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SHORTEST PATH RESOLUTION USING HADOOP

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ABSTRACT: The fast growth of scientific and business data has resulted in the evolution of the cloud computing. The MapReduce parallel programming model is a new framework favoring design of algorithms for cloud computing. Such framework favors processing problems across huge datasets using a large number of computers. Hadoop is an implementation of MapReduce framework that becomes one of the most interesting approaches for cloud computing. Our contribution consists in investigating how the MapReduce framework can create new trend in design of operational research algorithms and could define a new methodology to adapt algorithms to Hadoop. Our investigations are directed on the shortest path problem on large-scale real-road networks. The proposed algorithm is tested on a graph modeling French road network using the OpenStreetMap data. The computational results push us into considering that Hadoop offers a promising approach for problems where data are so large that numerous memory problems and excessive computational time could arise using a classical resolution scheme.

KEYWORDS: *Shortest path, cloud, hadoop, MapReduce.*

1 INTRODUCTION

The rapid growth of internet since last decades has led to a huge amount of information which has created a trend in design of modern data center and massive data processing algorithms especially in the cloud. Hadoop is one of the most interesting approaches for cloud computing which is an implementation of MapReduce framework first introduced and currently promoted by Google. In this article, we are interested in evaluating how hadoop framework offers a promising approach for operational research algorithms. Here we consider the shortest path problem (SPP) on large-scale real-road networks. The adaptation of shortest path algorithms (commonly used in resolution of scheduling problems or routing problems) for the clouds, required attention since the applications must be tuned to frameworks which take advantages of the cloud resources (Srirama et al., 2012).

1.1 Shortest path problems

Shortest path problems drawn attention for use in various transportation engineering applications. Without any doubt it could be directly attributed to the recent developments in Intelligent Transportation Systems (ITS), particularly in the field of Route Guidance System (RGS). The current RGS field in both North America and Europe has generated new interest in using heuristic algorithms to find shortest paths in a traffic network for vehicle routing operations. (Guzolek and Koch, 1989) discussed how heuristic search methods could be tuned for vehicle navigation systems. (Kuznetsov, 1993)

debates applications of an A* algorithm, a bi-directional search methods, and a hierarchical search one.

Several researchers have been addressed the definition of efficient search strategies and mechanisms. For example, the multi-objective shortest path problem is addressed by Umair et al. in 2014 (Umair et al., 2014). They introduced an evolutionary algorithm for the MOSP (Multi-Objective Shortest Path). They have also presented a state of the art on the MOSP where publications are gathered into classes depending on the approaches. Some authors including, but not limited to (Tadao, 2014), introduced new advance in complexity improvement in classical shortest path algorithms based on bucket approaches. (Cantone and Faro, 2014) introduced lately a hybrid algorithms for the Single Source Shortest Paths (and all-pairs SP) which is asymptotically fast in some special graph configurations. A recent survey of (Garroppo et al., 2010) focuses on the multi-constrained approximated shortest path algorithms representing by recent publications of (Gubichev et al., 2010) or (Willhalm, 2005).

1.2 Parallel data-processing paradigm with hadoop

Hadoop is an open-source Apache project which provides solutions for storage and large-scale distributed computing. It relies on two components: the first one Hadoop Distributed File System (HDFS) which allows to store large files across multiple computers; the second component is the wide spread MapReduce engine (Dean J. and S. Ghemawat, 2008) which provides a programming model for large-scale distributed computing.

As stressed in the figure 1, a hadoop system consists of a master and several slave nodes. The master should consist a NameNode and a JobTracker to manage respectively data storage and computation jobs scheduling. A slave node could be a DataNode for data

storage or/and a TaskTracker for processing computation jobs. A secondary NameNode can be used to replicate data of the NameNode to provide a high quality of service.

