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Preserving syntactic correctness while editing mathematical formulas

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GNU $\text{\TeX}_{\text{MACS}}$ is a free software for editing scientific documents with mathematical formulas, which can also be used as an interface for many computer algebra systems. We present the design of a new experimental mathematical editing mode which preserves the syntactic correctness of formulas during the editing process (i.e. all formulas can be parsed using a suitable, sufficiently rich grammar). The main constraint is to remain as closely as possible to the existing presentation-oriented formula editor, which has the advantage of being very user friendly.

KEYWORDS: mathematical editing, syntactic correctness, packrat parsing, $\text{\TeX}_{\text{MACS}}$
A.M.S. SUBJECT CLASSIFICATION: 68U15, 68U35, 68N99

1. INTRODUCTION

Most mathematical formulas in current scientific papers only carry very poor semantics. For instance, consider the two formulas $f(x + y)$ and $a(b + c)$. People typically enter these formulas using the \LaTeX pseudo-code $\text{\$f(x+y)\$}$ and $\text{\$a(b+c)\$}$. Doing so, we do not transmit the important information that we probably meant to apply f to $x + y$ in the first formula and to multiply a with $b + c$ in the second one. The problem to automatically recover such information is very hard in general. For this reason, it would be desirable to have mathematical authoring tools in which it is easy to write formulas which systematically carry this type of information.

One important application where semantics matters is computer algebra. Popular computer algebra systems such as MATHEMATICA and MAPLE contain formula editors in which it is only possible to input formulas which can at least be understood from a syntactical point of view by the system. However, these systems were not really designed for writing scientific papers: they only offer a suboptimal typesetting quality, no advanced document preparation features, and no support for more informal authoring styles which are typical for scientific papers.

The GNU $\text{\TeX}_{\text{MACS}}$ editor was designed to be a fully fledged wysiwyg alternative for $\text{\TeX}/\text{\LaTeX}$, as well as an interface for many computer algebra systems. The software is free and can be downloaded from <http://www.texmacs.org>. Although formulas only carried barely more semantics than \LaTeX in old versions of $\text{\TeX}_{\text{MACS}}$, we have recently started to integrate more and more semantic editing features. Let us briefly discuss some of the main ideas behind these developments; we refer to [7] for more details and historical references to related work.

First of all, we are only interested in what we like to call “syntactical semantics”. In the formula $2 + 3$, this means that we wish to capture the fact that $+$ is an infix operator with arguments 2 and 3, but that we are uninterested in the fact that $+$ stands for addition on integers. Such syntactical semantics can be modeled adequately using a formal grammar. Several other mathematical formula editors are grammar-based [1, 2, 3, 8, 10, 11], and they make use of various kinds of formal grammars. In $\text{\TeX}_{\text{MACS}}$, we have opted for so called packrat grammars [4, 5], which are particularly easy to implement and customize.

A second question concerns the precise grammar that we should use to parse formulas in scientific documents. Instead of using different grammars for various areas with different notations, we were surprised to empirically find out that a well-designed “universal” mathematical grammar is actually sufficient for most purposes; new notations can still be introduced using a suitable macro mechanism.

The last main point concerns the interaction between the editor and the grammar. So far, we implemented a packrat parser for checking the correctness of a formula. While editing a formula, its correctness is indicated using colored boxes. It is also possible to detect and visualize the scopes of operators through the grammar. In addition to the parser, we implemented a series of tools which are able to detect and correct the most common syntactical mistakes and enhance existing documents with more semantics.

In the present paper, we wish to go one step further and enforce syntactic correctness throughout the editing process. Ideally speaking, the following requirements should be met:

- As far as user input is concerned, there should be no essential difference between editing formulas with or without the new mechanism for preserving syntactic correctness. For instance, we do not wish to force users to provide additional “annotations” for indicating semantics. It should also be possible to perform any editing action which makes sense from the purely visual point of view.
- The implementation should be as independent as possible from the actual grammar being used. In other words, we strive for a generic approach, not one for which specific editing routines are implemented for each individual grammar symbol.

