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Channel Interleavers for Terrestrial Broadcast: Analysis and Design

Ronald Garzón Bohórquez, Student Member, IEEE, Charbel Abdel Nour, Member, IEEE, and Catherine Douillard, Senior Member, IEEE

Abstract-A method to design channel interleavers based on span properties and mutual information is presented. Resulting interleavers enjoy better burst error control and can mitigate the effect of regular error patterns. An application example based on the 2nd generation Digital Video Broadcasting Terrestrial (DVB-T2) standard is elaborated. Four channel interleaving structures are generated, resulting from a joint optimization of the interleaver span properties in the time and frequency domains, while guaranteeing good interaction with the bit interleaver. Proposed solutions are compared to the standardized DVB-T2 channel interleaver in terms of performance, latency and complexity. A significant improvement can be observed in severe channel conditions, especially over time and frequency-selective channels with erasures. Moreover, the complexity and latency of the proposed channel interleavers are reduced compared to the original DVB-T2.

Index Terms—Channel interleaver, DVB-T2, L^1 space, mutual information, span properties, time and frequency diversity.

I. INTRODUCTION

S TATE-OF-THE-ART Forward Error Correction (FEC) codes are now able to approach Shannon capacity [1], [2] especially for transmissions over memoryless channels in which errors are randomly distributed and statistically independent. In contrast, when FEC codes are used in transmissions over channels in which the signal undergoes impulsive noise (i.e., error bursts in a short period of time) and/or selective fading (i.e., interference in a short frequency interval), the error rate performance can be greatly degraded. One possible solution to such a problem involves distributing error patterns arriving in bursts among several FEC frames. Therefore, channel interleaving [3] is introduced to uniformly distribute codewords in time and frequency, in such a way that the transmitted symbols subject to impulsive noise and selective fading do not end up in the same coded frame. In other words, channel interleaving allows the overall system to take advantage of the available time and frequency diversities from the encountered channel.

The adaptive channel interleaver has become a subject of research in recent years. In [4], an interleaving structure with variable depth or length was proposed. It presents the advantage of dimensioning the latency and required memory with respect to the encountered channel. An estimate of the suitable depth is obtained by measuring the maximum Doppler shift at the receiver. It results in a gain, since interleaving depth is adapted to Doppler shift. However, this technique is not suited for broadcasting applications. In fact, due to the nature of the broadcast service, all receiver situations can be experienced, each with different channel characteristics and Doppler shift values. Therefore, interleaving depth should be scaled for the worst case scenario. In addition, a return channel is required to communicate the maximum Doppler shift back to the transmitter. In [5], the authors adapt the interleaving function with respect to the instantaneous Channel State Information (CSI) of the Orthogonal Frequency-Division Multiplexing (OFDM) carriers. It is shown to improve system performance. Compared to other interleaving structures, time diversity seems to be limited, since the proposed interleaver in [5] operates at the OFDM symbol level. Actually, this solution represents a family of adaptive frequency interleavers operating on the sub-carriers of one OFDM symbol. In addition, a return channel is once again required to send the CSI back to the transmitter.

In the early 2000s the DVB consortium developed the Digital Video Broadcasting Terrestrial (DVB-T) standard [6]. Although it included the OFDM modulation technique, the lack of time interleaving made the broadcast system perform poorly in mobile environments [7]. To overcome this limitation, the next generation terrestrial broadcast system, DVB-T2, includes more elaborate channel interleaving structures. Indeed, DVB-T2 advocates the use of three interleavers [8]: Cell Interleaver (CI), Time Interleaver (TI) and Frequency Interleaver (FI). The implementation of each of them introduces further system latency. On the other hand, since the implementation of each type of interleaver requires a specific part of the memory, the whole interleaving memory can represent a large part of the silicon area and of the power consumption of the receiver. In addition, from a diversity point of view, a bad interaction between channel interleavers can introduce a degradation of the overall system performance. To deal with these issues, a new technique to design channel interleavers is introduced.

The rest of the paper is organized as follows. In section II, an overview of DVB-T2 channel interleavers is presented. Section III identifies relevant criteria for the interleaver design and provides appropriate theoretical tools to represent the optimization constraints. Section IV analyzes the impact on performance of the different interleavers in the DVB-T2 transmission chain. Then, in section V, the design criteria are applied to obtain a set of optimized DVB-T2 channel interleavers. Their interaction with the Bit Interleaver (BI) is

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also studied. Finally, section VI shows simulation results of system performance with proposed interleavers and section VII concludes the paper.

II. OVERVIEW OF THE STRUCTURE OF DVB-T2 CHANNEL INTERLEAVERS

According to [8], [9], a basic DVB-T2 transmission chain not including the input adaptation stage can be established as shown in Fig. 1.

FEC Encoder	BI Mapper CI TI	OFDM Frame Builder	FI OFDM Modulator
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Fig. 1. Basic DVB-T2 transmission chain.

The data to be transmitted are first encoded by a BCH code followed by a Low-Density Parity-Check (LDPC) code. The concatenation of these two codes constitutes the FEC code of Fig. 1. The codewords at the output of the encoder are interleaved by the BI, which is composed of parity and column twist interleaving. This interleaver aims to avoid mapping multiple coded bits connected to the same check node on the same constellation symbol [10]. In the mapper, LDPC codewords are mapped to constellation symbols or cells using Gray mapping. The CI is a pseudo-random permutation on the cells of a codeword, also called FEC block. In order to achieve different interleaving patterns for different FEC blocks, a constant shift is introduced into the permutation. The TI is a column-row block interleaver intended to spread cells from several FEC blocks into one OFDM frame. The number of FEC blocks in the OFDM frame, NFEC, depends on the TI duration, which should be at least 70 ms to ensure some immunity to interference or impulsive noise. This interleaver represents the largest memory requirement of the system, since all the cells of the FEC blocks contained in the OFDM frame should be stored in the interleaver memory bank. The OFDM frame builder assembles the cells coming from the TI into arrays of OFDM symbols. Then the cells of each OFDM symbol are interleaved by the FI. This interleaver is a pseudo-random block interleaver with a different structure for odd and even symbols. The FI aims to mitigate the adverse interaction of the TI structure and regular error patterns (i.e., across frequencies) by breaking up the structured nature of the TI. The objective of the channel interleavers CI, TI and FI is to ensure an uncorrelated error distribution inside the FEC blocks, over time and/or frequency-selective propagation channels.