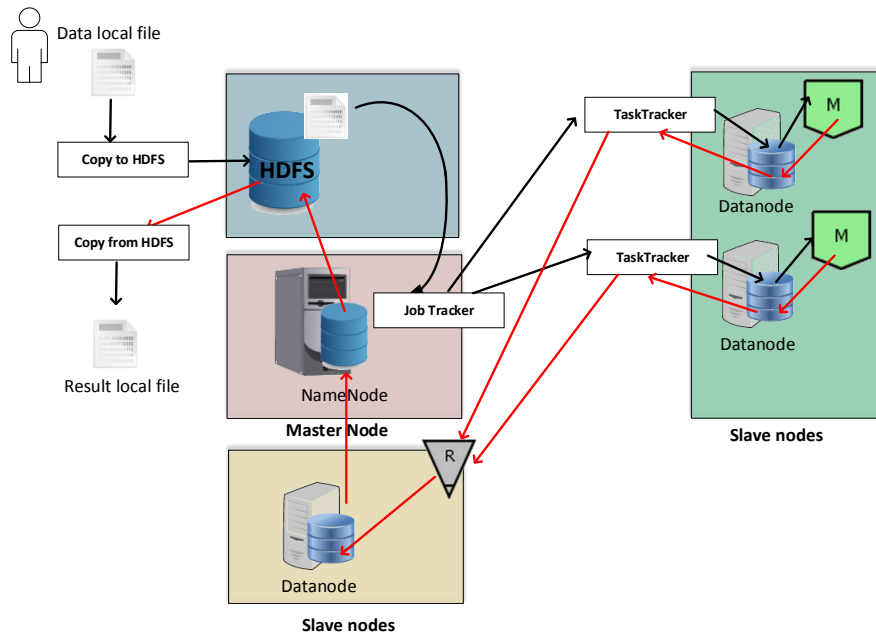


Figure 1: Typical component of one hadoop cluster

Hadoop uses the MapReduce engine as the parallel data-processing paradigm. Cohen in 2009 (Cohen, 2009) prove that MapReduce could be successfully applied for specific graph problems, including but not limited to computation of graph components, clustering, rectangles/triangles enumeration. MapReduce has also been used for scientific problems by (Bunch et al., 2009) proving that it could be used to solve problems including the Marsaglia polar method for generating random variables and integer sort. In (Sethia and Karlapalem, 2011), the authors explore the benefits hadoop-based multi-agents simulation framework implementation.

1.3 Hadoop terminology

In hadoop terminology, by 'job' we mean execution of a Mapper and Reducer across a data set and by 'task' we

mean an execution of a Mapper or a Reducer on a slice of data. Hadoop distributes the Map invocations across several computers by partitioning the input data automatically into a set of independent splits. Those input splits are processed in parallel as Mapper tasks on slave nodes.

Hadoop invokes a Record Reader method on the input split to read one record per line until the entire input split has been consumed. Each call of the Record Reader leads to another call to the Map function of the Mapper. Reduce invocations are distributed by splitting the key space into R pieces using a splitting function. One more thing to mention here is that some problems require a succession of MapReduce steps to accomplish their goals.

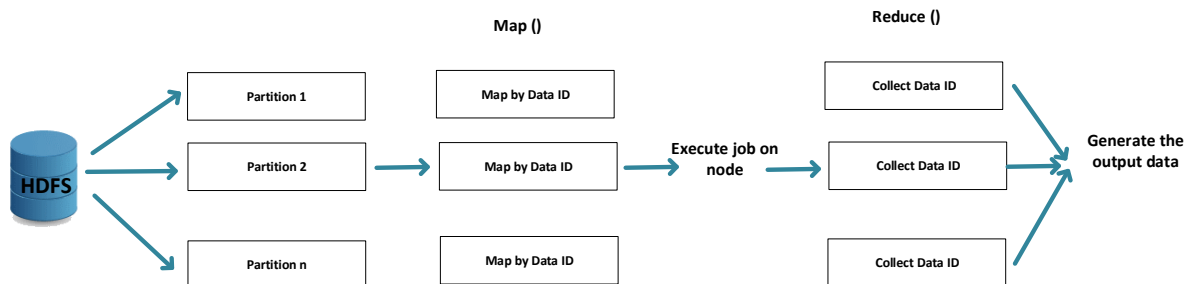


Figure 2: MapReduce Flow

As shown in figure 2, a MapReduce task consists in two following steps: first the Map tasks are scheduled and second the Reduce tasks. It gets periodic updates from

the datanodes about the average time on each datanode. The information on average time permits distribution of tasks favoring the faster datanodes.

