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Flame shape transition in a swirl stabilised liquid fueled burner

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Abstract

A laboratory-scale two-stage swirling burner fueled with dodecane is studied experimentally with the help of high speed (20 kHz) spray PIV and chemiluminescence imaging. For a lean operating point at 73 kW, fuel staging is changed and a hysteresis cycle is highlighted. The flame is first lifted from the injector exit plane and exhibits a strong thermo-acoustic instability. The transition to a more stable state is studied by changing the staging parameter while keeping the power constant. Thanks to a well-controlled environment, several runs are performed to ensure that the phenomena observed during these transitions are reproducible. In less than 10 ms, flashback happens in the inner recirculation zone and the flame attaches itself to the injector in a tulip-like shape. The spray then presents a wider angle. Thermo-acoustic instabilities are barely detected and the flame exhibits a strong response to the precessing vortex core. The flame finally widens into a more common V-shaped flame, either in less than 50 ms (for half of the experiments) or after more than 500 ms.

Keywords:

Flame dynamics, bifurcation, staging control, flashback, precessing vortex core

1. Introduction

Because of environmental concerns, increasingly restrictive norms on pollutant emissions of gas turbine plants or aircraft engines have been set up in recent years. Traditionally based on diffusion regimes for reasons of safety and stability, combustion in gas turbines produces large amounts of pollutants such as nitrogen oxides (NO_x) or carbon monoxide (CO). One of the numerous solutions envisaged is to switch to Lean Premixed Prevaporized (LPP) regimes where a more or less uniform lean mixture of fuel and air is supplied in order to reduce flame temperature and thus the emission of thermal NO_x. However, when operated in lean conditions, gas turbines often exhibit strong combustion dynamics that may lead to stability issues such as combustion instabilities, flashback or blowout [1, 2]. In particular, high amplitude self-excited oscillations can happen from the coupling between heat release and acoustic oscillations [3]. These interactions are known to be more

easily triggered in premixed or partially premixed conditions [4]. To tackle this issue, injecting a small amount of fuel upstream leads to the creation of a piloting region that can help in stabilizing the system and reducing the coupling between pressure and heat release. Since multipoint injection leads to a fast and efficient mixing and fuel staging procedures enable the control of the spatial fuel distribution, multipoint staged injectors are good candidates for practical applications. However, their dynamics still have to be studied thoroughly and their impact on flame stabilisation remains yet to be fully understood. Indeed, the simulation of a single sector of an industrial gas turbine recently showed that two different flame stabilisations were possible for the same inlet conditions [5]. The transition between the two states was forced, either by changing the air and fuel flow rates or by strongly modulating them. The purpose of this paper is to present similar phenomena from an experimental point of view in a turbulent swirled multi-injection device fueled with liquid dodecane and to study the naturally occurring transition between two flame shapes. Despite being closer to practical applications, the use of liquid fuel leads to an increased complexity by adding key parameters such as droplet distribution or fuel evap-

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oration that strongly influence flame dynamics [6].

2. Experimental setup and diagnostics

2.1. Experimental Setup

The experimental device BIMER [7, 8] is equipped with a multipoint staged injector based on an industrial geometry where fuel and air can mix. The mixture then flows into a rectangular combustion chamber ($500 \times 150 \times 150 \text{ mm}^3$) with two side silica walls for optical access and three stainless steel water-cooled walls at the top, bottom and entrance of the chamber. Air, controlled by a mass flow controller (Bronkhorst In-Flow), is preheated (Sylvana SureHeat Max) to enhance fuel vaporization and then flows through a plenum before being divided between the two stages of the injector shown in Figure 1.

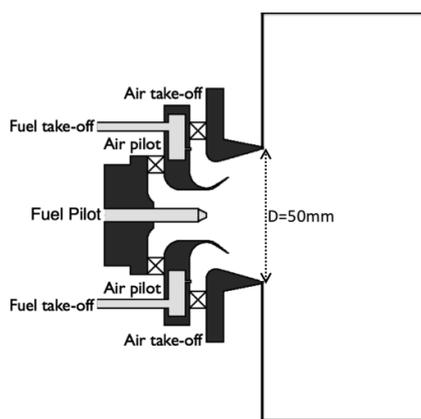


Figure 1: Lateral view of the injection device positioned at the entrance of the combustion chamber, showing the two fuel injection stages and their respective swirlers. Flow from left to right.

