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Investigation on Model Predictive Control of a Five-Phase Permanent Magnet Synchronous Machine under Voltage and Current limits

Xavier Kestelyn, Oleg Gomofov, Jérôme Buire, Frédéric Colas, Ngac Ky Nguyen and Eric Semail
 L2EP, Laboratoire d'Electrotechnique et d'Electronique de Puissance de Lille
 Ecole Nationale Supérieure d'Arts et Métiers (ENSAM) - Campus of Lille
 8 bd Louis XIV F-59046, Lille, France
 Email: Xavier.Kestelyn@ensam.eu

Abstract—The optimal control of electrical drives necessitates to take into account current and voltage limits that are imposed by the power electronics and the electrical machines. Let's cite for example the flux-weakening operation of electrical drives for propulsion. If the control of classical three-phase drives under voltage and current limits are known for a long time, the specific characteristics of multiphase drives open the way to researches on their control under such constraints. This paper aims to explain what are the main differences between three-phase and multiphase drives when they run under voltage and current constraints and try to show what are the scientific and technical problems to be solved. Some first results are given in order to show that Model Predictive Control (MPC) is expected to be a good candidate to answer the proposed challenge.

I. INTRODUCTION

Compared to classical three-phase drives, multiphase drives (having more than three phases) reduce the electrical stresses on machine and power electronic components and have inherent fault-tolerance capabilities [1], [2]. Such advantages lead to the use of multiphase drives on various applications where voltage and current limits can be reached. As an example, the use of a multiphase drive for the propulsion of an electrical car imposes to control the drive in the flux weakening region (where voltage limits are reached) [3],[4],[5]. Although there are still some researches on advanced control of three-phase drives working at their voltage and current limits, the specificity of multiphase drives imposes to develop specific control algorithms.

Electrical drives are mainly composed of electrical machines supplied by Voltage Source Inverter (VSI). The electrical limits that have to be considered when controlling the drive are due to the VSI and the machine itself. The maximum phase peak voltage (voltage limit) comes from the chosen bus voltage and current limits are due to the maximum phase peak current (current limit due to the inverter's switches or the demagnetizing current of the machine) and to the maximum copper losses or RMS phase current (current limit due to the machine). It is considered in this paper that the RMS value never exceeds its maximum. Electrical limits that are

considered are then the followings:

$$v_{phase-to-phase}(t) \leq U_{peak-max} \quad (1)$$

$$i_{phase}(t) \leq I_{peak-max} \quad (2)$$

Control of electrical drives are classically implemented in multiple dq reference frames (extended Park transformation). For a n -phase star-coupled drive, $\frac{n-1}{2}$ dq reference frames are needed. In that case, the k first current harmonics can be correctly tracked in steady-state with the use of simple PI controllers ($k < n$) [1],[2],[6].

For three-phase drives and considering only the voltage and current fundamentals, only one dq reference frame is used. Peak and RMS phase variables are easily related to dq variables since $\sqrt{x_d^2 + x_q^2} = \sqrt{3}X_{peak} = \sqrt{\frac{3}{2}}X_{RMS}$. Optimal control of three-phase drives working at their voltage and current limits is then easy to implement since the control of dq variables ensures the respect of imposed limits. As recalled in [7], below the limits and when the machine has smooth poles, it is sufficient to get a torque equal to its reference $T_{em}^* = T_{em}^*$ to set (considering the speed-normalized emf $\epsilon_q = \frac{e_q}{\Omega}$):

$$i_d^* = 0 \quad (3)$$

$$i_q^* = \frac{T_{em}^*}{\epsilon_q} \quad (4)$$

to ensure an optimal solution (from the copper losses point of view). When the drive works at its limits, it is sufficient to inject a negative current i_d to weaken the machine flux in order to respect the imposed voltage limit $V_{peak-max}$ and to adjust if necessary current i_q in order not to exceed the rated current $I_{peak-max}$. If the machine has salient poles, analytical expressions of i_d^* and i_q^* still exist and the optimal control is then easy to implement. It has however to be noticed that the classical approaches are most of the time applied considering the drive in steady-state (electrical and mechanical dynamics are not taken into account).

