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F Remus, S Mathis, J.-P Zahn, V Lainey. The surface signature of the tidal dissipation of the core in a two-layer planet. Metallurgical Transactions A, 2015, 573, pp.A23. 10.1051/0004-6361/201424472. hal-01202655

HAL Id: hal-01202655

https://hal.science/hal-01202655

Submitted on 23 Sep 2015

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The surface signature of the tidal dissipation of the core in a two-layer planet (Research Note)

F. Remus^{1,2,3}, S. Mathis^{3,4}, J.-P. Zahn², and V. Lainey¹

- ¹ IMCCE, Observatoire de Paris UMR 8028 du CNRS Université Pierre et Marie Curie, 77 avenue Denfert-Rochereau, 75014 Paris, France
 - e-mail: francoise.remus@obspm.fr, lainey@imcce.fr
- ² LUTH, Observatoire de Paris CNRS Université Paris Diderot, 5 place Jules Janssen, 92195 Meudon Cedex, France e-mail: jean-paul.zahn@obspm.fr
- ³ Laboratoire AIM Paris-Saclay, CEA/DSM CNRS Université Paris Diderot, IRFU/SAp Centre de Saclay, 91191 Gif-sur-Yvette, France
 - e-mail: stephane.mathis@cea.fr
- LESIA, Observatoire de Paris CNRS Université Paris Diderot Université Pierre et Marie Curie, 5 place Jules Janssen, 92195 Meudon, France

Received 25 June 2014 / Accepted 30 September 2014

ABSTRACT

Context. Tidal dissipation, which is directly linked to internal structure, is one of the key physical mechanisms that drive the evolution of systems and govern their architecture. A robust evaluation of its amplitude is thus needed to predict the evolution time for spins and orbits and their final states.

Aims. The purpose of this paper is to refine a recent model of the anelastic tidal dissipation in the central dense region of giant planets, which are commonly assumed to retain a large amount of heavy elements, which constitute an important source of dissipation. Methods. The previous paper evaluated the impact of the static fluid envelope on the tidal deformation of the core and on the associated anelastic tidal dissipation through the tidal quality factor Q_c . We examine here its impact on the corresponding effective anelastic tidal dissipation through the effective tidal quality factor Q_p .

Results. We show that the strength of this mechanism mainly depends on mass concentration. In the case of Jupiter- and Saturn-like planets, it can increase their effective tidal dissipation by, around, factors 2.4 and 2, respectively. In particular, the range of the rheologies compatible with the observations is enlarged compared to the results issued from previous formulations.

Conclusions. We derive here an improved expression of the tidal effective factor Q_p in terms of the tidal dissipation factor of the core Q_c , without assuming the commonly used assumptions. When applied to giant planets, the formulation obtained here allows a better match between the anelastic core's tidal dissipation of a two-layer model and the observations.

Key words. planetary systems – planets and satellites: gaseous planets – planets and satellites: dynamical evolution and stability – planets and satellites: interiors – planets and satellites: general – planet-star interactions

1. Introduction and motivations

In Remus et al. (2012, hereafter RMZL12), we have studied the tidal dissipation of the anelastic core of a two-layer planet. In that model, the core was assumed to be the main source of tidal dissipation. The envelope was considered as a non-viscous fluid, which was sensitive to the tidal deformation only through its action on shape deformation. The paper derived the tidal dissipation of the core, quantified by the ratio k_2^c/Q_c , where k_2^c is the norm of the complex Love number of second-order at the mean surface of the core $(\tilde{k}_2(R_c))$, and Q_c is its tidal quality factor. Nonetheless, the equations that describe the dynamical evolution of a given satellite are not directly expressed with $Im\left[\tilde{k}_2(R_c)\right] = k_2^c/Q_c$. According to Kaula (1962), for example, the evolution rate of the semi-major axis da/dt is proportional to $R_p^5 k_2^p/Q_p$, where we use "p" sub- and superscripts that relate to the surface of the planet. Thus, the quantity that intervenes

here is the global tidal dissipation, also called the effective tidal dissipation, i.e. the imaginary part of the complex Love number taken at the surface of the planet.