The upstream stage, called the pilot stage, contains an 18-vane swirler that is designed to allow around 15% of the global air flow rate to flow through this stage. It is associated with a controlled fuel flow (Bronkhorst Mini Cori-Flow) in a central injection nozzle. This pressurized nozzle (MMP 6390-0-0-03) can inject up to 6.3 l/h of dodecane (flow number: $1.4 \text{ l.h}^{-1} \cdot \text{bar}^{-1/2}$), creating a hollow cone of droplets with a 30° half angle.

The downstream stage, called the take-off stage, contains a 20-vane swirler through which the remaining 85% of the air flows. The fuel, controlled by a Coriolis flowmeter (Bronkhorst Cori-Flow), is injected through a multipoint device with ten equally spaced holes of 0.3 mm in diameter placed at the center of the exit of one swirler vane out of two to ensure proper droplet atomization.

The swirlers of each stage are co-rotating and designed to provide a geometrical swirl number close to 1.

The key parameter to this study being fuel staging, a fuel staging parameter named α has been defined to quantify the amount of fuel injected through the pilot stage [9]:

$$\alpha = \frac{\dot{m}_{f,p}}{\dot{m}_{f,g}} \times 100\% \quad (1)$$

where $\dot{m}_{f,p}$ is the mass flow rate of fuel injected through the pilot stage and $\dot{m}_{f,g}$ is the total fuel flow rate. A value of zero then represents the fact that all the fuel is injected through the take-off stage while $\alpha=100\%$ is associated with a pilot-only fuel injection.

In order to ensure a good repeatability between the experiments, the flowmeters are controlled through an in-house LabView software with a National Instruments PCI-6259 card.

For this study, a global equivalence ratio of 0.6 has been chosen with an air flow rate of 43 g/s. This leads to a thermal power around 73 kW. Air is preheated at about 433 K and the combustion chamber is operated at atmospheric pressure. This operating point was chosen because it shows a strong response to variations of the staging parameter and enough stability to avoid blow-off. A previous study, carried out at a slightly higher operating point (53 g/s of air and same equivalence ratio), found a Sauter mean diameter d_{32} for the droplets around $15 \mu\text{m}$. It led to the conclusion that d_{32} was weakly dependent on α [7].

2.2. Diagnostics

The test bench is equipped with several sensors for acoustic and optical analysis. Four B&K (4938) microphones placed in home-built water-cooled semi-infinite waveguides measure the pressure fluctuations in the plenum and along the chamber axis.

A high-speed camera (Photron Fastcam SA-5) is used to take images of the flame at a rate of 5 kHz. It is equipped with a 50 mm, f:1.4 lens (Nikon). The region of interest is then of $150 \times 150 \text{ mm}^2$ which allows the imaging of the full height of the chamber at the exit of the injector using the camera full frame (1024×1024 pixels). No specific filter is used in order to avoid detrimental decrease of the light signal.

For some of the tests, simultaneous recording of the spray and flame positions at high rates is needed to gather further information on the system. The CH^* spontaneous emission from the flame is thus recorded at 20 kHz with a first high-speed camera (Photron Fastcam SA-X) coupled with a light intensifier (Hamamatsu

C10880-03C) and a 431(± 10) nm filter. With a 105 mm lens, the chamber is imaged on a 150 \times 150 mm² region with 640 \times 640 pixels. On the other side of the chamber, a second high-speed camera (Photron Fastcam SA-5) is equipped with a 50 mm lens and a 532(± 10) nm filter to record the Mie scattering signal from the droplets. It is focused on a laser sheet placed vertically on the axis of the chamber and records a 110 \times 80 mm² region with 704 \times 520 pixels. The laser sheet is created with two Quantronix Nd:YAG lasers firing at 10 kHz each with a delay of 20 μ s between two pulses to enable the use of Particle Image Velocimetry (PIV) techniques.

The signals from the microphones and from the air and fuel flow-meters are acquired with a multiport acquisition card (National Instruments PCI-MIO-16E-4) at a frequency of 8192 Hz.

3. Operating point characterization

As stated above, the operating point is chosen to be around 73 kW with an equivalence ratio of 0.6. The global air flow rate is 43 g/s and the corresponding fuel flow rate is 1.66 g/s. These flow rates are kept constant while the fuel repartition between the pilot and take-off stages is changed so that the staging parameter α varies between 0 and 50%.