The main technique that we will use for sticking as close as possible to the old, presentation oriented editing behaviour is to automatically insert “transient” markup for enforcing correctness during the editing process. For instance, when typing $x +$, $\text{\texttt{TeX_MACS}}$ will display

$$x + \square$$

The transient box is used to indicate a missing symbol or subexpression and will be removed as soon as the user enters the missing part.

The use of transient boxes for missing symbols or subexpressions is common in other editors [9]. The question which interests us here is how to automatically insert such markup when needed in a way that is essentially independent from specific grammars. In this paper, we work out the following approach which was suggested in [7]: before and after each editing operation, subject the formula to suitable “correction” procedures that are only allowed to add or remove transient markup. Correcting all errors in a general formula is a very difficult problem, but the power of our approach comes from the fact that the editing process is incremental: while typing, the user only introduces small errors—mostly incomplete formulas—, which are highly localized; we may thus hope to deal with all possible problems using a small number of “kinds of corrections”.

Obviously, the simplest kinds of corrections are adding or removing a transient box at the current cursor position. This is indeed sufficient when typing simple formulas such as $x + y + z$, but additional mechanisms are needed in other situations. For instance, in the formula $\alpha + \beta$ (with the cursor between the “+” and the “ β ”), entering another + results in $\alpha + \square + \beta$ (instead of $\alpha + + \square \beta$ or $a + + b$). Hitting backspace in the same formula $\alpha + \beta$ yields $\alpha + \beta$; in this case, the transient “+” should be parsed as an infix addition, and not as an ordinary symbol (as was the case for a transient box).

The appropriate corrections are not always so simple. For instance, consider the quantified expression $\forall x, \exists y, P(x, y)$. Just after we entered the existential quantifier “ \exists ”, the formula will read $\forall x, \exists \square, \square$, i.e. it was necessary to add three transient symbols in order to make the expression syntactically correct. The fact that our approach should apply to general scientific documents with mathematical formulas raises several further problems. For instance, in the formula

$$a^2 + b^2 = c^2,$$

the trailing punctuation “,” is incorrect from a mathematical point of view, but needed inside the surrounding English sentence. Similarly, more work remains to be done on the most convenient way to include English text inside formulas while maintaining syntactic correctness.

Yet another difficulty stems from the implementation: one needs to make sure that the necessary corrections take place after *any* kind of editing operation. However, for efficiency reasons, it is important to only run the correction procedures on small parts of the document. Inside an existing editor such as $\text{\TeX}_{\text{MACS}}$, these requirements turn out to be quite strong, so some trade-offs may be necessary.

In what follows, we report on our first implementation of these ideas inside $\text{\TeX}_{\text{MACS}}$. We describe and motivate the current design, discuss remaining problems, and outline directions for future improvements. Of course, more user feedback will be necessary in order to make the new mechanisms suitable for wide-spread use.

2. SURVEY OF FORMULA EDITING WITH $\text{\TeX}_{\text{MACS}}$

In this section, we briefly recall the main design philosophy behind the $\text{\TeX}_{\text{MACS}}$ formula editor. We start with the description of the original, purely presentation-oriented mathematical editing mode. We pursue with the more recent grammar-based editing features, which are presented in more detail in [7].

2.1. Presentation oriented editing

The original goal behind $\text{\TeX}_{\text{MACS}}$ was to provide a user friendly editor for mathematical papers with a similar typesetting quality as \TeX . The challenge was to design a real time wysiwyg editor for complex, structured documents. Some early inspiration came from the idea [1] that graphically oriented math editors achieve the highest level of user friendliness. For instance, when pressing the right arrow key, the cursor should move to the right if possible (instead of moving forward in some abstract document tree, as was the case in some other existing editors). Early versions of $\text{\TeX}_{\text{MACS}}$ used algorithms for the cursor movement which achieved this in a systematic way [6], while still making sure that all possible cursor positions in the corresponding document tree could be reached.

Another aspect of user friendliness concerned the efficiency of mathematical input methods. We designed highly efficient (and easy to memorize) keyboard shortcuts for entering common mathematical symbols, such as \rightarrow for \rightarrow , \leq for \leq , \notin for \notin , \mathbb{R} for \mathbb{R} , etc. $\text{\TeX}_{\text{MACS}}$ also implements many “structured editing operations”, so as to fully exploit the structure of documents. For instance, adding a row or column to a matrix can be done by pressing a single key or keyboard combination. Similarly, it is easy to change a matrix into a determinant or *vice versa*.