Hadoop is a new trend in parallel and distributed computing. Providing a full integration into cloud architectures, hadoop permits to operational researchers to focus on the parallelization of algorithms without consideration of the network infrastructure required to achieve the computation. Hadoop is now proposed in numerous public and private cloud solutions including AWS, Google, IBM and Azure. Hadoop is a very interesting solution since it permits for a reasonable effort to create new parallel implementation of various algorithms.

This paper is organized as follow. In the next section, we present the proposed MapReduce-based method for large-scale shortest path problem. In Section 3, we describe the experimental study using large real-world

road networks. In Section 4, we conclude the work and we highlight some future works.

2 SHORTEST PATH RESOLUTION WITH HADOOP

2.1 Framework description

In the proposed framework for the shortest path computation, each iteration represents a single MapReduce pass. As stressed by (Srirama et al., 2012), such type of resolution scheme is difficult to benefit efficiently from parallelization, and the proposed framework does not guarantee to solve optimally the shortest path problem but lead to high quality solutions.

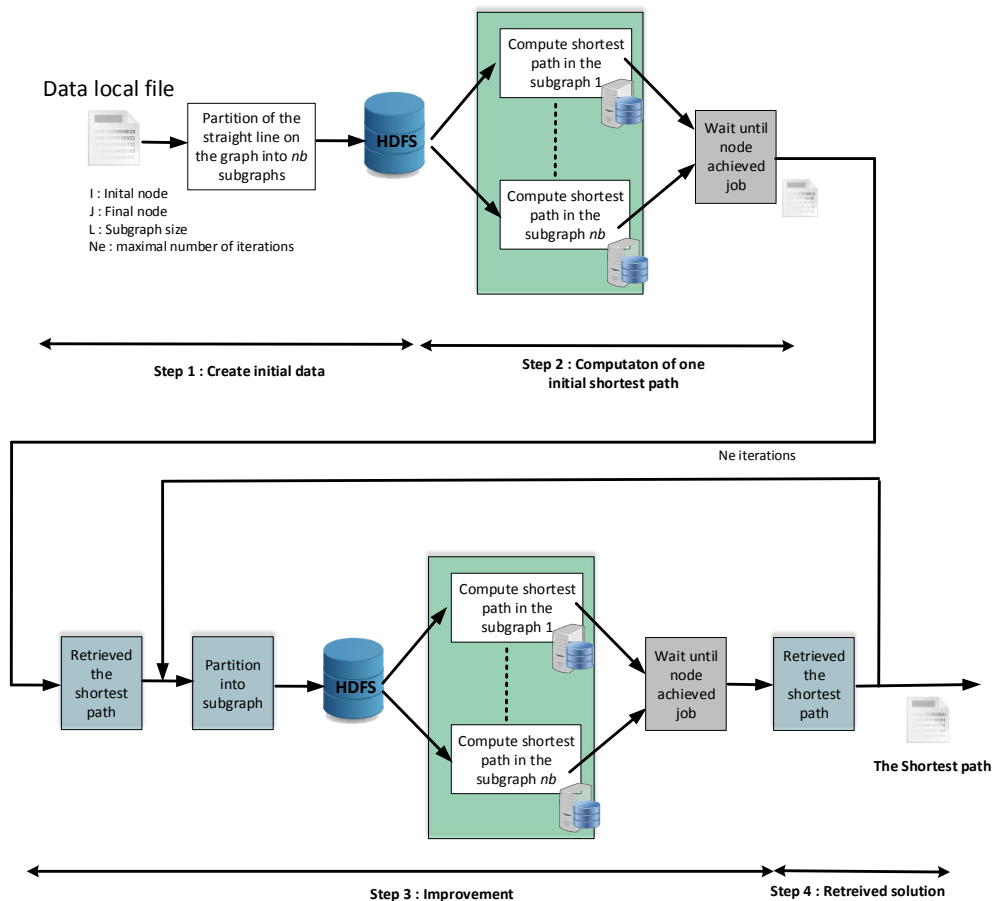


Figure 3: Hadoop based framework for the shortest path

2.2 Proposed algorithm

The hadoop-based shortest path resolution framework consists of 4 steps (see figure 3). The first step consists in uploading data to the hadoop file system. It consists also in specifying parameters like the initial/final positions, the maximal number of iterations and the subgraphs size. The second step aims to calculate one shortest path (Initial Shortest Path) which is iteratively improved in the next step. The initial shortest path computation begins with the creation of subgraphs which leads to jobs parallelization since computation of the

shortest path on each subgraph (noted as local shortest path) is considered as a job in hadoop. This step 2 is fully achieved when all local shortest paths have been uploaded from slave nodes. The initial shortest path is obtained by concatenating all local shortest paths.

The step 3 is an iterative improvement. In this step, a subgraph is defined by the middle points of two adjacent local shortest paths. One can note that the number of subgraphs depends the iteration number. It alternates between nb and $nb - 1$ where nb the number of subgraphs in step 2. The process is stopped when the number of iterations is reached. The step 4 consists in

