density, which is defined as the number of SP contour pixels divided by the total number of pixels in the image:

$$CD = \frac{\frac{1}{2}|S_c| + |S_b|}{|D|} \tag{3} \qquad 391$$

Note that $|S_c|$ is divided by 2 since contours are 392 two-pixel-wide. 393

The second property, *i.e.* similarity in size and shape, is 394 evaluated by an adapted version of the mismatch factor [22]. 395 The mismatch factor measures the shape and size dissimilarity 396 between two regions. Given two sets, A and B, the mismatch 397 factor *mf* between them is defined as: 398

$$mf(A, B) := \frac{|A \cup B \setminus A \cap B|}{|A \cup B|}$$

$$= 1 - \frac{|A \cup B|}{|A \cap B|}$$
(4) 400

The mismatch factor and the Jaccard index thus sum to 401 one. Aiming to measure the superpixel regularity, we adapted 402 the mismatch factor to estimate the spread of size and shape 403 distribution. Hence, the average mismatch factor MF is 404 proposed as: 405

$$MF = \frac{1}{N} \sum_{i=1}^{N} mf(s_i^*, \widehat{s}^*)$$
(5) 406

where s_i^* is the centered version of superpixel s_i , and \hat{s}^* is 407 the average centered shape of all superpixels. The complete 408 definition of the average mismatch factor is given in Appendix. 409

Note that although compactness is sometimes used in super-410 pixels evaluation (see [23]), it is a poor measurement for 411 region regularity. For example, perfectly-rectangular regions 412 are regular but not compact (because they are different from 413 discs). Waterpixels can in principle tend towards differently 414 shaped superpixels (rectangles, hexagons or other), depending 415 on the grid and the regularization function used. Since the 416 average mismatch factor compares each superpixel against an 417

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Fig. 3. Illustrations of waterpixels on the Berkeley segmentation database: All waterpixels images are computed with an hexagonal grid with step $\sigma = 30$ pixels and a regularization parameter k = 8, unless otherwise specified. (a): original image (middle) with corresponding *m*-waterpixels (left) and *c*-waterpixels (right). $\sigma = 25$ pixels, k = 16. (c): zooms of *m*-waterpixels (a) for k = 0, 4, 8, 16. (c): zooms of *c*-waterpixels (a) for k = 0, 4, 8, 16. (c): original image - *m*-wat. - *c*-wat. - *m*-wat. with square grid and $\sigma = 40$ pixels. (e): original image - *m*-wat. - *c*-wat. - zoom of *c*-wat. (f): original image - *m*-wat. - *c*-wat. - zoom of *m*-wat. with k = 16.

image dependent template, this measure is more appropriateto evaluate regularity than compactness.

To quantify the adherence to object boundaries, a classical measure used in the literature is the boundary-recall (BR). Boundary-recall is defined as the percentage of ground-truth contour pixels GT which fall within strictly less than 3 pixels from superpixel boundaries C:

$$BR = \frac{|\{p \in GT, d(p, C) < 3\}|}{|GT|}$$
(6)

where d is the L_1 (or Manhattan) distance.

While precision cannot be directly used in the context of 427 over-segmentations, boundary-recall has to be, in this partic-428 ular case of superpixels, interpreted with caution. Indeed, as 429 noted also by Kalinin and Sirota [24], very tortuous contours 430 systematically lead to better performances: because of their 431 higher number, SP contour pixels have a higher chance of 432 matching a true contour, increasing artificially the boundary-433 recall. Hence, we propose to always consider the trade-off 434 between boundary-recall and contour density to properly 435 evaluate the adherence to object boundaries, penalizing at the 436 same time the cost in pixels to describe SP contours. 437



Fig. 4. Contours missed by waterpixels: (a): original image from the Berkeley segmentation database. (b): *m*-waterpixels with step = 27 and k = 10. (c): *c*-waterpixels with step = 27 and k = 10. (d), (e), (f): zoom of (a), (b), (c) respectively. (g): zoom of the non-regularized gradient image. (h) and (i): reached (green) and missed (red) contours, respectively by *m*-waterpixels and *c*-waterpixels.

438 D. Quantitative Analysis and Comparison 439 With State-of-the-Art

In this paragraph, we will use *m*-waterpixels and denote them directly as "waterpixels" for the sake of simplicity.

During the design of the algorithm, we used intermedi-442 ate results from the train and test subsets of the Berkeley 443 database. Therefore, we report the results obtained for the 444 validation subset ("val"), which contains 100 images. Results 445 for boundary-recall, average mismatch factor and contour 446 density are averaged for this subset and shown in Figure 5. 447 Blue and red curves correspond to varying regularization 448 parameters k and k' respectively for waterpixels and SLIC. 449 The values for k and k' have been chosen such that they 450 cover a reasonable portion of the regularization space between 451 no regularization (k = 0) and a still acceptable level of 452 regularization. 453

Figure 5(a) shows contour density against boundary-recall 454 for waterpixels and SLIC. The ideal case being the lowest con-455 tour density for the highest boundary-recall, we can see that 456 the trade-off between both properties improves for decreasing 457 regularization, as expected. On the other hand, SLIC shows 458 another behavior: the trade-off improves, then gets worse 459 with regularization. At any rate, it is important to note that 460 waterpixels achieves a better "best" trade-off than SLIC 461 (see waterpixel k = 0 and SLIC k' = 15). Besides, this obser-462 vation is valid for the whole family of waterpixel-methods as 463 the zero-value regularization does not take into account d_0 . 464 In order to do a fair comparison between waterpixels and 465 SLIC over all criteria, we choose corresponding curves in the 466 trade-off contour density/boundary-recall, i.e. waterpixels with 467 k = 8 and SLIC with k' = 15, and compare this couple for 468 the other criteria. 469

Figure 5(b) shows that, for a given number of superpixels, contour density of waterpixels is more stable and most of the time lower than SLIC when varying regularization. More particularly, contour density is lower for waterpixels (k = 8)





Fig. 5. Benchmark: performance comparison between waterpixels and SLIC. (a) Contour Density against Boundary-recall. (b) Contour Density against Number of Superpixels. (c) Mismatch factor against Boundary-recall.

than for SLIC (k' = 15). This means that for the same number of superpixels, waterpixels contours are shorter than SLIC 476 contours, which is partly explained by less tortuous contours. 476

Figure 5(c) shows average mismatch factor against 477 boundary-recall for waterpixels and SLIC. We can see that 478 the curves for waterpixels with k = 8 and SLIC with k' = 15 479 are here again close to each other. 480



Fig. 6. Comparison between Waterpixels and SLIC superpixels for $\sigma = 25$ pixels on a zoom of an image from the Berkeley segmentation database. (a) SLIC k' = 15. (b) Waterpixels k = 8.