2.2. Grammar-based editing

The next challenge for $\text{\TeX}_{\text{MACS}}$ is to ensure that we can only enter syntactically correct formulas, while keeping a presentation-oriented interface, which proved to be most user friendly. The first steps of this program were made in [7]. Now syntactic correctness is usually modeled as “parsability against a suitable grammar”. Before anything else, one should decide on the grammar. In particular, does a single “universal grammar” suffice, or do we need many different grammars, depending on the preferred notations of authors?

For reasons that are explained in detail in [7], we opted for the development of a universal packrat grammar [4, 5] for parsing all our mathematical formulas. In order to conserve a sufficient degree of flexibility for the introduction of new notations, we rely on a combination of two techniques: on the one hand, $\text{\TeX}_{\text{MACS}}$ comes with a powerful macro language for introducing new markup elements. On the other hand, we introduced a special construct which allows a symbol or expression to behave (i.e. be parsed) as an arbitrary other symbol or expression. This allows you for instance to annotate the symbol \vee to behave as $+$, which implies that $a = b \vee c$ will be parsed as $a = (b + c)$ instead of $(a = b) \vee c$.

One of the major difficulties of semantic editing is a clean treatment of *homoglyphs*, i.e. symbols with the same graphical shape, but a different syntactical meaning. The most annoying homoglyph is the multiplication/function-application ambiguity mentioned in the introduction. Another good example concerns the wedge product $dx \wedge dy$ and logical conjunction $a = b \wedge x = y$, which admit different binding forces. Fortunately, there are not that many mathematical homoglyphs; for this reason, we advocate the introduction of separate symbols for them into the UNICODE standard.

icon and checking Semantic correctness.

3.1. The ideal strategy for preserving correctness

Ideally speaking, maintaining the syntactic correctness of mathematical formulas throughout the editing process can be done by

1. Writing a “formula correction” procedure which takes any (correct or incorrect) formula on input and which inserts or removes transient markup in order to make it correct.
2. Run the correction procedure on all modified formulas in the document(s) after every editing operation.

This ideal strategy is simple and robust; it trivially guarantees the correctness of all formulas throughout the editing process. However, it does not take into account the specific nature of certain editing operations. In particular, it does not exploit the locality of many editing actions.

Example 1. Consider the strict application of the ideal strategy to the creation of a subscript in the formula $x + \square$. Since \square is a valid symbol, the main editing action would create an empty subscript for it. We next launch the correction procedure, which replaces the empty subscript by a transient box, yielding $x + \square_{\square}$. However, the \square being transient, the user would rather expect to endow the “+” operator with a subscript: this is indeed what happens in the old presentation-oriented editing mode when ignoring all transient markup. In other words, we rather expect to obtain $x +_{\square} \square$.

The above example shows that an indiscriminate global correction procedure does not provide enough control. In fact, there are usually many ways to correct a formula by adding or removing transient markup. In order to determine the “best” solution, one typically needs to take into account the precise editing operation and the current cursor position.

Another constraint is that we would like the editor to behave as closely as possible as the old presentation-oriented editing mode when ignoring all transient markup. The above example shows that a global correction procedure does not necessarily respect this constraint. One theoretic solution to this problem is to remove all transient markup before performing the editing action and then put it back in when running the correction procedure. However, this approach may lead to non local changes in the document for every editing action, which is obviously not desirable.

Remark 2. For the above reasons, we have not implemented the correction strategy from this section yet. The idea nevertheless remains interesting for future research. Indeed, on the one hand side it raises the interesting theoretical question of correcting a string so as to make it parsable by a given (packrat) grammar. From the practical point of view, the ideal strategy has the important advantage of trivially guaranteeing syntactic correctness all along. In cases where this is hard to achieve using other means, it thereby remains a good fallback strategy.

