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# Complexity aspects of web services composition 

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#### Abstract

The web service composition problem can be stated as follows: given a finite state machine $M$, representing a service business protocol, and a set of finite state machines $\mathcal{R}$, representing the business protocols of existing services, the question is to check whether there is a simulation relation between $M$ and the shuffle product closure of $\mathcal{R}$. In fact the shuffle product is a subclass of the communication free petri net and basic parallel processes, for which the same problem of simulation is known to be 2-Exptime-hard. This paper studies the impact of several parameters on the complexity of this problem. We show that the problem is Exptime-complete if we bound either: ( $i$ ) the number of instances of services in $\mathcal{R}$ that can be used in a composition, or (ii) the number of the so-called hybrid states in the finite state machines of $\mathcal{R}$. Moreover, for the particular case where the bound of the hybrid states of the finite state machines of $\mathcal{R}$ is set to 2 , we show that the composition problem is in 3-Exptime.


## 1 Introduction

Web Services [1] is a new computing paradigm that tends to become a technology of choice to facilitate interoperation among autonomous and distributed applications. The UDDI consortium defines Web services as self-contained, modular business applications that have open, Internet-oriented, standards-based interfaces ${ }^{1}$. Several models have been proposed in the literature to describe different facets of services. In particular, the importance of specifying external behaviour of services, also called service business protocols, has been highlighted in several research works $[4,2,3]$. Through literature, different models have been used to represent web service business protocols. The Finite States Machines (FSM) formalism is widely adopted in this context to model statefull applications exposed as web services where states represent the different phases that a service may go through while transitions represent "abstract" activities that a service can perform [4,2,3].

We consider in this paper the problem of Web Service Composition (WSC). This problem arises from the situation where none of the existing services can provide a requested functionality. In this case, the idea is to find out, algorithmically, if the target functionality could be composed out of the existing services (components repository). This automatic approach of composition simplifies the

[^0]development of software by reusing existing components and offers capabilities to customize complex systems built on the fly [7]. We focus more particularly on a specific instance of WSC, namely the (business) protocol synthesis problem, which can be stated as follows: given a set of business protocols of available services and given a business protocol of a target service, is it possible to synthesize automatically a mediator that implements the target service using the existing ones?
[12] shows that when business protocols are described by means of FSMs, the WSC problem can then be formalized as the problem of deciding whether there exists a simulation relation between the target protocol and the shuffle (or asynchronous product) of the available ones. This result is however based on the implicit assumption that at most one instance of each available service can be used in a composition. This setting has been extended in [7] to the case where the number of instances that can be used in a composition is unbounded. WSC is formalized in this latter case as a simulation problem between an FSM and an infinite state machine, called Product Closure State Machine (PCSM), that is able to compute the shuffle closure of an FSM.

Shuffle product of FSMs (and PCSM) is a subclass of Basic Parallel Processes (BPP) [5], the class of communication free petri nets: every transition has at most one input place. Simulation of FSM by BPP was proven Expspace-hard by Lasota [11] and 2-Exptime-hard in [6].

Complexity analysis of WSC was first considered by Musholl et al.[12], under the aforementioned implicit assumption, where it is shown Exptime-Complete. In case of unbounded instances, the WSC problem has been proved decidable with an Ackermanian function as upper bound in [7]. The proof of [7] is based on Dickson lemma, and hence cannot be exploited to derive tighter upper bounds. An Expspace-hard lower bound is given by Lasota[11]. The source of complexity derived from the analysis of the algorithm given in [7] is related to the presence of the so-called hybrid states ${ }^{2}$ in the components and loops in the target: if the target FSM is loop free, the WSC problem becomes NP-complete and when the components are hybrid state free the problem is proven Exptime.

In this paper, we consider additional parameters related to bounded/unbounded web services composition. We consider as inputs an FSM $M$ (the target protocol) and a set of FSMs $\mathcal{R}$ (the protocols of the available services) and we investigate the complexity of testing simulation between $M$ and the shuffle closure of $\mathcal{R}$, represented as a PCSM [7]. More precisely, we study the complexity of the following problems:

1. $W S C(M, \mathcal{R})$ : The problem of composing $M$ using an unbounded number of instances of $\mathcal{R}$.
2. $B C(M, \mathcal{R}, k)$ : The problem of composing $M$ using at most $k$ instances of each FSM in $\mathcal{R}$.
3. $\operatorname{UCHS}(M, \mathcal{R}, k)$ : The problem of composing $M$ using an unbounded number of instances of $\mathcal{R}$, with the number of hybrid states in $\mathcal{R}$ is bounded by $k$.
[^1]Table 1 displays known and new complexity results regarding the WSC problem.

| $M$ | Acyclic FSM | general FSM |
| :--- | :---: | :---: |
| $B C(M, \mathcal{R}, 1)$ | NP-complete[7] | Exptime-complete [12] |
| $B C(M, \mathcal{R}, k)$ | NP-complete[7] | Exptime-complete (this paper) |
| $W S C(M, \mathcal{R})$ | NP-complete [7] | Decidable [7] |
| $U C H S(M, \mathcal{R}, 0)$ | NP-complete[7] | Exptime-complete (this paper) |
| $U C H S(M, \mathcal{R}, 1)$ | NP-complete[7] | Exptime-complete (this paper) |
| $U C H S(M, \mathcal{R}, 2)$ | NP-complete[7] | 3-Exptime (this paper) |

Table 1: Complexity of Web services composition problem.

Paper organisation Section 2 recalls some basic definitions needed in this paper. In section 2, investigates the problem of bounded web services composition and proves that it is Exptime-Complete. In section 2, we consider the web service composition when the number of hybrid states is bounded. We show that this problem is Exptime-Complete for $k=0, k=1$ and 3 -Exptime for $k=2$. We conclude in section 5.

## 2 Preliminaries

Finite State Machine We consider in this paper service business protocols formally described as FSMs. We recall below the definition of such machines.