As mentioned in RMZL12, recent studies managed to extract the tidal dissipation of Jupiter (Lainey et al. 2009) and Saturn (Lainey et al. 2012) from astrometric data. This quantity corresponds to the ratio k_2^p/Q_p , assuming that R_p and the other parameters are known. Then, the question is which tidal dissipation in the core is able to account for the observed dissipation. In other words, if one considers, as in RMZL12, that the source of tidal dissipation is restricted to the core, it seems obvious that one has to relate the tidal dissipation in the core to the effective tidal dissipation of the planet, which can be directly compared to the observations. The purpose of this paper is to explicitly derive such a relation. In Sect. 2 we first discuss the limits of application of the standard formulation and its implicit consequences. Then, we show how to derive the effective tidal dissipation, knowing

the tidal dissipation of the core, and taking both the overload and the gravitational attraction exerted by the envelope on the core into account. Finally, Sect. 3 evaluates the strength of this mechanism in giant gas planets.

2. Effective tidal dissipation of a two-layer planet

As assumed in RMZL12, we consider a two-layer planet of radius $R_{\rm p}$, that has homogeneous density $\rho_{\rm c}$ up to the radius $R_{\rm c}$ at which a density jump occurs down to $\rho_{\rm o}$, then staying constant up to the surface of the planet.

2.1. The standard approach

Except for Dermott (1979) and recently RMZL12, none of the studies dealing with the anelastic tidal dissipation of planets or satellites have taken the role of an outer layer surrounding the anelastic region into account as a non-negligible factor that could enhance the tidal dissipation of the core. Thus, since the envelope had no influence on the core, it so far could be omitted. The problem could then be reduced to seeking the tidal dissipation of a homogeneous planet of radius $R_{\rm c}$ and density $\rho_{\rm c}$, which would induce the same satellite migration as the supposed two-layer planet of radius $R_{\rm p}$. In that case, such a quantity would obey, as commonly assumed,

$$\frac{k_2^p}{Q_p} = \left(\frac{R_c}{R_p}\right)^5 \frac{k_2^c}{Q_c}.\tag{1}$$

Nevertheless, this formulation no longer holds if we consider both the gravitational attraction and the overload exerted by the tidally deformed envelope on the core.

2.2. Retroaction of the static envelope

In this section, we show that considering these effects as in RMZL12, Eq. (1) is no longer valid. According to Eq. (6) of Dermott et al. (1988),

$$\frac{k_2^{\rm p}}{Q_{\rm p}} = \left(\frac{R_{\rm c}}{R_{\rm p}}\right)^5 F_{\rm p}^2 \frac{k_2^{\rm c}}{Q_{\rm c}}.\tag{2}$$

In this paper, the authors referred to Dermott (1979) for the definition of the factor F_p , which "is a factor that allows for the enhancement of the tide in the core by the tide in the overlying ocean and for the effects of the density contrast between the core and the ocean".

We derive here an explicit expression of the factor

$$G_{\rm p} \equiv F_{\rm p}^2 = \left(\frac{R_{\rm p}}{R_{\rm c}}\right)^5 \frac{Im\left[\tilde{k}_2(R_{\rm p})\right]}{Im\left[\tilde{k}_2(R_{\rm c})\right]},\tag{3}$$

thanks to RMZL12, where we discussed the weaknesses of Dermott's formulation for the tidal dissipation of the core appearing in the 1979 paper.

The complex Love number is given by $\tilde{k}_2(R_\Lambda) = \tilde{\Phi}'(R_\Lambda)/U(R_\Lambda)$, where U designates the tidal potential, $\tilde{\Phi}'$ the perturbed gravitational potential, and the Λ subscripts stand either for c (for core surface quantities) or p (for planet surface quantities). At any point $P(r, \Theta)$, where r is the distance to the

center of the planet, Θ the angle formed by the radial vector and the line of centers, the tidal potential has the form

$$U(\mathbf{r}) = -\zeta_{\rm c} g_{\rm c} \frac{r^2}{R_{\rm c}^2} P_2(\cos\Theta),\tag{4}$$

where P_2 the Legendre polynomial of second order, g_c the gravity induced by the core at its surface, and

$$\zeta_{\rm c} = \frac{m}{M} \left(\frac{R_{\rm c}}{a}\right)^3 R_{\rm c} \tag{5}$$

is the tidal height at the surface of the core, with m the mass of the perturber and a the semi-major axis of its orbit.