For multiphase drives the problem is much more complex since it is necessary to control simultaneously multiple sets of dq variables. Under classical assumptions of linear behaviour of the machine and below voltage and current limits, each dq

set of variables is independent from the other and can then be controlled independently. As proved in [8], for a n -phase PMSM with harmonic rank k of EMF $e(t)$ supposed negligible if $k > n$, the optimal dq currents references (from a copper losses point of view) in order to get a torque $T_{em} = T_{em}^*$ are given by:

$$i_{d_k}^* = 0 \quad (5)$$

$$i_{q_k}^* = \frac{\epsilon_{qk}}{\sum_{i=1}^n \epsilon_{qi}^2} T_{em}^* \quad (6)$$

However, if voltage and current limits are taken into account, computing a set of dq current references for the generation of an expected torque at a given speed is not only a difficult problem to solve but also, from the authors' knowledge, does not have any analytical solution. The difficulty comes from the fact that it is not possible to compute optimal current references since peak and RMS values of phase variables have no analytical relationships. Indeed, the phase peak value of a variable depends on the peak value of each harmonic ($X_{peak_k} = \sqrt{x_{d_k}^2 + x_{q_k}^2} = \sqrt{2}X_{RMS_k}$) but also on their respective phase shifts. When a multiphase drive is subject to voltage and current constraints, simplifications on the expressions of the limits are necessary to get analytical expressions of peak values. One of the most popular assumptions consists in considering that the worst case, when all harmonics are in phase, permanently occurs [9] [10] [11] [12] [13]. In that case, the peak value of a phase variable is easily define by:

$$X_{peak-simplified} = \sum_{i=1}^n \sqrt{x_{d_i}^2 + x_{q_i}^2} \quad (7)$$

It is nothing to say that taking this assumption leads to severe restrictions in the expected performances of the drive.

This paper shows that Model Predictive Control (MPC) is as a good candidate to compute in real-time optimal current references of a PMSM five-phase drive under voltage and current constraints.

II. PRESENTATION OF THE STUDIED DRIVE

The chosen drive is a prototype that has been developed in the frame of an industrial project. It is composed of a star-coupled synchronous permanent magnet machine with five phases denoted A, B, C, D and E . The machine is supplied by a five-leg Voltage Source Inverter (VSI) connected to a DC bus denoted V_{bus} and controlled with Pulse Width Modulation (PWM). Fig. 1 shows a synoptic of the drive.

Speed Ω of the machine shaft is estimated via an incremental optical encoder and is controlled by a PI controller which generates the torque reference T^* . A Model Predictive Control based current reference generator is used to compute the dq current references. These references are compared to the dq currents which are estimated via an extended inverse Park transformation applied to the phase current measurements. Voltage references for the VSI are generated by the dq current

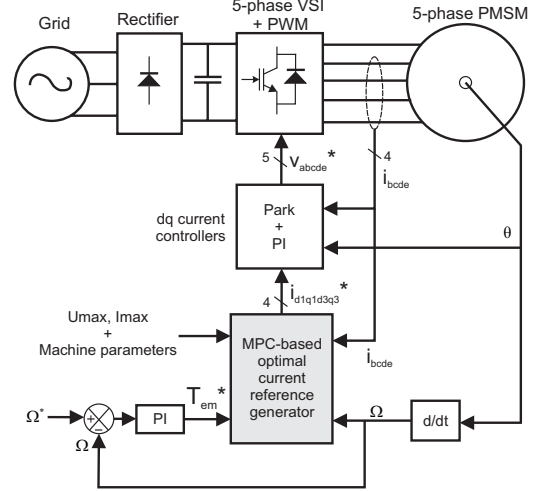


Fig. 1: Synoptic of the studied drive

controls, made with PI controllers, which generate the dq reference voltages.