downloading the results from the hadoop file system to a local directory. In the following, we present the algorithm of our approach (see Algorithm 1).

Algorithm 1. Hadoop shortest path framework

```

1. Procedure SSP_Hadoop_Framework
2. Input parameters
3.   L : subgraph size in km
4.   Ix, Iy : Initial latitude and longitude
5.   Jx, Jy : Final latitude and longitude
6.   Ne : maximal number of iterations
7. begin
8.   // Step 1. Create initial data
9.   (G,Dx,Dy,Ax,Ay) := Partition_Into_Subgraph(L,Ix,Iy,Jx,Jy);
10.  nb := |G|;
11.  // Step 2. Computation of the initial shortest path
12.  for j:=1 to nb do
13.    << copy G[j] from local to HDFS >>
14.    << G[j] will be copied from HDFS to a slave node >>
15.    SP''[j] = Start_Node_Job(G[j],Dx[j],Dy[j],Ax[j],Ay[j]);
16.  end for
17.  << wait until hadoop nodes have achieved work >>
18.  SP := Retrieved_Shortest_Path(SP'');
19.
20.  // Step 3. Improvement of the shortest path
21.  for i:=2 to Ne do
22.    if (i%2=0) Then
23.      for j:=1 to |SP| -1 do
24.        (Mx[j], My[j]) := the middle of the shortest path SP[j];
25.        (Mx[j+1], My[j+1]) := the middle of the shortest path SP[j+1];
26.        G[j] := Create_Graph(Mx[j], My[j], Mx[j+1], My[j+1]);
27.        << copy G[j] from local to HDFS >>
28.        << G[j] will be copied from HDFS to a slave node >>
29.        SP''[j] := Start_Node_Job(G[j], Mx[j], My[j], Mx[j+1], My[j+1]);
30.      end for
31.      << wait until hadoop nodes have achieved work >>
32.      SP' := Retrieved_Shortest_Path(SP'');
33.
34.      // Step 4. Load output files from the HDFS to local directory
35.      Load SP' from the HDFS to local directory
36.    else
37.      for j:=0 to |SP'| do // size of SP' = nb-1
38.        if (j=0)
39.          (Mx[j], My[j]) := (Ix, Iy);
40.        else
41.          (Mx[j], My[j]) := the middle of the shortest path SP'[j];
42.        end if
43.        if (j = |SP'|)
44.          (Mx[j+1], My[j+1]) := (Jx, Jy);
45.        else
46.          (Mx[j+1], My[j+1]) := the middle of the shortest path SP'[j+1];
47.        end if
48.        G[j+1] := Create_Graph(Mx[j], My[j], Mx[j+1], My[j+1]);
49.        << copy G[j+1] from local to HDFS >>
50.        << G[j+1] will be copied from HDFS to a slave node >>
51.        SP''[j+1] := Start_Node_Job(G[j+1], Mx[j+1], My[j+1], Mx[j+2], My[j+2]);
52.      end for
53.      << wait until hadoop nodes have achieved work >>
54.      SP := Retrieved_Shortest_Path(SP'');
55.
56.      // Step 4. Download data from HDFS
57.      Load SP from the HDFS to local directory
58.    end if
59.  end for
60.  return Concat(SP, SP', Ne);