Let us denote the core and planet surfaces by

$$s_c = R_c [1 + S_2 P_2(\cos \Theta)],$$
 (6)

$$s_p = R_p [1 + T_2 P_2(\cos \Theta)],$$
 (7)

respectively. Since there is no physical reason for the surfaces of the core and the envelope to suffer the same deformation, in general, $T_2 \neq S_2$. The way these quantities are linked depends on the effective forces acting on the surface of the core. From here on, we denote by ε the ratio defined by

$$T_2 = \varepsilon S_2. \tag{8}$$

We first consider a purely elastic core. The self-gravitational potential of the planet is the sum of the core and envelope contributions. In the envelope (where $s_c \le r \le s_p$), they are given by Eqs. (49), (50) of RMZL12:

$$\Phi_{\rm c}(r,\Theta) = -g_{\rm c}R_{\rm c} \left[\frac{R_{\rm c}}{r} + \frac{3}{5} \left(\frac{R_{\rm c}}{r} \right)^3 S_2 P_2 \right] , \qquad (9a)$$

$$\Phi_{o}(r,\Theta) = -g_{c}R_{c}\frac{\rho_{o}}{\rho_{c}} \left[\frac{3R_{p}^{2} - r^{2}}{2R_{c}^{2}} + \frac{3}{5} \left(\frac{r}{R_{c}} \right)^{2} T_{2}P_{2} - \frac{R_{c}}{r} - \frac{3}{5} \left(\frac{R_{c}}{r} \right)^{3} S_{2}P_{2} \right].$$
(9b)

Thus, the effective deforming parts are

$$\Phi'(R_{\Lambda}) = -g_{c}R_{c} \left(\frac{R_{\Lambda}}{R_{c}}\right)^{2} Z_{\Lambda}' S_{2} P_{2}(\cos\Theta), \tag{10a}$$

where

$$Z'_{\Lambda} = \frac{3}{5} \left[\frac{\rho_{\rm o}}{\rho_{\rm c}} \varepsilon + \left(1 - \frac{\rho_{\rm o}}{\rho_{\rm c}} \right) \left(\frac{R_{\Lambda}}{R_{\rm c}} \right)^5 \right]$$
 (10b)

Therefore,

$$k_2(\mathbf{R}_{\Lambda}) \equiv \frac{\Phi(\mathbf{R}_{\Lambda})}{U(\mathbf{R}_{\Lambda})} = \frac{R_c}{\zeta_c} Z_{\Lambda}' S_2. \tag{11}$$

The condition that the surface of the planet s_c is an equipotential of the total field $\Phi + U$ leads to

$$\frac{\zeta_c}{R_c} = \frac{2}{5} \frac{\rho_o}{\rho_c} (\alpha \varepsilon - \beta) S_2, \tag{12}$$

where

$$\alpha = 1 + \frac{5}{2} \left(\frac{\rho_{\rm c}}{\rho_{\rm o}} - 1 \right) \left(\frac{R_{\rm c}}{R_{\rm p}} \right)^3; \beta = \frac{3}{5} \left(\frac{R_{\rm c}}{R_{\rm p}} \right)^2 (\alpha - 1).$$
 (13)

We finally obtain the general form of the Love numbers, generalized to the case of a two-layer planet:

$$k_2(R_{\Lambda}) = \frac{5}{2} \frac{\rho_c}{\rho_o} \frac{Z_{\Lambda}'}{\alpha \varepsilon - \beta}.$$
 (14)

All the unknown quantities require the expression of ε to be completely determined. As mentioned before, it depends on the forces acting on the surface of the core. According to RMZL12, the radial displacement at the surface of the core $\xi_r(R_c)$ = $R_c S_2 P_2(\cos \Theta)$ is linked to the total normal traction $T_N(R_c) =$ $XP_2(\cos\Theta)$ applied to it, following

$$S_2 P_2(\cos\Theta) = \frac{\xi_r(R_c)}{R_c} = \frac{5}{19\mu_c} T_N(R_c) = \frac{5}{19\mu_c} X P_2(\cos\Theta), \quad (15)$$

where μ_c is the shear modulus of the core. This traction corresponds to the normal stress acting on the surface of the core, and it has to take both the gravitational forces and the solid and fluid loads into account. Therefore X is given by Eqs. (41) of RMZL12

$$X = \frac{2\rho_{\rm o}g_{\rm c}R_{\rm c}}{5} \left(1 - \frac{\rho_{\rm o}}{\rho_{\rm c}}\right) \left[\left(\alpha + \frac{3}{2}\right)\varepsilon - \beta - \frac{3}{2} - \frac{\rho_{\rm c}}{\rho_{\rm o}}\right] S_2. \tag{16}$$

