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# Statistical methodology for the analysis of dye-switch microarray experiments

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We consider a two-color microarray experiment where two treatments are compared, and where the number of slides is fixed.

We expect the experimental design to guarantee

- the balance between the two fluorochromes,
- a good compromise between technical and biological replicates.

We also need **efficient methods** for the statistical analysis of the proposed design.

# Globally balanced design : dye-switch

array	1	2	3	4	5	6	7	8	9	10
Cy5	A1	B2	A3	B4	A5	B6	A7	B8	A9	B10
Cy3	B1	A2	B3	A4	B5	A6	B7	A8	B9	A10

- $A_i$  :  $i^{th}$  biological sample in condition A
- The 10 arrays are independent
- 10 biological replicates per condition, no technical replicate.

The **dye-switch** design is often considered as optimal :

- ★ maximum number of biological replicates,
- ★ variance estimated with 9 *df*,
- ★ the statistical analysis is straightforward.

# Individually-balanced design : dye-swap

array	1	2	3	4	5	6	7	8	9	10
Cy5	A1	B1	A2	B2	A3	B3	A4	B4	A5	B5
Cy3	B1	A1	B2	A2	B3	A3	B4	A4	B5	A5

- 5 pairs of biological samples
- Each pair is used two times (with reverse dyes)
- Each dye-swap is independent of the other ones

The **dye-swap** design is commonly used :

- ★ used when the technical error is high,
- ★ the statistical analysis (after averaging by swap) is straightforward,
- ★ variance estimated with only 4 *df*.

# Individually-balanced : “hybrid” dye-switch

array	1	2	3	4	5	6	7	8	9	10
Cy5	A1	B1	A2	B2	A3	B3	A4	B4	A5	B5
Cy3	B1	A2	B2	A3	B3	A4	B4	A5	B5	A1

- 5 biological replicates per condition
- Each individual is used two times (one with Cy3, one with Cy5).
- Array  $k$  is correlated with  $k - 1$  and  $k + 1$

The **hybrid** design could be an alternative :

- ★ variance estimated with more than 4 *df*.
- ★ the statistical analysis is not straightforward,

⇒ Need of mixed models.

# Statistical model for a gene

After log-transformation :

$$\begin{aligned} X_i &= \mu_A + \delta_{j(i)} + B_{j(i)} + M_i + T_i \\ Y_i &= \mu_B + \delta_{j'(i)} + B_{j'(i)} + M_i + T'_i \end{aligned}$$

$B_{j(i)} \sim N(0, \sigma_B^2)$ ,  $j(i)$  : sample number corresponding to condition *A* and array *i*.

$M_i \sim N(0, \sigma_M^2)$  effect of the spot associated to the gene under concern in microarray *i*

$T_i \sim N(0, \sigma_T^2)$ , includes the steps of labeling, hybridization and measure of intensity of fluorescence.

# Model on the difference of expressions

For slide  $i = 1, \dots, 2n$  :

$$\begin{aligned} D_i &= X_i - Y_i \\ &= \mu + (-1)^{i+1} \delta + BD_i + TD_i \end{aligned}$$

- $\mu = \mu_A - \mu_B$  : true differential expression between  $A$  and  $B$ ,
- $BD_i = B_{j(i)} - B_{j'(i)} \sim N(0, 2\sigma_B^2)$ ,
- $TD_i = T_i - T'_i \sim N(0, 2\sigma_T^2)$ ,
- $\delta = \delta_1 - \delta_2$  : gene-specific dye bias.

$$\begin{aligned} E(D_i) &= \mu + (-1)^{i+1} \delta \\ V(D_i) &= 2\sigma_B^2 + 2\sigma_T^2 \\ \text{cov}(D_i, D_j) &= 0, \text{ except } \text{cov}(D_i, D_{i+1}) = \sigma_B^2. \end{aligned}$$



# Unbiased estimate of $V(\bar{D})$

Unbiased estimator of  $\mu$  :  $\bar{D} = \frac{1}{2n} \sum D_i$

$$V_{\bar{D}} = \frac{1}{2n} (4\sigma_B^2 + 2\sigma_T^2)$$

Naive variance estimate :  $S^2 = \frac{1}{2n-2} \sum_i (D_i - \bar{D}_{(i)})^2$

$$E(S^2) = 2\sigma_B^2 + 2\sigma_T^2 < 4\sigma_B^2 + 2\sigma_T^2$$

Unbiased variance estimate  $C = \frac{1}{2n-4} \sum_i (D_i - \bar{D}_{(i)})(D_{i+1} - \bar{D}_{(i+1)})$

$$E(C) = \sigma_B^2$$

$$S_c^2 = \frac{1}{2n} (S^2 + 2C)$$

$$E(S_c^2) = \frac{1}{2n} (4\sigma_B^2 + 2\sigma_T^2)$$

# Test statistics (for each gene)

Mixed Model with ML estimation (ML)

Mixed Model with REML estimation (REML)