Definition 1. (Finite State Machine (FSM))
A State Machine (SM) M is a tuple $M=\left(\Sigma_{M}, Q_{M}, F_{M}, q_{M}^{0}, \delta_{M}\right)$, where: $\Sigma_{M}$ is a finite alphabet, $Q_{M}$ is a set of states, $\delta_{M} \subseteq Q_{M} \times \Sigma_{M} \times Q_{M}$ is a set of labeled transitions, $F_{M} \subseteq Q_{M}$ is a set of final states, and $q_{M}^{0} \in Q_{M}$ is the initial state. If $Q_{M}$ is finite then $M$ is called a Finite State Machine (FSM).

Moreover, a state $q \in Q_{M}$ is called: accessible, if there exists a path from the initial state to q ; co-accessible, if there exists a path from q to a final state; intermediate, if $q \notin F_{M}$ and $\exists p_{1}, p_{2} \in Q_{M}$, s.t $\left(p_{1}, a, q\right) \in \delta_{M}$ and $\left(q, b, p_{2}\right) \in \delta_{M}$, we denote by $I(M)$ the set of intermediate states of $M$; hybrid, if $q \in F_{M}, q \neq q_{0}$ and there exist at least one transition $(q, b, p) \in \delta_{M}$, with $p \in Q_{M}$ and $b \in \Sigma$, the set of hybrid states is denoted $H(M)$ and terminal, if $q \in F_{M}$ and is not hybrid.

We consider here only FSMs where all states are both accessible and coaccessible. We define the norm of a state $q$ as the finite length of the shortest path from q to a final state. The norm of an FSM $M$, noted norm $(M)$, is the maximal norm of its states.
k-Iterated Product Machine (k-IPM) and Product State Machine (PCSM) We start by defining the shuffle (asynchronous product) and union operations on FSMs:

Definition 2. (Asynchronous product and Union of two FSMs)
Let $M=\left(\Sigma_{M}, Q_{M}, F_{M}, q_{M}^{0}, \delta_{M}\right)$ and $M^{\prime}=\left(\Sigma_{M^{\prime}}, Q_{M^{\prime}}, F_{M^{\prime}}, q_{M^{\prime}}^{0}, \delta_{M^{\prime}}\right)$ be two FSMs. We have :

- The shuffle or asynchronous product of $M$ and $M^{\prime}$, denoted $M \times M^{\prime}$, is an $\operatorname{FSM}\left(\Sigma_{M} \cup \Sigma_{M^{\prime}}, Q_{M} \times Q_{M^{\prime}}, F_{M} \times F_{M^{\prime}},\left(q_{M}^{0}, q_{M^{\prime}}^{0}\right)\right.$, $\left.\lambda\right)$ where the transition function $\lambda$ is defined as follows: $\lambda=\left\{\left(\left(q, q^{\prime}\right), a,\left(q_{1}, q_{1}^{\prime}\right)\right):\left(\left(q, a, q_{1}\right) \in\right.\right.$ $\delta_{M}$ and $\left.q^{\prime}=q_{1}^{\prime}\right)$ or $\left(\left(q^{\prime}, a, q_{1}{ }^{\prime}\right) \in \delta_{M^{\prime}}\right.$ and $\left.\left.q=q_{1}\right)\right\}$.
- The union of $M$ and $M^{\prime}$, denoted $M \cup M^{\prime}$, is the $\operatorname{FSM}\left(\Sigma_{M} \cup \Sigma_{M^{\prime}} \cup\{\epsilon\}\right.$, $\left.Q_{M} \cup Q_{M^{\prime}} \cup\left\{q_{0}\right\}, F_{M} \cup F_{M^{\prime}}, q_{0}, \delta_{M} \cup \delta_{M^{\prime}} \cup\left\{\left(q_{0}, \epsilon, q_{M}^{0}\right),\left(q_{0}, \epsilon, q_{M^{\prime}}^{0}\right)\right\}\right)$.

For a set of available FSMs $\mathcal{R}=\left\{M_{1}, \ldots M_{i}\right\}$, we consider a compact structure that abstracts all possible executions that can be produced using the components of $\mathcal{R}$. First, we begin by the simple case where each $M_{j}$ can be used only once:

Definition 3. (Asynchronous product of FSMs set) The asynchronous product of all the subsets elements of FSMs repository $\mathcal{R}=\left\{M_{1} \ldots M_{m}\right\}$ is the FSM: $\odot(\mathcal{R})=\bigcup_{\left\{M_{i_{1}}, \ldots, M_{i_{j}}\right\} \subseteq \mathcal{R}}\left(M_{i_{1}} \times \ldots \times M_{i_{j}}\right)$ where $j \in[0, i]$.

Second, we consider the case where the number of copies of each $M_{j} \in \mathcal{R}$ is bounded by an integer $k$ :

Definition 4. (k-iterated product of FSMs set $\mathcal{R}$ ) The $\boldsymbol{k}$-iterated product of $\mathcal{R}$ is defined by $\mathcal{R}^{\otimes_{k}}=\mathcal{R}^{\otimes_{k-1}} \times \odot(\mathcal{R})$ with $\mathcal{R}^{\otimes_{1}}=\odot(\mathcal{R})$.

Finally, we consider the general case where the number of instances of each $M_{j} \in \mathcal{R}$ is unbounded. This corresponds to the product closure of $\mathcal{R}$ [7]:

Definition 5. (Product closure of FSMs set) The product closure of $\mathcal{R}$, noted $\mathcal{R}^{\otimes}$, is defined as: $\mathcal{R}^{\otimes}=\bigcup_{i=0}^{+\infty} \mathcal{R}^{\otimes_{i}}$.