These properties are illustrated in Figure 6, where we can 481 see examples of reached and missed contours by both methods, 482 as well as their different behaviours in terms of regularity 483 (shape, size, tortuosity). 484

E. Computation Time 485

Computing time was measured on a personal computer 486 based on Intel(R) Core(TM) i7 central processing units 487 (4 physical cores, 4 virtual ones), operating at 2.93GHz. Both 488 methods have linear complexity with the number of pixels in 489 the image. For an image of size 481×321 , average computing 490 time for SLIC was 149 ms, and 132 ms for waterpixels 491 (82 ms without pre-filtering). A more detailed comparison of 492 computation times is presented in Figure 7 (showing average 493 and standard deviation for different numbers of superpixels). 494 We can see that waterpixels are generally faster to compute 495 than SLIC superpixels. Contrary to the latter's, their compu-496 tation time decreases slightly with the number of superpixels. 497 An analysis of computation times for the different steps of 498 waterpixels reveals that this variability is only introduced by 499 the grid computation and the minima selection procedure. 500 Concerning grid computation time, it rises from 2 ms for 501 small numbers of waterpixels to 27 ms for large numbers of 502 waterpixels. This simply means that we still have to optimize 503 this step. Concerning the computation time of the minima 504 selection procedure, it decreases as waterpixels become larger 505 because of pre-filtering step. Indeed, the size of this filtering 506 is directly proportional to the cell size. As such, resulting 507 images contain less minima, which simplifies the selection 508 procedure. Besides, the variance observed when we change 509 images is explained by the fact that the difficulty of minima 510 evaluation/computation depends on the content of each image. 511



Fig. 7. Computation time comparison with images of the Berkeley database.

We are currently working on a new implementation of minima 512 computation/evaluation which would be less dependent on the 513 number of superpixels.

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To conclude this section, waterpixels are generally faster 515 to compute than SLIC superpixels, and they are at least 516 as performant in the trade-off between adherence to object 517 boundaries and regularity in shape and size, while using much 518 less pixels to describe their contours. 519

V. DISCUSSION AND PERSPECTIVES

We have shown that waterpixels produce competitive results 52 with respect to the state-of-the-art. These advantages are 522 valuable in the classification/detection/segmentation pipeline, 523 where superpixels play the part of primitives. Moreover, there 524 is one major difference in the construction of the algorithm: 525 the SLIC approach does not impose any connectivity con-526 straint. The resulting superpixels are therefore not necessarily 527 connected, which requires some ad hoc postprocessing step. 528 In contrast, waterpixels are connected by definition, and the 529 connectivity constraint is actually implemented in the distance 530 used. 531

The proposed approach is gradient-based. Standard methods 532 can be used to compute this gradient, or a specific gradient 533 computation method can be designed for a given application. 534 In any case, this offers flexibility to waterpixels. One limitation 535 though is the quality of the signal in such a gradient image. 536 As seen in 4, alteration by noise or insufficiently contrasted 537 contours may lead to the prevalence of regularity over adher-538 ence to object boundaries. If filtering steps are usually enough 539 to deal with noise and remove non pertinent small details, 540 parameter values have to be optimized for each database. 541 Future work will aim at overcoming this limitation by adding a 542 learning step of optimal filtering values for specific databases. 543

The general design of waterpixels offers many prospects. 544 Among them, one promising field of improvement resides 545 in the placement of markers, as they constitute the main 546 degree of freedom of the method. We are currently inves-547 tigating the possibility to select the markers in an optimal 548 manner, for example by formulating the marker placement as a 549 p-dispersion problem (see [25]) in an augmented space. 550 MACHAIRAS et al.: WATERPIXELS

The speed of waterpixels contributes to expanding their 551 possible applications. For example, it could be interest-552 ing to compute different sets of waterpixels, by changing 553 design options (different cells, gradients, grid steps, etc.), 554 and then use ensemble clustering methods to obtain a final 555 segmentation [26], [27]. 556

Last buy not least, waterpixels lead to the efficient construc-557 tion of hierarchical partitions based on superpixels. Indeed, 558 the computation of the watershed can produce at the same 559 time a segmentation and a hierarchy of partitions based on 560 that segmentation, with only minor overhead computation 561 times [28]-[30]. 562

VI. CONCLUSION

This paper introduces waterpixels, a family of methods 564 for computing regular superpixels based on the watershed 565 transformation. Both adherence to object boundaries and regu-566 larity of resulting regions are encouraged thanks to the choice 567 of the markers and the gradient to be flooded. Different 568 design options, such as the distance function used to spatially 569 regularized the gradient, lead to different trade-offs between 570 both properties. The computational complexity of waterpixels 571 is linear. Our current implementation makes it one of the 572 fastest superpixel methods. Experimental results show that 573 waterpixels are competitive with respect to the state-of-the art. 574 They outperform SLIC superpixels, both in terms of quality 575 and speed. The trade-off between speed and segmentation 576 quality achieved by waterpixels, as well as their ability to 577 generate hierarchical segmentations at negligible extra cost, 578 offer interesting perspectives for this superpixels generation 579 method. 580