From Eq. (15), we are now able to write

$$\varepsilon = \frac{\frac{19\mu_{c}}{2\rho_{c}g_{c}R_{c}} + \frac{\rho_{o}}{\rho_{c}}\left(1 - \frac{\rho_{o}}{\rho_{c}}\right)\left(\beta + \frac{3}{2}\right) + \left(1 - \frac{\rho_{o}}{\rho_{c}}\right)}{\left(\alpha + \frac{3}{2}\right)\frac{\rho_{o}}{\rho_{c}}\left(1 - \frac{\rho_{o}}{\rho_{c}}\right)}.$$
(17)

To treat the anelastic case, we can apply the correspondence principle (Biot 1954), stipulating that all the developments made so far are still valid if we now consider complex quantities. We then denote the Fourier transform of a given quantity x by \tilde{x} . The complex Love numbers at the core and planet surfaces can be expressed in terms of $\tilde{\varepsilon}$:

$$\tilde{k}_2(R_c) = \frac{3}{2} \frac{\tilde{\varepsilon} - 1 + \frac{\rho_c}{\rho_o}}{\alpha \tilde{\varepsilon} - \beta}, \text{ and } \tilde{k}_2(R_p) = \frac{3}{2} \frac{\tilde{\varepsilon} + \frac{2}{3}\beta}{\alpha \tilde{\varepsilon} - \beta}.$$
(18)

Thanks to Eq. (18), we are now able to relate the tidal dissipation in the core to the effective tidal dissipation of the planet, given by the imaginary part of the corresponding Love numbers. We denote the real (resp. imaginary) part of $\tilde{\varepsilon}$ by ε_1 (resp. ε_2). The imaginary parts of the Love numbers $\tilde{k}_2(R_c)$ and $\tilde{k}_2(R_p)$ are

$$Im\left[\tilde{k}_{2}(R_{c})\right] = -\frac{k_{2}^{c}}{Q_{c}} = \frac{3}{2} \frac{\left[\left(1 - \frac{\rho_{c}}{\rho_{o}}\right)\alpha - \beta\right]\varepsilon_{2}}{\left(\alpha\varepsilon_{1} - \beta\right)^{2} + \left(\alpha\varepsilon_{2}\right)^{2}},$$
(19a)

$$Im\left[\tilde{k}_{2}(R_{\rm p})\right] = -\frac{k_{2}^{\rm p}}{Q_{\rm p}} = -\frac{3}{2} \frac{\left(1 + \frac{2}{3}\alpha\right)\beta\varepsilon_{2}}{\left(\alpha\varepsilon_{1} - \beta\right)^{2} + \left(\alpha\varepsilon_{2}\right)^{2}}.$$
 (19b)

Equation (2) linking these two quantities then becomes

$$\frac{k_2^{\rm p}}{Q_{\rm p}} = \left(\frac{R_{\rm c}}{R_{\rm p}}\right)^5 G_{\rm p} \frac{k_2^{\rm c}}{Q_{\rm c}},\tag{20a}$$

where G_p takes the form

$$G_{\rm p} = \frac{\alpha + \frac{3}{2}}{\alpha + \frac{3}{2} \left(\frac{R_{\rm c}}{R_{\rm p}}\right)^5}.$$
 (20b)

First, one may note that this quantity is not related to the factor F that accounts for the enhancement of the tidal deformation of the core due to the presence of the envelope (see Eq. (28) of RMZL12). That contradicts Dermott et al. (1988), in which, moreover, no derivation of the formula (given here in Eq. (2)) was detailed. Second, we note that G_p does not depend on ε , which links the amplitudes of the deformation of the core and planet surfaces, hence not on the shear modulus of the core μ_c . It only depends on the density contrast between the core and the envelope (through the ratio $\rho_{\rm o}/\rho_{\rm c}$) and the core size (through its normalized radius R_c/R_p). This result is coherent with our having considered a non-dissipative envelope. Therefore, factor G_p appears like a quantity that characterizes the transmission of the core's tidal dissipation up to the surface of the planet. Last, G_p tends to the value 5/2 of the uniform asymptotic case when either $R_{\rm c}/R_{\rm p} \to 0$ or $\rho_{\rm o}/\rho_{\rm c} \to 1$.

3. Application to Jupiter- and Saturn-like planets

In RMZL12, we used the standard formula (Eq. (1)) to quantify the effective tidal dissipation of Jupiter- and Saturn-like planets when modeled by a two-layer synthetic planet. In the present paper we show how using the refined formula (Eq. (20)) increases its predicted amplitude.