3.2. Multiple correction schemes

Instead of implementing one global correction procedure, our current $\text{T}_{\text{E}}\text{X}_{\text{MACS}}$ implementation relies on multiple “correction schemes”. Each correction scheme is allowed to add or remove transient markup both before and after the actual editing operation. In other words, it really encapsulates the editing action into a semantically enhanced editing action. Furthermore, the correction scheme is allowed to fail (i.e. to produce an incorrect formula at the end). For this reason, we try multiple correction schemes in a row (the set of “eligible” schemes depends on the specific editing action), and stop as soon as we managed to obtain a correct formula.

In summary, we proceed as follows:

1. Depending on the editing action, determine a list of eligible correction schemes.

2. Try each eligible correction scheme in the list until we managed to obtain a correct formula.
3. If none of the correction schemes succeeded, then cancel the editing action.

For the actual implementation, it is clearly crucial to be able to undo editing actions whenever necessary, and in a way that is orthogonal to the usual undo/redo operations in $\text{T}_{\text{E}}\text{X}_{\text{MACS}}$.

Example 3. When inserting a mathematical symbol, the first correction scheme we try is the following: first remove all transient markup around the cursor, then insert the symbol, and finally insert a transient box at the cursor position (if needed). For instance, typing $\mathbf{A+B}$ in an empty mathematical formula successively yields $\boxed{}$, a , $a + \boxed{}$, and $a + b$.

Example 4. The basic correction scheme from the previous example sometimes fails. For instance, assume that we are in the situation $a \wedge \boxed{}$, and that we add a second “ \wedge ”. When applying the basic correction scheme, we need to correct $a \wedge \wedge \boxed{}$ through the insertion of a single transient box. However, the formula $a \wedge \wedge \boxed{}$ is still incorrect. For this particular case, we therefore use the following correction scheme: first add a transient box ($a \wedge \boxed{}$), then perform the editing action ($a \wedge \boxed{} \wedge \boxed{}$), and finally correct (nothing needs to be done at this step).

In Step 3, we simply canceled the editing action if all correction schemes failed. Several other fallback strategies can be considered. If we do not aim to maintain correctness at all costs, then we may apply the editing action without any corrections, and temporarily tolerate incorrect formulas. We might also implement an unconditionally successful fallback strategy as in Remark 2; by always adding such a strategy at the end of our list of eligible correction schemes, we will never reach Step 3. Yet another idea is to introduce a correction scheme which annotates subexpressions with exotic notations in such a way that they become correct.

3.3. Quick survey of some of the implemented correction schemes

Our approach of using multiple correction schemes allows for fine-grained control, but also requires an increased amount of manual labour. Indeed, we both have to cover the complete set of editing actions, and for each editing action, we have to implement at least one correction scheme that will succeed in all possible situations.

Fortunately, the most common editing operations fall into four main categories: insertions and deletions that operate either on selections or not. Some other operations such as “search and replace” have not yet been adapted (see also the next section). Ultimately, the idea would be to provide manual support for the most common operations and to implement a suitable fallback strategy for the other ones.

3.3.1. Correction schemes for insertions

Let us briefly list how we perform the most prominent correction schemes for insertions, in absence of active selections. For each of the schemes, we show the successive states of the formula for a simple example.

- The basic scheme from Example 3.
- “Starting a prime or right script after a transient box” (e.g. inserting a new subscript in the formula $x + \boxed{}$ from Example 1): first jump over the box with the cursor ($x + \boxed{} \mid$), then perform the action ($x + \boxed{} \substack{} \mid$), and finally add a transient box if necessary ($x + \boxed{} \substack{} \boxed{}$).
- “Inserting a pure infix operator after a transient box” (e.g. inserting the infix operator “ \circ ” in $x + \boxed{}$): perform the editing action ($x + \boxed{} \circ \mid$) and add a transient box if necessary ($x + \boxed{} \circ \boxed{}$).
- The scheme from Example 4 for inserting two infix operators in a row.
- “Starting an extensible arrow with a script” (e.g. in the situation E): remove all transient markup around the cursor ($E \mid$), perform the operation ($E \xrightarrow{} \mid$), add a transient box after the arrow ($E \xrightarrow{} \boxed{}$), as well as a transient box at the cursor position ($E \xrightarrow{} \boxed{} \mid$).
- “Insert content after an ordinary symbol” (e.g. entering ψ after φ): remove all transient markup around the cursor ($\varphi \mid$), insert a transient “explicit space” ($\varphi \mid $), perform the editing action ($\varphi \mid $), insert further transient boxes if needed ($\varphi \mid \mid$).