A. Modelling of the drive

The model of the machine is written in multiple dq reference frames. Equations (8) to (14) are obtained by using the extended Park transformation T given by (15). The fictitious multimachine concept is used in this paper and makes possible to associate a two-phase fictitious machine to each dq subspace [18]. The first fictitious machine is called the Main Machine and is modelled in the dq_1 plane. This machine is associated with the fundamental variables of the real machine. The second fictitious machine is called the Secondary Machine and is modelled in the dq_3 plane. The variables of the Secondary Machine are associated with the third harmonic of the real machine variables. The assumptions that have been used are: 1-The magnetic saturation, the hysteresis effects and the iron losses are not taken into account, 2-Slot effects are neglected, 3-Only harmonic one and three of periodical variables are considered.

$$v_{1d} = Ri_{1d} + L_{1d} \frac{di_{1d}}{dt} - p\Omega L_{1q} i_{1q} \quad (8)$$

$$v_{1q} = Ri_{1q} + L_{1q} \frac{di_{1q}}{dt} + p\Omega \left(L_{1d} i_{1d} + \sqrt{\frac{5}{2}} \Phi_{1f} \right) \quad (9)$$

$$v_{3d} = Ri_{3d} + L_{3d} \frac{di_{3d}}{dt} + 3p\Omega L_{3q} i_{3q} \quad (10)$$

$$v_{3q} = Ri_{3q} + L_{3q} \frac{di_{3q}}{dt} + 3p\Omega \left(-L_{3d} i_{3d} + \sqrt{\frac{5}{2}} \Phi_{3f} \right) \quad (11)$$

$$T_{em1} = p \left[(L_{1d} - L_{1q}) i_{1d} i_{1q} + \sqrt{\frac{5}{2}} \Phi_{1f} i_{1q} \right] \quad (12)$$

$$T_{em3} = 3p \left[(L_{3d} - L_{3q}) i_{3d} i_{3q} + \sqrt{\frac{5}{2}} \Phi_{3f} i_{3q} \right] \quad (13)$$

$$T_{em} = T_{em1} + T_{em3} \quad (14)$$

In equations (8) to (14) appear:

- $v_{1d}, v_{1q}, v_{3d}, v_{3q}$ and $i_{1d}, i_{1q}, i_{3d}, i_{3q}$ the dq_1 and dq_3 voltages and currents respectively associated with the first and the third harmonic of phase variables
- R the phase resistance
- $L_{1d}, L_{1q}, L_{3d}, L_{3q}$ the inductances along d and q axis associated with the first and the third harmonic of the air gap flux
- p the pole pair number
- Ω the speed of the mechanical shaft
- Φ_{1f} and Φ_{3f} the flux along the d axis created by the permanent magnets respectively associated with the first and the third harmonic of the air gap flux
- T_{em1} the electromagnetic torque created by the first harmonic of the air gap flux
- T_{em3} the electromagnetic torque created by the third harmonic of the air gap flux
- T_{em} the total electromagnetic torque

Table I sums up the experimental data of the studied prototype drive developed in the frame of an industrial project.

III. PROPOSED MPC SOLUTION FOR THE REAL-TIME CONTROL OF MULTIPHASE ELECTRICAL DRIVES UNDER VOLTAGE AND CURRENT LIMITS

A. Existing MPC solutions for the real-time control of multi-phase electrical drives

Model Predictive Control (MPC) is based on a model of the system that is used to predict the behaviour of the plant in order to choose optimal values for the control variables. One of the main advantage of MPC is its ability to tackle problems involving multi-input multi-output systems that are subject to constraints, such as imposed limits on the state variables. Because of the computational effort required by MPC, its implementation has been for a long time restricted to slow systems. However, the advance in real-time solutions makes now possible to implement MPC for fast systems with shorter time steps, as power electronics and electrical drives, and become an established control technique in that fields [14].