Naive Method (NM)

$$T_N = \sqrt{2n} \frac{\bar{D}}{\sqrt{S^2}}$$

Unbiased Paired Method (UP)

$$T_{UP} = \sqrt{2n} \frac{\bar{D}}{\sqrt{S_c^2}}$$

# Level (in %) of the test procedures (simulation of 10000 genes, nominal level= 5%)

$$\sigma_B^2 = 0.5$$

Method	$n = 5$	$n = 10$	$n = 20$	$n = 30$
NM	7.0 (0.3)	7.3 (0.3)	7.3 (0.3)	7.6 (0.3)
UP	5.2 (0.2)	5.2 (0.2)	5.3 (0.2)	5.3 (0.2)
ML	8.5 (0.3)	8.6 (0.3)	8.3 (0.3)	8.3 (0.3)
REML	4.8 (0.2)	4.2 (0.2)	4.5 (0.2)	4.9 (0.2)

$$\sigma_B^2 = 2$$

Method	$n = 5$	$n = 10$	$n = 20$	$n = 30$
NM	13.2 (0.3)	14.0 (0.3)	14.0 (0.3)	14.2 (0.3)
UP	8.2 (0.3)	6.9 (0.2)	6.0 (0.2)	5.8 (0.2)
ML	12.5 (0.4)	11.1 (0.4)	9.9 (0.3)	9.9 (0.3)
REML	14.7 (0.4)	8.6 (0.3)	5.9 (0.2)	5.5 (0.2)

# Power of UP and REML tests

$\mu = 1$

n	$\sigma_B^2$	UP	REML
5	0.5	13.6	10.6
5	2	5.0	12.9
10	0.5	39.3	34.0
10	2	7.8	9.1
20	0.5	80.1	78.1
20	2	14.5	13.9
30	0.5	95.5	95.0
30	2	22.5	21.7

$\mu = 3$

n	$\sigma_B^2$	UP	REML
5	0.5	92.1	86.7
5	2	29.4	34.7
10	0.5	100	99.6
10	2	63.5	63.1
20	0.5	100	100
20	2	94.8	94.5
30	0.5	100	100
30	2	99.6	99.5

# Compared CPU time

$n$	UP CPU	REML CPU	no REML convergence
5	2.3	787	56.9
10	2.6	212	5
20	2.8	467	0
30	3.2	1046	0.16

User CPU time of procedures UP and REML ( $\sigma^2 = 0.5$ ).

Last column : average number of genes for which REML did not converge.

# Embriogenomics experiment

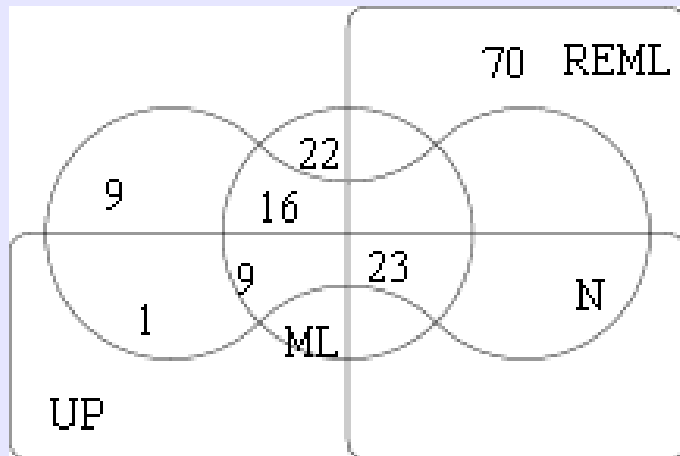
In Mammals, the implantation of the embryo is a key event in the establishment of a pregnancy.

Microarray experiment : 13300 genes in the endometrium of cows. Only 5 animals were available for each condition  $\Rightarrow$  hybrid dye-switch design.

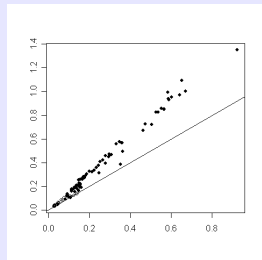
Condition A : cyclic (day 20 of cycle)

Condition B : pregnant (day 20 of pregnancy).

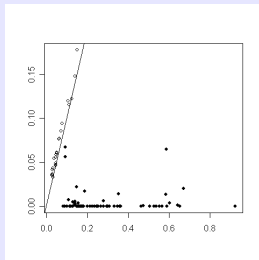
# Number of genes DE found by 4 methods



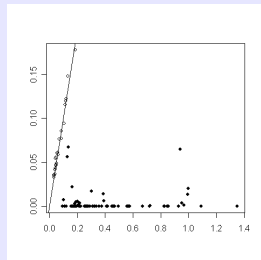
# Plots of variance estimates for 93 genes



x-axis :ML  
y-axis :UP



x-axis :ML  
y-axis :REML



x-axis :UP  
y-axis :REML

black points : classified DE only by REML  
circle : classified DE by all methods.



## Practical guidelines :

- ★ Correlations must be taken into account !
- ★ UP should be preferred to REML (more robust, computationally efficient).
- ★ ANOVA estimators for variances should be considered.

## Extension to more complex designs :

- ★ Loop designs
- ★ Interwoven loop designs

Often proposed for their theoretical properties (Wit et al 05, Altman & Hua 06) but with no practical considerations.

T. Mary-Huard, J. Aubert , N. Mansouri-Attia, O. Sandra & J.J. Daudin (2008), *Statistical methodology for the analysis of dye-switch microarray experiments*, BMC Bioinformatics, **9**, 98.

E. Wit, A. Nobile, & R. Khanin (2005), *Near-optimal designs for dual channel microarray studies*, JRSSC, **54**(5), 817–830

N.S. Altman & J. Hua (2006), *Extending the loop design for two-channel microarray experiments*, Genet. Res., **88**, 153–163