- “Insert content before an ordinary symbol” (e.g. entering ψ before φ): remove all transient markup around the cursor (φ), insert a transient “explicit space” after the cursor (φ), perform the editing action ($\psi\varphi$), insert further transient boxes if needed ($\psi\varphi$).
- “Insert content in the middle of an operator” (e.g. starting a fraction in \arcsin): remove all transient markup around the cursor (\arcsin), insert transient “explicit spaces” before and after the cursor (\arcsin), perform the editing action (\arcsin), insert further transient boxes if needed (\arcsin).

The last three schemes also show that it is sometimes necessary to insert transient markup with different semantics as an ordinary symbol in order to make the formula correct.

3.3.2. Correction schemes for deletions

For completion, we continue our list of examples with the most prominent correction schemes for deletions.

- “The basic deletion scheme if there is transient markup around the cursor” (e.g. hitting backspace in $a + \square$ or in $-\square$): remove the transient markup around the cursor ($a + \square$ resp. $-\square$), perform the editing action (a resp. $-$), again remove all transient markup around the cursor if we deleted any composite tag (a resp. $-$), add transient box if needed (a resp. $-$).
- “The basic deletion scheme” (e.g. hitting backspace in $a + b$): remove transient markup around the cursor ($a + b$), perform the deletion ($a +$), again remove all transient markup around the cursor if we deleted any composite tag ($a +$), add transient box if needed ($a + \square$).
- “Removal of actual infix operators” (e.g. hitting backspace in $a + b$, but *not* in $-a$): remove transient markup around the cursor ($a + b$), perform the deletion (ab), add a transient version of the deleted infix operator after the cursor ($a + b$), add transient boxes around the cursor if needed ($a + b$).
- “Need to jump over cursor before deletion” (e.g. hitting backspace in $\sum_{k=1}^{\infty} \square \circ \varphi_k$): jump over the cursor ($\sum_{k=1}^{\infty} \square \circ \varphi_k$), perform the “deletion” ($\sum_{k=1}^{\infty} \square \circ \varphi_k$), add transient boxes around the cursor if needed ($\sum_{k=1}^{\infty} \square \circ \varphi_k$).

These examples show that the correction schemes have to be implemented with quite a lot of care. This is due to the fact that it is convenient to design the schemes to apply with the right level of generality (e.g. not only to the deletion of symbols for the basic schemes, but also to the deletion of more complex structures, such as subscripts, fractions, etc.).

4. PROBLEMATIC CASES AND CHALLENGES

Several problems arose during the implementation of the new semantic mathematical editing mode which preserves syntactic correctness. Some of them were more or less expected and have been solved; others require more work and further experimentation. So far, all problematic cases that we encountered fall into two categories:

1. The incorrect treatment of special syntactic forms (and informal content in particular).
2. Complex editing operations (such as search and replace) that require special attention.

In this section, we will survey the most interesting issues that came up and highlight some of the remaining challenges.

4.1. Informal content inside formulas

One difficulty with mathematical formulas in scientific papers with respect to formulas in, say, computer algebra systems, is that they may contain punctuation, decorations, typesetting directives, or explicative text. For instance, consider the following formula:

$$\begin{aligned} Z &= \{i \in I: f_i(x) = 0 \text{ and } g_i(x) = 0 \text{ almost everywhere}\} \\ &= \{i \in I: (f_i^2 + g_i^2)(x) = 0 \text{ almost everywhere}\}. \end{aligned}$$

- Different authors use wildly varying notations for quantified expressions:

$$\begin{aligned} &\forall x, \exists y, P(x, y) \\ &\forall x \exists y: P(x, y) \\ &(\forall x)(\exists y)P(x, y) \\ &\vdots \end{aligned}$$

We already noticed in the introduction that it is “nice” to correct $\forall x, \exists$ into $\forall x, \exists$, \square , \square . However, $(\forall x)$ might be corrected just as well as $(\forall x, \square)$ or as $(\forall x)\square$, depending on the author’s preferred style. Our present solution to this kind of ambiguities is to further relax our grammar, by considering $(\forall x)$ to be a correct expression.