An implementation of waterpixels is available from 581 http://cmm.ensmp.fr/~machairas/waterpixels. 582

APPENDIX

MEAN MISMATCH FACTOR DEFINITION

Let $\{s_i\}_{1 \le i \le N}$ be a set of superpixels. The centered version 585 s_i^* of s_i is obtained by translating s_i so that its barycenter is 586 the origin of the coordinates system. 587

The average shape \hat{s}^* of the $\{s_i\}$ is computed as follows. 588 Let first define function S: 589

 $S: D \longrightarrow \mathbb{N}$

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$$x_p \longmapsto \sum_{i=1}^N 1_i(x_p)$$

(7)

where 1_i is the indicator function of s_i^* . Thus, image S cor-591 responds to the summation image of all centered superpixels. 592 Let furthermore $\mu_A = 1/n \sum_{i=1}^{N} |s_i|$ be the average area of the considered superpixels, and let S_t be the threshold of S at 593 594 level *t*: $S_t(x) = \{x_p \in D | |S(x_p)| \ge t\}.$ 595

The average centered shape \hat{s}^* is then the set S_{t_0} , where t_0 596 is the maximal threshold value which enables \hat{s}^* to have an 597 area greater than or equal to μ_A : 598

599
$$t_0 = \max\{t \mid |S_t| \ge \mu_A\}$$
 (8)

$$\widehat{s}^* = S_{t_0} \tag{9}$$

 $\{s_i\}_{1 \le i \le N}$ is: 602 3.7

$$MF = \frac{1}{N} \sum_{i=1}^{N} mf(s_i^*, \hat{s}^*).$$
(10) 603

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Waterpixels

Vaïa Machairas, Matthieu Faessel, David Cárdenas-Peña, Théodore Chabardes, Thomas Walter, and Etienne Decencière

Abstract—Many approaches for image segmentation rely on a first low-level segmentation step, where an image is partitioned 2 into homogeneous regions with enforced regularity and adherence 3 to object boundaries. Methods to generate these superpixels have 4 gained substantial interest in the last few years, but only a few 5 have made it into applications in practice, in particular because the requirements on the processing time are essential but are not met by most of them. Here, we propose waterpixels as a general 8 strategy for generating superpixels which relies on the marker controlled watershed transformation. We introduce a spatially 10 regularized gradient to achieve a tunable tradeoff between the 11 superpixel regularity and the adherence to object boundaries. 12 The complexity of the resulting methods is linear with respect 13 to the number of image pixels. We quantitatively evaluate our 14 approach on the Berkeley segmentation database and compare 15 it against the state-of-the-art. 16

Index Terms-Superpixels, watershed, segmentation. 17

I. INTRODUCTION

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AO:3

T UPERPIXELS (SP) are regions resulting from 19 a low-level segmentation of an image and are typically 20 used as primitives for further analysis such as detection, 21 segmentation, and classification of objects (see Figure 1 22 for an illustration). The underlying idea is that this first 23 low-level partition alleviates the computational complexity of 24 the following processing steps and improves their robustness, 25 as not single pixel values but pixel set features can be used. 26 27

- Superpixels should have the following properties:
- 1) homogeneity: pixels of a given SP should present 28 similar colors or gray levels; 29

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(a) (b)

Fig. 1. Superpixels illustration. The original image comes from the Berkeley segmentation database. (a) Original image. (b) Waterpixels.

- 2) connected partition: each SP is made of a single connected component and the SPs constitute a partition of the image;
- 3) adherence to object boundaries: object boundaries should be included in SP boundaries;
- 4) regularity: SPs should form a regular pattern on the image. This property is often desirable as it makes the SP more convenient to use for subsequent analysis steps.

The requirements on regularity and boundary adherence are to a certain extent oppositional, and a good solution typically aims at finding a compromise between these two requirements.

In addition to these requirements on superpixel quality, computational efficiency is an absolutely essential aspect, as the partition into superpixels is typically only the first step of an often complex and potentially time consuming workflow. Methods of linear complexity are consequently of particular interest.

We therefore hypothesized that the Watershed transformation [1], [2] should be an interesting candidate for superpixel generation, as it has been shown to achieve state-of-the-art performance in many segmentation problems, it is non-parametric, and there exist linear-complexity algorithms to compute it, as well as efficient implementations [3], [4]. The only often cited drawback, oversegmentation, does not seem to be problematic for superpixel generation, as long as we can control the degree of oversegmentation (number of superpixels), and the regularity of the resulting partition.

Given these considerations, we propose a strategy for 58 applying the watershed transform to superpixel generation, 59 where we use a spatially regularized gradient to achieve a 60 tunable trade-off between superpixel regularity and adherence 61 to object boundaries. We quantitatively evaluate our method 62 on the Berkeley segmentation database and show that we 63 outperform the best linear-time state-of-the art method: Simple 64 Linear Iterative Clustering (SLIC) [5]. We call the resulting 65 superpixels "waterpixels." 66

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AO:4

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Method	[11]	[12]	[13]	[5]	WP
Generation type	1	2	1 (iterated)	2	1
(see section II-B)					
Seed type (see	A	С	С	С	В
section II-A)					
Control on num-	yes	yes	yes	no	yes
ber of SPs					
Control on regu-	no	yes	no	yes	yes
larity					
Post-processing	no	no	no	no	yes
free					
Complexity	O(n)	$O(in\sqrt{N})$	O(in)	O(n)	O(n)

This paper is an extended version of [6]. It proposes a 67 more general approach (elaborating a whole family of water-68 pixels generation methods), with a more thorough validation 69 and improved results with regard to the trade-off between 70 boundary adherence and regularity, as well as computation time. Moreover, we have developed and made available a fast 72 implementation of waterpixels. 73