III. IDENTIFICATION OF RELEVANT DESIGN CRITERIA FOR CHANNEL INTERLEAVERS

An efficient channel interleaver has to take advantage of the time and frequency diversities allowed by OFDM multicarriers. Thus, from a diversity point of view, the parameters identified as being the most important are the channel interleaver span properties and the achieved mutual information distribution over FEC blocks.

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A. Span Properties

The channel interleaver operates at the OFDM frame level, between the constellation mapper and the OFDM modulator. Let NF and NT be the number of carriers and OFDM symbols, respectively. The channel interleaver reads the cells from the input OFDM frame address i, $i = 0...NT \times NF - 1$, and writes them to the output OFDM frame address $\Pi(i)$. The time and frequency minimum span, S_t and S_f , associated with the cell with address i can be defined according to [11], [12] as:

$$S_t(i) = \min_{j \neq i} [|t_i - t_j| + |t_{\Pi(i)} - t_{\Pi(j)}|]$$
(1)

$$S_f(i) = \min_{j \neq i} [|f_i - f_j| + |f_{\Pi(i)} - f_{\Pi(j)}|]$$
(2)

Where t_u and f_u represent the OFDM symbol and carrier indexes of the cell with address u. To design a channel interleaver with good scattering properties able to efficiently break error bursts, the minimum span values of equations (1) and (2) have to be maximized. In addition, their respective multiplicity (i.e., number of cells having the same span value) should be minimized.

B. Joint Representation of the Time and Frequency Span Properties in the L^1 Space

The validation of span properties in bi-dimensional channel interleavers, where the time and frequency components are treated separately, is a straightforward task that can be verified by equations (1) and (2). This validation may become difficult when one-dimensional interleavers are considered. Indeed, the modification of any of the interleaver parameters jointly affects both span properties. To tackle this problem, a joint representation of both the time and frequency span properties in the L^1 space is proposed.

The L^p spaces are function spaces defined using a natural generalization of the *p*-norm for finite dimensional vector spaces [13]. Let **x** be $\mathbf{x} = (x_1, x_2, x_3, ..., x_n)$ a vector in the L^p space over the *n*-dimensional real vector space \mathbb{R}^n . For a real number $p \ge 1$, the *p*-norm of *x* is defined by:

$$||x||_{p} = (|x_{1}|^{p} + |x_{2}|^{p} + \dots |x_{n}|^{p})^{1/p}$$
(3)

Thus, for p = 2 we get the Euclidean norm. For p = 1, in the bi-dimensional real vector space \mathbb{R}^2 , (3) becomes:

$$\|x\|_1 = |x_1| + |x_2| \tag{4}$$

At the OFDM frame level, a valid span region composed of four sub-regions can be defined (see Fig. 2). In the worst case, we consider a couple of neighbor cells (i, j) in the input OFDM frame. If the first interleaved cell $\Pi(i)$ is placed as shown in Fig. 2, the second interleaved cell $\Pi(j)$ must be placed inside one of the valid span sub-regions.

Let us define a vector $\mathbf{d} = (d_1, d_2)$ in the L¹ space over \mathbb{R}^2 by:

$$d_1 = i - j \tag{5}$$

$$d_2 = \Pi(i) - \Pi(j) \tag{6}$$

The 1-norm of this vector corresponds to the span between i and j. Then according to Fig. 2, a couple of cells (i, j)



Fig. 2. Valid span sub-regions in the output OFDM frame.

satisfying the minimum time and frequency span constraints, S_{Tmin} and S_{Fmin} verifies any of the following conditions:

Sub-region 1 :
$$l_1(k) \le ||d||_1 \le l_0(k)$$
 (7)

Sub-region 2:
$$l_3(k) \le ||d||_1 \le l_2(k)$$
 (8)

Sub-region 3 :
$$l_0(k) \le ||d||_1 \le l_1(k)$$
 (9)

Sub-region
$$4: l_2(k) \le ||d||_1 \le l_3(k)$$
 (10)

 l_0 , l_1 , l_2 and l_3 represent the boundaries of valid sub-regions in the OFDM frame. Their value depends on the OFDM symbol k considered. Those boundary values can be expressed as:

$$l_0(k) = |k \times NF - \Pi(i)| \tag{11}$$

$$l_1(k) = \left| f_{\Pi(i)} - S_{Fmin} + k \times NF - \Pi(i) \right|$$
(12)

$$l_2(k) = \left| f_{\Pi(i)} + S_{Fmin} + k \times NF - \Pi(i) \right|$$
(13)

$$l_3(k) = |(1+k) \times NF - 1 - \Pi(i)|$$
(14)

where k varies from 0 to $t_{\Pi(i)} - S_{Tmin}$ for sub-regions 1 and 2 and from $t_{\Pi(i)} + S_{Tmin}$ to NT - 1 for sub-regions 3 and 4.