- One of the advantages of the new correctness-preserving editing mode is that missing expressions are clearly indicated to the user. When entering a 2×2 matrix $\begin{pmatrix} \square & \square \\ \square & \square \end{pmatrix}$ in a computer algebra system, this is indeed quite pleasant. But in the example

$$\begin{pmatrix} \lambda_1 & & \\ & \ddots & \\ & & \lambda_n \end{pmatrix}$$

of a diagonal matrix, this also forces users to manually fill out six of the cells with “invisible zeros”. Our present solution is therefore to only require tables cells to be explicitly entered inside computer algebra sessions.

- The “universal grammar” from [7] also contains a few rules for “personal use”. In particular, inside subscripts, we allow for notations such as $L_{\times \varphi, +\psi}$ and $f_{n;}$. Here $\times \varphi$ has the semantics of “post-multiplication” with φ . Given a power series $f = f_0 + f_1 z + f_2 z^2 + \dots$, the notation $f_{n;}$ stands for $f_n z^n + f_{n+1} z^{n+1} + \dots$. Now we are facing a dilemma: on the one hand, we are fond of these notations, which do not harm anyone. On the other hand, some users might *want* to be constrained to input something behind the “;” in $f_{n;}$. One solution would be to depart from the idea from [7] to promote using a “universal grammar”. Instead, we might provide special style packages for specific notations. Another approach is to introduce suitable prefix and postfix homographs of \times and $;$, together with simple keyboard shortcuts for entering them.

4.3. Special editing operations and markup

Let us finally investigate to which extent existing editing operations have to be adapted to the new, more semantic editing mode. We will start with a few issues that are already dealt with and then turn our attention to the remaining challenges.

- $\text{T}_{\text{E}}\text{X}_{\text{MACS}}$ provides a special “\-style” input method for people who already know $\text{L}^{\text{A}}\text{T}_{\text{E}}\text{X}$. For instance, one may enter α by typing `\ALPHA`, or start a fraction by typing `\FRAC`. The fact that a wide variety of editing actions can be triggered in this way required us to implement special correction schemes for this input method.
- The main $\text{T}_{\text{E}}\text{X}_{\text{MACS}}$ input method for mathematical symbols is particularly powerful and intuitive. For instance, one may enter \rightarrow and \leq by typing `->` resp. `<=`. However, this facility requires a lot of control over the undo-mechanism: when typing a shortcut `->`, $\text{T}_{\text{E}}\text{X}_{\text{MACS}}$ “forgets” the incomplete keystroke `-` and treats the shortcut `->` as an atomic operation. In other words, typing `->` and pressing “undo” will remove the entire arrow and not leave any `-`. Now remember from Section 3.2 that trying several correction schemes in succession also makes use of the undo-mechanism inside $\text{T}_{\text{E}}\text{X}_{\text{MACS}}$. Trying corrections while entering shortcuts such as `->` necessitates the mechanism to work in a nested way. We had to further tweak our implementation so as to make that possible.
- Certain editing operations such as “save the current selection as an image” have side-effects that cannot be undone. Additional care is needed when implementing correction schemes for such operations. Fortunately, such operations usually do not need to be corrected.

- One interesting editing action which is not necessarily local is “search and replace”. Global editing actions of this kind are harder to support since the corresponding correction schemes need to track all modifications made throughout the document, and less indication is provided by the local context which corrections to choose in case of ambiguities. The “search and replace” operation also raises the question whether adapting the operation to a semantic context actually involves more than corrections *via* the addition or removal of transient markup: if we replace y by $a + b$ in $x \cdot y$, do we expect to obtain $x \cdot a + b$ or $x \cdot (a + b)$?
- For some editing operations, it is not always clear what their semantic counterparts should be. One good example concerns the facility to compute and inspect the structured differences between two versions of a document. When applied to the formulas $a + bc - d$ and $a + bcy$, the differences are indicated using red and green colors: $a + bc - dy$. How should we parse this formula? Both $a + bc - d$ and $a + bcy$ do make sense, but not $a + bc - dy$. It is not clear to us yet how the editor should behave in this situation.

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