The Product Closure Machine (PCSM) of $\mathcal{R}$, defined in [7] and proven equivalent to $\mathcal{R}^{\otimes}$, is the $\operatorname{SM}\left(\Sigma_{\mathcal{R}}, \mathcal{C}_{\mathcal{R}} \otimes, F_{\mathcal{C}}, c_{0}, \Phi_{\mathcal{R}^{\otimes}}\right)$, where:

1. $\Sigma_{\mathcal{R}}=\bigcup_{M_{j} \in \mathcal{R}} \Sigma_{M_{j}}$;
2. $\mathcal{C}_{\mathcal{R}} \otimes$ is the set of states (also called configurations of $\mathcal{R}^{\otimes}$ ). $\mathcal{C}_{\mathcal{R}} \otimes \subset \mathbb{N}^{n}$, with: $n=n_{I}(\mathcal{R})+n_{H}(\mathcal{R})$ with: $n_{I}(\mathcal{R})=\Sigma_{M_{j} \in \mathcal{R}}\left|I\left(M_{j}\right)\right|$ and $n_{H}(\mathcal{R})=$ $\Sigma_{M_{j} \in \mathcal{R}}\left|H\left(M_{j}\right)\right|$. For each configuration $\mathrm{c}, c[m]$ (the $m^{t h}$ component of c ) is called a witness of the unique state $q_{m} \in Q_{M_{j}}$. Note that:

- $q_{m}$ is an intermediate state, if $1 \leq m \leq n_{I}(\mathcal{R})$;
- $q_{m}$ is an hybrid state, if $n_{I}(\mathcal{R})+1 \leq m \leq n$.

In an abuse of notation, we use $c[m]$ and $c\left[q_{m}\right]$ interchangeably.
3. $F_{\mathcal{C}}$ is the set of final states. $F_{\mathcal{C}}=\left\{c \in \mathcal{C}_{\mathcal{R}} \otimes \mid c[m]=0\right.$, for each: $1 \leq m \leq$ $\left.n_{I}(\mathcal{R})\right\}$;
4. $c_{0}=\{0\}^{n}$ is the initial state of $\mathcal{R}^{\otimes}$;
5. $\Phi_{\mathcal{R} \otimes} \subseteq \mathcal{C}_{\mathcal{R} \otimes} \times \Sigma_{\mathcal{R}} \times \mathcal{C}_{\mathcal{R} \otimes}$ is the set of transitions. we have $\left(c_{1}, a, c_{2}\right) \in \Phi_{\mathcal{R} \otimes}$ iff:

- there exists $\left(q_{0}, a, q\right) \in Q_{M_{j}}$, such that: $q_{0}$ is the initial state of $M_{j}$ and $c_{2}[q]=c_{1}[q]+1$ and $c_{2}\left[p^{\prime}\right]=c_{1}\left[p^{\prime}\right]$ for each $p^{\prime} \neq q$.
- there exists $(p, a, q) \in Q_{M_{j}}$, such that: $c_{2}[p]=c_{1}[p]-1, c_{2}[q]=c_{1}[q]+1$ and $c_{2}\left[p^{\prime}\right]=c_{1}\left[p^{\prime}\right]$ for each $p^{\prime} \neq p, q$.
- there exists $(p, a, q) \in Q_{M_{j}}$, such that: q is a final state or the initial state, $c_{2}[p]=c_{1}[p]-1$ and $c_{2}\left[p^{\prime}\right]=c_{1}\left[p^{\prime}\right]$ for each $p^{\prime} \neq p$.

Simulation preorder We recall below the definition of the simulation preorder between two SMs.

Definition 6. (Simulation)
Let $M=\left(\Sigma_{M}, Q_{M}, F_{M}, q_{M}^{0}, \delta_{M}\right)$ and $N=\left(\Sigma_{M}, Q_{M}, F_{M}, q_{M}^{0}, \delta_{M}\right)$ be two SMs. $A$ state $p \in Q_{M}$ is simulated by a state $q \in Q_{N}$, denoted $p \ll_{(M, N)} q(p \ll q$ when $M$ and $N$ are understood from context), iff the following two conditions hold:

1. $\forall a \in \Sigma_{M}$ and $\forall p^{\prime} \in Q_{M}$ such that $\left(p, a, p^{\prime}\right) \in \delta_{M}$, there exists $\left(q, a, q^{\prime}\right) \in \delta_{N}$ such that $p^{\prime} \ll q^{\prime}$, and
2. if $p \in F_{M}$, then $q \in F_{N}$.
$M$ is simulated by $N$, denoted $M \ll N$, iff the initial state of $N$ simulates the initial sate of $M$.

Observe that, by definition, each transition of a PCSM can at most increase or decrease a configuration component by 1 . In addition, if a configuration is final then all intermediate states witnesses are equal to 0 . Therefore, given a set of FSMs $\mathcal{R}$ and $c \in \mathcal{C}_{\mathcal{R} \otimes}$, we have $\Sigma_{q \in \cup_{M_{i} \in \mathcal{R}} I\left(M_{i}\right)} c[q] \leq \operatorname{norm}(c)$. Moreover, since final states can only be simulated by final ones, then for $M$ an FSM and $p \in Q_{M}$, if $p \ll c$ then $\operatorname{norm}(c) \leq \operatorname{norm}(p)$. Hence, we are able to derive the following property.

Property 1. (Intermediate witnesses bound) [7] For $c \in \mathcal{C}_{\mathcal{R} \otimes}$ and $p \in$ $Q_{M}$, if $p \in c$ then $\Sigma_{q \in \cup_{M_{i} \in \mathcal{R}} I\left(M_{i}\right)} c[q] \leq \operatorname{norm}(p)$. we denote $\mathcal{C}_{\mathcal{R} \otimes}^{M}=\{c \in$ $\left.\mathcal{C}_{\mathcal{R} \otimes} \mid \Sigma_{q \in \cup_{M_{i} \in \mathcal{R}} I\left(M_{i}\right)} c[q] \leq \operatorname{norm}(M)\right\}$.