TABLE I: Data of the studied system

Parameter	Value
Resistance R	9.1m Ω
Inductance L_{d1}	0.13 mH
Inductance L_{q1}	0.13 mH
Inductance L_{d3}	0.051 mH
Inductance L_{q3}	0.041 mH
Flux Φ_{1f}	19.4 mWb
Flux Φ_{3f}	0.675 mWb
Bus voltage V_{bus}	50 V
Maximum peak current per inverter leg I_{VSI}	125 A
Thermal equivalent RMS current I_{TH}	64 A
Maximum expected speed Ω_{max}	16000 rpm

MPC techniques can be divided in two wide categories. Continuous-control-set MPC (CCS-MPC) is based on an average model of the system to be controlled and generates continuous reference signals. Finite-control-set MPC (FCS-MPC) takes advantage of the limited number of switching states available in the power converters for solving the optimization problem using a simple iterative algorithm. The main differences are the way the optimization is performed and how the control actions are applied [15].

MPC researches in the multiphase drive area predominantly relates to the closed-loop current controls. A finite control-set model predictive control (FCS-MPC), which consists in applying at each sampling time the best combination of switching states in order to minimize a cost function, is implemented [16],[17]. The objective is to use FCS-MPC for its ability to offer good transient performances over classical (PI+PWM)-based controls. Unfortunately, with FCS-MPC, voltage and current limits are not optimally taken into account in the proposed algorithms.

B. Proposed MPC solution for the real-time control of multi-phase electrical drives

In this paper, we propose to use a CCS-MPC to generate optimal current references of the drive under voltage and current constraints. Although the developed CCS-MPC generates also the optimal voltage references, it has been preferred to use PI current controls since the CCS-MPC needs a high computation time (around 10 ms), which is not acceptable for a safe current control (slowest electrical time constant equal to 4.5 ms).

The objective is to get the expected torque along the minimization of the copper losses with respect to fixed maximum peak current and voltage. The problem to be solved can be written as follows:

$$\text{minimize} \left(\omega_i (i_{1d}^2 + i_{1q}^2 + i_{3d}^2 + i_{3q}^2) + \omega_T (T_{em}^* - T_{em})^2 \right) \quad (16)$$

subject to:

$$\text{peak} \left(i_{A,B,C,D,E} \right) \leq I_{VSI} \quad (17)$$

$$\text{peak} \left(u_{AB,AC,AD,AE} \right) \leq V_{bus} \quad (18)$$

$$\text{the respect of equations (8) to (14)} \quad (19)$$

The proposed optimization problem can be transformed into a linear problem with a quadratic cost function and linear constraints. The interior-point-convex algorithm given by MATLAB (*quadprog* from the optimization toolbox) has then been chosen to solve the proposed problem.

Equations (8) to (14) are discretized at each sampling instant $k\Delta T$, where ΔT is the sampling time. The discretized model is used to obtain the first-step predicted phase voltages and currents that are used to compute the cost function and to calculate the peak values that constraint the optimization problem. The predictive model is assumed to be time-invariant across the prediction horizon, which implies that the torque

$$T = \sqrt{\frac{2}{5}} \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \cos(p\theta) & \cos(p\theta - \frac{2\pi}{5}) & \cos(p\theta - \frac{4\pi}{5}) & \cos(p\theta + \frac{4\pi}{5}) & \cos(p\theta + \frac{2\pi}{5}) \\ -\sin(p\theta) & -\sin(p\theta - \frac{2\pi}{5}) & -\sin(p\theta - \frac{4\pi}{5}) & -\sin(p\theta + \frac{4\pi}{5}) & -\sin(p\theta + \frac{2\pi}{5}) \\ \cos 3(p\theta) & \cos 3(p\theta - \frac{2\pi}{5}) & \cos 3(p\theta - \frac{4\pi}{5}) & \cos 3(p\theta + \frac{4\pi}{5}) & \cos 3(p\theta + \frac{2\pi}{5}) \\ \sin 3(p\theta) & \sin 3(p\theta - \frac{2\pi}{5}) & \sin 3(p\theta - \frac{4\pi}{5}) & \sin 3(p\theta + \frac{4\pi}{5}) & \sin 3(p\theta + \frac{2\pi}{5}) \end{pmatrix} \quad (15)$$