Note that the existence of each sub-region depends on the position of $\Pi(i)$; therefore they exist if the following conditions are met:

Sub-region 1 :
$$\begin{cases} t_{\Pi(i)} - S_{Tmin} > 0 & (15) \\ f_{\Pi(i)} - S_{Fmin} > 0 & (16) \end{cases}$$

Sub-region 2
$$(15)$$
 is verified

Sub-region 2:
$$\begin{cases} f_{\Pi(i)} + S_{Fmin} < NF - 1 \end{cases}$$
(17)

Sub-region 3 :
$$\begin{cases} (16) \text{ is verified} \\ t_{\Pi(i)} + S_{Tmin} < NT - 1 \end{cases}$$
(18)
Sub-region 4 :
$$\begin{cases} (17) \text{ is verified} \\ (18) \text{ is verified} \end{cases}$$

All valid span sub-regions can be plotted in a single bidimensional L^1 space. For instance, the first sub-region is shown in Fig. 3.



Fig. 3. First valid span sub-region.

C. Mutual Information Distribution

As advocated in [14], [15], capacity-based optimization is a computation-efficient tool to find a good tradeoff between the parameters of a Bit-Interleaved Coded Modulation (BICM) e.g., modulation order M, code rate R. Using capacity as a cost function, energy-efficient parameters can be found, i.e., parameters providing capacity-approaching performance at a minimum of E_b/N_0 .



Fig. 4. Composite channel in the BICM system.

Capacity is found by evaluating the average Mutual Information (MI) between the input and the output of the composite channel, consisting of the modulator, the transmission channel, and the soft output of the demodulator (Fig. 4). As BICM transforms the composite channel into $\log_2 M$ parallel binaryinput continuous output channels [16], the capacity of the overall system is:

$$C = \sum_{i=1}^{\log_2 M} C_i \tag{19}$$

The capacity of the *i*th BICM subchannel C_i is the average MI between the input $b_i \in \{0, 1\}$ and the corresponding log-likelihood ratio z_i at the output of the demodulator:

$$C_i = I(b_i; z_i) = E[i(b_i; z_i)]$$
 (20)

With the mutual information random variable i(b; z) expressed as in [17], and assuming that b is equally likely to be 1 or 0, i(b; z) evolves to:

$$i(b; z) = \log 2 - \max * \left(0, z \left(-1\right)^{b}\right)$$
 (21)

where, $\max * (x, y) = \log(e^x + e^y)$ as defined in [18]. Then, substituting (20) and (21) into (19) gives the expression for the BICM capacity:

$$C = \sum_{i=1}^{\log_2 M} \log 2 - E\left[\max * \left(0, z_i \left(-1\right)^{b_i}\right)\right]$$
 (22)

which is measured in nats per channel use. To convert the capacity into bits per channel use, (22) must be divided by $\log 2$.

In practice, the effect of the channel interleaver on BICM capacity is very small and, in the context of channel interleaver design, it is more relevant to visualize the MI distribution over the FEC blocks in the OFDM frame. Since an optimal channel interleaver must guarantee an uncorrelated error distribution inside the FEC blocks, the average MI should be homogeneously distributed between FEC blocks, guaranteeing that error bursts are uniformly distributed.

Let N be the FEC block length. The average MI per FEC block can be expressed as:

$$AMI_{j} = \log 2 - \sum_{i=1}^{N} \left(\max * \left(0, z_{i} \left(-1 \right)^{b_{i}} \right) \right) / N$$
 (23)

where the current FEC block number is represented by j, j = 1...NFEC. In addition, the variance of the MI distribution gives a measure of the amount of variation of the FEC block MI to the mean MI:

$$VAR(AMI) = \sum_{j=1}^{NFEC} \left((AMI_j - E [AMI])^2 \right) / NFEC \quad (24)$$

Therefore, a homogeneous distribution of MI is identified by a low VAR(AMI) value. Thus, the best interleaver candidates are those allowing the lowest values of VAR(AMI). It should be noted that this selection criterion is channel-dependent.

IV. PERFORMANCE ANALYSIS OF DVB-T2 CHANNEL INTERLEAVERS

The performance of the set of DVB-T2 interleaver components placed between the constellation mapper and OFDM modulator is analyzed in three steps. First, we observe the impact of each component on the overall system performance. The Bit Error Rate (BER) at the output of the LDPC decoder is plotted in different interleaving conditions, starting from no channel interleaving and then introducing the different components, CI, TI and FI. Second, the corresponding MI distributions are analyzed at the Signal-to-Noise Ratio (SNR) decoding threshold. Finally, the time and frequency span histograms of the complete T2 interleaver (i.e., CI, TI and FI) are determined. The simulation parameters are given in Table I. LDPC decoding runs 50 iterations of the sumproduct algorithm [19]. Both TU6 mobile channel [20] with Doppler frequency $f_d = 166$ Hz and P1 Rayleigh channel [20] are considered for transmission. The TU6 channel profile reproduces the propagation in a typical urban area including the classical Jakes [21] Doppler spectrum for 6 taps. The P1 channel profile reproduces portable indoor/outdoor reception conditions and does not include any Doppler effect. It has only non-line-of-sight components and uses 20 taps.

TABLE I Simulation Parameters.

System Parameter	Value
FEC codeword length	16,200 bits
Code rate	2/3
T2 frame length	100 ms
Constellation	Non-rotated QPSK
Bandwidth	8 MHz
FFT size	2k
Guard interval	1/4
Channel estimation	Perfect



Fig. 5. BER system performance with DVB-T2 channel interleaver components over the TU6 channel.

Fig. 5 shows simulation results over a TU6 channel. Since the frequency selectivity varies with time, the FI component does not bring much interleaving gain. The best performance is obtained when the complete T2 interleaver or TI only is implemented. This result is confirmed by Fig. 6, which shows that, in these cases, a homogeneous MI distribution in the FEC blocks is obtained. In contrast, poor performance is obtained with interleavers that produce a larger dispersion of the MI distribution, i.e., CI, and FI. We can deduce from these observations that the interleaving component that introduces the largest performance gain over the TU6 channel is the TI.