In [7], the WSC problem in the unbounded case is reduced to simulation test between an FSM and a PCSM and this later problem is proved to be decidable. The proof of the termination of the algorithm given in $[7]$ is based on the following property:

Property 2. (configuration cover) [7] Let $c$ and $c^{\prime}$ be two configurations of $\mathcal{R}^{\otimes}$, such that: $c[m]=c^{\prime}[m], m \in[1, I]$ and $\left.\left.c[m] \leq c^{\prime}[m], m \in\right] I, I+H\right]$. if $q \ll c$, where q is a state of a SM M, then $q \ll c^{\prime}$.
we say that $c^{\prime}$ covers $c$, denoted $c \triangleleft c^{\prime}$.

We introduce below the algorithm of [7], focusing the presentation on the structure of its execution tree.

Definition 7. (Simulation Tree)
We call a simulation tree $T_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)=\left(V, v_{0}, E\right)$ with: $v_{0}=\left(q_{M}^{0}, c_{0}\right)$ is the root of the tree; $V \subset Q_{M} \times \mathcal{C}_{\mathcal{R}}{ }^{\otimes}$ is the set of nodes; If $(q, c) \in$ $V$ and $q$ is final in $M$ then so is $c$ in $\mathcal{R}^{\otimes} ; E \subset V \times V$ is the set of the tree's edges. $\forall e=((p, c),(q, d)) \in E: \exists a \in \Sigma_{M}$ s.t $(p, a, q) \in \delta_{M}$ and $(c, a, d) \in \Phi_{\mathcal{R} \otimes}$. $v=(p, c) \in V$ is a leaf in $T_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$ iff $p$ is terminal in $A$ or there exists $\left(p, c^{\prime}\right) \in P=\left\{v_{0} \ldots v\right\}$ such that $c \triangleleft c^{\prime}$ where $P$ is the set of ancestors of $v$ in $T_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$.

In the next section, we shall bound the size of this tree in the case of bounded WSC problem (i.e., when the instances of services allowed to be used in the simulation is bounded by a parameter $k$ ).

## 3 Bounded Composition

We call a bounded WSC problem, a service composition problem where the number of copies of each web service in the repository $\mathcal{R}$ used to compose the target $M$ is bounded a priori by an integer $k$. This problem is formally stated as follows.

## Problem 1. Bounded Composition $B C(M, \mathcal{R}, k)$

Input : $\mathcal{R}$ a set of $\mathrm{FSMs} ; M$ a target $\mathrm{FSM} ; k$ an integer.
Question : $M \ll \mathcal{R}^{\otimes_{k}}$ ?
The particular case $B C(M, \mathcal{R}, 1)$ has been investigated by Muscholl and Walukiewicz [12] where it is shown to be Exptime-Complete. We shall prove in this section that $B C(M, \mathcal{R}, k)$ is also Exptime-Complete. We point out that the straightforward reduction of $B C(M, \mathcal{R}, k)$ to $B C(M, \mathcal{R}, 1)$, obtained by duplicating $k$ times each service of $\mathcal{R}$, is not polynomial in the input size, since $k$ may be large, and hence cannot be used to achieve our goal.

The parameter $k$ drops the infinite aspect and reduces the search space. In this case, a loop in $M$ can only be simulated by loops in $\mathcal{R}$. For example, one can observe that, in figure $1, S_{t}$ is not simulated by $\left\{R_{1}, R_{3}\right\}^{\otimes^{k}}$ for every $k \in \mathbb{N}$. This is because when we repeat the loop in $S_{t}(k+1)$ times, there is no corresponding execution in $\left\{R_{1}, R_{3}\right\}^{\otimes^{k}}$. However, we have $S_{t} \ll\left\{R_{1}, R_{2}\right\}^{\otimes^{k}}$, for any $k \geq 1$.

In the following, we give an upper bound of the number of states that might appear in $\mathcal{R}^{\otimes k}$, with $k \in \mathbb{N}$.

Lemma 1. Let $\mathcal{R}$ be a set of FSM and $k$ is an integer. The number of states in $\mathcal{R}^{\otimes_{k}}$ is bounded by $\left|\mathcal{C}_{\mathcal{R}^{\otimes_{k}}}\right| \leq\left|\left\{c \in \mathbb{N}^{n} \mid c[i] \leq k, i \in[1, n]\right\}\right|=O\left(2^{\text {nlogk }}\right)$, where $n=|\mathcal{R}|+n_{I}(\mathcal{R})+n_{H}(\mathcal{R})$.

This lemma reduces the search space to an exponential size and leads to the following theorem.


Fig. 1. A yes instance of $B C(M, \mathcal{R}, k)$ with $k=1$.

Theorem 1. $B C(M, \mathcal{R}, k)$ is Exptime-Complete
Proof. Exptime. To show that $B C(M, \mathcal{R}, k)$ is Exptime, we bound the size of the simulation tree. A node of the simulation tree corresponds to $(q, c)$ where $q$ is a state of $M$ and $c$ a configuration of $\mathcal{R}^{\otimes_{k}}$. According to Lemma 1, the number of PCSM's configurations is bounded by $k^{n}$. So the number of nodes in the simulation tree is at most $\left|Q_{M}\right| \times k^{n}=2^{n \log (k)+\log \left(\left|Q_{M}\right|\right)}$ and therefore the complexity is in Exptime.

Exptime-Hardness. It can be deducted directly from the Exptime-Hardness of the particular case $B C(M, \mathcal{R}, 1)$ [12].

Another factor of complexity of the WSC problem is the number of hybrid states in the available services. We investigate next the effect of this parameter on the complexity of the WSC problem.