reference T_{em}^* and the speed Ω remain constant throughout the prediction horizon. The derivative is approximated using a backward Euler method: $\frac{du(t)}{dt} \rightarrow \frac{u(k+1)-u(k)}{\Delta T}$. Currents at instant k are measured, filtered and transformed in order to predict voltages, currents and torque at instant $k+1$.

To be solved by the MATLAB solver *quadprog*, the optimization problem has to be written in a matrix form as follows:

$$\text{minimize} \left(\frac{1}{2} X'(k+1) * H * X(k+1) \right) \quad (20)$$

subject to:

$$A(k) * X(k+1) \leq b(k) \quad (21)$$

$$A_{eq}(k) * X(k+1) = b_{eq}(k) \quad (22)$$

with

$$X(k+1) = \begin{pmatrix} i_{1d}(k+1) \\ i_{1q}(k+1) \\ i_{3d}(k+1) \\ i_{3q}(k+1) \\ v_{1d}(k+1) \\ v_{1q}(k+1) \\ v_{3d}(k+1) \\ v_{3q}(k+1) \\ T_{em}^*(k) - T_{em}(k+1) \end{pmatrix} \quad (23)$$

Matrices $A(k)$, $b(k)$, $A_{eq}(k)$ and $b_{eq}(k)$ are given by (20) to (24).

IV. FIRST RESULTS

Simulations results have been carried out in order to validate the proposed approach. An average model is considered for the VSI. $U_{peak-max} = V_{bus}$ is set to 50 V and $I_{peak-max} = I_{VSI}$ to 125 A. The MPC reference generator has a sampling time of 10ms. The weights ω_i and ω_T define the trade off between the minimization of the copper losses and the tracking of the torque reference. Their values are chosen empirically with $\omega_i \ll \omega_T$ which allows, while always minimizing copper losses, the best tracking of torque reference when it is inside feasible region and having the torque equal to its maximum value when the reference is infeasible. In this work the following values are used : $\omega_i = 0.001$ and $\omega_T = 70$. To avoid numerical problems due to a bad conditioning, it should be noted that the choice of ω_i and ω_T values has to take into account the round-off effects. Too big or too small values are then to be avoided.

The first test consists in verifying the dynamic behaviour of the proposed MPC and its ability of respecting the current limit ($i_{phase}(t) \leq I_{VSI}$). All simulation results are shown in

Figure 2. The initial speed and torque references are set to zero. At $t=0.01$ s the speed is set to 100 rad/s. At $t=0.03$ s the torque reference is set to 25 Nm and at $t=0.06$ s at 75 Nm.

The torque plot shows that due to the sampling time of the MPC-based reference generator, there is a delay of 10ms between the torque and its reference. If the torque reference of 30 Nm can be tracked by the drive, at $t=0.07$ s, the torque is limited to its maximum value, which is equal to 48.2 Nm.

The current plot shows that at $t=0.07$ s the torque is limited because of the current constraint $i_{phase-peak} = I_{VSI}=125$ A. From $t=0.04$ s to $t=0.07$ s the phase shift between first and third current harmonics are opposite in phase in order to get the maximum torque for the minimum copper losses, while from $t=0.07$ s the harmonics are in phase to maximize the peak value of the phase currents. This analysis can also be done by inspecting the dq currents. Since the peak phase-to-phase voltages never reach their limits (set at 50 V), the machine is never flux-weakened and i_{d1} and i_{d3} are always equal to zero. Before the current limit is reached, i_{q1} and i_{q3} are both positive to produce the maximum torque for given copper losses (as stated by (5) and (6)). When the current limit is reached, i_{q3} becomes negative to makes possible to i_{q1} to be the greatest as possible. This very particular functioning mode, which is only possible with multiphase drives, can be considered as a "third-harmonic-based torque weakening".