```

In algorithm 1, lines 8-10 describe the first step. In which, the procedure `Partition_Into_Subgraph` consists in creation of subgraphs by dividing the "straight line" from an origin to a destination into several subgraphs according the predefined length (the diagonal length of subgraph). The subgraph data is created by extracting road information from the OpenStreetMap data. Figure 4 gives an example of subgraphs creation. It

consists in using the "straight line" from node I and J to create 4 subgraphs. A subgraph is defined by its origin node and destination node and the origin node of i^{th} subgraph is the destination node of $(i-1)^{th}$ subgraph. One can note that the origin position of i^{th} subgraph is the destination of $(i-1)^{th}$ subgraph, $\forall 1 < i \leq nb$, where nb the number of subgraphs.

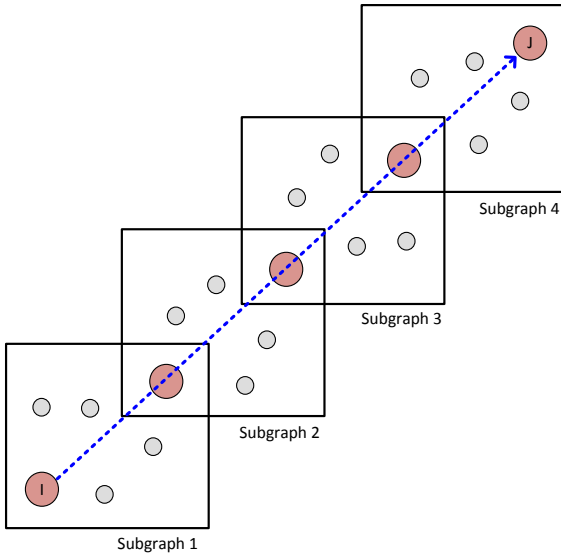


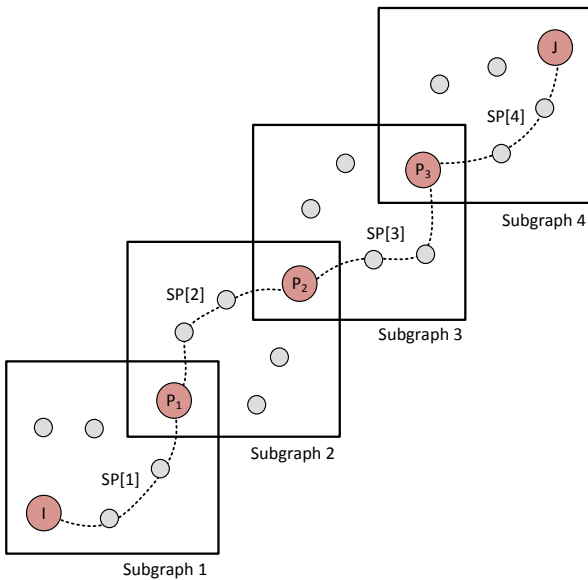
Figure 4: First partition and shortest path

Lines 11-18 illustrate the step 2 of algorithm. The procedure `Start_Node_Job` allows starting the computation of local shortest path on subgraphs using MapReduce engine. The procedure requires a subgraph G and the GPS coordinates of the origin and destination positions. In this step, it is possible that an origin or a destination does not correspond to a node of the subgraph. Therefore, a projection step is necessary to compute the nearest node of the subgraph from each GPS position before starting the shortest path computation. A Dijkstra algorithm is adapted here for the shortest path computation. As known, a classical shortest path problem can be solved using Dijkstra's