Over time-invariant channels such as the P1 Rayleigh channel, the frequency selectivity does not change with time. Thus, the frequency interleaver is an important interleaving component, as confirmed by Fig. 7. The best BER performance over the P1 channel is obtained with the complete T2 interleaver or when the FI only is implemented. These results are also



Fig. 6. MI Distribution, $E_s/N_0 = 5.2$ dB, TU6 channel.



Fig. 7. BER system performance with DVB-T2 channel interleaver components over the P1 channel.

consistent with the MI distribution shown in Fig. 8. On the other hand, there seems to be a contradiction between the BER performance obtained with the CI and the corresponding MI distribution, which is very close to the MI distribution obtained without interleaving. Actually, the effect of CI cannot be observed in the MI distribution curves, since CI is applied inside a FEC block and has no impact on the MI distribution per FEC block.

Finally, in order to identify potential bad scattering interactions between the different interleaver components, we have plotted the span histograms for the complete T2 interleaver. Fig. 9 shows the first 100 values of the histograms, with their



Fig. 8. MI Distribution, $E_s/N_0 = 6.8$ dB, P1 channel.

multiplicities. In the simulated configuration, the OFDM frame is composed of 357 OFDM symbols transmitted over 1705 carriers. Under these conditions and based on [11], the theoretical maximum minimum time and frequency span values are $\sqrt{2 \times NT} = 26$ and $\sqrt{2 \times NF} = 58$, respectively. According to the histogram results, this instance of T2 interleaver has poor span properties in both the time and frequency domains, since the minimum time and frequency span values are 0 and 1, respectively. These poor span properties are the result of a bad interaction between the different interleaving components due to a non-global optimization. This can lead to system performance degradation in transmissions where the FEC code approaches its limit in error correction capacity. For instance, in the case of channel impairments arriving by bursts and affecting a large number of consecutive OFDM symbols and/or subcarriers, low spans result into the packing of a large number of erroneous or erased bits into a limited number of FEC blocks. These blocks are then likely to be incorrectly decoded, especially for high code rates.

V. DESIGNING IMPROVED CHANNEL INTERLEAVERS FOR DVB-T2

The channel interleaving function can be defined as:

$$i' = \Pi(i) \tag{25}$$

where Π represents the permutation law, and *i* and *i'* represent the read and write cell addresses in the input and output OFDM frames, respectively. As explained in section III, Π should be designed in order to, first, maximize the minimum time and frequency span values; second, minimize their respective multiplicity; and third, reduce the MI distribution variance over the FEC blocks.

In order to limit the interleaver complexity, the proposed interleaver families are based on regular and Almost Regular Permutations (ARP). Thereby, the first interleaver family is



Fig. 9. Time and frequency span histograms for the complete T2 Interleaver. The Y-axis displays the number of cells having the same time/frequency span value.

based on a single regular permutation, the second one on a double regular permutation. In the third one, an ARP is introduced, and the last one is based on a double ARP. An application example is developed for each interleaver family using the parameters listed in Table I. Then, the interaction between the channel interleaver and the BI is studied and an optimized BI is proposed. Finally, a system latency and complexity analysis is performed.

A. Regular Interleaver

The permutation law for a regular interleaver can be defined as:

$$\Pi(i) = P \times i \bmod NC \tag{26}$$

where NC is the total number of cells in the OFDM frame and P is the interleaver period. NC and P have to be relatively prime. The Regular Interleaver (RI) period is calculated by:

$$P = P_t \times NF + P_f \tag{27}$$

where P_t and P_f represent the equivalent interleaver periods in the time and frequency domains. Given that there are NTsymbols in an OFDM frame, the best candidate values for P_t are the interleaver periods allowing the maximization of the minimum span value for a regular permutation in a vector of length NT. First, all admissible values for P_t according to the vector length are identified. Second, the best candidate values regarding the span criterion are selected. In the same way the best candidate values for P_f are determined regarding the span criterion in a vector of length NF.

Afterwards, the best candidates for P are chosen among the different values obtained with the selected couples of P_t and P_f . The candidates for P are validated if the span values of the resulting interleaved cells belong to one of the valid span sub-regions in the L¹space defined in III-B. Then, a limited number of values are kept for P, corresponding to the highest minimum time and frequency span values with low multiplicities in the complete OFDM frame. Finally, the selected P value is the one providing the best span properties with a low MI distribution variance.

B. Double Regular Interleaver

A Double Regular Interleaver (2RI) consists of two regular permutations in the time and frequency axes. The write cell address $\Pi(i)$ can be expressed using its carrier index $f_{\Pi(i)}$ and its OFDM symbol index $t_{\Pi(i)}$ as:

$$\Pi(i) = NF \times t_{\Pi(i)} + f_{\Pi(i)} \tag{28}$$

where,

$$t_{\Pi(i)} = P_t \times t_i \bmod NT \tag{29}$$

$$f_{\Pi(i)} = P_f \times f_i \bmod NF \tag{30}$$

$$t_i = \lfloor i/NF \rfloor \tag{31}$$

$$f_i = i \bmod NF \tag{32}$$

As the permutation law is designed independently for the time and frequency components, a modification of the interleaver period on one axis, P_t or P_f , does not impact the histogram of the other component, unlike the RI family. Consequently, the L¹ space representation is of no help in this case. On the other hand, the time interleaver component as defined in (29) has an important drawback: neighboring cells within the same OFDM symbol and belonging to the same FEC block are interleaved to the same OFDM symbol. To deal with this, a periodic shift $S_T \times (f_i \mod NT)$ is introduced into the time component (Fig. 10). Thus, (29) becomes:

$$t_{\Pi(i)} = (P_t \times t_i + S_T \times (f_i \bmod NT)) \bmod NT$$
(33)

 P_t , S_T and P_f are chosen from the same groups of admissible values for P_t and P_f considered in the RI family. Since the permutation law is designed component by component, the optimum P_f value can be identified via the frequency span criterion. Then, with P_f fixed to its optimum value, the best values for P_t and S_T are determined as those providing the



Fig. 10. Example of periodic shift with 7 OFDM symbols.

best time span property with a low MI distribution variance. Finally, the 2RI permutation law is defined by (28) using (30) and (33) as components.