II. RELATED WORK

Low-level segmentations have been used for a long time as 75 first step towards segmentation [7], [8]. The term superpixel 76 was coined much later [9], albeit in a more constrained frame-77 work. This approach has raised increasing interest since then. 78 Various methods exist to compute SPs, most of them based on 79 graphs [10], geometrical flows [11] or k-means [5]. We will 80 focus on linear complexity methods generating regular SPs. 81

Methods for SP generation are all based on two steps: 82 an initialization step where either seeds or a starting par-83 tition are defined and a (potentially iterative) assignment 84 step, where each pixel is assigned to one superpixel, starting 85 from the initialization. In the next section, we are going to 86 review previously published approaches for SP generation with 87 respect to these aspects and compare them regarding various 88 performance criteria. We limit the presentation of existing 89 methods to those with linear complexity. 90

A. Choosing the Seeds 91

In the first step, a set of seeds is chosen, which are typically 92 spaced regularly over the image plane and which can be either 93 94 regions or single pixels:

- Type A seeds are independent of the image content. These 95 are typically the cells or the centers of a regular grid. 96
- Type B seeds depend on the content of the image 97 (compromise between a regular cover of the image plane 98 and an adaption to the contour). 90
- Type C seeds are initially image independent, then they 100 are iteratively refined to take into account the image 101 contents. 102

If the seed does not depend on the image, an iterative 103 refinement is usually preferable, and therefore more time 104

is spent on the computation of the SP. Type B methods 105 may spend more time on finding appropriate seeds, but can 106 therefore afford not to iterate the SP generation. 107

B. Building Superpixels From Seeds

In the second step, the partition into superpixels is built 109 from the seeds. Among the methods with linear complexity, 110 there are two main strategies for this:

Shortest Path Methods (Type 1) [11], [13]: these methods 112 are based on region growing: they start from a set of seeds 113 (points or regions) and successively extend them by incor-114 porating pixels in their neighborhood according to a usually 115 image dependent cost function until every pixel of the image 116 plane has been assigned to exactly one superpixel. This process 117 may or may not be iterated. 118

Shortest Distance Methods (Type 2) [5], [12]: these are 119 iterative procedures inspired by the field of unsupervised 120 learning, where at each iteration step, seeds (such as centroids) 121 are calculated from the previous partition and pixels are then 122 re-assigned to the closest seed (like for example the k-means 123 approach). 124

Even though methods inspired by general clustering meth-125 ods (type 2) seem appealing at first sight, in particular when 126 they globally optimize a cost function, this class of methods 127 does not guarantee connectivity of the superpixels for arbi-128 trary choices of the pixel-seed distance (see [5], [12]). For 129 instance, the distance metric proposed in [5] (a combination 130 of Euclidean and grey level distance), leads to non-connected 131 superpixels, which is undesirable. To solve this issue, a post-132 processing step is necessary, consisting either in relabeling the 133 image so that every connected component has its own label 134 (see [12]), leading to a more irregular distribution of SP sizes 135 and shapes, or in reassigning isolated regions to the closest and 136 large enough Superpixel, as in [5], leading to non-optimality 137 of the solution and an unpredictable number of superpixels. 138 In addition, such postprocessing increases the computational cost and can turn out to be the most time-consuming step when the image contains numerous small objects/details compared 141 to the size of the Superpixel. 142

On the contrary, methods based on region growing (type 1) 143 inherently implement a "path-type" distance, where the dis-144 tance between two pixels does not only depend on value 145 and position of the pixels themselves, but on values and 146 positions along the path connecting them. Type 1 methods 147 imply connected superpixel regions, for which the number of 148 superpixels is exactly the number of seeds. 149

C. Other Properties

It is generally accepted that a good superpixel-generation 151 method should provide to the user total control over the num-152 ber of resulting Superpixels. While this property is achieved 153 by [11]-[14], some only reach approximatively this num-154 ber because of post-processing (either by splitting too big 155 superpixels, or removing small isolated superpixels as in [5]). 156 Another parameter is the control on superpixels regularity in 157 the trade-off between regularity and adherence to contours. 158 Only [5] and [12] enable the user to weight the importance 159

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of regularity compared to boundary adherence, so it can be 160 adapted to the application. 161

As far as performance is concerned, one of the main 162 criteria is undoubtedly the complexity that the method 163 requires. Indeed, for Superpixels to be used as primitives for 164 further analysis such as classification, their computation should 165 neither take too long nor too much memory. This is the reason 166 why we focus on linear complexity methods. Among them, 167 SLIC appears to offer the best performance with regards to the 168 trade-off between adherence to boundaries and regularity [5]. 169 Moreover, since its recent inception, this method has become 170 very popular in the computer vision community. We will 171 therefore use it as reference for the quantitative evaluation of 172 our method. 173

D. Superpixels and Watershed 174

In principle, the watershed transformation (see [15] for a 175 review) is well suited for SP generation: 176

- 1) It gives a good adherence to object boundaries when 177 computed on the image gradient. 178
- 2) It allows to control the number and spatial arrangement 179 of the resulting regions through the choice of markers. 180
- 3) The connectivity of resulting regions is guaranteed and 181 no postprocessing is required. 182
- 4) It offers linear complexity with the number of pixels in 183 the image. 184

Indeed, it has been used to produce low-level segmentations 185 in several applications, including computation intensive 186 3D applications [16], [17], in particular when shape regularity 187 of the elementary regions was not required. 188

Previous publications claimed that the watershed transfor-189 mation does not allow for the generation of spatially regular 190 SP [5], [11]. Recently, we and others [6], [18] have shown 191 that in principle the watershed transformation can be applied 192 to SP generation. 193

Here, we introduce waterpixels, a family of methods based 194 on the watershed transformation to compute superpixels. 195

III. WATERPIXELS

watershed-based segmentation As most methods. 197 waterpixels are based on two steps: the definition of 198 markers, from which the flooding starts, and the definition of 199 a gradient (the image to be flooded). We propose to design 200 these steps in such a way that regularity is encouraged. 201