On Figure 2, the sound pressure level (SPL) in the chamber is plotted as a function of the staging parameter α . Due to limitations on the acquisition duration at a proper sampling rate, four two-minutes runs were performed during which α is successively varied from 50% to 20%, 20% to 0%, 0% to 20% and finally 20% to 50%. Between these runs, the flame is kept on to avoid any transient effect. Each second, the mean value of α and the SPL are computed and the associated point is plotted on the graph.

As α is decreasing, starting from 50%, the SPL in the chamber is slightly increasing from 132 to 137 dB until α reaches very low values around a few percent. For very low α , the SPL suddenly rises to 145 dB and the combustor reaches a high amplitude limit cycle due to a thermo-acoustic instability associated with the longitudinal quarter-wave mode of the chamber. This loud state remains until α increases back to about 20% where the sound pressure level drops to values similar to those obtained when decreasing α .

A clear hysteresis cycle is then drawn and two different flame behaviours are shown to coexist for the same fuel staging depending on the path leading to this operating point. The main purpose of this paper is to study the flame state transition happening at the exit of the

hysteresis cycle, from the loud state to the quieter one (α close to 20% in Figure 2).

To gather enough data, 37 similar experiments were performed with slightly varying preheating temperatures (from 153 to 167°C), depending on the preheating power and the ambient air temperature. In all these runs, the SPL in the chamber due to the thermo-acoustic instability ranges from 141 to 148 dB and the value of α at the instant of the transition (namely when the signal from the microphone drops) is on average 19.1% with minimum and maximum values of 16.8 and 21.8% respectively. This transition value is named α_t in the remaining of the paper. There seems to be a small impact of the preheating temperature on the value of α_t since the transition happens, on average, for smaller staging values when the preheating is higher. Despite this slight variability, the transition event itself remains the same and the flame and spray shapes before and after the transition do not change between runs.

4. States before and after the transition

During the transition event, not only does the SPL drop but the flame shape also changes dramatically. Durox *et al.* showed that different flame stabilizations for the same operating points led to different dynamic flame behaviours [10]. Before analysing this change in stabilization, it is first necessary to describe the states just before and just after the transition.

4.1. Flame and spray shapes

As stated in section 2, some of the experiments were performed with a simultaneous recording of the flame CH* chemiluminescence and Mie scattering signal from the droplets. The Mie scattering images are treated with a PIV software (Dantec Dynamic Studio, adaptive correlation with 2 refinement steps, 16 \times 16 final window size with 50% overlap) to obtain velocity fields which are then conditioned depending on the presence of droplets. From these treatments and recordings, mean droplet velocity and Abel-inverted mean CH* spontaneous emission are computed before and 500 ms after the transition. During these 500 ms the injection conditions are almost constant as compared to the instant of transition, since this delay is below the liquid flowmeters characteristic timescale. The mean droplet velocity magnitude and flame shape are visible on Figure 3. On these mean images, it must be kept in mind that spray and flame can coexist in the same region because of intermittency.