The second test consists in plotting the maximum torque versus speed characteristic (see Figure 3) in order to validate the ability of the MPC-based current reference generator to respect the voltage constraints. The torque reference is set to its maximum (48.2 Nm) and a speed ramp is imposed to the machine. It has to be noticed that the base speed is equal to 1430 rpm and that the limit speed is over 30.000 rpm. Since we are looking for the maximum torque available, the peak phase currents are always equal to their limits (set at 125 A). Finally, peak phase-to-phase voltages are always inferior or equal to the maximum imposed voltage (50 V in our case).

dq_1 and dq_3 currents have very different behaviours depending on the functioning mode. Before the base speed, the machine is not flux-weaken since i_{d1} and i_{d3} are all set to zero. It has to be noticed that if i_{q1} is positive in order to produce a positive torque with the first harmonic of the flux, i_{q3} , associated with the third current harmonic is negative to get the maximum peak value for the phase currents. When the base speed is reached, as for a classical three-phase machine, the first and the third harmonics of the flux are weakened ($i_{d1} < 0$ and $i_{d3} < 0$). If i_{d1} and i_{q1} are kept respectively positive and negative over the base speed, it is important to note that i_{d3} and i_{q3} are adapted in order to maximize

$$H = \text{diag}(\omega_i, \omega_i, \omega_i, \omega_i, 0, 0, 0, 0, \omega_T) \quad (20)$$

$$A(k) = \begin{pmatrix} T_{0\dots 2\pi}(0) & 0 & 0 \\ 0 & T_{0\dots 2\pi}(0) - T_{0\dots 2\pi}(\frac{2\pi}{5}) & 0 \\ 0 & T_{0\dots 2\pi}(0) - T_{0\dots 2\pi}(\frac{4\pi}{5}) & 0 \end{pmatrix} \quad b(k) = \begin{pmatrix} I_{peak-max} \\ \vdots \\ I_{peak-max} \\ V_{bus} \\ \vdots \\ V_{bus} \end{pmatrix} \quad (21)$$

$$T_{0\dots 2\pi}(\alpha) = \sqrt{\frac{2}{5}} \begin{pmatrix} \cos(-\alpha) & -\sin(-\alpha) & \cos 3(-\alpha) & \sin 3(-\alpha) \\ \cos(\frac{2\pi}{h} - \alpha) & -\sin(\frac{2\pi}{h} - \alpha) & \cos 3(\frac{2\pi}{h} - \alpha) & \sin 3(\frac{2\pi}{h} - \alpha) \\ \cos(2\frac{2\pi}{h} - \alpha) & -\sin(2\frac{2\pi}{h} - \alpha) & \cos 3(2\frac{2\pi}{h} - \alpha) & \sin 3(2\frac{2\pi}{h} - \alpha) \\ \cos(3\frac{2\pi}{h} - \alpha) & -\sin(3\frac{2\pi}{h} - \alpha) & \cos 3(3\frac{2\pi}{h} - \alpha) & \sin 3(3\frac{2\pi}{h} - \alpha) \\ \dots & \dots & \dots & \dots \\ \cos(2\pi - \alpha) & -\sin(2\pi - \alpha) & \cos 3(2\pi - \alpha) & \sin 3(2\pi - \alpha) \end{pmatrix} \quad (22)$$