A waterpixel-generation method is characterized by the 202 following steps: 203

- 204 1) Computation of the gradient of the image;
- 2) Definition of regular cells on the image, centered on the 205 vertices of a regular grid; 206
- 3) Selection of one marker per cell; 207

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- 4) Spatial regularization of the gradient with the help of a 208 distance function; 209
- 5) Application of the watershed transformation on the 210 regularized gradient defined in step 4 from the markers 211 defined in step 2. 212

These steps are illustrated in figure 2 and developed in the 213 next paragraphs. 214

A. Gradient and Cells Definition

Let $f: D \to V$ be an image, where D is a rectangular 216 subset of Z^2 , and V a set of values, typically $\{0, \ldots, 255\}$ 217 when f is a grey level image, or $\{0, \ldots, 255\}^3$ for color 218 images. 219

The first step consists in computing the gradient image g220 of the image f. The choice of the gradient operator depends 221 on the image type, e.g. for grey level images we might 222 choose a morphological gradient. This gradient will be used 223 to choose the seeds (section III-B) and to build the regularised 224 gradient (III-C). 225

For the definition of cells, we first choose a set of N points 226 $\{o_i\}_{1 \le i \le N}$ in D, called *cell centers*, so that they are placed on 227 the vertices of a regular grid (a square or hexagonal one for 228 example). Given a distance d on D, we denote by σ the grid 229 step, *i.e.* the distance between closest grid points.

A Voronoi tesselation allows to associate to each o_i a 231 Voronoi cell. For each such cell, a homothety centered on o_i 232 with factor ρ (0 < ρ < 1) leads to the computation of the 233 final cell C_i . This last step allows for the creation of a margin 234 between neighbouring cells, in order to avoid the selection of 235 markers too close from each other. 236

B. Selection of the Markers

As each cell is meant to correspond to the generation of 238 a unique waterpixel, our method, through the choice of one 239 marker per cell, offers total control over the number of SP, 240 with a strong impact on their size and shape if desired. 241

First, we compute the minima of the gradient g. Each 242 minimum is a connected component, composed of one or more pixels. These minima are truncated along the grid, i.e. pixels which fall on the margins between cells are removed.

Second, every cell of the grid serves to define a region of interest in the gradient image. The content of g in this very region is then analyzed to select a unique marker, as explained in the next paragraph.

For each cell, the corresponding marker is chosen among the minima of g which are present in this very cell.

If several minima are present, then the one with the highest 252 surface extinction value [19] is used. We have found surface 253 extinction values to give the best performances compared with 254 volume and dynamic extinction values (data not shown). 255

It may happen that there is no minimum in a cell. This 256 is an uncommon situation in natural images. In such cases, 257 we must add a marker for the cell which is not a minimum 258 of g, in order to keep regularity. One solution could be to 259 simply choose the center of the cell; however, if this point 260 falls on a local maximum of the gradient g, the resulting 261 SP may coincide with the maximum region and therefore be 262 small in size (leading to a larger variability in size of the SP). 263 We propose instead to take, as marker, the flat zone with 264 minimum value of the gradient inside this very cell. 265

In both cases (i.e. either there exists at least one minimum in 266 the cell or there is not), the selected marker has to be composed 267 of a unique connected component to ensure regularity and 268 connectivity of the resulting superpixel. However, it might 269 not be the case, respectively if more than one minimum 270

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Fig. 2. Illustration of waterpixels generation: (a): original image; (b) corresponding Lab gradient; (c): selected markers within the regular grid of hexagonal cells (step $\sigma = 40$ pixels); (d): distance function to markers; (g): distance function to cell centers; (e) and (h): spatially regularized gradient respectively with distance functions to selected markers (d) and to cell centers (g); (f) and (i): Resulting waterpixels obtained by respectively applying the watershed transformation to (e) and (h), with markers (c).

have the same highest extinction value, or if more than one
flat zone present the same lowest gradient value in the cell.
Therefore, an additional step enables to keep only one of
the connected components if there is more than one potential
"best" candidate.

The set of resulting markers is denoted $\{M_i\}_{1 \ge i \ge N}$, $M_i \subset D$. The result of the marker selection procedure is illustrated in Figure 2.c.

279 C. Spatial Regularization of the Gradient and Watershed

The selection of markers has enforced the pertinence of future superpixel-boundaries but also the regularity of their pattern (by imposing only one marker per cell). In this paragraph, we design a spatially regularized gradient in order to further compromise between boundary adherence and regularity.

Let $Q = \{q_i\}_{1 \le i \le N}$ be a set of N connected components of the image f. For all $p \in D$, we can define a distance function d_Q with respect to Q as follows:

$$\forall p \in D, \, d_Q(p) = \frac{2}{\sigma} \min_{i \in [1,N]} d(p,q_i) \tag{1}$$

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where σ is the grid step defined in the previous section. The normalization by σ is introduced to make the regularization independent from the chosen SP size.

We have studied two possible choices of the q_i . The first one is to choose them equal to the markers: $q_i = M_i$. Resulting waterpixels are called *m*-waterpixels. The second one consists in setting them at the cell centers: $q_i = o_i$, which leads to *c*-waterpixels. We have found that the first gives the best adherence to object boundaries, while the second produces more regular superpixels. 299

The spatially regularized gradient g_{reg} is defined as follows:

$$g_{reg} = g + kd_Q \tag{2}$$

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where g is the gradient of the image f, d_Q is the distance function defined above and k is the spatial regularization parameter, which takes its values within \Re^+ . The choice of k is application dependent: when k equals zero, no regularization of the gradient is applied; when $k \to \infty$, we approach the Voronoi tessellation of the set $\{q_i\}_{1 \ge i \ge N}$ in the spatial domain.

In the final step, we apply the watershed transformation on the spatially regularized gradient g_{reg} , starting the flooding from the markers $\{M_i\}_{1 \le i \le N}$, so that an image partition $\{s_i\}_{1 \le i \le N}$ is obtained. The s_i are the resulting waterpixels.