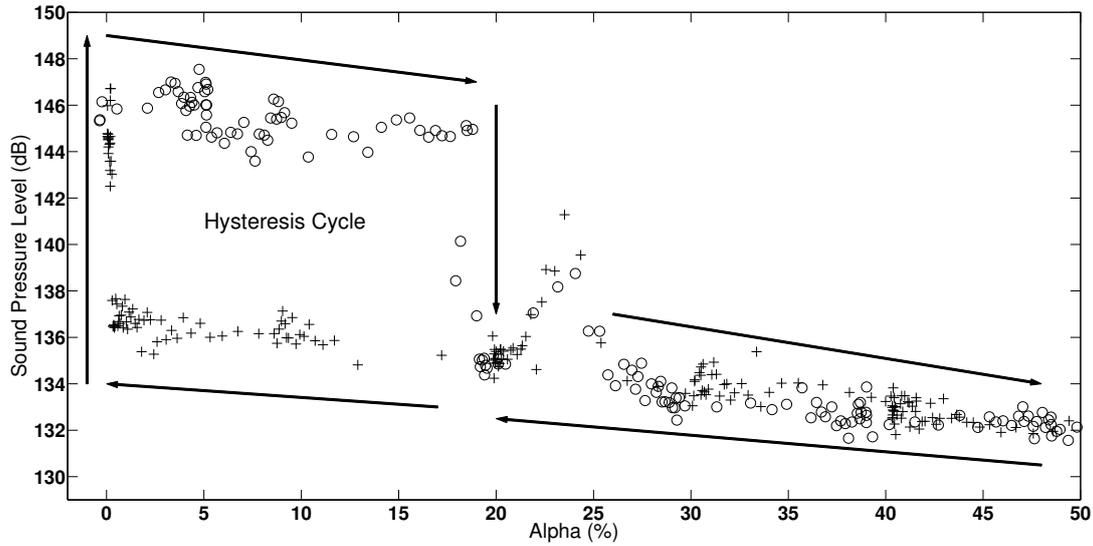


Figure 2: Evolution of the sound pressure level in the chamber as a function of the fuel staging parameter α . The plus signs represent decreasing values and the circles increasing values of the staging parameter.

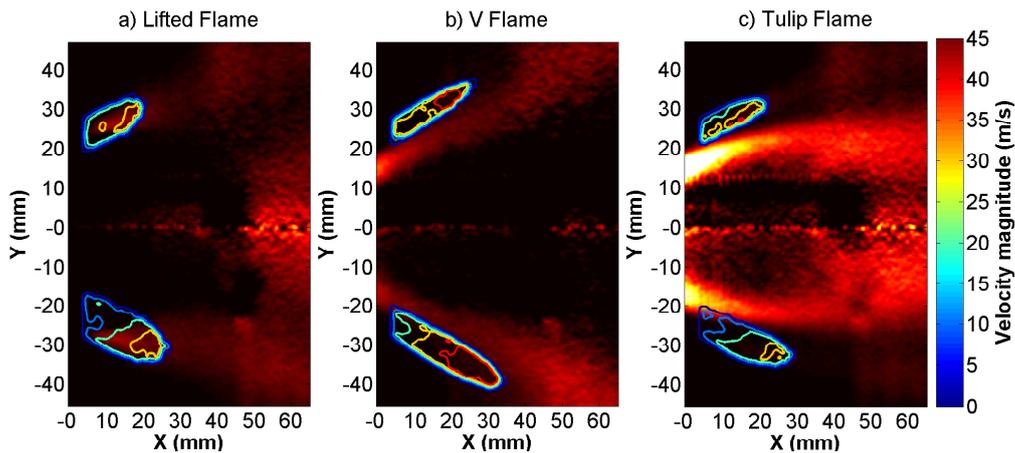


Figure 3: Abel-inverted mean CH^* chemiluminescence (image) and mean droplet velocity magnitude (contours) for the stable states before and after the transition. Flow from left to right.

Before the transition, as shown in section 3, the flame triggers a strong thermo-acoustic instability with, extracted from the 37 experiments, an average frequency of 329 Hz and minimum and maximum values of 320 and 344 Hz. From the flame and spray shapes presented on Figure 3a, it can be noted that the mean spray is quite thick with a small half angle (13°). This comes from the fact that, because of the thermo-acoustic instability, the fuel droplets are spread over a much wider area in the chamber than for the quieter states. The fuel droplets in the spray have a mean velocity magnitude around 25 m/s. Most of the signal from the mean flame comes from the downstream part of the chamber and

there is no signal around the injector lips. This means that the flame is not attached to the injector but *lifted* downstream in the chamber. Some signal however appears in the top and bottom parts of the upstream region ($Y = \pm 30$ mm) because of intermittent reactions seemingly happening in the Outer Recirculation Zone (ORZ). Overall, the spray is mainly surrounded by the flame.

After the transition, two different states can be obtained and the resulting flame and spray shapes can be seen on Figures 3b and 3c. Neither of these flames exhibit any thermo-acoustic instabilities even if large SPL values are still encountered due to broadband noise. On Figure 3b, the V state, named after the shape of the

flame, is visible. It occurred for 20 out of 37 experiments. The spray region is thinner than for the *lifted* state and has a wider half angle (26°). The mean velocity magnitude of the droplets is higher here than for the *lifted* case (more than 35 m/s), probably because of a smaller flow area due to the presence of the flame. On the contrary to the *lifted* state, the flame is surrounded by the spray and seems to have roots inside the injector, it can thus be considered as an attached flame. It has a wide angle and opens up downstream in a typical fashion for swirled flames [11, 12].