C. Almost Regular Permutation Interleaver

The effect of regular error patterns can be mitigated by the introduction of a minimum degree of disorder into the regular structure of the permutation. Such techniques have already been investigated in the past for the design of turbo codes: Almost Regular Permutations (ARP) [12] and Dithered Relative Prime (DRP) interleavers [22] belong to this category of interleavers.

To obtain an ARP interleaver, the structure of the RI interleaver is modified by introducing a vector of shifts whose length is equal to the degree of the introduced disorder. First, the best interleaver period P in the RI family is used as the interleaver period of the ARP. Then, the permutation law is obtained by introducing a vector of shifts **SG** in (26) that leads to:

$$\Pi(i) = (P \times i + SG[i \mod Q]) \mod NC \tag{34}$$

To ensure the bijectivity of the ARP function, the disorder degree Q must be a divisor of the total number of cells NC. In order to limit the search space for the shifts, Q is selected from the lower divisors of NC. In practice, the Q candidate shifts are randomly set one by one and submitted for validation: a shift vector is valid if the span values of the resulting interleaved cells belong to one of the valid span sub-regions in the L¹ space defined in III-B. Finally, the best candidate shifts are those allowing the best span properties with a low MI distribution variance.

D. Double Almost Regular Permutation Interleaver

The 2RI structure is modified by replacing each regular interleaver component by an ARP component: a shift vector is introduced in each axis, the vector length being equal to the degree of the introduced disorder. The resulting permutation is called Double Almost Regular Permutation (2ARP). Then, to define the frequency ARP component ARP_f , a vector of frequency shifts **SF** is introduced in (30):

$$f_{\Pi(i)} = (P_f \times f_i + SF[f_i \mod Q_f]) \mod NF \tag{35}$$

To ensure the bijectivity of this function, the frequency disorder degree Q_f must be a divisor of the number of carriers, NF. Similarly, on the time axis a vector of time shifts **ST** is

introduced to define the time ARP component, ARP_t . Equation (33) becomes:

$$t_{\Pi(i)} = (P_t \times t_i + S_T \times (f_i \mod NT) + ST[(f_i \mod NT) \mod Q_t]) \mod NT \quad (36)$$

To ensure the bijectivity of this function, the time disorder degree Q_t must be a divisor of the number of OFDM symbols, NT. It is worth noting that S_T is taken as the interleaver period for the ARP_t component, since S_T represents a time interleaver period for neighboring cells within the same OFDM symbol. Then, the 2ARP permutation law is defined by (28) using (35) and (36) as components.

Due to the introduction of ARP components, the number of interleaver parameters to be set is increased. Consequently, the design procedure is divided into the following steps:

Step 1. Determine the candidate vectors for **SF** in the ARP_f: The P_f value obtained for the 2RI is used as interleaver period in this component. In order to limit the search space for the frequency shifts, Q_f is selected from the lower divisors of NF. Then, in a vector of length NF the shifts of **SF** are defined. The Q_f candidate shifts are randomly set one by one and submitted for validation. The shifts are valid if the minimum span obtained is close to the one obtained with a regular interleaver period of P_f . A group of candidate vectors for **SF** is generated.

Step 2. Select the best candidate vectors for **SF**: The group of candidate vectors for **SF** are analyzed in the complete OFDM frame, using the best time component interleaver obtained in the 2RI design for the time axis. A first selection is carried out by applying the frequency span criterion. Then, the selected vector is the one providing the lowest MI distribution variance.

Step 3. Determine the candidate vectors for **ST** in the ARP_t: First, the S_T value obtained for the 2RI is used as the interleaver period for this component. Then, a group of candidate vectors for **ST** is generated in a vector of length *NT* following the guidelines presented in step 1. Other groups of candidates are generated by taking S_T from the best group of admissible values considered in the RI family.

Step 4. Select the best candidate vectors for **ST**: The group of candidate vectors for **ST** are analyzed in the complete OFDM frame, using the best ARP_f component obtained in step 2 for the frequency axis, and taking the candidate values for P_t from the group of admissible values considered in the RI family. Different couples of candidates for P_t and **ST** are analyzed. Finally, the best couple of P_t and **ST** is identified as the one providing the best time span property with a low MI distribution variance.

E. Application to DVB-T2

We have applied the previous guidelines to design RI, 2RI, ARP and 2ARP interleavers, for the frame parameters of DVB-T2 listed in Table I.

For the RI permutation law, all the admissible values for P_t are represented in Fig. 11. In practice, only the values of P_t allowing the highest minimum span, i.e. 24, are selected as candidates. The candidate values for P_f are selected in



Fig. 11. Admissible interleaver period values for a regular permutation in a vector of length NT=357.

the same way for NF=1705 carriers. Finally, only the combinations of P_t and P_f with the best time and frequency span properties and the lowest MI distribution variances in the TU6 channel are chosen. The four best candidates for P are given in Table II for NT=357 and NF=1705.

TABLE II BEST P values with NT=357, and NF=1705.

RI	Р	VAR
Ι	40627	2.42×10^{-7}
II	40373	$2.75 imes 10^{-7}$
III	284188	$2.28 imes 10^{-7}$
IV	81293	3.48×10^{-7}

Three parameters have to be obtained to define the permutation law of the 2RI: P_f , P_t and S_T . First, the best candidate value for P_f is identified as the one providing the maximum value of minimum frequency span with the lowest multiplicity. For the current OFDM configuration, 293 turns out to be the best value for P_f . Second, given that the time span properties depend not only on the value of P_t but also on its interaction with S_T , the best couples for such values are determined by taking as candidates the admissible values for P_t allowing a minimum span value between 19 and 24 from Fig. 11. Finally, the couples of P_t and S_t corresponding to the lowest MI distribution variances in the TU6 channel are chosen. The four best candidates for P_t and S_T are given in Table III for P_f = 293, NT=357 and NF=1705.