IV. EXPERIMENTS

In order to evaluate waterpixels, the proposed method has 313 been applied on the Berkeley segmentation database [20] 314 and benchmarked against the state-of-the-art. This database is 315 divided into three subsets, "train", "test" and "val", containing 316 respectively 200, 200 and 100 images of sizes 321×481 or 317 481×321 pixels. Approximately 6 human-annotated 318 ground-truth segmentations are given for each image. These 319 ground-truth images correspond to manually drawn contours. 320

A. Implementation 321

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We have found that it is beneficial to pre-process the images 322 from the database using an area opening followed by an area 323 closing, both of size $\sigma^2/16$ (where σ is the chosen step size 324 of the regular grid). This operation efficiently removes details 325 which are clearly smaller than the expected waterpixel area and 326 which should therefore not give rise to a superpixel contour. 327

The Lab-gradient is adopted here in order to best reflect our 328 visual perception of color differences and hence the pertinence 329 of detected objects. The margin parameter ρ , described 330 in III-A, is set to $\frac{2}{3}$. 331

The cell centers correspond to the vertices of a square or an 332 hexagonal grid of step σ . The grid is computed in one pass 333 over the image, by first calculating analytically the coordinates 334 of the set of pixels belonging to each cell and then assigning 335 to them the label of their corresponding cell. We will display 336 the results for the hexagonal grid, as hexagons are more 337 isotropic than squares. Interestingly, they also lead to a better 338 quantitative performance, which was intuitively expected. 339

The implementation of the waterpixels was done using the 340 Simple Morphological Image Library (SMIL) [21]. SMIL is a 341 Mathematical Morphology library that aims to be fast, light-342 weight and portable. It brings most classical morphological 343 operators re-designed in order to take advantage of recent 344 computer features (SIMD, parallel processing, ...) to allow 345 handling of very large images and real time processing. 346

B. Qualitative Analysis 347

Figure 3 shows various images from the Berkeley 348 segmentation database and their corresponding waterpixels 349 (*m*-waterpixels and *c*-waterpixels, hexagonal and square grids, 350 different steps). Figures 3.b and 3.c (zooms of original image 351 presented in 3.a for *m*-waterpixels and *c*-waterpixels respec-352 tively) show the influence of the regularization parameter k353 (0, 4, 8, 16) for an homogeneous (blue sky) and a 354 textured (orange rock) regions. As expected, when $k \to \infty$, 355 *m*-waterpixels tend towards the Voronoi tessellation of the 356 markers, while c-waterpixels approach the regular grid of 357 hexagonal cells. Both show good adherence to object bound-358 aries, as shown in Figures 3.d, 3.e, 3.f. Of course, enforcing 359 regularity decreases the adherence to object boundaries (see 360 the zoom in Figure 3.f for k = 16). One advantage of 361 waterpixels is that the user can choose the shape (and size) of 362 resulting superpixels depending on the application requisites. 363 Figure 3.d, for example, presents waterpixels for hexagonal 364 (second and third columns) and square (fourth column) grids. 365 As a gradient-based approach, the quality of the watershed 366

is dependant on the borders contrast. If we look at the contours 367

of objects missed by waterpixels, we see that it is due to the 368 weakness of the gradient, as illustrated in Figure 4. 369

C. Evaluation Criteria

SP methods produce an image partition $\{s_i\}_{1 \le i \le N}$. In order 371 to compute the SP borders, we use a morphological gradient 372 with a 4 neighborhood. Note that the resulting contours are 373 two pixels wide. To this set S_c , we add the one pixel wide 374 image borders S_b . The final set is denoted C. The ground 375 truth image corresponding to the contours of the objects to be 376 segmented, provided in the Berkeley segmentation database, 377 is called GT. 378

In superpixel generation, we look for an image decomposi-379 tion into regular regions that adhere well to object boundaries. 380 We propose to use three measures to evaluate this trade-381 off, namely boundary-recall, contour density and average 382 mismatch factor, as well as computation time.

There are two levels of regularity: (1) the number of pixels 384 required to describe the SP contours, which can be seen as a 385 measure of complexity of individual SP, and (2) the similarity 386 in size and shape between SP.

The first property is evaluated by the Contour Density, which is defined as the number of SP contour pixels divided by the total number of pixels in the image:

$$CD = \frac{\frac{1}{2}|S_c| + |S_b|}{|D|} \tag{3} \quad 391$$

Note that $|S_c|$ is divided by 2 since contours are two-pixel-wide.

The second property, *i.e.* similarity in size and shape, is 394 evaluated by an adapted version of the mismatch factor [22]. 395 The mismatch factor measures the shape and size dissimilarity 396 between two regions. Given two sets, A and B, the mismatch 397 factor *mf* between them is defined as: 398

$$mf(A, B) := \frac{|A \cup B \setminus A \cap B|}{|A \cup B|}$$

$$= 1 - \frac{|A \cap B|}{|A \cup B|}$$
(4) 400

The mismatch factor and the Jaccard index thus sum to 401 one. Aiming to measure the superpixel regularity, we adapted 402 the mismatch factor to estimate the spread of size and shape 403 distribution. Hence, the average mismatch factor MF is 404 proposed as: 405

$$MF = \frac{1}{N} \sum_{i=1}^{N} mf(s_i^*, \widehat{s}^*)$$
(5) 400

where s_i^* is the centered version of superpixel s_i , and \hat{s}^* is 407 the average centered shape of all superpixels. The complete 408 definition of the average mismatch factor is given in Appendix. 409

Note that although compactness is sometimes used in super-410 pixels evaluation (see [23]), it is a poor measurement for 411 region regularity. For example, perfectly-rectangular regions 412 are regular but not compact (because they are different from 413 discs). Waterpixels can in principle tend towards differently 414 shaped superpixels (rectangles, hexagons or other), depending 415 on the grid and the regularization function used. Since the 416 average mismatch factor compares each superpixel against an 417