The flame and spray shapes for the second type of state that occurred after the transition for the remaining 17 runs out of 37 can be seen on Figure 3c. The spray in this state is quite similar to the one for the V-shaped flame albeit less opened (17°). The droplet velocity is however lower than in the V case (around 30m/s). The flame is also attached in the injector but it does not widen downstream and keeps a *tulip*-like shape. While the spray is mainly outside of the flame, some chemiluminescence signal can however be found further outside. These reaction zones ($Y=\pm 30\text{mm}$) are quite similar to those found for the *lifted* state because of the intermittency in the ORZ. The spray can then be considered as surrounded on both sides by the flame.

Although it seems steady over hundreds of milliseconds, this *tulip* state is however not completely stable and the flame eventually widens into a V-shaped flame after a few seconds. Despite the use of several methods, no discrimination criterion between the two states after the transition could be extracted from the global parameters (air and fuel flow rates, temperature, acoustic characteristics of the *lifted* state, etc).

4.2. Dynamics of the attached states

Dynamic Mode Decomposition (DMD) analyses [13] have been performed on the spontaneous emission data (600 samples at 5 kHz) for the V and *tulip* states. Both of them exhibit a strong anti-symmetric mode around 2100 Hz (2081 Hz on average). Previous studies on the same setup [8] showed that this mode can be associated with a rotating helical vortical structure often found in flows with high swirl numbers, the Precessing Vortex Core (PVC) [14–17]. No PVC is detected in the *lifted* state, probably because of the thermo-acoustic instability as previously observed by Moeck *et al.* [18].

To allow comparisons between the runs, the impact intensity of the PVC on the flame is computed from the DMD spectrum as the height of the peak at the PVC frequency divided by the baseline (median value between 2000 and 2200 Hz). The variability (computed with the same procedure on different parts of the same run) of

this treatment is around ± 0.2 , which is quite high but the amount of runs enable tendencies to be drawn. The resulting values are plotted as a function of α_t on Figure 4. For the V flame, the impact of the PVC on the flame seems to be increasing with α_t . This may be due to the fact that the main chemiluminescence intensity zone for higher values of α in the V state seems to move a bit closer to the injector, which is where the PVC is more intense. A similar tendency can be observed for the *tulip* state even though the points are more scattered. Nevertheless, for a given α_t , the *tulip* flame systematically shows a stronger response to the PVC than the V flame.

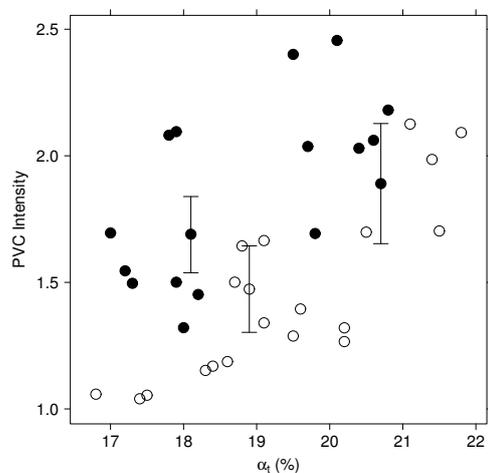


Figure 4: Intensity of the impact of the PVC on the flame after the transition versus the transition staging parameter α_t for the two attached states. Circles: V-shaped flame. Black dots: *tulip*-shaped flame. Three error bars are added to give an overview of the variability.

A similar DMD treatment has been performed on the Mie scattering images and the presence of an anti-symmetric mode around 2100 Hz is detected for all the *tulip* and V states. The PVC has then indeed an effect on the fuel spray. However, its intensity changes neither with α_t nor between the two states. What can be seen on Figure 4 is thus the result of the interaction between the PVC and the fuel vapor and/or the flame but does not reflect a change in the aerodynamical structure itself.

5. Progress of the transition event

Now that the states before and after the transition are clearly defined, the transition itself can be investigated. First, the evolution of the flame shape during the transition is studied and then focus is put on the very first step of the transition.