TABLE III BEST P_t and S_T values with P_f =293, NT=357, and NF=1705.

2RI	P_t	S_T	VAR
		-	
Ι	193	127	2.00×10^{-7}
Π	163	230	2.13×10^{-7}
III	200	127	$3.02 imes 10^{-7}$
IV	157	230	$2.66 imes 10^{-7}$

The best RI period is used as the interleaver period in the ARP permutation law. Given that the total number of cells in the OFDM frame is 608,685, the ARP disorder degree Q can be: 3, 5, 7, 11, 17, or 31. Considering the large depth of this interleaver, Q was set to 5 or 7, avoiding too long an exploration time, whilst maintaining a reasonable disorder degree. Then, the optimal **SG** vectors are obtained as described in V-C. Finally, to evaluate the performance of the ARP candidate interleavers in terms of MI distribution, a regular erasure pattern of 15% is introduced in the TU6 channel, since the disorder of ARP is intended to mitigate the effect of such error patterns. Table IV lists the best candidates for **SG**.

TABLE IV BEST ARP INTERLEAVERS WITH SG[0] = 0, P = 40627, NT = 357, and NF = 1705.

ARP	Ι	II	III	IV
\overline{Q}	5	5	5	7
SG[1]	292436	532541	533907	212779
SG[2]	605520	156805	422013	579212
SG[3]	117595	366665	337345	348202
SG[4]	412029	567614	377385	528456
SG[5]	-	-	-	303822
SG[6]	-	-	-	478957
VAR	3.64×10^{-6}	1.79×10^{-6}	3.44×10^{-6}	2.40×10^{-6}

The permutation law of the 2ARP interleaver is defined by its two ARP component functions. Due to the number of parameters to define, the complete design procedure is presented in the Appendix. The best candidate vectors for the ARP_f component are determined via the frequency span criterion. Then, their performance in terms of MI distribution is evaluated. Table V lists the best vectors for the ARP_f component function. Similarly, the best candidate vectors for the ARP_t component are identified. Table VI lists the best 2ARP candidate interleavers, which are composed of the best **ST** vectors shown in the table, and the ARP_f I function from Table V.



Fig. 12. Time span histogram for the best proposed interleavers.



Fig. 13. Frequency span histogram for the best proposed interleavers.

TABLE V Best SF values with SF[0]=0, $P_t=193$, $S_T=127$, $P_f=293$, NT=357, and NF=1705.

$\operatorname{ARP}_{\mathrm{f}}$	SF[1]	SF[2]	SF[3]	SF[4]	VAR
Ι	0	293	1412	0	$1.73 imes 10^{-7}$
II	1704	3	2	1	2.12×10^{-7}
III	243	1266	1509	1607	2.63×10^{-7}
IV	98	976	1609	1462	2.65×10^{-7}

Figs. 12 and 13 show the first 100 values of the time and frequency span histograms of the best interleavers from the different families. As expected, the interleavers allowing the highest values of minimum time and frequency span are those based on regular permutation (i.e, RI I, and 2RI I). According to the time span histogram, the best ARP-based interleaver is ARP II. This interleaver slightly reduces the span value multiplicity, whilst keeping a high minimum span. In contrast, with 2ARP I the minimum time span value decreases to 12,

TABLE VI Best 2ARP interleavers with ST[0]=0, NT=357, and NF=1705.

2ARP	Ι	II	III	IV
P_t	53	197	62	320
S_T	127	23	23	23
ST[1]	73	213	213	113
ST[2]	78	63	63	18
ST[3]	285	114	114	20
ST[4]	78	327	327	24
ST[5]	190	20	20	283
ST[6]	24	306	306	46
VAR	8.81×10^{-7}	9.97×10^{-7}	1.94×10^{-6}	1.06×10^{-6}

which is a considerable reduction compared to the theoretical value of 26. Finally, the frequency span histogram also shows ARP II to be the best ARP-based interleaver, since it reduces the span value multiplicity more than 2ARP I.

F. Interaction Between Channel Interleaver and BI

Correlated coded bits are defined as coded bits connected to the same check node in the LDPC parity-check matrix. In general, the Bit Interleaver (BI) has to map correlated bits to different constellation symbols or cells. To ensure a good interaction between our proposed channel interleavers and the BI, correlated coded bits must be mapped to neighboring cells, but not to the same cell. Afterwards, neighboring cells are spread out by the channel interleaver, ensuring that correlated coded bits are placed neither in neighboring cells, nor in the same cell. Therefore, if deep fading affects a particular constellation symbol, it affects only one of the bits connected to a given check node. Thanks to the contribution of the remaining connections, the affected bit can then be recovered.

In most cases, the BI in the DVB-T2 transmission chain is composed of a parity and a column twist interleaver [10]. In our case study, the codeword length is 16,200 with a QPSK constellation. For these parameters, only the parity interleaver is included [20]. Therefore, correlated coded bits are mapped to different cells far away in the frame, which is not suitable for the channel interleavers we propose. For easy identification of correlated coded bits, the proposed new BI is based on the DVB-T2 parity and column-row interleaver for a codeword length of 16,200 with a 16-QAM constellation. According to [8], the column-row memory block thus has eight columns, as shown in Fig. 14. Then, correlated bits are placed in the same row of the memory block. In the new BI the coded bits are no longer read out row-wise from the memory block, but rather following the mapping mask given in Table VII.



Fig. 14. Column-row and parity interleaver

TABLE VII New BI Mapping mask for bits read out from the memory block and written in the cells.