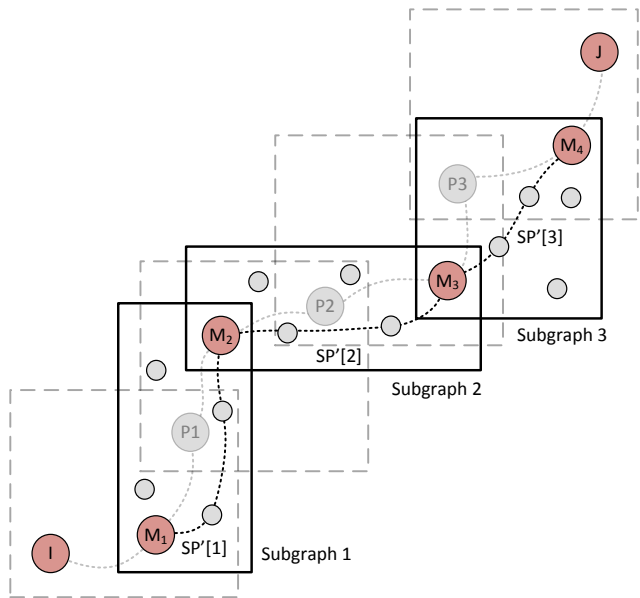
algorithm in $O(n \log n)$ with a priority queue such as a Fibonacci heap (Fredman and Tarjan, 1987) or 2-3 heaps (Takaoka, 1999). The obtained local shortest paths are saved into a vector denoted SP . One assumes that $SP[j]$ is the shortest path of the j^{th} subgraph.

Lines 21-32 and lines 36-54 describe the improvement step. The call of the procedure `Create_Graph` consists in creation the subgraphs induced by the middle of the shortest path of the current iteration (lines 24-25). As mentioned before, the subgraph number is different between an odd iteration and an even iteration. As shown in figure 5 (a), we assume that each square is one subgraph. At one odd iteration i , concatenating of the set of local shortest paths gives the initial shortest path from I to J .

Figure 5 (b) gives a solution at the even iteration $i + 1$. Considering SP the set of local shortest paths obtained at iteration i and $nb = |SP|$, a node M_j (with its coordinates $Mx[j], My[j]$) is the node corresponds to the middle of $SP[j]$ in terms of kilometers (the nearest node to the middle of the path). The subgraph creation consists in encompassing the nodes M_j and M_{j+1} . In this example, 3 subgraphs have been created. The obtained set of local shortest paths is denoted SP' . One can note that the concatenations of all local shortest paths do not give the path from I to J . It is necessary to include the path from the node I to M_1 and the path from M_4 to J in order to form a solution to the initial problem. To do so, we have to use the set of local shortest paths obtained at iteration i .



(a) set of LSP at an odd iteration i



(b) set of LSP at an even iteration $i + 1$

Figure 5: Two adjacent iterations of shortest paths computation

Line 34 and line 57 describe the last step which consists in downloading the results of last of two iterations from the hadoop file system. The shortest path is obtained by

calling the procedure `concat` which takes 3 parameters including the number of iterations and the solutions of two last iterations.

3 NUMERICAL EXPERIMENTS

All tests were conducted using hadoop 0.23.9 with a cluster of 8 homogenous nodes. Each node is a PC with AMD Opteron processor (2.3 GHz) under Linux (CentOS 64-bit). The number of cores used for experiments is limited to 1. The iteration number of algorithm is set to 2.

3.1 Instances

A graph of French road network has been created using the OpenStreetMap data. The road profile is fixed to pedestrian. A group of 15 instances are created using the same graph. Each instance contains an origin and a destination (see table 1). The subgraph size $D \in \{15, 30, 50, 100, 150, 200, +\infty\}$ km is addressed. Note that the graph will not be split into subgraphs when $D = +\infty$. The used graph can be downloaded from: http://www.isima.fr/~lacomme/hadoop_mosim/.