5.1. Evolution of the flame shape during the transition

To follow the evolution of the flame shape during the transition and precisely define in which state the flame is, 2D-correlation is used. For each chemiluminescence frame recorded, three correlation coefficients associated with the mean flame shape of each stable state (*lifted*, *tulip* and *V*) are computed using the following formula:

$$C_M(t) = \frac{\sum_m \sum_n (X_{mn}(t) - \bar{X}(t)) (\overline{M_{mn} - \bar{M}})}{\sqrt{\left(\sum_m \sum_n (X_{mn}(t) - \bar{X}(t))^2 \right) \left(\sum_m \sum_n (\overline{M_{mn} - \bar{M}})^2 \right)}} \quad (2)$$

where X is the instantaneous image of the flame, M the mean image of chemiluminescence in the considered state and the overline denotes the spatial averaging operation. A high correlation coefficient means that the instantaneous flame shape is sufficiently close to the mean flame shape of one of the stable states to be considered in this state. The evolution of these three correlation coefficients with the frame number (frame rate: 5kHz) is plotted on Figure 5 for a typical transition that ends up with a *V* flame.

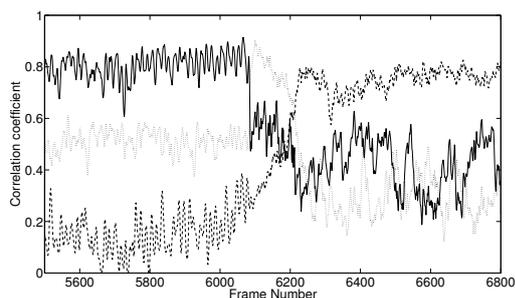


Figure 5: Evolution of the flame shape correlation coefficient during the transition. The solid line represents the correlation coefficient with the *lifted* flame, the dotted line the correlation with the *tulip* flame and the dashed line the correlation with the *V* flame. The frame rate is 5,000 fps.

First, it can be seen that the transition itself is a very fast phenomenon since most of the graph shows either a very high correlation with the *lifted* state in the beginning or a high correlation with the *V*-shaped flame in the end. The change between the two states (ie the transition itself) actually happens between the frames 6000 and 6300, that is in the order of 50 ms. An interesting feature in this window is that, for a few frames, the instantaneous flame shape correlates well with the mean shape of the *tulip* state and then ends up widening in the *V* shape. It means that, even if it ends up in a *V* shape, the flame always goes through a *tulip* phase. This behaviour is confirmed by the analysis of the whole set of transitions. Two steps can then be defined. The first one is the attachment of the flame from the *lifted* state to a

tulip shape and the second one is the widening of the flame into a *V* shape. This widening can occur a long time after the first step (more than half a second) meaning that the shape seen after 500 ms is still a *tulip* (figure 3c). This second step may also occur very quickly and the final state is then a *V* flame (figure 3b). In the latter case, the *tulip* shape lifetime ranges from 14 to 46 ms with an average value of 23 ms which is more than an order of magnitude shorter than the shortest stable *tulip* state described in section 4.

5.2. Focus on the attachment step

The first step of the transition is the instant when the *lifted* flame gets anchored inside the injector with a *tulip* shape. It is studied using the intensified high-speed camera at 20kHz that allows a good decomposition of the flame motion. Several pictures extracted from the resulting movie are visible on Figure 6.

The first image (top left) shows an instantaneous *lifted* flame. The reaction zone is mainly located in the downstream part of the chamber, 30 mm away from the injection plane. On the next three images, a filament of flame can be seen in the center of the chamber, moving towards the injector. This is a flashback happening in the Inner Recirculation Zone (IRZ). This step takes one to two milliseconds to occur and the flame filament ends up igniting the injector region as can be seen on the fifth frame. This kernel of flame is then convected downstream by the flow on the next two pictures. This ends up in a *tulip*-shaped instantaneous flame visible on the last picture. This “ignition” phenomenon through a flashback inside the IRZ is the mechanism causing the change in the relative positions of the flame and spray. The effect of flashback in flame bifurcations was already highlighted by Huang *et al.* [19] in a numerical simulation. The main difference here is that the flashback happens in the IRZ and not near a wall.