## 4 Bounded number of hybrid states

The presence of hybrid states is a source of complexity in a WSC problem. As mentioned before, the size of intermediate states witnesses in configurations of $\mathcal{R}^{\otimes}$ used to simulate $M$ is bounded by $\operatorname{norm}(M)$. We are however unable to provide a similar bound for the number of hybrid states witnesses. Figure 2 illustrates the different roles that an hybrid state of $\mathcal{R}$ can play to simulate a state of $M$. Indeed an hybrid state of $\mathcal{R}$, can be used as: (i) a terminal state, e.g., when testing wether $q_{5} \ll(1,1)$, we can consider the second hybrid state of $\mathcal{R}$ as a terminal state and terminate the test, or an intermediate state, e.g., when testing wether $q_{2} \ll(1,1)$, the second hybrid state of $\mathcal{R}$ here plays the role of intermediate state, or both a terminal and an intermediate state, e.g., when testing wether $q_{1} \ll(1,0)$, a transition of $\Phi_{\mathcal{R} \otimes}$ labeled by $(b,(-1,0))$ only appears in one branch in the simulation tree $\mathcal{T}_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$. Hence, the first hybrid state of $\mathcal{R}^{\otimes}$ is considered intermediate in one branch and terminal in the other, or a hybrid state, e.g., when it is used to simulate an hybrid state of $H(M)$.


Fig. 2. Example of the simulation tree

We consider in the following the problem defined below.
Problem 2. Unbounded Composition With limited number of Hybrid States $U C H S(M, \mathcal{R}, k)$
Input : $k$ an integer; $\mathcal{R}$ a set of FSMs, containing at most k hybrid states; $M$ a target FSM.
Question : $M \ll \mathcal{R}^{\otimes}$ ?
It is worth noting that $\operatorname{UCHS}(M, \mathcal{R}, k+1)$ is harder then $\operatorname{UCHS}(M, \mathcal{R}, k)$. In the sequel, we progressively investigate the complexity of $\operatorname{UCHS}(M, \mathcal{R}, k)$ problem for $k=0$, then for $k=1$ and finally for $k=2$.

### 4.1 Case of composition without hybrid states (i.e. $k=0$ )

In this section, we are interested by the problem $\operatorname{UCHS}(M, \mathcal{R}, 0)$. We first give a polynomial transformation, denoted $\mathcal{K}$, which is used to reduce $B C(M, \mathcal{R}, 1)$ to $U C H S\left(N, \mathcal{R}^{\prime}, 0\right)$. This transformation provides a mean to bound the number of instances used to prove simulation.

Definition 8. Transformation $\mathcal{K}$. For an $\operatorname{FSM} M=\left(\Sigma_{M}, Q_{M}, F_{M}, q_{0}^{M}, \delta_{M}\right)$ and a set of FSMs $\mathcal{R}=\left\{M_{1}, \ldots, M_{m}\right\}$, we define $\mathcal{K}(M, \mathcal{R})=\left(N, \mathcal{R}^{\prime}=\left\{N_{1}, . ., N_{m}\right\}\right)$ where:

1. Each $N_{i}$ is built based on $M_{i}$, by adding a letter $t_{i}$ to its alphabet, a final state $f_{i}$ and a transition set $\left\{\left(q_{0}^{M_{i}}, t_{i}, f_{i}\right)\right\} \cup\left\{\left(q, t_{i}, f_{i}\right) \mid q \in F_{M_{i}}\right\}$. All final states of $M_{i}$ become intermediate in $N_{i}$.
2. $N$ is defined as:
```
\(-\Sigma_{N}=\Sigma_{M} \cup\left\{t_{i} \mid 1 \leq i \leq m\right\} ;\)
\(-Q_{N}=Q_{M} \cup\left\{r_{i} \mid 1 \leq i \leq m\right\} ;\)
- \(F_{N}=\left\{r_{m}\right\}\);
\(-\delta_{N}=\delta_{M} \cup\left\{\left(q, t_{1}, r_{1}\right) \mid q \in F_{M}\right\} \cup\left\{\left(r_{i}, t_{i+1}, r_{i+1}\right) \mid 1 \leq i<m\right\}\).
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Figure 3 shows an example of a transformation $\mathcal{K}$.


Fig. 3. An example of transformation $\mathcal{K}$

The following propositions show that the transformation $\mathcal{K}$ preserves the simulation preorder.

Proposition 1. Let $M$ be an FSM, $\mathcal{R}=\left\{M_{1}, \ldots, M_{m}\right\}$ be a set of FSMs and $\mathcal{K}(M, \mathcal{R})=\left(N, \mathcal{R}^{\prime}=\left\{N_{1}, . ., N_{m}\right\}\right)$. For $p$ and $q$ two states of respectively $M$ and $\mathcal{R}^{\otimes_{1}}$, we have: $p \ll_{\left(M,(\mathcal{R})^{\left.\otimes_{1}\right)}\right.} q$ iff $p \ll_{\left(N,\left(\mathcal{R}^{\prime}\right)^{\left.\otimes_{1}\right)}\right.} q$.

Proof. By construction of $\mathcal{K}(M, \mathcal{R})$, if $p \ll_{\left(M, \mathcal{R}^{\left.\otimes_{1}\right)}\right.} q$ and p is terminal in M then $p \ll_{\left(N,\left(\mathcal{R}^{\prime}\right)^{\otimes_{1}}\right)} q$.

We suppose next that:
If $\left(p, a, p^{\prime}\right) \in \delta_{M},\left(q, a, q^{\prime}\right) \in \delta_{\mathcal{R} \otimes_{1}}$ and $p^{\prime} \ll_{\left(M, \mathcal{R}^{\otimes}\right)} q^{\prime}$, then $p^{\prime} \ll_{\left(N,\left(\mathcal{R}^{\prime}\right) \otimes_{1}\right)}$ $q^{\prime}$.
and prove that $p \ll_{\left(N,\left(\mathcal{R}^{\prime}\right) \otimes_{1}\right)} q$.
For each $\left(p, a, p^{\prime}\right) \in \delta_{N}$, we have:

- if $a \in \Sigma_{M}$, then there exists $\left(q, a, q^{\prime}\right) \in \delta_{\mathcal{R}^{\otimes_{1}}} \subseteq \delta_{\left(\mathcal{R}^{\prime}\right)^{\otimes_{1}}}$ such that $p^{\prime}$ $\ll{ }_{\left(N,\left(\mathcal{R}^{\prime}\right) \otimes_{1}\right)} q^{\prime}$.
- else $a=t_{1}, p^{\prime}=r_{1}$ and q is a product of final states of $\mathcal{R}$. therefore, there exists $\left(q, t_{1}, q^{\prime}\right) \in \delta_{\left(\mathcal{R}^{\prime}\right)^{\otimes_{1}}}$ such that $q^{\prime}=\left(f_{1}, q^{\prime}{ }_{i_{1}}, \ldots, q^{\prime}{ }_{i_{l}}\right)$ where $q^{\prime}{ }_{i_{j}}$ is final in $\mathcal{R}$ such that $p^{\prime} \ll_{\left(N,\left(\mathcal{R}^{\prime}\right) \otimes_{1}\right)} q^{\prime}$.

We conclude that if $p \ll_{\left(M, \mathcal{R}^{\left.\otimes_{1}\right)}\right.} q$ then $p \ll_{\left(N,\left(\mathcal{R}^{\prime}\right) \otimes_{1)}\right)} q$.
Reciprocally, we have $\left(p, a, p^{\prime}\right) \in \delta_{N}$ (respectively $\left.\delta_{\left(\mathcal{R}^{\prime}\right)^{\otimes}}\right)$ and $a \notin\left\{t_{i} \mid 1 \leq\right.$ $i \leq m\}$ iff $\left(p, a, p^{\prime}\right) \in \delta_{M}$ (respectively $\delta_{\mathcal{R} \otimes_{1}}$ ). In addition, the definition of $\mathcal{K}$ ensures that if p is final in M and $p \ll_{\left(N,\left(\mathcal{R}^{\prime}\right) \otimes_{1}\right)} q$ then q is final in $\mathcal{R}^{\otimes_{1}}$. Hence if $p \ll_{\left(N,\left(\mathcal{R}^{\prime}\right)^{\left.\otimes_{1}\right)}\right.} q$ then $p \ll_{\left(M, \mathcal{R}^{\left.\otimes_{1}\right)}\right.} q$.

In particular, we take p as the initial state of $M$ and q the initial state of $\mathcal{R}^{\otimes_{1}}$. This implies that:

Proposition 2. Let $M$ be an FSM, $\mathcal{R}=\left\{M_{1}, \ldots, M_{m}\right\}$ be a set of FSMs and $\mathcal{K}(M, \mathcal{R})=\left(N, \mathcal{R}^{\prime}=\left\{N_{1}, . ., N_{m}\right\}\right)$. We have: $M \ll \mathcal{R}^{\otimes_{1}}$ iff $N \ll\left(\mathcal{R}^{\prime}\right)^{\otimes}$.

Proof. We have $N \ll\left(\mathcal{R}^{\prime}\right)^{\otimes_{1}}$ iff $N \ll\left(\mathcal{R}^{\prime}\right)^{\otimes}$. Indeed, each path that starts from the initial state to a final one in $N$ contains exactly one transition labeled by $t_{i}$, for each $i \in[1, m]$ and a similar path in each $N_{i}$ contains exactly one transition labeled by $t_{i}$.

Hence, $\mathcal{K}$ is a polynomial reduction of $B C(M, \mathcal{R}, 1)$ problem to the UCHS problem. This enables to derive the following result.

Theorem 2. $U C H S(M, \mathcal{R}, 0)$ problem is Exptime-complete.
Proof. According to proposition 2 , the $\mathcal{K}$ transformation reduces $B C(M, \mathcal{R}, 1)$ to $\operatorname{UCHS}(M, \mathcal{R}, 0)$ in polynomial time. Thus $\operatorname{UCHS}(M, \mathcal{R}, 0)$ is Exptime-hard. Since it is also proven Exptime in [7], then $\operatorname{UCHS}(M, \mathcal{R}, 0)$ is Exptime-complete.

### 4.2 Case of composition with one hybrid state

We consider the problem $\operatorname{UCHS}(M, \mathcal{R}, 1)$ where $M$ is an FSM and $\mathcal{R}$ a set of FSMs containing at most one hybrid state $\left(n_{H}(\mathcal{R}) \leq 1\right)$. We denote $k_{0}=$ $\left|Q_{A}\right| \cdot 2^{n_{I}(\mathcal{R}) \cdot \log (\text { norm }(M))}$. Two nodes $(q, c)$ and $\left(q^{\prime}, c^{\prime}\right)$ in a simulation tree are called comparable if $q=q^{\prime}$ and either $c \triangleleft c^{\prime}$ or $c^{\prime} \triangleleft c$. The nodes $(q, c)$ and $\left(q^{\prime}, c^{\prime}\right)$ are said incomparable otherwise.