Read	Write	Read	Write	Read	Write	Read	Write
0	0	17	10	20	20	11	30
8	1	33	11	30	21	27	31
1	2	6	12	21	22	24	32
9	3	38	13	31	23	34	33
2	4	7	14	14	24	25	34
18	5	39	15	22	25	35	35
3	6	4	16	15	26	12	36
19	7	28	17	23	27	36	37
16	8	5	18	10	28	13	38
32	9	29	19	26	29	37	39

G. Impact on Latency and Complexity

The impacts of the adoption of the proposed interleaving structures on the latency and hardware complexity of the channel interleaver are analyzed below.

1) Impact on latency: In the complete T2 interleaver, the component interleavers operate at different levels: the CI operates on cells inside a FEC block, the TI operates on several FEC blocks and the FI operates on the OFDM subcarriers of each symbol. The CI reads cells from its input vector in normal order and writes them to its output vector in permuted order. Therefore, the TI is supposed to wait until the CI output vector is completed to start reading the cells from it and writing them column-wise to the TI memory block. The FI reads cells from the TI memory block row-wise in permuted order and writes them to its output vector in natural order. Thus, the FI is supposed to wait until the whole TI memory block is completed to start writing the cells to its output vector. Consequently, the three interleaving steps adopted in the standard cannot be performed jointly in one step, since they operate on different sizes. In contrast, our proposed channel interleavers operate on the total interleaving depth size. Therefore, they can be performed directly in one step. Thus, proposed channel interleavers allow a reduction on the overall system latency corresponding to the cumulated CI and FI latencies.

2) Impact on complexity: Two different levels of complexity have to be considered. First, the memory required to store the data to be interleaved, which is the dominant factor in terms of silicon area. Table VIII compares these requirements for the complete T2 interleaver and our proposal. The proposed interleavers only require the TI memory block. saving the CI and the FI memory space. The TI size represents the dominant term for DVB-T2. However, with the FFT size of 32k adopted in the standard, the memory requirements for the FI are no longer negligible. On the other hand, the complexity related to the implementation of the permutation function (i.e., to compute interleaved memory addresses) must be considered. It highly depends on the permutation function. Both the complete T2 and our proposed interleavers require only very simple address computation logic. The CI and FI address computations are based on simple linear feedback shift registers. The DVB-T2 TI is a simple column-row interleaver and only a limited number of parameters have to be stored, depending on the LDPC codeword length and modulation mode. For the proposed interleavers, the address computation complexity is similar to the case of a column-row interleaver, since the same operations are involved. The only difference lies in the number of parameters to store. For each interleaving size, the proposed interleavers need to store the number of parameters listed in Table IX. Therefore, all things considered, the proposed channel interleavers are less complex, especially due to reduced memory requirements.

VI. SIMULATION RESULTS

Computer simulations were carried out to evaluate the performance of the proposed channel interleavers, including the new BI structure. We considered transmissions over a TU6

TABLE VIII MEMORY REQUIREMENTS FOR THE COMPLETE T2 AND PROPOSED CHANNEL INTERLEAVERS.

Interleaver	Number of blocks to store
Complete T2	(NFEC+1) FEC blocks and 1 OFDM symbol
Proposed interleavers	NFEC FEC blocks

TABLE IX Number of parameters to store to implement proposed interleavers.

Interleaver	Number of parameters to store
RI	1
2RI	3
ARP	Q + 1
2ARP	$Q_t + Q_f + 3$

and a P1 channel, with and without regular erasure patterns on the OFDM carriers. These patterns can be caused by manmade noise, e.g., motor vehicle ignition noise [23]. Indeed, several man-made noise sources generally cause error bursts for broadcast signals. The corresponding model is performed via the introduction of erasure events as proposed in [24]. For comparative purposes, the complete T2 interleaver structure was also simulated. The simulation parameters are listed in Table I. The erasure ratio of 15% is an average value considered during the specification of DVB-T2 [20]. Additional simulation results are presented for the LDPC effective code rate 37/45, which corresponds to LDPC code rate identifier 5/6 [8].

Figs. 15 and 16 show the BER performance of the proposed channel interleavers for LDPC code rate 2/3 over a TU6 and a P1 channel, respectively. In both channel types the performance of the proposed interleavers is very close to the performance of the complete T2 interleaver. Actually, in normal channel conditions, the time and frequency diversities allowed by the FEC code and the OFDM frame are large enough for the complete T2 interleaver to recover from channel impairments. In contrast, when the transmitted signal undergoes a regular erasure pattern of 15%, the performance improvement due to the proposed interleavers can be easily identified. As shown in Figs. 15 and 16, the performance gain is about 0.5 and 0.8 dB over a TU6 and a P1 channel, respectively compared to the complete T2 interleaver performance. Fig. 17 compares the corresponding MI distributions over the TU6 channel with 15% of erasures. One can observe that the MI of the complete T2 interleaver is no longer uniformly distributed, thus bringing out its weakness in such severe channels.

Figs. 18 and 19 show the BER performance of the proposed channel interleavers for the LDPC effective code rate 37/45 over a TU6 and a P1 channel, respectively. In normal channel conditions the same conclusions as for the code rate 2/3 can be drawn. Nevertheless, the system performance improvements with the proposed interleavers are increased for transmissions with erasures. As shown in Fig. 18, over a TU6 channel, the performance gain obtained with the 2ARP I and 2RI I is about 5 dB compared to the complete T2 interleaver performance,



Fig. 15. BER performance comparison between the best interleavers over the TU6 channel for LDPC code rate 2/3.