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Fig. 3. Illustrations of waterpixels on the Berkeley segmentation database: All waterpixels images are computed with an hexagonal grid with step $\sigma = 30$ pixels and a regularization parameter k = 8, unless otherwise specified. (a): original image (middle) with corresponding *m*-waterpixels (left) and *c*-waterpixels (right). $\sigma = 25$ pixels, k = 16. (c): zooms of *m*-waterpixels (a) for k = 0, 4, 8, 16. (c): zooms of *c*-waterpixels (a) for k = 0, 4, 8, 16. (c): original image - *m*-wat. - *c*-wat. - *m*-wat. with square grid and $\sigma = 40$ pixels. (e): original image - *m*-wat. - *c*-wat. - zoom of *c*-wat. (f): original image - *m*-wat. - *c*-wat. - zoom of *m*-wat. with k = 16.

image dependent template, this measure is more appropriateto evaluate regularity than compactness.

To quantify the adherence to object boundaries, a classical measure used in the literature is the boundary-recall (BR). Boundary-recall is defined as the percentage of ground-truth contour pixels GT which fall within strictly less than 3 pixels from superpixel boundaries C:

$$BR = \frac{|\{p \in GT, d(p, C) < 3\}|}{|GT|}$$
(6)

where *d* is the L_1 (or Manhattan) distance.

While precision cannot be directly used in the context of 427 over-segmentations, boundary-recall has to be, in this partic-428 ular case of superpixels, interpreted with caution. Indeed, as 429 noted also by Kalinin and Sirota [24], very tortuous contours 430 systematically lead to better performances: because of their 431 higher number, SP contour pixels have a higher chance of 432 matching a true contour, increasing artificially the boundary-433 recall. Hence, we propose to always consider the trade-off 434 between boundary-recall and contour density to properly 435 evaluate the adherence to object boundaries, penalizing at the 436 same time the cost in pixels to describe SP contours. 437



Fig. 4. Contours missed by waterpixels: (a): original image from the Berkeley segmentation database. (b): *m*-waterpixels with step = 27 and k = 10. (c): *c*-waterpixels with step = 27 and k = 10. (d), (e), (f): zoom of (a), (b), (c) respectively. (g): zoom of the non-regularized gradient image. (h) and (i): reached (green) and missed (red) contours, respectively by *m*-waterpixels and *c*-waterpixels.

438 D. Quantitative Analysis and Comparison 439 With State-of-the-Art

In this paragraph, we will use *m*-waterpixels and denote them directly as "waterpixels" for the sake of simplicity.

During the design of the algorithm, we used intermedi-442 ate results from the train and test subsets of the Berkeley 443 database. Therefore, we report the results obtained for the 444 validation subset ("val"), which contains 100 images. Results 445 for boundary-recall, average mismatch factor and contour 446 density are averaged for this subset and shown in Figure 5. 447 Blue and red curves correspond to varying regularization 448 parameters k and k' respectively for waterpixels and SLIC. 449 The values for k and k' have been chosen such that they 450 cover a reasonable portion of the regularization space between 451 no regularization (k = 0) and a still acceptable level of 452 regularization. 453

Figure 5(a) shows contour density against boundary-recall 454 for waterpixels and SLIC. The ideal case being the lowest con-455 tour density for the highest boundary-recall, we can see that 456 457 the trade-off between both properties improves for decreasing regularization, as expected. On the other hand, SLIC shows 458 another behavior: the trade-off improves, then gets worse 459 with regularization. At any rate, it is important to note that 460 waterpixels achieves a better "best" trade-off than SLIC 461 (see waterpixel k = 0 and SLIC k' = 15). Besides, this obser-462 vation is valid for the whole family of waterpixel-methods as 463 the zero-value regularization does not take into account d_Q . 464 In order to do a fair comparison between waterpixels and 465 SLIC over all criteria, we choose corresponding curves in the 466 trade-off contour density/boundary-recall, *i.e.* waterpixels with 467 k = 8 and SLIC with k' = 15, and compare this couple for 468 the other criteria. 469

Figure 5(b) shows that, for a given number of superpixels, contour density of waterpixels is more stable and most of the time lower than SLIC when varying regularization. More particularly, contour density is lower for waterpixels (k = 8)





Fig. 5. Benchmark: performance comparison between waterpixels and SLIC. (a) Contour Density against Boundary-recall. (b) Contour Density against Number of Superpixels. (c) Mismatch factor against Boundary-recall.

than for SLIC (k' = 15). This means that for the same number of superpixels, waterpixels contours are shorter than SLIC 476 contours, which is partly explained by less tortuous contours. 476

Figure 5(c) shows average mismatch factor against 477 boundary-recall for waterpixels and SLIC. We can see that 478 the curves for waterpixels with k = 8 and SLIC with k' = 15 479 are here again close to each other. 480



Fig. 6. Comparison between Waterpixels and SLIC superpixels for $\sigma = 25$ pixels on a zoom of an image from the Berkeley segmentation database. (a) SLIC k' = 15. (b) Waterpixels k = 8.

These properties are illustrated in Figure 6, where we can 481 see examples of reached and missed contours by both methods, 482 as well as their different behaviours in terms of regularity 483 (shape, size, tortuosity). 484

E. Computation Time 485

Computing time was measured on a personal computer 486 based on Intel(R) Core(TM) i7 central processing units 487 (4 physical cores, 4 virtual ones), operating at 2.93GHz. Both 488 methods have linear complexity with the number of pixels in 489 the image. For an image of size 481×321 , average computing 490 time for SLIC was 149 ms, and 132 ms for waterpixels 491 (82 ms without pre-filtering). A more detailed comparison of 492 computation times is presented in Figure 7 (showing average 493 and standard deviation for different numbers of superpixels). 494 We can see that waterpixels are generally faster to compute 495 than SLIC superpixels. Contrary to the latter's, their compu-496 tation time decreases slightly with the number of superpixels. 497 An analysis of computation times for the different steps of 498 waterpixels reveals that this variability is only introduced by 499 the grid computation and the minima selection procedure. 500 Concerning grid computation time, it rises from 2 ms for 501 small numbers of waterpixels to 27 ms for large numbers of 502 waterpixels. This simply means that we still have to optimize 503 this step. Concerning the computation time of the minima 504 selection procedure, it decreases as waterpixels become larger 505 because of pre-filtering step. Indeed, the size of this filtering 506 is directly proportional to the cell size. As such, resulting 507 images contain less minima, which simplifies the selection 508 procedure. Besides, the variance observed when we change 509 images is explained by the fact that the difficulty of minima 510 evaluation/computation depends on the content of each image. 511



Fig. 7. Computation time comparison with images of the Berkeley database.