Property 3. Let $\mathcal{R}$ be a set of FSMs containing at most one hybrid state. Two configurations of $\mathcal{R}^{\otimes}$ are comparable by the cover relation, iff they have exactly the same intermediate witnesses.

Property 4. Let S be a set of nodes of $\mathcal{T}_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$ that are pairwise incomparable, then $|S| \leq k_{0}$.

Proof. In configurations considered in $\mathcal{T}_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$, intermediate witnesses are bounded by norm $(M)$ (property 1 ). Therefore and according to property 3 , the number of incomparable configurations considered in $\mathcal{T}_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$ is at most $2^{n_{I}(\mathcal{R}) \cdot \log (\operatorname{norm}(M))}$. Since $S \subset Q_{M} \times \mathcal{C}_{\mathcal{R}} \otimes$, then $|S| \leq k_{0}$.
Proposition 3. If $n_{H}(\mathcal{R}) \leq 1$, then foreach $(q, c) \in \mathcal{T}_{\operatorname{sim}}\left(M, \mathcal{R}^{\otimes}\right), c[I+1] \leq$ $k_{0}{ }^{2}$.
Proof. let P be a path in $\mathcal{T}_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$ and $S=\left(v_{n}=\left(q_{n}, c_{n}\right)\right)_{n \in I n t \subset \mathbb{N}}$ be a sequence of nodes in P such that:
$-v_{i}$ is the $i^{t h}$ node met in P that is comparable to one of its predecessors $v=\left(q_{i}, c\right) ;$ and
-For each $i, j \in I n t, v_{i}$ and $v_{j}$ are incomparable.
If Int $=\emptyset$, then all nodes of P are not comparable. The size of P is then bounded by $k_{0}$, therefore, $c[I+1] \leq k_{0}$ for each (q, c) in P.

We suppose next that $I \neq \emptyset$ and take $\operatorname{Int}=[1, k], k \in \mathbb{N}$. We prove recursively that for each $n \in[1, k], c_{n}[I+1] \leq n . k_{0}$.

For $n=1$, we have $c_{1}[I+1] \leq k_{0}$.
For $1<n<k$, we suppose that $c_{n}[I+1] \leq n . k_{0}$. Each node $v=(q, c)$ between $v_{n}$ and $v_{n+1}$ in P is either:

1. comparable to a node $v_{i}$ with $i \in[1, n]$. In this case, $c[I+1]<c_{i}[I+1] \leq n . k_{0}$ (otherwise v should be a leaf).
2. incomparable to all its predecessors. The number of such nodes is bounded by $k_{0}$. And since transitions displacements is in $\{-1,0,1\}^{I+1}$, then we have $c[I+1]<n . k_{0}+k_{0}$.
Therefore $c_{n+1}[I+1] \leq(n+1) . K_{0}$.

Once we reach $v_{k}$, all its possible successors are comparable to a node $v_{i}$ with $c[I+1]<c_{i}[I+1]$, except for the last one that is the leaf of P .

Finally, since $k<k_{0}$ (because S is a sequence of incomparable nodes), we conclude that each node of P is in $Q_{A} \times\left([1, \operatorname{norm}(A)]^{I} \times\left[1,{k_{0}}^{2}\right]\right)$.

Since deciding simulation only requires to visit a node once, we argue next that this problem is in APspace: the size of a position of the simulation tree is polynomial in the input size (Proposition 3). Hence a polynomial space alternating turing machine can solve this simulation problem: universal states correspond to the target's and existential states correspond to the shuffle product's configurations. Given the above, we conclude that:
Lemma 2. $U C H S(M, \mathcal{R}, 1)$ is in Exptime.
To prove the Exptime-hardness of the problem, we recall that $\operatorname{UCHS}(M, \mathcal{R}, 0)$ is Exptime-hard (theorem 2) and that $\operatorname{UCHS}(M, \mathcal{R}, 1)$ is harder than $\operatorname{UCHS}(M$, $\mathcal{R}, 0)$.
Theorem 3. $\operatorname{UCHS}(M, \mathcal{R}, 1)$ is Exptime-complete.

### 4.3 Case of composition with two hybrid states

In this section, we consider the problem of unbounded composition of web services with at most 2 hybrid states in $\mathcal{R}$, i.e. $\operatorname{UCHS}(M, \mathcal{R}, 2)$. Our approach is based on relating this simulation problem to the reachability issue.

For $x \in \mathbb{N}^{i_{1}}$ and $y \in \mathbb{N}^{i_{2}}$, we denote the concatenation of two vectors $x$ and $y,(x . y) \in \mathbb{N}^{i_{1}+i_{2}}$ such that:

$$
(x . y)[j]=\left\{\begin{array}{l}
x[j] \text { if } j \in\left[1, i_{1}\right] \\
y[j] \text { if } j \in\left[i_{1}+1, i_{1}+i_{2}\right]
\end{array}\right.
$$

We define the 2-dimension Vector Addition System with States (VASS) [8] $\mathcal{V}_{M, \mathcal{R}}$ as follows:

- States: $S \subseteq Q_{M} \times\left\{c \in \mathbb{N}^{n_{I}(\mathcal{R})} \mid \sum_{i=1}^{i=n_{I}(\mathcal{R})} c[i] \leq \operatorname{norm}(M)\right\}$.
- Transitions: $W \subseteq S \times S \times\{-1,0,1\}^{2}$ such that: $((q, c),(p, d), x) \in W$ iff there exists $a \in \Sigma_{M}, y \in \mathbb{N}^{2}$ such that $(p, a, q) \in$ $Q_{M}$ and $((c, y), a,(d, y+x)) \in \Phi_{\mathcal{R} \otimes}$ and $\sum_{i=1}^{i=n_{I}(\mathcal{R})} c[i] \leq \operatorname{norm}(M)$ and $\sum_{i=1}^{i=n_{I}(\mathcal{R})} d[i] \leq \operatorname{norm}(M)$.
- Initial configuration: the system starts with the state $\left(q_{0}^{M},\{0\}^{n_{I}(\mathcal{R})}\right)$ and the vector $(0,0)$.

Figure 4 depicts an example of a VASS associated to an FSM $M$ and a set of FSMs $\mathcal{R}$.


Fig. 4. An example of a VASS associated to an FSM M and an FSMs set.

The reachability issue in 2-dimension VASSs has been investigated by Hopcroft and Pansiot [8] in the general case where displacements are in $\mathbb{N}^{2}$. [8] gives an algorithm to prove the semi-linearity of the reachability set of such