$$A_{eq}(k) = \begin{pmatrix} R + \frac{L_{1d}}{\Delta T} & -p\Omega L_{1q} & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ p\Omega L_{1d} & R + \frac{L_{1q}}{\Delta T} & 0 & 0 & 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & R + \frac{L_{3d}}{\Delta T} & 3p\Omega L_{3q} & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & -3p\Omega L_{3d} & R + \frac{L_{3q}}{\Delta T} & 0 & 0 & 0 & -1 & 0 \\ p(L_{1d} - L_{1q})i_{1q}(k) & p(L_{1d} - L_{1q})i_{1d}(k) + p\sqrt{\frac{5}{2}}\phi_{1f} & 3p(L_{3d} - L_{3q})i_{3q}(k) & p(L_{3d} - L_{3q})i_{3d}(k) + p\sqrt{\frac{5}{2}}\phi_{3f} & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \quad (23)$$

$$b_{eq}(k) = \begin{pmatrix} \frac{L_{1d}}{\Delta T} i_{1d}(k) \\ \frac{L_{1q}}{\Delta T} i_{1q}(k) - p\Omega \sqrt{\frac{5}{2}} \phi_{1f} \\ \frac{L_{3d}}{\Delta T} i_{3d}(k) \\ \frac{L_{3q}}{\Delta T} i_{3q}(k) - 3p\Omega \sqrt{\frac{5}{2}} \phi_{3f} \\ p(L_{1d} - L_{1q})i_{1d}(k)i_{1q}(k) + 3p(L_{3d} - L_{3q})i_{3d}(k)i_{3q}(k) + T^*(k) \end{pmatrix} \quad (24)$$

the torque produce by the first harmonic of the flux along respecting the current and voltage limits.

This analysis demonstrates that the optimality of the proposed solution is only possible because amplitudes and phase shifts of the third current and voltage harmonics have been adapted in a specific way for each functioning point.

V. CONCLUSION

This paper shows that Model Predictive Control is a good candidate to optimally control in real-time multiphase drives under voltage and/or current constraints. Future works are in progress in order to implement (with FPGA or microcontroller systems) the proposed solution on a five-phase prototype drive that has been developed for industrial purposes.

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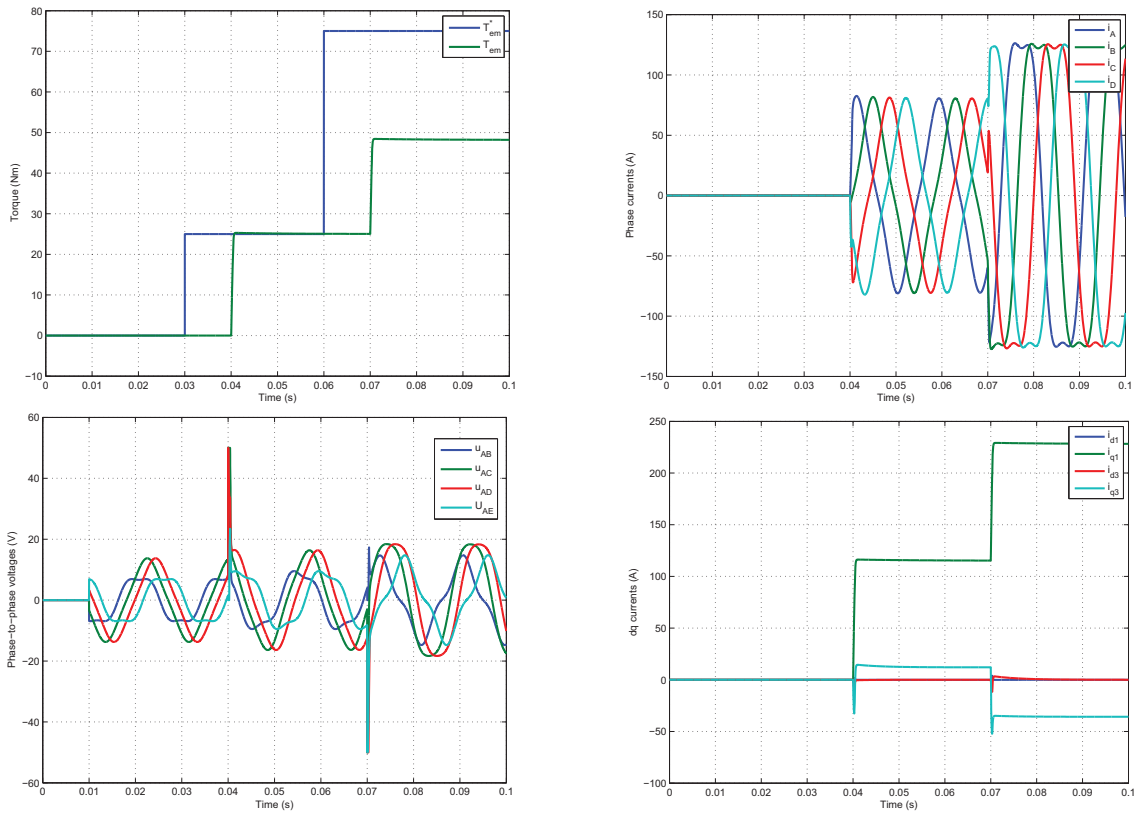