Instance	Origin		Destination	
	City	GPS position	City	GPS position
1	Clermont-Ferrand	45.779796 3.086371	Montluçon	46.340765 2.606664
2	Paris	48.858955 2.352934	Nice	43.70415 7.266376
3	Paris	48.858955 2.352934	Bordeaux	44.840899 -0.579729
4	Clermont-Ferrand	45.779796 3.086371	Bordeaux	44.840899 -0.579729
5	Lille	50.63569 3.062081	Toulouse	43.599787 1.431127
6	Brest	48.389888 -4.484496	Grenoble	45.180585 5.742559
7	Bayonne	43.494433 -1.482217	Brive-la-Gaillarde	45.15989 1.533916
8	Bordeaux	44.840899 -0.579729	Nancy	48.687334 6.179438
9	Grenoble	45.180585 5.742559	Bordeaux	44.840899 -0.579729
10	Reims	49.258759 4.030817	Montpellier	43.603765 3.877974
11	Reims	49.258759 4.030817	Dijon	47.322709 5.041509
12	Dijon	47.322709 5.041509	Lyon	45.749438 4.841852
13	Montpellier	43.603765 3.877974	Marseille	43.297323 5.369897
14	Perpignan	42.70133 2.894547	Reims	49.258759 4.030817
15	Rennes	48.113563 -1.66617	Strasbourg	48.582786 7.751825

Table 1: Instances data

3.2 Influence of the subgraphs size on the results quality

Table 2 contains the computational results for different subgraph sizes from 15 to 200 kilometers. In which, the optimal solutions is obtained using $D = +\infty$ which lead to computation of a shortest path on the whole graph. Column "Ins." contains the instance; column "Opt." contains the optimal solution (execution of a Dijkstra algorithm in the whole graph); columns "Val." reports the obtained value with 2 iterations; and "Gap" is the gap

(%) the best found solution to the optimal value. As shown in in the table 2, the average Gap is improved when we increase subgraph size. More precisely, the average Gap is improved from 9.55% to 1.11%. When $D = 200$ km, the optimal solution were obtained for 6 instances out of 15. On the other hand, when $D \leq 30$ km, no feasible solution is found for several instances. Since the nodes distribution could arise several problems of connectivity in small subgraphs.

Ins.	D = 15			D = 30			D = 50			D = 100			D = 150			D = 200		
	Opt.	Val.	Gap	Val.	GAP	Val.	GAP	Val.	GAP	Val.	GAP	Val.	Gap	Val.	GAP	Val.	GAP	
1	87.1	96.8	11.11	92.3	5.95	87.1	0.00	87.1	0.00	87.1	0.00	87.1	0.00	87.1	0.00	87.1	0.00	
2	841.2	-	-	-	-	934.7	11.12	908.7	8.02	854.7	1.60	850.5	1.09	850.5	1.09	850.5	1.09	
3	537.4	574.3	6.87	557.7	3.78	549.5	2.25	542.4	0.93	542.0	0.85	537.4	0.00	537.4	0.00	537.4	0.00	
4	355.6	381.6	7.31	375.1	5.49	369.6	3.95	361.5	1.67	355.6	0.00	358.0	0.68	358.0	0.68	358.0	0.68	
5	883.8	954.4	7.99	933.2	5.59	926.4	4.82	912.9	3.29	913.1	3.31	908.7	2.82	908.7	2.82	908.7	2.82	
6	948.2	1032.0	8.84	1007.5	6.25	989.6	4.37	971.8	2.48	970.3	2.33	965.1	1.78	965.1	1.78	965.1	1.78	
7	349.6	377.0	7.85	372.4	6.55	361.8	3.51	356.1	1.88	352.4	0.81	349.6	0.00	349.6	0.00	349.6	0.00	
8	750.1	814.3	8.56	792.5	5.65	782.7	4.35	774.0	3.19	761.6	1.53	750.9	0.11	750.9	0.11	750.9	0.11	
9	611.7	639.2	15.14	682.2	11.52	639.7	4.57	658.5	7.64	632.3	3.36	630.8	3.12	630.8	3.12	630.8	3.12	
10	737.1	852.5	15.65	828.2	12.35	806.6	9.42	793.0	7.58	774.4	5.06	763.5	3.57	763.5	3.57	763.5	3.57	
11	264.2	282.6	6.95	273.1	3.36	272.2	3.00	268.2	1.50	264.2	0.00	264.2	0.00	264.2	0.00	264.2	0.00	
12	192.6	206.8	7.36	199.0	3.31	197.8	2.72	198.0	2.81	192.6	0.00	192.6	0.00	192.6	0.00	192.6	0.00	
13	152.4	-	-	167.7	10.01	163.1	7.01	160.9	5.53	152.4	0.00	152.4	0.00	152.4	0.00	152.4	0.00	
14	872.3	974.4	11.70	941.3	7.91	921.0	5.59	893.7	2.45	900.1	3.19	878.8	0.74	878.8	0.74	878.8	0.74	
15	763.3	830.8	8.84	824.2	7.97	807.9	5.84	785.7	2.94	784.9	2.82	784.4	2.76	784.4	2.76	784.4	2.76	
AVG. Gap			9.55		6.84		4.83		3.46		1.66		1.11		1.11		1.11	