systems. The algorithm builds a tree $T_{\text {reach }}$ labeled by 3 -tuples $\left(p, c, A_{c}\right)$ where $p$ is the current state, $c \in \mathbb{N}^{2}$ is a vector reached in the system and $A_{c} \subset \mathbb{N}^{2}$. $\left(p, c, A_{c}\right)$ denotes that every vector in the linear set $\left\{c+\alpha_{1} a_{1}+\ldots+\alpha_{n} a_{n} \mid i \in\right.$ $[1, n], a_{i} \in A_{c}$ and $\left.\alpha_{i} \in \mathbb{N}\right\}$ can be reached in state $p$ from the initial configuration.

We consider in the following a simulation tree $T_{\operatorname{sim}}\left(M, \mathcal{R}^{\otimes}\right)=\left(V, v_{0}, E\right)$, a recheability tree $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)=\left(V^{\prime}, v_{0}^{\prime}, E^{\prime}\right)$ and a function $\pi$ defined as follows:

$$
\begin{aligned}
& \pi: \quad V^{\prime} \rightarrow \\
&\left((p, c), x, A_{x}\right) \mapsto \\
&(p,(c . x))
\end{aligned}
$$

The following proposition enables to establish a connection between paths in a simulation tree and a corresponding recheability tree.

Proposition 4. Let $\mu=v_{0} \ldots v_{t}$ be a path in $T_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$. Then there exists a path $\mu^{\prime}=v_{0}^{\prime} \ldots v_{t}^{\prime}$ in $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$ such that $v_{i}=\pi\left(v_{i}^{\prime}\right), i \in[0, t]$.

Proof. We proof by induction on the length $i$ of the path $\mu=v_{0} \ldots v_{t}$.
For $i=0$ we have $v_{0}=\left(q_{0}^{M}, c_{0}\right)=\pi\left(\left(q_{0}^{M},\{0\}^{n_{I}(\mathcal{R})}\right), x_{0}, A_{c_{0}}\right)=\pi\left(v_{0}^{\prime}\right)$.
Now suppose that the property is true for $i<t$ and $v_{0} \ldots v_{i+1}$ is a path in $T_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$. Then by hypothesis there exists a path $v_{0}^{\prime} \ldots v_{i}^{\prime}$ in $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$, such that $v_{j}=\pi\left(v_{j}^{\prime}\right), j \in[0, i]$.

Suppose that $v_{i}^{\prime}$ is a leaf in $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$. Then according to the algorithm of Hopcroft and Pansiot [8], we have either:

- There exist $j \in[0, i-1]$ such that $v_{j}^{\prime}=\left((p, c), y, A_{x}\right)$ and $v_{i}^{\prime}=\left((p, c), x, A_{x}\right)$ with $y \leq x$ (see Algorithm ??, line 1). This implies that $v_{j} \triangleleft v_{i}$, which contradicts that $v_{i}$ is not a leaf in $T_{\operatorname{sim}}\left(M, \mathcal{R}^{\otimes}\right)$, i.e. $(c, y) \triangleleft(c, x)$.
- There is no transition from $v_{i}^{\prime}$ in the system (see Algorithm ??, line 1). But for $v_{i}=(p,(c, x))$ and $v_{i+1}=(q,(d, y))$ we have $v_{i} v_{i+1} \in E$ which means that $(p, a, q) \in \delta_{M}$ and $((c, x), a,(d, y)) \in \Phi_{\mathcal{R} \otimes}$. This implies that $((p, c),(q, d), y-x) \in W$. Contradiction.
Therefore, we have : $v_{i+1}^{\prime}=\left((q, d), y, A_{y}\right)$ is a successor of $v_{i}^{\prime}$ in $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$, with $v_{i+1}=(q,(d, y))$. We conclude that $\mu^{\prime}$ is a path in $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$.

The following corollary is a consequence of Proposition 4.
Corollary 1. $T_{\text {sim }}\left(M, \mathcal{R}^{\otimes}\right)$ is a sub-tree of $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$.
Clearly the time complexity for computing $T_{\operatorname{sim}}\left(M, \mathcal{R}^{\otimes}\right)$ is dominated by the complexity of computing $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$. Moreover we know from [9] that the size of $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$ is in 2-Exptime. Hence, we derive the following complexity result.

Theorem 4. $\operatorname{UCHS}(M, \mathcal{R}, 2)$ is in 3-Exptime.
Proof. According to [9], the size of $T_{\text {reach }}\left(\mathcal{V}_{M, \mathcal{R}}\right)$ is of order $O\left(2^{2^{\alpha}}\right)$ where $\alpha=\max (|S|,|W|) \leq c \times\left(\left|Q_{M}\right| \times \operatorname{Norm}(M)^{n_{I}(\mathcal{R})}\right)^{2}$ with $c$ is a constant. Then according to Corollary 1 , the size of $T_{\operatorname{sim}}\left(M, \mathcal{R}^{\otimes}\right)$ is bounded by $2^{2^{2^{c_{1}+c_{2} * \beta}}}$ where $c_{1}$ and $c_{2}$ are constants and $\beta=\log \left(\left|Q_{M}\right|\right)+n_{I}(\mathcal{R}) \times \log (\operatorname{Norm}(M))$.

Our proof for Theorem 4 can be seen more as an embedding of the search space explored by a simulation test to the one explored when the reachability issue is considered. This is an approach that can not so far be generalized because the best upper bound provided for vector addition systems reachability is nonprimitive recursive; in fact even the existence of a primitive upper-bound is still open [10].

## 5 Conclusion

In this paper we have considered two parameters that are source of complexity of the web services composition problem. We have shown that among the considered problems, several instances remain Exptime-complete when a parameter is bounded. It remains an open question to identify whether the unbounded web services composition problem is in $X P$, where $X P$ is the complexity class that contains all problems solvable in $O\left(n^{f(k)}\right)$ with $n$ is the size of $M$ and $\mathcal{R}$, and $f$ is a recursive function. Since $F P T \subset X P$, it is interesting as well to investigate what kind of fixed parameters can lead to FPT complexity.

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[^0]:    ${ }^{1}$ http://www.uddi.org/

[^1]:    ${ }^{2}$ Hybrid states of an FSM are final states with outgoing transitions and correspond to unbounded places in Petri net terminology.