Fig. 2: Simulation results of the first test

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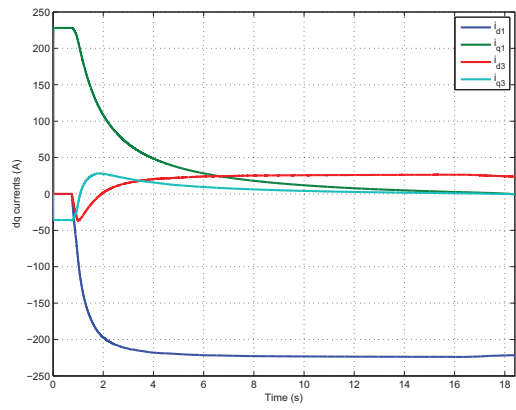
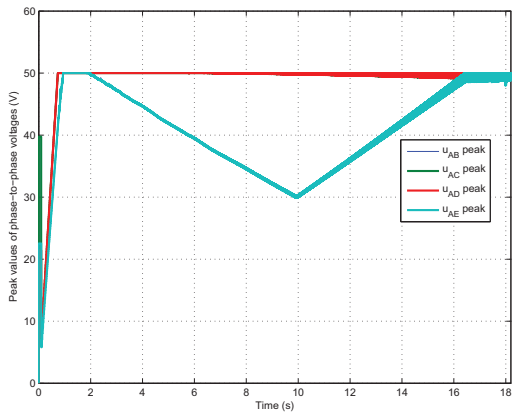
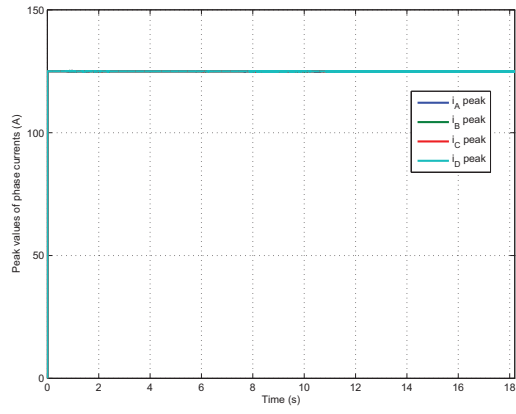
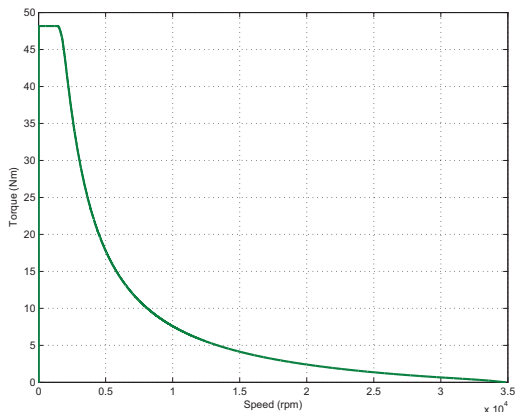


Fig. 3: Simulation results of the second test