Overall, the duration of this attachment phenomenon, from the *lifted* state to the *tulip* flame, is around 5 to 10 ms. Interestingly, other similar IRZ flashbacks occur before the transition but they do not end up with a successful ignition inside the injector as the final one does. The key parameters associated with a successful ignition remain however yet to be found. As noticed in section 3, α_t seems to be lower for higher preheating temperatures, possibly an effect of fuel vaporization. Another key parameter is probably the instantaneous aerodynamic field inside the IRZ and the injector to ensure a proper flashback and a strong ignition in the premixing zone. Further techniques such as local time-resolved equivalence ratio measurements, which are out of reach for the moment, or 3D instantaneous velocity

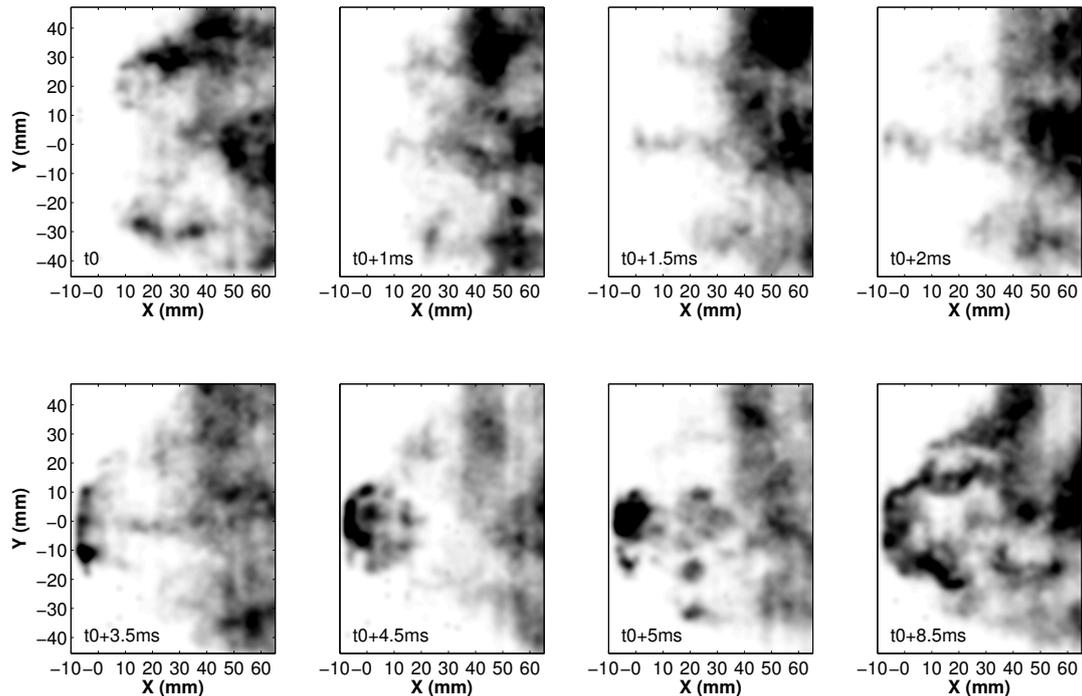


Figure 6: Evolution of the attachment step extracted from a CH* chemiluminescence high speed movie (20,000 fps). The camera is slightly tilted to allow a better imaging of the injector exit. A grayscale, saturated on the white (zero) side, is used to clearly identify the flame front propagation. Flow from left to right.

fields would clearly help in suggesting a proper mechanism for the phenomenon. A lead to follow up is the use of Global Rainbow Thermometry (GRT) [20] which may provide time-resolved average size and temperature of the fuel droplets in a probe volume.

6. Conclusion

Flame transitions in a well controlled turbulent swirl-stabilised spray combustor were experimentally studied with time-resolved diagnostics. All the studied transitions switch from a *lifted* state with a strong thermoacoustic peak around 330 Hz to a *tulip*-like shape with a strong signature of an helical structure around 2100 Hz that is associated with the flow PVC. The transition scenario is an initial flashback in the center of the injector that forces the spray cone to open towards a wider angle and allows the flame to be entrapped in the IRZ. The obtained *tulip* flame eventually degenerates into a more conventional V-shaped flame, found in many pilot-stabilised burners.

While all transitions exhibit this scenario, they differ in the lifetime of the *tulip* shape, showing a bimodal distribution. About half of the events have a lifetime lower than 50 ms whereas the other half show lifetimes

larger than 500 ms. The fact that no widening happens between these two timescales leads to think that the process hidden behind is not entirely stochastic although its key parameters remain to be found.

To perform further investigation on this phenomenon, 3D diagnostics providing key values (aerodynamic field unsteadiness, local equivalence ratio) are needed as well as additional experiments to enable the use of powerful data analysis tools such as principal component analysis for example.

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