Table 2: Influence of the subgraphs size

3.3 Influences of the number of slave hadoop nodes

Table 3 reports the computational time with different number of nodes: column "1-sn" for time consumption with one slave node, column "4-sn" for 4 slave nodes resolution time, and column "8-sn" for 8 slave nodes resolution time. One can note that the average computational time varies strongly between the different numbers of slaves and the size of subgraph. For the

instance 2, the computation time decreased from 613 seconds to 76 seconds with $D = 15$ km. For several instances, increasing of the slave nodes number does not improve the computational time. For the instance 8 with $D = 100$ km, the computational time is equal between 4 nodes and 8 nodes. Such analysis pushes us into considering that there exists an optimal configuration on the number of nodes and the subgraph size for resolution of each instance.

Ins.	D = 15			D = 50			D = 100			D = 200		
	1-sn	4-sn	8-sn	1-sn	4-sn	8-sn	1-sn	4-sn	8-sn	1-sn	4-sn	8-sn
1	84	49	54	55	54	49	51	48	48	60	60	59
2	613	127	76	247	62	55	177	58	58	194	92	92
3	457	106	65	181	61	55	129	59	60	132	78	78
4	281	75	52	122	52	52	97	58	56	80	72	68
5	689	138	76	277	73	58	192	65	63	179	91	88
6	746	149	87	318	75	56	250	74	62	244	92	90
7	274	73	51	119	52	49	88	53	53	81	73	72
8	573	121	69	228	65	51	160	56	54	159	78	81
9	444	102	108	171	55	51	119	55	55	114	75	75
10	530	110	65	203	56	49	142	56	56	152	80	80
11	216	61	49	87	50	51	65	55	51	68	63	64
12	179	54	51	81	52	55	62	58	58	68	67	66
13	137	47	48	66	52	51	60	59	59	59	59	58
14	614	119	76	234	69	53	167	59	53	125	62	64
15	601	122	73	221	61	51	160	63	64	146	72	74
AVG.	429.2	96.9	66.7	174.0	59.3	52.4	127.9	58.4	56.7	124.1	74.3	73.9

Table 3: Impact of slave nodes number on the computation time

4 CONCLUDING REMARKS

The MapReduce framework is a new approach for operational research algorithms and our contribution stands at the crossroads of optimization research community and map-reduce community. Our contribution consists in proving there is a great interest in defining approaches taking advantages of research coming from information system and parallelization.

As future work, we are interested in adapting the operational research algorithms to such framework, especially for those which could be more easily to take advantages of parallel computing platform as GRASP or Genetic algorithm.

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