3.1. Internal structure parameters

As explained in RMZL12, we have poor constraints on the internal structure of the giant planets Jupiter and Saturn. Nonetheless, several models have been developed that give some insight into the plausible density profiles in such planets. Following RMZL12, we used the models of Guillot (1999) for Jupiter and Hubbard et al. (2009) for Saturn, from which we are able to build two-layer synthetic planetary models with a dense central icy/rocky core and a fluid envelope made of hydrogen and

- Jupiter-like: $R_c^{\rm J}=0.126\times R_{\rm p}^{\rm J}$ and $M_c^{\rm J}=6.41\times M_{\oplus},$ Saturn-like: $R_c^{\rm S}=0.219\times R_{\rm p}^{\rm S}$ and $M_c^{\rm S}=18.65\times M_{\oplus},$

where M_{\oplus} stands for the mass of the Earth. The most unknown quantities concern the rheology of the predicted core of giant planets. Even so, one may consider some boundary values defining intervals in which the viscoelastic parameters, of the used Maxwell rheological model, are likely to take their values. In RMZL12, we estimated such ranges based on our present knowledge of the rheology of the Earth mantle and the icy satellites of Jupiter (Henning et al. 2009; Tobie 2003).

Recent studies of rocks viscosity at very high pressure (Karato 2011) were also considered. Thus, in RMZL12, the more realistic values of the viscoelastic parameters were assumed to lie in the ranges $10^{12} \, \text{Pa} \, \text{s} \le \eta \le 10^{21} \, \text{Pa} \, \text{s}$ for the viscosity and 4×10^9 Pa $\leq G \leq 10^{11}$ Pa for the rigidity, for an unknown mixture of ice and silicates. We may also extrapolate the range of values taken by G at very high pressure and temperature by using a simple Steinberg-Cochran-Guinam law (Steinberg et al. 1980):

$$G(P,T) = G_0 + \frac{\partial G}{\partial P} \frac{P}{(\rho/\rho_0)^{1/3}} + \frac{\partial G}{\partial T} (T - 300),$$
 (21)

where P, T, ρ , and ρ_0 are the pressure, temperature, density, and density at the reference temperature $T = 300 \,\mathrm{K}$, respectively. Assuming the values of $G_0 = 1.66 \times 10^{11} \,\mathrm{Pa}$, $\partial_P G = 1.56$,

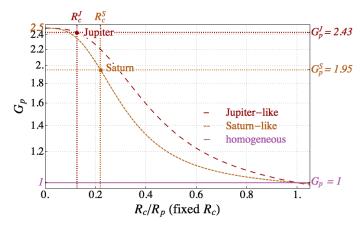


Fig. 1. Factor G_p which quantifies the impact of the fluid envelope on the effective tidal dissipation factor Q_p , as a function of the envelope height through the ratio R_c/R_p .

and $\partial_T G = -0.020\,\mathrm{GPa}\,\mathrm{K}^{-1}$ given by Murakami et al. (2012) for the lower mantle of the Earth, and the rough approximation $(\rho/\rho_0)^{1/3}=1$, the rigidity of silicates at $T=12\,300\,\mathrm{K}$ and $P=2000\,\mathrm{GPa}$ (as intermediate values at the upper boundary of the core of Jupiter and Saturn) reaches the value $G=3\times10^{12}\,\mathrm{Pa}$. In the following, we thus assume, as the most likely values of the viscoelastic parameters,

- for the viscosity: 10^{12} Pa s $\leq \eta \leq 10^{21}$ Pa s,
- for the rigidity: $4 \times 10^9 \, \text{Pa} \le G \le 10^{12} \, \text{Pa}$.

3.2. Impact of the envelope height

Our goal is to quantify the role of the fluid envelope in the effective tidal dissipation. According to Eq. (3), the strength of the associated mechanism is given by the factor G_p , represented in Fig. 1 as a function of the fluid envelope height, for gas giant planets. This figure shows that the effective tidal dissipation increases with the height of the envelope, by a factor of 1.95 to 2.43 for an envelope at least as high as for Jupiter and Saturn.