We are currently working on a new implementation of minima 512 computation/evaluation which would be less dependent on the 513 number of superpixels.

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To conclude this section, waterpixels are generally faster 515 to compute than SLIC superpixels, and they are at least 516 as performant in the trade-off between adherence to object 517 boundaries and regularity in shape and size, while using much 518 less pixels to describe their contours. 519

V. DISCUSSION AND PERSPECTIVES

We have shown that waterpixels produce competitive results 52 with respect to the state-of-the-art. These advantages are 522 valuable in the classification/detection/segmentation pipeline, 523 where superpixels play the part of primitives. Moreover, there 524 is one major difference in the construction of the algorithm: 525 the SLIC approach does not impose any connectivity con-526 straint. The resulting superpixels are therefore not necessarily 527 connected, which requires some ad hoc postprocessing step. 528 In contrast, waterpixels are connected by definition, and the 529 connectivity constraint is actually implemented in the distance 530 used. 531

The proposed approach is gradient-based. Standard methods 532 can be used to compute this gradient, or a specific gradient 533 computation method can be designed for a given application. 534 In any case, this offers flexibility to waterpixels. One limitation 535 though is the quality of the signal in such a gradient image. 536 As seen in 4, alteration by noise or insufficiently contrasted 537 contours may lead to the prevalence of regularity over adher-538 ence to object boundaries. If filtering steps are usually enough 539 to deal with noise and remove non pertinent small details, 540 parameter values have to be optimized for each database. 541 Future work will aim at overcoming this limitation by adding a 542 learning step of optimal filtering values for specific databases. 543

The general design of waterpixels offers many prospects. 544 Among them, one promising field of improvement resides 545 in the placement of markers, as they constitute the main 546 degree of freedom of the method. We are currently inves-547 tigating the possibility to select the markers in an optimal 548 manner, for example by formulating the marker placement as a 549 p-dispersion problem (see [25]) in an augmented space. 550 MACHAIRAS et al.: WATERPIXELS

The speed of waterpixels contributes to expanding their 551 possible applications. For example, it could be interest-552 ing to compute different sets of waterpixels, by changing 553 design options (different cells, gradients, grid steps, etc.), 554 and then use ensemble clustering methods to obtain a final 555 segmentation [26], [27]. 556

Last buy not least, waterpixels lead to the efficient construc-557 tion of hierarchical partitions based on superpixels. Indeed, 558 the computation of the watershed can produce at the same 559 time a segmentation and a hierarchy of partitions based on 560 that segmentation, with only minor overhead computation 561 times [28]-[30]. 562

VI. CONCLUSION

This paper introduces waterpixels, a family of methods 564 for computing regular superpixels based on the watershed 565 transformation. Both adherence to object boundaries and regu-566 larity of resulting regions are encouraged thanks to the choice 567 of the markers and the gradient to be flooded. Different 568 design options, such as the distance function used to spatially 569 regularized the gradient, lead to different trade-offs between 570 both properties. The computational complexity of waterpixels 571 is linear. Our current implementation makes it one of the 572 fastest superpixel methods. Experimental results show that 573 waterpixels are competitive with respect to the state-of-the art. 574 They outperform SLIC superpixels, both in terms of quality 575 and speed. The trade-off between speed and segmentation 576 quality achieved by waterpixels, as well as their ability to 577 generate hierarchical segmentations at negligible extra cost, 578 offer interesting perspectives for this superpixels generation 579 method. 580

An implementation of waterpixels is available from 581 http://cmm.ensmp.fr/~machairas/waterpixels. 582

APPENDIX

MEAN MISMATCH FACTOR DEFINITION

Let $\{s_i\}_{1 \le i \le N}$ be a set of superpixels. The centered version 585 s_i^* of s_i is obtained by translating s_i so that its barycenter is 586 the origin of the coordinates system. 587

The average shape \hat{s}^* of the $\{s_i\}$ is computed as follows. 588 Let first define function S: 589

 $S: D \longrightarrow \mathbb{N}$

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$$x_p \longmapsto \sum_{i=1}^N 1_i(x_p)$$

(7)

where 1_i is the indicator function of s_i^* . Thus, image S cor-591 responds to the summation image of all centered superpixels. 592 Let furthermore $\mu_A = 1/n \sum_{i=1}^{N} |s_i|$ be the average area of the considered superpixels, and let S_t be the threshold of S at 593 594 level *t*: $S_t(x) = \{x_p \in D | |S(x_p)| \ge t\}.$ 595

The average centered shape \hat{s}^* is then the set S_{t_0} , where t_0 596 is the maximal threshold value which enables \hat{s}^* to have an 597 area greater than or equal to μ_A : 598

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$$t_0 = \max\{t \mid |S_t| \ge \mu_A\}$$
 (8)

$$\widehat{s}^* = S_{t_0} \tag{9}$$

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607 AO:5

610 AQ:6

Finally, the mean mismatch factor of superpixels 601 $\{s_i\}_{1 \le i \le N}$ is: 602

$$MF = \frac{1}{N} \sum_{i=1}^{N} mf(s_i^*, \hat{s}^*).$$
(10) 603

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