Fig. 16. BER performance comparison between the best interleavers over the P1 channel for LDPC code rate 2/3.

and about 7 dB with the RI I and ARP II interleavers. Over the P1 channel, similar gains can be observed with the 2ARP I and 2RI I interleavers (4 dB) and the RI I and ARP II interleavers (6 dB), as shown in Fig. 19. The performance gap observed between the RI I/ARP II and 2ARP I/2RI I interleavers can be explained by a better interaction of the former interleavers with the BI, for this code rate. When the correction capability is weakened, the impact of this interaction becomes greater.

According to these results, performance improvements are expected when increasing the code rate or the erasure ratio, provided that the latter does not exceed the redundancy ratio



Fig. 17. MI Distribution, $\rm E_s/\!N_0$ = 8 dB, TU6 channel with 15% of erasures, for LDPC code rate 2/3.



Fig. 18. BER performance comparison between the best interleavers over the TU6 channel for LDPC effective code rate 37/45.

bound. To illustrate these trends, Fig. 20 shows the BER performance of the ARP II and the complete T2 interleavers, for LDPC code rate 2/3 over a TU6 channel with different erasure ratios. The ARP II gain increases from 0.5 to almost 1.5 dB, when the erasure ratio increases from 15 to 20%.

In order to evaluate the proposed channel interleavers with higher-order modulations, Figs. 21 and 22 show the BER performance of the ARP II and complete T2 interleavers for 16-QAM modulation and LDPC effective code rate 37/45 over the TU6 and P1 channels. Similarly to the QPSK case, BER performance of both interleavers remains very close for normal channel conditions. When the transmitted signal



Fig. 19. BER performance comparison between the best interleavers over the P1 channel for LDPC effective code rate 37/45.



Fig. 20. BER performance comparison between ARP II and complete T2 interleavers over the TU6 channel for LDPC code rate 2/3 and different erasure percentages.

undergoes a regular erasure pattern of 15%, a performance gain of about 2.5 dB in both channels is observed, although 16-QAM makes constellation symbols more vulnerable to channel impairments than QPSK. Therefore, the proposed interleaver structure is also appropriate for the different constellation orders considered in the DVB-T2 standard.

VII. CONCLUSIONS

In this paper, we have presented a new method to design channel interleavers. It calls for a joint optimization of time and frequency span properties. A graphical representation of the span properties in a bi-dimensional L^1 space can be used to efficiently parameterize interleavers.

The MI distribution between FEC blocks was identified as a relevant selection criterion for channel interleavers. A suitable target is a homogeneous distribution of the MI in the FEC blocks. Thus, it is possible to select the best channel interleaver candidates according to the MI distribution variance, before running long BER simulations.



Fig. 21. BER performance comparison between ARP II and complete T2 interleavers over the TU6 channel for LDPC effective code rate 37/45 and 16-QAM modulation.



Fig. 22. BER performance comparison between ARP II and complete T2 interleavers over the P1 channel for LDPC effective code rate 37/45 and 16-QAM modulation.

Improvements in the BER performance of the DVB-T2 chain can be achieved when using this approach, especially in poor channel conditions, such as in the presence of regular erasure patterns. Furthermore, the reduction in the number of channel interleaving components allows better control of the interleaver design parameters and provides reductions in system latency and complexity.

In transmission systems including a bit interleaver (BI), it was shown that a good interaction between the BI and the channel interleaver is achieved by using an appropriate constellation symbol mapping mask.

A further optimization of the interleavers in a Multiple Input Single Output (MISO) transmission still has to be undertaken to consider all DVB-T2 transmission scenarios.

APPENDIX 2ARP INTERLEAVER DESIGN

The permutation law of the 2ARP interleaver is defined by its two component functions ARP_f and ARP_t . Due to the number of parameters to define, the design procedure is divided into the four steps presented in V-D:

Step 1. Determine the candidate vectors for **SF** in the ARP_f: First, P_f is fixed to 293. Since the frequency disorder degree Q_f must be a divisor of NF=1705, Q_f can only be 5, 11 or 31. Only Q_f =5 was considered in order to limit the search space, avoiding too long an exploration time. Then, the best **SF** vectors are determined in a vector of length 1705 as described in V-D. A group of 19 candidates for **SF** giving a minimum span between 55 and 56 is identified.

Step 2. Select the best candidate vectors for **SF**: A selection via the frequency span criterion is carried out in the complete OFDM frame using the time component of the 2RI I in the time axis. Then, the performance of the best candidate vectors in terms of MI distribution is evaluated. Table V lists the best candidate vectors for **SF** as well as the corresponding MI distribution variance on the TU6 channel.

Step 3. Determine the candidate vectors for **ST** in the ARP_t: Given that the OFDM frame has 357 OFDM symbols, the time disorder degree Q_t can be: 3, 7, or 17. To avoid too long an exploration time, whilst maintaining a reasonable disorder degree, Q_t is fixed to 7. Then, the shifts of **ST** are defined in a vector of length 357. Two groups of candidates are obtained: in the first one S_T is fixed to 127 (best value in the 2RI family), and in the second one to 23, since this is one of the admissible interleaver period values given the maximum of the minimum span from Fig. 11. Finally, 40 candidate vectors for **ST** giving a minimum span between 21 and 23 are determined following the guidelines in V-D.

Step 4. Select the best candidate vectors for **ST**: A selection via the time span criterion is carried out in the complete OFDM frame using the ARP_fI component in the frequency axis, and taking as possible values for P_t those giving a minimum span value between 21 and 24 from Fig. 11. Even if we consider a large group of candidates for the ARP_t component, the maximum value of the minimum time span is 12. In fact, as the time diversity gets smaller than the frequency diversity for the current OFDM configuration, the minimum

time span values are affected more by the introduced disorder than the minimum frequency span values are. Finally, the performance of the best 2ARP candidate interleavers, which are composed of the $ARP_{f}I$ function and the best **ST** candidate vectors, is evaluated in terms of MI distribution over the TU6 channel with a regular erasure pattern of 15%. Table VI lists the best 2ARP candidate interleavers.

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