3.3. Amplitude of the effective tidal dissipation

Using astrometric data, Lainey et al. (2009, 2012) determined the tidal dissipation in Jupiter ($Q_{\text{Jupiter}} = (3.56 \pm 0.56) \times 10^4$) and Saturn ($Q_{\text{Saturn}} = (1.682 \pm 0.540) \times 10^3$), respectively. Figure 2 shows the amplitude of the effective tidal dissipation factor Q_{p} , as given by Eq. (1) for Figs. 2a and c, and Eq. (20) for Figs. 2b and d, as a function of the viscoelastic parameters G and η of the Maxwell model, for the synthetic models of Jupiter and Saturn built in Sect. 3.1, and compares the results with the observed values.

The contour plots of Q_p from Eq. (20) (Figs. 2b and d) are slightly shifted to the bottom and expanded when compared to those resulting from Eq. (1) (Figs. 2a and c), as in Remus et al. (2012). If we only consider the more realistic values of the rheological parameters (as defined in Sect. 3.1), the observed values of tidal dissipation in Jupiter and Saturn are thus reached for slightly enlarged ranges of values of G and η compared with previous results (Table 1).

4. Conclusions

In this work, we revisit the role of the fluid envelope of a twolayer giant planet where the dissipation is assumed to originate

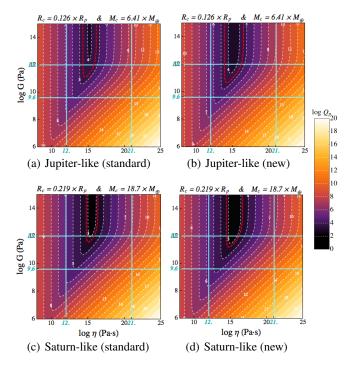


Fig. 2. Effective tidal dissipation factor Q_p of synthetic models of Jupiter (\mathbf{a}, \mathbf{c}) and Saturn (\mathbf{b}, \mathbf{d}) as a function of the viscoelastic parameters G and η : (\mathbf{a}, \mathbf{b}) use Eq. (1) and (\mathbf{c}, \mathbf{d}) use Eq. (20). The red dashed lines give the values of Lainey et al. (2009, 2012). The blue lines bound the region of the most likely rheological values (see text). We assume: $R_p = \{10.97, 9.14\} R_{\oplus} (R_{\oplus} \text{ is the Earth radius}); M_p = \{317.8, 95.16\} M_{\oplus}$.

Table 1. Ranges of values of the rheological parameters G and η for which the effective tidal dissipation factor $Q_{\rm p}$ of the two-layer model reaches the observed values.

(a) Jupiter	
Standard model (Eq. (1))	This paper (Eq. (20))
$G \in [1.28 \times 10^{11}, 10^{12}] \text{ Pa}$	$G \in [4.46 \times 10^{10}, 10^{12}] \text{ Pa}$
$\eta \in [0.18, 6.23] \times 10^{15} \text{ Pa s}$	$\eta \in [0.07, 15.5] \times 10^{15} \text{ Pa s}$
(b) Saturn	
Standard model (Eq. (1))	This paper (Eq. (20))
$G \in [3.52 \times 10^{11}, 10^{12}] \text{ Pa}$	$G \in [1.49 \times 10^{11}, 10^{12}] \text{ Pa}$
$\eta \in [0.59, 6.58] \times 10^{15} \text{ Pa s}$	$\eta \in [0.28, 13.7] \times 10^{15} \text{ Pa s}$

in the anelastic core. We derive an improved formulation of the effective tidal dissipation factor (Eq. (20)), which we express in terms of the tidal dissipation factor of the core obtained by RMZL12. It improves modeling of the role of the anelastic core of giant planets as an important source of tidal dissipation. When applied to the gas giants Jupiter and Saturn, the amplitude of their effective tidal dissipation is enhanced by about a factor of two, thus keeping the same order of magnitude (see Figs. 1 and 2). However, the model now takes all the physical mechanisms that act on the tidal dissipation of the core of giant planets into account. Finally, this new model has recently been used to compare the relative strength of the different tidal mechanisms that take place in gas giant planets, namely the anelastic tidal dissipation in the core (Remus et al. 2012) and the turbulent friction

acting on tidal inertial waves in the convective envelope (Ogilvie & Lin 2004), showing that the former could slightly dominate the latter (Guenel et al. 2014).

Acknowledgements. This work was supported in part by the Programme National de Planétologie (CNRS/INSU), the EMERGENCE-UPMC project EME0911, the CNRS program *Physique théorique et ses interfaces*, the Campus Spatial Université Paris-Diderot, and the L'Oréal France-UNESCO foundation.

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